

# Inverse Functions

# Objectives

- 1 Find the inverse of a function
- 2 State the Domain and Range of an Inverse Function

# Inverse of an Ordered Pair

The **inverse** of the ordered pair  $(x, y)$  is  $(y, x)$ .

## Example 1

Find the inverse of each.

(a)  $(2, -7)$

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(a)  $(2, -7)$   $(-7, 2)$

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(a)  $(2, -7)$   $(-7, 2)$

(b)  $(0, 3)$

## Example 1

Find the inverse of each.

(a)  $(2, -7)$   $(-7, 2)$

(b)  $(0, 3)$   $(3, 0)$

# Review of Functions

Recall that a function is nothing more than a machine that

- 1 Accepts an input,  $x$



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Recall that a function is nothing more than a machine that

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The inverse function is somewhat of an “undo” function.

# Review of Functions

Recall that a function is nothing more than a machine that

- 1 Accepts an input,  $x$
- 2 Performs some operation(s)
- 3 Gives an output,  $y$

The inverse function is somewhat of an “undo” function.

It allows us to take the output of a function, put it into our inverse function, and get our original input value back.

Suppose we put a value of 10 into the function

$$f(x) = x^2$$

# Visualization

Suppose we put a value of 10 into the function

$$f(x) = x^2$$

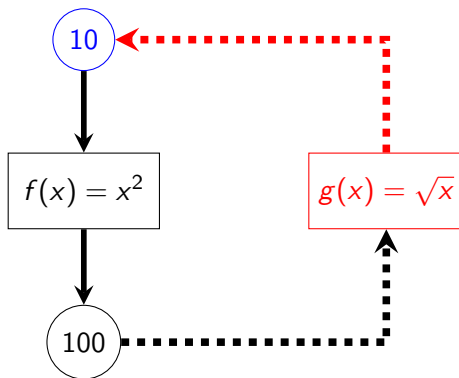
If we put the output (100) into the inverse, we get our 10 back.

# Visualization

Suppose we put a value of 10 into the function

$$f(x) = x^2$$

If we put the output (100) into the inverse, we get our 10 back.



# Inverse Notation

We use the notation

$$f^{-1}(x)$$

to denote the inverse of  $f(x)$ .



# Inverse Notation

We use the notation

$$f^{-1}(x)$$

to denote the inverse of  $f(x)$ .

**Note:** The notation **does not mean** raise the function to the  $-1$  power.

# Steps in Finding the Inverse of a Function

- 1 Rewrite  $f(x) =$  as  $y =$

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- 1 Rewrite  $f(x) =$  as  $y =$
- 2 Switch your  $x$  and  $y$  variables.

# Steps in Finding the Inverse of a Function

- ① Rewrite  $f(x) =$  as  $y =$
- ② Switch your  $x$  and  $y$  variables.
- ③ Solve this result for  $y$  and rewrite using inverse notation.

## Example 2

Find the inverse of each of the following.

(a)  $f(x) = 5x$

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(a)  $f(x) = 5x$

$$y = 5x$$

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Find the inverse of each of the following.

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$$y = 5x$$

$$x = 5y$$

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Find the inverse of each of the following.

(a)  $f(x) = 5x$

$$y = 5x$$

$$x = 5y$$

$$\frac{x}{5} = y$$



## Example 2

Find the inverse of each of the following.

