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Final Results

Bronnen

Time Spent on the Project

A toolbox for solving the travelling salesman problem (TSP) was provided. Some parameter tuning with the default operators, selection methods, ... was performed. New tour representations and accompanying operators were implemented. Local heuristics, other selection methods, the island model, adaptive parameter tuning and a seeding technique were experimented with. The results are outlined below. Pointers to relevant source code files are provided next to section headings (all code is written in MATLAB).

Existing Genetic Algorithm

/experiments/*.m

To get an initial feel for what may or may not be worth it, 375 configurations (table 1) were experimented with for a total of 15,000 runs. This made it possible to draw some initial conclusions and perform some increasingly targeted experiments afterwards. All of the experiments outlined throughout this report were automated, with occasional use of parallelism (using MATLAB's parallel computing toolbox).

| Population Size | Crossover Rate $(\%)$ | Mutation Rate (%) | Elitism $(\%)$ |
|-----------------|----------------------------|---------------------------|----------------|
| [150,300,600] | $[10,\!25,\!50,\!75,\!95]$ | $[5,\!25,\!50,\!75,\!95]$ | [1,5,10] |

Table 1: Parameter ranges for the initial experiments. Each configuration was run 10 times on 4 different datasets (with 25, 41, 70 and 127 cities). No stopping criterion was applied, and each run lasted 250 generations. For all configurations with population size set to 150 we also performed runs with 500 generations and higher rates of elitism. Results are visualised in tables 4 to 8.

After selecting 4 datasets (with an increasing amount of cities) each of the resulting algorithms were ran 10 times. The resulting (best, average and worst) tour lengths and runtimes were recorded and averaged. The best tour found by each was also recorded, since the very point of the travelling salesman problem is to find the smallest possible tour. Diversity of solutions is only of indirect benefit as it increases the probability of reaching a global optimum. The minimum tour length found by every configuration is visualised in tables 4 to 8. It is calibrated against the minimum and maximum found by any of the 375 configurations (darker cells in the table indicate better solutions).

Aside from the obvious conclusion that the first benchmark is a tad too easy to resolve, two observations could be made; larger population sizes improved results and lead to longer runtimes, and setting the rate of elitism too low is contra-productive. The first is not surprising since a larger population may increase diversity and the probability of finding a better local (or even global) minimum. At its worst it introduces redundancy and needlessly increases runtime. As for the second conclusion, retaining a reasonable proportion of the best individuals looks like a safe bet. Higher levels of elitism (>10%) proved to be somewhat less fruitful. While better individuals may appear attractive to the greedy, some of them probably represent second-hand solutions

(those that haven't been mutated to one of the better individuals yet, or better individuals that have been unsuccessfully mutated) that may safely be disregarded.

The effect of population size was suspected - at least partially - to be due to increased speed of convergence. This was tested by running all configurations with population size of 150 for a larger number of generations which confirmed the suspicion (table 7). Therefor, future experiments use a reasonably large population size (300), fair rate of elitism (5-20%) and an appropriate stopping criterion (or the number of generations is set reasonably high).

One slightly more surprising result is that higher mutation - and crossover rates appeared to worsen results. High rates of mutation are too disruptive and the default crossover operator (alternating edges) preserves few edges from the parent. In subsequent experiments, only rates of 5% and 95% were abandoned.

It can be noted that just 10 runs and 250 generations is hardly enough (from a statistical point of view). However, only soft conclusions were drawn and limited computing power and time was available. Subsequent experiments were run 30 times per configuration and tend to make use of a stopping criterion (in combination with a high maximum number of generations) to avoid prematurely stopping a run. Additionally, while the number of values that were tried per parameter isn't very high, testing out more values would make for a combinatorial explosion. So only a small part of the utility landscape was explored. For a better analysis iterative methods could be used rather than this basic GENERATE-and-TEST approach.

Stopping Criterion

/stop_criteria/*.m

Implement a stopping criterion that avoids that rather useless iterations (generations) are computed.

- 1. Stopping criterion & explain why you selected this criterion
- 2. Test results (incl. performance criteria and parameter settings)
- 3. Discussion of test results

Other Representation and Appropriate Operators

/crossovers/*.m, /mutations/*.m

Aside from the adjacency representation, (at least) four alternative representations are available. Two of those are binary which were avoided due to previous experiences in constraint programming where the use of binary representations for problems with integer domains is discouraged. They are the binary and matrix representations. The other two alternatives were both implemented. The ordinal representation because it allows for the use of the 'classic' single-point crossover. The path representation because it is probably the most 'natural' representation. For the latter a few crossover operators were implemented (inspired by [2] & [1]). Some of these were mentioned either in Eiben's book or in the course notes; the heuristic - , partially matched -, order -, cycle -, edge recombination - and sequential constructive crossovers in particular. Operators that weren't mentioned include:

- Heuristic Edge Recombination (HERX): equivalent to the edge recombination crossover, but with some hybridisation in that the shortest edge is picked from the edge list of the current city, rather than the edge corresponding to the city with the shortest edge list.
- Max Preservative (MPX): similar to the partially matched crossover. A subtour of the first parent is selected and remaining cities are appended to this sequence in the order that they appear in the other parent. The subtour's length needs to be within a specified interval.
- Order Based (OX2): a few random cities are selected in a parent. These cities are removed from the other parent and replaced by the same cities, at the same locations, but in the order that they appear in the first parent.
- Position Based (POS): this one also selects a few random cities but imposes their positions as well, such that the offspring is the same as the first parent with respect to the cities that were selected, after which the remaining cities are added to it in the order that they appear in the other parent.
- Unnamed Heuristic (UHX): a city is selected randomly. Four edges connected to city are compared, the smallest is picked (if there are edges of equal length, one is picked at random). The city at the other side of this edge becomes the current city and the whole routine is repeated until all cities have been added to the offspring.

The following mutation operators were implemented:

- Insertion: a city is selected, removed and inserted at some other (random) point in the tour.
- Displacement: a subtour is selected, removed and inserted at some other point in the tour.
- *Inversion*: the 'simple' inversion was already implemented. It involves picking out two cities and inverting the subtour between them (which is what 2-opt does). Inversion adds to this by subsequently placing it somewhere else (like the displacement operator does).
- Scramble: selects a random subtour and shuffles the cities around. Clearly quite a disruptive operator.
- *Unnamed*: a hybridised operator, just like its accompanying crossover. A random city is selected and the subtour from this city to the one closest to it is reversed.

These operators were selected such that a general idea could be formed about them. Some are clearly less 'respectful' than others, yet it wasn't entirely clear what to expect aside from what was reported in a fairly limited amount of studies which used other benchmarks. After some manual experiments (within the GUI that was extended for this purpose) further experimentation was done with all crossovers. From the configurations that were trialed before, 9 were selected and each of the crossover operators were tested in conjunction with those parameter values (table 2). The results are displayed in figures 1 to 4 (heatmaps might have been a preferable visualisation and can be generated from the crossoverlatex script, but they were a tad less interpretable).

As for the runtimes; the edge recombination crossovers (both the classical and heuristic one) involve construction of an edge map which makes them the slowest in our list. The others are all about as fast. It's the classical operator (used in the ordinal representation), SCX, HERX or UHX operators who converge more rapidly. The last three are hybrid which makes this unsurprising.

| $Population\ Size$ | Crossover Rate (%) | Mutation Rate (%) | Elitism $(\%)$ | Generations |
|--------------------|--------------------|-------------------|----------------|-------------|
| [300] | [25,50,70] | [25,50,70] | [5] | [1000] |

Table 2: Parameter ranges for the experiments on crossover operators. Each configuration was run 10 times on 4 different datasets (with 70, 100, 127 and 131 cities). A stopping criterion was used to avoid useless iterations; the algorithm stops if the best individual hasn't improved much in the past 100 generations. Results are visualised in figures 1 to 4.

