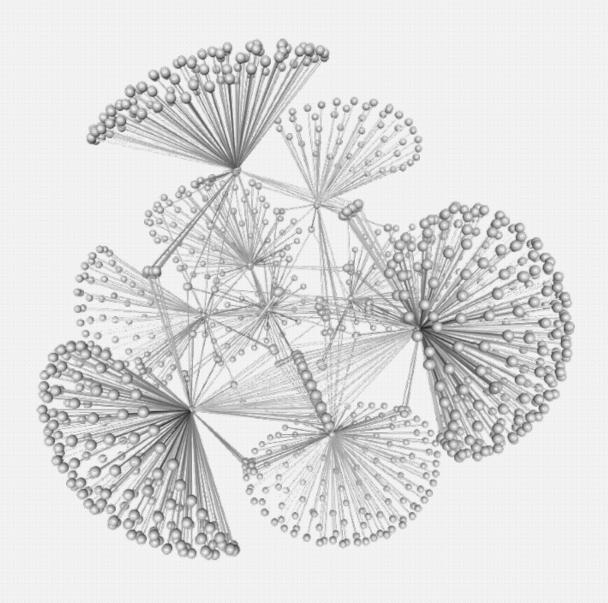
## Probabilistic Programming

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H05N0A: CAPITA SELECTA: ARTIFICIAL

Intelligence

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Below's our solution for the given challenges. The questions in each section of the original assignment are answered in a section having the same title.

```
person(a).
person(b).
person(c).

0.2::stress(X) :- person(X).

0.1::friends(X,Y) :- person(X), person(Y).

0.3::smokes(X) :- stress(X).

0.4::smokes(X) :- friends(X,Y), smokes(Y).

query(smokes(a)).
```

Code snippet 1: PROBLOG program used throughout the first two chapters of the report.

```
Probabilistic Inference Using Weighted
Model Counting
```

## SRL to CNF

First the program is grounded. This is a matter of collecting all atoms involved in all proofs of the query.

```
collecting all atoms involved in all proofs of the quality of the
```

0.1::friends(c,b).

0.1::friends(c,c).

0.3::smokes(a) :- stress(a).

0.3::smokes(b) :- stress(b).

0.3::smokes(c) :- stress(c).

15

17

```
0.4::smokes(b):- friends(b,c), smokes(c).

0.4::smokes(c):- friends(c,a), smokes(a).

0.4::smokes(c):- friends(c,b), smokes(b).

0.4::smokes(c):- friends(c,c), smokes(c).
```

0.4::smokes(a):- friends(a,a), smokes(a). 0.4::smokes(a):- friends(a,b), smokes(b).

0.4::smokes(a) :- friends(a,c), smokes(c). 0.4::smokes(b) :- friends(b,a), smokes(a).

0.4::smokes(b):- friends(b,b), smokes(b).

Code snippet 2: Relevant ground program.

The proofs of the query make for a trie as shown in figure 1, where colourings indicate the presence of cycles. Any proof involving an atom friends(X,X) or friends(Y,a) (with  $Y \in \{b,c\}$ ) is non-minimal and doesn't affect the final probability. These atoms are disregarded. For the remaining cycles (involving friends(b,c) and friends(c,b)) auxiliary variables can be used to obtain a cycle-free program without intensional probabilistic facts:

```
0.2::stress(a).
2 0.2::stress(b).
3 0.2::stress(c).
```

```
0.1::friends(a,b).
                                                                       \land (\neg smokes(a) \lor p(a) \lor p(a,b) \lor friends(a,c))
     0.1::friends(a,c).
                                                                       \land (\neg smokes(a) \lor p(a) \lor p(a,b) \lor smokes(c))
     0.1::friends(b,c).
                                                                       \wedge \left(\neg smokes(a) \vee p(a) \vee p(a,b) \vee p(a,c)\right)
     0.1::friends(c,b).
                                                                       \land (\neg stress(a) \lor \neg p(a) \lor smokes(a))
                                                                       \land (\neg friends(a,b) \lor \neg smokes(b) \lor \neg p(a,b) \lor smokes(a))
                                                                       \land (\neg friends(a, c) \lor \neg smokes(c) \lor \neg p(a, c) \lor smokes(a))
     0.3::p(a).
10
     0.3::p(b).
                                                                       \land (\neg smokes(b) \lor stress(b) \lor friends(b, c))
11
     0.3::p(c).
                                                                       \land (\neg smokes(b) \lor stress(b) \lor stress(c))
12
                                                                       \land (\neg smokes(b) \lor stress(b) \lor p(c))
13
     0.4::p(a,b).
                                                                       \land (\neg smokes(b) \lor stress(b) \lor p(b,c)
14
                                                                       \land (\neg smokes(b) \lor p(b) \lor friends(b, c))
     0.4::p(a,c).
15
                                                                       \land (\neg smokes(b) \lor p(b) \lor stress(c))
     0.4::p(b,c).
                                                                       \land (\neg smokes(b) \lor p(b) \lor p(c))
     0.4::p(c,b).
17
                                                                       \land (\neg smokes(b) \lor p(b) \lor p(b,c)
18
     smokes(a) :- stress(a), p(a).
                                                                       \land (\neg stress(b) \lor \neg p(b) \lor smokes(b))
19
     smokes(b) :- stress(b), p(b).
                                                                       \land (\neg friends(b,c) \lor \neg stress(c) \lor \neg p(c) \lor \neg p(b,c) \lor 
     smokes(c) :- stress(c), p(c).
                                                                       smokes(b)
21
                                                                       \land (\neg smokes(c) \lor stress(c) \lor friends(c,b))
22
     smokes(a) :-
                                                                       \land (\neg smokes(c) \lor stress(c) \lor stress(b))
23
           friends(a,b), smokes(b), p(a,b).
                                                                       \wedge \left(\neg smokes(c) \vee stress(c) \vee p(b)\right)
24
                                                                       \land (\neg smokes(c) \lor stress(c) \lor p(c,b))
     smokes(a) :-
25
           friends(a,c), smokes(c), p(a,c).
                                                                       \wedge \left( \neg smokes(c) \lor p(c) \lor friends(c,b) \right)
26
                                                                       \wedge \left(\neg smokes(c) \vee p(c) \vee stress(b)\right)
     smokes(b) :-
27
           friends(b,c), stress(c), p(c), p(b,c).
                                                                      \wedge \left(\neg smokes(c) \vee p(c) \vee p(b)\right)
28
                                                                       \land (\neg smokes(c) \lor p(c) \lor p(c,b))
29
           friends(c,b), stress(b), p(b), p(c,b).
                                                                      \land (\neg stress(c) \lor \neg p(c) \lor smokes(c))
30
                                                                       \land (\neg friends(c,b) \lor \neg stress(b) \lor \neg p(b) \lor \neg p(c,b) \lor
31
     query(smokes(a)).
                                                                       smokes(c))
```

