

Table 3: Benchmarks - Problems with correlated variables

LSF significance	Case No.	Limit State function(s)	Stochastic variable(s)	R_x	β	Ref
Beam deflection	(1)	$g(X) = 0.02 - 8 \frac{X_1}{X_2 X_3}$	$X_1 : LN(1000, 200)$ $X_2 : LN(2 \times 10^{10}, 1 \times 10^9)$ $X_3 : LN(3.9025 \times 10^{-5}, 3.9025 \times 10^{-6})$	$\begin{bmatrix} 1.0 & 0.2 & 0.2 \\ 0.2 & 1.0 & 0.2 \\ 0.2 & 0.2 & 1.0 \end{bmatrix}$	4.0	[1]
R x S	(2)	$g(X) = x_1 - x_2$	$X_1 : N(150, 20)$ $X_2 : N(120, 25)$	$\begin{bmatrix} 1.0 & 0.75 \\ 0.75 & 1.0 \end{bmatrix}$	1.809	[2]
Moment in beam	(3)	$g(X) = x_1 x_2 - x_3$	$X_1 : N(40, 5)$ $X_2 : N(50, 2.5)$ $X_3 : N(1000, 200)$	$\begin{bmatrix} 1.0 & 0.4 & 0.0 \\ 0.4 & 1.0 & 0.0 \\ 0.0 & 0.0 & 1.0 \end{bmatrix}$	2.862	[3]
Moment in beam	(4)	$g(X) = x_1 x_2 - x_3$	$X_1 : LN(40, 5)$ $X_2 : LN(50, 2.5)$ $X_3 : G(1000, 200)$	$\begin{bmatrix} 1.0 & 0.4 & 0.0 \\ 0.4 & 1.0 & 0.0 \\ 0.0 & 0.0 & 1.0 \end{bmatrix}$	2.658	[3]

References

- [1] RASHKI, M. Hybrid control variates-based simulation method for structural reliability analysis of some problems with low failure probability. *Appl. Math. Model.*, v. 60, p. 220–234, 2018.
- [2] ANG, A. H.-S.; TANG, W. H. *Probability Concepts in Engineering: Emphasis on Applications in Civil and Environmental Engineering*. 2. ed. New York: Wiley, 2007.
- [3] ANG, A. H.-S.; TANG, W. H. *Probability Concepts in Engineering Planning and Design. Volume II: Decision, Risk and Reliability*. New York: John Wiley & Sons, 1984.