

bruhdge

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```
# Import necessary library  
library(dplyr)
```

```
##  
## Attaching package: 'dplyr'  
  
## The following objects are masked from 'package:stats':  
##  
##   filter, lag  
  
## The following objects are masked from 'package:base':  
##  
##   intersect, setdiff, setequal, union
```

```
library(knitr)  
library(car)
```

```
## Loading required package: carData  
  
##  
## Attaching package: 'car'  
  
## The following object is masked from 'package:dplyr':  
##  
##   recode
```

```
#library(kableExtra)  
  
# Read the final dataset  
data <- read.csv("df_2024_model.csv")  
  
# Rename the columns to be more readable for the regression analysis  
names(data) <- c("State", "Demographics", "Tot_citizen", "Tot_reg", "Prop_reg",  
                 "Tot_voted", "Prop_voted", "Voter_part_rate")  
  
# Establish the age levels as detailed by the census  
age_patterns <- c(  
  "18 to 24 years", "25 to 34 years", "35 to 44 years",  
  "45 to 64 years", "65 years and over"
```

```

)

# Establish the gender levels as detailed by the census
gender_patterns <- c("Male", "Female")

# Establish the region levels as detailed by the census (See Note)
## Note: The region separations are defined here:
### https://www2.census.gov/geo/pdfs/maps-data/maps/reference/us\_regdiv.pdf
west <- c("WASHINGTON", "OREGON", "MONTANA", "IDAHO", "WYOMING", "COLORADO", "NEW MEXICO",
          "ARIZONA", "UTAH", "NEVADA", "CALIFORNIA", "HAWAII", "ALASKA")

midwest <- c("NORTH DAKOTA", "SOUTH DAKOTA", "NEBRASKA", "KANSAS", "MINNESOTA", "IOWA", "MISSOURI",
             "WISCONSIN", "ILLINOIS", "MICHIGAN", "INDIANA", "OHIO")

northeast <- c("CONNECTICUT", "MAINE", "MASSACHUSETTS", "NEW HAMPSHIRE", "RHODE ISLAND", "VERMONT", "NEW
              "NEW YORK", "PENNSYLVANIA")

# Separate demographic and region factors of interest into separate columns for easier analysis
data_24 <- data %>% filter(Demographics != "Total", State != "UNITED STATES")
data_24["Age"] <- ifelse(data_24[["Demographics"]] %in% age_patterns, data_24[["Demographics"]], NA)
data_24["Gender"] <- ifelse(data_24[["Demographics"]] %in% gender_patterns, data_24[["Demographics"]], NA)
data_24["Race"] <- ifelse(!(data_24[["Demographics"]] %in% age_patterns) & !(data_24[["Demographics"]]
                                data_24[["Demographics"]], NA)

data_24["Region"] <- "South"
data_24["Region"] <- ifelse(data_24[["State"]] %in% west, "West", data_24[["Region"]])
data_24["Region"] <- ifelse(data_24[["State"]] %in% midwest, "Midwest", data_24[["Region"]])
data_24["Region"] <- ifelse(data_24[["State"]] %in% northeast, "Northeast", data_24[["Region"]])

head(data_24)

```

```

##      State      Demographics Tot_citizen Tot_reg Prop_reg Tot_voted Prop_voted
## 1 ALABAMA 18 to 24 years      400      212    53.0      167      41.6
## 2 ALABAMA 25 to 34 years      681      409    60.0      318      46.7
## 3 ALABAMA 35 to 44 years      555      370    66.7      304      54.8
## 4 ALABAMA 45 to 64 years     1228      904    73.6      793      64.6
## 5 ALABAMA 65 years and over    915      709    77.5      637      69.7
## 6 ALABAMA Asian alone        45       30    65.9       30      65.9
## Voter_part_rate      Age Gender      Race Region
## 1 0.7877358 18 to 24 years <NA>      <NA> South
## 2 0.7775061 25 to 34 years <NA>      <NA> South
## 3 0.8216216 35 to 44 years <NA>      <NA> South
## 4 0.8772124 45 to 64 years <NA>      <NA> South
## 5 0.8984485 65 years and over <NA>      <NA> South
## 6 1.0000000 <NA> <NA> Asian alone South

```

Contingency Tables

Region

Table 1: Contingency Table: Count by Region

Region	Count
Midwest	180
Northeast	135
South	255
West	195
Total	765

