# Honors Algebra 2



# **Extra Practice Problems**

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# **Equations and Inequalities**

#### **Equations**

Solve each equation. For decimal equations, round your answers to 2 decimal places.

1. 
$$-7x + 5 = -10x + 11$$

2. 
$$\frac{2}{3}x - 10 = \frac{5}{8}$$

3. 
$$-0.2x - 3(x + 1.4) = -5.2x + 1$$

4. 
$$1.3 + 2.1(6.3x + 12) = -19.7$$

5. 
$$\frac{1}{4}x + \frac{3}{7} = -2\left(x + \frac{3}{8}\right)$$

6. 
$$\frac{1}{3} \left( \frac{2}{5}x - \frac{4}{7} \right) = 3x - 8$$

Solve each for the variable indicated.

7. 
$$F = ma$$
; for a

8. 
$$PV = nRT$$
; for  $n$ 

9. 
$$m = \frac{y_2 - y_1}{x_2 - x_1}$$
; for  $y_2$ 

10. 
$$m = \frac{y_2 - y_1}{x_2 - x_1}$$
; for  $y_1$ 

11. 
$$v = v_0 + gt$$
; for  $t$ 

12. 
$$S = 180(n-2)$$
; for  $n$ 

#### **Inequalities**

Solve each inequality. Graph your answers on a number line.

1. 
$$2(x+2) \le 4x - 2(x-1)$$

2. 
$$-3.2x - 5(x - 1.5) > 7.7 + 1.8x$$

#### **Equations**

1. 
$$x = 2$$

4. 
$$x \approx -3.49$$

7. 
$$a = \frac{F}{m}$$

10. 
$$y_1 = y_2 - m(x_2 - x_1)$$

2. 
$$x = \frac{255}{16}$$

5. 
$$x = -\frac{11}{21}$$

8. 
$$n = \frac{PV}{RT}$$

11. 
$$t = \frac{v - v_0}{g}$$

3. 
$$x = 2.6$$

6. 
$$x = \frac{820}{301}$$

9. 
$$y_2 = m(x_2 - x_1) + y_1$$

12. 
$$n = \frac{s}{180} + 2$$





# **Compound Inequalities**

Solve each. Graph your answers on a number line.

1. 
$$-3 < x - 8 \le 12$$

4. 
$$x - 1.5 > 8$$
 or  $-x + 2 > 9$  5.  $4 \le x + 7 < 9$ 

7. 
$$3x > 9$$
 or  $-5x > 25$ 

10. 
$$-5x + 9 \ge 12$$
 or  $2x + 6 > 5$ 

2. 
$$7 \le 2x - 5 < 18$$

5. 
$$4 < x + 7 < 9$$

8. 
$$8x + 12 \le 20$$
 or  $x + 12 > 9$  9.  $-8 \le 3x + 7 < 40$ 

10. 
$$-5x + 9 \ge 12$$
 or  $2x + 6 > 5$  11.  $3x - 1 < x + 5$  or  $-x \ge 5 + 7x$ 

3. 
$$x + 8 < 10$$
 or  $5x - 9 \ge 26$ 

6. 
$$-2 < 6x + 10 \le 5$$

9. 
$$-8 \le 3x + 7 < 40$$

- 1.  $5 < x \le 20$
- 4. x < -7 or  $x > \frac{19}{2}$
- 7. x < -5 or x > 3
- 8. ℝ
- 10.  $x \le -\frac{3}{5}$  or  $x > -\frac{1}{2}$

- 2.  $6 \le x < \frac{23}{2}$
- 5.  $-3 \le x < 2$
- 9.  $-5 \le x < 11$



11.

- 3.  $x < 2 \text{ or } x \ge 7$
- 6.  $-2 < x \le -\frac{5}{6}$



12. *x* < 3



# **Absolute Value Equations and Inequalities**

#### 3.1 Absolute Value Equations

Solve each of the following.

1. 
$$|2x| = 10$$

4. 
$$|x + 7| = 9$$

7. 
$$\left| \frac{1}{2}x + 2 \right| = x - 3$$

2. 
$$|3x - 7| = 8$$

5. 
$$|8x + 16| = -24$$

8. 
$$\left| \frac{3}{4}x + 2 \right| = 19$$

3. 
$$|5x + 1| = -4$$

6. 
$$|-x-4|=-3$$

9. 
$$-5|-3x+5|=-30$$

#### 3.2 Absolute Value Inequaltiies

Solve each. Graph your answers on a number line.

