

**Functions and Their Graphs**

\_\_\_\_\_ / 10

Determine if the relation represents a function. For those that are, state the domain and range.

1.  $\{(-3, 9), (-2, 4), (-1, 1), (0, 0), (1, 1), (2, 4), (3, 9)\}$       2.  $\{(-3, 0), (1, 6), (2, -3), (4, 2), (-5, 6), (4, -9), (6, 2)\}$

Determine if each represent  $y$  as a function of  $x$ .

3.  $y = x^3 - x$       4.  $x^2 - y^2 = 1$       5.  $x = 4$       6.  $y = x^2 + 4$

Find an expression for  $f(x)$  of each given the function's description.

7. (1) add 3; (2) multiply by 2; (3) divide by 4
8. (1) subtract 5; (2) take the square root; (3) multiply by  $-1$
9. (1) multiply by  $-1$ ; (2) take the square root; (3) subtract 5

Given  $f(x) = 2x^2 - 5$ , simplify or evaluate each.

10.  $f(3)$       11.  $f(0)$       12.  $f(-2)$
13.  $f(2x)$       14.  $f(-x)$       15.  $f(x + 1)$

Find the domain of each. Write your answers in interval notation.

16.  $f(x) = x^2 + 4$

17.  $f(x) = \frac{x-2}{x+1}$

18.  $f(x) = \frac{3x}{x^2 + x - 2}$

19.  $f(x) = \sqrt{2x+5}$

20.  $f(x) = \sqrt[3]{6x-2}$

21.  $f(x) = \frac{\sqrt{6x-2}}{x^2-36}$

Find the intercepts (both  $x$ - and  $y$ -) of each.

22.  $y = x^2 + 1$

23.  $y = \sqrt{x-2}$

24.  $y = x^2 - 2x - 8$

## Key

1. Yes. Domain:  $\{-3, -2, -1, 0, 1, 2, 3\}$ . Range =  $\{9, 4, 1, 0\}$
2. Not a function.
3. Yes.
4. No.
5. No.
6. Yes.
7.  $f(x) = \frac{2(x+3)}{4} = \frac{2x+6}{4}$
8.  $f(x) = -\sqrt{x-5}$
9.  $f(x) = \sqrt{-x} - 5$
10. 13
11. -5
12. 3
13.  $8x^2 - 5$
14.  $2x^2 - 5$
15.  $2x^2 + 4x - 3$
16.  $(-\infty, \infty)$
17.  $(-\infty, -1) \cup (-1, \infty)$
18.  $(-\infty, -2) \cup (-2, 1) \cup (1, \infty)$
19.  $[-\frac{5}{2}, \infty)$
20.  $(-\infty, \infty)$
21.  $[\frac{1}{3}, 6) \cup (6, \infty)$
22. No  $x$ -intercepts;  $y$ -intercept:  $(0, 1)$
23.  $x$ -intercept:  $(2, 0)$ ; No  $y$ -intercept
24.  $x$ -intercepts:  $(4, 0)$  and  $(-2, 0)$ ;  $y$ -intercept:  $(0, -8)$