After selection of the 4 more promising crossovers they were tested in combination with all of the 6 remaining mutation operators (all but simple inversion). The results are visualised in figures ??. To some extent an assumption is made that the performance of mutation operators can be gauged separately from the crossover operator in the sense that it wasn't tested if the other 9 crossover operators perform better than others when combined with a particular mutation operator. Again, given the multitude of possible combinations some simplification is in order. Ideally a meta-algorithm would be used to automate the parameter tuning.

| $Population\ Size$ | Crossover Rate (%) | Mutation Rate (%) | Elitism $(\%)$ | Generations |
|--------------------|--------------------|-------------------|----------------|-------------|
| [300] | [50] | [20,40,50,70] | [5] | [1000] |

Table 3: Parameter ranges for the experiments on mutation operators. Each configuration was run for 4 different datasets (with 70, 100, 127 and 131 cities). A stopping criterion was used to avoid useless iterations; the algorithm stops if the best individual hasn't improved much in the past 100 generations. Results are visualised in figure ??.

Local Optimisation

/hybridisation/twoopt.m,/hybridisation/oropt.m

In addition to the loop detection heuristic which was already part of the toolbox, two of the more simple heuristics were applied on some of the benchmarks. Two-opt and Or-opt in particular¹. While not as powerful as the Lin-Kernighan heuristic (which even has some efficient implementations), they're simple to implement and provide good results. The time complexity of improving a tour with those is $\mathcal{O}(N^2)$. The experiments turned out to be fairly uninteresting in that apparently optimal results were found for each of the smaller tours. Though a bit preliminary, we tested out one of the better crossovers in combination with these heuristics on XQF131. A near-optimal tour was found with just one erroneous sequence in the bottom left corner.

Or-opt is a restricted version of 3-opt in which subtours of length 1, 2 or 3 are displaced. If the resulting tour is shorter it is picked for further processing. While 2-opt makes the simple inversion mutation redundant, Or-opt

 $^{^{1}}$ There's some overlap between the two-opt operator and the local loop detection so it's somewhat useless to combine both.

obviously overlaps with some mutation operators as well.

Test to which extent a local optimisation heuristic can improve the result.

- 1. Local optimisation heuristic & explain why you selected this heuristic
- 2. Test results (incl. performance criteria and parameter settings)
- 3. Discussion of test results

Benchmark Problems

Tests on benchmarks were run without any local heuristic (results where they *are* activated are visualised at the end of this report). The results are displayed in table ?? and speak for themselves.

Test the performance of your algorithm using *some* benchmark problems (available on Toledo) and critically evaluate the achieved performance.

Keep in mind that for a large number of cities the search space is extremely large! If your algorithm doesn't perform well for a rather small number of cities, it doesn't make sense to use it for a benchmark problem with a large number of cities

Note: For most of the benchmark problems the length of the optimal tour is known. However, the Matlab template program scales the data. Therefore this scaling must be switched off to be able to compare your result with the optimal tour length.

- 1. List of benchmark problems
- 2. Test results (incl. performance criteria and parameter settings)
- 3. Discussion of test results

Other Tasks

Parent Selection /selection/*.m

The most interesting parent selection strategy that was implemented is probably tournament selection. Its parameter k denotes the number of participants in each tournament and allows one to control selective pressure. Diversity was clearly increased by this operator and results were superior. In contrast the other strategies - fitness proportionate selection with or without σ scaling, exponential ranking and built-in non-linear ranking - did not see similar improvements.

Survivor Selection /reinsertion/*.m

Out of the three survivor selection strategies that were implemented - $\mu + \lambda$, round robin and uniform selection - the first two led to premature convergence and the latter was highly unpredictable but definitely not particularly useful. Any of the parent selection methods can be used for survivor selection.

Diversity Preservation

An island model was implemented where the population is divided into islands if it is large enough. Every island hosts at least 25 individuals and the best ones are transferred from one to the other every so often (leading to periodic drops in average and worst fitness values throughout the generations). It obviously helped with diversity but not in the way tournament selection does; if there was premature convergence in some algorithm, the island model tends to the population in islands with most islands experiencing some degree of premature convergence. The degree of convergence tends to drop a bit as individuals are transferred from one island to an other.

Adaptive Parameter Tuning

It would seem that, as several good solutions have been found after quite a few generations, increased frequency of mutation and reduced frequency of local optimisation (if hybridisation is activated) would prove useful by allowing for a more liberal exploration of the search space. Therefor, an adaptive parameter strategy was implemented which does just that. Instead of seeing interesting new solutions emerge, divergence occurred.

Seeding is a frequently used technique to give a head start. There's many possible approximate solutions for the TSP that can be used for this purpose. One of them is a nearest neighbour solution where a random city is picked and a tour is formed by repeatedly selecting the city nearest to the current one until all of them have been selected. This works well until at the end the remaining edges have to be added, often at high cost. It provides a decent initial solution which is retained through elitism and may provide inspiration for subsequent tours (or lead the algorithm towards a local optimum). While this initial tour generally is within 15% of the optimal one for all given benchmarks, the genetic algorithm tends to cause further improvements until (in a typical run) the resulting tour is within about 6% of the optimum. A nice illustration of the value of hybridisation.

You should select at least one task from the list below:

- 1. Implement and use two other parent selection methods, i.e. fitness proportional selection and tournament selection. Compare the results with those obtained using the default rank-based selection.
- 2. Implement one survivor selection strategy (besides the already implemented elitism). Perform experiments and evaluate the results.
- 3. Implement and use one of the techniques aimed at preserving population diversity (e.g. subpopulations/islands, crowding, ...). Perform experiments and evaluate the results.
- 4. Incorporate an adaptive or self-adaptive parameter control strategy (e.g. parameters that depend on the state of the population, parameters that co-evolve with the population, . . .). Perform experiments and evaluate the results.

For each task:

- 1. Description of implementation
- 2. Description of the experiments
- 3. Test results
- 4. Discussion of test results

Final Results

Combining all of the above, the benchmarks were tested yet again.

We returned to our the default algorithm provided in the toolbox for comparison.