1. 
$$|x-9| < 10$$

4. 
$$|6x - 18| < 42$$

7. 
$$|3x + 2| > 1$$

10. 
$$3\left|\frac{1}{3}x+9\right| > 27$$

13. 
$$|3x+1| > -2x+2$$

2. 
$$|-x+1| \ge 7$$

5. 
$$|-2x+1| \ge 9$$

8. 
$$|2x - 1| \le 7$$

11. 
$$|0.1x + 5.4| < 4.7$$

14. 
$$-5|x+7| < -15$$

3. 
$$|x+8| < -1$$

6. 
$$|5x + 2| < 3x$$

9. 
$$|2x - 8| \le 3x$$

12. 
$$|2x - 5| \le 12$$

15. 
$$|-2x-5| \ge x+1$$

#### **Absolute Value Equations**

1. 
$$x = \pm 5$$

4. 
$$x = 2$$
 or  $x = -16$ 

7. 
$$x = 10$$

2. 
$$x = -\frac{1}{3}$$
 or  $x = 5$ 

8. 
$$x = -28$$
 or  $x = \frac{68}{3}$ 

9. 
$$x = -\frac{1}{3}$$
 or  $x = \frac{11}{3}$ 

#### **Absolute Value Inequalities**

1. 
$$-1 < x < 19$$



2. 
$$x \le -6 \text{ or } x \ge 8$$



3. ∅



4. 
$$-4 < x < 10$$



5. 
$$x \le -4 \text{ or } x \ge 5$$





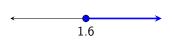
7. 
$$x < -1$$
 or  $x > \frac{1}{3}$ 



8. 
$$-3 \le x \le 4$$



9. 
$$x \ge 1.6$$



10. 
$$x < -54$$
 or  $x > 0$ 



11. 
$$-101 < x < -7$$



12. 
$$-3.5 \le x \le 8.5$$



13. 
$$x < -3$$
 or  $x > \frac{1}{5}$ 



14. 
$$x < -10$$
 or  $x > -4$ 



15. 
$$x = \mathbb{R}$$



# **Factoring Techniques**

Factor each completely.

1. 
$$x^2 + 2x - 15$$

2. 
$$a^2 - 15a + 56$$

3. 
$$8x^2 + 10x + 3$$

4. 
$$w^2 + w - 12$$

5. 
$$5b^2 - 9b - 2$$

6. 
$$12x^2 + 40x - 7$$

7. 
$$4x^2 - 4x - 24$$

8. 
$$18t^2 - 9t - 5$$

9. 
$$6a^2 + 23a + 21$$

10. 
$$x^2 - 12x + 36$$

11. 
$$9x^2 - 1$$

12. 
$$4x^2 + 4x + 1$$

13. 
$$x^3 - x^2 - 2x$$

14. 
$$6x^2 - 32x + 10$$

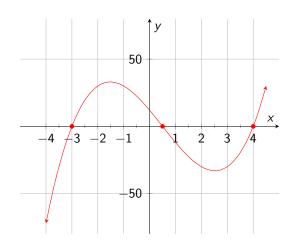
15. 
$$2x^3 - 9x^2 - 51x - 40$$
 16.  $2x^3 + 3x^2 - 3x - 2$ 

16. 
$$2x^3 + 3x^2 - 3x - 2$$

17. 
$$4x^3 + 3x^2 - 42x + 40$$

18. 
$$6x^3 - 27x^2 - 168x$$

19. The graph of a factorable expression is shown below. If the expression is in lowest terms (i.e. there is no number in front of all of the parentheses when it is factored) and contains integer coefficients, write the factored form of the expression.



- 1. (x+5)(x-3)
- 2. (a-8)(a-7)
- 3. (4x+3)(2x+1)
- 4. (w+4)(w-3)
- 5. (b-2)(5b+1)
- 6. (2x+7)(6x-1)
- 7. 4(x-3)(x+2)
- 8. (3t+1)(6t-5)
- 9. (3a+7)(2a+3)
- 10.  $(x-6)^2$
- 11. (3x-1)(3x+1)
- 12.  $(2x+1)^2$
- 13. x(x-2)(x+1)
- 14. 2(3x-1)(x-5)
- 15. (2x+5)(x+1)(x-8)
- 16. (x+2)(2x+1)(x-1)
- 17. (x+4)(4x-5)(x-2)
- 18. 3x(2x+7)(x-8)
- 19. (x+3)(2x-1)(x-4)

# The Quadratic Formula

Solve each. Exact answers only.

