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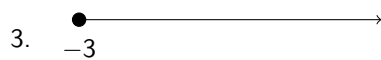
# Chapter 1

## Basic Set Theory and Interval Notation

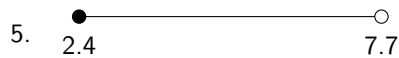
You are given either interval notation, set-builder notation, or a graph. Write each of the following in its other 2 forms.

1.  $(-5, 8]$

2.  $\{x|x \leq 1\}$



4.  $\{x|x \neq 4, 11\}$



6.  $(9, \infty)$

Write each using interval notation and graph on a number line.

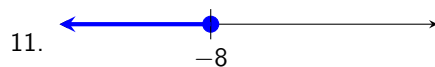
7.  $\{x|x \geq 2\}$

8.  $\{x|x < -8\}$

9.  $\{x|x \neq 3\}$

10.  $\{x|x \neq -2, 5\}$

You are given the graph of an interval. Write the interval and set-builder notation for it.

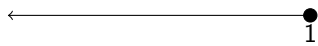


# BASIC SET THEORY AND INTERVAL NOTATION KEY

1.  $\{x | -5 < x \leq 8\}$

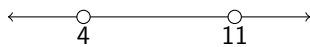


2.  $(-\infty, 1]$



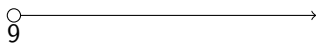
3.  $[-3, \infty)$   $\{x | x \geq -3\}$

4.  $(-\infty, 4) \cup (4, 11) \cup (11, \infty)$

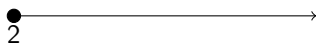


5.  $[2.4, 7.7)$   $\{x | 2.4 \leq x < 7.7\}$

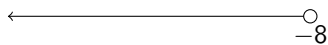
6.  $\{x | x > 9\}$



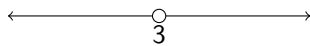
7.  $[2, \infty)$



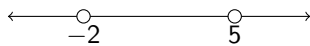
8.  $(-\infty, -8)$



9.  $(-\infty, 3) \cup (3, \infty)$



10.  $(\infty, -2) \cup (-2, 5) \cup (5, \infty)$



11.  $(-\infty, -8]$   $\{x | x \leq -8\}$

12.  $(-\infty, 7) \cup (7, 12) \cup (12, \infty)$   $\{x | x \neq 7, 12\}$

## Chapter 2

# Functions and Their Graphs

### 2.1 Evaluating Functions

Given  $f(x) = -3x^2 + 4x$  and  $g(x) = \frac{1}{x} - 5$ , evaluate each.

1.  $f(5)$
2.  $f(-2)$
3.  $f(0)$
4.  $g(1)$
5.  $g(-5)$
6.  $g(1/4)$

### 2.2 Domain of Functions

Find the domain of each write your answers in interval notation.

- |                                   |  |
|-----------------------------------|--|
| 1. $f(x) = -8x^2 - 7x + 1$        | 12. $f(x) = -\frac{x+7}{x^2-5x-6}$     |
| 2. $g(x) = \sqrt{5x+12} - 2$      | 13. $g(x) = \sqrt{2x+3}$               |
| 3. $h(x) = \frac{x+2}{9x-7}$      | 14. $h(x) = \sqrt[3]{2x+3}$            |
| 4. $f(x) = -5x + 4$               | 15. $f(x) = -\frac{7x-10}{x^2+3x+2}$   |
| 5. $f(x) = x^2 + 2$               | 16. $g(x) = \sqrt{-9x+8}$              |
| 6. $f(x) = \frac{2x+1}{3x-5}$     | 17. $h(x) = -\sqrt[3]{4x+1}$           |
| 7. $f(x) = \sqrt{3x-12}$          | 18. $f(x) = \sqrt[3]{8x+1}$            |
| 8. $f(x) = \frac{x}{x^2-16}$      | 19. $g(x) = \frac{x^2-1}{\sqrt{x+3}}$  |
| 9. $f(x) = \frac{x+4}{x^3-4x}$    | 20. $h(x) = \frac{3}{9+\frac{4}{x+7}}$ |
| 10. $f(x) = \frac{x}{\sqrt{x-4}}$ | 21. $f(x) = \frac{x+1}{\sqrt{10x+8}}$  |
| 11. $f(x) = \frac{x^2+1}{2x^2+8}$ | 22. $g(x) = \frac{5}{1+\frac{3}{x+2}}$ |

### 2.3 Piecewise Functions

Find the value of each given the piecewise function below. Use exact answers when possible.

