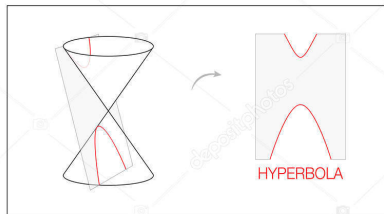
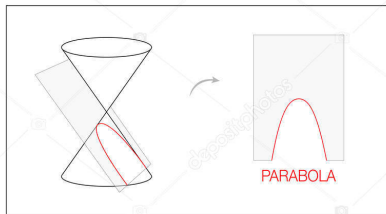
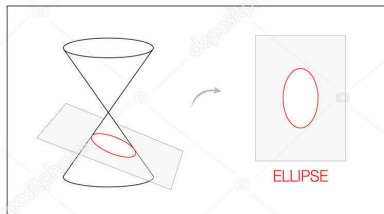
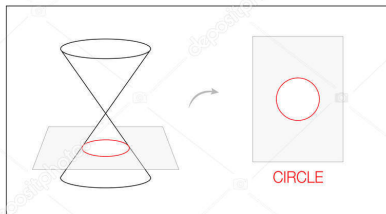


Ellipses



Objectives

- 1 Identify the center, vertices, and foci of an ellipse.
- 2 Write the equation of an ellipse in standard form.
- 3 Write the equation of an ellipse given information about it

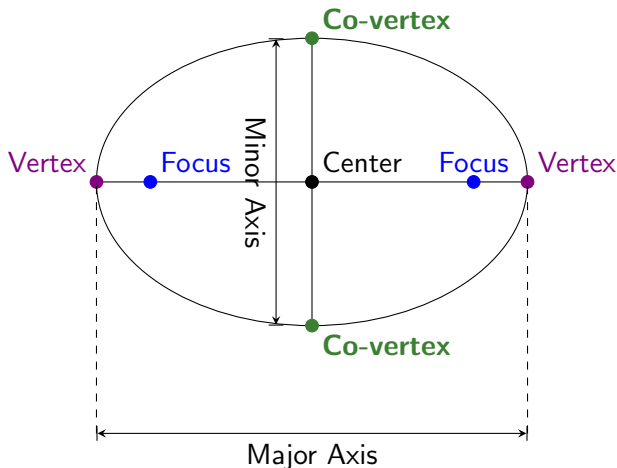
Ellipses

Ellipses

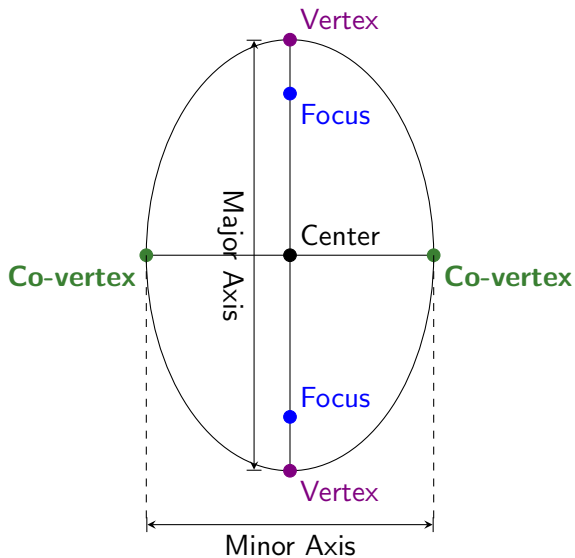
The set of points such that the **sum** of their distances from 2 fixed points (called **foci**) is constant.

Appearance

Ellipses will typically either appear wider or taller based on their equation. Below are key parts of each type of ellipse:



Appearance



The *center* of an ellipse is denoted by (h, k) , just like with circles.

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Each focal point (*pl: foci*) is c units from the center. The foci are on the *major axis*.

Vocab

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Each vertex (*pl: vertices*) also lies on the major axis, and is a units away from the center.

