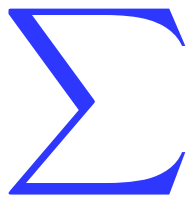
Honors PreCalculus



Extra Practice Problems

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April 21, 2021

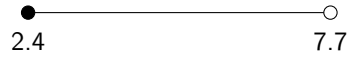
Contents

Chapter 1

Basic Set Theory and Interval Notation

You are given either interval notation, set-builder notation, or a graph. Write each of the following in its other 2 forms.

1. $(-5, 8]$
2. $\{x|x \leq 1\}$
3. 

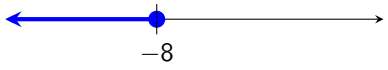
4. $\{x|x \neq 4, 11\}$
5. 

6. $(9, \infty)$

Write each using interval notation and graph on a number line.

7. $\{x|x \geq 2\}$
8. $\{x|x < -8\}$
9. $\{x|x \neq 3\}$
10. $\{x|x \neq -2, 5\}$

You are given the graph of an interval. Write the interval and set-builder notation for it.

11. 

12. 

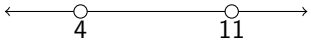
1.1 Answer Key

1. $\{x| -5 < x \leq 8\}$

2. $(-\infty, 1]$

3. $[-3, \infty)$ $\{x|x \geq -3\}$

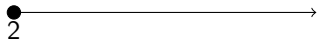
4. $(-\infty, 4) \cup (4, 11) \cup (11, \infty)$



5. $[2.4, 7.7)$ $\{x|2.4 \leq x < 7.7\}$

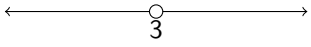
6. $\{x|x > 9\}$

7. $[2, \infty)$



8. $(-\infty, -8)$

9. $(-\infty, 3) \cup (3, \infty)$



10. $(\infty, -2) \cup (-2, 5) \cup (5, \infty)$

11. $(-\infty, -8]$ $\{x|x \leq -8\}$

12. $(-\infty, 7) \cup (7, 12) \cup (12, \infty)$ $\{x|x \neq 7, 12\}$

Chapter 2

Functions and Their Graphs

2.1 Evaluating Functions

Given $f(x) = -3x^2 + 4x$ and $g(x) = \frac{1}{x} - 5$, evaluate each.

1. $f(5)$
2. $f(-2)$
3. $f(0)$
4. $g(1)$
5. $g(-5)$
6. $g(1/4)$

2.2 Domain of Functions

Find the domain of each write your answers in interval notation.

1. $f(x) = -8x^2 - 7x + 1$
2. $g(x) = \sqrt{5x + 12} - 2$
3. $h(x) = \frac{x+2}{9x-7}$
4. $f(x) = -5x + 4$
5. $f(x) = x^2 + 2$
6. $f(x) = \frac{2x+1}{3x-5}$
7. $f(x) = \sqrt{3x - 12}$
8. $f(x) = \frac{x}{x^2-16}$
9. $f(x) = \frac{x+4}{x^3-4x}$
10. $f(x) = \frac{x}{\sqrt{x-4}}$
11. $f(x) = \frac{x^2+1}{2x^2+8}$
12. $f(x) = -\frac{x+7}{x^2-5x-6}$
13. $g(x) = \sqrt{2x + 3}$
14. $h(x) = \sqrt[3]{2x + 3}$
15. $f(x) = -\frac{7x-10}{x^2+3x+2}$
16. $g(x) = \sqrt{-9x + 8}$
17. $h(x) = -\sqrt[3]{4x + 1}$
18. $f(x) = \sqrt[3]{8x + 1}$
19. $g(x) = \frac{x^2-1}{\sqrt{x+3}}$
20. $h(x) = \frac{3}{9+\frac{4}{x+7}}$
21. $f(x) = \frac{x+1}{\sqrt{10x+8}}$
22. $g(x) = \frac{5}{1+\frac{3}{x+2}}$
23. $i(x) = \frac{7}{3-\frac{4}{x+1}}$
24. $n(x) = \frac{7x+14}{\sqrt{2x-1}}$
25. $a(x) = \frac{\frac{x}{x-2}}{\frac{3}{x-2} + 6}$
26. $d(x) = \frac{7x-5}{\sqrt[3]{5x+2}}$

2.3 Piecewise Functions

Find the value of each given the piecewise function below. Use exact answers when possible.

$$f(x) = \begin{cases} x^2 - 1 & \text{if } x < -3 \\ 0.2x + 7 & \text{if } -3 \leq x < 2 \\ \sqrt{5x} & \text{if } x \geq 2 \end{cases}$$

1. $f(3)$
2. $f(0)$
3. $f(-2)$
4. $f(-3)$
5. $f(0.5)$

Find each of the following given the piecewise function

$$f(x) = \begin{cases} x^2 - 7 & x \leq -4 \\ \sqrt{2x + 7} & -4 < x < 0 \\ |-x - 1| & x \geq 0 \end{cases}$$

6. $f(3)$
7. $f(-2)$
8. $f(0)$
9. $f(-5)$

Find the value of each given the piecewise function below. Round to 3 decimal places when necessary.

$$f(x) = \begin{cases} x^2 - 5 & \text{if } x \leq -3 \\ \sqrt{-4x + 1} & \text{if } -3 < x \leq 0 \\ \frac{5x^2}{x+7} & \text{if } x > 0 \end{cases}$$

10. $f(7)$
11. $f(-3)$
12. $f(1)$
13. $f(0)$
14. $f(-1)$
15. $f(-3/2)$

2.4 Answer Key

Evaluating Functions

1. -55
2. -20
3. 0
4. -4
5. -5.2
6. -1

Domain of Functions

1. $(-\infty, \infty)$
2. $\left[\frac{-12}{5}, \infty\right)$
3. $\left(-\infty, \frac{7}{9}\right) \cup \left(\frac{7}{9}, \infty\right)$
4. $(-\infty, \infty)$
5. $(-\infty, \infty)$
6. $\left(-\infty, \frac{5}{3}\right) \cup \left(\frac{5}{3}, \infty\right)$
7. $[4, \infty)$
8. $(-\infty, -4) \cup (-4, 4) \cup (4, \infty)$
9. $(-\infty, -2) \cup (-2, 0) \cup (0, 2) \cup (2, \infty)$
10. $(4, \infty)$
11. $(-\infty, \infty)$
12. $(-\infty, -1) \cup (-1, 6) \cup (6, \infty)$
13. $\left[-\frac{3}{2}, \infty\right)$
14. $(-\infty, \infty)$
15. $(-\infty, -2) \cup (-2, -1) \cup (-1, \infty)$
16. $\left(-\infty, \frac{8}{9}\right]$
17. $(-\infty, \infty)$
18. $(-\infty, \infty)$
19. $(-3, \infty)$
20. $\left(-\infty, -\frac{67}{9}\right) \cup \left(-\frac{67}{9}, -7\right) \cup (-7, \infty)$
21. $\left(-\frac{4}{5}, \infty\right)$
22. $(\infty, -5) \cup (-5, -2) \cup (-2, \infty)$
23. $(-\infty, -1) \cup (-1, \frac{1}{3}) \cup (\frac{1}{3}, \infty)$
24. $(\frac{1}{2}, \infty)$
25. $\left(-\infty, \frac{3}{2}\right) \cup \left(\frac{3}{2}, 2\right) \cup (2, \infty)$
26. $\left(-\infty, -\frac{2}{5}\right) \cup \left(-\frac{2}{5}, \infty\right)$

Piecewise Functions

1. $\sqrt{15} \approx 3.873$
2. 7
3. 6.6
4. 6.4
5. 7.1
6. 4
7. $\sqrt{3} \approx 1.732$
8. 1
9. 18
10. 17.5
11. 4
12. $\frac{5}{8}$
13. 1
14. $\sqrt{5} \approx 2.236$
15. $\sqrt{7} \approx 2.646$

Chapter 3

Properties of Functions

3.1 Maxima and Minima

Find the coordinates of the any relative maxima or minima. Round to 3 decimal places when necessary.

1. $f(x) = x^2 - 3x^2 + 5$
2. $g(x) = -0.4x^3 + 0.6x^2 + 3x - 2$
3. $f(x) = -x^4 + 3x^2 - 2x + 6$
4. $g(x) = 0.25x^5 - 0.1x^4 + 2x^2 - 6x$
5. $f(x) = -4x^3 + 2x^2 + 10x + 4$
6. $g(x) = x^4 - 4x^3 + 3x^2 + 4x - 4$
7. The concentration C of a medication in the bloodstream t hours after being administered can be modeled by

$$C(t) = -0.002t^4 + 0.039t^3 - 0.285t^2 + 0.766t + 0.085, \quad t \geq 0$$

   After how many hours will the concentration be the highest?

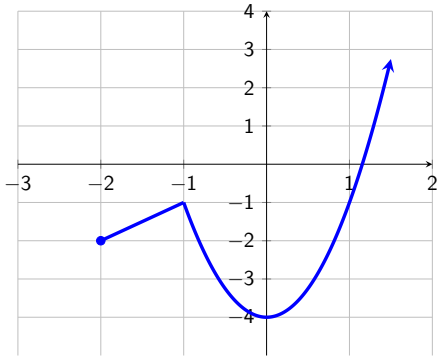
3.2 Increasing, Decreasing, and Constant Intervals

Find the intervals in which each is increasing or decreasing. Round to 3 decimal places when necessary.

1. $f(x) = x^2 - 3x^2 + 5$
2. $g(x) = -0.4x^3 + 0.6x^2 + 3x - 2$
3. $f(x) = x^3 + 2x^2 - 4x - 8$
4. $g(x) = x^4 - 2x^2 + 1$
5. $h(x) = \sqrt{x+1} - 2$
6. $f(x) = -4x^3 + 2x^2 + 10x + 4$
7. $g(x) = x^4 - 4x^3 + 3x^2 + 4x - 4$

3.3 Miscellaneous

Use the graph of $y = f(x)$ below to answer the following questions. Write your answers using interval notation.

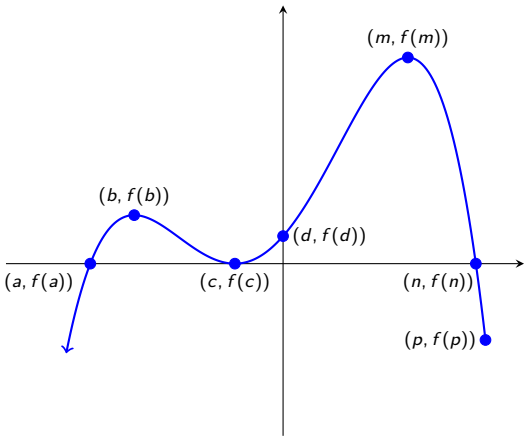


1. Domain of f
2. Range of f
3. Relative Minimum
4. Relative Maximum
5. $f(1)$
6. $f(0)$
7. Increasing Interval(s)
8. Decreasing Interval(s)
9. Absolute Maximum
10. Absolute Minimum

Find each of the following given $f(x) = -2x^3 + 6x^2 - 5x + 1$. Round to 3 decimal places and use interval notation when applicable.

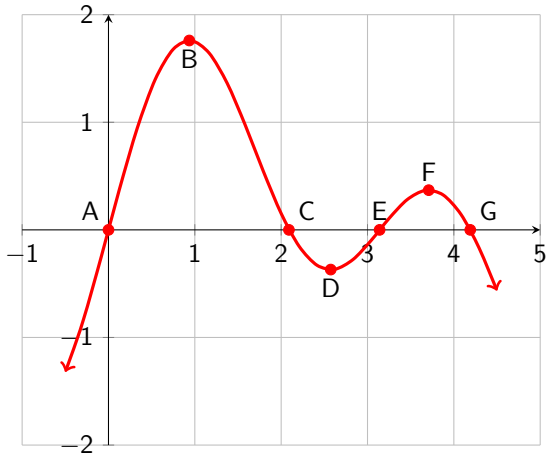
11. $f(7)$
12. $f(-2)$
13. Rel. Max
14. Rel. Min
15. Global Max
16. Global Min
17. Increasing Interval(s)
18. Decreasing Interval(s)

Use the graph of $f(x)$ to answer each.