$$f(x) = \begin{cases} x^2 - 1 & \text{if } x < -3 \\ 0.2x + 7 & \text{if } -3 \leq x < 2 \\ \sqrt{5x} & \text{if } x \geq 2 \end{cases}$$

1.  $f(3)$
2.  $f(0)$
3.  $f(-2)$
4.  $f(-3)$
5.  $f(0.5)$

Find each of the following given the piecewise function

$$f(x) = \begin{cases} x^2 - 7 & x \leq -4 \\ \sqrt{2x + 7} & -4 < x < 0 \\ |-x - 1| & x \geq 0 \end{cases}$$

6.  $f(3)$
7.  $f(-2)$
8.  $f(0)$
9.  $f(-5)$

## Evaluating Functions

1.  $-55$
2.  $-20$
3.  $0$
4.  $-4$
5.  $-5.2$
6.  $-1$

## Domain of Functions

1.  $(-\infty, \infty)$
2.  $[-\frac{12}{5}, \infty)$
3.  $(-\infty, \frac{7}{9}) \cup (\frac{7}{9}, \infty)$
4.  $(-\infty, \infty)$
5.  $(-\infty, \infty)$
6.  $(-\infty, \frac{5}{3}) \cup (\frac{5}{3}, \infty)$
7.  $[4, \infty)$
8.  $(-\infty, -4) \cup (-4, 4) \cup (4, \infty)$
9.  $(-\infty, -2) \cup (-2, 0) \cup (0, 2) \cup (2, \infty)$
10.  $(4, \infty)$
11.  $(-\infty, \infty)$
12.  $(-\infty, -1) \cup (-1, 6) \cup (6, \infty)$
13.  $[-\frac{3}{2}, \infty)$
14.  $(-\infty, \infty)$
15.  $(-\infty, -2) \cup (-2, -1) \cup (-1, \infty)$
16.  $(-\infty, \frac{8}{9}]$
17.  $(-\infty, \infty)$
18.  $(-\infty, \infty)$
19.  $(-3, \infty)$
20.  $(-\infty, -\frac{67}{9}) \cup (-\frac{67}{9}, -7) \cup (-7, \infty)$
21.  $(-\frac{4}{5}, \infty)$
22.  $(\infty, -5) \cup (-5, -2) \cup (-2, \infty)$

## Piecewise Functions

1.  $\sqrt{15} \approx 3.873$
2.  $7$
3.  $6.6$
4.  $6.4$
5.  $7.1$
6.  $4$
7.  $\sqrt{3} \approx 1.732$
8.  $1$
9.  $18$

## Chapter 3

# Properties of Functions

### 3.1 Maxima and Minima

Find the coordinates of the any relative maxima or minima. Round to 3 decimal places when necessary.

1.  $f(x) = x^2 - 3x^2 + 5$

2.  $g(x) = -0.4x^3 + 0.6x^2 + 3x - 2$

3.  $f(x) = -x^4 + 3x^2 - 2x + 6$

4.  $g(x) = 0.25x^5 - 0.1x^4 + 2x^2 - 6x$

5.  $f(x) = -4x^3 + 2x^2 + 10x + 4$

6.  $g(x) = x^4 - 4x^3 + 3x^2 + 4x - 4$

7. The concentration  $C$  of a medication in the bloodstream  $t$  hours after being administered can be modeled by

$$C(t) = -0.002t^4 + 0.039t^3 - 0.285t^2 + 0.766t + 0.085, \quad t \geq 0$$

After how many hours will the concentration be the highest?

### 3.2 Increasing, Decreasing, and Constant Intervals

Find the intervals in which each is increasing or decreasing. Round to 3 decimal places when necessary.

1.  $f(x) = x^2 - 3x^2 + 5$

2.  $g(x) = -0.4x^3 + 0.6x^2 + 3x - 2$

3.  $f(x) = x^3 + 2x^2 - 4x - 8$

4.  $g(x) = x^4 - 2x^2 + 1$

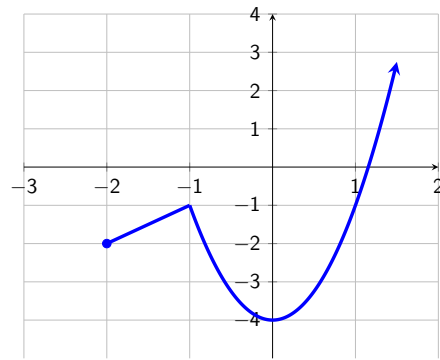
5.  $h(x) = \sqrt{x+1} - 2$

6.  $f(x) = -4x^3 + 2x^2 + 10x + 4$

7.  $g(x) = x^4 - 4x^3 + 3x^2 + 4x - 4$

### 3.3 Miscellaneous

Use the graph of  $y = f(x)$  below to answer questions 1–10. Write your answers using interval notation.