Vocab

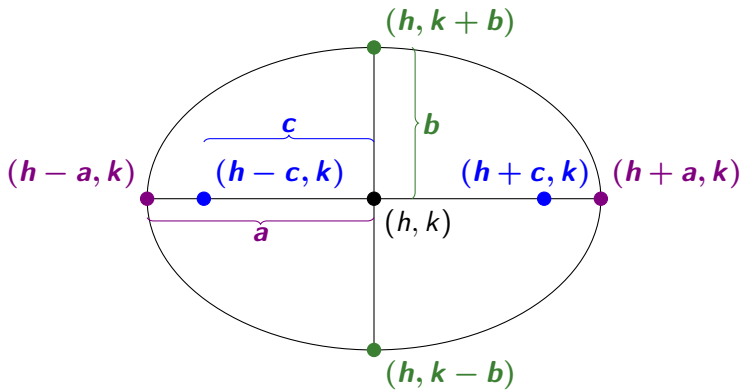
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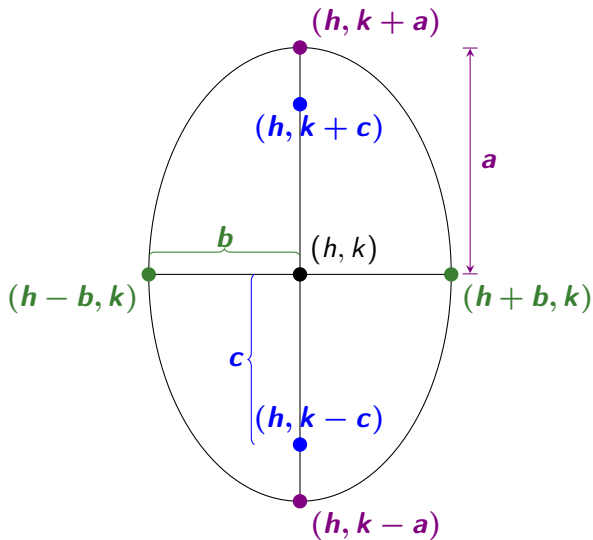
Each vertex (*pl: vertices*) also lies on the major axis, and is a units away from the center.

Each *co-vertex* (*pl: co-vertices*) lies on the *minor axis*, which is perpendicular to the major axis. The co-vertices are each b units away from the center.

$$\frac{(x - h)^2}{a^2} + \frac{(y - k)^2}{b^2} = 1$$



$$\frac{(y - k)^2}{a^2} + \frac{(x - h)^2}{b^2} = 1$$



Foci and a vs. b

Note: In both cases, $c^2 = a^2 - b^2$, and $a > b$.

Example 1

Identify the coordinates of the center, vertices, and foci for each.
Exact answers only.

(a) $\frac{x^2}{36} + \frac{y^2}{25} = 1$

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Center: $(0, 0)$

Vertices: $a^2 = 36$

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$$(a) \quad \frac{x^2}{36} + \frac{y^2}{25} = 1$$

Center: $(0, 0)$

Vertices: $a^2 = 36 \rightarrow a = \pm 6$

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Identify the coordinates of the center, vertices, and foci for each.
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Center: $(0, 0)$

Vertices: $a^2 = 36 \longrightarrow a = \pm 6$

Vertices at $(0 \pm 6, 0)$

Example 1

Identify the coordinates of the center, vertices, and foci for each.
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Vertices at $(0 \pm 6, 0)$

Vertices $(\pm 6, 0)$

Example 1a $\frac{x^2}{36} + \frac{y^2}{25} = 1$

Foci:

$$c^2 = a^2 - b^2$$

Example 1a

$$\frac{x^2}{36} + \frac{y^2}{25} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 36 - 25$$

