Objectives

- 1 List the terms of an explicit sequence.
- 2 List the terms of a recursive sequence.
- Understand factorial notation
- 4 Find terms of an arithmetic sequence
- 5 Find terms of a geometric sequence

An sequence $\{a_n\}$ is a list of numbers written as a function whose domain is the set of non-negative integers (i.e. 0, 1, 2, ...).

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We will mostly stick with positive integers $(1, 2, 3, \ldots)$.

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We will mostly stick with positive integers $(1, 2, 3, \ldots)$.

The function values (**terms**) are $a_1, a_2, a_3, a_4, \ldots, a_n$; or $a_0, a_1, a_2, a_3, \ldots, a_n$ if using a starting value of 0.

The value a(n) is often written as a_n and is called the n^{th} term of the sequence.

The sequence is denoted by a_n or $\{a_n\}_{n=1}^{\infty}$.

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We list out the terms of a sequence by substituting values of n into the sequence's definition.

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We list out the terms of a sequence by substituting values of n into the sequence's definition.

Note: We can use any variable to name a sequence a_n , b_n , c_n , etc. We can also use any letter we want instead of n.

(a)
$$a_n = \frac{5^{n-1}}{3^n}$$

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$$a(1) = \frac{5^{1-1}}{3^1} = \frac{1}{3}$$

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$$a(1) = \frac{5^{1-1}}{3^1} = \frac{1}{3}$$

$$a(2) = \frac{5^{2-1}}{3^2} = \frac{5}{9}$$

(a)
$$a_n = \frac{5^{n-1}}{3^n}$$

$$a(1) = \frac{5^{1-1}}{3^1} = \frac{1}{3}$$

$$a(3) = \frac{5^{3-1}}{3^3} = \frac{25}{27}$$

$$a(2) = \frac{5^{2-1}}{3^2} = \frac{5}{9}$$

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$$a(2) = \frac{5^{2-1}}{3^2} = \frac{5}{9}$$

$$a(4) = \frac{5^{4-1}}{3^4} = \frac{125}{81}$$

(b)
$$b_k = \frac{(-1)^k}{2k+1}, \ k \ge 0$$

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$$b(0) = \frac{(-1)^0}{2(0)+1} = 1$$

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$$b(0) = \frac{(-1)^0}{2(0)+1} = 1$$

$$b(2) = \frac{(-1)^2}{2(2)+1} = \frac{1}{5}$$

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$$b(1) = \frac{(-1)^1}{2(1)+1} = -\frac{1}{3}$$