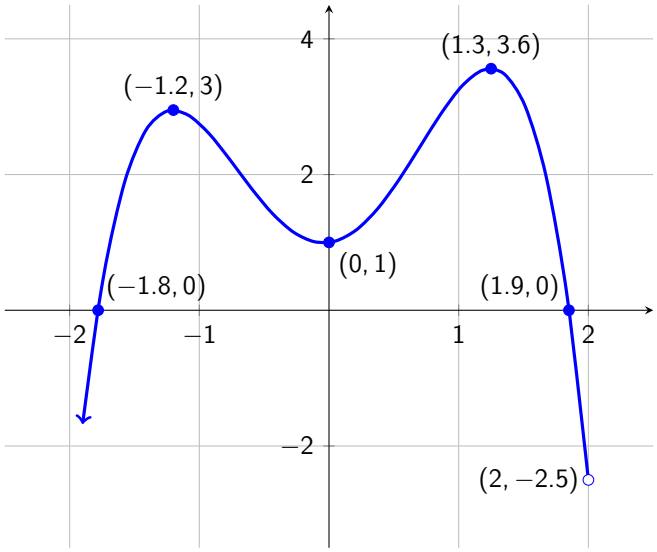
19. Relative maxima of $f(x)$
20. Relative minima of $f(x)$
21. Absolute maxima of $f(x)$
22. Absolute minima of $f(x)$
23. Intervals where f is increasing
24. Intervals where f is decreasing
25. Zeros of f

Given the labeled points A through G on the graph of $f(x)$ below, find each of the following.



26. Increasing interval(s)
27. Decreasing interval(s)
28. Relative max
29. Relative min
30. Global max
31. Global min
32. Zeros of f
33. Number of solutions to $f(x) = 1$

Answer each of the following about the function $f(x)$ below.



34. Domain of f
35. Range of f
36. Relative maxima
37. Relative minima
38. Absolute maximum
39. Absolute minimum
40. Increasing intervals
41. Decreasing intervals
42. Zeros of $f(x)$
43. Number of solutions to $f(x) = 2$

3.4 Answer Key

Maxima and Minima

1. Rel max @ $(0, 5)$; No rel min
2. Rel max @ $(2.158, 3.248)$; Rel min @ $(-1.158, -4.048)$
3. Rel Max $(-1.366, 10.848)$ and $(1, 6)$; Rel Min $(0.366, 5.652)$
4. Rel Max $(-1.716, 11.598)$; Rel Min $(1.132, -3.929)$
5. Rel Max: $(1.095, 12.096)$; Rel Min $(-0.761, -0.680)$
6. Rel Max: $(1.366, 0.348)$; Rel Min: $(-0.366, -4.848)$ and $(2, 0)$
7. About 2.16 hours

Increasing, Decreasing, and Constant Intervals

1. Increasing: $(-\infty, 0)$ Decreasing: $(0, \infty)$
2. Increasing: $(-1.158, 2.158)$ Decreasing: $(-\infty, -1.158) \cup (2.158, \infty)$
3. Inc: $(-\infty, -2) \cup \left(\frac{2}{3}, \infty\right)$ Dec: $\left(-2, \frac{2}{3}\right)$
4. Inc; $(-1, 0) \cup (1, \infty)$ Dec: $(-\infty, -1) \cup (0, 1)$
5. Inc: $(-1, \infty)$ No intervals where it is decreasing
6. Inc: $(-0.761, 1.095)$; Dec: $(-\infty, -0.761) \cup (1.095, \infty)$
7. Inc: $(-0.366, 1.366) \cup (2, \infty)$; Dec: $(-\infty, -0.366) \cup (1.366, 2)$;

Miscellaneous

1. $[-2, \infty)$
2. $[-4, \infty)$
3. $(0, -4)$
4. $(-1, -1)$
5. -1
6. $-4)$
7. $(-2, -1) \cup (0, \infty)$
8. $(-1, 0)$
9. $(0, -4)$
10. None
11. -426
12. 51
13. (1.408, 0.272)
14. (0.592, -0.272)
15. None
16. None
17. (0.592, 1.408)
18. $(-\infty, 0.592) \cup$ $(1.408, \infty)$
19. $(b, f(b))$ and $(m, f(m))$
20. $(c, f(c))$
21. $(m, f(m))$
22. None
23. $(-\infty, b) \cup (c, m)$
24. $(b, c) \cup (m, p)$
25. $x = a$, $x = c$, $x = n$
26. $(\infty, B) \cup (D, F)$
27. $(B, D) \cup (F, \infty)$
28. B and F
29. D
30. B
31. None
32. A, C, E, G
33. 2
34. $(-\infty, 2)$
35. $(-\infty, -2.5) \cup (-2.5, 3.6]$
36. $(-1.2, 3)$ and $(1.3, 3.6)$
37. $(0, 1)$
38. $(1.3, 3.6)$
39. Does not exist
40. $(-\infty, -1.2) \cup (0, 1.3)$
41. $(-1.2, 0) \cup (1.3, 2)$
42. $(-1.8, 0)$ and $(1.9, 0)$
43. 4

Chapter 4

Linear Functions and Slope

4.1 Equations of Lines

Write the equation of each line **in point-slope form** that goes through each pair of points.

1. $(-2, 1)$, $(7, 8)$
2. $(0, 4)$, $(9, -15)$
3. $(-1, -2)$, $(-3, -13)$

4.2 Average Rate of Change

For the function $f(x) = x^2$, compute the average rate of change for each interval.

1. $[1, 1.1]$
2. $[1, 1.01]$
3. $[1, 1.001]$
4. $[1, 1.0001]$
5. For your answers in the previous four problems, what value do your average rates of change get closer and closer to?

Find the average rate of change of the function $f(x) = -6x^2 + 7x + 4$ over each specified interval.

6. $[-2, -1]$
7. $[5, 6]$
8. $[0, 1]$
9. $[5, 5.001]$
10. $[5, 5.0001]$
11. $[5, 5.00001]$
12. What value are your last 3 answers getting closer to?

For the function $f(x) = -3x^2 + 5$, determine the average rate of change of each over the given interval.

13. $[7, 7.001]$
14. $[7, 7.0001]$
15. $[7, 7.00001]$
16. For your answers in the previous three problems, what value do your average rates of change get closer and closer to?

Given $f(x) = \sqrt{x}$, find the average rate of change of each over the given interval.

17. $[1, 1.0001]$
18. $[1, 1.00001]$
19. $[1, 1.000001]$
20. For your answers in the previous three problems, what value do your average rates of change get closer and closer to?

Given $f(x) = 6\sqrt{x}$, find the average rate of change of each over the given interval.

21. $[25,\ 25.1]$
22. $[25,\ 25.01]$
23. $[25,\ 25.001]$
24. For your answers in the previous three problems, what value do your average rates of change get closer and closer to?

Find the average rate of change of the function $f(x) = -7x^3 + 6\sqrt{3x} + 4$ over each interval. Round your answers to 4 decimal places.

25. $[0, 1]$
26. $[10, 11]$
27. $[8, 15]$

4.3 Answer Key

Equations of Lines

1. $y - 1 = \frac{7}{9}(x + 2)$ or $y - 8 = \frac{7}{9}(x - 7)$
2. $y - 4 = -\frac{19}{9}(x - 0)$ or $y + 15 = -\frac{19}{9}(x - 9)$
3. $y + 2 = \frac{11}{2}(x + 1)$ or $y + 13 = \frac{11}{2}(x + 3)$

Average Rate of Change

1. 2.1
2. 2.01
3. 2.001
4. 2.0001
5. 2
6. 25
7. -59
8. 1
9. -53.006
10. -53.0006
11. -53.00006
12. -53
13. -42.003
14. -42.0003
15. -42.00003
16. -42
17. -0.499988
18. -0.4999988
19. -0.49999988
20. -0.5
21. 0.5994
22. 0.59999
23. 0.6
24. 0.6
25. 3.3923
26. $-2,315.3960$
27. -2861.4492

Chapter 5

Function Transformations

Write the function for $g(x)$ if it is the result of $f(x)$ after the following ordered sequence of transformations.

1. (1) Vertical stretch by 3
   (2) Shift left 1 unit
   (3) Reflect across y-axis
2. (1) Horizontal compression by 2
   (2) Shift up 1 unit
3. (1) Reflect across x-axis
   (2) Vertical compression by 4
   (3) Move right 7 units

Write the function $g(x)$ that is a result of the following ordered sequence of transformations to $f(x) = |x|$.

4. (1) Reflect across x-axis
   (2) Shift right 3 units
   (3) Horizontal stretch by factor of 5
5. (1) Shift down 2 units
   (2) Reflect across y-axis
   (3) Shift up 1 unit
6. (1) Horizontal compression by factor of 7
   (2) Vertical compression by factor of 4
   (3) Shift left 9 units

Given $f(x) = \sqrt{x}$, determine the resulting function $g(x)$ after the following ordered sequence of transformations.

7. (1) Shift up 2 units
   (2) Horizontal stretch by 5
   (3) Shift left 3 units
8. (1) Vertical compression by factor of 3
   (2) Reflect across y-axis
   (3) Horizontal compression by 5
9. (1) Shift right 8 units
   (2) Reflect across x-axis
   (3) Horizontal compression by factor of 4

Write the final equation of $g(x)$ if it is found by taking $f(x) = \sqrt{x}$ after the following ordered sequence of transformations.

10. (1) Shift right 2 units
    (2) Horizontal stretch by factor 3
    (3) Shift down 2 units
    (4) Reflect across x-axis

11. (1) Horizontal stretch by factor 3
    (2) Shift left 1 unit
    (3) Shift up 2 units
    (4) Reflect across y-axis

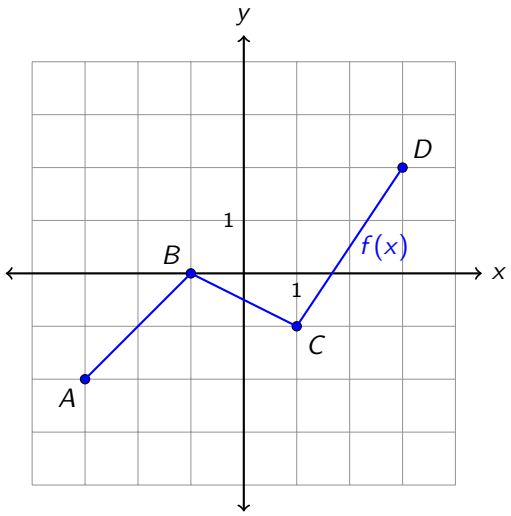
12. (1) Vertical stretch by factor 5
    (2) Horizontal stretch by factor 2
    (3) Shift up 3 units
    (4) Reflect across x-axis

Find the equation for $g(x)$ if $g(x)$ is found by performing the following *ordered* sequence of transformations to $f(x) = \frac{1}{x}$.

13. (1) Shift left 3 spaces
    (2) Reflect across y-axis
    (3) Shift down 5 spaces
    (4) Vertical stretch by factor of 7

14. (1) Shift up 3 spaces
    (2) Reflect across x-axis
    (3) Shift right 5 spaces
    (4) Horizontal compression by factor of 7

Given the graph of $f(x)$ below, find the new coordinates of each point after the following transformations.