Example 1a

$$\frac{x^2}{36} + \frac{y^2}{25} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 36 - 25$$

$$c^2 = 11$$

Example 1a

$$\frac{x^2}{36} + \frac{y^2}{25} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 36 - 25$$

$$c^2 = 11$$

$$c = \pm\sqrt{11}$$

Example 1a

$$\frac{x^2}{36} + \frac{y^2}{25} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 36 - 25$$

$$c^2 = 11$$

$$c = \pm\sqrt{11}$$

Foci at $(0 \pm \sqrt{11}, 0)$

Example 1a $\frac{x^2}{36} + \frac{y^2}{25} = 1$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 36 - 25$$

$$c^2 = 11$$

$$c = \pm\sqrt{11}$$

Foci at $(0 \pm \sqrt{11}, 0) \longrightarrow (\pm\sqrt{11}, 0)$

Example 1

$$(b) \quad \frac{y^2}{16} + \frac{x^2}{1} = 1$$

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Center: $(0, 0)$

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Center: $(0, 0)$

Vertices: $a^2 = 16$

Example 1

$$(b) \quad \frac{y^2}{16} + \frac{x^2}{1} = 1$$

Center: $(0, 0)$

Vertices: $a^2 = 16 \longrightarrow a = \pm 4$

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$$(b) \quad \frac{y^2}{16} + \frac{x^2}{1} = 1$$

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Vertices: $a^2 = 16 \longrightarrow a = \pm 4$

Vertices at $(0, 0 \pm 4)$

Example 1

$$(b) \quad \frac{y^2}{16} + \frac{x^2}{1} = 1$$

Center: $(0, 0)$

Vertices: $a^2 = 16 \longrightarrow a = \pm 4$

Vertices at $(0, 0 \pm 4)$

Vertices $(0, \pm 4)$

Example 1b

$$\frac{y^2}{16} + \frac{x^2}{1} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

Example 1b

$$\frac{y^2}{16} + \frac{x^2}{1} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 16 - 1$$

Example 1b

$$\frac{y^2}{16} + \frac{x^2}{1} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 16 - 1$$

$$c^2 = 15$$

Example 1b

$$\frac{y^2}{16} + \frac{x^2}{1} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 16 - 1$$

$$c^2 = 15$$

$$c = \pm\sqrt{15}$$

Example 1b

$$\frac{y^2}{16} + \frac{x^2}{1} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 16 - 1$$

$$c^2 = 15$$

$$c = \pm\sqrt{15}$$

Foci at $(0, 0 \pm \sqrt{15})$

Example 1b

$$\frac{y^2}{16} + \frac{x^2}{1} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 16 - 1$$

$$c^2 = 15$$

$$c = \pm\sqrt{15}$$

Foci at $(0, 0 \pm \sqrt{15}) \longrightarrow (0, \pm\sqrt{15})$

Example 1

$$(c) \quad \frac{(x+5)^2}{49} + \frac{(y-2)^2}{25} = 1$$

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Center: $(-5, 2)$

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Center: $(-5, 2)$

Vertices: $a^2 = 49 \longrightarrow a = \pm 7$

Example 1

$$(c) \quad \frac{(x+5)^2}{49} + \frac{(y-2)^2}{25} = 1$$

Center: $(-5, 2)$

Vertices: $a^2 = 49 \longrightarrow a = \pm 7$

Vertices at $(-5 \pm 7, 2)$

Example 1

$$(c) \quad \frac{(x+5)^2}{49} + \frac{(y-2)^2}{25} = 1$$

Center: $(-5, 2)$

Vertices: $a^2 = 49 \rightarrow a = \pm 7$

Vertices at $(-5 \pm 7, 2)$

Vertices $(-12, 2)$ and $(2, 2)$

Example 1c $\frac{(x+5)^2}{49} + \frac{(y-2)^2}{25} = 1$

Foci:

$$c^2 = a^2 - b^2$$

Example 1c

$$\frac{(x+5)^2}{49} + \frac{(y-2)^2}{25} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 49 - 25$$