$$b(3) = \frac{(-1)^3}{2(3)+1} = -\frac{1}{7}$$

(c)
$$\{2n-1\}_{n=1}^{\infty}$$

(c)
$$\{2n-1\}_{n=1}^{\infty}$$

$$c(1) = 2(1) - 1 = 1$$

(c)
$$\{2n-1\}_{n=1}^{\infty}$$

$$c(1) = 2(1) - 1 = 1$$

$$c(2) = 2(2) - 1 = 3$$

(c)
$$\{2n-1\}_{n=1}^{\infty}$$

$$c(1) = 2(1) - 1 = 1$$

$$c(2) = 2(2) - 1 = 3$$

$$c(3) = 2(3) - 1 = 5$$

(c)
$$\{2n-1\}_{n=1}^{\infty}$$

$$c(1) = 2(1) - 1 = 1$$

$$c(2) = 2(2) - 1 = 3$$

$$c(3) = 2(3) - 1 = 5$$

$$c(4) = 2(4) - 1 = 7$$

$$(d) \quad \left\{ \frac{1 + (-1)^i}{i} \right\}_{i=2}^{\infty}$$

$$(\mathsf{d}) \quad \left\{ \frac{1 + (-1)^i}{i} \right\}_{i=2}^{\infty}$$

$$c(2) = \frac{1 + (-1)^2}{2} = 1$$

$$(d) \qquad \left\{ \frac{1 + (-1)^i}{i} \right\}_{i=2}^{\infty}$$

$$c(2) = \frac{1 + (-1)^2}{2} = 1$$

$$c(3) = \frac{1 + (-1)^3}{3} = 0$$

(d)
$$\left\{\frac{1+(-1)^i}{i}\right\}_{i=2}^{\infty}$$

$$c(2) = \frac{1 + (-1)^2}{2} = 1$$

$$c(4) = \frac{1 + (-1)^4}{4} = \frac{1}{2}$$

$$c(3) = \frac{1 + (-1)^3}{3} = 0$$

$$(\mathsf{d}) \quad \left\{ \frac{1 + (-1)^i}{i} \right\}_{i=2}^{\infty}$$

$$c(2) = \frac{1 + (-1)^2}{2} = 1$$

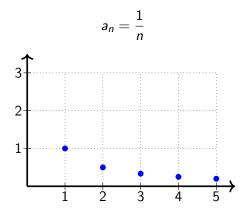
$$c(4) = \frac{1 + (-1)^4}{4} = \frac{1}{2}$$

$$c(3) = \frac{1 + (-1)^3}{3} = 0$$

$$c(5)=\frac{1+(-1)^5}{5}=0$$

Graphs of Sequences

We can graph a sequence by using coordinates.



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Recursive Sequences

A recursive sequence is one that is defined using previous terms.

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You are given a starting term value and then a rule for generating additional terms.

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You are given a starting term value and then a rule for generating additional terms.

The notations for successive terms are either

$$a_n$$
 and a_{n+1}

or

$$a_{n-1}$$
 and a_n

Write the first four terms of each sequence.

(a)
$$a_1 = 5$$
 and $a_n = 3a_{n-1} + 2$ for $n \ge 2$

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$$a_1 = 5$$
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Write the first four terms of each sequence.

(a)
$$a_1=5$$
 and $a_n=3a_{n-1}+2$ for $n\geq 2$ Each new term $= (3\times \text{previous term})+2$ $a_1=5$

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(a)
$$a_1=5$$
 and $a_n=3a_{n-1}+2$ for $n\geq 2$

Each new term $=(3\times \text{previous term})+2$

$$a_1=5 \qquad a_2=3(5)+2=17$$

$$a_3=3(17)+2=53$$

(a)
$$a_1 = 5$$
 and $a_n = 3a_{n-1} + 2$ for $n \ge 2$

Each new term $= (3 \times \text{previous term}) + 2$
 $a_1 = 5$
 $a_2 = 3(5) + 2 = 17$
 $a_3 = 3(17) + 2 = 53$
 $a_4 = 3(53) + 2 = 161$

(b)
$$a_1 = 7 \text{ and } a_{n+1} = 2 - a_n \text{ for } n \ge 1$$

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$$a_1=7$$
 and $a_{n+1}=2-a_n$ for $n\geq 1$ Each new term $=2$ - previous term

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$$a_1 = 7$$
 $a_2 = 2 - 7 = -5$

(b)
$$a_1 = 7 \text{ and } a_{n+1} = 2 - a_n \text{ for } n \ge 1$$

Each new term = 2 – previous term

$$a_1 = 7$$

$$a_2 = 2 - 7 = -5$$

$$a_3 = 2 - (-5) = 7$$

(b)
$$a_1 = 7 \text{ and } a_{n+1} = 2 - a_n \text{ for } n \ge 1$$

Each new term = 2 – previous term

$$a_1 = 7$$

$$a_2 = 2 - 7 = -5$$

$$a_3 = 2 - (-5) = 7$$

$$a_4 = 2 - 7 = -5$$

(c)
$$f_0 = 1$$
 and $f_n = n \cdot f_{n-1}$ for $n \ge 1$

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(c) $f_0 = 1$ and $f_n = n \cdot f_{n-1}$ for $n \ge 1$

$$f_0 = 1$$

$$f_1 = 1(1) = 1$$

(c) $f_0 = 1$ and $f_n = n \cdot f_{n-1}$ for $n \ge 1$

$$f_0 = 1$$

$$f_1 = 1(1) = 1$$

$$f_2=2(1)=2$$

(c) $f_0 = 1$ and $f_n = n \cdot f_{n-1}$ for $n \ge 1$

$$f_0 = 1$$

$$f_1 = 1(1) = 1$$

$$f_2 = 2(1) = 2$$

$$f_3=3(2)=6$$

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Factorial Notation

Products of consecutive positive integers can be expressed using factorial notation.

