

# Basic Set Theory and Interval Notation

# Sets

A **set** is a well-defined collection of things called *elements*. By “well-defined”, we mean that we will know whether or not an element belongs in the set.

# Ways of Describing Sets

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The **empty set** is a set with no elements (symbol is  $\emptyset$ ). This is notation used for “No Solution” answers.

# Table of Contents





- 1 Write a set using interval notation
- 2 Finding intersections and unions of intervals





# Interval Notation

Interval Notation	Set-Builder Notation	Graph
$(4, 9)$	$\{x \mid 4 < x < 9\}$	
$[4, 9]$	$\{x \mid 4 \leq x \leq 9\}$	
$[4, 9)$	$\{x \mid 4 \leq x < 9\}$	
$(4, 9]$	$\{x \mid 4 < x \leq 9\}$	

# Interval Notation

Interval Notation	Set-Builder Notation	Graph
$(4, \infty)$	$\{x \mid x > 4\}$	
$[4, \infty)$	$\{x \mid x \geq 4\}$	
$(-\infty, 9)$	$\{x \mid x < 9\}$	
$(-\infty, 9]$	$\{x \mid x \leq 9\}$	

# Interval Notation

Interval Notation	Set-Builder Notation	Graph
$(-\infty, \infty)$	$\mathbb{R}$	
$\emptyset$	$\{ \}$	

# Example 1

Express each interval in set-builder notation and graph:

(a)  $(-1, 4]$

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(a)  $(-1, 4]$



$$\{x \mid -1 < x \leq 4\}$$

## Example 1

(b)  $[2.5, 4]$

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(b)  $[2.5, 4]$



$$\{x \mid 2.5 \leq x \leq 4\}$$

## Example 1

(c)  $(-4, \infty)$

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(c)  $(-4, \infty)$



$$\{x \mid x > -4\}$$

# Example 1

(d)  $(-\infty, 5]$

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$$\{x \mid x \leq 5\}$$

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Intersections are common when the variable is *between* two values.

# Unions

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The union of sets  $A$  and  $B$  is denoted

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Unions are common when the intervals do not overlap (although they can).



## Example 2

Write each of the following in interval notation and graph.

(a)  $x \leq 4$  or  $x > 7$

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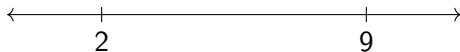
$$(-\infty, 4] \cup (7, \infty)$$

## Example 2

$$(b) \quad x < 2 \text{ or } x \geq 9$$

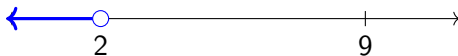
## Example 2

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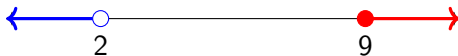
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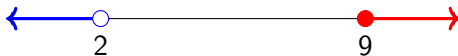
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$$(-\infty, 2) \cup [9, \infty)$$

## Example 2

$$(c) \quad 0 < x \leq 5$$

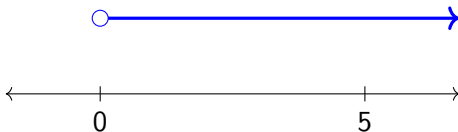
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(c)  $0 < x \leq 5$



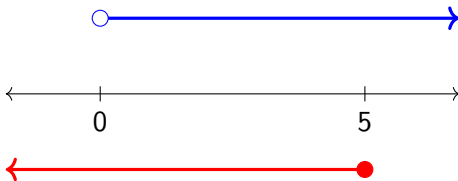
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$$(0, 5]$$

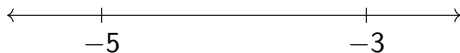


## Example 1

$$(d) \quad -5 \leq x \leq -3$$

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$$[-5, -3]$$

## Example 3

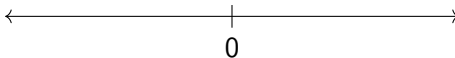
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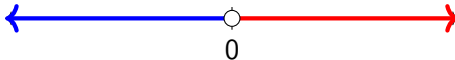




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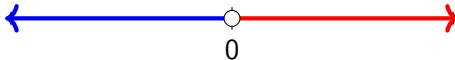
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$$(-\infty, 0) \cup (0, \infty)$$

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Write each of the following in interval notation and graph.

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$$(-\infty, 0) \cup (0, 2) \cup (2, \infty)$$

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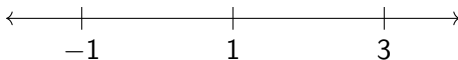
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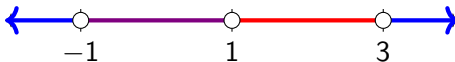




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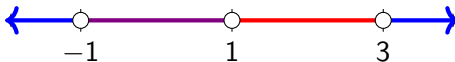
(c)  $\{x \mid x \neq -1, 1, 3\}$



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$$(-\infty, -1) \cup (-1, 1) \cup (1, 3) \cup (3, \infty)$$