(a)  $f(x) = 5x$

$$y = 5x$$

$$x = 5y$$

$$\frac{x}{5} = y$$

$$f^{-1}(x) = \frac{x}{5}$$

## Example 2

$$(b) \quad f(x) = 3x + 2$$

## Example 2

$$(b) \quad f(x) = 3x + 2$$

$$y = 3x + 2$$

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$$(b) \quad f(x) = 3x + 2$$

$$y = 3x + 2$$

$$x = 3y + 2$$

## Example 2

$$(b) \quad f(x) = 3x + 2$$

$$y = 3x + 2$$

$$x = 3y + 2$$

$$x - 2 = 3y$$

## Example 2

$$(b) \quad f(x) = 3x + 2$$

$$y = 3x + 2$$

$$x = 3y + 2$$

$$x - 2 = 3y$$

$$\frac{x - 2}{3} = y$$

## Example 2

$$(b) \quad f(x) = 3x + 2$$

$$y = 3x + 2$$

$$x = 3y + 2$$

$$x - 2 = 3y$$

$$\frac{x - 2}{3} = y$$

$$f^{-1}(x) = \frac{x - 2}{3}$$

## Example 2

$$(c) \quad f(x) = \frac{x+5}{7}$$



## Example 2

$$(c) \quad f(x) = \frac{x+5}{7}$$

$$y = \frac{x+5}{7}$$

## Example 2

$$(c) \quad f(x) = \frac{x+5}{7}$$

$$y = \frac{x+5}{7}$$

$$x = \frac{\textcolor{red}{y}+5}{7}$$

## Example 2

$$(c) \quad f(x) = \frac{x+5}{7}$$

$$y = \frac{x+5}{7}$$

$$x = \frac{y+5}{7}$$

$$7x = y + 5$$

## Example 2

$$(c) \quad f(x) = \frac{x+5}{7}$$

$$y = \frac{x+5}{7}$$

$$x = \frac{y+5}{7}$$

$$7x = y + 5$$

$$7x - 5 = y$$

## Example 2

$$(c) \quad f(x) = \frac{x+5}{7}$$

$$y = \frac{x+5}{7}$$

$$x = \frac{y+5}{7}$$

$$7x = y + 5$$

$$7x - 5 = y$$

$$f^{-1}(x) = 7x - 5$$

## Example 2

$$(d) \quad g(x) = x^3 + 1$$

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$$(d) \quad g(x) = x^3 + 1$$

