### Live Archive 6139

Interval Product

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#### **Problema**

It's normal to feel worried and tense the day before a programming contest. To relax, you went out for a drink with some friends in a nearby pub. To keep your mind sharp for the next day, you decided to play the following game. To start, your friends will give you a sequence of N integers  $X_1, X_2, \ldots, X_N$ . Then, there will be K rounds; at each round, your friends will issue a command, which can be:

- a change command, when your friends want to change one of the values in the sequence;
   or
- a product command, when your friends give you two values I, J and ask you if the product  $X_I \times X_{I+1} \times \ldots \times X_{J-1} \times X_J$  is positive, negative or zero.

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#### **Problema**

Since you are at a pub, it was decided that the penalty for a wrong answer is to drink a pint of beer. You are worried this could affect you negatively at the next day's contest, and you don't want to check if Ballmer's peak theory is correct. Fortunately, your friends gave you the right to use your notebook. Since you trust more your coding skills than your math, you decided to write a program to help you in the game.

#### Entrada e saída

### Input

Each test case is described using several lines. The first line contains two integers N and K. indicating respectively the number of elements in the sequence and the number of rounds of the game  $(1 \le N, K \le 10^5)$ . The second line contains N integers  $X_i$  that represent the initial values of the sequence  $(-100 \le X_i \le 100 \text{ for } i = 1, 2, \dots, N)$ . Each of the next K lines describes a command and starts with an uppercase letter that is either 'C' or 'P'. If the letter is 'C', the line describes a change command, and the letter is followed by two integers I and Vindicating that  $X_I$  must receive the value  $V(1 \le I \le Nand - 100 \le V \le 100)$ . If the letter is 'P', the line describes a product command, and the letter is followed by two integers I and Jindicating that the product from  $X_I$  to  $X_J$ , inclusive must be calculated  $(1 \le I \le J \le N)$ . Within each test case there is at least one product command.

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#### Entrada e saída

### Output

For each test case output a line with a string representing the result of all the product commands in the test case. The i-th character of the string represents the result of the i-th product command. If the result of the command is positive the character must be '+' (plus); if the result is negative the character must be '-' (minus); if the result is zero the character must be '0' (zero).

4

### Exemplo de entradas e saídas

#### Sample Input

- 4 6
- -2 6 0 -1
- C 1 10
- P 1 4
- C 3 7
- P 2 2
- C 4 -5
- P 1 4
- 5 9
- 1 5 -2 4 3
- P 1 2
- P 1 5
- C 4 -5
- P 1 5
- P 4 5
- C 3 0
- P 1 5
- C 4 -5
- C 4 -5

### Sample Output

- 0+-
- +-+-0

- Embora fique claro a necessidade do uso de uma árvore de segmentos (ou uma árvore de Fenwick), alguns cuidados são necessários
- Em primeiro lugar, se os números forem armazenados de acordo com os valores dados na entrada, ocorrerá o erro de *overflow*
- Além disso, o zero não é inversível na operação de multiplicação
- Assim, os zeros devem ser armazenados e tratados à parte
- Uma saída é manter duas árvores, que mantenham o registro dos números negativos e dos zeros
- Assim, em uma consulta, se o número de zeros no intervalo for maior que zero, a resposta será zero
- Caso contrário, o resultado depende da paridade do número de negativos no intervalo

```
1 #include <bits/stdc++.h>
₃ using namespace std;
5 class SegmentTree {
      int N;
     std::vector<int> ns:
9 public:
      SegmentTree(int n) : N(n), ns(4*N, 0) { }
      void update(int i, int value)
          update(1, 0, N - 1, i, value):
14
16
      int RSQ(int a, int b)
1.8
          return RSQ(1, 0, N - 1, a, b);
20
```

```
22 private:
      void update(int node, int L, int R, int i, int value)
23
24
          if (i > R \text{ or } i < L)
               return;
26
          ns[node] += value:
28
29
          if (L == R)
30
               return:
31
32
          update(2*node, L. (L+R)/2, i, value):
          update(2*node + 1, (L+R)/2 + 1, R, i, value);
34
35
36
      int RSQ(int node, int L, int R, int a, int b)
37
38
          if (a > R or b < L)
39
               return 0;
```

```
if (a <= L and R <= b)
42
               return ns[node];
43
44
          auto x = RSO(2*node, L, (L + R)/2, a, b);
45
          auto y = RSQ(2*node + 1, (L + R)/2 + 1, R, a, b);
46
47
          return x + y;
48
49
50 };
51
52 int main()
53 {
      int N, K;
54
55
      while (cin >> N >> K) {
56
          vector<int> xs(N):
57
          SegmentTree zeroes(N), negatives(N);
58
59
          for (int i = 0; i < N; ++i) {
60
               int x; cin >> x;
61
```

```
if (x == 0)
63
                   zeroes.update(i, 1);
64
               else if (x < \emptyset)
65
                   negatives.update(i, 1);
66
67
68
          while (K--)
69
70
               string cmd;
               int x, y;
               cin >> cmd >> x >> y;
74
75
               switch (cmd.front()) {
76
               case 'C':
                    --x:
78
                    zeroes.update(x, -zeroes.RSQ(x, x));
80
                    negatives.update(x, -negatives.RSO(x, x));
81
```

```
if (y == 0)
83
                         zeroes.update(x, 1);
84
                    else if (y < 0)
85
                         negatives.update(x, 1);
86
                    break:
87
                default:
88
                    --x; --y;
89
90
                    if (zeroes.RSQ(x, y))
91
                         cout << 0:
92
                    else
93
                         cout << (negatives.RSO(x, v) % 2 ? '-' : '+');</pre>
94
95
96
97
           cout << '\n':
98
99
100
       return 0;
101
102 }
```