Loopring: A Decentralized Token Exchange Protocol

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Abstract

Loopring is an open protocol for building decentralized exchanges. Loopring operates as a public set of smart contracts responsible for trade and settlement, with an off-chain group of actors aggregating and communicating orders. The protocol is free, extensible, and serves as a standardized building block for decentralized applications (dApps) that incorporate exchange functionality. Important improvements over current decentralized exchange protocols are the ability for users orders to be mix-and-matched with other orders, obviating the constraints of two-token trading pairs, drastically improving liquidity, and price improvement possibility. Loopring also employs a robust and unique solution to prevent front-running: the unfair attempt to submit transactions into a block quicker than the original solution provider. Loopring is blockchain agnostic, and deployable on any blockchain with smart contract functionality. At the time of writing, its operable on Ethereum and QTUM, with NEO also under construction. Its interoperable standards ensure trustless, decentralized, and anonymous trading.

1 Introduction

With the proliferation of blockchain-based assets, the need to exchange these assets amongst counterparties has significantly increased. As thousands of new tokens are introduced - including the tokenization of traditional assets - this need is magnified. Whether exchanging for speculative trading motivations, or converting to access networks via their native utility tokens, the ability to exchange one cryptoasset for another is foundational for the larger ecosystem.

As such, the trustless exchange of tokens (value) is a compelling use case for blockchain technology. Until now, however, crypto enthusiasts have largely settled for trading tokens on traditional centralized exchanges. The Loopring protocol is needed because, just as Bitcoin(1) dutifully pointed out that, in regards to peer-to-peer electronic cash, the main benefits are lost if a trusted third party is still required to prevent double-spending, so too are the main benefits of decentralized assets lost if they must pass through trusted, gated, centralized exchanges.

Trading decentralized tokens on centralized exchanges doesnt make sense from a philosophical perspective, as it fails to uphold the virtues these decentralized projects espouse. There are also numerous practical risks and limitations in using centralized exchanges which are described below. Decentralized exchanges (DEXs) have sought to address these issues, and in many cases have succeeded in alleviating security risks. However, there is still vast room for improvement in performance as DEX capability becomes important infrastructure

for the new economy. Loopring hopes to provide critical tools for said infrastructure with its open protocol for building DEXs.

2 Current Exchange Landscape

2.1 Inadequacies of Centralized Exchanges

The three primary risks of centralized exchanges are; 1) Lack of security, 2) Lack of transparency, and 3) Lack of liquidity.

2.1.1 Lack of Security

Security risks arise from the fact that users must typically surrender control of their private keys (funds) to one centralized entity. This exposes users to the possibility that centralized exchanges fall prey to malicious hackers. The security and hacking risks facing all centralized exchanges are well known(2), yet are often accepted as table stakes for token trading. Centralized exchanges, such as Coinbase and Bittrex, continue to be honeypots for hackers to attack, as their servers control millions of dollars of users funds. Exchange developers can also make honest, accidental errors with your funds. You are simply not in control of your own tokens when they are deposited at a centralized exchange.

2.1.2 Lack of Transparency

Beyond security hacks, a lack of transparency exposes users to the risk of dishonest exchanges acting unfairly. The distinction here is by the exchange operators malintentions.

Users are not truly trading their own assets on a centralized exchange, but rather, an IOU - a promissory note that the exchange will redeem your note for your original asset. When tokens are sent to the exchange's wallet, they take custody, and offer an IOU. All trades are then effectively between users' IOUs. To withdraw, you redeem your IOU with the exchange, and get back your tokens to your external wallet address. Throughout this process there is a lack of transparency, and the exchange can shutdown, freeze your account, go bankrupt, etc. It is also possible that they use your assets for other purposes while in custody (such as lending them out to third parties), which makes you susceptible along another attack vector. Lack of transparency can also cost you without total loss of funds, such as in higher trading fees, delays at peak demand, regulatory risk, and your orders being front ran.

2.1.3 Lack of Liquidity

From the point of view of exchange operators, fragmented liquidity inhibits entry by new exchanges because of two winner-takes-all scenarios. First, the exchange with the most number of trading pairs available wins, because users find it desirable to conduct all their trades on one exchange. Second, the exchange with the largest order book wins, because of favorable bid-ask spreads for each trading pair. This discourages competition from newcomers because it is difficult for them to build up initial liquidity. As a result, many legacy exchanges command a high market share despite user complaints and even major hacking incidents. Its worth noting that as centralized exchanges win market share, they make themselves an ever-larger hacking target.

From the point of view of users, fragmented liquidity significantly reduces user experience. In a centralized exchange, users are only able to trade within the exchange's own liquidity pools, against its own order book, and between its supported token pairs. To trade Token A, for Token B, you must go to an exchange that supports both tokens or register at different exchanges, disclosing personal information. You often need to execute preliminary or intermediate trades, usually against BTC or ETH, absorbing bid-ask spreads in the process. Finally, the order books may not be deep enough to complete your trade without material slippage.

The result is disconnected silos of liquidity and a fragmented ecosystem that resembles the legacy financial system, with significant trading volume centralized on few exchanges. The global liquidity promises of blockchains hold no merit within centralized exchanges.

2.2 Inadequacies of Decentralized Exchanges

Decentralized exchanges, such as KyberNetwork or EtherDelta, differ from centralized exchanges in that users maintain control of their assets (private keys) by performing trades directly on the underlying blockchain. By leveraging the trustless technology of cryptocurrencies themselves, they successfully mitigate many of the above mentioned risks surrounding security. However, problems persist in regards to performance and structural limitations.