| Crossover Rate | Mutation Rate | Elitism | rondrit025 | rondrit070 | rondrit0127 | belgiumtour | Total Time (s) |
|----------------------------|----------------------|-------------------|-------------------------|--------------------|----------------------------|------------------|-------------------------|
| 5 | 10 | 1 | 39.88 | 1129.53 | 301.73 | 705.33 | 3.16 |
| 5 | 10 | 5 | 39.85 | 1111.11 | 295.07 | 704.37 | 2.92 |
| 5 | 10 | 10 | 39.88 | 1128.86 | 292.94 | 714.93 | 3.07 |
| 25 | 10 | 1 | 39.85 | 1089.23 | 277.36 | 717.66 | 6.33 |
| 25 | 10 | 5 | 39.95 | 1078.36 | 271.84 | 701.80 | 5.30 |
| 25 | 10 | 10 | 39.81 | 1060.66 | 269.12 | 701.97 | 5.54 |
| 50 | 10 | 1 | 39.81 | 1252.28 | 333.35 | 733.01 | 10.01 |
| 50 | 10 | 5 | 39.81 | 1047.86 | 272.19 | 701.33 | 9.16 |
| 50 | 10 | 10 | 39.81 | 1052.85 | 267.24 | 689.64 | 8.89 |
| 75 | 10 | 1 | 50.24 | 2044.69 | 443.77 | 1285.26 | 15.39 |
| 75 | 10 | 5 | 39.81 | 1398.13 | 325.15 | 784.33 | 15.31 |
| 75 | 10 | 10 | 39.81 | 1139.36 | 291.46 | 701.02 | 13.24 |
| 95 | 10 | 1 | 57.56 | 2332.09 | 462.01 | 1465.70 | 18.95 |
| 95 | 10 | 5 | 45.43 | 1888.66 | 398.31 | 1198.29 | 17.31 |
| 95 | 10 | 10 | 39.81 | 1444.34 | 354.56 | 790.83 | 16.69 |
| 5 | 25 | 1 | 39.85 | 984.46 | 275.61 | 684.16 | 3.79 |
| 5 | 25 25 | 5 | 39.81 | 982.26 | 262.45 | 685.49 | 3.48 |
| | | | | | | | |
| 5 | 25 | 10 | 39.81 | 939.78 | 259.67 | 677.71 | 3.46 |
| 25 | 25 | 1 | 39.81 | 1107.00 | 274.10 | 691.25 | 7.05 |
| 25 | 25 | 5 | 39.81 | 1005.26 | 260.25 | 690.62 | 6.43 |
| 25 | 25 | 10 | 39.88 | 1023.40 | 239.45 | 678.65 | 5.99 |
| 50 | 25 | 1 | 39.95 | 1474.90 | 333.94 | 883.15 | 11.77 |
| 50 | 25 | 5 | 39.85 | 1089.82 | 282.48 | 680.63 | 10.57 |
| 50 | 25 | 10 | 39.81 | 992.49 | 270.82 | 677.26 | 9.88 |
| 75 | 25 | 1 | 53.05 | 2013.87 | 422.98 | 1273.33 | 16.31 |
| 75 | 25 | 5 | 40.26 | 1388.90 | 328.45 | 881.81 | 15.09 |
| 75 | 25 | 10 | 39.81 | 1196.01 | 296.75 | 684.32 | 13.83 |
| 95 | 25 | 1 | 58.29 | 2324.97 | 469.66 | 1495.37 | 20.09 |
| 95 | 25 | 5 | 43.54 | 1733.56 | 400.03 | 1129.13 | 18.53 |
| 95 | 25 | 10 | 39.81 | 1458.97 | 350.66 | 772.29 | 17.59 |
| 5 | 50 | 1 | 39.81 | 1037.46 | 263.77 | 706.61 | 4.92 |
| 5 | 50 | 5 | 39.81 | 941.95 | 249.01 | 677.22 | 4.48 |
| | | | | | | | |
| 5 | 50 50 | 10 | 39.85 | 957.15 | 246.60 | 690.40 | 4.75 |
| 25 | 50 | 1 | 39.81 | 1129.27 | 287.48 | 794.02 | 8.40 |
| 25 | 50 | 5 | 39.81 | 1004.02 | 255.89 | 684.30 | 7.99 |
| 25 | 50 | 10 | 39.85 | 989.45 | 252.58 | 681.72 | 7.07 |
| 50 | 50 | 1 | 42.25 | 1518.22 | 342.51 | 916.12 | 12.75 |
| 50 | 50 | 5 | 39.81 | 1162.22 | 278.63 | 691.92 | 11.67 |
| 50 | 50 | 10 | 39.81 | 1056.73 | 270.87 | 687.67 | 10.79 |
| 75 | 50 | 1 | 45.89 | 2040.46 | 417.27 | 1160.69 | 17.57 |
| 75 | 50 | 5 | 40.23 | 1381.74 | 323.16 | 830.28 | 16.54 |
| 75 | 50 | 10 | 39.81 | 1274.47 | 306.12 | 746.85 | 15.28 |
| 95 | 50 | 1 | 56.11 | 2190.59 | 463.83 | 1393.32 | 20.43 |
| 95 | 50 | 5 | 43.70 | 1730.25 | 387.40 | 1015.05 | 19.47 |
| 95 | 50 | 10 | 40.05 | 1516.67 | 339.17 | 892.06 | 18.64 |
| 5 | 75 | 1 | 39.81 | 1163.46 | 269.17 | 812.60 | 6.57 |
| 5 | 75 | 5 | 39.81 | 945.76 | 238.76 | 700.27 | 6.26 |
| 5 | 75 | 10 | 39.85 | 930.06 | 240.42 | 682.05 | 6.05 |
| 25 | 75 | 1 | 40.26 | 1276.73 | 287.03 | 859.56 | 10.01 |
| 25 | 75 75 | 5 | 39.81 | 1008.69 | 248.93 | 714.51 | 9.28 |
| 25 25 | 75 75 | | | | | | 8.09 |
| | | 10 | 39.85 | 1003.08 | 243.49 | 713.66 | |
| 50 | 75 75 | 1 | 41.63 | 1520.14 | 338.83 | 929.25 | 13.45 |
| 50 | 75 75 | 5 | 39.81 | 1136.45 | 279.42 | 740.43 | 12.74 |
| 50 | 75 | 10 | 39.81 | 1071.56 | 281.17 | 689.91 | 12.13 |
| 75 | 75 | 1 | 47.22 | 1958.61 | 406.44 | 1221.32 | 17.49 |
| 75 | 75 | 5 | 40.04 | 1388.59 | 312.78 | 860.72 | 17.59 |
| 75 | 75 | 10 | 39.85 | 1292.43 | 308.98 | 780.71 | 18.28 |
| 95 | 75 | 1 | 59.41 | 2290.11 | 469.52 | 1480.32 | 23.01 |
| 95 | 75 | 5 | 41.28 | 1760.24 | 384.56 | 1146.44 | 21.89 |
| 95 | 75 | 10 | 40.63 | 1539.35 | 352.51 | 930.64 | 19.27 |
| 5 | 95 | 1 | 40.35 | 1215.18 | 263.81 | 821.78 | 7.13 |
| 5 | 95 | 5 | 39.85 | 1021.89 | 244.37 | 709.13 | 6.58 |
| 5 | 95 | 10 | 39.81 | 1009.70 | 236.50 | 695.87 | 6.51 |
| 25 | 95 | 1 | 42.21 | 1354.51 | 297.81 | 878.39 | 10.48 |
| 25 | 95 | 5 | 39.88 | 1082.92 | 262.25 | 719.63 | 10.23 |
| $\frac{25}{25}$ | 95 | 10 | 39.81 | 1060.29 | 263.16 | 703.41 | 9.34 |
| 50 | 95 95 | 10 | 46.21 | 1435.87 | 339.08 | 985.20 | 15.25 |
| | | | | | | | |
| EU | 95 05 | 5 | 39.81 | 1198.67 | 290.15 | 823.71 | 13.31 |
| 50 | | 10 | 39.88 | 1152.10 | 274.71 | 766.47 | 12.85 |
| 50 | 95 | | | | 404.15 | 1170 40 | |
| 50 75 | 95 | 1 | 47.77 | 1908.15 | 404.15 | 1178.48 | 20.32 |
| 50 75 75 | 95 95 | 1 5 | 40.49 | 1384.93 | 336.02 | 913.31 | 18.70 |
| 50 75 75 75 | 95 95 95 | 1 5 10 | 40.49 40.49 | 1384.93 1398.93 | 336.02 316.32 | 913.31 814.54 | 18.70 17.73 |
| 50 75 75 75 95 | 95 95 95 95 | 1 5 10 1 | 40.49 40.49 57.91 | 1384.93 | 336.02 316.32 460.84 | 913.31 | 18.70 17.73 21.39 |
| 50 75 75 75 | 95 95 95 | 1 5 10 | 40.49 40.49 | 1384.93 1398.93 | 336.02 316.32 | 913.31 814.54 | 18.70 17.73 |

Table 4: Results of 75 configurations (population size of 150). The grayscale values of the cells are calibrated against the minimum and maximum for all tests (from table 4 to 8). Darker cells represent better solutions. No stopping criterion was used, maximum number of generations was set to 250. Each configuration was run 10 times.

