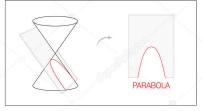
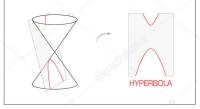
Hyperbolas









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Objectives

1 Find the vertices and foci for a hyperbola in standard form.

2 Write the equation for a hyperbola in standard form.

Hyperbolas

Hyperbolas

The set of points such that the **difference** of their distances from 2 fixed points (called **foci**) is constant.

Comparing Hyperbolas and Ellipses

Just like an ellipse, the midpoint joining the foci is the **center**.

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Just like an ellipse, the midpoint joining the foci is the **center**.

Whereas ellipses could appear taller or wider, hyperbolas will open up and down, or left and right.

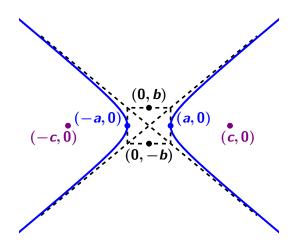
Comparing Hyperbolas and Ellipses

Just like an ellipse, the midpoint joining the foci is the **center**.

Whereas ellipses could appear taller or wider, hyperbolas will open up and down, or left and right.

A key difference, however, is that hyperbolas will open left/right if the sign in front of x is positive, and will open up/down if the sign in front of y is positive; regardless of the values of a and b.

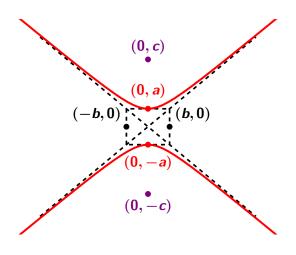
Opening Left and Right



Properties

Equation
$$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1$$
Center
$$(h,k)$$
Vertices
$$(h\pm a,0)$$
Foci
$$(h\pm c,0)$$
Co-vertices
$$(h,k\pm b)$$
Transverse Axis
$$x$$
-Axis Conjugate Axis
$$c^2 \qquad a^2 + b^2$$

Opening Up and Down



Properties

Equation
$$\frac{(y-k)^2}{a^2} - \frac{(x-h)^2}{b^2} = 1$$
Center
$$(h,k)$$
Vertices
$$(h,k\pm a)$$
Foci
$$(h,k\pm c)$$
Co-vertices
$$(h\pm a,k)$$
Conjugate Axis
$$x$$
-Axis
$$y$$
-Axis
$$c^2$$
Transverse Axis
$$a^2 + b^2$$

Find the exact coordinates for the vertices and foci for each of the following.

(a)
$$\frac{(y-3)^2}{4} - \frac{x^2}{16} = 1$$

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Center: (0,3)

$$a^2 = 4$$

Find the exact coordinates for the vertices and foci for each of the following.

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$$\frac{(y-3)^2}{4} - \frac{x^2}{16} = 1$$

Center: (0,3)

$$a^2 = 4$$

$$a = \pm 2$$

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$$\frac{(y-3)^2}{4} - \frac{x^2}{16} = 1$$

Center: (0,3)

$$a^2 = 4$$

$$a = \pm 2$$

Vertices: $(0, 3 \pm 2)$

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(a)
$$\frac{(y-3)^2}{4} - \frac{x^2}{16} = 1$$

Center: (0,3)

$$a^2 = 4$$

$$a = \pm 2$$

Vertices: $(0, 3 \pm 2) \longrightarrow (0, 1)$ and (0, 5)

$$c^2 = a^2 + b^2$$

$$c^2 = a^2 + b^2$$

$$c^2 = 4 + 16$$

$$c^2 = a^2 + b^2$$

$$c^2 = 4 + 16$$

$$c^2 = 20$$

$$c^{2} = a^{2} + b^{2}$$
$$c^{2} = 4 + 16$$
$$c^{2} = 20$$
$$c = \pm 2\sqrt{5}$$

$$c^{2} = a^{2} + b^{2}$$
$$c^{2} = 4 + 16$$
$$c^{2} = 20$$
$$c = \pm 2\sqrt{5}$$