1. Domain of  $f$

2. Range of  $f$

3. Relative Minimum

4. Relative Maximum

5.  $f(1)$

6.  $f(0)$

7. Increasing Interval(s)

8. Decreasing Interval(s)

9. Absolute Maximum

10. Absolute Minimum

Find each of the following given  $f(x) = -2x^3 + 6x^2 - 5x + 1$ . Round to 3 decimal places and use interval notation when applicable.

11.  $f(7)$

12.  $f(-2)$

13. Rel. Max

14. Rel. Min

15. Global Max

16. Global Min

17. Increasing Interval(s)

18. Decreasing Interval(s)



## Maxima and Minima

1. Rel max @  $(0, 5)$ ; No rel min
2. Rel max @  $(2.158, 3.248)$ ; Rel min @  $(-1.158, -4.048)$
3. Rel Max  $(-1.366, 10.848)$  and  $(1, 6)$ ; Rel Min  $(0.366, 5.652)$
4. Rel Max  $(-1.716, 11.598)$ ; Rel Min  $(1.132, -3.929)$
5. Rel Max:  $(1.095, 12.096)$ ; Rel Min  $(-0.761, -0.680)$
6. Rel Max:  $(1.366, 0.348)$ ; Rel Min:  $(-0.366, -4.848)$  and  $(2, 0)$
7. About 2.16 hours

## Increasing, Decreasing, and Constant Intervals

1. Increasing:  $(-\infty, 0)$  Decreasing:  $(0, \infty)$
2. Increasing:  $(-1.158, 2.158)$  Decreasing:  $(-\infty, -1.158) \cup (2.158, \infty)$
3. Inc:  $(-\infty, -2) \cup (\frac{2}{3}, \infty)$  Dec:  $(-2, \frac{2}{3})$
4. Inc:  $(-1, 0) \cup (1, \infty)$  Dec:  $(-\infty, -1) \cup (0, 1)$
5. Inc:  $(-1, \infty)$  No intervals where it is decreasing
6. Inc:  $(-0.761, 1.095)$ ; Dec:  $(-\infty, -0.761) \cup (1.095, \infty)$
7. Inc:  $(-0.366, 1.366) \cup (2, \infty)$ ; Dec:  $(-\infty, -0.366) \cup (1.366, 2)$

## Miscellaneous

1.  $[-2, \infty)$
2.  $[-4, \infty)$
3.  $(0, -4)$
4.  $(-1, -1)$
5.  $-1$
6.  $-4)$
7.  $(-2, -1) \cup (0, \infty)$
8.  $(-1, 0)$
9.  $(0, -4)$
10. None
11.  $-426$
12. 51
13.  $(1.408, 0.272)$
14.  $(0.592, -0.272)$
15. None
16. None
17.  $(0.592, 1.408)$
18.  $(-\infty, 0.592) \cup (1.408, \infty)$

## Chapter 4

# Linear Functions and Slope

### 4.1 Average Rate of Change

For the function  $f(x) = x^2$ , compute the average rate of change for each interval.

1.  $[1, 1.1]$
2.  $[1, 1.01]$
3.  $[1, 1.001]$
4.  $[1, 1.0001]$
5. For your answers in the previous four problems, what value do your average rates of change get closer and closer to?

Find the average rate of change of the function  $f(x) = -6x^2 + 7x + 4$  over each specified interval.

6.  $[-2, -1]$
7.  $[5, 6]$
8.  $[0, 1]$
9.  $[5, 5.001]$
10.  $[5, 5.0001]$
11.  $[5, 5.00001]$
12. What value are your last 3 answers getting closer to?

For the function  $f(x) = -3x^2 + 5$ , determine the average rate of change of each over the given interval.

13.  $[7, 7.001]$
14.  $[7, 7.0001]$
15.  $[7, 7.00001]$
16. For your answers in the previous three problems, what value do your average rates of change get closer and closer to?

Given  $f(x) = \sqrt{x}$ , find the average rate of change of each over the given interval.

17.  $[1, 1.0001]$
18.  $[1, 1.00001]$
19.  $[1, 1.000001]$
20. For your answers in the previous three problems, what value do your average rates of change get closer and closer to?

