Confidence Intervals

Objectives

1 Determine confidence intervals for population mean

2 Determine confidence intervals for population proportion

Oetermine the necessary sample size

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So, for our samples, how confident are we that they contain the population mean?

That is where confidence intervals come into play.

How Confident Are We?

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Typical confidence levels are 90%, 95%, 98%, and 99%.

Confidence Interval Setup

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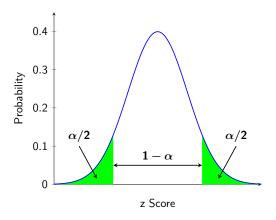
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The margin of error is in the form

critical value × standard error

Critical Values

Critical values are typically in the form $z_{\alpha/2}$ where



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Note: If σ is unknown, you can use the sample standard deviation, s, when the sample size is large enough $(n \ge 30)$.

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The waiting time of a sample of 100 patients at a hospital is 3.5 minutes. Construct a 95% confidence interval for the mean waiting time of all patients at the hospital. Assume $\sigma=0.75$ minutes.

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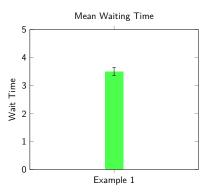
A 95% confidence interval for the population mean waiting time is 3.353 to 3.647 minutes.

Error Bars

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However, be advised that some graphs use standard deviation for their error bars.

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- We are ____ % confident that the population mean is in this interval.
- There is a ____ % chance that the population mean is (whatever the sample mean is).

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