15. $-2f(x+1)$

16. $f\left(-\frac{1}{2}x\right) - 3$

17. $\frac{1}{2}f(-x-2)+2$

18. $f(2x+2)-1$

19. $-3f(-x+1)+2$

20. $5f\left(-\frac{1}{2}x\right)$

5.1 Answer Key

1. $g(x) = 3f(-x+1)$
2. $g(x) = f(2x)+1$
3. $g(x) = -\frac{1}{4}f(x-7)$
4. $g(x) = -\left|\frac{1}{5}x-3\right|$
5. $g(x) = |-x|-1$
6. $g(x) = \frac{1}{4}|7(x+9)| = \frac{1}{4}|7x+63|$
7. $g(x) = \sqrt{\frac{1}{5}(x+3)}+2 = \sqrt{\frac{1}{5}x+\frac{3}{5}}+2$
8. $g(x) = \frac{1}{3}\sqrt{-5x}$
9. $g(x) = -\sqrt{4x-8}$
10. $g(x) = -\left(\sqrt{\frac{1}{3}x-2}-2\right) = -\sqrt{\frac{1}{3}x-2}+2$
11. $g(x) = \sqrt{\frac{1}{3}(-x+1)}+2 = \sqrt{-\frac{1}{3}x+\frac{1}{3}}+2$
12. $g(x) = -\left(5\sqrt{\frac{1}{2}x}+3\right) = -5\sqrt{\frac{1}{2}x}-3$
13. $g(x) = \frac{7}{-x+3}-35$
14. $g(x) = -\frac{1}{7x-5}-3$
15. $A'(-4,4),\ B'(-2,0),\ C'(0,2),\ D'(2,-4)$
16. $A'(6,-5),\ B'(2,-3),\ C'(-2,-4),\ D'(-6,-1)$
17. $A'(1,1),\ B'(-1,2),\ C'(-3,1.5),\ D'(-5,3)$
18. $A'(-2.5,-3),\ B'(-1.5,-1),\ C'(-0.5,-2),\ D'(0.5,1)$
19. $A'(4,8),\ B'(2,2),\ C'(0,5),\ D'(-2,-4)$
20. $A'(6,-10),\ B'(2,0),\ C'(-2,-5),\ D'(-6,10)$

Chapter 6

Function Operations

6.1 Adding, Subtracting, Multiplying, and Dividing Functions

Given $f(x) = x + 5$, $g(x) = x^2 - 1$, and $h(x) = \sqrt{x - 10}$, simplify or evaluate each.

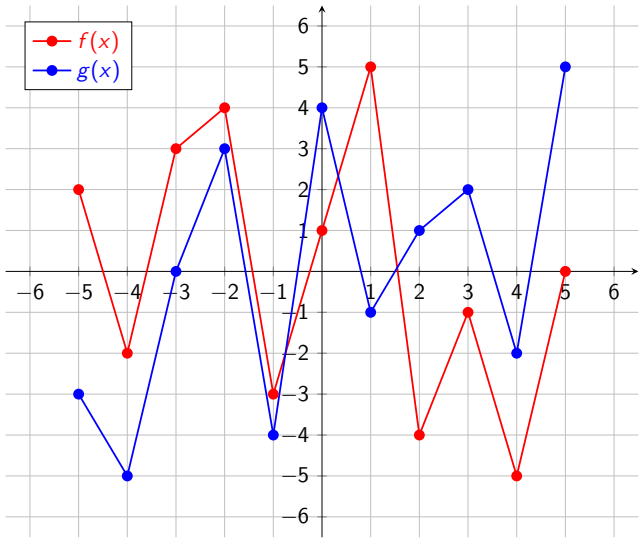
1. $(g - f)(x)$
2. $(fh)(14)$
3. $(f + g)(x)$

Find each of the following given the table below.

x	**−4**	**−3**	**−2**	**−1**	**0**	**1**	**2**	**3**	**4**
f(x)	−3	0	−1	3	1	2	4	−4	−2
g(x)	3	−1	0	1	4	−2	−4	2	−3

4. $(f + g)(-2)$
5. $(f - g)(0)$
6. $(fg)(1)$
7. $\left(\frac{f}{g}\right)(3)$
8. $(f + f)(-4)$

Find each of the following given the graphs of $f(x)$ (in red) and $g(x)$ (in blue) below:



9. $(f + g)(2)$
10. $(f - g)(1)$
11. $(g - f)(-3)$
12. $(fg)(4)$
13. $\left(\frac{f}{g}\right)(0)$

6.2 Operations with Functions: Domain

Given $f(x) = \sqrt{2x+7}$ and $g(x) = 3x + 3$, find the domain of each.

1. $(f+g)(x)$
2. $\left(\frac{f}{g}\right)(x)$
3. $\left(\frac{g}{f}\right)(x)$

6.3 Difference Quotient

Write the difference quotient for each.

1. $f(x) = 2x - 7$
2. $g(x) = x^2 + 4x$
3. $h(x) = -1$
4. $f(x) = \frac{3}{x+2}$
5. $g(x) = \sqrt{3x}$
6. $f(x) = x^2 - 2x + 5$
7. $g(x) = \frac{5}{x}$
8. $f(x) = -2x^2 + 3x - 5$
9. $g(x) = \frac{6}{2x+3}$
10. $h(x) = \sqrt{7x+5}$
11. $f(x) = -x^2 + x$
12. $f(x) = 3x - 1$
13. $f(x) = x^3 + 5x$

6.4 Answer Key

Adding, Subtracting, Multiplying, and Dividing Functions

1. $x^2 - x - 6$
2. 38
3. $x^2 + x + 4$
4. -1
5. -3
6. -4
7. -2
8. -6
9. -3
10. 6
11. -3
12. 10
13. $\frac{1}{4}$

Operations with Functions: Domain

1. $\left[-\frac{7}{2}, \infty\right)$
2. $\left[-\frac{7}{2}, -1\right) \cup (-1, \infty)$
3. $\left(-\frac{7}{2}, \infty\right)$

Difference Quotient

1. 2
2. $2x + h + 4$
3. 0
4. $\frac{-3}{(x+2)(x+h+2)}$
5. $\frac{3}{\sqrt{3x+3h}+\sqrt{3x}}$
6. $2x + h - 2$
7. $\frac{-5}{x(x+h)}$
8. $-4x - 2h + 3$
9. $\frac{-12}{(2x+3)(2x+2h+3)}$
10. $\frac{7}{\sqrt{7x+7h+5}+\sqrt{7x+5}}$
11. $-2x - h + 1$
12. 3
13. $3x^2 + 3xh + h^2 + 5$

Chapter 7

Polynomials and Their Graphs

Determine the end behavior of each.

1. $f(x) = -x^5 + \sqrt{7}x^3 - 2x^2$
2. $g(x) = 4x^2 - 16x^6 + 3x$
3. $h(x) = 1 + x^{11} - 4x^8$
4. $f(x) = -x^4 + 3x^2 - 2x + 6$
5. $g(x) = 0.25x^5 - 0.1x^4 + 2x^2 - 6x$
6. $f(x) = -6x^3 + 2x^2 + 7x^4 - 1$
7. $g(x) = \frac{1}{3}x^3 - \frac{\pi}{8}x^2 + x\sqrt{2} - 3^4$

7.1 Answer Key

1. $\lim_{x\to-\infty} f(x) = \infty \quad \lim_{x\to\infty} f(x) = -\infty$
2. $\lim_{x\to-\infty} g(x) = -\infty, \quad \lim_{x\to\infty} g(x) = \infty$
3. $\lim_{x\to-\infty} h(x) = -\infty \quad \lim_{x\to\infty} h(x) = \infty$
4. $\lim_{x\to-\infty} f(x) = -\infty \quad \lim_{x\to\infty} f(x) = -\infty$
5. $\lim_{x\to-\infty} g(x) = -\infty \quad \lim_{x\to\infty} g(x) = \infty$
6. $\lim_{x\to-\infty} f(x) = \infty \quad \lim_{x\to\infty} f(x) = -\infty$
7. $\lim_{x\to-\infty} g(x) = -\infty \quad \lim_{x\to\infty} g(x) = \infty$

Chapter 8

Dividing Polynomials

8.1 Dividing Polynomials

Divide each.

1. $(28x^3 - 26x^2 + 41x - 15) \div (7x - 3)$
2. $(44y^2 + 12y^3 + 61y - 37) \div (3y + 5)$
3. $\left(4x^3 - 3x^2 + x + 1\right) \div (x + 2)$
4. $\left(5x^4 - x^2 + x - 2\right) \div (x^2 + 2)$
5. $\left(10x^3 + 27x^2 + 8x - 11\right) \div (2x + 3)$
6. $\left(7x^3 + 23x^2 + 12x + 1\right) \div \left(x^2 + 3x + 1\right)$

8.2 Remainder and Factor Theorems

Determine the remainder of each.

1. $\left(2x^{53} - 9x^{44} + 13x^8\right) \div (x - 1)$
2. $\left(x^{71} + 15x^{58} - 3x^{14} + 2\right) \div (x + 1)$
3. $\left(x^{23} - 5x^{20} + 17x^8 - 5\right) \div (x + 2)$
4. $\left(-7x^{17} + 40x^{15} - 6x^8 + 4x^3\right) \div (x - 3)$

8.3 Answer Key

Dividing Polynomials

1. $4x^2 - 2x + 5$
2. $4y^2 + 8y + 7 - \dfrac{72}{3y + 5}$
3. $4x^2 - 11x + 23 - \dfrac{45}{x + 2}$
4. $5x^2 - 11 + \dfrac{x + 20}{x^2 + 2}$
5. $5x^2 + 6x - 5 + \dfrac{4}{2x + 3}$
6. $7x + 2 + \dfrac{-x - 1}{x^2 + 3x + 1}$

Remainder and Factor Theorems

1. 6
2. 13
3. $-13,627,141$
4. $-330,064,119$

Chapter 9

Rational Functions and Their Graphs

Find the domain, coordinates of any holes, and equations of all asymptotes.

1. $f(x) = \dfrac{2x^2 + 5x - 3}{2x^2 - 15x + 7}$
2. $g(x) = \dfrac{3x^3 + 7x^2 - 20x}{x^2 - x - 12}$
3. $f(x) = \dfrac{3x}{x + 4}$
4. $g(x) = \dfrac{x^2 + 3x + 2}{x - 1}$
5. $h(x) = \dfrac{x^2 + 3x - 4}{x^3 - 2x^2 + x}$
6. $f(x) = \dfrac{2x^3 - 13x^2 + 6x + 45}{x^2 - 4x - 5}$
7. $g(x) = \dfrac{5x^2 - 19x - 4}{x^3 + 2x^2 - 24x}$
8. $h(x) = \dfrac{2x^2 - x - 3}{8x^2 + 51x + 18}$
9. $f(x) = \dfrac{6x^3 - 21x^2 - 51x + 30}{3x^2 + 7x + 2}$
10. $g(x) = \dfrac{10x^2 - 29x - 21}{10x^3 - 33x^2 - 7x}$

State the end behavior of each.

