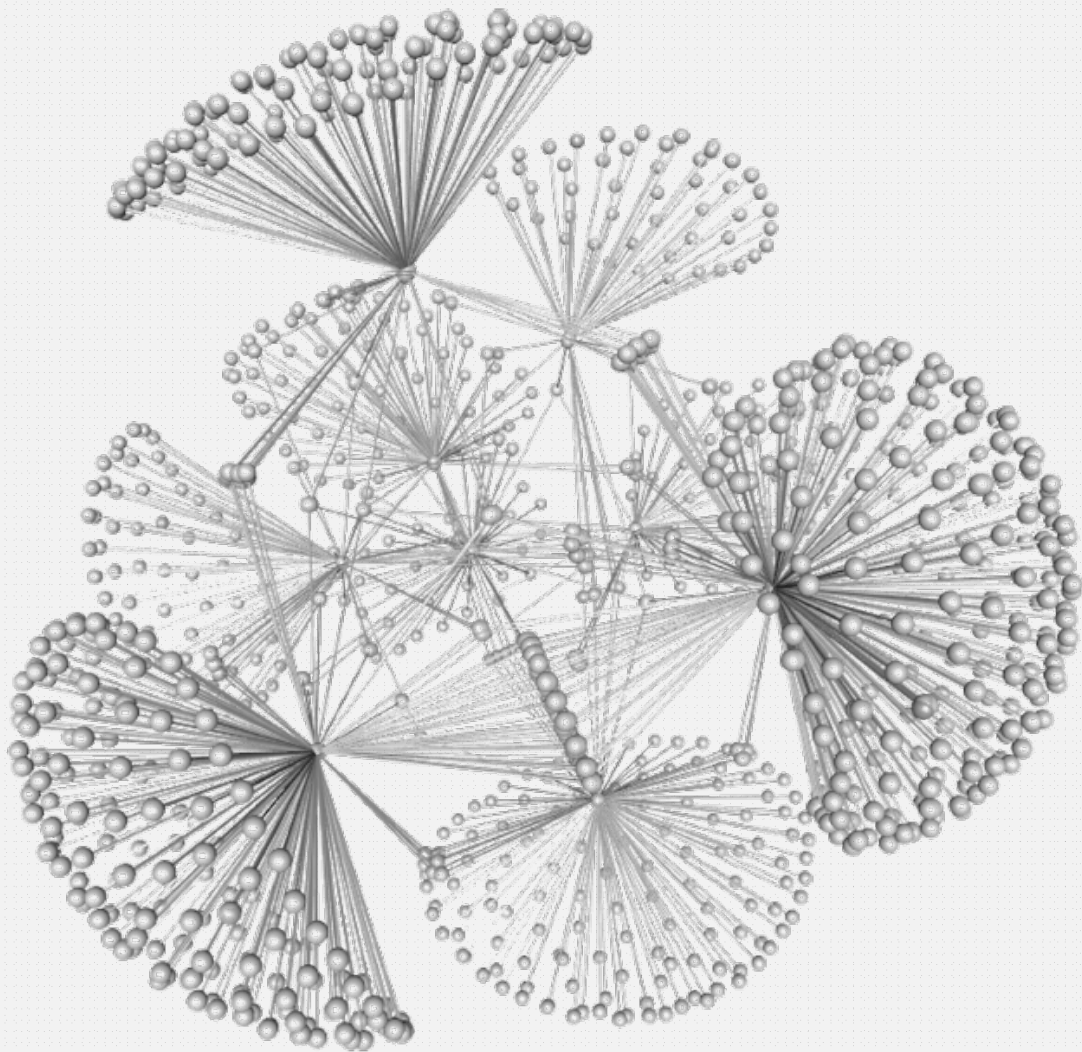


Probabilistic Programming

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INTELLIGENCE

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Below's our solution for the given challenges. The questions in each section of the original assignment are answered in a section having the same title.

```
1 person(a).
2 person(b).
3 person(c).
4 0.2::stress(X) :- person(X).
5 0.1::friends(X,Y) :- person(X), person(Y).
6 0.3::smokes(X) :- stress(X).
7 0.4::smokes(X) :- friends(X,Y), smokes(Y).
8 query(smokes(a)).
```

Code snippet 1: PROLOG program used throughout the first two chapters of the report.

