Doors

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Abstract. In this paper we describe and explore a simple restraint logic programming solution for the logic problem *Doors*.

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1 Examples

2 Problem Description

The logic problem *Doors* is a puzzle on a rectangular board whose cells are either empty or contain natural numbers. The board is thought of like a *house*. Each cell is a *room*, and two adjacent cells are separated by a *wall* with one *door*. That door may be either open or closed. If it is open, then the cell can see its adjacent room through the doorway. A man standing in a room can look in all four directions — north, east, west, south — and count the number of *visible rooms*.

The puzzle consists in discovering an assignment of open and closed doors to the walls of the board such that the natural number in each non-empty cell is how many rooms are visible from that cell (including itself). There may be multiple solutions, or none at all.

3 Representation

A puzzle of size $n \times m$ is represented internally by three matrices (list of lists): Board, of size $n \times m$, holding the cell numbers; Vertical, of size $n \times (m-1)$, holding the vertical walls; and Horizontal, of size $(n-1) \times m$, holding the horizontal walls.

For each cell $(R,C), R=1,2,\cdots,n, C=1,2,\cdots,m$, indices in Board, the left wall has index (R,C-1) in Vertical, the right wall has index (R,C) in Vertical, the top wall has index (R-1,C) in Horizontal, the bottom wall has index (R,C) in Horizontal. Each wall in the board is assigned the number 0 for closed door and 1 for open door.

4 Restrictions

When solving a puzzle Board is fully instantiated, while Vertical and Horizontal contain domain variables (domain $\{0,1\}$). Empty cells in the Board are represented by a 0, as it is never a valid visible room counter.

Consider the puzzle above. The horizontal range A-G consists of 7 rooms and 6 vertical doors: let $\{b, c, d, e, f, g\}$ be these vertical doors, from left to right.

Focus on room A. If b=0 then A sees no rooms to its right. If b=1 and c=0 then A sees only room B. A general formula can be deduced by noticing that closed doors behave as zero elements.

Let e_A be the total number of rooms A sees to its right (east), then

$$e_A = b + b(c + c(d + d(e + e(f + f(g + g \cdot 0)))))$$
(1)

Now, if we analogously define w_A for west, n_A for north and s_A for south, then we find that the number in cell A must be $e_A + w_A + n_A + s_A + 1$.

Implementing these restrictions in PROLOG is surprisingly simple. We start with a predicate to compute formula (1):

```
calculate_value([], 0).
calculate_value([H|T], V) :-
    calculate_value(T, V1),
    V #= H + H*V1.
```

Then, for each non-zero cell (R, C) on the Board, we retrieve as a list the four ranges of doors to the right, left, top and bottom of (R, C), apply the formula for each list, and finally the restriction:

```
restrict_cell(Board, _, _, [R,C]) :-
    matrixnth1([R,C], Board, 0), !. % empty cell
restrict_cell(Board, Vertical, Horizontal, [R,C]) :-
    matrixnth1([R,C], Board, Value),
    right_total(Vertical, [R,C], Right),
    left_total(Vertical, [R,C], Left),
    top_total(Horizontal, [R,C], Top),
    bot_total(Horizontal, [R,C], Bot),
    Right + Left + Top + Bot + 1 #= Value.
```

References

- 1. Author, F.: Article title. Journal $\mathbf{2}(5)$, 99–110 (2016)
- 2. Author, F., Author, S.: Title of a proceedings paper. In: Editor, F., Editor, S. (eds.) CONFERENCE 2016, LNCS, vol. 9999, pp. 1–13. Springer, Heidelberg (2016). https://doi.org/10.10007/1234567890
- 3. Author, F., Author, S., Author, T.: Book title. 2nd edn. Publisher, Location (1999)
- 4. Author, A.-B.: Contribution title. In: 9th International Proceedings on Proceedings, pp. 1–2. Publisher, Location (2010)
- $5.\ \ LNCS\ Homepage,\ http://www.springer.com/lncs.\ Last\ accessed\ 4\ Oct\ 2017$