11. $k(x) = \dfrac{5x^3 - 7x^2 + 8}{-3x^3 + 6x - 4}$
12. $m(x) = \dfrac{2x - 1}{3x^2 + 7x + 1}$

9.1 Answer Key

1. Domain: $x \neq -\frac{1}{2}$, 7; V.A.: $x = 7$; Hole @ $\left(-\frac{1}{2}, -\frac{7}{13}\right)$; H.A.: $y = 1$
2. Domain: $x \neq -3$, 4; V.A.: $x = -3\, x = 4$; Obl. Asymp: $y = 3x + 10$
3. Domain: $x \neq -4$; V.A.: $x = -4$; H.A.: $y = 3$
4. Domain: $x \neq 1$; V.A.: $x = 1$; Obl. Asymp: $y = x + 4$
5. Domain: $x \neq 0, 1$; V.A.: $x = 0$ and $x = 1$; H.A.: $y = 0$
6. Domain: $x \neq -1, 5$; V.A. $x = -1$; Hole @ $\left(5, \frac{13}{3}\right)$; Obl. Asym $y = 2x - 5$
7. Domain: $x \neq -6, 0, 4$; V.A. $x = -6$, $x = 0$; Hole @ $\left(4, \frac{21}{40}\right)$; H.A. $y = 0$
8. Domain: $x \neq -6, -\frac{3}{8}$; V.A. $x = -6$, $x = -\frac{3}{8}$; H.A. $y = \frac{1}{4}$
9. Domain: $x \neq -2$, $-\frac{1}{3}$; Hole @ $(-2, -21)$; V.A.: $x = -\frac{1}{3}$; S.A. $y = 2x - \frac{35}{3}$
10. Domain: $x \neq -\frac{1}{5}$, 0, $\frac{7}{2}$; Hole @ $\left(\frac{7}{2}, \frac{82}{259}\right)$; V.A. $x = -\frac{1}{5}$ and $x = 0$; H.A. $y = 0$
11. $\lim_{x \to -\infty} k(x) = \infty = \lim_{x \to \infty} k(x) = -\frac{5}{3}$
12. $\lim_{x \to -\infty} m(x) = \infty = \lim_{x \to \infty} m(x) = 0$

Chapter 10

Polynomial and Rational Inequalities

10.1 Polynomial Inequalities

Solve each. Write your answers using interval notation.

1. $6x^3 - 4x^2 - 10x \geq 0$
2. $x^4 < 9x^2$
3. $3x^3 - 7x^2 - 22x + 8 < 0$
4. $3x^2 - 4x + 1 \leq 0$
5. $12x^4 + 76x^3 + 43x^2 - 346x - 280 \geq 0$
6. $-2x^4 + 49x^2 + 21x^3 - 1029x + 2401 \geq 0$
7. $-x^2 - 7x - 6 \leq 0$
8. $x^2 + 4x + 4 < 0$
9. $-x^4 - 6x^3 + 61x^2 + 234x - 1008 \geq 0$
10. $-x^2 + 3x + 1 > 3$
11. $-3x^4 + 123x^3 + 142x^2 - 424x + 320 \leq 122x^3$
12. $-x^4 - 1120 + 77x^2 - 36x + 15x^3 \geq 15x^3$
13. $-3x^4 - 22x^3 + 271x^2 + 152x - 96 \geq 267x^2$

10.2 Domain

State the domain of each. Write your answers using interval notation.

1. $b(x) = \sqrt{21x^2 - 23x - 20}$

10.3 Rational Inequalities

Solve each. Write your answers using interval notation.

1. $\dfrac{3x-4}{x+1} < 0$
2. $\dfrac{x^2+3x+2}{x-7} \leq 0$
3. $\dfrac{x^2-4x+4}{x^2-1} \geq 0$
4. $\dfrac{x+2}{x-4} \leq 1$
5. $\dfrac{x^2-7x-8}{x^2-4x-32} \geq 0$
6. $\dfrac{4+3x}{5-x} \leq 2$
7. $\dfrac{x-4}{x+7} < 0$
8. $\dfrac{x+5}{x+7} < 0$
9. $\dfrac{2x-26}{5x+20} > -3$
10. $\dfrac{2x-50}{5x+15} \leq -1$
11. $\dfrac{x+5}{x^2-2x-15} \leq 0$
12. $-\dfrac{2}{x} \geq -\dfrac{3}{x+1}$
13. $-\dfrac{3}{x+6} > -\dfrac{4}{x+7}$

10.4 Answer Key

Polynomial Inequalities

1. $[-1, 0] \cup \left[\frac{5}{3}, \infty\right)$
2. $(-3, 0) \cup (0, 3)$
3. $(-\infty, -2) \cup \left(\frac{1}{3}, 4\right)$
4. $\left[\frac{1}{3}, 1\right]$
5. $(-\infty, -4] \cup \left[-\frac{7}{2}, -\frac{5}{6}\right] \cup [2, \infty)$
6. $\left[-7, \frac{7}{2}\right] \cup 7$
7. $(-\infty, -6] \cup [-1, \infty)$
8. $\emptyset$
9. $[-8, -7] \cup [3, 6]$
10. $(1, 2)$
11. $(-\infty, -8] \cup \left[\frac{4}{3}, 2\right] \cup [5, \infty)$
12. $[-8, -4] \cup [5, 7]$
13. $[-6, -4] \cup \left[\frac{2}{3}, 2\right]$

Domain

1. $\left(-\infty, -\frac{12}{21}\right] \cup \left[\frac{5}{3}, \infty\right)$

Rational Inequalities

1. $\left(-1, \frac{4}{3}\right)$
2. $(-\infty, -2] \cup [-1, 7)$
3. $(-\infty, -1) \cup (1, \infty)$
4. $(-\infty, 4)$
5. $(-\infty, -4) \cup [-1, 8) \cup (8, \infty)$
6. $(-\infty, 1.2] \cup (5, \infty)$
7. $(-7, 4)$
8. $(-7, -5)$
9. $(-\infty, -4) \cup (-2, \infty)$
10. $(-3, 5]$
11. $(-\infty, -5] \cup (-3, 5)$
12. $(-1, 0) \cup [2, \infty)$
13. $(-7, -6) \cup (-3, \infty)$

Chapter 11

Function Compositions

Given $f(x) = x - 5$, $g(x) = 4 + \sqrt{2x+1}$, and $h(x) = \dfrac{3}{x+7}$, simplify each and state the domain.

1. $(f \circ g)(x)$
2. $(g \circ f)(x)$
3. $h(h(x))$

Find each of the following given the table below.

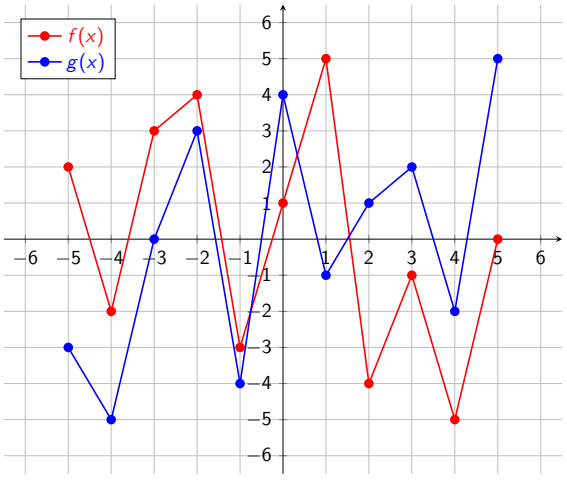
x	-4	-3	-2	-1	**0**	**1**	**2**	**3**	**4**
f(x)	-3	0	-1	3	1	2	4	-4	-2
g(x)	3	-1	0	1	4	-2	-4	2	-3

4. $(f \circ g)(-1)$
5. $(g \circ g)(0)$
6. $(f \circ f)(2)$
7. $(g \circ g)(-3)$
8. $f(g(0))$

Given $f(x) = \sqrt{3x+2}$, $g(x) = x^2 - 1$, and $h(x) = 9x - 2$, find each of the following.

9. $(g \circ f)(x)$
10. $f(g(x))$
11. $(h \circ h)(x)$

Find each of the following given the graphs of $f(x)$ (in red) and $g(x)$ (in blue) below:



12. $(f \circ g)(-1)$
13. $(g \circ f)(-4)$
14. $f(g(3))$
15. $g(g(-2))$
16. $(f \circ f)(-5)$

11.1 Answer Key

1. $-1+\sqrt{2x+1}$ Domain: $\left[-\frac{1}{2},\infty\right)$
2. $4+\sqrt{2x-9}$ Domain: $\left[\frac{9}{2},\infty\right)$
3. $\frac{3x+21}{7x+52}$ Domain: $\left(-\infty,-\frac{52}{7}\right)\cup\left(-\frac{52}{7},-7\right)\cup(-7,\infty)$
4. 2
5. -3
6. -2
7. 1
8. -2
9. $3x+1$
10. $\sqrt{3x^2-1}$
11. $81x-20$
12. -2
13. 3
14. -4
15. 2
16. -4

Chapter 12

Inverse Functions

Find the inverse of each. Then state the domain and range of the function and the inverse.

1. $f(x) = \sqrt{-2x+3} + 1$
2. $g(x) = (x+4)^2 - 1,\ x \leq -4$
3. $h(x) = \dfrac{9x}{4x-1}$
4. $f(x) = \sqrt{x} - 3$
5. $g(x) = \dfrac{1}{1-x}$
6. $h(x) = x^2 + 6x + 4,\ x \leq -3$
7. $f(x) = \sqrt{5x-4}$
8. $g(x) = x^2 - 2x + 3,\ x \leq 1$
9. $h(x) = \dfrac{3}{x-1}$

12.1 Answer Key

1. $f^{-1}(x) = -\frac{1}{2}\left((x-1)^2 - 3\right)$

	Domain	Range
$f(x)$	$(-\infty, 1.5]$	$[1, \infty)$
$f^{-1}(x)$	$[1, \infty)$	$(-\infty, 1.5]$

2. $g^{-1}(x) = -\sqrt{x+1} - 4$

	Domain	Range
$g(x)$	$(-\infty, -4]$	$[-1, \infty)$
$g^{-1}(x)$	$[-1, \infty)$	$(-\infty, -4]$

3. $h^{-1}(x) = \frac{-x}{9-4x}$

	Domain	Range
$h(x)$	$(-\infty, 1/4) \cup (1/4, \infty)$	$(\infty, 9/4) \cup (9/4, \infty)$
$h^{-1}(x)$	$(\infty, 9/4) \cup (9/4, \infty)$	$(-\infty, 1/4) \cup (1/4, \infty)$

4. $f^{-1}(x) = (x+3)^2$

	Dom	Ran
$f(x)$	$[0, \infty)$	$[-3, \infty)$
$f^{-1}(x)$	$[-3, \infty)$	$[0, \infty)$

5. $g^{-1}(x) = 1 - \frac{1}{x}$

	Dom	Ran
$g(x)$	$(-\infty, 1) \cup (1, \infty)$	$(-\infty, 0) \cup (0, \infty)$
$g^{-1}(x)$	$(-\infty, 0) \cup (0, \infty)$	$(-\infty, 1) \cup (1, \infty)$

6. $h^{-1}(x) = -\sqrt{x+5} - 3$

	Dom	Ran
$h(x)$	$(-\infty, -3]$	$[-5, \infty)$
$h^{-1}(x)$	$[-5, \infty)$	$(-\infty, -3]$

7. $f^{-1}(x) = \frac{1}{5}x^2 + \frac{4}{5}$

	Dom	Ran
$f(x)$	$\left[\frac{4}{5}, \infty\right)$	$[0, \infty)$
$f^{-1}(x)$	$[0, \infty)$	$\left[\frac{4}{5}, \infty\right)$

8. $g^{-1}(x) = -\sqrt{x-2} + 1$

	Dom	Ran
$g(x)$	$(-\infty, 1]$	$[2, \infty)$
$g^{-1}(x)$	$[2, \infty)$	$(-\infty, 1]$

9. $h^{-1}(x) = \frac{3}{x} + 1$

	Dom	Ran
$h(x)$	$(-\infty, 1) \cup (1, \infty)$	$(-\infty, 0) \cup (0, \infty)$
$h^{-1}(x)$	$(-\infty, 0) \cup (0, \infty)$	$(-\infty, 1) \cup (1, \infty)$

Chapter 13

Exponential Functions

13.1 End Behavior

Determine the end behavior of each. Write your answers using limit notation.