```
contingency_region <- data_24 %>%
  group_by(Region) %>%
  summarise(Count=n())

grand_total <- data_24 %>%
  summarise(
    Region = "Total", # Set a label for the total row
    Count = n()      # Sum the 'count' column from the group summary
  )

contingency_region <- bind_rows(contingency_region, grand_total)
contingency_region
```

```
## # A tibble: 5 x 2
##   Region    Count
##   <chr>    <int>
## 1 Midwest    180
## 2 Northeast  135
## 3 South     255
## 4 West     195
## 5 Total     765
```

```
(kable(contingency_region, format = "latex", caption = "Contingency Table: Count by Region"))
```

Race

```
contingency_race <- data_24 %>%
  filter(!is.na(Race)) %>%
  group_by(Race) %>%
  summarise(Count=n())

grand_total <- data_24 %>%
  filter(!is.na(Race)) %>%
  summarise(
    Race = "Total", # Set a label for the total row
    Count = n()      # Sum the 'count' column from the group summary
  )

contingency_race <- bind_rows(contingency_race, grand_total)
contingency_race
```

```
## # A tibble: 9 x 2
```

Table 2: Contingency Table: Count by Race

Region	Count
Midwest	180
Northeast	135
South	255
West	195
Total	765

```
## Race Count
## <chr> <int>
## 1 Asian alone 51
## 2 Asian alone or in combination 51
## 3 Black alone 51
## 4 Black alone or in combination 51
## 5 Hispanic (any race) 51
## 6 White alone 51
## 7 White alone or in combination 51
## 8 White non-Hispanic alone 51
## 9 Total 408
```

```
(kable(contingency_region, format = "latex", caption = "Contingency Table: Count by Race"))
```

Gender

```
contingency_gender <- data_24 %>%
  filter(!is.na(Gender)) %>%
  group_by(Gender) %>%
  summarise(Count=n())

grand_total_gender <- data_24 %>%
  filter(!is.na(Gender)) %>%
  summarise(
    Gender = "Total",
    Count = n()
  )

contingency_gender <- bind_rows(contingency_gender, grand_total_gender)
contingency_gender
```

```
## # A tibble: 3 x 2
## Gender Count
## <chr> <int>
## 1 Female 51
## 2 Male 51
## 3 Total 102
```

```
(kable(contingency_gender, format = "latex", caption = "Contingency Table: Count by Gender"))
```

Age

Table 3: Contingency Table: Count by Gender

Gender	Count
Female	51
Male	51
Total	102

Table 4: Contingency Table: Count by Age

Gender	Count
Female	51
Male	51
Total	102

```
contingency_age <- data_24 %>%
  filter(!is.na(Age)) %>%
  group_by(Age) %>%
  summarise(Count=n())

grand_total_age <- data_24 %>%
  filter(!is.na(Age)) %>%
  summarise(
    Age = "Total",
    Count = n()
  )

contingency_age <- bind_rows(contingency_age, grand_total_age)
contingency_age
```

```
## # A tibble: 6 x 2
##   Age          Count
##   <chr>        <int>
## 1 18 to 24 years     51
## 2 25 to 34 years     51
## 3 35 to 44 years     51
## 4 45 to 64 years     51
## 5 65 years and over  51
## 6 Total           255
```

```
(kable(contingency_gender, format = "latex", caption = "Contingency Table: Count by Age"))
```

VIF

Race + Region