Code snippet 3: Relevant ground program without cycles.

The probabilistic literals in the CNF are assigned weights (derived literals get a weight of 1):

The above logic program is equivalent to the following propositional formula :

```
 (smokes(a) \leftrightarrow (stress(a) \land p(a)) \\ \lor (friends(a,b) \land smokes(b) \land p(a,b)) \\ \lor (friends(a,c) \land smokes(c) \land p(a,c))) \\ \land \\ (smokes(b) \leftrightarrow (stress(b) \land p(b)) \\ \lor (friends(b,c) \land stress(c) \land p(c) \land p(b,c))) \\ \land \\ (smokes(c) \leftrightarrow (stress(c) \land p(c)) \\ \lor (friends(c,b) \land stress(b) \land p(b) \land p(c,b)))
```

## Which yields the following CNF:

is get a weight of 1).		
Literal	Weight	
stress(a)	0.2	
$\neg stress(a)$	0.8	
stress(b)	0.2	
$\neg stress(b)$	0.8	
stress(c)	0.2	
$\neg stress(c)$	0.8	
friends(a,b)	0.1	
$\neg friends(a,b)$	0.9	
friends(a,c)	0.1	
$\neg friends(a,c)$	0.9	
friends(b,c)	0.1	
$\neg friends(b,c)$	0.9	
friends(c,b)	0.1	
$\neg friends(c,b)$	0.9	
p(a)	0.3	
$\neg p(a)$	0.7	
p(b)	0.3	
$\neg p(b)$	0.7	
p(c)	0.3	
$\neg p(c)$	0.7	
p(a,b)	0.4	
$\neg p(a,b)$	0.6	
p(a,c)	0.4	
$\neg p(a,c)$	0.6	
p(b,c)	0.4	
$\neg p(b,c)$	0.6	
p(c,b)	0.4	
$\neg p(c,b)$	0.6	

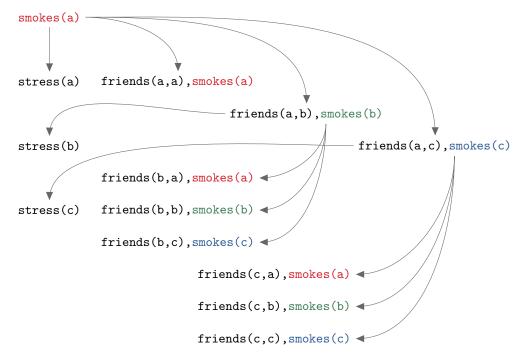


Figure 1: Trie representing proofs of the query. Coloured atoms indicate the presence of cycles.

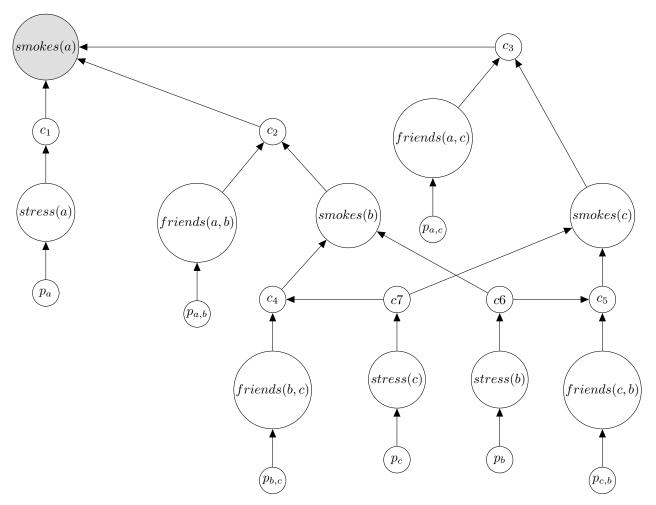


Figure 2: Bayesian network representing the ground acyclic program.

SRL to PGM

PGM to CNF

Weighted Model Counting

Lifted Inference

Parameter Learning