## Average Rate of Change

1. 2.1
2. 2.01
3. 2.001
4. 2.0001
5. 2
6. 25
7.  $-59$
8. 1
9.  $-53.006$
10.  $-53.0006$
11.  $-53.00006$
12.  $-53$
13.  $-42.003$
14.  $-42.0003$
15.  $-42.00003$
16.  $-42$
17.  $-0.499988$
18.  $-0.4999988$
19.  $-0.49999988$
20.  $-0.5$

## Chapter 5

# Function Transformations

Write the function for  $g(x)$  if it is the result of  $f(x)$  after the following ordered sequence of transformations.

1. (1) Vertical stretch by 3  
(2) Shift left 1 unit  
(3) Reflect across  $y$ -axis
2. (1) Horizontal compression by 2  
(2) Shift up 1 unit
3. (1) Reflect across  $x$ -axis  
(2) Vertical compression by 4  
(3) Move right 7 units

Write the function  $g(x)$  that is a result of the following ordered sequence of transformations to  $f(x) = |x|$ .

4. (1) Reflect across  $x$ -axis  
(2) Shift right 3 units  
(3) Horizontal stretch by factor of 5
5. (1) Shift down 2 units  
(2) Reflect across  $y$ -axis  
(3) Shift up 1 unit
6. (1) Horizontal compression by factor of 7  
(2) Vertical compression by factor of 4  
(3) Shift left 9 units

Given  $f(x) = \sqrt{x}$ , determine the resulting function  $g(x)$  after the following ordered sequence of transformations.

7. (1) Shift up 2 units  
(2) Horizontal stretch by 5  
(3) Shift left 3 units
8. (1) Vertical compression by factor of 3  
(2) Reflect across  $y$ -axis  
(3) Horizontal compression by 5
9. 1) Shift right 8 units  
2) Reflect across  $x$ -axis  
3) Horizontal compression by factor of 4

## FUNCTION TRANSFORMATIONS KEY

1.  $g(x) = 3f(-x + 1)$

2.  $g(x) = f(2x) + 1$

3.  $g(x) = -\frac{1}{4}f(x - 7)$

4.  $g(x) = -\left|\frac{1}{5}x - 3\right|$

5.  $g(x) = |-x| - 1$

6.  $g(x) = \frac{1}{4}|7(x + 9)| = \frac{1}{4}|7x + 63|$

7.  $g(x) = \sqrt{\frac{1}{5}(x + 3)} + 2 = \sqrt{\frac{1}{5}x + \frac{3}{5}} + 2$

8.  $g(x) = \frac{1}{3}\sqrt{-5x}$

9.  $g(x) = -\sqrt{4x - 8}$

## Chapter 6

# Function Operations

### 6.1 Adding, Subtracting, Multiplying, and Dividing Functions

Given  $f(x) = x + 5$ ,  $g(x) = x^2 - 1$ , and  $h(x) = \sqrt{x - 10}$ , simplify or evaluate each.

1.  $(g - f)(x)$
2.  $(fh)(14)$
3.  $(f + g)(x)$

### 6.2 Operations with Functions: Domain

Given  $f(x) = \sqrt{2x + 7}$  and  $g(x) = 3x + 3$ , find the domain of each.

1.  $(f + g)(x)$
2.  $\left(\frac{f}{g}\right)(x)$
3.  $\left(\frac{g}{f}\right)(x)$

### 6.3 Difference Quotient

Write the difference quotient for each.

1.  $f(x) = 2x - 7$
2.  $g(x) = x^2 + 4x$
3.  $h(x) = -1$
4.  $f(x) = \frac{3}{x+2}$
5.  $g(x) = \sqrt{3x}$
6.  $f(x) = x^2 - 2x + 5$
7.  $g(x) = \frac{5}{x}$

## Adding, Subtracting, Multiplying, and Dividing Functions

1.  $x^2 - x - 6$
2. 38
3.  $x^2 + x + 4$

## Operations with Functions: Domain

1.  $[-\frac{7}{2}, \infty)$
2.  $[-\frac{7}{2}, -1) \cup (-1, \infty)$
3.  $(-\frac{7}{2}, \infty)$

## Difference Quotient

1. 2
2.  $2x + h + 4$
3. 0
4.  $\frac{-3}{(x+2)(x+h+2)}$
5.  $\frac{3}{\sqrt{3x+3h}+\sqrt{3x}}$
6.  $2x + h - 2$
7.  $\frac{-5}{x(x+h)}$

## Chapter 7

# Polynomials and Their Graphs

Determine the end behavior of each.