```
# --- Model A: Race + Region ---
# Filter for non-NA values in Region and Race
data_region_race <- data_24 %>%
  filter(!is.na(Region), !is.na(Race))

# Linear Model
```

Table 5: VIF Results: Region and Race

	GVIF	Df	$GVIF^{1/(2*Df)}$
Region	1	3	1
Race	1	7	1

```
model_region_race <- lm(Voter_part_rate ~ Region + Race, data = data_region_race)

# Calculate VIF
vif_region_race <- vif(model_region_race)

print("--- VIF: Region + Race (LaTeX) ---")

## [1] "--- VIF: Region + Race (LaTeX) ---"

print(vif_region_race)

##          GVIF Df GVIF^(1/(2*Df))
## Region      1  3              1
## Race        1  7              1

kable(as.data.frame(vif_region_race), format = "latex", caption = "VIF Results: Region and Race")
```

Region + Age

```
# Filter for non-NA values in Region and Age
data_region_age <- data_24 %>%
  filter(!is.na(Region), !is.na(Age))

# Linear Model
model_region_age <- lm(Voter_part_rate ~ Region + Age, data = data_region_age)

# Calculate VIF
vif_region_age <- vif(model_region_age)

print("--- VIF: Region + Age (LaTeX) ---")

## [1] "--- VIF: Region + Age (LaTeX) ---"

print(vif_region_age)

##          GVIF Df GVIF^(1/(2*Df))
## Region      1  3              1
## Age         1  4              1

kable(as.data.frame(vif_region_age), format = "latex", caption = "VIF Results: Region and Age")
```

Region + Gender

Table 6: VIF Results: Region and Age

	GVIF	Df	$\text{GVIF}^{1/(2 \cdot \text{Df})}$
Region	1	3	1
Age	1	4	1

Table 7: VIF Results: Region and Gender

	GVIF	Df	$\text{GVIF}^{1/(2 \cdot \text{Df})}$
Region	1	3	1
Gender	1	1	1

```
# Filter for non-NA values in Region and Gender
data_region_gender <- data_24 %>%
  filter(!is.na(Region), !is.na(Gender))

# Linear Model
model_region_gender <- lm(Voter_part_rate ~ Region + Gender, data = data_region_gender)

# Calculate VIF
vif_region_gender <- vif(model_region_gender)

print("--- VIF: Region + Gender (LaTeX) ---")

## [1] "--- VIF: Region + Gender (LaTeX) ---"

print(vif_region_gender)

##           GVIF Df GVIF^(1/(2*Df))
## Region      1  3              1
## Gender      1  1              1

kable(as.data.frame(vif_region_gender), format = "latex", caption = "VIF Results: Region and Gender")
```

VIF Debugging

```
# # 1. Create a dataset where one variable is a perfect copy of another
# data_vif_debug <- data_24 %>%
#   filter(!is.na(Region), !is.na(Gender)) %>%
#   mutate(
#     Region = Region,
#     Region_Copy = Region # Perfect correlation
#   )
#
# # 2. Linear Model with two identical predictors
# # Note: lm() will often drop one of the perfectly correlated predictors automatically,
# # but VIF analysis should still flag the issue or throw an error/warning.
# model_vif_debug <- lm(Voter_part_rate ~ Region + Region_Copy, data = data_vif_debug)
#
# # 3. Calculate VIF
```

```

# # This is expected to produce a high number (or an error/warning)
# vif_vif_debug <- vif(model_vif_debug)
#
# print("--- VIF: Debug Test (Region + Region_Copy) (LaTeX) ---")
# # Only kable the result if the VIF calculation was successful
# if (is.numeric(vif_vif_debug)) {
#   kable(as.data.frame(vif_vif_debug), format = "latex", caption = "VIF Debug Results: Region and Region_Copy")
# } else {
#   print("VIF calculation failed or returned non-numeric result due to perfect collinearity. Check model specification.")
# }
#
# summary(model_vif_debug)

```