Measures of Center

Objectives

1 Calculate the mean, median, and mode of a dataset

2 Calculate the weighted mean of a dataset

3 Approximate the mean for a grouped dataset

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In some instances, this can give us a good value to expect from that dataset.

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When most people use the term *average*, they are referring to the mean.

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- The mean of a data set uses every value, unless the mean is a *trimmed mean*.
- One extreme value (called an outlier) can change the value of the mean drastically.

Mean Formula

Sample mean: $\overline{\mathbf{x}}$ Population mean: μ

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$$\bar{\mathbf{x}}$$
, or μ , $=\frac{\sum x_i}{n} = \frac{1}{n} \sum x_i$

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The median is denoted by \tilde{x} , however, some technologies uses Med to denote it.

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The mode is the only measure of center that is applicable to qualitative data.

The dataset below represents the number of complaints I receive each week about my teaching.

Calculate the mean, median, and mode of the number of complaints.

The total number of complaints is 50. There are 10 complaints listed.

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Median number of complaints per week is 4.5

Mode number of complaints per week are 4 and 7.

The next week, I received 400 complaints. Re-calculate the mean, median, and mode now.

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Mode: 4 and 7 complaints per week.

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California has a mean class size of 20.9 students per teacher and Alaska has a mean of 16.8 students per teacher.

If we combine the two states, we might find the mean number of students per teacher to be 18.85 (0.5 * (20.9 \pm 16.8)) but is this result correct? Why or why not?

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It is not correct because California has a much higher population that Alaska. We would have to find what is known as the **weighted mean**.

Weighted Mean

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- Add those results.
- **1** Then divide that by the total of the weights.

You've recently completed a semester. Determine the semester's GPA (A = 4pts, B = 3pts, etc).

Course	Grade	Credit Hours
Statistics	А	4
Advanced Chris Farley	Α	3
Airplane! Quotes	В	5
Obnoxious Examples	С	3

Grade	Credit Hours	TOTALS
4	4	16
4	3	12
3	5	15
2	3	6
	15	49

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Weighted Mean: 49/15 = 3.267

In a statistics course, tests count for 60% of the final grade, homework for 20% and midterm and final exams are 10% each. Suppose you've earned an 87% average on tests, 94% average on homeworks and a 77% average on the exams.

What is your overall percentage?

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What is your overall percentage?

Assessment	Your Scores	Grade Weights	TOTALS
Tests	0.87	0.60	0.522
Homework	0.94	0.20	0.188
Exams	0.77	0.20	0.154

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Grade: 0.864/1 = 86.4%

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We will use similar techniques like we did in finding the weighted mean, however we will have to use the class midpoints as our observed values.