1.  $f(x) = -x^5 + \sqrt{7}x^3 - 2x^2$

2.  $g(x) = 4x^2 - 16x^6 + 3x$

3.  $h(x) = 1 + x^{11} - 4x^8$

4.  $f(x) = -x^4 + 3x^2 - 2x + 6$

5.  $g(x) = 0.25x^5 - 0.1x^4 + 2x^2 - 6x$



## POLYNOMIALS AND THEIR GRAPHS

1.  $\lim_{x \rightarrow -\infty} f(x) = \infty \quad \lim_{x \rightarrow \infty} f(x) = -\infty$

2.  $\lim_{x \rightarrow -\infty} g(x) = -\infty, \quad \lim_{x \rightarrow \infty} g(x) = \infty$

3.  $\lim_{x \rightarrow -\infty} h(x) = -\infty \quad \lim_{x \rightarrow \infty} h(x) = \infty$

4.  $\lim_{x \rightarrow -\infty} f(x) = -\infty \quad \lim_{x \rightarrow \infty} f(x) = -\infty$

5.  $\lim_{x \rightarrow -\infty} g(x) = -\infty \quad \lim_{x \rightarrow \infty} g(x) = \infty$

## Chapter 8

# Dividing Polynomials

### 8.1 Dividing Polynomials

Divide each.

1.  $(28x^3 - 26x^2 + 41x - 15) \div (7x - 3)$

2.  $(44y^2 + 12y^3 + 61y - 37) \div (3y + 5)$

### 8.2 Remainder and Factor Theorems

Determine the remainder of each.

1.  $(2x^{53} - 9x^{44} + 13x^8) \div (x - 1)$

2.  $(x^{71} + 15x^{58} - 3x^{14} + 2) \div (x + 1)$

## Dividing Polynomials

1.  $4x^2 - 2x + 5$

2.  $4y^2 + 8y + 7 - \frac{72}{3y + 5}$

## Remainder and Factor Theorems

1. 6

2. 13

## Chapter 9

# Rational Functions and Their Graphs

Find the domain, coordinates of any holes, and equations of all asymptotes.

1.  $f(x) = \frac{2x^2 + 5x - 3}{2x^2 - 15x + 7}$

2.  $g(x) = \frac{3x^3 + 7x^2 - 20x}{x^2 - x - 12}$

3.  $f(x) = \frac{3x}{x + 4}$

4.  $g(x) = \frac{x^2 + 3x + 2}{x - 1}$

5.  $h(x) = \frac{x^2 + 3x - 4}{x^3 - 2x^2 + x}$

## RATIONAL FUNCTIONS AND THEIR GRAPHS KEY

1. Domain:  $x \neq -\frac{1}{2}, 7$ ; V.A.:  $x = 7$ ; Hole @  $\left(-\frac{1}{2}, -\frac{7}{13}\right)$ ; H.A.:  $y = 1$
2. Domain:  $x \neq -3, 4$ ; V.A.:  $x = -3$ ; Obl. Asymp:  $y = 3x + 10$
3. Domain:  $x \neq -4$ ; V.A.:  $x = -4$ ; H.A.:  $y = 3$
4. Domain:  $x \neq 1$ ; V.A.:  $x = 1$ ; Obl. Asymp:  $y = x + 4$
5. Domain:  $x \neq 0, 1$ ; V.A.:  $x = 0$  and  $x = 1$ ; H.A.:  $y = 0$

## Chapter 10

# Polynomial and Rational Inequalities

### 10.1 Polynomial Inequalities

Solve each. Write your answers using interval notation.

1.  $6x^3 - 4x^2 - 10x \geq 0$

### 10.2 Rational Inequalities

Solve each. Write your answers using interval notation.

1.  $\frac{3x - 4}{x + 1} < 0$

2.  $\frac{x^2 + 3x + 2}{x - 7} \leq 0$

## Polynomial Inequalities

1.  $[-1, 0] \cup \left[\frac{5}{3}, \infty\right)$

## Rational Inequalities

1.  $\left(-1, \frac{4}{3}\right)$

2.  $(-\infty, -2] \cup [-1, 7)$

## Chapter 11

# Function Compositions

Given  $f(x) = x - 5$ ,  $g(x) = 4 + \sqrt{2x + 1}$ , and  $h(x) = \frac{3}{x + 7}$ , simplify each and state the domain.