1. 
$$x^2 - 6x = -2$$

4. 
$$5x^2 + 6x - 2 = 3x^2 + 10$$

7. 
$$8x^2 - 2x - 7 = 3x + 1$$

10. 
$$3x^2 - 5x + 4 = 3$$

2. 
$$4x^2 + 7x - 1 = 0$$

5. 
$$7x^2 - 5 = 6x + 11$$

8. 
$$x^4 + 7x^2 - 5 = x^4 + 3x$$

3. 
$$8x^2 + 4x = 3$$

6. 
$$8x^2 + 2x + 1 = 7x^2 - 8x - 9$$

9. 
$$-8x^2 = 3x - 14$$

- 1.  $x = 3 \pm \sqrt{7}$
- 2.  $x = \frac{-7 \pm \sqrt{65}}{8}$
- 3.  $x = \frac{-1 \pm \sqrt{7}}{4}$
- 4.  $x = \frac{-3 \pm \sqrt{33}}{2}$
- 5.  $x = -\frac{8}{7}$ , x = 2
- 6.  $x = -5 \pm \sqrt{15}$
- 7.  $x = \frac{5 \pm \sqrt{281}}{16}$
- 8.  $x = \frac{3 \pm \sqrt{149}}{14}$
- 9.  $x = \frac{-3 \pm \sqrt{457}}{16}$
- 10.  $x = \frac{5 \pm \sqrt{13}}{6}$

# **Complex Numbers**

Simplify each.

1. 
$$(4-7i)+(-2+6i)$$

4. 
$$3(-2+7i)$$

7. 
$$\frac{3+i}{2-i}$$

10. 
$$\frac{2+3i}{4-5i}$$

13. 
$$\frac{3+2i}{8+9i}$$

2. 
$$(2-4i)-(2-3i)$$

5. 
$$(2+3i)(-2-5i)$$

8. 
$$3(7-4i)+2i(1+6i)$$
 9.  $(-2-6i)^2$ 

11. 
$$(2+3i)(-5+i)$$

14. 
$$\frac{-1+5i}{-9-2i}$$

3. 
$$6 - (8 + 4i)$$

6. 
$$(4+6i)(4-6i)$$

9. 
$$(-2-6i)^2$$

12. 
$$(-7-5i)^2$$

Solve each. Exact answers only.

15. 
$$3x^2 - 7x + 6 = 0$$

16. 
$$5x^2 - 3x + 2 = 0$$

17. 
$$3x^2 + 7x - 4 = 5x^2 + 2x + 5$$

- 1. 2 i
- 2. -i
- 3. -2-4i
- 4. -6 + 21i
- 5. 11 16*i*
- 6. 52
- 7. 1 + i
- 8. 9 10i
- 9. -32 + 24i
- 10.  $-\frac{7}{41} + \frac{22}{41}i$
- 11. -13 13i
- 12. 24 + 70i
- 13.  $\frac{42}{145} \frac{11}{145}i$
- 14.  $\frac{-1}{85} \frac{47}{85}i$
- 15.  $x = \frac{7 \pm i\sqrt{23}}{6}$
- 16.  $x = \frac{3 \pm i\sqrt{31}}{10}$
- 17.  $x = \frac{5 \pm i\sqrt{47}}{4}$

# **Graphs of Quadratic Expressions**

Identify the vertex and axis of symmetry for each.

1. 
$$y = 5x^2 - 15x + 7$$

2. 
$$y = x^2 + 8x - 1$$

3. 
$$y = \frac{1}{4}(x+3)^2 + 1$$

Write each of the following in general,  $y = ax^2 + bx + c$ , form.

