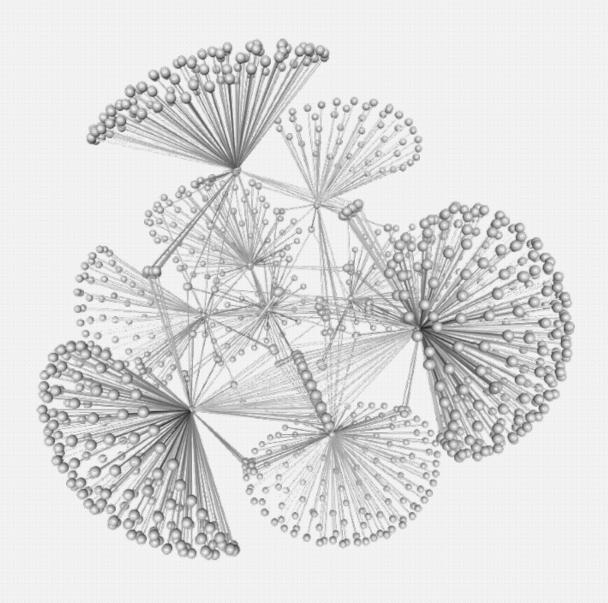
Probabilistic Programming

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H05N0A: CAPITA SELECTA: ARTIFICIAL

Intelligence

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Below's our solution for the given challenges. The questions in each section of the original assignment are answered in a section having the same title.

```
person(a).
person(b).
person(c).
0.2::stress(X) :- person(X).
0.1::friends(X,Y) :- person(X), person(Y).
0.3::smokes(X) :- stress(X).
0.4::smokes(X):- friends(X,Y), smokes(Y).
query(smokes(a)).
```

Code snippet 1: PROBLOG program used throughout the first two chapters of the report.

```
Probabilistic Inference Using Weighted
Model Counting
```

SRL to CNF

13

15

17

0.1::friends(c,b).

0.1::friends(c,c).

0.3::smokes(a) :- stress(a).

0.3::smokes(b) :- stress(b).

0.3::smokes(c) :- stress(c).

First the program is grounded. This is a matter of collecting all atoms involved in all proofs of the query.

```
0.2::stress(a).
   0.2::stress(b).
   0.2::stress(c).
   0.1::friends(a,a).
  0.1::friends(a,b).
   0.1::friends(a,c).
   0.1::friends(b,a).
   0.1::friends(b,b).
10
   0.1::friends(b,c).
12
   0.1::friends(c,a).
```

```
in figure 1, where colourings indicate the presence of
cycles. Any proof involving an atom friends(X,X)
or friends(Y,a) (with Y \in \{b,c\}) is non-minimal
and doesn't affect the final probability. These atoms
are disregarded. For the remaining cycles (involving
```

```
0.2::stress(a).
0.2::stress(b).
0.2::stress(c).
```

Code snippet 2: Relevant ground program.

0.4::smokes(a) :- friends(a,a), smokes(a).

0.4::smokes(a):- friends(a,b), smokes(b). 0.4::smokes(a):- friends(a,c), smokes(c).

0.4::smokes(b) :- friends(b,a), smokes(a). 0.4::smokes(b):- friends(b,b), smokes(b).

0.4::smokes(b) :- friends(b,c), smokes(c).

0.4::smokes(c):- friends(c,a), smokes(a).

0.4::smokes(c):- friends(c,b), smokes(b).

0.4::smokes(c):- friends(c,c), smokes(c).

The proofs of the query make for a trie as shown friends(b,c) and friends(c,b)) auxiliary variables can be used to obtain a cycle-free program:

```
0.1::friends(a,b).
   0.1::friends(a,c).
   0.1::friends(b,c).
   0.1::friends(c,b).
   0.3::p(a).
10
   0.3::p(b).
11
   0.3::p(c).
12
13
   0.4::p(a,b).
14
   0.4::p(a,c).
15
   0.4::p(b,c).
   0.4::p(c,b).
17
18
   smokes(a) :- stress(a), p(a).
19
   smokes(b) :- stress(b), p(b).
   smokes(c) :- stress(c), p(c).
21
22
   smokes(a) :-
23
        friends(a,b), smokes(b), p(a,b).
24
   smokes(a) :-
25
        friends(a,c), smokes(c), p(a,c).
26
   smokes(b) :-
27
        friends(b,c), stress(c), p(c), p(b,c).
28
29
        friends(c,b), stress(b), p(b), p(c,b). SRL to PGM
30
31
   query(smokes(a)).
```

Code snippet 3: Relevant ground program without cycles.

