

1a.  $a(t) = (-20 - 10t) \hat{e}_y$

$$V_x = 100$$

$$V_y = (-20t - 5t^2)$$

1b.  $x(t) = 100t$        $y(t) = (-10t^2 - \frac{5}{3}t^3)$

1c.  $x(t) = 100t \rightarrow t_{exit} = \frac{L}{100} = \frac{2}{100} = \frac{1}{50} \text{ sec}$

1d.  $y(t) = -10t^2 - \frac{5}{3}t^3$

$$y_{exit} = -10\left(\frac{1}{50}\right)^2 - \frac{5}{3}\left(\frac{1}{50}\right)^3 \rightarrow y_{exit} = -4.01 \times 10^{-3} \text{ m}$$

1e.  $V_y = -20t - 5t^2$

@  $t = \frac{1}{50}$

$$V_y = -20\left(\frac{1}{50}\right) - 5\left(\frac{1}{50}\right)^2 = -0.402 \text{ m/s}$$

$$\theta = \tan^{-1}\left(\frac{-0.402}{100}\right) = -0.00402 \text{ rad}$$

$$= \approx 0.23^\circ$$

2a. The Reynold's Number measures the ratio of inertial vs. viscous forces

$$F_{\text{in}} = 3\pi\eta Dv$$

Low  $Re \rightarrow$  Smooth flow

High  $Re \rightarrow$  Rough flow & bumpy

$$F_{\text{quad}} = k\rho A v^2$$

$$A_{\text{sphere}} = \frac{\pi D^2}{4}, \quad k = 0.25$$

$$F_{\text{quad}}/F_{\text{in}} = \frac{0.25\rho(\pi D^2/4)v^2}{3\pi\eta Dv}$$


$$= \frac{\rho Dv}{48\eta} \rightarrow \frac{F_{\text{quad}}}{F_{\text{in}}} = \frac{Re}{48}$$

$Re < 48$  ; lin drag

$Re > 48$  ; quad drag

2b. Low  $Re \rightarrow$  Small bacteria swimming in water

High  $Re \rightarrow$  Airplane flying in the air

Low  High

Raindrop, Parachutist, Car, Plane

2c. The Péclet number is a dimensionless number that represents the diffusion rate of something (e.g. Heat transfer, mass transfer)

$$Pe = \frac{\text{advective transport rate}}{\text{diffusive transport rate}} = \frac{vL}{D}$$

Low  $Pe$ : Heat conduction in Solids

High  $Pe$ : Oxygen transporting in blood