

Functions and Their Graphs

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Determine if the relation represents a function. For those that are, state the domain and range.

1. $\{(-3, 9), (-2, 4), (-1, 1), (0, 0), (1, 1), (2, 4), (3, 9)\}$ 2. $\{(-3, 0), (1, 6), (2, -3), (4, 2), (-5, 6), (4, -9), (6, 2)\}$

Determine if each represent y as a function of x .

3. $y = x^3 - x$ 4. $x^2 - y^2 = 1$ 5. $x = 4$ 6. $y = x^2 + 4$

Find an expression for $f(x)$ of each given the function's description.

7. (1) add 3; (2) multiply by 2; (3) divide by 4
8. (1) subtract 5; (2) take the square root; (3) multiply by -1
9. (1) multiply by -1 ; (2) take the square root; (3) subtract 5

Given $f(x) = 2x^2 - 5$, simplify or evaluate each.

10. $f(3)$ 11. $f(0)$ 12. $f(-2)$
13. $f(2x)$ 14. $f(-x)$ 15. $f(x + 1)$

Find the domain of each. Write your answers in interval notation.

16. $f(x) = x^2 + 4$

17. $f(x) = \frac{x-2}{x+1}$

18. $f(x) = \frac{3x}{x^2 + x - 2}$

19. $f(x) = \sqrt{2x+5}$

20. $f(x) = \sqrt[3]{6x-2}$

21. $f(x) = \frac{\sqrt{6x-2}}{x^2-36}$

Find the intercepts (both x - and y -) of each.

22. $y = x^2 + 1$

23. $y = \sqrt{x-2}$

24. $y = x^2 - 2x - 8$

Key

1. Yes. Domain: $\{-3, -2, -1, 0, 1, 2, 3\}$. Range = $\{9, 4, 1, 0\}$
2. Not a function.
3. Yes.
4. No.
5. No.
6. Yes.
7. $f(x) = \frac{2(x+3)}{4} = \frac{2x+6}{4}$
8. $f(x) = -\sqrt{x-5}$
9. $f(x) = \sqrt{-x} - 5$
10. 13
11. -5
12. 3
13. $8x^2 - 5$
14. $2x^2 - 5$
15. $2x^2 + 4x - 3$
16. $(-\infty, \infty)$
17. $(-\infty, -1) \cup (-1, \infty)$
18. $(-\infty, -2) \cup (-2, 1) \cup (1, \infty)$
19. $[-\frac{5}{2}, \infty)$
20. $(-\infty, \infty)$
21. $[\frac{1}{3}, 6) \cup (6, \infty)$
22. No x -intercepts; y -intercept: $(0, 1)$
23. x -intercept: $(2, 0)$; No y -intercept
24. x -intercepts: $(4, 0)$ and $(-2, 0)$; y -intercept: $(0, -8)$