Matrix Algebra

Objectives

1 Find the sum and difference of two or more matrices.

2 Multiply a matrix by a scalar.

3 Multiply matrices together.

Matrix

A matrix is a rectangular array of numbers.

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Matrix Dimensions

The dimensions of a matrix (pl: matrices) are listed as

Number of rows $(r) \times \text{Number of columns } (c)$

We use upper-case letters to refer to entire matrices.

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Example of some matrices:

$$3 \times 2 \text{ matrix}$$
 $2 \times 2 \text{ matrix}$ $1 \times 4 \text{ matrix}$:
$$A = \begin{bmatrix} 5 & -3 \\ 2 & 1 \\ 0 & 4.5 \end{bmatrix}$$
 $B = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ $C = \begin{bmatrix} 8 & 6 & 7 & 5 \end{bmatrix}$

Square Matrix

A square matrix is a matrix in which the number of rows equals the number of columns.

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Matrix Elements

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For instance, the element in row 3 column 1 of matrix A is denoted

Adding and Subtracting Matrices

We can add and subtract matrices **that are of the same dimension** by adding or subtracting corresponding elements.

For the matrices

$$A = \begin{bmatrix} 5 & -8 & 4 \\ 2 & 0 & -1 \end{bmatrix} \quad B = \begin{bmatrix} -4 & 6 & 12 \\ 7 & 2 & -9 \end{bmatrix} \quad \text{and} \quad C = \begin{bmatrix} 10 & 9 \\ -5 & 7 \end{bmatrix}$$

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(a)
$$A + B$$

$$\begin{bmatrix} 1 \\ \end{bmatrix}$$

For the matrices

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$$\begin{bmatrix} 1 & -2 & & \end{bmatrix}$$

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$$\begin{bmatrix} 1 & -2 & 16 \end{bmatrix}$$

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Example 1
$$A = \begin{bmatrix} 5 & -8 & 4 \\ 2 & 0 & -1 \end{bmatrix}$$
 $B = \begin{bmatrix} -4 & 6 & 12 \\ 7 & 2 & -9 \end{bmatrix}$

(b)
$$A - B$$

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$$\left[\begin{array}{cc}9&-14\end{array}\right]$$

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(c)
$$B+A$$

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Example 1
$$A = \begin{bmatrix} 5 & -8 & 4 \\ 2 & 0 & -1 \end{bmatrix}$$
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(d)
$$A + C$$

Example 1
$$A = \begin{bmatrix} 5 & -8 & 4 \\ 2 & 0 & -1 \end{bmatrix}$$
 $C = \begin{bmatrix} 10 & 9 \\ -5 & 7 \end{bmatrix}$

(d)
$$A + C$$

The dimensions are not the same.

$$A_{2\times3}$$
 $C_{2\times2}$

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(d)
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The dimensions are not the same.

$$A_{2\times3}$$
 $C_{2\times2}$

Matrix addition is **not possible**.

Objectives

Find the sum and difference of two or more matrices

2 Multiply a matrix by a scalar.

Multiply matrices together.

What is a Scalar?

Scalar

A scalar is a real number.

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Scalar

A scalar is a real number.

To multiply a matrix by a scalar, multiply each element of the matrix by the scalar.

For the matrices

$$A = \begin{bmatrix} 5 & -8 & 4 \\ 2 & 0 & -1 \end{bmatrix} \quad \text{and} \quad B = \begin{bmatrix} -4 & 6 & 12 \\ 7 & 2 & -9 \end{bmatrix}$$

For the matrices

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(a)
$$5A$$

$$\begin{bmatrix} 25 & -40 & 20 \end{bmatrix}$$

For the matrices

$$A = \begin{bmatrix} 5 & -8 & 4 \\ 2 & 0 & -1 \end{bmatrix} \quad \text{and} \quad B = \begin{bmatrix} -4 & 6 & 12 \\ 7 & 2 & -9 \end{bmatrix}$$

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Example 2
$$A = \begin{bmatrix} 5 & -8 & 4 \\ 2 & 0 & -1 \end{bmatrix}$$
 and $B = \begin{bmatrix} -4 & 6 & 12 \\ 7 & 2 & -9 \end{bmatrix}$

(b) 6*B*

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$$A = \begin{bmatrix} 5 & -8 & 4 \\ 2 & 0 & -1 \end{bmatrix}$$
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$$\begin{bmatrix} -24 & 36 \\ \end{bmatrix}$$

Example 2
$$A = \begin{bmatrix} 5 & -8 & 4 \\ 2 & 0 & -1 \end{bmatrix}$$
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$$A = \begin{bmatrix} 5 & -8 & 4 \\ 2 & 0 & -1 \end{bmatrix}$$
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$$\begin{bmatrix} -24 & 36 & 72 \\ 42 & 12 & -54 \end{bmatrix}$$