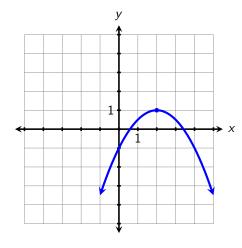
4. 
$$y = (x-7)^2 + 4$$

5. 
$$y = -3(x+2)^2 - 5$$

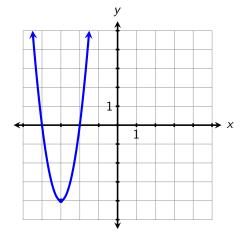
6. 
$$y = \frac{1}{4}(x-7)^2 + 1$$

Write each of the following in  $y = a(x - h)^2 + k$  and  $y = ax^2 + bx + c$  form.

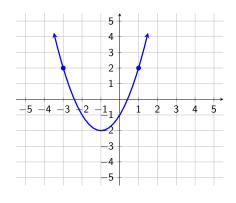
7.



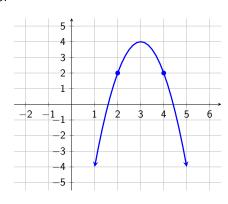
8.



9.



10.



- 1. Vertex:  $(\frac{3}{2}, -\frac{17}{4})$ ; Axis of Symmetry:  $x = \frac{3}{2}$
- 2. Vertex: (-4, -17); Axis of Symmetry: x = -4
- 3. Vertex: (-3, 1); Axis of Symmetry: x = -3
- 4.  $y = x^2 14x + 53$
- 5.  $y = -3x^2 12x 17$
- 6.  $y = \frac{1}{4}x^2 \frac{7}{2}x + \frac{53}{4}$
- 7.  $y = -\frac{1}{2}(x-2)^2 + 1 = -\frac{1}{2}x^2 + 2x 1$
- 8.  $y = 4(x+3)^2 4 = 4x^2 + 24x + 32$
- 9.  $y = (x+1)^2 2 = x^2 + 2x 1$
- 10.  $y = -2(x-3)^2 + 4 = -2x^2 + 12x 14$

# **Intro to Functions**

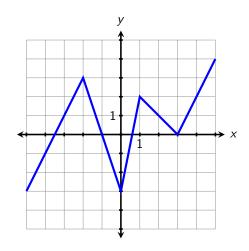
Evaluate each of the following given  $f(x) = \frac{x}{5} + 8$ .

1. f(9)

2. f(-1)

3. f(8)

Given the graph of f(x) below, find each of the following.



4. f(-5)

5. f(-4)

6. f(-1)

7. f(-2)

8. *f*(3)

9. f(4)

10. f(2)

11. f(0)

- 1.  $\frac{49}{5}$ 2.  $\frac{39}{5}$
- 3.  $\frac{48}{5}$
- 4. -3
- 5. -1
- 6. 0
- 7. 3
- 8. 0
- 9. 2
- 10. 1
- 11. -3

# **Operations with Functions**

Given  $f(x) = x^2 + 2x - 3$  and g(x) = 5x + 2, simplify or evaluate each.

1. 
$$(f+g)(x)$$

1. 
$$(f+g)(x)$$
 2.  $(f-g)(x)$  3.  $(g-f)(x)$ 

3. 
$$(g - f)(x)$$

4. 
$$(fg)(x)$$

5. 
$$\left(\frac{f}{g}\right)(x)$$

6. 
$$\left(\frac{g}{f}\right)(x)$$

7. 
$$(g+f)(7)$$

8. 
$$(fg)(0)$$

Given  $f(x) = x^2 + 5$  and g(x) = -3x - 2, find or evaluate each.

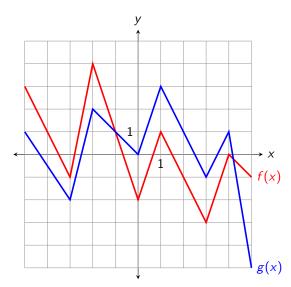
9. 
$$(f + g)(x)$$

10. 
$$(fg)(x)$$

11. 
$$(f-g)(4)$$

12. 
$$\left(\frac{f}{g}\right)$$
 (7)

Given the graph of f(x) and g(x), find each.



13. 
$$(f+g)(-2)$$

14. 
$$(f - \sigma)(1)$$

13. 
$$(f+g)(-2)$$
 14.  $(f-g)(1)$  15.  $(fg)(3)$  16.  $(g-f)(-5)$  17.  $(\frac{f}{g})(4)$  18.  $(\frac{g}{f})(-5)$ 

17. 
$$\left(\frac{f}{g}\right)$$
 (4)

18. 
$$\left(\frac{g}{f}\right)(-5)$$

Find the value of each of the following given the table below.