1. $f(x) = 3 + e^{2x}$
2. $h(x) = 5^{-x}$
3. $h(x) = -\frac{2}{3}e^{x+7} + 1$
4. $f(x) = -7e^{x} + 4$
5. $g(x) = \frac{1}{3}e^{2x+1} - 5$
6. $h(x) = -\frac{1}{2}e^{-4x} + 1$

13.2 Answer Key

1. $\lim_{x\to-\infty} f(x) = 3 \quad \lim_{x\to\infty} f(x) = \infty$
2. $\lim_{x\to-\infty} f(x) = \infty \quad \lim_{x\to\infty} f(x) = 0$
3. $\lim_{x\to-\infty} h(x) = 1 \quad \lim_{x\to\infty} h(x) = -\infty$
4. $\lim_{x\to-\infty} f(x) = 4 \quad \lim_{x\to\infty} f(x) = -\infty$
5. $\lim_{x\to-\infty} f(x) = -5 \quad \lim_{x\to\infty} f(x) = \infty$
6. $\lim_{x\to-\infty} f(x) = -\infty \quad \lim_{x\to\infty} f(x) = 1$

Chapter 14

Logarithmic Functions

Write each of the following in exponential or logarithmic form.

1. $\ln(a) = 7$
2. $\log_4(x+1) = 9$
3. $\log(5x) = 30$
4. $\ln(w) = c$
5. $5^x = 19$
6. $8^{-3} = \dfrac{1}{512}$
7. $e^{14} = x$
8. $(1.1)^{-t} = 50$

Find the domain of each. Write your answers in interval notation.

9. $b(x) = \log_7\left(x^2 - 8x + 6\right)$
10. $a(x) = \ln\left(\dfrac{x^2 + 3x + 2}{5x + 15}\right)$
11. $f(x) = -7\ln\left(x^2 + 9x + 8\right)$
12. $g(x) = \log\left(5x^2 + 13x - 6\right)$
13. $h(x) = 3\log_2\left(x^3 + 2x^2 - x - 2\right)$
14. $c(x) = \ln\left(4x^2 - 15x - 4\right)$

State the end behavior of each.

15. $j(x) = 5\log_3(2x - 5) - 2$

14.1 Answer Key

1. $e^7 = a$
2. $4^9 = x + 1$
3. $10^{30} = 5x$
4. $e^c = w$
5. $\log_5(19) = x$
6. $\log_8\left(\frac{1}{512}\right) = -3$
7. $\ln(x) = 14$
8. $\log_{1.1}(50) = -t$
9. $(-\infty, 0.838) \cup (7.162, \infty)$
10. $(-3, -2) \cup (-1, \infty)$
11. $(-\infty, -8) \cup (-1, \infty)$
12. $(-\infty, -3) \cup \left(\frac{2}{5}, \infty\right)$
13. $(-2, -1) \cup (1, \infty)$
14. $\left(-\infty, -\frac{1}{4}\right) \cup (4, \infty)$
15. $\lim_{x \to (5/2)^+} j(x) = -\infty \quad \lim_{x \to \infty} j(x) = \infty$

Chapter 15

Properties of Logarithms

Expand or condense each completely. Simplify numerical answers.

1. $\log_b\left(\frac{x^2}{y^8}\right)$
2. $\ln(ez)^3$
3. $\log_5(x) + \log_5(9) - 2\log_5(w)$

Write an equivalent expression for each of the following using natural logarithms.

4. $\log_7(10)$
5. $\log_9(x)$
6. $\log_b(c)$
7. $\log_3(10)$
8. $\log_{17}(\pi)$
9. $\log_w(x)$

Suppose that $\log_a(b) = 5$, $\log_a(c) = 12$, and $\log_a(d) = 9$. Evaluate each of the following.

10. $\log_a(bc)$
11. $\log_a(c^3)$
12. $\log_a\left(\frac{d}{c}\right)$
13. $\log_a\left(\frac{bd}{c}\right)$

15.1 Answer Key

1. $2\log_b(x) - 8\log_b(y)$
2. $3 + 3\ln(z)$
3. $\log_5\left(\frac{9x}{w^2}\right)$
4. $\frac{\ln(10)}{\ln(7)}$
5. $\frac{\ln(x)}{\ln(9)}$
6. $\frac{\ln(c)}{\ln(b)}$
7. $\frac{\ln(10)}{\ln(3)}$
8. $\frac{\ln(\pi)}{\ln(17)}$
9. $\frac{\ln(x)}{\ln(w)}$
10. 17
11. 36
12. -3
13. 2

Chapter 16

Exponential Equations

Solve each. Round to 3 decimal places when necessary.

1. $3e^{x-2} = 7$
2. $5^x + 4 > 1$
3. $2^{3x+4} = 32^{x-7}$
4. $5e^{7x} + 10 = 42$
5. $7^{4x+1} \geq 343$
6. $1000e^{0.04x} = 2000$
7. $3(4.1)^{x-2} = 8$
8. $2^{x+1} = 5^{7x-5}$
9. $8(17)^{-5x} = 22$
10. $-3(11)^{x-10} = -58$
11. $12^{-10x} + 8 = 80$
12. $-5(10)^{7x} + 9 = -46$
13. $8(8)^{10x} - 1 = 55.2$
14. $3(3)^{-5x} - 8 = 74$
15. $6(16)^{4x-9} = 19$
16. $-7(11)^{5x-7} = -3$
17. $3^{9-6x} - 7 = 26$

16.1 Applications

1. Plutonium has a half-life of 24,360 years. If 15 grams are initially present, how long until 9.5 grams remain?
2. Cadmium-109 has a half-life of about 1.267 years. If 50 mg are initially present, how many years will it take for 16 mg to remain?
3. The half-life of bismuth-207 is about 32.9 years. If 90 mg are initially present, how many years will it take for 75 mg to remain?

16.2 Answer Key

1. $x \approx 2.847$
2. $(-\infty, \infty)$
3. $x = 19.5$
4. $x \approx 0.265$
5. $\left[\frac{1}{2}, \infty\right)$
6. $x \approx 17.329$
7. $x \approx 2.695$
8. $x \approx 0.827$
9. $x \approx -0.071$
10. $x \approx 11.235$
11. $x \approx -0.172$
12. $x \approx 0.149$
13. $x \approx 0.094$
14. $x \approx -0.602$
15. $x \approx 2.354$
16. $x \approx 1.323$
17. $x \approx 0.970$

Applications

1. Approximately 17,952 years
2. Approximately 2.0828 years
3. Approximately 8.6538 years

Chapter 17

Logarithmic Equations and Inequalities

Solve each. Round to 3 decimal places when necessary.

1. $\log_5(x) + x\log_5(x) > 0$
2. $\ln\left(8 - x^2\right) = \ln(2 - x)$
3. $\log_{25}\left(\frac{3x+1}{2x-2}\right) = \frac{1}{2}$
4. $\log_3(2x+1) - \log_3(x-5) = \log_3(x+1)$
5. $\log_4(x+1) + \log_4(x-5) > 2$
6. $\log(x+1) - \log(x-5) = \log(x-3)$
7. $x\log_3(x+2) - \log_3(x+2) = 0$
8. $\log_{1/2}(x+1) > -3$
9. $\log_{12}(4x+4) = \log_{12}(5x+1)$
10. $\log_{15}(-4x+2) = \log_{15}(6-2x)$
11. $\log_{11}(-5-3x^2) = \log_{11}(-2x^2+6x)$
12. $\log_{16}(x^2+4) = \log_{16}(2x+3)$
13. $\log_7(8x-1) = \log_7(x^2+14)$
14. $-7\log_5(x+5) = -7$
15. $7\log_8(-x) = 28$
16. $-10\log_3(x-5) = -20$

17.1 Answer Key

1. $(1, \infty)$
2. $x = -2$
3. $x \approx 1.571$
4. $x \approx 6.873$
5. $(2, \infty)$
6. $x = 7$
7. $x = \pm 1$
8. $(-1, 7)$
9. $x = 3$
10. $x = -2$
11. No Solution
12. $x = 1$
13. $x = 3,\ 5$
14. $x = 0$
15. $x = -4096$
16. $x = 14$

Chapter 18

Sequences

Write the first 4 terms of each sequence.

1. $a_n = 2(-3)^n$
2. $b_n = \dfrac{n!}{2^n}$
3. $c_{n+1} = 5c_n + 1;\ c_1 = 2$
4. $d_n = \dfrac{1}{2}d_{n-1} + n;\ d_1 = 3$

Find the indicated term of each sequence. For term values above 10 billion or below 0.00001, write the first 4 digits after the decimal point when the answer is given in scientific notation. **Do not round**.

5. $a_n = \{343,\ 667,\ 991,\ 1315, \ldots\}$; Find the 582nd term.
6. $b_n = \{300,\ 240,\ 192, 153.6,\ \ldots\}$; Find the 711th term.
7. $c_n = \left\{1,\ \dfrac{1}{3},\ \dfrac{1}{5},\ \dfrac{1}{7},\ \ldots\right\}$; Find the 8,675,309th term.

Given each sequence, find the first 4 digits **after the decimal point** in the **scientific notation** version of each term.

8. $a_n = 17,\ 33,\ 49,\ 65,\ \ldots;\quad a_{21,972}$
9. $b_n = 25,\ 36,\ 49,\ 64,\ 81,\ \ldots\quad b_{413,401}$
10. $c_n = \dfrac{1}{3},\ \dfrac{1}{6},\ \dfrac{1}{12},\ \dfrac{1}{24},\ \ldots\quad c_{152}$

18.1 Answer Key

1. -6, 18, -54, 162
2. $\frac{1}{2}$, $\frac{1}{2}$, $\frac{3}{4}$, $\frac{3}{2}$
3. 2, 11, 56, 281
4. 3, $\frac{7}{2}$, $\frac{19}{4}$, $\frac{51}{8}$
5. 188,587
6. 6882
7. 7634
8. 5155 (3.51553×10^{5})
9. 7090 ($1.7090369403 \times 10^{11}$)
10. 1677 ($1.1677487203 \times 10^{-46}$)

Chapter 19

Series

Find the sum of each, if possible.

1. $\sum_{i=1}^{\infty} \left(\frac{1}{5}\right)^i$
2. $\sum_{i=0}^{\infty} 3\left(-\frac{2}{3}\right)^i$
3. $\sum_{k=1}^{\infty} -2\left(\frac{1}{3}\right)^k$
4. $\sum_{j=0}^{\infty} -\frac{1}{2}\left(\frac{3}{2}\right)^j$
5. $\sum_{i=0}^{\infty} 1.2(0.8)^i$
6. $\sum_{i=1}^{\infty} 1.2(0.8)^i$
7. $\sum_{i=0}^{\infty} 0.8(1.2)^i$
8. $\sum_{k=1}^{\infty} \frac{2}{3^k}$

Find the sum of each of the following. Round to 4 decimal places when necessary.

9. $9 + 13 + 17 + 21 + \cdots + 1565$
10. $-3 + 6 - 12 + 24 - 48 + \cdots + 50,331,648$
11. $1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \frac{1}{5} + \cdots + \frac{1}{981}$
12. $2 + 4 + 6 + 8 + 10 + \cdots + 38,214$
13. $3 + 7 + 11 + 15 + \cdots + 11,491$
14. $\frac{4}{5} + \frac{5}{6} + \frac{6}{7} + \cdots + \frac{742}{743}$

19.1 Answer Key

1. $\frac{1}{4}$
2. $\frac{9}{5}$
3. -1
4. Diverges
5. 6
6. 4.8
7. Diverges
8. 2
9. 306,930
10. $-33,554,433$
11. 7.4663
12. 365,096,556
13. 16,511,131
14. 733.8947

Chapter 20

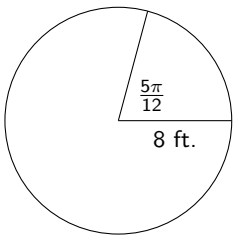
Angles and Radian Measure

Sketch each of the following. Then find a coterminal between 0 and 360° (or 0 and 2π radians) for each.

