

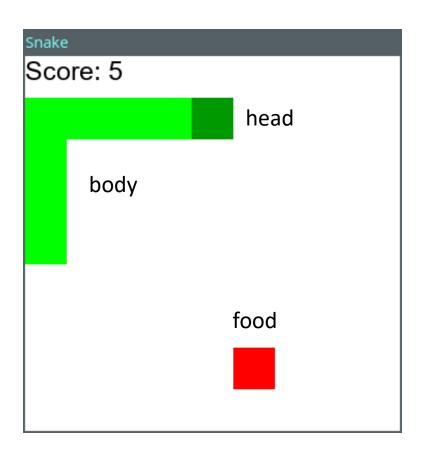
Reinforcement Learning Snake

- Simone Brusatin
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- github.com/Brusa99/Snake_RL

What is Snake?

- Snake is a 1977 video game.
- The player maneuvers the end of a growing line, often themed as a snake.
- The objective is to grow as much as possible by eating food.
- While maneuvering the player has to avoid obstacles, such as the walls and the body of the snake. Hitting the obstacles results in game over.

How I represent it



- You can play the game by running: python Game.py
- You can move in 4 directions using the arrow keys. The head will move and the body will trail on.
- If the head reaches the food, the snake will become one block longer and you will increase your score.
- The objective of the game is to score as high as possible.

Model of the environment

- The playground is a matrix of size self.w * self.h
- Current direction, score, head and food position, and rest of the body position are class attributes.
- Walls are not modeled: head position outside of boundaries is considered as a collision.

Reinforcement Learning Framework

Action Space

4 absolute actions

- Up
- Down
- Left
- Right



3 relative actions

- Turn Left
- Straight
- Turn Right

All actions are deterministic.

Relative action

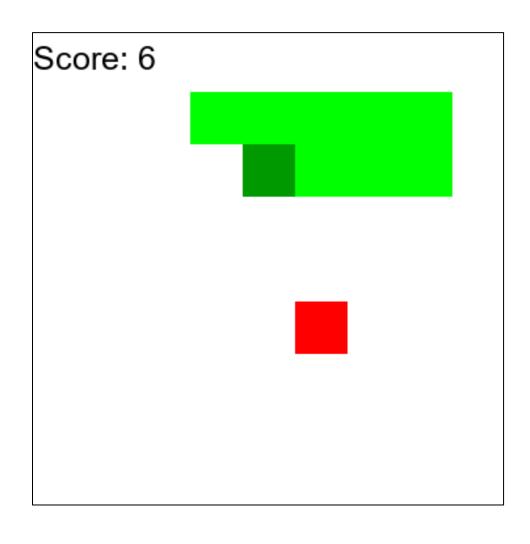
- In this way the action space has a lower cardinality, which reduces model complexity.
- Effectiveness of the model is equivalent: going backwards always results in game over.
- The agent must know current direction.

State Space

- 3 Boolean attributes that signal an immediate collision for each relative direction
- 4 Boolean attributes for each direction
- 4 Boolean attributes for food position:
 - food.x < head.x</pre>
 - food.x > head.x
 - food.y < head.y</pre>
 - food.y > head.y

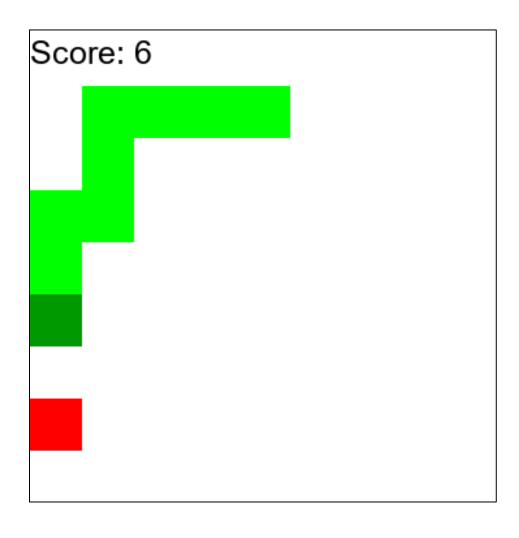
^{*}Note that this isn't the only option. Different state spaces will be discussed later.

