Discrete Probability Distributions

Objectives

Create a probability distribution

Determine the expected value of a probability distribution

Oetermine the variance and standard deviation of a probability distribution

Probability Distribution

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- The sum of all probabilities in a distribution equals 1

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Familiar Characteristics:

- ullet 0 \leq each probability ≤ 1
- The sum of all probabilities in a distribution equals 1
- P(A or B) = P(A) + P(B)

	1	2	3	4	5	6
1	2	3	4	5	6	7
2	3	4	5	6	7	8
3	4	5	6	7	8	9
4	5	6	7	8	9	10
5	6	7	8	9	10	11
6	7	8	9	5 6 7 8 9 10	11	12

We can create a probability distribution of the sums of rolling two dice.

	1	2	3	4	5	6
1	2	3	4	5	6	7
2	3	4	5	6	7	8
3	4	5	6	7	8	9
4	5	6	7	8	9	10
5	6	7	8	9	10	11
6	7	8	9	5 6 7 8 9	11	12

We can create a probability distribution of the sums of rolling two dice.

We use the notation P(X = x) where X is our random variable and x represents the outcomes, such as 2, 3, 4, ..., 12.

X	P(X=x)
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	

X	P(X=x)
2	1/36
3 4	
4	
5	
6	
7	
8	
9	
10	
11	
12	

X	P(X=x)
2	1/36
3	1/18
4	
5	
6	
7	
8	
9	
10	
11	
12	

X	P(X=x)
2	1/36
3	1/18
4	1/12
5	
6	
7	
8	
9	
10	
11	
12	

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12	

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11	
12	

X	P(X=x)
2	1/36
3	1/18
4	1/12
5	1/9
6	5/36
7	1/6
8	5/36
9	
10	
11	
12	

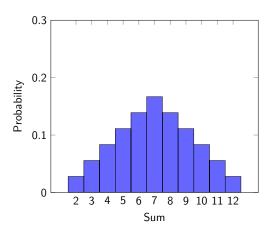
X	P(X=x)
2	1/36
3	1/18
4	1/12
5	1/9
6	5/36
7	1/6
8	5/36
9	1/9
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7	1/6
8	5/36
9	1/9
10	1/12
11	1/18
12	1/36

Probability Histogram of Rolling 2 Dice



(a) Create a probability distribution for flipping a coin three times, where X represents the number of times heads is flipped.

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x	P(X=x)
0	
1	
2	
3	

(a) Create a probability distribution for flipping a coin three times, where X represents the number of times heads is flipped.

x	P(X=x)
0	1/8
1	
2	
3	

(a) Create a probability distribution for flipping a coin three times, where X represents the number of times heads is flipped.

x	P(X=x)
0	1/8
1	1/4
2	
3	

(a) Create a probability distribution for flipping a coin three times, where X represents the number of times heads is flipped.

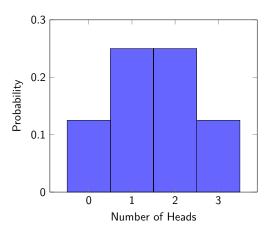
x	P(X=x)
0	1/8
1	1/4
2	1/4
3	

(a) Create a probability distribution for flipping a coin three times, where X represents the number of times heads is flipped.

x	P(X=x)
0	1/8
1	1/4
2	1/4
3	1/8

(b) Create a probability distribution histogram for the number of times heads appears when flipping a coin 3 times.

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The distribution below represents the percentage of households that have x dogs according to a recent study.

x	P(X=x)
0	44%
1	27%
2	18%
3 or more	11%

How many households have at least 1 dog?

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x	P(X=x)
0	44%
1	27%
2	18%
3 or more	11%

How many households have at least 1 dog?

Using the Complement Rule: 100% - 44% = 56%

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The **expected value** of a probability distribution is the outcome we would expect to happen if the experiment was performed a very large number of times.

In other words, it is a **weighted mean** of the distribution of outcomes.

Determine the expected value of rolling two dice.

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Calculating the weighted mean of our distribution, the expected value is 7.

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