### Doors

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**Abstract.** In this paper we describe and explore a simple solution for the logic problem *Doors*.

In this paper we present a simple restraint logic programming solution to this puzzle.

Keywords: doors logic puzzle rooms

### 1 Examples

# 2 Problem Description

The logic problem *Doors* is a puzzle on a rectangular board whose cells are either empty or contain natural numbers. The board is thought of like a *house*. Each cell is a *room*, and two adjacent cells are separated by a *wall* with one *door*. That door may be either open or closed. If it is open, then the cell can see its adjacent room through the doorway. A man standing in a room can look in all four directions — north, east, west, south — and count the number of *visible rooms* 

The puzzle consists in discovering an assignment of open and closed doors to the walls of the board such that the natural number in each non-empty cell is how many rooms are visible from that cell (including itself). There may be multiple solutions, or none at all.

#### 3 Representation

A puzzle of size  $n \times m$  is represented internally by three matrices (list of lists): Board, of size  $n \times m$ , holding the cell numbers; Vertical, of size  $n \times (m-1)$ , holding the vertical walls; and Horizontal, of size  $(n-1) \times m$ , holding the horizontal walls.

For each cell  $(R,C), R=1,2,\cdots,n, C=1,2,\cdots,m$ , indices in Board, the left wall has index (R,C-1) in Vertical, the right wall has index (R,C) in Vertical, the top wall has index (R-1,C) in Horizontal, the bottom wall has index (R,C) in Horizontal. Each wall in the board is assigned the number 0 for closed door and 1 for open door.

#### 4 Restrictions

When solving a puzzle Board is fully instantiated, while Vertical and Horizontal contain domain variables (domain  $\{0,1\}$ ). Empty cells in the Board are represented by a 0, as it is never a valid visible room counter.

Consider the puzzle above. The horizontal range A-G consists of 7 rooms and 6 vertical doors: let  $\{b, c, d, e, f, g\}$  be these vertical doors, from left to right.

Focus on room A. If b=0 then A sees no rooms to its right. If b=1 and c=0 then A sees only room B. A general formula can be deduced by noticing that closed doors behave as zero elements.

Let  $e_A$  be the total number of rooms A sees to its right (east), then

$$e_A = b + b(c + c(d + d(e + e(f + f(g + g \cdot 0)))))$$
(1)

Now, if we analogously define  $w_A$  for west,  $n_A$  for north and  $s_A$  for south, then we find that the number in cell A must be  $e_A + w_A + n_A + s_A + 1$ .

Implementing these restrictions in PROLOG is surprisingly simple. We start with a predicate to compute formula (1):

```
calculate_value([], 0).
calculate_value([H|T], V) :-
    calculate_value(T, V1),
    V #= H + H*V1.
```

Then, for each non-zero cell (R, C) on the Board, we retrieve as a list the four ranges of doors to the right, left, top and bottom of (R, C), apply the formula for each list, and finally the restriction:

```
restrict_cell(Board, _, _, [R,C]) :-
    matrixnth1([R,C], Board, 0), !. % empty cell
restrict_cell(Board, Vertical, Horizontal, [R,C]) :-
    matrixnth1([R,C], Board, Value),
    right_total(Vertical, [R,C], Right),
    left_total(Vertical, [R,C], Left),
    top_total(Horizontal, [R,C], Top),
    bot_total(Horizontal, [R,C], Bot),
    Right + Left + Top + Bot + 1 #= Value.
```

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