Example



- 0 danger left
- 0 danger straight
- 1 danger right
- 1 direction left
- 0 direction right
- 0 direction up
- 0 direction down
- 0 food left
- 1 food right
- 0 food up
- 1 food down

Example



- 0 danger left
- 0 danger straight
- 1 danger right
- 0 direction left
- 0 direction right
- 0 direction up
- 1 direction down
- 0 food left
- 0 food right
- 0 food up
- 1 food down

State Space Dimension

- We have 11 variables.
- All variables are Boolean.
- We have a total of $2^{11} = 2048$ possible states.

$$S = D_l \times D_s \times D_r \times L \times R \times U \times D \times Fx_< \times Fx_> \times Fy_< \times Fy_>$$
danger direction food position

But...

- The Boolean variables are sub-optimal: not all tuples are valid states.
- For example it is not possible that both direction up and direction down are 1.
- A better state space would be:

$$S = D_l \times D_s \times D_r \times Dir \times F_x \times F_y$$

$$\begin{cases} \text{up} & < < \\ \text{down} \\ \text{left} & > \end{cases} \begin{cases} < \\ = \\ > \end{cases}$$

• Which would give us a total of $2^4 * 4 * 3^2 = 576$ possible states.

Rewards

- +15 for eating the food
- -10 for colliding
- -10 if the game goes on for too long (MAX_ITER * len(snake))
- -0.1 else*

*this is designed to avoid the loop bottleneck: In a vast playground the chance of randomly stumble into the food is very low. So, the agent may adopt "don't die" as a policy, which is guaranteed in a loop.

Solving the problem

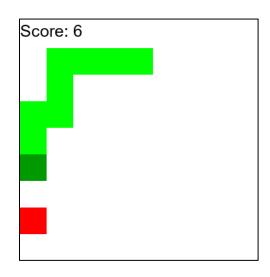
Model based or model free?

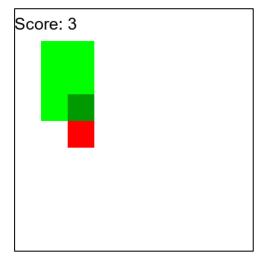
- We have no prior knowledge on the transition probability p(s'|s,a)
- We have limited knowledge on the expected immediate reward r(s, a).

Example: The figures on the right are interpreted as the same state.

Taking action Straight will lead to a reward of 0 in the left game configuration and of +15 in the right configuration.

Taking action Turn right will lead to a reward of -10 (and game over) in the first case, while in the second case it will produce a reward of -0.01.





We will opt for a model free approach

• In a model free context, we know N sequences obtained by the agent by interacting with the environment:

$$S_0^n, A_0^n, R_1^n, S_1^n, A_1^n, R_2^n, \dots \text{ with } n = 1, \dots, N$$

• We will use TD-Learning to estimate the state-action value:

$$Q^{\pi}(s,a) = \mathbb{E}_{\pi}ig[R_t|s_t=s,a_t=aig]$$

Value of states

• We can get the value of the states from the action-value. Since

$$Q_{\pi}(s, a) = \mathbb{E}\left[\sum_{t=0}^{\infty} \gamma^{t} R_{t+1} | S_{0} = s, A_{0} = a\right]$$

$$= \sum_{s'} P(s'|s, a) \left[r(s, a, s') + \gamma \sum_{a'} \pi(a'|s) Q_{\pi}(s', a')\right]$$

$$= \sum_{s'} P(s'|s, a) \left[r(s, a, s') + \gamma V_{\pi}(s')\right]$$

• We obtain:

$$V_{\pi}(s) = \sum_{a'} \pi(a'|s) Q_{\pi}(s', a')$$

TD-Learning

- To estimate the state action values, we will use the TD-Learning algorithm.
- Other methods, such as Monte Carlo, can be used.

