

bruhdge

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```
# Import necessary library
library(dplyr)

##
## Attaching package: 'dplyr'

## The following objects are masked from 'package:stats':
##     filter, lag

## The following objects are masked from 'package:base':
##     intersect, setdiff, setequal, union

library(knitr)
library(car)

## Loading required package: carData

##
## Attaching package: 'car'

## The following object is masked from 'package:dplyr':
##     recode

#library(kableExtra)

# Read the final dataset
data <- read.csv("df_2024_model.csv")

# Rename the columns to be more readable for the regression analysis
names(data) <- c("State", "Demographics", "Tot_citizen", "Tot_reg", "Prop_reg",
                 "Tot_voted", "Prop_voted", "Voter_part_rate")

# Establish the age levels as detailed by the census
age_patterns <- c(
  "18 to 24 years", "25 to 34 years", "35 to 44 years",
  "45 to 64 years", "65 years and over")
```

```

)

# Establish the gender levels as detailed by the census
gender_patterns <- c("Male", "Female")

# Establish the region levels as detailed by the census (See Note)
## Note: The region separations are defined here:
### https://www2.census.gov/geo/pdfs/maps-data/maps/reference/us_regdiv.pdf
west <- c("WASHINGTON", "OREGON", "MONTANA", "IDAHO", "WYOMING", "COLORADO", "NEW MEXICO",
         "ARIZONA", "UTAH", "NEVADA", "CALIFORNIA", "HAWAII", "ALASKA")

midwest <- c("NORTH DAKOTA", "SOUTH DAKOTA", "NEBRASKA", "KANSAS", "MINNESOTA", "IOWA", "MISSOURI",
            "WISCONSIN", "ILLINOIS", "MICHIGAN", "INDIANA", "OHIO")

northeast <- c("CONNECTICUT", "MAINE", "MASSACHUSETTS", "NEW HAMPSHIRE", "RHODE ISLAND", "VERMONT", "NEW YORK",
               "PENNSYLVANIA")

# Separate demographic and region factors of interest into separate columns for easier analysis
data_24 <- data %>% filter(Demographics != "Total", State != "UNITED STATES")
data_24["Age"] <- ifelse(data_24[["Demographics"]] %in% age_patterns, data_24[["Demographics"]], NA)
data_24["Gender"] <- ifelse(data_24[["Demographics"]] %in% gender_patterns, data_24[["Demographics"]], NA)
data_24["Race"] <- ifelse((!(data_24[["Demographics"]] %in% age_patterns) & !(data_24[["Demographics"]] %in% gender_patterns)), data_24[["Demographics"]], NA)

data_24["Region"] <- "South"
data_24["Region"] <- ifelse(data_24[["State"]] %in% west, "West", data_24[["Region"]])
data_24["Region"] <- ifelse(data_24[["State"]] %in% midwest, "Midwest", data_24[["Region"]])
data_24["Region"] <- ifelse(data_24[["State"]] %in% northeast, "Northeast", data_24[["Region"]])

head(data_24)

##      State    Demographics Tot_citizen Tot_reg Prop_reg Tot_voted Prop_voted
## 1 ALABAMA 18 to 24 years        400     212    53.0      167     41.6
## 2 ALABAMA 25 to 34 years        681     409    60.0      318     46.7
## 3 ALABAMA 35 to 44 years        555     370    66.7      304     54.8
## 4 ALABAMA 45 to 64 years       1228     904    73.6      793     64.6
## 5 ALABAMA 65 years and over      915     709    77.5      637     69.7
## 6 ALABAMA Asian alone           45      30    65.9      30     65.9
##   Voter_part_rate          Age Gender      Race Region
## 1 0.7877358 18 to 24 years <NA> <NA> South
## 2 0.7775061 25 to 34 years <NA> <NA> South
## 3 0.8216216 35 to 44 years <NA> <NA> South
## 4 0.8772124 45 to 64 years <NA> <NA> South
## 5 0.8984485 65 years and over <NA> <NA> South
## 6 1.0000000                  <NA> <NA> Asian alone South

```

Contingency Tables

Region

Table 1: Contingency Table: Count by Region

Region	Count
Midwest	180
Northeast	135
South	255
West	195
Total	765

```

contingency_region <- data_24 %>%
  group_by(Region) %>%
  summarise(Count=n())

grand_total <- data_24 %>%
  summarise(
    Region = "Total", # Set a label for the total row
    Count = n()      # Sum the 'count' column from the group summary
  )

contingency_region <- bind_rows(contingency_region, grand_total)
contingency_region

```

```

## # A tibble: 5 x 2
##   Region     Count
##   <chr>     <int>
## 1 Midwest     180
## 2 Northeast   135
## 3 South       255
## 4 West        195
## 5 Total       765

```

```
(kable(contingency_region, format = "latex", caption = "Contingency Table: Count by Region"))
```

Race

```

contingency_race <- data_24 %>%
  filter(!is.na(Race)) %>%
  group_by(Race) %>%
  summarise(Count=n())

grand_total <- data_24 %>%
  filter(!is.na(Race)) %>%
  summarise(
    Race = "Total", # Set a label for the total row
    Count = n()      # Sum the 'count' column from the group summary
  )

contingency_race <- bind_rows(contingency_race, grand_total)
contingency_race

```

```
## # A tibble: 9 x 2
```

Table 2: Contingency Table: Count by Race

Region	Count
Midwest	180
Northeast	135
South	255
West	195
Total	765

```
##   Race           Count
##   <chr>          <int>
## 1 Asian alone      51
## 2 Asian alone or in combination 51
## 3 Black alone      51
## 4 Black alone or in combination 51
## 5 Hispanic (any race) 51
## 6 White alone      51
## 7 White alone or in combination 51
## 8 White non-Hispanic alone    51
## 9 Total             408
```

