

$$1a. \quad a(t) = (-20 - 10t)\hat{e}_y$$

$$V_x = 100$$

$$V_y = (-20t - 5t^2)$$

$$1b. \quad x(t) = 100t \quad y(t) = (-10t^2 - \frac{5}{3}t^3)$$

$$1c. \quad x(t) = 100t \rightarrow t_{exit} = \frac{L}{100} = \frac{2}{100} = \frac{1}{50} \text{ sec}$$

$$1d. \quad y(t) = -10t^2 - \frac{5}{3}t^3$$

$$y_{exit} = -10\left(\frac{1}{50}\right)^2 - \frac{5}{3}\left(\frac{1}{50}\right)^3 \Rightarrow y_{exit} = -4.01 \times 10^{-3} \text{ m}$$

$$1e. \quad V_y = -20t - 5t^2$$

$$\textcircled{a} \quad t = \frac{1}{50}$$

$$V_y = -20\left(\frac{1}{50}\right) - 5\left(\frac{1}{50}\right)^2 = -0.402 \text{ m/s}$$

$$\theta = \tan^{-1}\left(\frac{-0.402}{100}\right) = -0.00402 \text{ rad}$$

$$= -0.23^\circ$$

2a. The Reynolds Number measures the ratio of internal vs. viscous forces

$$f_{\text{int}} = 3\pi \eta D v$$

Low Re \rightarrow Smooth flow

High Re \rightarrow Rough flow, bumpy

$$f_{\text{quad}} = k \rho A v^2$$

$$\text{Aspect} = \frac{\pi D^2}{4}, k = 0.25$$

$$\frac{f_{\text{quad}}}{f_{\text{int}}} = \frac{0.25 \rho (\pi D^3 / 4) v^2}{3 \pi \eta D v}$$

$$= \frac{\rho D v}{48 \eta} \rightarrow \frac{f_{\text{quad}}}{f_{\text{int}}} = \frac{Re}{48}$$

$Re < 48$; lin drag

$Re > 48$; quad drag

2b. Low $Re \rightarrow$ Small bacteria swimming in water

High $Re \rightarrow$ Airplane flying in the air

Low ————— High

Raindrop, Parachutist, Car - plane

2c. The Péclet number is a dimensionless number that represents the diffusion rate of something (e.g. heat transfer, mass transfer)

$$Pe = \frac{\text{advective transport rate}}{\text{diffusive transport rate}} = \frac{VL}{D}$$

Low Pe : Heat conduction in Solids

High Pe : Oxygen transporting in blood