Foci:
$$(0,3\pm2\sqrt{5})$$

(b)
$$\frac{(y+1)^2}{16} - (x-1)^2 = 1$$

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$$a = \pm 4$$

(b)
$$\frac{(y+1)^2}{16} - (x-1)^2 = 1$$

$$a^2 = 16$$

$$a = \pm 4$$

Vertices:
$$(1, -1 \pm 4)$$

(b)
$$\frac{(y+1)^2}{16} - (x-1)^2 = 1$$

$$a^2 = 16$$

$$a = \pm 4$$

Vertices:
$$(1,-1\pm 4) \longrightarrow (1,-5)$$
 and $(1,3)$

$$c^2 = a^2 + b^2$$

$$c^2 = a^2 + b^2$$

$$c^2 = 16 + 1$$

$$c^{2} = a^{2} + b^{2}$$
$$c^{2} = 16 + 1$$
$$c^{2} = 17$$

$$c^{2} = a^{2} + b^{2}$$

$$c^{2} = 16 + 1$$

$$c^{2} = 17$$

$$c = \pm \sqrt{17}$$

$$c^{2} = a^{2} + b^{2}$$
$$c^{2} = 16 + 1$$
$$c^{2} = 17$$
$$c = \pm \sqrt{17}$$

Foci:
$$(1,-1\pm\sqrt{17})$$

(c)
$$(x+4)^2 - \frac{(y+2)^2}{9} = 1$$

(c)
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Center: (-4, -2)

(c)
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Center:
$$(-4, -2)$$

$$a^2 = 1$$

(c)
$$(x+4)^2 - \frac{(y+2)^2}{9} = 1$$

Center:
$$(-4, -2)$$

$$a^2 = 1$$

$$a=\pm 1$$

(c)
$$(x+4)^2 - \frac{(y+2)^2}{9} = 1$$

Center: (-4, -2)

$$a^2 = 1$$

$$a = \pm 1$$

Vertices:
$$(-4 \pm 1, -2)$$

(c)
$$(x+4)^2 - \frac{(y+2)^2}{9} = 1$$

Center: (-4, -2)

$$a^2 = 1$$

$$a = \pm 1$$

Vertices:
$$(-4 \pm 1, -2) \longrightarrow (-5, -2)$$
 and $(-3, -2)$

$$c^2 = a^2 + b^2$$

$$c^2 = a^2 + b^2$$
$$c^2 = 1 + 9$$

$$c^2=1+9$$

$$c^2 = a^2 + b^2$$

$$c^2 = 1 + 9$$

$$c^2 = 10$$

$$c^{2} = a^{2} + b^{2}$$
$$c^{2} = 1 + 9$$
$$c^{2} = 10$$
$$c = \pm \sqrt{10}$$

$$c^{2} = a^{2} + b^{2}$$
$$c^{2} = 1 + 9$$
$$c^{2} = 10$$
$$c = \pm \sqrt{10}$$

Foci:
$$\left(-4 \pm \sqrt{10}, -2\right)$$

(d)
$$\frac{(x+2)^2}{9} - \frac{(y-2)^2}{4} = 1$$

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$$a^2 = 9$$

(d)
$$\frac{(x+2)^2}{9} - \frac{(y-2)^2}{4} = 1$$

$$a^2 = 9$$

$$a = \pm 3$$

(d)
$$\frac{(x+2)^2}{9} - \frac{(y-2)^2}{4} = 1$$

$$a^2 = 9$$

$$a = \pm 3$$

Vertices:
$$(-2 \pm 3, 2)$$

(d)
$$\frac{(x+2)^2}{9} - \frac{(y-2)^2}{4} = 1$$

$$a^2 = 9$$

$$a = \pm 3$$

Vertices:
$$(-2 \pm 3, 2) \longrightarrow (-5, 2)$$
 and $(1, 2)$

$$c^2 = a^2 + b^2$$

$$c^2 = a^2 + b^2$$
$$c^2 = 9 + 4$$

$$c^2 = 9 + 4$$

$$c^2 = a^2 + b^2$$

$$c^2 = 9 + 4$$

$$c^2 = 13$$

$$c^{2} = a^{2} + b^{2}$$

$$c^{2} = 9 + 4$$

$$c^{2} = 13$$

$$c = \pm \sqrt{13}$$

$$c^{2} = a^{2} + b^{2}$$
$$c^{2} = 9 + 4$$
$$c^{2} = 13$$
$$c = \pm \sqrt{13}$$

Foci:
$$\left(-2\pm\sqrt{13},2\right)$$

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Find the vertices and foci for a hyperbola in standard form.

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