Liquidity often remains an issue as users must search for counterparties across disparate silos and standards. Fragmented liquidity effects are present if users dont employ consistent standards to interoperate, and if orders are not shared/propagated across a wide network.

Furthermore, since trades are performed on chain, DEXs often inherit the limitations of the underlying blockchain, namely: scalability, delays in execution (mining), and costly modifications to orders. Thus, blockchain order books do not scale well, as executing code on the blockchain incurs a cost (gas), making multiple order-cancel cadences prohibitively expensive.

Finally, because blockchain order books are public, the transaction to place an order is visible by miners as it awaits being mined into the next block, and placed into an order book. This delay exposes the user to the risk of being front run and having the price move against him.

2.3 Hybrid Solutions

For the above reasons, purely blockchain-based exchanges have limitations that make them uncompetitive with centralized exchanges. There is a tradeoff between on-chain inherent trustlessness, and centralized exchange speed and order flexibility. Protocols such as Loopring and 0x extend a solution of on-chain settlement with off-chain order relay. These solutions revolve around open smart contracts, but navigate scalability limitations by performing several functions off-chain, and giving nodes flexibility in fulfilling critical roles for the network. While Loopring admires protocols such as 0x, as we demonstrate throughout the paper, we propose meaningful differences in our approach to a hybrid solution.

3 Loopring Protocol

Loopring is not a DEX, but a protocol for building DEXs on multiple blockchains. We disassemble the component parts of a traditional exchange and offer a set of public smart contracts and decentralized actors in its place. The roles in the network include wallets, relays, liquidity-sharing consortium blockchains, order book browsers, ring-miners, and asset tokenization services. Before defining each, we should first understand what a Loopring compliant order looks like.

3.1 Order Ring

Loopring orders are expressed in what we call a Unidirectional Order Model (UDOM (2)). UDOM expresses orders as token exchange requests - amountS/amountB - instead of bids and asks. Since every order is just an exchange rate between two tokens, a powerful feature of the protocol is the mixing and matching of multiple orders in circular trade. By using up to 10 orders instead of a single trading pair, there is a dramatic increase in liquidity and potential for price improvement.

Each order's token to sell is another order's token to buy. It creates a loop that allows each order to exchange their desired tokens without requiring an opposing order for its pair.

Traditional order pair trades can, of course, still be executed, in what is essentially a special case of an Order Ring.

Definition 3.1 (Order Ring) Let C_0, C_1, \dots, C_{n-1} be n different kinds of token, $O_{0\to 1}, \dots, O_{i\to i\oplus 1}, \dots, O_{n-1\to 0}$ be n orders. Those orders can form a ring for trading:

$$O_{0\to 1} \to \cdots \to O_{i\to i\oplus 1} \to \cdots \to O_{n-1\to 0}$$

where n is the length of the ring, and $i \oplus 1 \equiv i+1 \mod n$.

An order ring is valid when all component transactions can be executed at an exchange rate equal to or better than the original rate specified by the user. To verify ring validity, Loopring protocol smart contract (protocol) must receive Order Rings from miners where the product of the original exchange rates of all orders is equal to or greater than 1. (further calculations in section 4).

Every order has two basic elements: two assets offered for trading and an exchange rate. The price is the exchange rate with one of the assets fixed as parameter. Let assume Alice and Bob want to trade their tokens A and B. Alice has 15 tokens A and she wants 4 tokens B for them; Bob has 10 tokens B and he wants 30 tokens A for them.

Who is buying and who is selling? This depends only on the asset we fix to give price quotations. If token A is the reference, then Alice is buying tokens B for $\frac{15}{4} = 3.75$ XTA, while Bob is selling 10 tokens B for $\frac{30}{10} = 3.00$ XTA. In the case of fixing token B as reference we say that Alice is selling 15 tokens A for $\frac{4}{15} = 0.26666667$ XTB and Bob is buying 10 tokens A for $\frac{10}{30} = 0.33333334$ XTB. Hence, who's the buyer or seller is purely arbitrary.

In the first situation Alice is willing to pay a higher price than the price Bob is selling his tokens for, in the second situation Bob is willing to pay a higher price than the price Alice is selling her tokens for. It is clear that a trade is possible whenever the buyer is willing to pay an equal or higher price than the selling price, no matter how we fix the prices. If we recall our basic arithmetic we learned in school we can verify easily that:

$$\frac{\frac{15}{4}}{\frac{30}{10}} = \frac{3.75}{3.00} = \frac{0.33333334}{0.26666667} = \frac{\frac{10}{30}}{\frac{4}{15}} = \frac{15}{4} \cdot \frac{10}{30} = \frac{150}{120} = 1.25 > 1 \tag{1}$$

4 Ecosystem Participants

The following ecosystem participants jointly provide all functionalities a centralized exchange has to offer.

- Wallets: A common wallet service or interface that gives you access to your tokens and a way to send orders to the Loopring network. Wallets will be incentivized to produce orders by sharing fees (see section 5.1).
- Relays / Ring Miners: Relays are nodes that form a decentralized network for order propagation. They maintain public order books and trade history and broadcast new orders to other relays via any arbitrary off-chain medium. Ring-mining is a feature of relays. It is computational heavy and is done completely off-chain. Ring-mining produces Order Rings: rings of between 2 and 10 tokens created by stitching together disparate orders. Relays are free in how they choose to communicate with one another (or not).
- Consortium Liquidity Sharing Blockchain: TODO(daniel)
- Loopring Protocol Smart Contracts: A set of public and free smart contracts that checks Order Rings received from miners, does token transfers on behalf of users, incentivizes miners/wallets, and emits events. Relays/order browsers listen to these events to keep their order books and trade history up to date.