Probabilistic Inference Using Weighted Model Counting

SRL to CNF

First the program is grounded. This is a matter of collecting all atoms involved in all proofs of the query.

```
1 0.2::stress(a).
2 0.2::stress(b).
3 0.2::stress(c).
4
5 0.1::friends(a,a).
6 0.1::friends(a,b).
7 0.1::friends(a,c).
8
9 0.1::friends(b,a).
10 0.1::friends(b,b).
11 0.1::friends(b,c).
12
13 0.1::friends(c,a).
14 0.1::friends(c,b).
15 0.1::friends(c,c).
16
17 0.3::smokes(a) :- stress(a).
18 0.3::smokes(b) :- stress(b).
19 0.3::smokes(c) :- stress(c).
```

```
20
21 0.4::smokes(a) :- friends(a,a), smokes(a).
22 0.4::smokes(a) :- friends(a,b), smokes(b).
23 0.4::smokes(a) :- friends(a,c), smokes(c).
24 0.4::smokes(b) :- friends(b,a), smokes(a).
25 0.4::smokes(b) :- friends(b,b), smokes(b).
26 0.4::smokes(b) :- friends(b,c), smokes(c).
27
28 0.4::smokes(c) :- friends(c,a), smokes(a).
29 0.4::smokes(c) :- friends(c,b), smokes(b).
30 0.4::smokes(c) :- friends(c,c), smokes(c).
```

Code snippet 2: Relevant ground program.

The proofs of the query make for a trie as shown in figure 1, where colourings indicate the presence of cycles. Any proof involving an atom `friends(X,X)` or `friends(Y,a)` (with $Y \in \{b,c\}$) is non-minimal and doesn't affect the final probability. These atoms are disregarded. For the remaining cycles (involving `friends(b,c)` and `friends(c,b)`) auxiliary variables can be used to obtain a cycle-free program :

```
1 0.2::stress(a).
2 0.2::stress(b).
3 0.2::stress(c).
4
```

```

5  0.1::friends(a,b).
6  0.1::friends(a,c).
7  0.1::friends(b,c).
8  0.1::friends(c,b).
9
10 0.3::p(a).
11 0.3::p(b).
12 0.3::p(c).
13
14 0.4::p(a,b).
15 0.4::p(a,c).
16 0.4::p(b,c).
17 0.4::p(c,b).
18
19 smokes(a) :- stress(a), p(a).
20 smokes(b) :- stress(b), p(b).
21 smokes(c) :- stress(c), p(c).
22
23 smokes(a) :-
24     friends(a,b), smokes(b), p(a,b).
25 smokes(a) :-
26     friends(a,c), smokes(c), p(a,c).
27 smokes(b) :-
28     friends(b,c), stress(c), p(c), p(b,c).
29 smokes(c) :-
30     friends(c,b), stress(b), p(b), p(c,b).
31
32 query(smokes(a)).

```

$\wedge (\neg p(c) \vee stress(c))$
 $\wedge (\neg stress(c) \vee p(c))$

The probabilistic literals CNF are assigned weights (derived literals have a weight of 1) :

Atom	Weight
stress(a)	0.2
$\neg stress(a)$	0.8
stress(b)	0.2
$\neg stress(b)$	0.8
stress(c)	0.2
$\neg stress(c)$	0.8
friends(a,b)	0.1
$\neg friends(a,b)$	0.9
friends(a,c)	0.1
$\neg friends(a,c)$	0.9
friends(b,c)	0.1
$\neg friends(b,c)$	0.9
friends(c,b)	0.1
$\neg friends(c,b)$	0.9

SRL to PGM

PGM to CNF

Weighted Model Counting

Lifted Inference

Parameter Learning

Code snippet 3: Relevant ground program without cycles.