1. $-\frac{3\pi}{4}$
2. 900°
3. $\frac{27\pi}{10}$
4. -125°

Find the arc length and sector area formed by the central angle of each. Exact answers only.

5.



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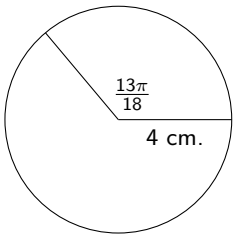

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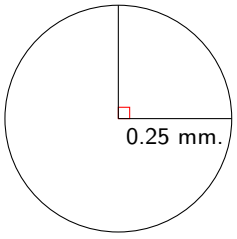
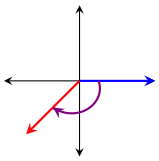


A belt runs on a pulley with radius 4 inches at 250 revolutions per minute.

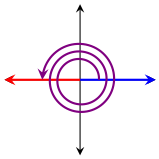
8. Find the angular velocity in rad/sec. Round your answer to 2 decimal places.
9. Find the linear velocity in ft/sec. Round your answer to 2 decimal places.

20.1 Answer Key

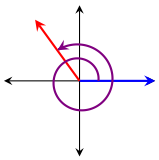
1. $\frac{5\pi}{4}$



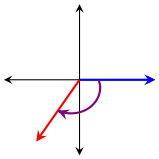
2. 180°



3. $\frac{7\pi}{10}$



4. 235°



5. $s = \frac{10\pi}{3}$ ft.; $A = \frac{40\pi}{3}$ sq.ft.
6. $s = \frac{26\pi}{9}$ cm.; $A = \frac{52\pi}{9}$ sq.cm.
7. $s = \frac{\pi}{8}$ mm.; $A = \frac{\pi}{64}$ sq.mm.
8. 26.18 rad/sec
9. 8.73 ft/sec

Chapter 21

Trig Functions of Any Angle

Find the exact value of each of the six trig functions of θ if P is a point on the terminal side of θ.

1. $P(-2, 3)$
2. $P(0, -4)$
3. $P(-2\sqrt{3}, 2)$
4. $P(-3, 5)$
5. $P(-2, 1)$
6. $P(-4, -7)$

Find the exact values of the 6 trig functions of the following angles.

7. $\theta = \dfrac{-17\pi}{4}$
8. $\theta = \dfrac{21\pi}{2}$
9. $\theta = 24\pi$

21.1 Answer Key

1. $\sin\theta = \frac{3\sqrt{13}}{13}$, $\cos\theta = \frac{-2\sqrt{13}}{13}$, $\tan\theta = -\frac{3}{2}$, $\csc\theta = \frac{\sqrt{13}}{3}$, $\sec\theta = -\frac{\sqrt{13}}{2}$, $\cot\theta = -\frac{2}{3}$
2. $\sin\theta = -1$, $\cos\theta = 0$, $\tan\theta =$ undef., $\csc\theta = -1$, $\sec\theta =$ undef., $\cot\theta = 0$
3. $\sin\theta = \frac{1}{2}$, $\cos\theta = -\frac{\sqrt{3}}{2}$, $\tan\theta = -\frac{\sqrt{3}}{3}$, $\csc\theta = 2$, $\sec\theta = -\frac{2\sqrt{3}}{3}$, $\cot\theta = -\sqrt{3}$
4. $\sin\theta = \frac{5\sqrt{34}}{34}$, $\cos\theta = -\frac{3\sqrt{34}}{34}$, $\tan\theta = -\frac{5}{3}$, $\csc\theta = \frac{\sqrt{34}}{5}$, $\sec\theta = -\frac{\sqrt{34}}{3}$, $\cot\theta = -\frac{3}{5}$
5. $\sin\theta = \frac{\sqrt{5}}{5}$, $\cos\theta = -\frac{2\sqrt{5}}{5}$, $\tan\theta = -\frac{1}{2}$, $\csc\theta = \sqrt{5}$, $\sec\theta = -\frac{\sqrt{5}}{2}$, $\cot\theta = -2$
6. $\sin\theta = -\frac{7\sqrt{65}}{65}$, $\cos\theta = -\frac{4\sqrt{65}}{65}$, $\tan\theta = \frac{7}{4}$, $\csc\theta = -\frac{\sqrt{65}}{7}$, $\sec\theta = -\frac{\sqrt{65}}{4}$, $\cot\theta = \frac{4}{7}$
7. $\sin\theta = -\frac{\sqrt{2}}{2}$, $\cos\theta = \frac{\sqrt{2}}{2}$, $\tan\theta = -1$, $\csc\theta = -\sqrt{2}$, $\sec\theta = \sqrt{2}$, $\cot\theta = -1$
8. $\sin\theta = 1$, $\cos\theta = 0$, $\tan\theta =$ undefined, $\csc\theta = 1$, $\sec\theta =$ undefined, $\cot\theta = 0$
9. $\sin\theta = 0$, $\cos\theta = 1$, $\tan\theta = 0$, $\csc\theta =$ undefined, $\sec\theta = 1$, $\cot\theta =$ undefined

Chapter 22

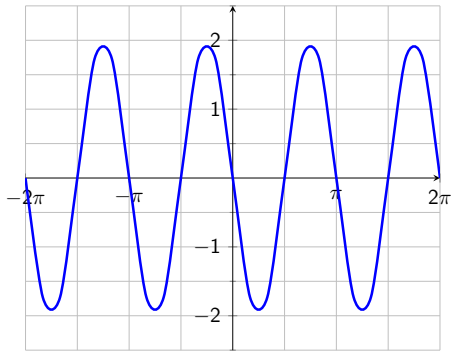
Graphs of Sine and Cosine Functions

Determine the amplitude, period, phase shift, and vertical shift for each. Exact answers only.

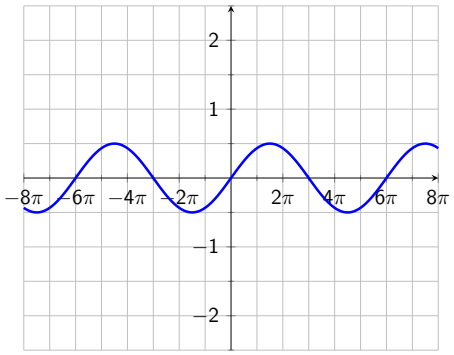
1. $f(x) = -2\sin\left(3x - \frac{\pi}{4}\right) + 1$
2. $g(x) = \frac{1}{3}\cos\left(\frac{1}{2}x + 2\right)$
3. $f(x) = 2\sin\left(x - \frac{\pi}{3}\right) + 7$
4. $f(x) = -4\cos\left(\frac{2}{3}x - \frac{2\pi}{3}\right)$

Write the equation of each of the following in the form $y = a\sin(bx)$.

5.



6.



22.1 Answer Key

1. Amp $= 2$, Per $= \dfrac{2\pi}{3}$, P.S. $= \dfrac{\pi}{12}\ \rightarrow$, V.S. $= 1\ \uparrow$
2. Amp $= \dfrac{1}{3}$, Per $= 4\pi$, P.S. $= 4\ \leftarrow$, V.S. $=$ None
3. Amp $= 2$, Period $= 2\pi$, P.S. $= \dfrac{\pi}{3}$ right, V.S. $= 7$ up
4. Amp $= 4$, Period $= 3\pi$, P.S. $= \pi$ right, V.S. $= 0$ (or none)
5. $y = -2\sin(2x)$
6. $y = \dfrac{1}{2}\sin\left(\dfrac{1}{3}x\right)$

Chapter 23

Graphs of Other Trig Functions

Determine the amplitude, period, phase shift, and vertical shift for each. Exact answers only.

1. $h(x) = \tan\left(\frac{3}{4}x + \frac{\pi}{12}\right) - 8$
2. $f(x) = 3\tan\left(2x + \frac{\pi}{2}\right) - \sqrt{3}$

23.1 Answer Key

1. Amp = n/a, Per = $\frac{4\pi}{3}$, P.S. = $\frac{\pi}{9}$ $\leftarrow$, V.S. = 8 $\downarrow$
2. Amp = n/a, Period = $\frac{\pi}{2}$, P.S. = $\frac{\pi}{4}$ left, V.S. = $\sqrt{3}$ down

Chapter 24

Inverse Trig Functions

State the exact, simplified value of each or write as an expression of x.

1. $\tan^{-1}\left(-\sqrt{3}\right)$
2. $\sec\left(\sin^{-1}\left(\frac{2}{5}\right)\right)$
3. $\cot\left(\sec^{-1}(x)\right)$
4. $\sin\left(\cos^{-1}\left(\frac{3x}{4}\right)\right)$
5. $\cot\left(\csc^{-1}\left(-\frac{7}{2}\right)\right)$
6. $\sec\left(\arcsin\left(\frac{9}{13}\right)\right)$
7. $\cos\left(\tan^{-1}(7x)\right)$
8. $\sin\left(\sec^{-1}\left(\frac{8}{x}\right)\right)$

24.1 Answer Key

1. $-\frac{\pi}{3}$
2. $\frac{5\sqrt{21}}{21}$
3. $\frac{1}{\sqrt{x^2-1}} = \frac{\sqrt{x^2-1}}{x^2-1}$
4. $\frac{\sqrt{16-9x^2}}{4}$
5. $-\frac{3\sqrt{5}}{2}$
6. $\frac{13\sqrt{22}}{44}$
7. $\frac{\sqrt{49x^2+1}}{49x^2+1}$
8. $\frac{\sqrt{64-x^2}}{x}$

Chapter 25

Trig Equations and Inequalities

Solve each in the interval $[0, 2\pi)$. Write your answers to inequalities using interval notation.

1. $\tan(6x) = 1$
2. $\cot(2x) = -\frac{\sqrt{3}}{3}$
3. $\sin^2(x) = \frac{3}{4}$
4. $\sin(2x) = \cos(x)$
5. $\sin(2x) \geq \sin(x)$
6. $\cos(2x) < 0$
7. $2\sin\left(x - \frac{\pi}{3}\right) = -1$
8. $3\tan\left(-2x + \frac{\pi}{2}\right) = \sqrt{3}$
9. $\sin^2(x) < \frac{1}{2}$
10. $\tan^2(x) = 3\sec(x) - 3$
11. $2\csc(x) - 3\csc^2(x) = -2\csc^2(x) + 1$
12. $-2\cot(x) - \csc^2(x) = 0$
13. $\tan(x) = -\tan(x)\cos(x)$
14. $3\cos(x) = 2\cos^2(x) + 1$
15. $\csc(x) - \cot^2(x) + 1 = 0$
16. $-\sin(x) + \sin(2x) = 2\sin(2x)$
17. $3\cos(x) = \sin(2x) + 2\cos(x)$

25.1 Answer Key

1. $\frac{\pi}{24}, \frac{5\pi}{24}, \frac{3\pi}{8}, \frac{13\pi}{24}, \frac{17\pi}{24}, \frac{7\pi}{8}, \frac{25\pi}{24}, \frac{29\pi}{24}, \frac{11\pi}{8}, \frac{37\pi}{24}, \frac{41\pi}{24}, \frac{15\pi}{8}$
2. $\frac{\pi}{3}, \frac{5\pi}{6}, \frac{4\pi}{3}, \frac{11\pi}{6}$
3. $\frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}, \frac{5\pi}{3}$
4. $\frac{\pi}{2}, \frac{5\pi}{6}, \frac{3\pi}{2}$
5. $\left[0, \frac{\pi}{3}\right] \cup \left[\pi, \frac{5\pi}{3}\right]$
6. $\left(\frac{\pi}{4}, \frac{3\pi}{4}\right) \cup \left(\frac{5\pi}{4}, \frac{7\pi}{4}\right)$
7. $x = \frac{\pi}{6}, \frac{3\pi}{2}$
8. $x = \frac{\pi}{6}, \frac{2\pi}{3}, \frac{7\pi}{6}, \frac{5\pi}{3}$
9. $\left[0, \frac{\pi}{4}\right) \cup \left(\frac{3\pi}{4}, \frac{5\pi}{4}\right) \cup \left(\frac{7\pi}{4}, 2\pi\right)$
10. $x = 0\, \frac{\pi}{3}, \frac{5\pi}{3}$
11. $x = \frac{\pi}{2}$
12. $x = \frac{3\pi}{4}, \frac{7\pi}{4}$
13. $x = 0, \pi$
14. $x = 0\, \frac{\pi}{3}, \frac{5\pi}{3}$
15. $x = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{3\pi}{2}$
16. $x = 0, \frac{2\pi}{3}, \pi, \frac{4\pi}{3}$
17. $x = \frac{\pi}{6}, \frac{\pi}{2}, \frac{5\pi}{6}, \frac{3\pi}{2}$

Chapter 26

Law of Sines and Cosines

Solve each of the following. Round your answers to 1 decimal place.