• Asset Tokenization Services: A bridge between assets that cannot be directly traded on Loopring. They are centralized services run by trustworthy companies or organizations. A user could deposit his assets (real, fiat or tokens from other chains) and get tokens issued. By returning these tokens the user gets back his deposit. Loopring is not a cross-chain exchange protocol, but Asset Tokenization Services make it possible to trade Ethereum ERC20 tokens with physical assets as well as assets on other blockchains.

5 Exchange Process

- 1. Order Initiation & ERC20 Authorization: A user wants to exchange X amount of TokenA for Y amount of TokenB. The current rate and order book for this pair can be found on multiple sources provided by relays or other interfaces hooked up to the network, such as order book browsers (4). The user places an order through a wallet interface. An amount of LRx can be added to the order as a fee for miners; higher LRx fee means a better chance to be processed earlier by miners. The wallet authorizes the LSC to handle X amount of TokenA the user wants to sell, but does not lock the user's tokens, who remains free to move them while the order is being processed.
- 2. **Send order to the network**: Once the authorization is made, the order's data is signed with the private key of the sender. Then, the wallet sends the order along with its signature to one or more nodes (relays) in the network.
- 3. Relay broadcast: On the reception of the order, relays update their public order book and broadcast the order to other relays/ring miners. The protocol doesnt require order books to be built in a certain way, for example, first-come-first-serve. Instead, relays have the power to make their own design decisions to build their own order books.
- 4. Ring-mining (order matching): Ring Miners receive the order and add it to their order book. Each miner tries to fill it fully or partially at the given exchange rate or better by ring-matching it with multiple other orders. Ring-matching is the main reason why the protocol is able to provide high liquidity over any pair. If the executed rate is better than what the user asked for, the savings (margin) are shared amongst all orders in the ring. As a reward (fee), the miner can choose between claiming the Margin Split and giving back the LRx to the user, or just keeping the LRx fee.
- 5. Verification & Settlement: The ring is received by the Loopring Smart Contract. It makes multiple checks to verify the miner's supplied data and determines if the ring can be settled fully or partially (depending on the fill rate of orders in the ring and the tokens in the users' wallets). If all checks are successful, the contract automatically makes the token transfers to the users and pays the miner's fees at the same time. If the sender's balance as determined by the LSC are insufficient, it will be considered scaled-down. A scaled-down order is not the same as a cancelled order: a scaled-down order will automatically scale up to its original size if sufficient funds are deposited to its address, while cancellation is a one way manual operation and cant be reversed.

6 Business Model Flexibility

Its important to note that Looprings open standard allows participants significant flexibility in how they conduct business. Actors with novel business models are free to implement them and provide value for their users, earning LRx fees on volume in the process.

6.1 Order Book

Relays can design their order books in any number of ways to display and match users trades. A first implementation of our own order book follows an OTC model, where limit

orders are ranked or positioned based on price alone. Timestamps of orders, in other words, have no bearing on the order book. However, a relay is free to design their order book in such a way as to emulate a typical centralized exchanges matching engine, where orders are ranked by price, but with a timestamp respecting filter as well. If a relay was inclined to offer this type of order book, they can own/integrate with a wallet, and have those wallet orders sent solely to the single relay, who would then be able to match orders based on time. Any such configuration is possible.

6.2 Liquidity Sharing

Relays are similarly free to design how they share liquidity and orders with one another. Our consortium blockchain is but one solution to accomplish this, and the ecosystem is free to network and communicate as they wish. Besides joining a consortium blockchain, they can build and manage their own, creating rules/incentives as they see fit. Relays can also work solo, as seen in the time-sensitive wallet implementation above. Of course, there are clear advantages in communicating with other relays in pursuit of network effects, however, different business models could merit peculiar sharing designs.

7 Protocol Specification

7.1 Anatomy of an Order

An order is a pack of data that describes the intent of the users trade. To ensure the origin of the order, it is signed against the hash of its parameters with the user's private key. The signature is sent alongside the order on the network. This requires the order to stay immutable during its whole lifetime to verify the sender's address. Even if the order never changes, the LSC has the possibility to compute its current state.

```
message Order {
address protocol;
address owner;
address tokenS;
 address tokenB;
uint256 amountS;
uint256 amountB;
unit256 lrcFee
unit256 validSince;
                                 // Seconds since epoch
                                 // Seconds since epoch
unit256 validUntil;
                                // In the rage of [1-100]
uint8
        marginSplitPercentage;
bool
        buyNoMoreThanAmountB;
uint256 walletId;
address authAddr; // Dual-Authoring address
uint8 v;
                  // Part of the signature
bytes32 r;
                  // Part of the signature
bytes32 s;
                  // Part of the signature
string _authKey; // Dual-Authoring private key,
                   // not used for calculating order's hash.
}
```

where authAddr is not signed by the order addresss private key.

7.2 Signing an Order

[TODO:] Daniel Wang.

8 Ring Verification

9 ========

10 Market and Industry

Today, decentralized exchange protocols built on blockchain technology already exist. Examples include Ripple, BitShares, Openledger, Bancor, and 0x.