$$y = x^3 + 1$$

## Example 2

$$(d) \quad g(x) = x^3 + 1$$

$$y = x^3 + 1$$

$$x = \textcolor{red}{y}^3 + 1$$



## Example 2

$$(d) \quad g(x) = x^3 + 1$$

$$y = x^3 + 1$$

$$x = y^3 + 1$$

$$x - 1 = y^3$$

## Example 2

$$(d) \quad g(x) = x^3 + 1$$

$$y = x^3 + 1$$

$$x = y^3 + 1$$

$$x - 1 = y^3$$

$$\sqrt[3]{x - 1} = y$$

## Example 2

$$(d) \quad g(x) = x^3 + 1$$

$$y = x^3 + 1$$

$$x = y^3 + 1$$

$$x - 1 = y^3$$

$$\sqrt[3]{x - 1} = y$$

$$g^{-1}(x) = \sqrt[3]{x - 1}$$

## Example 2

$$(e) \quad h(x) = 4x^5 - 1$$

## Example 2

$$(e) \quad h(x) = 4x^5 - 1$$

$$y = 4x^5 - 1$$

## Example 2

$$(e) \quad h(x) = 4x^5 - 1$$

$$y = 4x^5 - 1$$

$$x = 4y^5 - 1$$

## Example 2

$$(e) \quad h(x) = 4x^5 - 1$$

$$y = 4x^5 - 1$$

$$x = 4y^5 - 1$$

$$x + 1 = 4y^5$$

## Example 2

$$(e) \quad h(x) = 4x^5 - 1$$

$$y = 4x^5 - 1$$

$$x = 4y^5 - 1$$

$$x + 1 = 4y^5$$

$$\frac{x + 1}{4} = y^5$$



## Example 2

$$(e) \quad h(x) = 4x^5 - 1$$

$$y = 4x^5 - 1$$

$$x = 4y^5 - 1$$

$$x + 1 = 4y^5$$

$$\frac{x + 1}{4} = y^5$$

$$\sqrt[5]{\frac{x + 1}{4}} = y$$

## Example 2

$$(e) \quad h(x) = 4x^5 - 1$$

$$y = 4x^5 - 1$$

$$x = 4y^5 - 1$$

$$x + 1 = 4y^5$$

$$\frac{x + 1}{4} = y^5$$

$$\sqrt[5]{\frac{x + 1}{4}} = y$$

$$h^{-1}(x) = \sqrt[5]{\frac{x + 1}{4}}$$

## Example 2

$$(f) \quad f(x) = \sqrt{x+3}$$

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$$y = \sqrt{x+3}$$

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$$y = \sqrt{x+3}$$

$$x = \sqrt{\textcolor{red}{y}+3}$$

## Example 2

$$(f) \quad f(x) = \sqrt{x+3}$$

$$y = \sqrt{x+3}$$

$$x = \sqrt{y+3}$$

$$x^2 = y + 3$$

## Example 2

$$(f) \quad f(x) = \sqrt{x+3}$$

$$y = \sqrt{x+3}$$

$$x = \sqrt{y+3}$$

$$x^2 = y + 3$$

$$x^2 - 3 = y$$

## Example 2

$$(f) \quad f(x) = \sqrt{x+3}$$

$$y = \sqrt{x+3}$$

$$x = \sqrt{y+3}$$

$$x^2 = y + 3$$

$$x^2 - 3 = y$$

$$f^{-1}(x) = x^2 - 3$$



## Example 2

$$(g) \quad g(x) = \frac{5}{x}$$

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$$y = \frac{5}{x}$$

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$$(g) \quad g(x) = \frac{5}{x}$$

$$y = \frac{5}{x}$$

$$x = \frac{5}{\textcolor{red}{y}}$$

## Example 2

$$(g) \quad g(x) = \frac{5}{x}$$

$$y = \frac{5}{x}$$

$$x = \frac{5}{\textcolor{red}{y}}$$

$$x\textcolor{red}{y} = 5$$

## Example 2

$$(g) \quad g(x) = \frac{5}{x}$$

$$y = \frac{5}{x}$$

$$x = \frac{5}{\textcolor{red}{y}}$$

$$x\textcolor{red}{y} = 5$$

$$\textcolor{red}{y} = \frac{5}{x}$$

## Example 2

$$(g) \quad g(x) = \frac{5}{x}$$

$$y = \frac{5}{x}$$

$$x = \frac{5}{y}$$

$$xy = 5$$

$$y = \frac{5}{x}$$

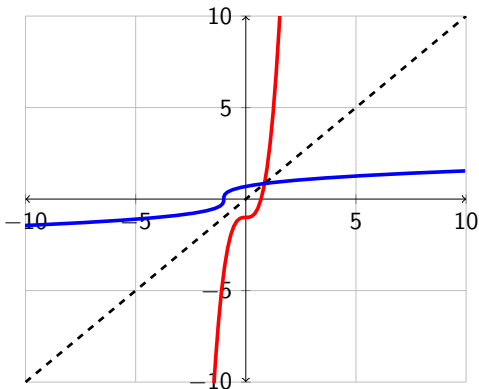
$$g^{-1}(x) = \frac{5}{x}$$

# Visual Interpretation of Inverse Functions

Visually, when finding the inverse of a function, you are **reflecting that function across the line  $y = x$** .

# Visual Interpretation of Inverse Functions

Below are the graphs of  $f(x) = 3x^3 - 1$  and  $f^{-1}(x) = \sqrt[3]{\frac{x+1}{3}}$  as well as the line  $y = x$ :





# Objectives

- 1 Find the inverse of a function
- 2 State the Domain and Range of an Inverse Function

# Domain and Range of Inverse Functions

When switching the  $x$  and  $y$  in finding the inverse function, you also switch the domain and range of the function and its inverse.

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When you graph a function and its inverse, **you'll want to make sure that they are reflections across the line  $y = x$** . This is VERY IMPORTANT for a function such as  $y = x^2$ .

# Domain and Range of Inverse Functions

When switching the  $x$  and  $y$  in finding the inverse function, you also switch the domain and range of the function and its inverse.

When you graph a function and its inverse, **you'll want to make sure that they are reflections across the line  $y = x$** . This is VERY IMPORTANT for a function such as  $y = x^2$ .

This might mean we need to **restrict the domain and/or range** of our original function.

