# Rational Equations and Inequalities

# Objectives

Solve rational equations

Solve rational inequalities

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However, because our fractions contain variables in the denominator, we must remember that the denominator can never equal zero.

Thus, we must always check for extraneous solutions when solving rational equations and inequalities.

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$$x = 1 - 5(x+5)$$
 
$$x = 1 - 5x - 25$$

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Since  $x \neq -1$  from the domain, our final answer is x = 2.

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$$\frac{1}{3x-15} = \frac{1}{x^2-2x-15} + \frac{x^2}{3x^2-6x-45}$$

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$$x \neq 5, -3 \qquad \text{LCD is } 3(x - 5)(x + 3)$$
$$(3(x - 5)(x + 3)) \left(\frac{1}{3(x - 5)}\right)$$

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$$(3(x - 5)(x + 3)) \left(\frac{1}{3(x - 5)}\right) = x + 3$$
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$$\left(\frac{1}{(x - 5)(x + 3)} + \frac{x^2}{3(x - 5)(x + 3)}\right) (3(x - 5)(x + 3))$$
$$= 3 + x^2$$

$$3 + x^2 = x + 3$$

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$$x(x - 1) = 0$$
$$x = 0, 1$$

## Objectives

Solve rational equations

Solve rational inequalities

### Rational Inequalities

We will continue the theme of solving inequalities like equations, setting up a number line, and using test values.

However, in addition to the answers we get from treating the inequality like an equation, we must also use the values outside the domain (i.e. where the denominator equals zero) on our number line.

Solve each of the following and graph your solution on a number line.

(a) 
$$\frac{1}{5x} < \frac{1}{5x^2} - \frac{x+5}{x^2}$$

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$$x < -4$$

$$(b) \quad \frac{5}{3} - \frac{1}{x} \ge \frac{1}{3x}$$

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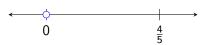
(b) 
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From Example 1b, we got  $x = \frac{4}{5}$  and  $x \neq 0$ 

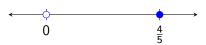
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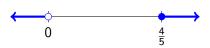
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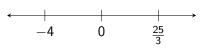
$$x < 0$$
 or  $x \ge \frac{4}{5}$ 

(c) 
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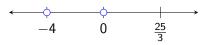
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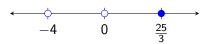
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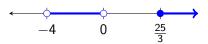
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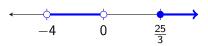
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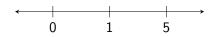
$$-4 < x < 0$$
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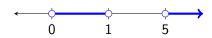
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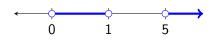
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(d) 
$$\frac{1}{x^2 - x} + \frac{1}{x} > \frac{5}{x^2 - x}$$
$$\frac{1}{x^2 - x} + \frac{1}{x} = \frac{5}{x^2 - x}$$



(d) 
$$\frac{1}{x^2 - x} + \frac{1}{x} > \frac{5}{x^2 - x}$$
$$\frac{1}{x^2 - x} + \frac{1}{x} = \frac{5}{x^2 - x}$$



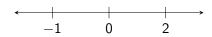
$$0 < x < 1$$
 or  $x > 5$ 

(e) 
$$1 \le \frac{2}{x^2 + x} + \frac{2}{x + 1}$$

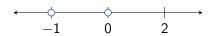
(e) 
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$$1 = \frac{2}{x^2 + x} + \frac{2}{x + 1}$$

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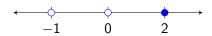
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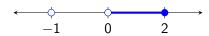
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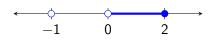
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$$0 < x \le 2$$

(f) 
$$\frac{1}{3x-15} \ge \frac{1}{x^2-2x-15} + \frac{x^2}{3x^2-6x-45}$$

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$$\frac{1}{3x - 15} \ge \frac{1}{x^2 - 2x - 15} + \frac{x^2}{3x^2 - 6x - 45}$$
$$\frac{1}{3x - 15} = \frac{1}{x^2 - 2x - 15} + \frac{x^2}{3x^2 - 6x - 45}$$

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