Example 1c

$$\frac{(x+5)^2}{49} + \frac{(y-2)^2}{25} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 49 - 25$$

$$c^2 = 24$$

Example 1c

$$\frac{(x+5)^2}{49} + \frac{(y-2)^2}{25} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 49 - 25$$

$$c^2 = 24$$

$$c = \pm 2\sqrt{6}$$

Example 1c $\frac{(x+5)^2}{49} + \frac{(y-2)^2}{25} = 1$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 49 - 25$$

$$c^2 = 24$$

$$c = \pm 2\sqrt{6}$$

Foci at $(-5 \pm 2\sqrt{6}, 2)$

Example 1

$$(d) \quad (x - 2)^2 + \frac{(y + 1)^2}{36} = 1$$

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Center: $(2, -1)$

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Vertices at $(2, -1 \pm 6)$

Example 1

$$(d) \quad (x - 2)^2 + \frac{(y + 1)^2}{36} = 1$$

Center: $(2, -1)$

Vertices: $a^2 = 36 \longrightarrow a = \pm 6$

Vertices at $(2, -1 \pm 6)$

Vertices $(2, -7)$ and $(2, 5)$

Example 1d

$$\frac{(x-2)^2}{1} + \frac{(y+1)^2}{36} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

Example 1d

$$\frac{(x-2)^2}{1} + \frac{(y+1)^2}{36} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 36 - 1$$

Example 1d

$$\frac{(x-2)^2}{1} + \frac{(y+1)^2}{36} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 36 - 1$$

$$c^2 = 35$$

Example 1d

$$\frac{(x-2)^2}{1} + \frac{(y+1)^2}{36} = 1$$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 36 - 1$$

$$c^2 = 35$$

$$c = \pm\sqrt{35}$$

Example 1d $\frac{(x-2)^2}{1} + \frac{(y+1)^2}{36} = 1$

Foci:

$$c^2 = a^2 - b^2$$

$$c^2 = 36 - 1$$

$$c^2 = 35$$

$$c = \pm\sqrt{35}$$

Foci at $(2, -1 \pm \sqrt{35})$

Objectives

- 1 Identify the center, vertices, and foci of an ellipse.
- 2 Write the equation of an ellipse in standard form.
- 3 Write the equation of an ellipse given information about it

Converting From General to Standard Form

Just like circles may not be written in standard form, you may need to find the center and vertices to write an ellipse in standard form.

Converting From General to Standard Form

Just like circles may not be written in standard form, you may need to find the center and vertices to write an ellipse in standard form.

Luckily, the process is similar to that for circles.

Example 2

Write the standard form for the equation of an ellipse for each of the following.

(a) $9x^2 + 16y^2 - 144 = 0$

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(a) $9x^2 + 16y^2 - 144 = 0$

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$$9x^2 + 16y^2 = 144$$

$$\frac{9x^2}{144} + \frac{16y^2}{144} = 1$$

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(a) $9x^2 + 16y^2 - 144 = 0$

$$9x^2 + 16y^2 - 144 = 0$$

$$9x^2 + 16y^2 = 144$$

$$\frac{9x^2}{144} + \frac{16y^2}{144} = 1$$

$$\frac{x^2}{16} + \frac{y^2}{9} = 1$$

Example 2

$$(b) \quad 25x^2 + y^2 - 25 = 0$$

Example 2

$$(b) \quad 25x^2 + y^2 - 25 = 0$$

$$25x^2 + y^2 - 25 = 0$$

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$$25x^2 + y^2 - 25 = 0$$

$$25x^2 + y^2 = 25$$

Example 2

$$(b) \quad 25x^2 + y^2 - 25 = 0$$

$$25x^2 + y^2 - 25 = 0$$

$$25x^2 + y^2 = 25$$

$$\frac{25x^2}{25} + \frac{y^2}{25} = 1$$

Example 2

$$(b) \quad 25x^2 + y^2 - 25 = 0$$

$$25x^2 + y^2 - 25 = 0$$

$$25x^2 + y^2 = 25$$

$$\frac{25x^2}{25} + \frac{y^2}{25} = 1$$

$$x^2 + \frac{y^2}{25} = 1$$

Example 2

$$(c) \quad 9x^2 - 54x + 4y^2 - 8y + 49 = 0$$

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$$(c) \quad 9x^2 - 54x + 4y^2 - 8y + 49 = 0$$