Algorithm 2 TD-Learning

Input Learning Rate $\alpha \in (0; 1]$, small $\epsilon > 0$

- 1: Initialize $\hat{Q}(s, a) \ \forall \ s \in S, \ a \in A$
- 2: **loop** for each episode:
- 3: Initialize s
- 4: **loop** Derive π from \hat{Q} (with $\epsilon greedy$)
- 5: Choose a from A
- 6: Take A, observe R, S'
- 7: Compute TD-error δ
- 8: Compute eligibility *e*
- 9: $Q \leftarrow Q + +\alpha \delta e$
- 10: $S \leftarrow S'$

- For eligibility we will use $1(S_t = s, A_t = a)$
- To calculate the TD-error we will try different algorithms, for example SARSA:

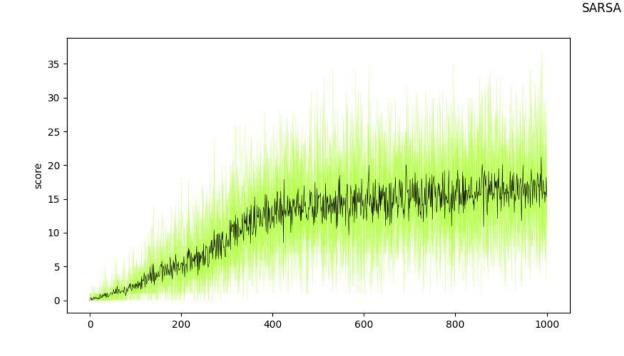
$$\delta = R + \gamma \hat{Q}(S', A') - \hat{Q}(S, A)$$

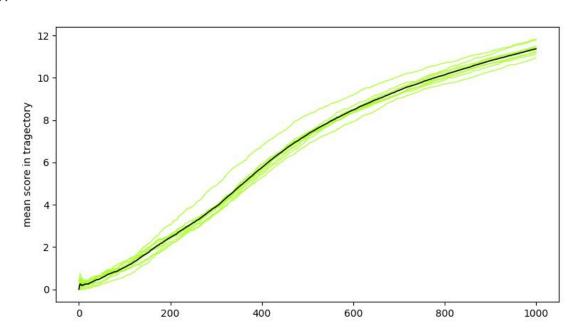
We will follow an ε-greedy policy, that means that we will take the action which we estimate has the most value with probability 1-ε otherwise we will take an action at random. This permits exploration.

Results

Training the model

- We trained the model on a 9 * 9 board.
- At around 400 games, the agent stops to learn
- We repeated the learning process 10 times.





Other algorithms

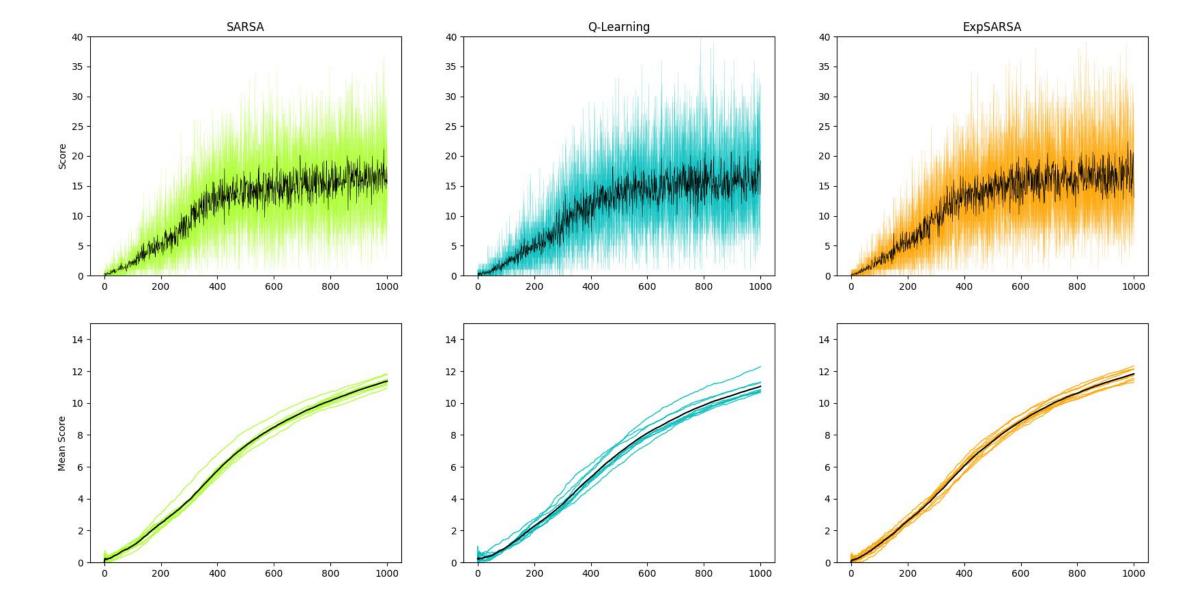
- We can try to use different TD-errors for the algorithm, for example:
- Q-Learning:

$$Q(S_t, A_t) \leftarrow Q(S_t, A_t) + \alpha \left[R_{t+1} + \gamma \max_{a} Q(S_{t+1}, a) - Q(S_t, A_t) \right]$$

Expected SARSA:

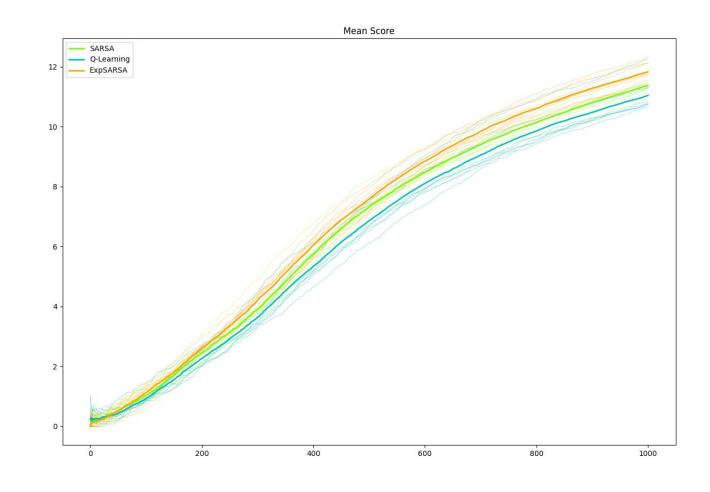
$$Q(S_t, A_t) \leftarrow Q(S_t, A_t) + \alpha \left[R_{t+1} + \gamma \mathbb{E}_{\pi} [Q(S_{t+1}, A_{t+1}) \mid S_{t+1}] - Q(S_t, A_t) \right]$$

$$\leftarrow Q(S_t, A_t) + \alpha \left[R_{t+1} + \gamma \sum_{a} \pi(a \mid S_{t+1}) Q(S_{t+1}, a) - Q(S_t, A_t) \right]$$



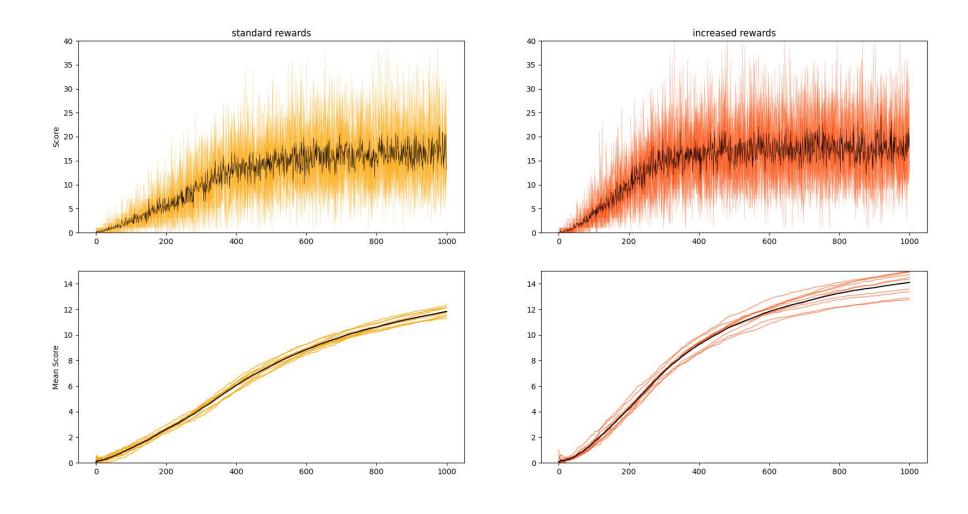
Comparing the algorithms

- We are looking at the average score of the models.
- The idea is that the faster it grows, the sooner the model has learned the optimal policy.
- The fastest model uses the expected SARSA algorithm.