```
(kable(contingency_region, format = "latex", caption = "Contingency Table: Count by Race"))
```

Gender

```
contingency_gender <- data_24 %>%
  filter(!is.na(Gender)) %>%
  group_by(Gender) %>%
  summarise(Count=n())

grand_total_gender <- data_24 %>%
  filter(!is.na(Gender)) %>%
  summarise(
    Gender = "Total",
    Count = n()
  )

contingency_gender <- bind_rows(contingency_gender, grand_total_gender)
contingency_gender
```

```
## # A tibble: 3 x 2
##   Gender Count
##   <chr>  <int>
## 1 Female   51
## 2 Male     51
## 3 Total   102
```

```
(kable(contingency_gender, format = "latex", caption = "Contingency Table: Count by Gender"))
```

Age

Table 3: Contingency Table: Count by Gender

Gender	Count
Female	51
Male	51
Total	102

Table 4: Contingency Table: Count by Age

Gender	Count
Female	51
Male	51
Total	102

```

contingency_age <- data_24 %>%
  filter(!is.na(Age)) %>%
  group_by(Age) %>%
  summarise(Count=n())

grand_total_age <- data_24 %>%
  filter(!is.na(Age)) %>%
  summarise(
    Age = "Total",
    Count = n()
  )

contingency_age <- bind_rows(contingency_age, grand_total_age)
contingency_age

```

```

## # A tibble: 6 x 2
##   Age           Count
##   <chr>        <int>
## 1 18 to 24 years     51
## 2 25 to 34 years     51
## 3 35 to 44 years     51
## 4 45 to 64 years     51
## 5 65 years and over   51
## 6 Total            255

```

```
(kable(contingency_gender, format = "latex", caption = "Contingency Table: Count by Age"))
```

VIF

Race + Region

```

# --- Model A: Race + Region ---
# Filter for non-NA values in Region and Race
data_region_race <- data_24 %>%
  filter(!is.na(Region), !is.na(Race))

# Linear Model

```

Table 5: VIF Results: Region and Race

	GVIF	Df	$GVIF^{(1/(2*Df))}$
Region	1	3	1
Race	1	7	1

```

model_region_race <- lm(Voter_part_rate ~ Region + Race, data = data_region_race)

# Calculate VIF
vif_region_race <- vif(model_region_race)

print("--- VIF: Region + Race (LaTeX) ---")

## [1] "--- VIF: Region + Race (LaTeX) ---"

print(vif_region_race)

##          GVIF Df GVIF^(1/(2*Df))
## Region      1  3                 1
## Race        1  7                 1

kable(as.data.frame(vif_region_race), format = "latex", caption = "VIF Results: Region and Race")

```

Region + Age

```

# Filter for non-NA values in Region and Age
data_region_age <- data_24 %>%
  filter(!is.na(Region), !is.na(Age))

# Linear Model
model_region_age <- lm(Voter_part_rate ~ Region + Age, data = data_region_age)

# Calculate VIF
vif_region_age <- vif(model_region_age)

print("--- VIF: Region + Age (LaTeX) ---")

## [1] "--- VIF: Region + Age (LaTeX) ---"

print(vif_region_age)

##          GVIF Df GVIF^(1/(2*Df))
## Region      1  3                 1
## Age         1  4                 1

kable(as.data.frame(vif_region_age), format = "latex", caption = "VIF Results: Region and Age")

```

Region + Gender

Table 6: VIF Results: Region and Age

	GVIF	Df	$GVIF^{(1/(2*Df))}$
Region	1	3	1
Age	1	4	1

Table 7: VIF Results: Region and Gender

	GVIF	Df	$GVIF^{(1/(2*Df))}$
Region	1	3	1
Gender	1	1	1

```
# Filter for non-NA values in Region and Gender
data_region_gender <- data_24 %>%
  filter(!is.na(Region), !is.na(Gender))

# Linear Model
model_region_gender <- lm(Voter_part_rate ~ Region + Gender, data = data_region_gender)

# Calculate VIF
vif_region_gender <- vif(model_region_gender)

print("--- VIF: Region + Gender (LaTeX) ---")

## [1] "--- VIF: Region + Gender (LaTeX) ---"

print(vif_region_gender)

##          GVIF Df GVIF^(1/(2*Df))
## Region     1   3             1
## Gender     1   1             1

kable(as.data.frame(vif_region_gender), format = "latex", caption = "VIF Results: Region and Gender")
```

VIF Debugging

```
# # 1. Create a dataset where one variable is a perfect copy of another
# data_vif_debug <- data_24 %>%
#   filter(!is.na(Region), !is.na(Gender)) %>%
#   mutate(
#     Region = Region,
#     Region_Copy = Region # Perfect correlation
#   )
#
# # 2. Linear Model with two identical predictors
# # Note: lm() will often drop one of the perfectly correlated predictors automatically,
# # but VIF analysis should still flag the issue or throw an error/warning.
# model_vif_debug <- lm(Voter_part_rate ~ Region + Region_Copy, data = data_vif_debug)
#
# # 3. Calculate VIF
```

```
# # This is expected to produce a high number (or an error/warning)
# vif_vif_debug <- vif(model_vif_debug)
#
# print(" --- VIF: Debug Test (Region + Region_Copy) (LaTeX) ---")
# # Only kable the result if the VIF calculation was successful
# if (is.numeric(vif_vif_debug)) {
#   kable(as.data.frame(vif_vif_debug), format = "latex", caption = "VIF Debug Results: Region and Regi
# } else {
#   print("VIF calculation failed or returned non-numeric result due to perfect collinearity. Check mod
# }
#
# summary(model_vif_debug)
```