| Crossover Rate | Mutation Rate | Elitism | rondrit025 | rondrit070 | rondrit0127 | belgiumtour | Total Time (s) |
|-----------------|---------------|---------|----------------|------------|-------------|-------------|----------------|
| 5 | 10 | 1 | 39.81 | 1026.32 | 277.45 | 689.66 | 5.42 |
| 5 | 10 | 5 | 39.85 | 995.24 | 267.05 | 684.67 | 4.70 |
| 5 | 10 | 10 | 39.85 | 1034.40 | 271.66 | 677.14 | 4.97 |
| 25 | 10 | 1 | 39.81 | 967.10 | 267.26 | 680.93 | 12.03 |
| 25 | 10 | 5 | 39.85 | 942.67 | 248.75 | 679.28 | 11.62 |
| 25 | 10 | 10 | 39.81 | 942.36 | 252.09 | 679.51 | 10.81 |
| 50 | 10 | 1 | 39.85 | 1181.41 | 308.58 | 699.21 | 20.95 |
| 50 | 10 | 5 | 39.85 | 995.10 | 260.14 | 677.24 | 19.37 |
| 50 | 10 | 10 | 39.85 | 932.83 | 251.33 | 681.64 | 17.94 |
| 75 | 10 | 1 | 49.77 | 1909.07 | 413.22 | 1189.79 | 34.17 |
| 75 | 10 | 5 | 39.81 | 1331.43 | 312.04 | 764.27 | 28.72 |
| 75 | 10 | 10 | 39.81 | 1110.10 | 301.25 | 679.07 | 25.53 |
| 95 | 10 | 1 | 52.69 | 2099.32 | 436.22 | 1388.94 | 41.01 |
| 95 | 10 | 5 | 43.11 | 1699.08 | 384.74 | 1015.50 | 37.93 |
| 95 | 10 | 10 | 39.81 | 1435.37 | 347.33 | 826.52 | 36.89 |
| 5 | 25 | 1 | 39.81 | 921.40 | 255.56 | 660.77 | 8.42 |
| 5 | 25 | 5 | 39.81 | 871.97 | 255.94 | 681.10 | 7.11 |
| 5 | 25 | 10 | 39.81 | 915.70 | 252.50 | 677.05 | 6.94 |
| 25 | 25 | 1 | 39.81 | 1021.10 | 263.19 | 677.28 | 12.73 |
| 25 | 25 | 5 | 39.81 | 923.51 | 244.58 | 672.53 | 12.60 |
| 25 | 25 | 10 | 39.85 | 904.66 | 237.40 | 664.40 | 12.21 |
| 50 | 25 | 1 | 39.81 | 1303.49 | 317.24 | 765.23 | 21.33 |
| 50 | 25 | 5 | 39.81 | 1002.86 | 267.11 | 666.79 | 19.68 |
| 50 | 25 | 10 | 39.81 | 990.84 | 254.46 | 680.47 | 18.79 |
| 75 | 25 | 1 | 44.17 | 1799.59 | 397.71 | 1053.97 | 32.16 |
| 75 | 25 | 5 | 39.81 | 1263.23 | 303.54 | 792.28 | 30.09 |
| 75 | 25 | 10 | 39.81 | 1127.83 | 288.70 | 697.76 | 29.91 |
| 95 | 25 | 1 | 52.78 | 2121.78 | 449.08 | 1309.36 | 39.69 |
| 95 | 25 | 5 | 41.60 | 1663.95 | 376.11 | 993.88 | 40.59 |
| 95 | 25 | 10 | 39.81 | 1476.09 | 325.93 | 842.27 | 36.03 |
| 5 | 50 | 1 | 39.81 | 956.59 | 238.68 | 677.69 | 10.07 |
| 5 | 50 | 5 | 39.81 | 898.48 | 239.26 | 665.35 | 10.19 |
| 5 | 50 | 10 | 39.81 | 858.82 | 227.84 | 678.52 | 8.44 |
| 25 | 50 | 1 | 39.81 | 1063.69 | 254.09 | 686.64 | 15.23 |
| 25 | 50 | 5 | 39.81 | 933.68 | 247.84 | 674.69 | 14.41 |
| 25 | 50 | 10 | 39.81 | 918.11 | 239.30 | 670.85 | 13.57 |
| 50 | 50 | 1 | 39.88 | 1277.97 | 296.90 | 787.59 | 23.64 |
| 50 | 50 | 5 | 39.81 | 1009.26 | 266.49 | 703.43 | 24.47 |
| 50 | 50 | 10 | 39.81 | 1005.42 | 254.37 | 689.34 | 23.99 |
| 75 | 50 | 1 | 41.75 | 1633.11 | 374.51 | 995.25 | 36.07 |
| 75 | 50 | 5 | 39.81 | 1230.24 | 315.37 | 773.48 | 33.90 |
| 75 | 50 | 10 | 39.81 | 1118.49 | 296.97 | 753.74 | 28.70 |
| 95 | 50 | 1 | 50.10 | 2044.78 | 418.96 | 1323.22 | 39.23 |
| 95 | 50 | 5 | 41.54 | 1650.17 | 373.91 | 950.69 | 37.83 |
| 95 | 50 | 10 | 40.39 | 1478.49 | 344.82 | 850.07 | 39.25 |
| 5 | 75 | 1 | 39.85 | 978.26 | 251.08 | 709.15 | 12.48 |
| 5 | 75 | 5 | 39.81 | 950.27 | 232.39 | 659.82 | 13.75 |
| 5 | 75 | 10 | 39.81 | 906.79 | 226.98 | 674.53 | 13.02 |
| 25 | 75 | 1 | 39.85 | 1171.11 | 272.02 | 737.26 | 20.39 |
| 25 | 75 | 5 | 39.81 | 938.22 | 247.26 | 689.44 | 19.30 |
| 25 | 75 | 10 | 39.81 | 965.60 | 241.18 | 676.45 | 17.34 |
| 50 | 75 | 1 | 40.43 | 1308.53 | 302.33 | 819.90 | 28.25 |
| 50 | 75 | 5 | 39.81 | 1083.16 | 261.68 | 712.63 | 26.59 |
| 50 | 75 | 10 | 39.81 | 1057.10 | 259.96 | 689.85 | 25.56 |
| 75 | 75 | 1 | 41.99 | 1472.81 | 365.27 | 1002.86 | 34.86 |
| 75 | 75 | 5 | 39.81 | 1334.12 | 310.97 | 809.11 | 35.57 |
| 75 | 75 | 10 | 39.85 | 1204.97 | 301.66 | 728.16 | 36.40 |
| 95 | 75 | 1 | 49.62 | 1958.84 | 437.49 | 1228.65 | 44.36 |
| 95 | 75 | 5 | 40.83 | 1672.70 | 375.14 | 993.54 | 41.09 |
| 95 | 75 | 10 | 40.11 | 1561.75 | 345.73 | 916.72 | 39.94 |
| 5 | 95 | 1 | 39.81 | 1101.82 | 259.08 | 751.20 | 14.21 |
| 5 | 95 | 5 | 39.81 | 937.43 | 239.62 | 682.55 | 13.48 |
| 5 | 95 | 10 | 39.81 | 910.88 | 237.34 | 674.67 | 13.08 |
| 25 | 95 | 1 | 39.81 | 1180.11 | 267.77 | 757.28 | 20.92 |
| 25 25 | 95 95 | 5 | 39.81 | 1054.81 | 253.74 | 682.71 | 20.92 |
| $\frac{25}{25}$ | 95 95 | 10 | 39.85 | 1001.84 | 247.52 | 693.13 | 19.87 |
| 50 | 95 95 | 10 | 39.95 | 1321.32 | 295.87 | 810.30 | 29.16 |
| 50 50 | 95 95 | 5 | 39.81 | 1081.48 | 272.77 | 716.21 | 29.10 |
| 50 50 | 95 95 | 5 10 | 39.81 | 1081.48 | 275.22 | 736.31 | 29.37 |
| 50 75 | 95 95 | 10 | 39.81 41.47 | 1562.49 | 347.35 | 1038.87 | 40.31 |
| | 95 95 | 5 | | | 326.74 | | 40.31 |
| 75 75 | | | 40.11 | 1369.60 | | 834.21 | 1 |
| 75 | 95 05 | 10 | 39.85 | 1272.90 | 302.24 | 832.11 | 36.91 |
| 95 | 95 05 | 1 | 51.78 | 2012.85 | 421.27 | 1265.05 | 48.92 |
| 95 95 | 95 05 | 5 10 | 41.43 | 1692.14 | 373.30 | 1030.19 | 48.13 |
| 90 | 95 | 10 | 41.12 | 1575.49 | 360.56 | 985.45 | 44.60 |

Table 5: Results of 75 configurations (population size of 300). The grayscale values of the cells are calibrated against the minimum and maximum for all tests (from table 4 to 8). Darker cells represent better solutions. No stopping criterion was used, maximum number of generations was set to 250. Each configuration was run 10 times.