1. $m\angle B = 37.8^\circ$, $a = 15$, $c = 21.1$
2. $m\angle A = 41.9^\circ$, $m\angle C = 59.2^\circ$, $a = 10.2$
3. $a = 14$, $b = 19.6$, $c = 13.1$
4. $c = 29$, $b = 23$, $m\angle A = 55^\circ$
5. $c = 8$, $b = 12$, $m\angle A = 90^\circ$
6. $m\angle B = 67.2^\circ$, $a = 15.6$, $c = 18.9$
7. $b = 20$, $a = 30$, $c = 12$
8. $a = 14$, $b = 6$, $c = 12$
9. $a = 7$, $b = 14$, $c = 12$
10. $m\angle B = 119^\circ$, $a = 11$, $b = 28$
11. $m\angle A = 125^\circ$, $c = 21$, $a = 28$
12. $m\angle B = 108^\circ$, $m\angle C = 61^\circ$, $b = 25$

26.1 Answer Key

1. $b \approx 13.0$, $m\angle A \approx 44.8^\circ$, $m\angle C \approx 97.4^\circ$
2. $m\angle B = 78.9^\circ$, $b \approx 15.0$, $c \approx 13.1$
3. $m\angle A \approx 45.5^\circ$, $m\angle B \approx 92.6^\circ$, $m\angle C \approx 41.9^\circ$
4. $m\angle B \approx 50.1^\circ$, $m\angle C \approx 74.9^\circ$, $a \approx 24.6$
5. $m\angle B \approx 56.3^\circ$, $m\angle C \approx 33.7^\circ$, $a \approx 14.4$
6. $m\angle A \approx 48.2^\circ$, $m\angle C \approx 64.6^\circ$, $b \approx 19.3$
7. $m\angle A \approx 137.8^\circ$, $m\angle B \approx 26.6^\circ$, $m\angle C \approx 15.6^\circ$
8. $m\angle A \approx 96.4^\circ$, $m\angle B \approx 25.2^\circ$, $m\angle C \approx 58.4^\circ$
9. $m\angle A \approx 30^\circ$, $m\angle B \approx 91^\circ$, $m\angle C \approx 59^\circ$
10. $m\angle A \approx 20.1^\circ$, $m\angle C \approx 40.9^\circ$, $c \approx 21$
11. $m\angle B \approx 17.1^\circ$, $m\angle C \approx 37.9^\circ$, $b \approx 10.1$
12. $m\angle A \approx 11^\circ$, $a \approx 5$, $c \approx 23$

Chapter 27

Area of Triangles

Find the area of each. Round your answers to 1 decimal place.

1. $m\angle B = 37.8^\circ$, $a = 15$, $c = 21.1$
2. $m\angle A = 41.9^\circ$, $m\angle C = 59.2^\circ$, $a = 10.2$
3. $a = 14$, $b = 19.6$, $c = 13.1$
4. $p = 14$, $k = 9$, $h = 9$
5. $m\angle T = 15^\circ$, $m\angle S = 140^\circ$, $r = 11.1$
6. $m\angle Z = 67^\circ$, $y = 6$, $m\angle Y = 41^\circ$
7. $m\angle R = 129^\circ$, $r = 10$, $m\angle P = 28^\circ$
8. $a = 6.9$, $m\angle B = 115^\circ$, $m\angle C = 39^\circ$
9. $d = 6$, $3 = 12$, $f = 8$
10. $m\angle Y = 120^\circ$, $x = 13$, $m\angle Z = 21^\circ$
11. $z = 10$, $y = 14$, $x = 6$
12. $m\angle P = 18^\circ$, $h = 6.9$, $m\angle H = 147^\circ$
13. $m\angle S = 118^\circ$, $m\angle T = 30^\circ$, $s = 6.3$
14. $r = 8$, $t = 7.5$, $m\angle S = 50^\circ$
15. $d = 15.3$, $m\angle E = 105^\circ$, $f = 5$
16. $m\angle R = 31^\circ$, $p = 12$, $m\angle Q = 26^\circ$
17. $m\angle D = 120^\circ$, $f = 4$, $m\angle E = 36^\circ$

27.1 Answer Key

1. Approximately 97.0 sq. units
2. Approximately 65.7 sq. units
3. Approximately 91.6 sq. units
4. Approximately 39.6 sq. units
5. Approximately 24.3 sq. units
6. Approximately 24.0 sq. units
7. Approximately 11.7 sq. units
8. Approximately 31.0 sq. units
9. Approximately 21.3 sq. units
10. Approximately 41.7 sq. units
11. Approximately 26.0 sq. units
12. Approximately 3.5 sq. units
13. Approximately 6.0 sq. units
14. Approximately 23.0 sq. units
15. Approximately 36.9 sq. units
16. Approximately 19.5 sq. units
17. Approximately 10.0 sq. units

Chapter 28

Polar Coordinates

Convert each to exact rectangular coordinates.

1. $\left(3, \frac{5\pi}{6}\right)$
2. $\left(-2, -\frac{\pi}{4}\right)$
3. $\left(\frac{5}{2}, 240^\circ\right)$

Convert each to exact polar coordinates. Use $r > 0$ and $0 \leq \theta < 2\pi$.

4. $\left(-2\sqrt{3}, -2\right)$
5. $\left(-\frac{1}{2}, \frac{1}{2}\right)$
6. $\left(7\sqrt{2}, -7\sqrt{2}\right)$

Convert each to either rectangular or polar coordinates.

7. $2x + 5y = 9$
8. $3y = 1$
9. $-5x - 8y = -10$
10. $r = 8$
11. $r = 4\sec(\theta)$
12. $\theta = -\frac{\pi}{6}$

28.1 Answer Key

1. $\left(-\frac{3\sqrt{3}}{2}, \frac{3}{2}\right)$
2. $(-\sqrt{2}, \sqrt{2})$
3. $\left(\frac{5}{4}, \frac{5\sqrt{3}}{4}\right)$
4. $\left(4, \frac{7\pi}{6}\right)$
5. $\left(\frac{\sqrt{2}}{2}, \frac{3\pi}{4}\right)$
6. $\left(14, \frac{7\pi}{4}\right)$
7. $r = \frac{9}{2\cos\theta + 5\sin\theta}$
8. $r = \frac{1}{3}\csc\theta$
9. $r = \frac{10}{5\cos\theta + 8\sin\theta}$
10. $x^2 + y^2 = 64$
11. $x = 4$
12. $y = -\frac{\sqrt{3}}{3}x$

Chapter 29

Vectors

Given $\vec{v} = 3\mathbf{i} - 5\mathbf{j}$ and $\vec{w} = \langle -2, 1 \rangle$, find each. Exact and simplified answers only.

1. $\vec{v} + \vec{w}$
2. $-4\vec{w}$
3. $|v|$
4. $\hat{w}$

Given $\vec{a} = \langle 4, -3 \rangle$, $\mathbf{b} = 11\mathbf{i} + 2\mathbf{j}$, and $\vec{c} = \langle 0, 2 \rangle$, find each. Exact and simplified answers only.

5. $\vec{a} + \vec{b}$
6. $\vec{a} - \vec{b}$
7. $\mathbf{a} + \mathbf{c}$
8. $-\mathbf{b}$
9. $2\vec{c}$
10. $3\vec{a} + 5\vec{b}$
11. $-2\vec{c} - 1.5\vec{a}$
12. $||\vec{b}||$
13. $|\mathbf{c}|$
14. $\hat{a}$
15. $\hat{b}$
16. $\hat{c}$

Find the exact horizontal and vertical component form of each vector with the given magnitude and direction angle.

17. $|u| = 8, \quad \theta = 120^\circ$
18. $|u| = 5, \quad \theta = \dfrac{\pi}{4}$
19. $|u| = 1.5, \quad \theta = -300^\circ$
20. $|u| = \sqrt{2}, \quad \theta = \dfrac{3\pi}{2}$
21. $|u| = 4, \quad \theta = 210^\circ$
22. $|u| = 2\sqrt{3}, \quad \theta = -\dfrac{\pi}{6}$

Write each of the following in $|\vec{v}|\langle \cos(\theta), \sin(\theta) \rangle$ form, where $0 \leq \theta < 2\pi$.

23. $\vec{v} = \langle \sqrt{2}, -\sqrt{2} \rangle$
24. $\vec{v} = \langle -1, \sqrt{3} \rangle$
25. $\vec{v} = \langle 0, 4 \rangle$

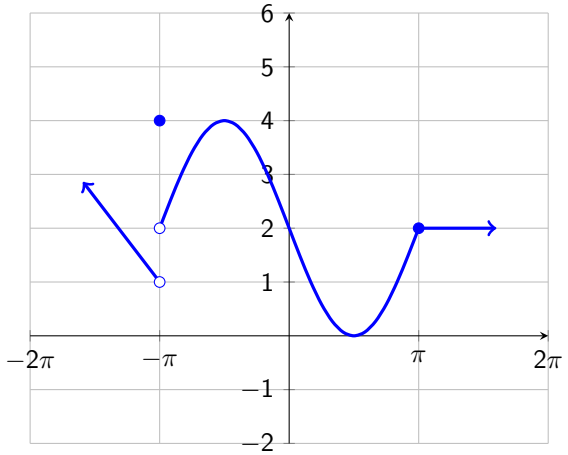
29.1 Answer Key

1. $\mathbf{i} - 4\mathbf{j}$
2. $\langle 8, -4 \rangle$
3. $\sqrt{34}$
4. $\left\langle -\frac{2\sqrt{5}}{5}, \frac{\sqrt{5}}{5} \right\rangle$
5. $\langle 15, -1 \rangle$
6. $\langle -7, -5 \rangle$
7. $\langle 4, -1 \rangle$
8. $\langle -11, -2 \rangle$
9. $\langle 0, 4 \rangle$
10. $\langle 67, 1 \rangle$
11. $\langle -6, 0.5 \rangle$
12. $5\sqrt{5}$
13. 2
14. $\left\langle \frac{4}{5}, -\frac{3}{5} \right\rangle$
15. $\left\langle \frac{11\sqrt{5}}{25}, \frac{2\sqrt{5}}{25} \right\rangle$
16. $\langle 0, 1 \rangle$
17. $\left\langle -4, 4\sqrt{3} \right\rangle$
18. $\left\langle \frac{5\sqrt{2}}{2}, \frac{5\sqrt{2}}{2} \right\rangle$
19. $\left\langle \frac{3}{4}, \frac{3\sqrt{3}}{4} \right\rangle$
20. $\left\langle 0, -\sqrt{2} \right\rangle$
21. $\left\langle -2\sqrt{3}, -2 \right\rangle$
22. $\left\langle 3, -\sqrt{3} \right\rangle$
23. $2\left\langle \cos\left(\frac{7\pi}{4}\right), \sin\left(\frac{7\pi}{4}\right) \right\rangle$
24. $2\left\langle \cos\left(\frac{2\pi}{3}\right), \sin\left(\frac{2\pi}{3}\right) \right\rangle$
25. $4\left\langle \cos\left(\frac{\pi}{2}\right), \sin\left(\frac{\pi}{2}\right) \right\rangle$

Chapter 30

Numerical and Graphical Limits

Solve using the graph of $f(x)$ below.