Ripple[1]is areal-time gross settlementsystem, currency exchange, and remittance network operated by Ripple (the company). The Ripple Transaction Protocol (RTXP) or Ripple protocol, it is built upon a distributed open source Internet protocol also known as the consensus ledger. Ripple's solution is built around an open, neutral protocol (Interledger Protocol or ILP[2]) that powers payments across different ledgers and networks globally. It offers a cryptographically secure end-to-end payment flow with transaction immutability and information redundancy. Architected to fit within a bank's existing infrastructure, Ripple is designed to comply with risk, privacy, and compliance requirements.

BitShares[3][4] is an industrial grade financial blockchain smart contract platform. The Bit-Sharesdecentralized exchange - also known as "The DEX" is a next-generation cryptocurrency trading platform. The DEXis inherently decentralized, enabling one to trade the BitShares core token (BTS) and a range of trustless price-stable, market-pegged assets, such as bitUSD, bitCNY, bitBTC, bitGold, and others. These assets can all be traded withzerocounter-party risk, putting the user in total control of their funds. However, the Bitshares project has many limitations.

The OpenLedger Dex[5] is a cryptocurrency exchange. It allows users to exchange Bitcoin into smartcoins and then withdraw the smartcoins and convert them into cash through PayPal, Ripple, or NanoCard. Additionally, Openledger relies greatly on the BitShares 2.0 platform and Graphene Toolkit's operation.

The Bancor[6][7] protocol enables built-in price discovery and a liquidity mechanism for tokens on smart contract blockchains. These "smart tokens" hold one or more other tokens in reserve and enable any party to instantly purchase or liquidate the smart token in exchange for any of its reserve tokens. This is done directly through the smart token's contract, at a continuously calculated price according to a formula which balances buy and sell volumes.

"0x" [8] is a protocol that facilitates low friction peer-to-peer exchange of ERC20[9] tokens on the Ethereum blockchain. The protocol is intended to serve as an open standard and common building block driving interoperability among decentralized applications (dApps) that incorporate exchange functionality. Trades are executed by a system of Ethereum smart contracts that are publicly accessible, free to use and that any dApp can hook into. DApps built on top of the protocol can access public liquidity pools or create their own liquidity pool and charge transaction fees on the resulting volume. However, 0x protocol has limitations including only being able to accept simple OTC orders, having an unclear competing mechanism among different exchanges, and lacking a protection mechanism for miners.

Taking in to account the advantages and limitations stated above, it is clear that centralized exchange still plays an important role in the cryptocurrency market at present. Nevertheless, Our team, inspired by both 0x protocol and payment channel, have conceived a new solution for a decentralized exchange protocol.

11 Protocol Design

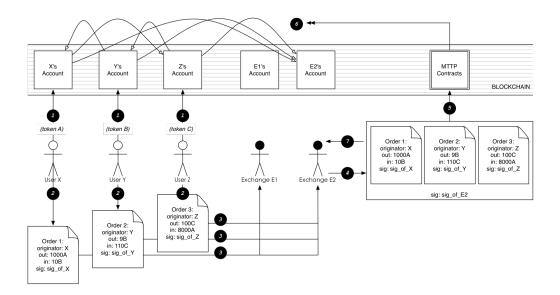


Figure 1: Figure shows mix and match 3 orders

Figure 1 presents the general sequence of steps used for three separate transactions under Loopring:

- 1. User X, Y, and Z authorize the Loopring smart contract to access their accounts for token trading. From the above figure, such a contract may transfer out 1000 A tokens from User X's account, transfer out 9 B tokens from User Y's account, and 100 C tokens from User Z's account;
- 2. User X, Y, and Z place their own orders with signature using their private keys. Thus, all orders go into a medium and are ready to be exchanged Order 1 is selling no more than 1000 A tokens and purchasing no less than 10 B tokens; if the order is partially matched, then the exchange rate between tokens A to B should be no less than 1000/10=100.00 (number of tokens sold divided by number of tokens purchased). Furthermore, to illustrate other parameters involved in chapter 3.7;
- 3. User X, Y, and Z continue to send their orders to one of the other multiple exchanges;
- 4. After the exchange received all three separated orders, they will replace them into a corresponding order-book, while updating a new block and calculating each orders status to match the set order creating a loop we delineate as a ring exchange or matching exchange. Once all the orders are confirmed and successfully mix-matched;
- 5. Exchange will send out a signature to the given Loopring smart contract address;
- 6. Loopring smart contract will verify quadruple signatures in order to verify three orders closing. If closing fails, the contract will be terminated (certain exchange gas cost exempt); otherwise, Loopring smart contract needs to calculate the proceeds and cost for each users, to complete the token exchange as illustrated in the figure below. During each step, Loopring smart contract will use Loopring Registration Contract to calculate all the fees and discount before closing. The system will also need to use Loopring Stats Contract to update the database.

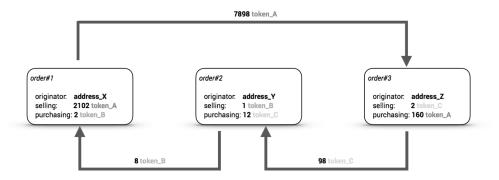


Figure 2: LoopringMatch-Ring Settlement

7. Exchange begins receiving new block and new data from the chain in order to update the order-book to mix-match new and existing orders.

11.1 Definition of Symbol

Symbols are defined as follows.

 C_i : stands for the *i*-th token.

 $O_{i \to j}$: stands for an order selling token C_i for token C_j .