19. 
$$(f + g)(1$$

19. 
$$(f+g)(1)$$
 20.  $(f-g)(-2)$  21.  $(fg)(0)$ 

21. 
$$(fg)(0)$$

22. 
$$\binom{8}{f}$$
 (2)

22. 
$$(\frac{g}{f})(2)$$
 23.  $(g+g)(-3)$ 

- 1.  $x^2 + 7x 1$
- 2.  $x^2 3x 5$
- 3.  $-x^2 + 3x + 5$
- 4.  $5x^3 + 12x^2 11x 6$
- 5.  $\frac{x^2+2x+3}{5x+2}$
- 6.  $\frac{5x+2}{x^2+2x+3}$
- 7. 97
- 8. -6
- 9.  $x^2 3x + 3$
- 10.  $-3x^3 2x^2 15x 10$
- 11. 35
- 12.  $-\frac{54}{23}$
- 13. 6
- 14. -2
- 15. 3
- 16. -2
- 17. 0
- 18.  $\frac{1}{3}$
- 19. 0
- 20. 0
- 21. 4
- 22.  $-\frac{2}{3}$
- 23. -8

# **Compositions of Functions**

Given  $f(x) = x^2 + 5$  and g(x) = -3x - 2, find or evaluate each.

1. 
$$(f \circ g)(x)$$

2. 
$$(g \circ f)(x)$$

3. 
$$(f \circ f)(x)$$

4. 
$$g(g(x))$$

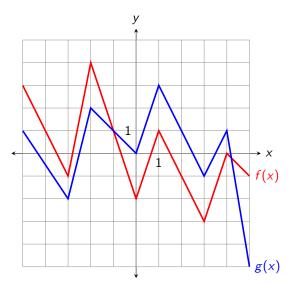
5. 
$$(f \circ g)(1)$$

6. 
$$(g \circ f)(-2)$$

7. 
$$(f \circ f)(0)$$

8. 
$$g(g(-8))$$

Given the graph of f(x) and g(x), find each.



9. 
$$(f \circ g)(0)$$

10. 
$$(g \circ f)(-5)$$

11. 
$$(f \circ f)(1)$$

12. 
$$(g(g(5)))$$

Find the value of each of the following given the table below.

13. 
$$(f \circ g)(1)$$

14. 
$$(g \circ f)(3)$$
 15.  $(f \circ f)(0)$ 

15. 
$$(f \circ f)(0)$$

16. 
$$g(g(4))$$

17. 
$$f(g(-1))$$

#### **Answer Key**

- 1.  $9x^2 + 12x + 9$
- 2.  $-3x^2 17$
- 3.  $x^4 + 10x^2 + 30$
- 4. 9x + 4
- 5. 30
- 6. -29
- 7. 30
- 8. -68
- 9. -2
- 10. -1
- 11. 1
- 12. 1
- 13. 0
- 14. 2
- 15. 1
- 16. -1
- 17. 3

#### **Function Transformations**

For the function  $f(x) = \sqrt{x}$ , write the resulting function g(x) after the final ordered sequence of transformations.

- 1. (1) Shift up 3 units
  - (2) Shift right 2 units
- 3. (1) Vertical compression by factor of 3
  - (2) Reflect across y-axis

- 2. (1) Shift left 3 units
  - (2) Reflect across x-axis
- 4. (1) Vertical stretch by factor of 4
  - (2) Shift down 7 units

- 1.  $g(x) = \sqrt{x-2} + 3$
- 2.  $g(x) = -\sqrt{x+3}$
- $3. g(x) = \frac{1}{3}\sqrt{-x}$
- 4.  $g(x) = 4\sqrt{x} 7$

# **Domain and Range**

State the domain and range of each.

1. 
$$f(x) = -\frac{1}{4}x - \frac{3}{7}$$

$$2. g(x) = \frac{1}{4+x}$$

3. 
$$h(x) = \sqrt{2x+5}-1$$

1. Domain:  $\mathbb{R}$  Range:  $\mathbb{R}$ 

2. Domain:  $x \neq -4$  Range:  $y \neq 0$ 

3. Domain:  $x \ge -\frac{5}{2}$  Range:  $y \ge -1$