| Crossover Rate | Mutation Rate | | rondrit025 | rondrit070 | rondrit0127 | belgiumtour | Total Time (s) |
|----------------|---------------|----|------------|--------------------|-------------|------------------|----------------|
| 5 | 10 | 1 | 39.85 | 930.43 | 256.78 | 680.21 | 13.03 |
| 5 | 10 | 5 | 39.81 | 942.02 | 259.12 | 674.14 | 13.41 |
| 5 | 10 | 10 | 39.81 | 951.70 | 261.30 | 669.99 | 11.99 |
| 25 | 10 | 1 | 39.81 | 923.12 | 248.02 | 675.16 | 26.50 |
| 25 | 10 | 5 | 39.81 | 890.55 | 236.60 | 676.53 | 23.47 |
| 25 | 10 | 10 | 39.88 | 873.56 | 234.77 | 659.82 | 23.67 |
| 50 | 10 | 1 | 39.85 | 1167.88 | 297.34 | 686.65 | 42.95 |
| 50 | 10 | 5 | 39.85 | 952.54 | 251.20 | 669.99 | 37.99 |
| 50 | 10 | 10 | 39.81 | 884.58 | 240.65 | 680.78 | 35.27 |
| 75 | 10 | 1 | 47.98 | 1727.69 | 388.89 | 1005.35 | 62.23 |
| 75 | 10 | 5 | 39.81 | 1205.74 | 304.29 | 768.49 | 58.18 |
| 75 | 10 | 10 | | | | 659.82 | 54.04 |
| | | | 39.85 | 1130.15 | 279.38 | | |
| 95 | 10 | 1 | 55.65 | 2149.21 | 442.85 | 1285.62 | 74.09 |
| 95 | 10 | 5 | 39.81 | 1677.19 | 369.89 | 1108.41 | 76.86 |
| 95 | 10 | 10 | 39.85 | 1420.02 | 337.04 | 833.56 | 73.09 |
| 5 | 25 | 1 | 39.81 | 891.62 | 244.70 | 673.74 | 20.15 |
| 5 | 25 | 5 | 39.81 | 855.17 | 236.98 | 682.29 | 18.65 |
| 5 | 25 | 10 | 39.81 | 865.42 | 235.36 | 678.32 | 18.50 |
| 25 | 25 | 1 | 39.85 | 973.69 | 244.89 | 684.03 | 35.46 |
| 25 | 25 | 5 | 39.81 | 860.88 | 230.74 | 679.11 | 33.15 |
| 25 | 25 | 10 | 39.81 | 896.96 | 227.69 | 659.82 | 31.72 |
| 50 | 25 | 1 | 39.81 | 1143.05 | 294.28 | 703.27 | 51.45 |
| 50 | 25 | 5 | 39.81 | 969.63 | 260.42 | 664.53 | 50.82 |
| | | | | | | | |
| 50 | 25 | 10 | 39.81 | 934.17 | 241.03 | 659.82 | 42.09 |
| 75 | 25 | 1 | 41.33 | 1611.60 | 357.94 | 1038.32 | 66.56 |
| 75 | 25 | 5 | 39.92 | 1206.36 | 303.92 | 745.79 | 63.17 |
| 75 | 25 | 10 | 39.81 | 1123.31 | 288.50 | 680.52 | 62.24 |
| 95 | 25 | 1 | 50.13 | 2096.39 | 423.11 | 1355.53 | 83.54 |
| 95 | 25 | 5 | 40.46 | 1614.63 | 365.97 | 976.52 | 76.27 |
| 95 | 25 | 10 | 39.95 | 1520.48 | 343.53 | 866.19 | 66.51 |
| 5 | 50 | 1 | 39.81 | 922.21 | 240.11 | 664.32 | 19.89 |
| 5 | 50 | 5 | 39.85 | 878.41 | 228.43 | 674.69 | 21.16 |
| 5 | 50 | 10 | 39.81 | 858.99 | 222.21 | 669.45 | 19.55 |
| 25 | 50 | 1 | 39.81 | 1001.98 | 251.38 | 707.75 | 39.39 |
| 25 | 50 | 5 | 39.81 | 901.20 | 231.07 | 682.90 | 35.02 |
| | | | | | | | |
| 25 | 50 | 10 | 39.81 | 881.74 | 233.71 | 673.95 | 29.01 |
| 50 | 50 | 1 | 39.85 | 1151.30 | 293.41 | 774.45 | 48.71 |
| 50 | 50 | 5 | 39.85 | 1005.83 | 246.74 | 685.03 | 49.16 |
| 50 | 50 | 10 | 39.81 | 912.96 | 258.98 | 669.43 | 48.11 |
| 75 | 50 | 1 | 40.16 | 1536.11 | 348.50 | 944.13 | 66.21 |
| 75 | 50 | 5 | 39.81 | 1218.18 | 310.51 | 785.96 | 74.57 |
| 75 | 50 | 10 | 39.81 | 1170.13 | 280.64 | 705.90 | 68.51 |
| 95 | 50 | 1 | 49.69 | 2052.34 | 437.40 | 1244.72 | 89.73 |
| 95 | 50 | 5 | 41.26 | 1607.94 | 372.48 | 938.75 | 90.36 |
| 95 | 50 | 10 | 39.81 | 1525.31 | 349.08 | 903.00 | 79.17 |
| 5 | 75 | 1 | 39.81 | 954.07 | 243.90 | 687.42 | 29.31 |
| 5 | 75 | 5 | 39.81 | 881.50 | 226.49 | 666.27 | 29.93 |
| 5 | 75 | 10 | | | 232.14 | | 27.87 |
| | | | 39.81 | 878.71 | | 675.99 | |
| 25 | 75 | 1 | 39.88 | 1084.91 | 247.89 | 723.22 | 47.19 |
| 25 | 75 | 5 | 39.81 | 894.75 | 238.77 | 677.30 | 42.40 |
| 25 | 75 | 10 | 39.81 | 923.96 | 229.14 | 681.82 | 38.25 |
| 50 | 75 | 1 | 39.81 | 1177.05 | 275.39 | 823.70 | 68.42 |
| 50 | 75 | 5 | 39.81 | 1073.21 | 260.73 | 715.15 | 61.51 |
| 50 | 75 | 10 | 39.81 | 991.54 | 252.15 | 706.53 | 50.47 |
| 75 | 75 | 1 | 40.38 | 1455.75 | 364.65 | 917.46 | 81.53 |
| 75 | 75 | 5 | 39.81 | 1305.71 | 285.74 | 789.07 | 78.83 |
| 75 | 75 | 10 | 39.88 | 1249.36 | 290.64 | 723.96 | 75.63 |
| 95 | 75 | 1 | 48.52 | 2013.42 | 426.76 | 1216.01 | 102.22 |
| 95 | 75 | 5 | 41.53 | 1589.63 | 363.68 | 964.11 | 100.81 |
| 95 | 75 | 10 | | | | | |
| | | | 39.85 | 1544.52 | 346.05 | 925.74 | 93.16 |
| 5 | 95 | 1 | 39.85 | 1028.84 | 233.52 | 717.65 | 27.73 |
| 5 | 95 | 5 | 39.81 | 942.56 | 237.00 | 678.32 | 26.74 |
| 5 | 95 | 10 | 39.81 | 955.08 | 231.25 | 681.05 | 25.91 |
| 25 | 95 | 1 | 39.85 | 1104.89 | 259.69 | 727.78 | 40.92 |
| 25 | 95 | 5 | 39.81 | 996.10 | 242.36 | 700.38 | 40.91 |
| 25 | 95 | 10 | 39.85 | 964.75 | 249.32 | 703.11 | 38.52 |
| 50 | 95 | 1 | 39.92 | 1188.30 | 292.16 | 816.51 | 57.02 |
| 50 | 95 | 5 | 39.85 | 1136.67 | 272.94 | 725.23 | 53.99 |
| 50 | 95 | 10 | 39.81 | 1094.00 | 259.76 | 757.17 | 50.85 |
| 75 | 95 | 10 | 40.76 | 1385.94 | 344.12 | 882.17 | 73.13 |
| | 95 95 | | | | 314.43 | 820.45 | 69.95 |
| | | 5 | 39.95 | 1314.50 1364.09 | | 820.45 795.39 | |
| 75 75 | | | | | 306.11 | 795.39 | 65.77 |
| 75 | 95 | 10 | 39.96 | | | | |
| 75 95 | 95 | 1 | 47.15 | 2067.66 | 429.05 | 1222.32 | 87.39 |
| 75 | | | | | | | |

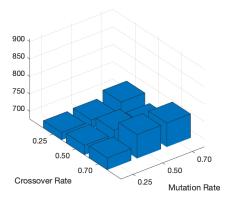
Table 6: Results of 75 configurations (population size of 600). The grayscale values of the cells are calibrated against the minimum and maximum for all tests (from table 4 to 8). Darker cells represent better solutions. No stopping criterion was used, maximum number of generations was set to 250. Each configuration was run 10 times.