 $s_{i\to j}$: selling token upper limit in order $O_{i\to j}$.

 $b_{i\to j}$: buying token lower limit in order $O_{i\to j}$.

 $r_{i\to j}$: max exchange rate in order $O_{i\to j}$, which is $s_{i\to j}/b_{i\to j}$.

We underlined the symbols to place emphasis on their original numbers. For example $\bar{s}_{i\to j}$ and $\bar{b}_{i\to j}$ stands for the number of tokens from the original order.

11.2 Rate Immutability

Loopring requires that the max-return exchange rate in an order remains immutable until the order is closed: $s_{i\to j}/b_{i\to j} = \bar{s}_{i\to j}/\bar{b}_{i\to j}$. This guarantees that after an order is partially filled, the remaining order still satisfies the user's original intention.

11.3 Order Reducibility

We can use token C_j to connect two orders ($O_{i\to j}$ and $O_{j\to k}$), to recognize it as one single order for selling token C_i for buying token C_k . we use $O_{i\to j\to k}$ to represent this order. The resulting $O_{i\to k}$'s properties can be calculated as:

$$s_{i \to j \to k} = \min(b_{i \to j}, s_{j \to k}) \cdot r_{i \to j} \tag{2}$$

$$b_{i \to j \to k} = \min(b_{i \to j}, s_{j \to k}) / r_{j \to k} \tag{3}$$

$$r_{i \to j \to k} = r_{i \to j} \cdot r_{j \to k} \tag{4}$$

Here we introduce the concept of an order-chain. It contains two or more orders, each selling token order is the following purchasing token order except the last one in the chain. Additionally, final purchasing token order should be different from the first orders selling token (otherwise it will become ring).

$$s_{0 \to \dots \to n} = \begin{cases} s_{0 \to 1} & \text{as } n = 1\\ \min(b_{0 \to \dots \to n-1}, s_{n-1 \to n}) \cdot r_{0 \to \dots \to n-1} & \text{as } n > 1 \end{cases}$$

$$b_{0\to\dots\to n} = \begin{cases} b_{0\to 1} & \text{as } n=1\\ \min(b_{0\to\dots\to n-1}, s_{n-1\to n})/r_{n-1\to n} & \text{as } n>1 \end{cases}$$
$$r_{0\to\dots\to n} = \prod_{i=0}^{n-1} r_{i\to i+1}$$

11.4 Match-Ring

Most, if not all, centralized exchanges match orders from the two sides of a trading pair. Loopring, however, detects a ring of orders that may involve multiple tokens/currencies. With one order Match-Ring, multiple orders can be filled instantly.

Definition 11.1 (Match-Ring) Let C_0, C_1, \dots, C_{n-1} be n different kinds of token, $O_{0\to 1}, \dots, O_{i\to i\oplus 1}, \dots, O_{n-1\to 0}$ be n orders. Those orders can form a ring for trading:

$$O_{0\to 1} \to \cdots \to O_{i\to i\oplus 1} \to \cdots \to O_{n-1\to 0},$$

where n is the length of the ring, and $i \oplus 1 \equiv i + 1 \mod n$.

Once the prices match the orders under circumstance, we could start to complete trading in this circle.

11.4.1 Price

We will provide an example for a better understanding of the pricing mechanism. Assume three kinds of token are C_0 , C_1 and C_2 , and three separated orders: $O_{0\to 1}$, $O_{1\to 2}$ and $O_{2\to 0}$. Easy to approve: if and only if $r_{0\to 1}\cdot r_{1\to 2}\cdot r_{2\to 0}=1$, all three orders could be filled using their respective exchange rate; If $r_{0\to 1}\cdot r_{1\to 2}\cdot r_{2\to 0}>1$, all these orders can be filled using a rate lower than their implicit max exchange rate. We named the first situation as original-price matching, the second as discount-price matching.

According to Loopring protocol, each order in the ring would share the same rate (price) discount. For instance, if the discounted rate is γ , then the price for each order will be: $r_{0\to 1} \cdot (1-\gamma)$, $r_{1\to 2} \cdot (1-\gamma)$, $r_{2\to 0} \cdot (1-\gamma)$, and satisfied:

$$r_{0\to 1} \cdot (1-\gamma) \cdot r_{1\to 2} \cdot (1-\gamma) \cdot r_{2\to 0} \cdot (1-\gamma) = 1$$
 (5)

We can find out:

$$\gamma = 1 - \frac{1}{\sqrt[3]{r_{0 \to 1} \cdot r_{1 \to 2} \cdot r_{2 \to 0}}}.$$

In the other circumstance, if transaction cross n orders, the discount is:

$$\gamma = 1 - \frac{1}{\sqrt[n]{\prod_{i=0}^{n-1} r^i}},$$

where r^i is the order turnover rate of *i*-th order. Obviously, only when the discount rate is $\gamma \geq 0$, these orders can be filled; and the *i*-th order's O^i actual exchange rate $\hat{r^i} = r^i \cdot (1 - \gamma)$, $\hat{r^i} \leq r^i$.

