Adding and Subtracting Radical Expressions

Summary

1. We can add or subtract like radicals just as we can add or subtract like terms.

Just like we can add 2x + 3x to get 5x, we can also add like radical expressions together.

Like Radicals

Radicals with the same root and the same radicand.

Like Radicals	Not Like Radicals
$2\sqrt{7} + 3\sqrt{7}$	$2\sqrt{7} + 3\sqrt[3]{7}$ (Different roots)
$5\sqrt[3]{10} - 9\sqrt[3]{10}$	$8\sqrt{10} - 3\sqrt{6}$ (Different radicands)

Example 1. Add or subtract each. Assume all variables represent positive real numbers.

(a)
$$4\sqrt{11} + 8\sqrt{11}$$

(b)
$$5\sqrt[3]{3x} - 7\sqrt[3]{3x}$$

(c)
$$4\sqrt{5} + 4\sqrt[3]{5}$$

Sometimes you have to simplify before you can combine like radicals.

Example 2. Add or subtract each. Assume all variables represent positive real numbers.

(a)
$$\sqrt{20} + 2\sqrt{45}$$

(b)
$$\sqrt[3]{54} - 5\sqrt[3]{16} + \sqrt[3]{2}$$

(c)
$$\sqrt{27x} - 2\sqrt{9x} + \sqrt{72x}$$

(d)
$$\sqrt[3]{48x^4} + \sqrt[3]{6x^4}$$