# Relationship Between Domain and Range

Domain of  $f = \text{Range of } f^{-1}$

and

Range of  $f = \text{Domain of } f^{-1}$

## Example 3

Find the domain and range of both the function and its inverse.

(a)  $f(x) = 5x$

	Domain ( $x$ )	Range ( $y$ )
$f(x)$		
$f^{-1}(x)$		

## Example 3

Find the domain and range of both the function and its inverse.

(a)  $f(x) = 5x$      $f^{-1}(x) = \frac{x}{5}$

	Domain (x)	Range (y)
$f(x)$		
$f^{-1}(x)$		

## Example 3

Find the domain and range of both the function and its inverse.

(a)  $f(x) = 5x$      $f^{-1}(x) = \frac{x}{5}$

	Domain (x)	Range (y)
$f(x)$	$\mathbb{R}$	
$f^{-1}(x)$		



## Example 3

Find the domain and range of both the function and its inverse.

(a)  $f(x) = 5x$      $f^{-1}(x) = \frac{x}{5}$

	Domain (x)	Range (y)
$f(x)$	$\mathbb{R}$	
$f^{-1}(x)$		$\mathbb{R}$

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Find the domain and range of both the function and its inverse.

(a)  $f(x) = 5x$      $f^{-1}(x) = \frac{x}{5}$

	Domain ( $x$ )	Range ( $y$ )
$f(x)$	$\mathbb{R}$	
$f^{-1}(x)$		$\mathbb{R}$

## Example 3

Find the domain and range of both the function and its inverse.

(a)  $f(x) = 5x$      $f^{-1}(x) = \frac{x}{5}$

	Domain (x)	Range (y)
$f(x)$	$\mathbb{R}$	$\mathbb{R}$
$f^{-1}(x)$	$\mathbb{R}$	$\mathbb{R}$

## Example 3

(b)  $f(x) = 3x + 2$

	Domain (x)	Range (y)
$f(x)$		
$f^{-1}(x)$		

## Example 3

$$(b) \quad f(x) = 3x + 2 \quad f^{-1}(x) = \frac{x-2}{3}$$

	Domain (x)	Range (y)
$f(x)$		
$f^{-1}(x)$		

## Example 3

$$(b) \quad f(x) = 3x + 2 \quad f^{-1}(x) = \frac{x-2}{3}$$

	Domain (x)	Range (y)
$f(x)$	$\mathbb{R}$	
$f^{-1}(x)$		

## Example 3

$$(b) \quad f(x) = 3x + 2 \quad f^{-1}(x) = \frac{x-2}{3}$$

	Domain (x)	Range (y)
$f(x)$	$\mathbb{R}$	
$f^{-1}(x)$		$\mathbb{R}$

## Example 3

$$(b) \quad f(x) = 3x + 2 \quad f^{-1}(x) = \frac{x-2}{3}$$

	Domain (x)	Range (y)
$f(x)$	$\mathbb{R}$	
$f^{-1}(x)$		$\mathbb{R}$



## Example 3

$$(b) \quad f(x) = 3x + 2 \quad f^{-1}(x) = \frac{x-2}{3}$$

	Domain (x)	Range (y)
$f(x)$	$\mathbb{R}$	$\mathbb{R}$
$f^{-1}(x)$	$\mathbb{R}$	$\mathbb{R}$