The above logic program is equivalent to the following propositional formula:

```
(smokes(a) \leftrightarrow (stress(a) \land p(a)))
   \vee (friends(a,b) \land smokes(b) \land p(a,b))
   \vee (friends(a, c) \land smokes(c) \land p(a, c)))
(smokes(b) \leftrightarrow (stress(b) \land p(b))
\vee (friends(b,c) \wedge stress(c) \wedge p(c) \wedge p(b,c)))
(smokes(c) \leftrightarrow (stress(c) \land p(c)))
\vee \; (friends(c,b) \land stress(b) \land p(b) \land p(c,b)))
```

Which gives the following CNF:

```
(\neg smokes(a) \lor stress(a) \lor friends(a,b) \lor friends(a,c))
\land (\neg smokes(a) \lor stress(a) \lor friends(a,b) \lor smokes(c))
\land (\neg smokes(a) \lor stress(a) \lor smokes(b) \lor friends(a, c))
\land (\neg smokes(a) \lor stress(a) \lor smokes(b) \lor smokes(c))
\land (\neg stress(a) \lor smokes(a))
\land (\neg friends(a,b) \lor \neg smokes(b) \lor smokes(a))
\land (\neg friends(a, c) \lor \neg smokes(c) \lor smokes(a))
\land (\neg smokes(b) \lor p(b) \lor friends(b, c))
\land (\neg smokes(b) \lor p(b) \lor p(c))
\wedge \left(\neg p(b) \vee smokes(b)\right)
\wedge \left(\neg friends(b,c) \vee \neg p(c) \vee smokes(b)\right)
\land (\neg smokes(c) \lor p(c) \lor friends(c,b))
\land (\neg smokes(c) \lor p(c) \lor p(b))
\land (\neg p(c) \lor smokes(c))
```

```
\wedge \left(\neg friends(c,b) \vee \neg p(b) \vee smokes(c)\right)
\wedge (\neg p(b) \vee stress(b))
\land (\neg stress(b) \lor p(b))
\wedge (\neg p(c) \vee stress(c))
\wedge (\neg stress(c) \vee p(c))
```

The probabilistic literals CNF are assigned weights (derived literals have a weight of 1):

Atom	Weight
stress(a)	0.2
$\neg stress(a)$	0.8
stress(b)	0.2
¬stress(b)	0.8
stress(c)	0.2
$\neg stress(c)$	0.8
friends(a,b)	0.1
$\neg friends(a,b)$	0.9
friends(a,c)	0.1
$\neg friends(a,c)$	0.9
friends(b,c)	0.1
$\neg friends(b,c)$	0.9
friends(c,b)	0.1
$\neg friends(c,b)$	0.9

PGM to CNF

Weighted Model Counting

Lifted Inference

Parameter Learning

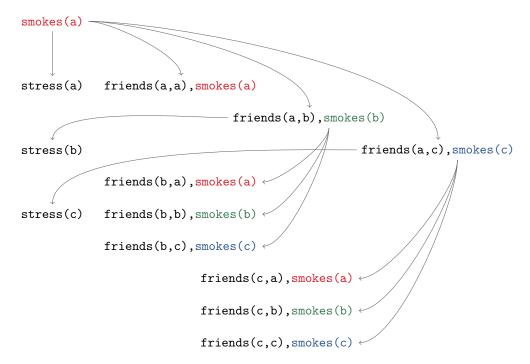


Figure 1: SLG-tree produced while turning the ground program into a boolean formula. Coloured atoms indicate the presence of cycles.