11.4.2 Fill Volume

Finding the lowest value order can help to figure out the fill volume for each order. For instance, if the *i*-th order is the lowest value order, then the number of tokens sold from each order \hat{s} and number of tokens purchased \hat{b} from each order can be calculated as:

$$\begin{split} \hat{s}^{i} &= \bar{s}_{i}, \, \hat{b}^{i} = \hat{s}^{i} / \hat{r}^{i}, \, ; \\ \hat{s}^{i \oplus 1} &= \hat{b}^{i}, \, \hat{b}^{i \oplus 1} = \hat{s}^{i \oplus 1} / \hat{r}^{i \oplus 1}; \\ \hat{s}^{i \oplus 2} &= \hat{b}^{i \oplus 1}, \, \hat{b}^{i \oplus 2} = \hat{s}^{i \oplus 2} / \hat{r}^{i \oplus 2}; \end{split}$$

where \bar{s}_i is the the balance left after orders are partially filled.

During implementation we can safely assume any order in the ring to have the lowest value, then iterate through the ring at most twice to calculate each orders' fill volume.

11.4.3 Cost and Fee

Exchanges normally charge a transaction fee. For instance, we assume the fee will be calculated in Loopring token LRC, order ID is i and total fee for completing the transaction is m^i :

$$f^i = b^i \cdot m^i / \overline{b^i}$$

In order to encourage an exchange to offer the best rate for users, Loopring would distribute profit from margin to the given exchange. As an order O^i , if price for purchasing is $b^i(b^i \leq \overline{b^i})$, then we define margin as:

$$\Delta^i = b^i \cdot r^i \cdot \gamma$$

If Loopring requires every order to set up a margin split θ^i , and minimum margin split percentage is Θ . Then order O^i should pay to exchange:

$$f^i = \Delta^i \cdot \Theta = b^i \cdot r^i \cdot \gamma \cdot \Theta$$

Income from margin among each matching trade is explicated by:

$$F = \sum_{i=0}^{n-1} b^i \cdot r^i \cdot \gamma \cdot \Theta$$

In order to encourage LRC usage, if the order has no preset token fee m^i , or $m^i = 0$, then the actual ratio is 100% regardless of the relevant hash in this order. If none of the orders have set up this rate $\Theta = 100\%$, then all of the margin proceeds will go to the exchange.

In the next chapter we will introduce a token pledge policy, and explain how the smart contract will out each exchanges depositing tokens and rank them up. It will also calculate a mandatory discount cost for each exchange, λ . This figure will affect the total cost. Meanwhile, an exchange can also offer a discount, η . Total cost for completion of a full trade:

$$F = (1 - \lambda) \cdot (1 - \eta) \cdot \sum_{i=0}^{n-1} (b^i \cdot r^i \cdot \gamma \cdot \Theta + b^i \cdot m^i / \overline{b^i})$$

11.4.4 Fee Discount

Loopring requires an exchange platform to offer a discount for each transaction. The discount fee is dependent upon the number of LRC token deposited. The higher the rank, the lower the charged fee. For example rank n's cost will be:

$$\lambda_n = 0.05 \cdot (\ln(n + e - 1) - 1).$$

Details below:

For those exchanges ranked under 1001 and those undeposited exchanges, 30% cost will apply.

Figure 3 shows, $\lambda_2 - \lambda_1 \gg \lambda_{100} - \lambda_{99}$.

| Deposit Ranking n | cost for discount λ | |
|---------------------|-----------------------------|--|
| 1 | 0% | |
| 2 | 1.57% | |
| 10 | 7.31% | |
| 20 | 10.39% | |
| 99 | 18.06% | |
| 100 | 18.11% | |
| 1000 | 29.55% | |
| 1001 | 30.00%* | |

Table 1: Deposit LRC Ranking and cost for discount

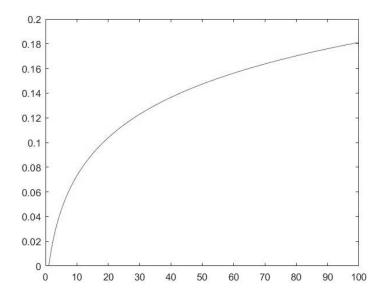


Figure 3: LRC token deposit rank and cost for discount

11.5 Fraud and Attack Protection

11.5.1 Exchange Covered Interest Arbitrage

Loopring endeavors to create a fair ecosystem and to find a balance between customers (users) and exchanges. First, we will explain how an exchange could achieve a zero-risk covered interest arbitrage.

Assume there are two orders $O_{a\to b}$, $O_{b\to a}$ that form a loop, $r_{a\to b}\cdot r_{b\to a}>1$. An exchange can input three new orders between those two. $O_{b\to c}$, $O_{c\to d}$, $O_{d\to b}$, to create a five order loop, $r_{a\to b}\cdot r_{b\to c}\cdot r_{c\to d}\cdot r_{d\to b}\cdot r_{b\to a}=1$. An exchange could bring the possible cost down to zero once the transaction completed, implementing zero-risk covered interest arbitrage, $O_{b\to c}\to O_{c\to d}\to O_{d\to b}$. In order to stop these parameters, Loopring requires: a verified loop that cannot create a further sub-loop to continue trading.

11.5.2 Denial-of-Service

Loopring allows exchanges to selectively handle orders. An exchange can set up their own criteria and may choose to hide or reveal these criteria. Therefore Loopring does not see denial of service as a form of unethical behavior.

11.5.3 Massive Tiny Order Attacks

A user can send out a large amount of tiny orders to attack exchanges. Exchanges however, will reject most of these tiny orders because they do not yield satisfying profit when matched. As denial-of-service is not deemed as a form of attack, massive tiny order attacks are not feasible.