$$9x^2 - 54x + 4y^2 - 8y = -49$$

Example 2

$$(c) \quad 9x^2 - 54x + 4y^2 - 8y + 49 = 0$$

$$9x^2 - 54x + 4y^2 - 8y = -49$$

Vertex: $(3, -81)$

Example 2

$$(c) \quad 9x^2 - 54x + 4y^2 - 8y + 49 = 0$$

$$9x^2 - 54x + 4y^2 - 8y = -49$$

Vertex: $(3, -81)$

Vertex: $(1, -4)$

Example 2

$$(c) \quad 9x^2 - 54x + 4y^2 - 8y + 49 = 0$$

$$9x^2 - 54x + 4y^2 - 8y = -49$$

Vertex: (3, -81)

Vertex: (1, -4)

$$9(x - 3)^2 + 4(y - 1)^2 = -49 + |-81| + |-4|$$

Example 2

$$(c) \quad 9x^2 - 54x + 4y^2 - 8y + 49 = 0$$

$$9x^2 - 54x + 4y^2 - 8y = -49$$

Vertex: (3, -81)

Vertex: (1, -4)

$$9(x - 3)^2 + 4(y - 1)^2 = -49 + |-81| + |-4|$$

$$9(x - 3)^2 + 4(y - 1)^2 = 36$$

Example 2

$$(c) \quad 9x^2 - 54x + 4y^2 - 8y + 49 = 0$$

$$9x^2 - 54x + 4y^2 - 8y = -49$$

Vertex: (3, -81)

Vertex: (1, -4)