## Example 3

(c)  $g(x) = \sqrt{x+3}$

	Domain ( $x$ )	Range ( $y$ )
$g(x)$		
$g^{-1}(x)$		

## Example 3

$$(c) \quad g(x) = \sqrt{x+3} \quad g^{-1}(x) = x^2 - 3$$

	Domain (x)	Range (y)
$g(x)$		
$g^{-1}(x)$		

## Example 3

$$(c) \quad g(x) = \sqrt{x+3} \quad g^{-1}(x) = x^2 - 3$$

	Domain (x)	Range (y)
$g(x)$	$x \geq -3$	
$g^{-1}(x)$		

## Example 3

$$(c) \quad g(x) = \sqrt{x+3} \quad g^{-1}(x) = x^2 - 3$$

	Domain (x)	Range (y)
$g(x)$	$x \geq -3$	
$g^{-1}(x)$		$y \geq -3$

## Example 3

$$(c) \quad g(x) = \sqrt{x+3} \quad g^{-1}(x) = x^2 - 3$$

	Domain (x)	Range (y)
$g(x)$	$x \geq -3$	$y \geq 0$
$g^{-1}(x)$		$y \geq -3$

## Example 3

$$(c) \quad g(x) = \sqrt{x+3} \quad g^{-1}(x) = x^2 - 3$$

	Domain (x)	Range (y)
$g(x)$	$x \geq -3$	$y \geq 0$
$g^{-1}(x)$	$x \geq 0$	$y \geq -3$

## Example 3

$$(d) \quad f(x) = -\sqrt{x-4} + 2$$



## Example 3

$$(d) \quad f(x) = -\sqrt{x-4} + 2$$

$$y = -\sqrt{x-4} + 2$$

## Example 3

$$(d) \quad f(x) = -\sqrt{x-4} + 2$$

$$y = -\sqrt{x-4} + 2$$

$$x = -\sqrt{\textcolor{red}{y}-4} + 2$$

## Example 3

$$(d) \quad f(x) = -\sqrt{x-4} + 2$$

$$y = -\sqrt{x-4} + 2$$

$$x = -\sqrt{y-4} + 2$$

$$x - 2 = -\sqrt{y-4}$$

## Example 3

$$(d) \quad f(x) = -\sqrt{x-4} + 2$$

$$y = -\sqrt{x-4} + 2$$

$$x = -\sqrt{y-4} + 2$$

$$x - 2 = -\sqrt{y-4}$$

$$-x + 2 = \sqrt{y-4}$$

## Example 3

$$(d) \quad f(x) = -\sqrt{x-4} + 2$$

$$y = -\sqrt{x-4} + 2$$

$$x = -\sqrt{y-4} + 2$$

$$x - 2 = -\sqrt{y-4}$$

$$-x + 2 = \sqrt{y-4}$$

$$(-x + 2)^2 = y - 4$$

## Example 3

$$(d) \quad f(x) = -\sqrt{x-4} + 2$$

$$y = -\sqrt{x-4} + 2$$

$$x = -\sqrt{y-4} + 2$$

$$x - 2 = -\sqrt{y-4}$$

$$-x + 2 = \sqrt{y-4}$$

$$(-x + 2)^2 = y - 4$$

$$(-x + 2)^2 + 4 = y$$

## Example 3

$$(d) \quad f(x) = -\sqrt{x-4} + 2$$

$$y = -\sqrt{x-4} + 2$$

$$x = -\sqrt{y-4} + 2$$

$$x - 2 = -\sqrt{y-4}$$

$$-x + 2 = \sqrt{y-4}$$

$$(-x + 2)^2 = y - 4$$

$$(-x + 2)^2 + 4 = y$$

$$f^{-1}(x) = (-x + 2)^2 + 4$$

## Example 3d

$$f(x) = -\sqrt{x-4} + 2 \quad f^{-1}(x) = (-x+2)^2 + 4$$

	Domain (x)	Range (y)
$f(x)$		
$f^{-1}(x)$		



## Example 3d

$$f(x) = -\sqrt{x-4} + 2 \quad f^{-1}(x) = (-x+2)^2 + 4$$

	Domain (x)	Range (y)
$f(x)$	$x \geq 4$	
$f^{-1}(x)$		

## Example 3d

$$f(x) = -\sqrt{x-4} + 2 \quad f^{-1}(x) = (-x+2)^2 + 4$$

	Domain (x)	Range (y)
$f(x)$	$x \geq 4$	
$f^{-1}(x)$		$y \geq 4$

## Example 3d

$$f(x) = -\sqrt{x-4} + 2 \quad f^{-1}(x) = (-x+2)^2 + 4$$

	Domain (x)	Range (y)
$f(x)$	$x \geq 4$	$y \leq 2$
$f^{-1}(x)$		$y \geq 4$

## Example 3d

$$f(x) = -\sqrt{x-4} + 2 \quad f^{-1}(x) = (-x+2)^2 + 4$$

	Domain (x)	Range (y)
$f(x)$	$x \geq 4$	$y \leq 2$
$f^{-1}(x)$	$x \leq 2$	$y \geq 4$