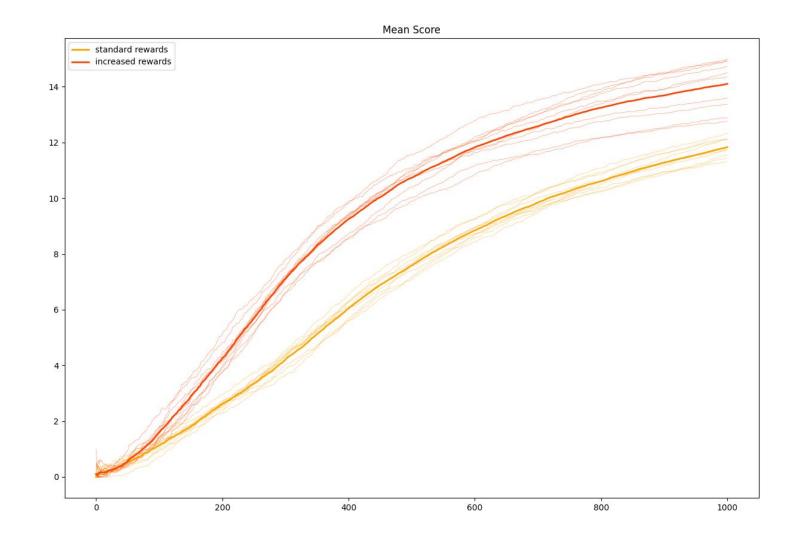


Changing parameters

Increased rewards



- We increased the positive of eating food from 15 to 150.
- The algorithm converges faster but it has more variance.
- This is due to the rewards being sparse.



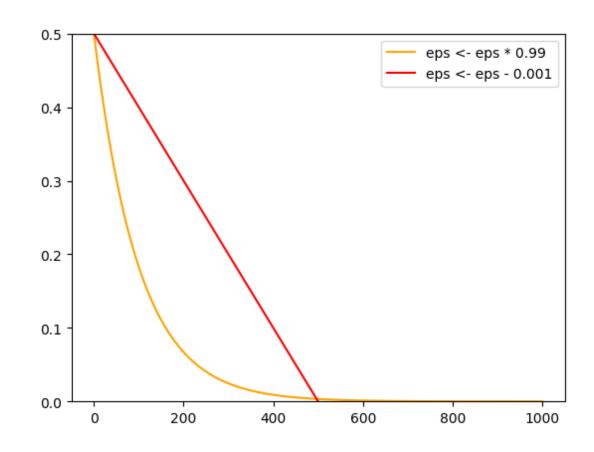
Change how ε decreases.

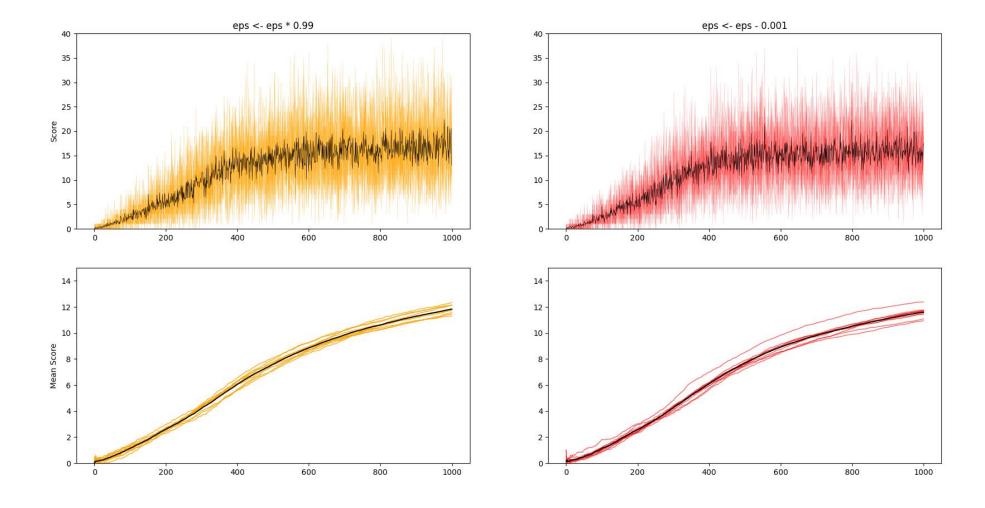
• In the previous models, to update ε , we used the rule:

$$\epsilon_t = 0.99 \; \epsilon_{t-1}$$

 We tried instead a linear decrease:

$$\epsilon_t = \epsilon_{t-1} - 0.01$$



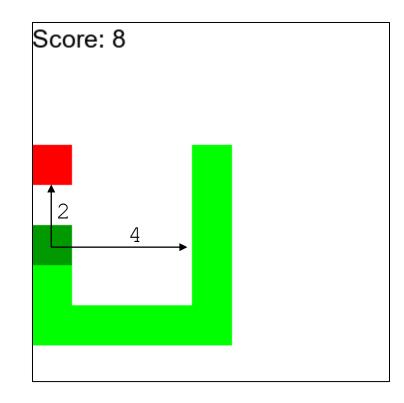


• It doesn't have any effect

How could it improve

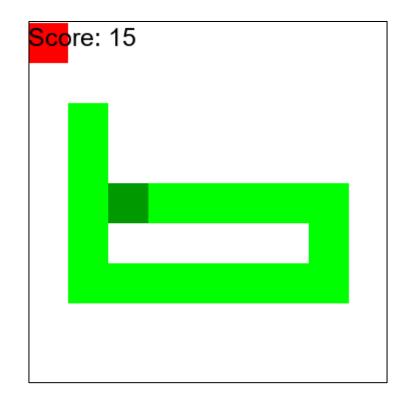
Different state space configurations

- Instead of signaling danger only in three directions, we can also signal the corners.
- Instead of a Boolean we could use distances.
- We could use binning to limit computational complexity increase.



The problem

- From the picture we can see that if the snakes turns left he will become stuck by his own body.
- The snake isn't aware of his body movement, due to how the game is represented through states.
- Getting stuck is the only way to lose if playing with the optimal policy.

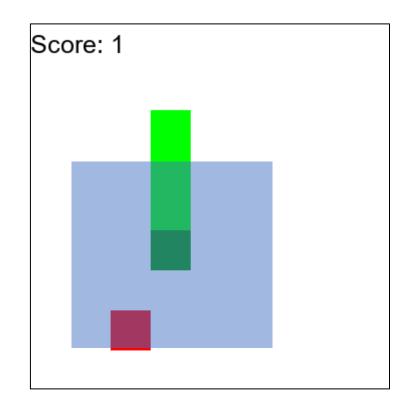


Solution?

- We could change our state space.
- We can make the state space a vector representing each cell of the playground, with different values representing empty, blocked, head, food.
- This will lead to a total of 4^{w*h} possible states. Which is computationally unfeasable.
- For example, for a 9*9 board, there will be in the order of 10^{48} states.
- Moreover, the learned policy won't work on different sized playgrounds.

Slight improvements

- Instead of giving the whole board we can only give a limited area around the snake head.
- Still computationally expensive but better.
- State no longer depend on playground size.
- Doesn't solve the problem at its core.



Trivial Solution: Space filling curves

- Compute a curve that fills the square.
- Make the snake follow the curve in a loop.
- No actual learning.

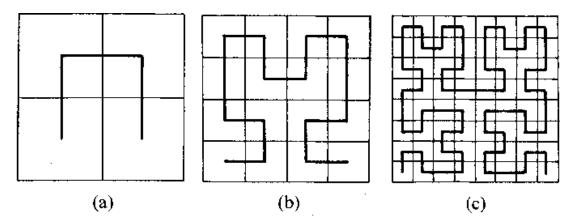


Fig. 1. Hilbert's geometric construction of a space-filling curve.

The End