11.5.4 Insufficient Balance

Malicious users may sign and spread out orders in which the order value is not zero, but the wallet address actually has a zero balance. This again is a not a good way to attack exchanges. Exchanges will monitor and notice that some orders' actual balance is zero and update these orders states accordingly, then discard them.

Exchanges do have to spend time to update the order status, but can also choose to minimize these effort by, for example, blacklisting some addresses and drop all related orders.

11.5.5 Ring Filch

A deviant exchange could monitor all unconfirmed Match-Rings and broadcast the same rings with their own digital signature. We call this Ring Filch. In order to prevent Ring Filch Loopring requires exchanges to use two steps in order to submit the order:

- Submit the hash of a Match-Ring, then wait for confirmation.
- Submit the ring itself.

Hash rate:

$$h = H(r, nonce),$$

where H() is a one-way hash function, r is Match-Ring record. Hash function contains a random number nonce.

11.6 Market Depth

Exchanges do not need to offer market depth data. Under this ecosystem, it is possible for both single entities and corporations to possibly pool all unclosed orders into one instance of market depth data. We can ascertain trading data between any two ERC20 tokens according to the agreement in chapter 3.3.

11.7 Data Structure

All orders can be represented by using one data structure due to adopting the OTC module. This data structure contains both a digital signature and all parameters. Before the signature, the parameter data is connected from the orders into a set of data, the order's hash is calculated by using Keccak SHA3 method, and then signed by using this account's private keys with ECDSA.

```
message Order {
  address protocol;
  address owner;
  address outToken;
  address inToken;
  uint256 outAmount;
  uint256 inAmount;
  unit256 expiration
  unit256 fee;
  uint8 marginSplit;
  unit8 v;
```

```
bytes32 r;
bytes32 s;
}
```

Though there is no indicated price from the order, we are still able to find out through the formula: outAmount/inAmount to determine the exchange rate r. The actual exchange rate must be less than r. A user-friendly exchange should allow user to input outAmount, inAmount, selling and asking price, and use any two of those numbers in order to calculate the missing outAmount or inAmount figure. Actual orders can be defined in two different ways: Definition A - transaction can be completed once the number of tokens sold reaches outAmount; Definition B - transaction can be completed once the number of tokens purchased reaches inAmount; Therefore, we can setup a quote for exchange and mix-matching contract to help to define the trade. At our initial version, we would support Definition A only.

The exchange can create a Match-Ring by using this data structure:

```
rmessage MatchRing {
  Order[] orders;
  address feeRecipient;
  unit256 additionalDiscount;
  unit256 nonce;
  unit8 v;
  bytes32 r;
  bytes32 s;
}
```

11.8 Order Status

An order cannot be modified once it has been signed and announced. Data will be updated on the blockchain once the smart contract finds the matched order. Thus inAmount and outAmount will be modified correspondingly with the updated price. If inAmount/outAmount shows 0, it means that the order has been fully closed. For example, if the user wants to cancel the order, a special request will be filed, inAmount/outAmount will be 0 to close the order. An expired order will not be updated on the blockchain - it can be tracked through the final cutting time. Therefore, we expect most of the orders will expire or be invalidated.

11.9 Smart Contracts

Loopring consists of many smart contracts, including:

- Mix-Matched Contract is responsible for ensuring each order status in the loop, calculating the price and volume, transferring and interaction with other smart contracts, API for Loopring;
- Order Contract updates order database and supports cancelling policy;
- Registration Contract maintains and upgrades service for exchanges who accepted Loopring, support the token deposit from exchange and defaulted parameters backup;
- Stats Contract calculates the exchange volume and price between two tokens.

12 Protocol Token

We will issue a token based on ERC20 Ethereum Token Standard called LRC (displays in italics).

12.1 Token Application

LRC will be used in the following areas:

- Gas Fees LRC can be paid as transaction fees to the exchange. It will be simple and productive for the exchange to calculate all the cost in LRC. Same as request sender and receiver. We mentioned this fee structure in chapter 11.4.3.
- Deposit for Exchange Registration The decentralized exchange mechanism has no limits on location or time. Consequently, exchanges with a high turnover would receive more orders and get more users. As a result, we have designed a policy for such exchanges that allow users to use *LRC* to deposit into a smart contract in order to increase the exchanges credibility. Moreover, it can also protect users from certain adverse circumstances.

12.2 Decentralized Governance

Regulation has been updated as well as the exchanges mechanism. Any LRC holders have the voting power S, and number of the pledging N and pledging time CoinAge

$$S = f(N, CoinAge),$$

where $CoinAge = H_c - H_s$. Joining CoinAge aids to protect customers from speculation. The decentralized mechanism includes token registration, exchange registration, stat hash, deposit scale, maximum length, discount hash, and subcontract address.

- Token registration Loopring would adjust token; low trading volume will be eliminated and new popular token will be replaced. All the adjustments have to be recorded on the smart contract.
- Exchange registration Only those exchanges that accept Loopring would allow trading to begin.
- Stat hash Data will increase to a certain amount after a long period of operation. The more data exchanges have, the more accurate the system computation ability will be
- **Deposit scale** Deposit for each exchange should be measurable. If the amount is large, the liquidation gets worse; and vice verse.
- Maximum length Technically, more orders can create more profit, however the risk of failure also increases, as well as the trading cost.
- **Discount hash** Discount hash will be adjusted with the market. The below figure shows the normal market (represented by the blue line), the supply market (represented by the blue line), and the demand market (represented by the red line).