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If n is a positive integer, then

$$n! = n(n-1)(n-2)\cdots(3)(2)(1)$$

By definition, 0! = 1.

Factorial Values

Factorial values grow very quickly.

$$1! = 1$$

$$2! = 2 \cdot 1 = 2$$

$$3! = 3 \cdot 2 \cdot 1 = 6$$

$$4! = 4 \cdot 3 \cdot 2 \cdot 1 = 24$$

$$5! = 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 120$$

$$6! = 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 720$$

Grouping Symbols

Unless grouping symbols, like () are involved, factorials only affect the number or variable they follow.

$$2 \cdot 3! = 2(3 \cdot 2 \cdot 1) = 12$$
, but $(2 \cdot 3)! = 6! = 720$.

(a)
$$a_n = \frac{2^n}{(n-1)!}$$

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$$a_1 = \frac{2^1}{(1-1)!} = 2$$

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 $a_2 = \frac{2^2}{(2-1)!} = 4$

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$$a_2 = \frac{2^2}{(2-1)!} = 4$$

(a)
$$a_n = \frac{2^n}{(n-1)!}$$

$$a_1 = \frac{2^1}{(1-1)!} = 2$$

$$= 2 a_2 = \frac{2^2}{(2-1)!} = 4$$

$$a_3 = \frac{2^3}{(3-1)!} = 4$$

$$a_4 = \frac{2^4}{(4-1)!} = \frac{8}{3}$$

(b)
$$b_n = \frac{20}{(n+1)!}$$

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$$b_1 = \frac{20}{(1+1)!} = 10$$

$$b_3 = \frac{20}{(3+1)!} = \frac{5}{6}$$

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$$b_2 = \frac{20}{(2+1)!} = \frac{10}{3}$$

$$b_4 = \frac{20}{(4+1)!} = \frac{1}{6}$$

Simplifying Factorial Expressions

When simplifying factorial expressions, it helps to remember that

$$n! = n(n-1)(n-2)\cdots(3)(2)(1)$$

(a)
$$\frac{(n+1)!}{n!}$$

(a)
$$\frac{(n+1)!}{n!} = \frac{(n+1)(n)(n-1)(n-2)\cdots(2)(1)}{n(n-1)(n-2)\cdots(2)(1)}$$

(a)
$$\frac{(n+1)!}{n!} = \frac{(n+1)(n)(n-1)(n-2)\cdots(2)(1)}{n(n-1)(n-2)\cdots(2)(1)}$$
$$= \frac{(n+1)(n)(n-1)(n-2)\cdots(2)(1)}{(n)(n-1)(n-2)\cdots(2)(1)}$$

(a)
$$\frac{(n+1)!}{n!} = \frac{(n+1)(n)(n-1)(n-2)\cdots(2)(1)}{n(n-1)(n-2)\cdots(2)(1)}$$
$$= \frac{(n+1)(n)(n-1)(n-2)\cdots(2)(1)}{(n)(n-1)(n-2)\cdots(2)(1)}$$
$$= n+1$$

(b)
$$\frac{n!}{(n-1)!}$$

Simplify each.

(b)
$$\frac{n!}{(n-1)!}$$

$$\frac{n!}{(n-1)!} = \frac{n(n-1)(n-2)\cdots(2)(1)}{(n-1)(n-2)\cdots(2)(1)}$$

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$$= \frac{n(n-1)(n-2)\cdots(2)(1)}{(n-1)(n-2)\cdots(2)(1)}$$

$$= n$$

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Arithmetic Sequences

When the difference between consecutive terms of a sequence is always the same, such as 8, 11, 14, 17, ..., that sequence is an arithmetic sequence.

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When the difference between consecutive terms of a sequence is always the same, such as 8, 11, 14, 17, ..., that sequence is an arithmetic sequence.

The difference between those consecutive terms is called the common difference.

To find the common difference of an arithmetic sequence, **subtract** any two consecutive terms.

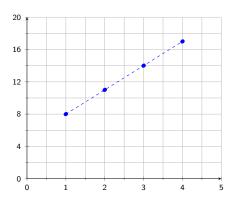
Arithmetic Sequences and Linear Functions

Arithmetic sequences model linear functions.