$$9(x - 3)^2 + 4(y - 1)^2 = -49 + |-81| + |-4|$$

$$9(x - 3)^2 + 4(y - 1)^2 = 36$$

$$\frac{9(x - 3)^2}{36} + \frac{4(y - 1)^2}{36} = 1$$

Example 2c

$$\frac{9(x-3)^2}{36} + \frac{4(y-1)^2}{36} = 1$$

Example 2c

$$\frac{9(x-3)^2}{36} + \frac{4(y-1)^2}{36} = 1$$

$$\frac{(x-3)^2}{4} + \frac{(y-1)^2}{9} = 1$$

Example 2

$$(d) \quad x^2 + 6x + 9y^2 + 18y + 9 = 0$$

Example 2

$$(d) \quad x^2 + 6x + 9y^2 + 18y + 9 = 0$$

$$x^2 + 6x + 9y^2 + 18y = -9$$

Example 2

$$(d) \quad x^2 + 6x + 9y^2 + 18y + 9 = 0$$

$$x^2 + 6x + 9y^2 + 18y = -9$$

Vertex: $(-3, -9)$

Example 2

$$(d) \quad x^2 + 6x + 9y^2 + 18y + 9 = 0$$

$$x^2 + 6x + 9y^2 + 18y = -9$$

Vertex: $(-3, -9)$

Vertex: $(-1, -9)$

Example 2

$$(d) \quad x^2 + 6x + 9y^2 + 18y + 9 = 0$$

$$x^2 + 6x + 9y^2 + 18y = -9$$

Vertex: $(-3, -9)$

Vertex: $(-1, -9)$

$$(x + 3)^2 + 9(y + 1)^2 = -9 + |-9| + |-9|$$

Example 2

$$(d) \quad x^2 + 6x + 9y^2 + 18y + 9 = 0$$

$$x^2 + 6x + 9y^2 + 18y = -9$$

Vertex: $(-3, -9)$

Vertex: $(-1, -9)$

$$(x + 3)^2 + 9(y + 1)^2 = -9 + |-9| + |-9|$$

$$(x + 3)^2 + 9(y + 1)^2 = 9$$

Example 2

$$(d) \quad x^2 + 6x + 9y^2 + 18y + 9 = 0$$

$$x^2 + 6x + 9y^2 + 18y = -9$$

Vertex: $(-3, -9)$

Vertex: $(-1, -9)$

$$(x + 3)^2 + 9(y + 1)^2 = -9 + |-9| + |-9|$$

$$(x + 3)^2 + 9(y + 1)^2 = 9$$

$$\frac{(x + 3)^2}{9} + \frac{9(y - 1)^2}{9} = 1$$

Example 2d

$$\frac{(x+3)^2}{9} + \frac{9(y-1)^2}{9} = 1$$

Example 2d

$$\frac{(x+3)^2}{9} + \frac{9(y-1)^2}{9} = 1$$

$$\frac{(x+3)^2}{9} + (y-1)^2 = 1$$

Objectives

- 1 Identify the center, vertices, and foci of an ellipse.
- 2 Write the equation of an ellipse in standard form.
- 3 Write the equation of an ellipse given information about it

Example 3

- (a) Write the equation of an ellipse with
vertices at $(10, 0)$ and $(-4, 0)$, and foci at $(3 \pm 2\sqrt{6}, 0)$

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Center at $(3, 0)$

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(a) Write the equation of an ellipse with