## Example 3

(e)  $f(x) = x^2$  with  $x \geq 0$

## Example 3

(e)  $f(x) = x^2$  with  $x \geq 0$

$$y = x^2$$

## Example 3

(e)  $f(x) = x^2$  with  $x \geq 0$

$$y = x^2$$

$$x = y^2$$

## Example 3

$$(e) \quad f(x) = x^2 \text{ with } x \geq 0$$

$$y = x^2$$

$$x = y^2$$

$$\pm \sqrt{x} = y$$



## Example 3

$$(e) \quad f(x) = x^2 \text{ with } x \geq 0$$

$$y = x^2$$

$$x = y^2$$

$$\pm \sqrt{x} = y$$

$$f^{-1}(x) = \pm \sqrt{x}$$

## Example 3

(e)  $f(x) = x^2$  with  $x \geq 0$

$$y = x^2$$

$$x = y^2$$

$$\pm \sqrt{x} = y$$

$$f^{-1}(x) = \pm \sqrt{x}$$

*Note:* It can NOT be both  $\sqrt{x}$  and  $-\sqrt{x}$  because it would fail the **vertical line test**.

## Example 3

$$f(x) = x^2 \text{ with } x \geq 0 \quad f^{-1}(x) = \pm\sqrt{x}$$

	Domain (x)	Range (y)
$f(x)$		
$f^{-1}(x)$		

## Example 3

$$f(x) = x^2 \text{ with } x \geq 0 \quad f^{-1}(x) = \pm\sqrt{x}$$

	Domain (x)	Range (y)
$f(x)$	$x \geq 0$	
$f^{-1}(x)$		

## Example 3

$$f(x) = x^2 \text{ with } x \geq 0 \quad f^{-1}(x) = \pm\sqrt{x}$$

	Domain (x)	Range (y)
$f(x)$	$x \geq 0$	
$f^{-1}(x)$		$y \geq 0$

## Example 3

$$f(x) = x^2 \text{ with } x \geq 0 \quad f^{-1}(x) = \pm\sqrt{x}$$

	Domain (x)	Range (y)
$f(x)$	$x \geq 0$	$y \geq 0$
$f^{-1}(x)$		$y \geq 0$

## Example 3

$$f(x) = x^2 \text{ with } x \geq 0 \quad f^{-1}(x) = \pm\sqrt{x}$$

	Domain (x)	Range (y)
$f(x)$	$x \geq 0$	$y \geq 0$
$f^{-1}(x)$	$x \geq 0$	$y \geq 0$

## Example 3

$$f(x) = x^2 \text{ with } x \geq 0 \quad f^{-1}(x) = \pm\sqrt{x}$$

	Domain (x)	Range (y)
$f(x)$	$x \geq 0$	$y \geq 0$
$f^{-1}(x)$	$x \geq 0$	$y \geq 0$