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Arithmetic sequences model linear functions.

The following graph shows the first 4 terms of the sequence 8, 11, 14, 17:



Find the Rule for the Sequence

Notice that the common difference between terms (3 in this case) is the same as the slope of the line.

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If we subtract that 3 from the first term, we get 5; which is the *y*-intercept of the graph.

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Notice that the common difference between terms (3 in this case) is the same as the slope of the line.

If we subtract that 3 from the first term, we get 5; which is the *y*-intercept of the graph.

Thus, a sequence rule for this sequence is

$$y = 3x + 5$$
 or $a_n = 3n + 5$ for $n > 1$

Find an explicit formula for the $n^{\rm th}$ term of each of the following sequences.

(a)
$$-31, -24, -17, -10, \dots$$

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Common Difference: -24 - (-31) = 7

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Common Difference:
$$-24 - (-31) = 7$$

y-intercept:
$$-31 - 7 = -38$$

Find an explicit formula for the n^{th} term of each of the following sequences.

(a)
$$-31, -24, -17, -10, \dots$$

Common Difference: -24 - (-31) = 7

y-intercept:
$$-31 - 7 = -38$$

$$a_n=7n-38$$

(b) 37, 67, 97, 127,...

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Common Difference: 67 - 37 = 30

(b) 37, 67, 97, 127,...

Common Difference: 67 - 37 = 30

y-intercept: 37 - 30 = 7

(b) 37, 67, 97, 127,...

Common Difference: 67 - 37 = 30

y-intercept: 37 - 30 = 7

$$b_n=30n+7$$

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Geometric Sequences

A geometric sequence is one in which each term after the first is obtained by multiplying the preceding term by a fixed nonzero constant r (called the **common ratio**).

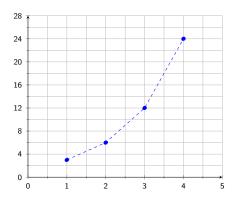
Geometric Sequences

A geometric sequence is one in which each term after the first is obtained by multiplying the preceding term by a fixed nonzero constant r (called the **common ratio**).

Geometric sequences model exponential growth or decay.

Model of a Geometric Sequence

The following graph shows the first 4 terms of the sequence 3, 6, 12, 24:



Notice each point's y-coordinate is twice the previous one. This indicates that the common ratio, r, is the base of the exponential function, or 2.

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To find the y-intercept, divide the first term by the base of 2 to get 1.5.

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To find the y-intercept, divide the first term by the base of 2 to get 1.5.

Thus, the function can be modeled as

$$y = 1.5(2)^x$$
 or $a_n = 1.5(2)^n$ for $n \ge 1$

Notice each point's y-coordinate is twice the previous one. This indicates that the common ratio, r, is the base of the exponential function, or 2.

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Thus, the function can be modeled as

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 or $a_n = 1.5(2)^n$ for $n \ge 1$

**Note: Unlike exponential functions, geometric sequences can have negative common ratios.

Find the 8th term of each geometric sequence.

(a)
$$a_1 = -4$$
 $r = -2$

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$$a_n=2\left(-2\right)^n$$

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$$a_1 = -4$$
 $r = -2$

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$$a_8 = 2(-2)^8$$

Find the 8th term of each geometric sequence.

(a)
$$a_1 = -4$$
 $r = -2$

$$a_n = 2\left(-2\right)^n$$

$$a_8=2\left(-2\right)^8$$

$$a_8 = 512$$

Find the 8th term of each geometric sequence.

(b)
$$a_1 = 80 \quad r = 0.5$$

Find the 8th term of each geometric sequence.

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Find the 8th term of each geometric sequence.

(b)
$$a_1 = 80 \quad r = 0.5$$

$$a_n=160\,(0.5)^n$$

Find the 8th term of each geometric sequence.

(b)
$$a_1 = 80 \quad r = 0.5$$

y-intercept: 160

$$a_n = 160 (0.5)^n$$

$$a_8 = 160 (0.5)^8$$

Find the 8th term of each geometric sequence.