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Center at $(3, 0)$

$$a = \pm 7$$

Example 3

(a) Write the equation of an ellipse with

vertices at $(10, 0)$ and $(-4, 0)$, and foci at $(3 \pm 2\sqrt{6}, 0)$

Center at $(3, 0)$

$$a = \pm 7 \longrightarrow a^2 = 49$$

Example 3

(a) Write the equation of an ellipse with

vertices at $(10, 0)$ and $(-4, 0)$, and foci at $(3 \pm 2\sqrt{6}, 0)$

Center at $(3, 0)$

$$a = \pm 7 \longrightarrow a^2 = 49$$

$$c = \pm 2\sqrt{6}$$

Example 3

(a) Write the equation of an ellipse with

vertices at $(10, 0)$ and $(-4, 0)$, and foci at $(3 \pm 2\sqrt{6}, 0)$

Center at $(3, 0)$

$$a = \pm 7 \longrightarrow a^2 = 49$$

$$c = \pm 2\sqrt{6} \longrightarrow c^2 = 24$$

Example 3

(a) Write the equation of an ellipse with

vertices at $(10, 0)$ and $(-4, 0)$, and foci at $(3 \pm 2\sqrt{6}, 0)$

Center at $(3, 0)$

$$a = \pm 7 \longrightarrow a^2 = 49$$

$$c = \pm 2\sqrt{6} \longrightarrow c^2 = 24$$

$$c^2 = a^2 - b^2$$

Example 3

(a) Write the equation of an ellipse with

vertices at $(10, 0)$ and $(-4, 0)$, and foci at $(3 \pm 2\sqrt{6}, 0)$

Center at $(3, 0)$

$$a = \pm 7 \longrightarrow a^2 = 49$$

$$c = \pm 2\sqrt{6} \longrightarrow c^2 = 24$$

$$c^2 = a^2 - b^2$$

$$24 = 49 - b^2$$

Example 3

(a) Write the equation of an ellipse with

vertices at $(10, 0)$ and $(-4, 0)$, and foci at $(3 \pm 2\sqrt{6}, 0)$

Center at $(3, 0)$

$$a = \pm 7 \longrightarrow a^2 = 49$$

$$c = \pm 2\sqrt{6} \longrightarrow c^2 = 24$$

$$c^2 = a^2 - b^2$$

$$24 = 49 - b^2$$

$$-25 = -b^2$$

Example 3

(a) Write the equation of an ellipse with

vertices at $(10, 0)$ and $(-4, 0)$, and foci at $(3 \pm 2\sqrt{6}, 0)$

Center at $(3, 0)$

$$a = \pm 7 \longrightarrow a^2 = 49$$

$$c = \pm 2\sqrt{6} \longrightarrow c^2 = 24$$

$$c^2 = a^2 - b^2$$

$$24 = 49 - b^2$$

$$-25 = -b^2$$

$$b^2 = 25$$

Example 3a

Center at $(3, 0)$ $a^2 = 49$ $b^2 = 25$ “wider”

Example 3a

Center at $(3, 0)$ $a^2 = 49$ $b^2 = 25$ “wider”

$$\frac{(x - 3)^2}{49} + \frac{y^2}{25} = 1$$

Example 3

(b) Vertices at $(-6, 2)$ and $(-6, -22)$, and co-vertices at $(-5, -10)$ and $(-7, -10)$

Example 3

(b) Vertices at $(-6, 2)$ and $(-6, -22)$, and co-vertices at $(-5, -10)$ and $(-7, -10)$

Center at $(-6, -10)$

Example 3

(b) Vertices at $(-6, 2)$ and $(-6, -22)$, and co-vertices at $(-5, -10)$ and $(-7, -10)$

Center at $(-6, -10)$

$$a = \pm 12$$

Example 3

(b) Vertices at $(-6, 2)$ and $(-6, -22)$, and co-vertices at $(-5, -10)$ and $(-7, -10)$

Center at $(-6, -10)$

$$a = \pm 12 \longrightarrow a^2 = 144$$

Example 3

(b) Vertices at $(-6, 2)$ and $(-6, -22)$, and co-vertices at $(-5, -10)$ and $(-7, -10)$

Center at $(-6, -10)$

$$a = \pm 12 \longrightarrow a^2 = 144$$

$$b = \pm 1$$

Example 3

(b) Vertices at $(-6, 2)$ and $(-6, -22)$, and co-vertices at $(-5, -10)$ and $(-7, -10)$

Center at $(-6, -10)$

$$a = \pm 12 \longrightarrow a^2 = 144$$

$$b = \pm 1 \longrightarrow b^2 = 1$$

$$(x + 6)^2 + \frac{(y + 10)^2}{144} = 1$$

Example 3

(c) Center: $(0, 2)$, Vertex: $(-12, 2)$, Focus: $(6\sqrt{3}, 2)$

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$$c^2 = a^2 - b^2$$

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$$c^2 = a^2 - b^2$$

$$108 = 144 - b^2$$

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(c) Center: $(0, 2)$, Vertex: $(-12, 2)$, Focus: $(6\sqrt{3}, 2)$

$$a = \pm 12 \longrightarrow a^2 = 144$$

$$c = \pm 6\sqrt{3} \longrightarrow c^2 = 108$$

$$c^2 = a^2 - b^2$$

$$108 = 144 - b^2$$

$$-36 = -b^2$$

Example 3

(c) Center: $(0, 2)$, Vertex: $(-12, 2)$, Focus: $(6\sqrt{3}, 2)$

$$a = \pm 12 \longrightarrow a^2 = 144$$

$$c = \pm 6\sqrt{3} \longrightarrow c^2 = 108$$

$$c^2 = a^2 - b^2$$

$$108 = 144 - b^2$$

$$-36 = -b^2$$

$$b^2 = 36$$

Example 3c

Center at $(0, 2)$ $a^2 = 144$ $b^2 = 36$ “wider”

Example 3c

Center at $(0, 2)$ $a^2 = 144$ $b^2 = 36$ “wider”

$$\frac{x^2}{144} + \frac{(y - 2)^2}{36} = 1$$