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$$A = \begin{bmatrix} 5 & -8 & 4 \\ 2 & 0 & -1 \end{bmatrix}$$
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(c)
$$2A - 3B$$

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$$2A - 3B$$

$$2A = \begin{bmatrix} 10 & -16 & 8 \\ 4 & 0 & -2 \end{bmatrix} \quad 3B = \begin{bmatrix} -12 & 18 & 36 \\ 21 & 6 & -27 \end{bmatrix}$$

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$$A = \begin{bmatrix} 5 & -8 & 4 \\ 2 & 0 & -1 \end{bmatrix}$$
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$$2A = \begin{bmatrix} 10 & -16 & 8 \\ 4 & 0 & -2 \end{bmatrix} \quad 3B = \begin{bmatrix} -12 & 18 & 36 \\ 21 & 6 & -27 \end{bmatrix}$$
$$2A - 3B = \begin{bmatrix} 22 & -34 & -28 \\ -17 & -6 & 25 \end{bmatrix}$$

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Find the sum and difference of two or more matrices

2 Multiply a matrix by a scalar.

3 Multiply matrices together.

Multiplying matrices does not work in the way you might think.

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When multiplying matrices, we **DO NOT** multiply corresponding elements (like when we add and subtract corresponding elements with adding and subtracting matrices).

Instead, we multiply corresponding elements of a row by corresponding elements of a column and store the sum of that product of row and column in the intersection of that row and column.

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That being said:

 We can only multiply matrices if the number of columns in the first matrix equals the number of rows in the second.

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That being said:

- We can only multiply matrices if the number of columns in the first matrix equals the number of rows in the second.
- Our final result will be a matrix with dimensions equal to the number of rows in the first matrix × the number of columns in the second.

So to multiply

$$D = \begin{bmatrix} 4 & -1 & -7 \\ 2 & 0 & 6 \end{bmatrix} \quad \text{and} \quad E = \begin{bmatrix} 1 & 9 \\ 3 & -2 \\ 4 & 0 \end{bmatrix}$$

So to multiply

$$D = \begin{bmatrix} 4 & -1 & -7 \\ 2 & 0 & 6 \end{bmatrix} \quad \text{and} \quad E = \begin{bmatrix} 1 & 9 \\ 3 & -2 \\ 4 & 0 \end{bmatrix}$$

Note that the dimensions of D are $\mathbf{2} \times \mathbf{3}$ and the dimensions of E are $\mathbf{3} \times \mathbf{2}$.

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Note that the dimensions of D are $\mathbf{2} \times \mathbf{3}$ and the dimensions of E are $\mathbf{3} \times \mathbf{2}$.

Since the number of columns in D (3) equals the number of rows in E (3), we can multiply the matrices.

The product will be a matrix with 2 rows and 2 columns.

$$\begin{bmatrix} 4 & -1 & -7 \\ 2 & 0 & 6 \end{bmatrix} \cdot \begin{bmatrix} 1 & 9 \\ 3 & -2 \\ 4 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 4 & -1 & -7 \\ 2 & 0 & 6 \end{bmatrix} \cdot \begin{bmatrix} 1 & 9 \\ 3 & -2 \\ 4 & 0 \end{bmatrix}$$

Matrix Algebra

$$\begin{bmatrix} 4 & -1 & -7 \\ 2 & 0 & 6 \end{bmatrix} \cdot \begin{bmatrix} 1 & 9 \\ 3 & -2 \\ 4 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 4(1) + (-1)(3) + (-7)(4) \end{bmatrix}$$

$$\begin{bmatrix} 4 & -1 & -7 \\ 2 & 0 & 6 \end{bmatrix} \cdot \begin{bmatrix} 1 & 9 \\ 3 & -2 \\ 4 & 0 \end{bmatrix}$$

$$4(1) + (-1)(3) + (-7)(4)$$

Matrix Algebra

$$\begin{bmatrix} 4 & -1 & -7 \\ 2 & 0 & 6 \end{bmatrix} \cdot \begin{bmatrix} 1 & 9 \\ 3 & -2 \\ 4 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 4(1) + (-1)(3) + (-7)(4) & 4(9) + (-1)(-2) + (-7)(0) \end{bmatrix}$$

$$\begin{bmatrix} -27 \end{bmatrix}$$

$$\begin{bmatrix} 4 & -1 & -7 \\ 2 & 0 & 6 \end{bmatrix} \cdot \begin{bmatrix} 1 & 9 \\ 3 & -2 \\ 4 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 4(1) + (-1)(3) + (-7)(4) & 4(9) + (-1)(-2) + (-7)(0) \end{bmatrix}$$

$$\begin{bmatrix} -27 & 38 \end{bmatrix}$$

$$\begin{bmatrix} 4 & -1 & -7 \\ 2 & 0 & 6 \end{bmatrix} \cdot \begin{bmatrix} 1 & 9 \\ 3 & -2 \\ 4 & 0 \end{bmatrix}$$

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$$\begin{bmatrix} -27 & 38 \\ 26 & \end{bmatrix}$$

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$$\begin{bmatrix} -27 & 38 \\ 26 & 18 \end{bmatrix}$$

Note: Always remember to check that the number of columns in the first matrix equals the number of rows in the second. If this is not the case, you can not multiply the matrices together.