(b)
$$a_1 = 80 \quad r = 0.5$$

y-intercept: 160

$$a_n = 160 (0.5)^n$$

$$a_8 = 160 (0.5)^8$$

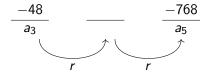
$$a_8=\frac{5}{8}$$

(c)
$$a_3 = -48$$
 $a_5 = -768$

(c)
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 $a_5 = -768$

$$-\frac{-48}{a_3}$$
 $-\frac{-768}{a_5}$

(c)
$$a_3 = -48$$
 $a_5 = -768$



(c)
$$a_3 = -48$$
 $a_5 = -768$

$$-48r^2 = -768$$

(c)
$$a_3 = -48$$
 $a_5 = -768$

$$-48r^2 = -768$$
$$r^2 = 16$$

(c)
$$a_3 = -48$$
 $a_5 = -768$

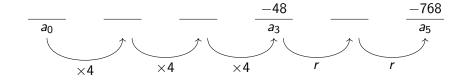
$$-48r^2 = -768$$
$$r^2 = 16$$
$$r = \pm 4$$

(c)
$$a_3 = -48$$
 $a_5 = -768$

$$\frac{-48}{a_0} \qquad \frac{-768}{a_5}$$

$$-48r^2 = -768$$
$$r^2 = 16$$
$$r = \pm 4$$

(c)
$$a_3 = -48$$
 $a_5 = -768$



$$-48r^2 = -768$$
$$r^2 = 16$$
$$r = \pm 4$$

$$64a_0 = -48$$

$$64a_0 = -48$$
$$a_0 = -0.75$$

$$64a_0 = -48$$

$$a_0 = -0.75$$

$$a_n = -0.75(4)^n$$

$$64a_0 = -48$$

$$a_0 = -0.75$$

$$a_n = -0.75(4)^n$$

$$a_8 = -0.75(4)^8$$

$$64a_0 = -48$$

$$a_0 = -0.75$$

$$a_n = -0.75(4)^n$$

$$a_8 = -0.75(4)^8$$

$$= -49, 152$$

(d)
$$a_1 = 5$$
 $a_4 = 16.875$

(d)
$$a_1 = 5$$
 $a_4 = 16.875$ $5r^3 = 16.875$

(d)
$$a_1 = 5$$
 $a_4 = 16.875$ $5r^3 = 16.875$ $r^3 = 3.375$

(d)
$$a_1 = 5$$
 $a_4 = 16.875$
$$5r^3 = 16.875$$

$$r^3 = 3.375$$

$$r = 1.5$$

(d)
$$a_1 = 5$$
 $a_4 = 16.875$
$$5r^3 = 16.875$$

$$r^3 = 3.375$$

$$r = 1.5$$

$$a_0 = 5/1.5$$

(d)
$$a_1 = 5$$
 $a_4 = 16.875$ $5r^3 = 16.875$ $r^3 = 3.375$ $r = 1.5$ $a_0 = 5/1.5$ $a_0 = \frac{10}{3}$

$$a_n = \frac{10}{3} \left(1.5\right)^n$$

$$a_n = \frac{10}{3} \left(1.5 \right)^n$$

$$a_8 = \frac{10}{3} (1.5)^8$$

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$$a_8 = \frac{10}{3} (1.5)^8$$

$$= \frac{10,935}{128}$$

Write an explicit rule for each geometric sequence.

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 $Common\ ratio = 6/3 = 2$

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$$y$$
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Common ratio
$$= 6/3 = 2$$

$$y$$
-intercept = 1.5

$$a_n=1.5(2)^n$$

(b)
$$2, -10, 50, -250, 1250, \dots$$

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$$2, -10, 50, -250, 1250, \dots$$

$$Common\ ratio = -10/2 = -5$$

(b)
$$2, -10, 50, -250, 1250, \dots$$

Common ratio =
$$-10/2 = -5$$

y-intercept =
$$-\frac{2}{5}$$

(b)
$$2, -10, 50, -250, 1250, \dots$$

Common ratio =
$$-10/2 = -5$$

y-intercept
$$=-rac{2}{5}$$

$$b_n=-rac{2}{5}\left(-5
ight)^n$$