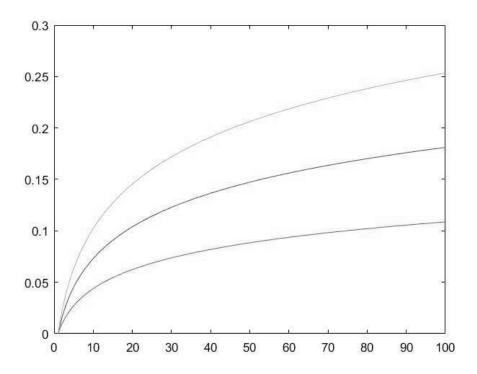


Figure 4: discount rate after adjustment

• Subcontract address If Loopring exchange is based on the Ethereum ecosystem, then the smart contract cannot be modified. Therefore, the users must update Loopring's subcontract in order to modify the subcontract address.

12.3 Token's Liquidity

Loopring's token is based on the ERC20 Ethereum Token Standard and can be liquidated through a Loopring smart contract. This means that LRC trading can be done through a centralized exchange. All the ERC20 Ethereum tokens can be exchanged to LRC token (assume pre-order is LRC, with zero fee) by adopting Loopring's decentralized mechanism.

13 Exchange

An exchange is unable to guarantee that all transactions will lead to profits after Loopring adoption. The first reason is high operation cost. Secondly, high expectation may not result in projected outcomes. There are few other reasons that would cause this saturation. Overall, both the exchange platform and other parties have a reciprocal relationship: the exchange looks for a profitable order, while order senders look for an exchange with the lowest fee. An exchange is not responsible for users ERC20 token after accepting Loopring. The workload has moved from money deposit, withdrawal, and internal virtual account management services, to mix-matched order service. Meanwhile, for the users, Loopring does not require the customer to deposit or lock any asset, meaning an asset has zero third-party custod risk. Concurrently, a single order can mix and match multiple trades. For Non-ERC20 assets, an exchange can offer an asset tokenization service.

13.1 Regular and Loopring Exchange Comparison

In a regular exchange, the "Maker" sends an order, and the "Taker" receives this order. The exchange's price highly depends on the sender's end. However Loopring has adopted the over-the-counter (OTC) model. In the current marketplace, centralized exchanges pose considerably high risk for users trading in these platforms; there are no laws to regulate the exchange if they vanish. But with Loopring, users do not deposit money to centralized exchange. All of the transactions will be made through the user's coin address. Loopring also changes the "Trading Pair" concept utilized by centralized exchanges. Transactions can be completed with multiple parties, rather than two parties in current exchange scenarios.

| | Centralized Ex- | Loopring Ex- |
|--------------------------------|-----------------|--------------------|
| | change | change |
| Deposit for the order | Yes | No ¹ |
| Frozen Account | Yes | No ² |
| Deposit/Withdraw | Yes | No ³ |
| Internal Trading Risk | Yes | No^4 |
| Customer loss from exchange | Yes | No^5 |
| closing | | |
| Transaction is the main income | Yes | No ⁶ |
| Accept Fiat Money | Yes | Yes ⁷ |
| Can be traded among multiple | No | Yes ⁸ |
| exchanges | | |
| Fairness for Maker and Taker | No | Yes ⁹ |
| Mix and Match Trading | No | Yes^{10} |
| Supervision | Strong | Weak ¹¹ |

Table 2: Contrast between a centralized exchange and Loopring exchange

14 Summary

Loopring is a protocol that facilitates decentralized exchange of ERC20 tokens on the Ethereum blockchain. Loopring allows multi-token transaction exchange, as well as liquidation exchange on the blockchain under different circumstances. Loopring offers benefits to both users and exchanges by deferring risk from both parties in decentralized smart contracts, minimizing fees and cost to create more profitable orders through ring-matching and order-sharing, and as a cross-platform protocol. Loopring protocol fits any ERC20 and smart contract blockchain platform. After many discussions, our team will develop Loopring on the Ethereum blockchain.

¹Exchanges execute under Loopring ecosystem do not require any deposit - Tokens are kept in user's wallet, no transaction will be made before the full contract close. As a result, no account can be stolen, or asset lost risk.

²Loopring exchanges do not require freeze trading fund — If a user partially or fully modifies the fund, the contract will be withdraw automatically.

³The sender's order can be distributed to multiple receivers to be partially or fully fulfilled under Loopring ecosystem.

 $^{^4}$ All matching trades are based on smart contract on blockchain, data are immutable and transparent.

⁵Loopring exchanges are not responsible for tokenization, thus Loopring users will not be affected if an exchange becomes insolvent. For example, a blockchain account will not affected if mining is terminated. In conclusion, exchanges are responsible for matching trades. Loopring's smart contract will complete clearing and settlement, furthermore, assets are always kept in users blockchain account.

⁶Transaction fee is not a mainstream income for Loopring exchanges, mainstream comes from profit of transaction margin, because it can effectively encourage trade matching.

 $^{^7}$ Loopring exchanges fully support asset tokenization, hence, it requires legitimate currency being tokenized on ERC20 standard.

⁸Loopring allows multiple Loopring exchanges to partially or fully trade off one order at same time.

⁹Transaction price is closed to the balance price instead of being tendered to the makers offer price under Loopring protocol.

 $^{^{10}}$ Loopring exchanges multiple supporting feature can help sender to find the most profitable order.

¹¹Loopring exchanges do not require a deposit. Clearing and settlement are made through the open source smart contract. Therefore, regulation is not necessaryif there is no asset tokenization occurrence.

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