For the matrices below, find the products.

$$A = \begin{bmatrix} 4 & 8 & -9 \\ 2 & 0 & 3 \end{bmatrix} \quad B = \begin{bmatrix} 7 & 4 \\ 1 & -5 \\ 0 & 6 \end{bmatrix} \quad C = \begin{bmatrix} 6 & -5 \\ 4 & 1 \end{bmatrix}$$

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$$\left[4(7) + 8(1) + (-9)(0)\right]$$

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(a) AB

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$$\begin{bmatrix} 36 & -78 \\ 14 & 26 \end{bmatrix}$$

Example 3
$$B = \begin{bmatrix} 7 & 4 \\ 1 & -5 \\ 0 & 6 \end{bmatrix}$$
 $A = \begin{bmatrix} 4 & 8 & -9 \\ 2 & 0 & 3 \end{bmatrix}$

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$$7(4) + 4(2)$$

Example 3
$$B = \begin{bmatrix} 7 & 4 \\ 1 & -5 \\ 0 & 6 \end{bmatrix}$$
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$$\begin{bmatrix} 7(4) + 4(2) & 7(8) + 4(0) \end{bmatrix}$$

Example 3
$$B = \begin{bmatrix} 7 & 4 \\ 1 & -5 \\ 0 & 6 \end{bmatrix}$$
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$$7(4) + 4(2)$$
 $7(8) + 4(0)$

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$$\begin{bmatrix} 36 & 56 & -51 \end{bmatrix}$$

Example 3
$$B = \begin{bmatrix} 7 & 4 \\ 1 & -5 \\ 0 & 6 \end{bmatrix}$$
 $A = \begin{bmatrix} 4 & 8 & -9 \\ 2 & 0 & 3 \end{bmatrix}$

$$\begin{bmatrix} 7(4) + 4(2) & 7(8) + 4(0) & 7(-9) + 4(3) \\ 1(4) + (-5)(2) & & \end{bmatrix}$$

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$$\begin{bmatrix} 36 & 56 & -51 \\ -6 & 8 & -24 \end{bmatrix}$$

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$$\begin{bmatrix} 36 & 56 & -51 \\ -6 & 8 & -24 \\ 12 \end{bmatrix}$$

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 $A = \begin{bmatrix} 4 & 8 & -9 \\ 2 & 0 & 3 \end{bmatrix}$

$$\begin{bmatrix} 7(4) + 4(2) & 7(8) + 4(0) & 7(-9) + 4(3) \\ 1(4) + (-5)(2) & 1(8) + (-5)(0) & 1(-9) + (-5)(3) \\ 0(4) + 6(2) & 0(8) + 6(0) \end{bmatrix}$$

$$\begin{bmatrix} 36 & 56 & -51 \\ -6 & 8 & -24 \\ 12 & & \end{bmatrix}$$

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$$\begin{bmatrix} 36 & 56 & -51 \\ -6 & 8 & -24 \\ 12 & 0 \end{bmatrix}$$

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$$\begin{bmatrix} 36 & 56 & -51 \\ -6 & 8 & -24 \\ 12 & 0 & 18 \end{bmatrix}$$

Example 3
$$A = \begin{bmatrix} 4 & 8 & -9 \\ 2 & 0 & 3 \end{bmatrix}$$
 $C = \begin{bmatrix} 6 & -5 \\ 4 & 1 \end{bmatrix}$

(c) *AC*

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Not possible

Example 3
$$C = \begin{bmatrix} 6 & -5 \\ 4 & 1 \end{bmatrix}$$

(d) C^2

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$$C = \begin{bmatrix} 6 & -5 \\ 4 & 1 \end{bmatrix}$$

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$$C^2$$

$$\begin{bmatrix} 6 & -5 \\ 4 & 1 \end{bmatrix} \cdot \begin{bmatrix} 6 & -5 \\ 4 & 1 \end{bmatrix}$$

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$$C = \begin{bmatrix} 6 & -5 \\ 4 & 1 \end{bmatrix}$$

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$$(6(6) + (-5)(4)$$

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$$\begin{bmatrix} 6 & -5 \\ 4 & 1 \end{bmatrix} \cdot \begin{bmatrix} 6 & -5 \\ 4 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 6(6) + (-5)(4) & 6(-5) + (-5)(1) \end{bmatrix}$$

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$$\begin{bmatrix} 16 & -35 \end{bmatrix}$$

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$$\begin{bmatrix} 16 & -35 \\ 28 & -19 \end{bmatrix}$$