| Crossover Rate | Mutation Rate | e Elitism | rondrit025 | rondrit070 | rondrit0127 | belgiumtour | Total Time (s |
|-----------------|----------------|-----------|----------------|--------------------|------------------|------------------|----------------|
| 5 | 10 | 10 | 39.81 | 998.91 | 278.60 | 684.21 | 4.35 |
| 5 | 10 | 20 | 39.88 | 1021.32 | 283.56 | 714.14 | 3.97 |
| 5 | 10 | 40 | 39.81 | 1197.49 | 297.72 | 701.67 | 3.27 |
| 25 | 10 | 10 | 39.81 | 963.74 | 255.61 | 683.17 | 9.30 |
| 25 | 10 | 20 | 39.85 | 958.17 | 267.42 | 688.87 | 8.37 |
| 25 | 10 | 40 | 39.81 | 1125.63 | 281.72 | 721.75 | 6.55 |
| 50 | 10 | 10 | 39.81 | 985.41 | 256.67 | 692.25 | 15.75 |
| 50 | 10 | 20 | 39.81 | 1026.09 | 252.21 | 687.57 | 14.24 |
| 50 | 10 | 40 | 39.81 | 1077.53 | 274.45 | 690.53 | 10.89 |
| 75 | 10 | 10 | 39.88 | 1048.69 | 296.26 | 693.85 | 23.21 |
| 75 | 10 | 20 | 39.81 | 1101.46 | 281.61 | 673.74 | 20.24 |
| 75 | 10 | 40 | 39.81 | 1149.65 | 300.44 | 690.24 | 15.45 |
| 95 | 10 | 10 | 39.85 | 1489.54 | 360.88 | 786.25 | 30.25 |
| 95 | 10 | 20 | 39.81 | 1262.33 | 310.76 | 768.36 | 26.09 |
| 95 | 10 | 40 | 39.85 | 1384.64 | 329.65 | 768.77 | 19.83 |
| 5 | 25 | 10 | 39.85 | 930.60 | 244.39 | 687.91 | 5.62 |
| 5 | 25 | 20 | 39.81 | 981.64 | 257.45 | 677.25 | 5.13 |
| 5 | 25 | 40 | 39.85 | 1065.91 | 293.39 | 684.94 | 4.08 |
| 25 | 25 | 10 | 39.85 | 895.79 | 249.12 | 665.48 | 10.67 |
| 25 | 25 | 20 | 39.81 | 907.49 | 238.69 | 678.20 | 9.60 |
| $\frac{25}{25}$ | $\frac{1}{25}$ | 40 | 40.08 | 987.49 | 279.64 | 682.90 | 7.68 |
| 50 | $\frac{1}{25}$ | 10 | 39.81 | 930.06 | 259.44 | 679.09 | 17.27 |
| 50 | 25 | 20 | 39.81 | 983.54 | 262.35 | 673.49 | 15.57 |
| 50 | 25 | 40 | 39.81 | 1014.45 | 273.68 | 686.19 | 11.89 |
| 75 | 25 | 10 | 39.81 | 1175.26 | 298.26 | 707.98 | 24.84 |
| 75 75 | 25 | 20 | 39.81 | 1139.01 | 269.62 | 691.57 | 21.67 |
| 75 75 | 25 | 40 | 39.81 | 1166.39 | 290.27 | 684.86 | 16.46 |
| 95 | 25 25 | 10 | 39.81 | 1501.04 | 344.14 | 928.82 | 31.65 |
| 95 | 25 | 20 | 39.81 | 1331.36 | 320.25 | 752.12 | 27.59 |
| 95 | 25 | 40 | 39.88 | 1317.27 | 320.03 | 782.09 | 20.84 |
| 5 | 50 | 10 | 39.81 | 888.57 | 242.11 | 684.69 | 7.71 |
| 5 | 50 | 20 | 39.81 | 905.60 | 245.25 | 675.28 | 7.00 |
| 5 | 50 | 40 | 39.88 | 1009.15 | 259.02 | 674.71 | 5.50 |
| $\frac{5}{25}$ | 50 | 10 | 39.81 | 938.81 | 243.48 | 664.40 | 12.92 |
| $\frac{25}{25}$ | 50 | 20 | 39.81 | 923.20 | 246.14 | 677.71 | 11.58 |
| $\frac{25}{25}$ | 50 | 40 | 39.85 | 1051.47 | 256.28 | 702.04 | 8.99 |
| 50 | 50 50 | 10 | 39.81 | 1000.19 | 259.62 | 689.94 | 19.76 |
| 50 50 | 50 | 20 | 39.85 | 1034.11 | 261.99 | 660.77 | 17.62 |
| 50 50 | 50 50 | | | | | | 13.34 |
| 75 | 50 50 | 40 | 39.85 | 1081.69 | 286.20 311.46 | 698.26 | 27.33 |
| 75 75 | 50 50 | 10 20 | 39.81 | 1188.37 | 269.57 | 738.11 740.21 | |
| 75 75 | 50 50 | 40 | 39.81 39.81 | 1172.89 1170.34 | 301.70 | 763.01 | 23.88 18.17 |
| | 50 50 | | | 1493.67 | | | |
| 95 | | 10 | 39.81 | | 358.62 | 829.74 | 34.27 |
| 95 | 50 50 | 20 | 39.81 | 1475.72 | 337.97 | 843.31 | 29.58 |
| 95 | | 40 | 39.81 | 1435.66 | 346.59 | 860.19 | 22.30 |
| 5 | 75 | 10 | 39.85 | 840.14 | 236.99 | 681.11 | 9.66 |
| 5 | 75 75 | 20 | 39.81 | 912.07 | 240.76 | 679.31 | 8.73 |
| 5 | 75 75 | 40 | 39.81 | 1057.58 | 261.20 | 688.88 | 6.86 |
| 25 | 75 75 | 10 | 39.85 | 977.63 | 240.95 | 673.74 | 15.03 |
| 25 | 75 75 | 20 | 39.81 | 1013.75 | 248.55 | 690.24 | 13.45 |
| 25 | 75 | 40 | 39.81 | 1010.13 | 270.87 | 691.52 | 10.41 |
| 50 50 | 75 75 | 10 | 39.81 | 1076.18 | 265.19 | 697.80 | 22.01 |
| 50 50 | 75 75 | 20 | 39.85 | 1105.90 | 274.20 | 695.24 | 19.52 |
| 50 | 75 75 | 40 | 39.81 | 1166.18 | 282.47 | 681.93 | 15.03 |
| 75 75 | 75 75 | 10 | 39.81 | 1280.02 | 300.91 | 781.15 | 29.49 |
| 7 5 | 75 75 | 20 | 39.81 | 1183.88 | 293.88 | 742.12 | 25.93 |
| 75 25 | 75 75 | 40 | 39.81 | 1269.35 | 308.44 | 806.14 | 19.67 |
| 95 | 75 75 | 10 | 40.41 | 1566.22 | 356.75 | 993.65 | 35.70 |
| 95 | 75 | 20 | 40.28 | 1454.29 | 350.82 | 909.13 | 31.58 |
| 95 | 75 | 40 | 39.81 | 1465.02 | 339.11 | 921.52 | 23.89 |
| 5 | 95 | 10 | 39.81 | 978.23 | 235.28 | 690.17 | 11.25 |
| 5 | 95 | 20 | 39.81 | 964.56 | 243.53 | 692.42 | 10.19 |
| 5 | 95 | 40 | 39.81 | 1066.87 | 253.69 | 709.25 | 7.99 |
| 25 | 95 | 10 | 39.81 | 1023.99 | 241.74 | 701.62 | 16.68 |
| 25 | 95 | 20 | 39.85 | 1012.17 | 256.76 | 698.19 | 15.01 |
| 25 | 95 | 40 | 39.81 | 1102.06 | 274.07 | 727.95 | 11.65 |
| 50 | 95 | 10 | 39.85 | 1102.65 | 275.30 | 753.05 | 23.72 |
| 50 | 95 | 20 | 39.85 | 1156.65 | 277.78 | 762.74 | 21.20 |
| 50 | 95 | 40 | 39.81 | 1224.12 | 284.71 | 782.02 | 16.16 |
| 75 | 95 | 10 | 39.81 | 1344.22 | 319.51 | 822.96 | 31.30 |
| 75 | 95 | 20 | 39.81 | 1273.87 | 307.99 | 849.56 | 27.75 |
| 75 | 95 | 40 | 39.88 | 1409.01 | 313.02 | 846.51 | 21.07 |
| 95 | 95 | 10 | 40.98 | 1637.14 | 356.96 | 1018.36 | 37.32 |
| 30 | | | 10.05 | 1590.00 | 353.30 | 957.62 | 99.14 |
| 95 95 | 95 | 20 | 40.35 40.56 | 1536.69 1544.99 | 393.30 | 983.28 | 33.14 25.08 |