1. $\lim_{x \to -\pi^-} f(x)$
2. $\lim_{x \to -\pi^+} f(x)$
3. $\lim_{x \to -\pi} f(x)$
4. $f(-\pi)$
5. $\lim_{x \to \pi^-} f(x)$
6. $\lim_{x \to \pi^+} f(x)$
7. $\lim_{x \to \pi} f(x)$
8. $f(\pi)$

30.1 Answer Key

1. 1
2. 2
3. Does not exist
4. 4
5. 2
6. 2
7. 2
8. 2

Chapter 31

Algebraic Limits

Evaluate each limit.

1. $\lim\limits_{x \to -4} \left(\dfrac{x+4}{x^2+6x+8} \right)$
2. $\lim\limits_{x \to -3} \left(-\dfrac{x^2+2x-3}{x+3} \right)$
3. $\lim\limits_{x \to 3} \left(\dfrac{x-3}{x^2-8x+15} \right)$
4. $\lim\limits_{x \to -2} \left(\dfrac{x^2-2x-8}{x+2} \right)$
5. $\lim\limits_{x \to -1} \left(-\dfrac{x^2+5x+4}{x+1} \right)$
6. $\lim\limits_{x \to -4} \left(\dfrac{x^2+7x+12}{x+4} \right)$
7. $\lim\limits_{x \to 2} \left(\dfrac{x^2-2x}{x-2} \right)$
8. $\lim\limits_{x \to -1} \left(-\dfrac{x^2-3x-4}{x+1} \right)$

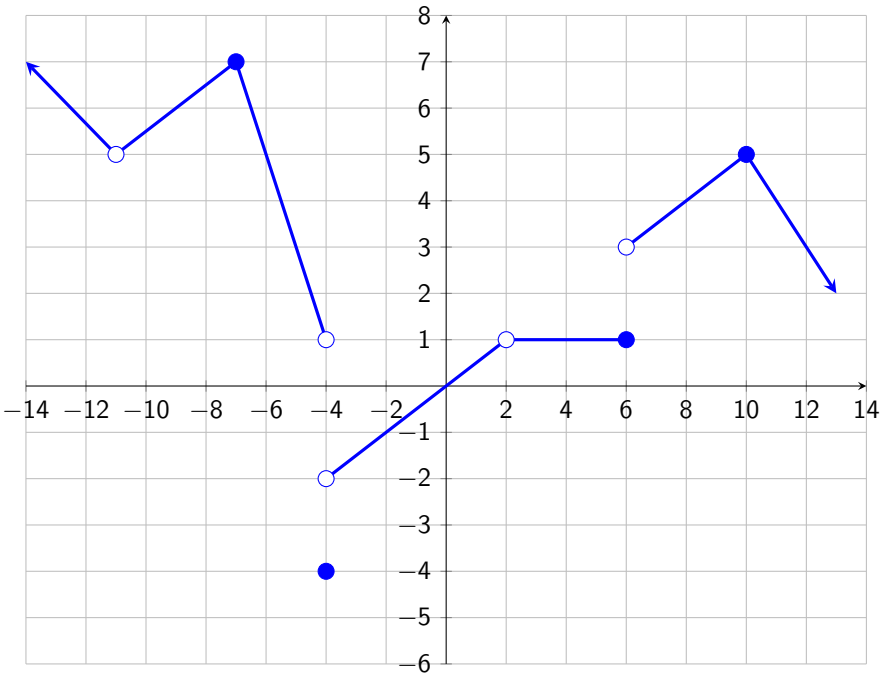
31.1 Answer Key

1. $-\frac{1}{2}$
2. 4
3. $-\frac{1}{2}$
4. -6
5. -3
6. -1
7. 2
8. 5

Chapter 32

Continuity

For each of the following, determine whether the function graphed below is continuous at that value. If not, explain why.



1. $x = -11$
2. $x = -7$
3. $x = -4$
4. $x = 2$
5. $x = 6$
6. $x = 10$

Identify all discontinuities for each of the following.

7. $f(x) = \dfrac{x^2 - 6x}{x^2 + 6x}$

8. $f(x) = \dfrac{x+3}{x-3}$

9. $f(x) = \dfrac{x+4}{3\ln(x)}$

10. $f(x) = \dfrac{2x+5}{x^2-9}$

11. $f(x) = \begin{cases} 2\sin(x), & x < 0 \\ 0, & x = 0 \\ 3x - 2, & x > 0 \end{cases}$

12. $f(x) = \begin{cases} e^x - 1, & x \leq 0 \\ x^2, & x > 0 \end{cases}$

13. $f(x) = \begin{cases} \dfrac{x^2-1}{x+1}, & x < -1 \\ 2x, & x > -1 \end{cases}$

14. $f(x) = \begin{cases} \dfrac{x^2-1}{x+1}, & x < -1 \\ 2x, & x \geq -1 \end{cases}$

32.1 Answer Key

1. Discontinuous; Not defined at $x = -11$
2. Continuous
3. Discontinuous; Left- and right-hand limits are not equal, nor do they equal the function value at $x = -4$
4. Discontinuous; Not defined at $x = 2$
5. Discontinuous; Left- and right-hand limits are not equal
6. Continuous
7. Discontinuous at $x = 0, -6$
8. Discontinuous at $x = 3$
9. Discontinuous at $x = 1$
10. Discontinuous at $x = \pm 3$
11. Discontinuous at $x = 0$
12. Continuous for all values of x
13. Discontinuous at $x = -1$
14. Continuous for all values of x

Chapter 33

Derivatives

Use the definition of the derivative to find the derivative of each function with respect to x.

1. $f(x) = x^2 + 2x + 4$
2. $f(x) = -5x + 5$
3. $f(x) = 2x^2 - 5x - 2$
4. $f(x) = 5x + 2$
5. $f(x) = x^3 - x^2$
6. $f(x) = 5x^2 + 5$
7. $f(x) = 2x + 3$
8. $f(x) = x^2 - 2$
9. $f(x) = -5x^3 + 4$
10. $f(x) = -4x^2 + x - 5$
11. $f(x) = 2x^2 - 3x + 5$

33.1 Answer Key

1. $2x + 2$
2. -5
3. $4x - 5$
4. 5
5. $3x^2 - 2x$
6. $10x$
7. 2
8. $2x$
9. $-15x^2$
10. $-8x + 1$
11. $4x - 3$

Appendix A

Factoring

Factor each of the following completely.

1. $x^2 + 2x - 15$
2. $x^2 - 8x + 12$
3. $x^2 + 15x + 56$
4. $5x^2 + 19x - 4$
5. $4x^2 - 5x - 6$
6. $9x^2 - 400$
7. $5x^2 - 7x - 6$
8. $9x^2 - 54x + 45$
9. $3x^3 + 12x^2 + 9x$
10. $9y^2 - 16$
11. $4x^2 - 28x + 49$
12. $14x^2 + 11xy - 15y^2$
13. $6x^2 - 48x - 120$
14. $9x^4 - 54x^3 + 45x^2$
15. $16y^2 - 40y + 25$
16. $30x^2 + xy - y^2$
17. $8w^2 + 33w + 4$
18. $3p^2 + 22p - 16$
19. $18x^2 - 27x + 4$
20. $14a^2 + 15a - 9$
21. $4x^2 - 4x - 24$
22. $18t^2 - 9t - 5$
23. $6a^2 + 23a + 21$
24. $25x^2 - 1$

A.1 Answer Key

1. $(x+5)(x-3)$
2. $(x-6)(x-2)$
3. $(x+7)(x+8)$
4. $(5x-1)(x+4)$
5. $(4x+3)(x-2)$
6. $(3x+20)(3x-20)$
7. $(5x+3)(x-2)$
8. $9(x-5)(x-1)$
9. $3x(x+3)(x+1)$
10. $(3y+4)(3y-4)$
11. $(2x-7)^2$
12. $(7x-5y)(2x+3y)$
13. $6(x-10)(x+2)$
14. $9x^2(x-1)(x-5)$
15. $(4y-5)^2$
16. $(6x-y)(5x+y)$
17. $(8w+1)(w+4)$
18. $(3p-2)(p+8)$
19. $(6x-1)(3x-4)$
20. $(7a-3)(2a+3)$
21. $4(x-3)(x+2)$
22. $(6t-5)(3t+1)$
23. $(2a+3)(3a+7)$
24. $(5x+1)(5x-1)$

Appendix B

Complex Fractions

Simplify each as much as possible.

1. $\dfrac{5+\frac{3}{x}}{x-\frac{1}{2}}$
2. $\dfrac{\frac{1}{x}+\frac{2}{x^2}}{x+\frac{8}{x^2}}$
3. $\dfrac{3}{2-\frac{x}{x-1}}$
4. $\dfrac{1+\frac{3}{x}}{\frac{2}{x}+7}$
5. $\dfrac{\frac{4}{x}-\frac{x}{x-2}}{\frac{1}{x}+\frac{3}{x-2}}$
6. $\dfrac{\frac{3}{x+1}-4}{\frac{2}{x+1}}$
7. $\dfrac{\frac{5}{x}+\frac{3}{x-2}}{\frac{7}{x^2-2x}}$
8. $\dfrac{\frac{1}{x}-\frac{1}{7}}{x-7}$
9. $\dfrac{\frac{1}{x}+\frac{1}{x+1}}{5}$
10. $\dfrac{\frac{5}{x}-5x}{x-1}$
11. $\dfrac{\frac{1}{2+x}-\frac{1}{2}}{x}$
12. $\dfrac{\frac{3}{x-4}+\frac{2x}{x+1}}{4x}$
13. $\dfrac{\frac{1}{x-a}+\frac{1}{a}}{x}$
14. $\dfrac{\frac{1}{x-1}-\frac{1}{x-3}}{\frac{2}{x-1}+\frac{3}{x+1}}$
15. $\dfrac{\frac{2}{x^2-4}+\frac{1}{x-2}}{\frac{4}{x+2}}$

B.1 Answer Key

1. $\frac{2(5x+3)}{x(2x-1)}$
2. $\frac{1}{x^2-2x+4}$
3. $\frac{3(x-1)}{x-2}$
4. $\frac{x+3}{2+7x}$
5. $\frac{-1(x^2-4x+8)}{2(2x-1)}$
6. $\frac{-4x-1}{2}$
7. $\frac{8x-10}{7}$
8. $-\frac{1}{7x}$
9. $\frac{2x+1}{5x(x+1)}$
10. $\frac{-5x-5}{x}$
11. $\frac{-1}{2x+4}$
12. $\frac{(x-1)(2x-3)}{4x(x-4)(x+1)}$
13. $\frac{1}{a(x-a)}$
14. $\frac{-2x-2}{5x^2-16x+3}$
15. $\frac{x+4}{4x-8}$