SPOJ FENTREE

Fenwick Trees

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Problema

Mr. Fenwick has an array a with many integers, and his children love to do operations on the array with their father. The operations can be a query or an update.

For each query the children say two indices l and r, and their father answers back with the sum of the elements from indices l to r (both included).

When there is an update, the children say an index i and a value x, and Fenwick will add x to a_i (so the new value of a_i is $a_i + x$).

Because indexing the array from zero is too obscure for children, all indices start from 1. Fenwick is now too busy to play games, so he needs your help with a program that plays with his children for him, and he gave you an input/output specification.

1

Entrada e saída

Input

The first line of the input contains N $(1 \le N \le 10^6)$. The second line contains N integers a_i $(-10^9 \le a_i \le 10^9)$, the initial values of the array. The third line contains Q $(1 \le Q \le 3 \times 10^5)$, the number of operations that will be made. Each of the next Q lines contains an operation. Query operations are of the form "q l" $(1 \le l \le r \le N)$, while update operations are of the form "u l" $(1 \le i \le N, -10^9 \le x \le 10^9)$.

Output

You have to print the answer for every query in a different line, in the same order of the input.

Exemplo de entradas e saídas

Sample Input

10

3 2 4 0 42 33 -1 -2 4 4

6

q 3 5

q 1 10

u 5 -2

q 3 5

u 6 7

q 4 7

Sample Output

46

89

44

79

Solução

- A solução *naive* consiste em percorrer cada intervalo a cada consulta, de modo que a complexidade seria igual a O(QN), onde Q é o número de *queries* do tipo q
- Como $Q \leq 3 \times 10^5$ e $N \leq 10^6$, esta solução levaria ao TLE
- O uso de uma árvore de Fenwick permite responder cada uma das queries com complexidade $O(\log N)$
- A construção da árvore tem complexidade $O(N\log N)$, de modo que a solução teria complexidade $O((N+Q)\log N)$
- É preciso tomar cuidado com possíveis *overflows*, usando o tipo **long long** para armazenar as informações dos nós da árvore

```
1 #include <bits/stdc++.h>
₃ using namespace std;
4 using 11 = long long;
6 struct BITree {
     vector<11> ts;
     size_t N;
9
     BITree(size_t n) : ts(n + 1, 0), N(n) {}
10
     11 LSB(11 n) { return n & (-n); }
      void add(size_t i, ll x)
14
          while (i <= N)
16
              ts[i] += x;
              i += LSB(i);
18
20
```

```
11 RSQ(size_t i, size_t j)
22
23
           return RSQ(j) - RSQ(i - 1);
24
25
26
      11 RSO(size_t k)
28
           11 \text{ sum} = 0:
29
30
           while (k)
31
32
               sum += ts[k]:
               k = LSB(k);
34
35
36
           return sum;
37
38
39 };
```

```
41 int main()
42 {
      ios::sync_with_stdio(false);
43
44
      size_t N;
45
      cin >> N:
46
47
      BITree ft(N);
48
49
      for (size_t i = 1; i \le N; ++i)
50
51
           int a:
52
           cin >> a;
53
54
           ft.add(i, a);
55
56
57
      int Q;
58
      cin >> 0;
59
```

```
while (0--)
61
62
           string cmd;
63
           11 L, R;
64
65
           cin >> cmd >> L >> R;
66
67
           switch (cmd[0]) {
           case 'q':
69
               cout << ft.RSQ(L, R) << '\n';</pre>
70
               break;
           default:
               ft.add(L, R);
74
75
76
78
      return 0;
79 }
```