1.  $(f \circ g)(x)$

2.  $(g \circ f)(x)$

3.  $h(h(x))$



# FUNCTION COMPOSITIONS KEY

1.  $-1 + \sqrt{2x+1}$  Domain:  $\left[-\frac{1}{2}, \infty\right)$

2.  $4 + \sqrt{2x-9}$  Domain:  $\left[\frac{9}{2}, \infty\right)$

3.  $\frac{3x+21}{7x+52}$  Domain:  $\left(-\infty, -\frac{52}{7}\right) \cup \left(-\frac{52}{7}, -7\right) \cup (-7, \infty)$

# Appendix A

## Factoring

Factor each of the following completely.

1.  $x^2 + 2x - 15$

2.  $x^2 - 8x + 12$

3.  $x^2 + 15x + 56$

4.  $5x^2 + 19x - 4$

5.  $4x^2 - 5x - 6$

6.  $9x^2 - 400$

7.  $5x^2 - 7x - 6$

8.  $9x^2 - 54x + 45$

9.  $3x^3 + 12x^2 + 9x$

10.  $9y^2 - 16$

11.  $4x^2 - 28x + 49$

12.  $14x^2 + 11xy - 15y^2$

13.  $6x^2 - 48x - 120$

14.  $9x^4 - 54x^3 + 45x^2$

15.  $16y^2 - 40y + 25$

16.  $30x^2 + xy - y^2$

17.  $8w^2 + 33w + 4$

18.  $3p^2 + 22p - 16$

19.  $18x^2 - 27x + 4$

20.  $14a^2 + 15a - 9$

21.  $4x^2 - 4x - 24$

22.  $18t^2 - 9t - 5$

23.  $6a^2 + 23a + 21$

24.  $25x^2 - 1$

## FACTORING KEY

1.  $(x + 5)(x - 3)$

2.  $(x - 6)(x - 2)$

3.  $(x + 7)(x + 8)$

4.  $(5x - 1)(x + 4)$

5.  $(4x + 3)(x - 2)$

6.  $(3x + 20)(3x - 20)$

7.  $(5x + 3)(x - 2)$

8.  $9(x - 5)(x - 1)$

9.  $3x(x + 3)(x + 1)$

10.  $(3y + 4)(3y - 4)$

11.  $(2x - 7)^2$

12.  $(7x - 5y)(2x + 3y)$

13.  $6(x - 10)(x + 2)$

14.  $9x^2(x - 1)(x - 5)$

15.  $(4y - 5)^2$

16.  $(6x - y)(5x + y)$

17.  $(8w + 1)(w + 4)$

18.  $(3p - 2)(p + 8)$

19.  $(6x - 1)(3x - 4)$

20.  $(7a - 3)(2a + 3)$

21.  $4(x - 3)(x + 2)$

22.  $(6t - 5)(3t + 1)$

23.  $(2a + 3)(3a + 7)$

24.  $(5x + 1)(5x - 1)$

## Appendix B

# Complex Fractions

Simplify each as much as possible.

$$1. \frac{5 + \frac{3}{x}}{x - \frac{1}{2}}$$

$$2. \frac{\frac{1}{x} + \frac{2}{x^2}}{x + \frac{8}{x^2}}$$

$$3. \frac{3}{2 - \frac{x}{x-1}}$$

$$4. \frac{1 + \frac{3}{x}}{\frac{2}{x} + 7}$$

$$5. \frac{\frac{4}{x} - \frac{x}{x-2}}{\frac{1}{x} + \frac{3}{x-2}}$$

$$6. \frac{\frac{3}{x+1} - 4}{\frac{2}{x+1}}$$

$$7. \frac{\frac{5}{x} + \frac{3}{x-2}}{\frac{7}{x^2-2x}}$$

$$8. \frac{\frac{1}{x} - \frac{1}{7}}{x - 7}$$

$$9. \frac{\frac{1}{x} + \frac{1}{x+1}}{5}$$

COMPLEX FRACTIONS KEY

$$1. \frac{2(5x+3)}{x(2x-1)}$$

$$2. \frac{1}{x^2-2x+4}$$

$$3. \frac{3(x-1)}{x-2}$$

$$4. \frac{x+3}{2+7x}$$

$$5. \frac{-1(x^2-4x+8)}{2(2x-1)}$$

$$6. \frac{-4x-1}{2}$$

$$7. \frac{8x-10}{7}$$

$$8. -\frac{1}{7x}$$

$$9. \frac{2x+1}{5x(x+1)}$$