Table 7: Investigation of higher rates of elitism (higher rates of elitism don't appear to improve results). Results of 75 configurations (population size of 150). The grayscale values of the cells are calibrated against the minimum and maximum for all tests (from table 4 to 8). Darker cells represent better solutions. No stopping criterion was used, maximum number of generations was set to 250. Each configuration was run 10 times.

| - | Mutation Rate | | rondrit025 | rondrit070 | rondrit0127 | belgiumtour | Total Time (s |
|----------------------|---------------|---------|----------------|--------------------|------------------|------------------|---------------|
| 5 | 10 | 1 | 39.81 | 798.23 | 221.93 | 667.22 | 5.51 |
| 5 | 10 | 5 | 39.81 | 800.32 | 214.99 | 677.22 | 6.03 |
| 5 | 10 | 10 | 40.35 | 855.03 | 212.22 | 659.82 | 5.75 |
| 25 | 10 | 1 | 39.81 | 824.85 | 220.84 | 679.12 | 11.80 |
| 25 | 10 | 5 | 39.81 | 780.99 | 216.14 | 708.19 | 10.48 |
| 25 | 10 | 10 | 39.81 | 792.45 | 206.12 | 677.22 | 10.00 |
| 50 | 10 | 1 | 39.81 | 998.84 | 262.47 | 677.32 | 18.84 |
| 50 | 10 | 5 | 39.81 | 763.28 | 206.57 | 683.67 | 17.24 |
| 50 | 10 | 10 | 39.81 | 759.71 | 207.28 | 674.14 | 16.23 |
| 75 | 10 | 1 | 48.51 | 1936.12 | 410.20 | 1241.86 | 28.98 |
| 75 | 10 | 5 | 39.85 | 1030.30 | 292.26 | 674.53 | 25.95 |
| 75 75 | 10 | | | | 220.41 | | 23.14 |
| | | 10 | 39.81 | 842.67 | | 673.16 | |
| 95 | 10 | 1 | 53.91 | 2277.86 | 469.51 | 1453.19 | 35.41 |
| 95 | 10 | 5 | 40.57 | 1604.17 | 357.54 | 1058.75 | 33.84 |
| 95 | 10 | 10 | 39.95 | 1091.10 | 297.81 | 674.14 | 30.28 |
| 5 | 25 | 1 | 39.85 | 774.41 | 200.65 | 681.68 | 6.99 |
| 5 | 25 | 5 | 39.81 | 729.42 | 187.68 | 669.45 | 6.72 |
| 5 | 25 | 10 | 39.81 | 748.27 | 185.29 | 682.78 | 6.44 |
| 25 | 25 | 1 | 39.81 | 839.93 | 215.04 | 675.16 | 12.67 |
| 25 | 25 | 5 | 39.92 | 738.24 | 181.63 | 677.32 | 12.00 |
| 25 | 25 | 10 | 40.11 | 748.23 | 182.84 | 679.31 | 11.42 |
| 50 | 25 | 1 | 39.88 | 1186.09 | 286.35 | 773.08 | 21.24 |
| | | | | | | | |
| 50 | 25 | 5 | 39.81 | 778.69 | 219.01 | 683.87 | 19.04 |
| 50 | 25 | 10 | 39.88 | 758.84 | 199.88 | 659.82 | 17.69 |
| 75 | 25 | 1 | 48.16 | 1795.08 | 396.64 | 1150.86 | 30.24 |
| 75 | 25 | 5 | 39.85 | 1093.56 | 280.48 | 691.31 | 28.01 |
| 75 | 25 | 10 | 39.81 | 869.67 | 236.77 | 684.99 | 24.96 |
| 95 | 25 | 1 | 55.68 | 2306.38 | 460.72 | 1412.22 | 36.68 |
| 95 | 25 | 5 | 40.38 | 1514.12 | 352.94 | 943.33 | 35.13 |
| 95 | 25 | 10 | 39.81 | 1194.99 | 283.63 | 692.60 | 31.99 |
| 5 | 50 | 1 | 39.81 | 859.93 | 204.75 | 687.18 | 9.39 |
| 5 | 50 | 5 | 39.85 | 726.00 | 177.49 | 678.52 | 9.01 |
| | 50 | 10 | 39.81 | 730.74 | 180.55 | 678.20 | 8.59 |
| 5 | | | | | | | |
| 25 | 50 | 1 | 39.92 | 989.30 | 239.87 | 722.17 | 15.45 |
| 25 | 50 | 5 | 39.81 | 770.96 | 196.54 | 688.00 | 14.54 |
| 25 | 50 | 10 | 39.81 | 731.32 | 185.71 | 677.24 | 13.72 |
| 50 | 50 | 1 | 39.81 | 1206.34 | 300.53 | 863.52 | 24.01 |
| 50 | 50 | 5 | 39.81 | 874.65 | 212.70 | 700.99 | 21.94 |
| 50 | 50 | 10 | 39.81 | 791.85 | 195.57 | 677.10 | 20.36 |
| 75 | 50 | 1 | 42.74 | 1718.14 | 379.48 | 1072.10 | 32.67 |
| 75 | 50 | 5 | 39.81 | 1069.07 | 268.12 | 725.72 | 30.66 |
| 75 | 50 | 10 | 39.81 | 966.67 | 238.25 | 683.39 | 27.84 |
| 95 | 50 | 1 | 52.66 | 2194.85 | 454.80 | 1381.65 | 38.81 |
| 95 | 50 | 5 | | | | | |
| | | | 40.66 | 1463.04 | 344.99 | 915.54 | 37.26 |
| 95 | 50 | 10 | 39.85 | 1178.59 | 291.26 | 731.80 | 34.53 |
| 5 | 75 | 1 | 39.81 | 922.42 | 222.04 | 744.06 | 11.60 |
| 5 | 75 | 5 | 39.81 | 760.67 | 180.52 | 659.82 | 11.18 |
| 5 | 75 | 10 | 39.81 | 729.88 | 176.65 | 678.50 | 10.61 |
| 25 | 75 | 1 | 40.08 | 1054.43 | 253.36 | 720.25 | 17.77 |
| 25 | 75 | 5 | 39.81 | 818.27 | 196.65 | 670.28 | 16.86 |
| 25 | 75 | 10 | 39.81 | 759.18 | 184.73 | 678.32 | 15.87 |
| 50 | 75 | 1 | 39.92 | 1340.11 | 289.93 | 835.43 | 26.12 |
| 50 | 75 | 5 | 39.88 | 905.59 | 208.14 | 702.32 | 24.40 |
| 50 | 75 | 10 | 39.85 | 813.66 | 215.77 | 678.65 | 22.90 |
| 75 | 75 | 1 | 40.35 | 1578.21 | 356.97 | 1018.76 | 34.47 |
| | | | | | | | |
| 75 | 75 | 5 | 40.11 | 1063.12 | 270.97 | 746.47 | 32.75 |
| 75 | 75 | 10 | 39.88 | 998.40 | 240.25 | 687.51 | 30.21 |
| 95 | 75 | 1 | 58.31 | 2132.52 | 434.13 | 1372.71 | 40.90 |
| 95 | 75 | 5 | 40.08 | 1431.33 | 344.71 | 887.70 | 39.29 |
| 95 | 75 | 10 | 39.81 | 1246.93 | 307.08 | 746.63 | 36.66 |
| 5 | 95 | 1 | 39.85 | 1030.89 | 236.36 | 733.34 | 13.32 |
| 5 | 95 | 5 | 39.81 | 775.10 | 193.08 | 677.12 | 12.82 |
| 5 | 95 | 10 | 39.85 | 775.18 | 187.48 | 674.57 | 12.28 |
| 25 | 95 | 1 | 39.95 | 1139.96 | 268.00 | 812.21 | 19.68 |
| $\frac{25}{25}$ | 95 95 | 5 | 39.81 | 825.21 | 198.97 | 691.17 | 18.66 |
| | | | | | | | ! |
| 25 50 | 95 | 10 | 39.81 | 817.35 | 198.17 | 678.54 | 17.71 |
| 50 | 95 | 1 | 40.08 | 1281.54 | 275.92 | 869.53 | 27.97 |
| | 95 | 5 | 39.85 | 915.83 | 232.84 | 722.80 | 26.25 |
| 50 | 95 | 10 | 39.88 | 873.46 | 224.81 | 679.28 | 24.59 |
| 50 50 | 05 | 1 | 42.88 | 1588.25 | 370.08 | 1096.23 | 36.62 |
| | 95 | 1 | | 1 | | | |
| 50 75 | | | | 1156.23 | 271.29 | 703.57 | 34.44 |
| 50 75 75 | 95 | 5 | 39.81 | 1156.23 1055.12 | 271.29 257.24 | 703.57 711.60 | 34.44 |
| 50 75 75 75 | 95 95 | 5 10 | 39.81 39.85 | 1055.12 | 257.24 | 711.60 | 32.14 |
| 50 75 75 | 95 | 5 | 39.81 | | | | |