The above logic program is equivalent to the following propositional formula :

$$\begin{aligned}
 smokes(a) &\leftrightarrow stress(a) \\
 &\quad \vee (friends(a,b) \wedge smokes(b)) \\
 &\quad \vee (friends(a,c) \wedge smokes(c)) \\
 \wedge (smokes(b) &\leftrightarrow p(b) \vee (friends(b,c) \wedge p(c))) \\
 \wedge (smokes(c) &\leftrightarrow p(c) \vee (friends(c,b) \wedge p(b))) \\
 \wedge (p(b) &\leftrightarrow stress(b)) \\
 \wedge (p(c) &\leftrightarrow stress(c))
 \end{aligned}$$

Which gives the following CNF :

$$\begin{aligned}
 &(\neg smokes(a) \vee stress(a) \vee friends(a,b) \vee friends(a,c)) \\
 &\wedge (\neg smokes(a) \vee stress(a) \vee friends(a,b) \vee smokes(c)) \\
 &\wedge (\neg smokes(a) \vee stress(a) \vee smokes(b) \vee friends(a,c)) \\
 &\wedge (\neg smokes(a) \vee stress(a) \vee smokes(b) \vee smokes(c)) \\
 &\wedge (\neg stress(a) \vee smokes(a)) \\
 &\wedge (\neg friends(a,b) \vee \neg smokes(b) \vee smokes(a)) \\
 &\wedge (\neg friends(a,c) \vee \neg smokes(c) \vee smokes(a)) \\
 &\wedge (\neg smokes(b) \vee p(b) \vee friends(b,c)) \\
 &\wedge (\neg smokes(b) \vee p(b) \vee p(c)) \\
 &\wedge (\neg p(b) \vee smokes(b)) \\
 &\wedge (\neg friends(b,c) \vee \neg p(c) \vee smokes(b)) \\
 &\wedge (\neg smokes(c) \vee p(c) \vee friends(c,b)) \\
 &\wedge (\neg smokes(c) \vee p(c) \vee p(b)) \\
 &\wedge (\neg p(c) \vee smokes(c)) \\
 &\wedge (\neg friends(c,b) \vee \neg p(b) \vee smokes(c)) \\
 &\wedge (\neg p(b) \vee stress(b)) \\
 &\wedge (\neg stress(b) \vee p(b))
 \end{aligned}$$

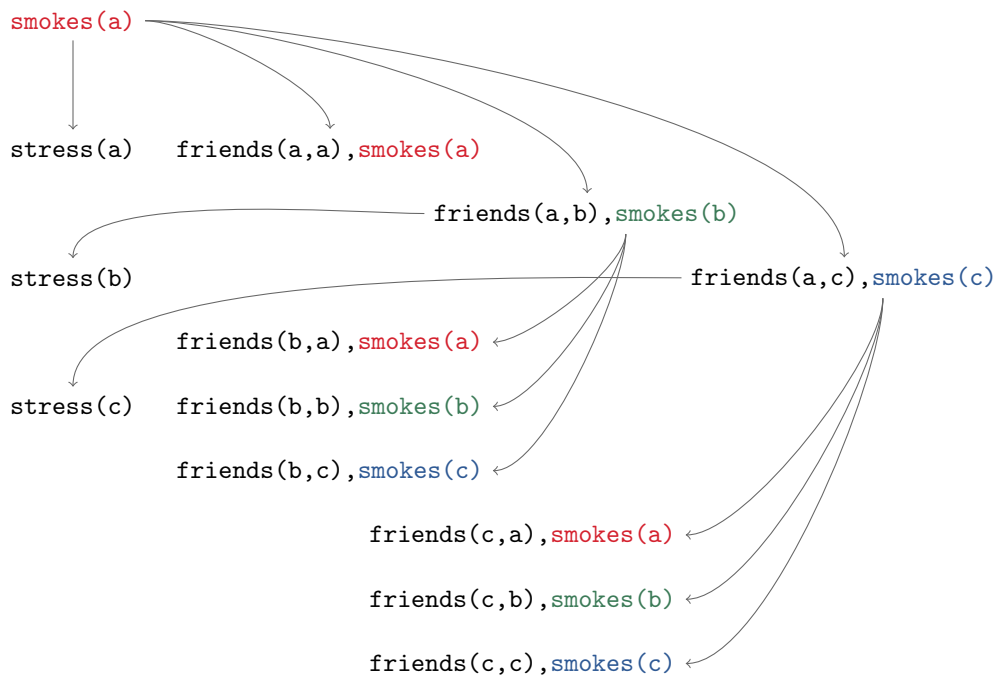


Figure 1: SLG-tree produced while turning the ground program into a boolean formula. Coloured atoms indicate the presence of cycles.