$$f^{-1}(x) = \sqrt{x}$$



## Example 3

$$(f) \quad f(x) = \frac{1}{x} - 7$$

## Example 3

$$(f) \quad f(x) = \frac{1}{x} - 7$$

$$y = \frac{1}{x} - 7$$

## Example 3

$$(f) \quad f(x) = \frac{1}{x} - 7$$

$$y = \frac{1}{x} - 7$$

$$x = \frac{1}{\textcolor{red}{y}} - 7$$

## Example 3

$$(f) \quad f(x) = \frac{1}{x} - 7$$

$$y = \frac{1}{x} - 7$$

$$x = \frac{1}{\textcolor{red}{y}} - 7$$

$$x + 7 = \frac{1}{\textcolor{red}{y}}$$

## Example 3

$$(f) \quad f(x) = \frac{1}{x} - 7$$

$$y = \frac{1}{x} - 7$$

$$x = \frac{1}{\textcolor{red}{y}} - 7$$

$$x + 7 = \frac{1}{\textcolor{red}{y}}$$

$$\textcolor{red}{y}(x + 7) = 1$$

## Example 3

$$(f) \quad f(x) = \frac{1}{x} - 7$$

$$y = \frac{1}{x} - 7$$

$$x = \frac{1}{\textcolor{red}{y}} - 7$$

$$x + 7 = \frac{1}{\textcolor{red}{y}}$$

$$\textcolor{red}{y}(x + 7) = 1$$

$$\textcolor{red}{y} = \frac{1}{x + 7}$$

## Example 3

$$f(x) = \frac{1}{x} - 7 \quad f^{-1}(x) = \frac{1}{x+7}$$

	Domain (x)	Range (y)
$f(x)$		
$f^{-1}(x)$		

## Example 3

$$f(x) = \frac{1}{x} - 7 \quad f^{-1}(x) = \frac{1}{x+7}$$

	Domain (x)	Range (y)
$f(x)$	$x \neq 0$	
$f^{-1}(x)$		



## Example 3

$$f(x) = \frac{1}{x} - 7 \quad f^{-1}(x) = \frac{1}{x+7}$$

	Domain (x)	Range (y)
$f(x)$	$x \neq 0$	
$f^{-1}(x)$		$y \neq 0$

## Example 3

$$f(x) = \frac{1}{x} - 7 \quad f^{-1}(x) = \frac{1}{x+7}$$

	Domain (x)	Range (y)
$f(x)$	$x \neq 0$	
$f^{-1}(x)$	$x \neq -7$	$y \neq 0$

## Example 3

$$f(x) = \frac{1}{x} - 7 \quad f^{-1}(x) = \frac{1}{x+7}$$

	Domain (x)	Range (y)
$f(x)$	$x \neq 0$	$y \neq -7$
$f^{-1}(x)$	$x \neq -7$	$y \neq 0$

## Example 3

$$(g) \quad f(x) = \frac{3}{2x + 5}$$

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$$x(2y + 5) = 3$$

$$2y + 5 = \frac{3}{x}$$

$$2y = \frac{3}{x} - 5$$

## Example 3g

$$2y = \frac{3}{x} - 5$$

## Example 3g

$$2y = \frac{3}{x} - 5$$

$$y = \frac{3}{2x} - \frac{5}{2}$$

## Example 3g

$$2y = \frac{3}{x} - 5$$

$$y = \frac{3}{2x} - \frac{5}{2}$$

$$f^{-1}(x) = \frac{3}{2x} - \frac{5}{2}$$

## Example 3g

$$f(x) = \frac{3}{2x+5} \quad f^{-1}(x) = \frac{3}{2x} - \frac{5}{2}$$

	Domain (x)	Range (y)
$f(x)$		
$f^{-1}(x)$		

## Example 3g

$$f(x) = \frac{3}{2x+5} \quad f^{-1}(x) = \frac{3}{2x} - \frac{5}{2}$$

	Domain (x)	Range (y)
$f(x)$	$x \neq -\frac{5}{2}$	
$f^{-1}(x)$		

## Example 3g

$$f(x) = \frac{3}{2x+5} \quad f^{-1}(x) = \frac{3}{2x} - \frac{5}{2}$$

	Domain (x)	Range (y)
$f(x)$	$x \neq -\frac{5}{2}$	
$f^{-1}(x)$		$y \neq -\frac{5}{2}$

## Example 3g

$$f(x) = \frac{3}{2x+5} \quad f^{-1}(x) = \frac{3}{2x} - \frac{5}{2}$$

	Domain (x)	Range (y)
$f(x)$	$x \neq -\frac{5}{2}$	
$f^{-1}(x)$	$x \neq 0$	$y \neq -\frac{5}{2}$



## Example 3g

$$f(x) = \frac{3}{2x+5} \quad f^{-1}(x) = \frac{3}{2x} - \frac{5}{2}$$

	Domain (x)	Range (y)
$f(x)$	$x \neq -\frac{5}{2}$	$y \neq 0$
$f^{-1}(x)$	$x \neq 0$	$y \neq -\frac{5}{2}$