Table 8: Investigation of effect of the number of generations (the results are much better than when 250 generations were run). Results of 75 configurations (population size of 150). The grayscale values of the cells are calibrated against the minimum and maximum for all tests (from table 4 to 8). Darker cells represent better solutions. No stopping criterion was used, maximum number of generations was set to 500. Each configuration was run 10 times.



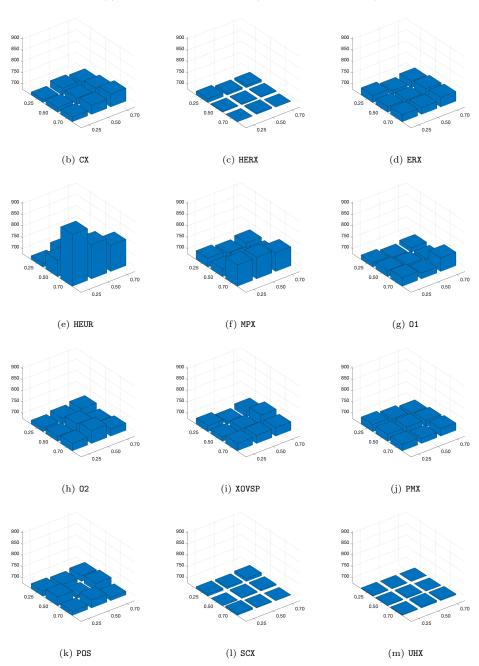
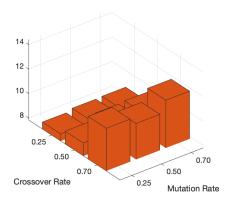


Figure 1: Shortest tour found by each crossover operator (tour of 70 cities). Maximum of 1000 generations and basic stopping criterion (the algorithm stops when there has been no improvement in 100 generations which is quite strict, such that late and surprising improvements can be ruled out). The stop condition was met in most cases.



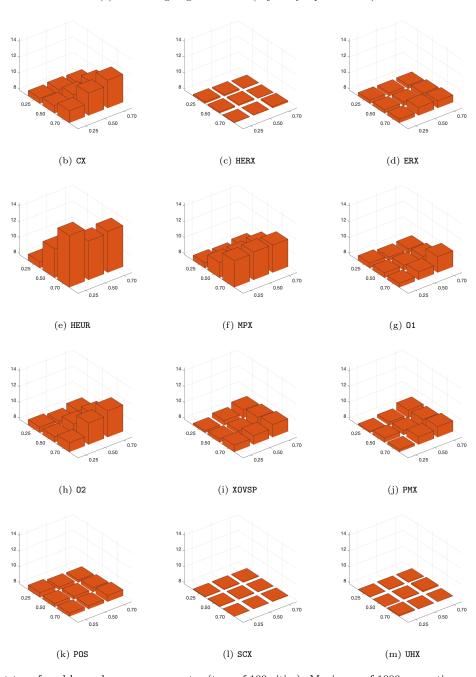
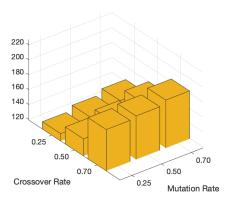


Figure 2: Shortest tour found by each crossover operator (tour of 100 cities). Maximum of 1000 generations and basic stopping criterion (the algorithm stops when there has been no improvement in 100 generations which is quite strict, such that late and surprising improvements can be ruled out). The stop condition was met in most cases.



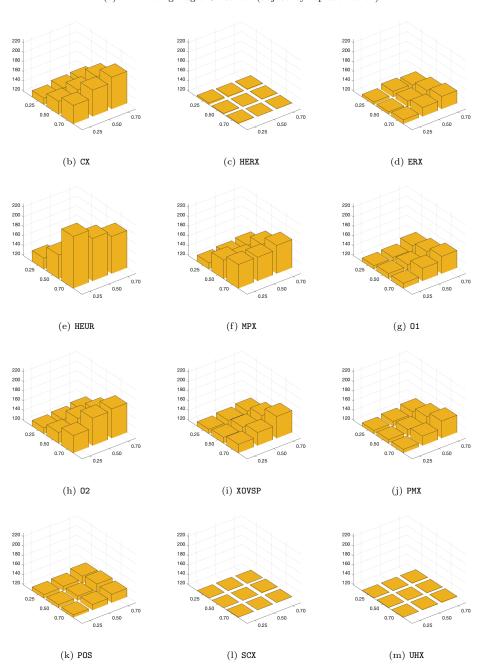
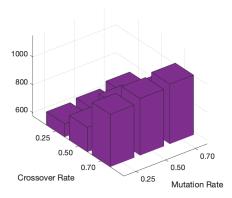


Figure 3: Shortest tour found by each crossover operator (tour of 127 cities). Maximum of 1000 generations and basic stopping criterion (the algorithm stops when there has been no improvement in 100 generations which is quite strict, such that late and surprising improvements can be ruled out). The stop condition was met in most cases.



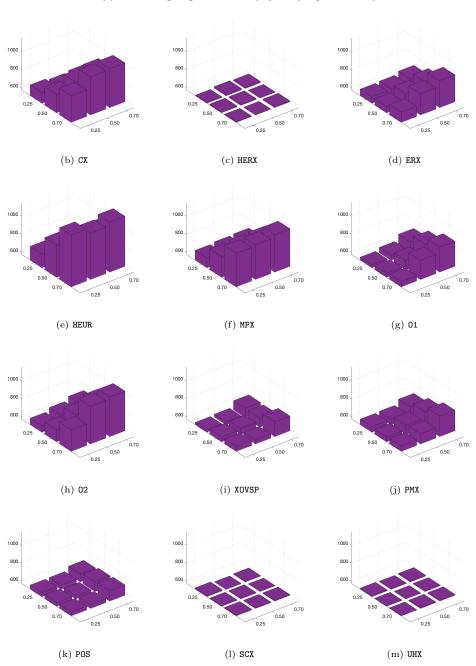


Figure 4: Shortest tour found by each crossover operator (tour of 131 cities). Maximum of 1000 generations and basic stopping criterion (the algorithm stops when there has been no improvement in 100 generations which is quite strict, such that late and surprising improvements can be ruled out). The stop condition was met in most cases.

References

- [1] Hassan Ismkhan and Kamran Zamanifar. Study of some recent crossovers effects on speed and accuracy of genetic algorithm, using symmetric travelling salesman problem. CoRR, abs/1504.02590, 2015.
- [2] P. Larrañaga, C.M.H. Kuijpers, R.H. Murga, I. Inza, and S. Dizdarevic. *Artificial Intelligence Review*, 13(2):129–170, 1999.

Time Spent on the Project

- 1. For each student of the team: estimate how many hours spent on the project (NOT including studying textbook and other reading material).
 - (a) Michaël Dooreman :
 - (b) Bruno Vandekerkhove :