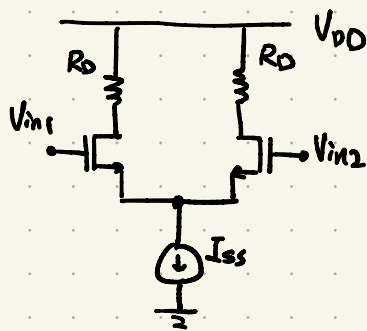


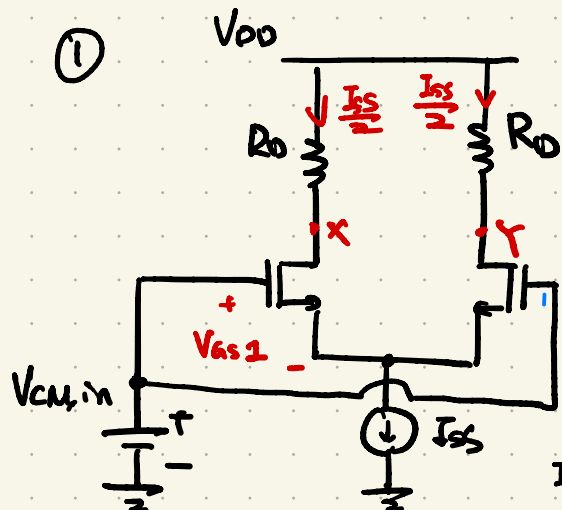
Lec 12

- MOS Differential Pair
- General Properties
- Large-Signal Behavior



General Properties

①



$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$$

(device on & sat.)

$$V_X = V_Y = V_{DD} - R_O \frac{I_{SS}}{2}$$

$$V_{GS} = \sqrt{\frac{I_{SS}}{\mu_n C_{ox} \frac{W}{L}}} + V_{TH}$$

If $V_{in1} = V_{in2}$, the diff pair is in "equilibrium"

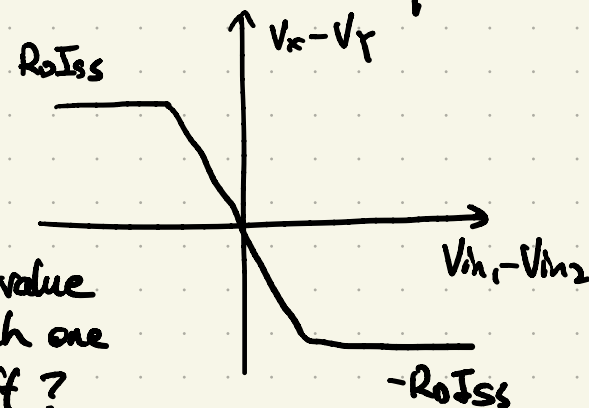
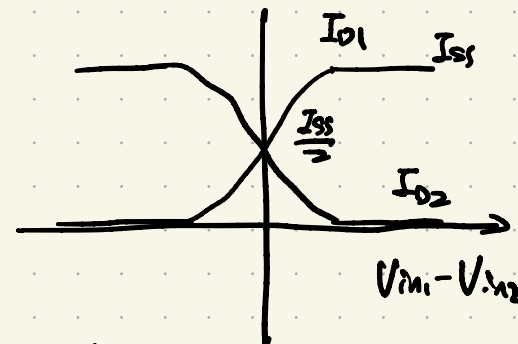
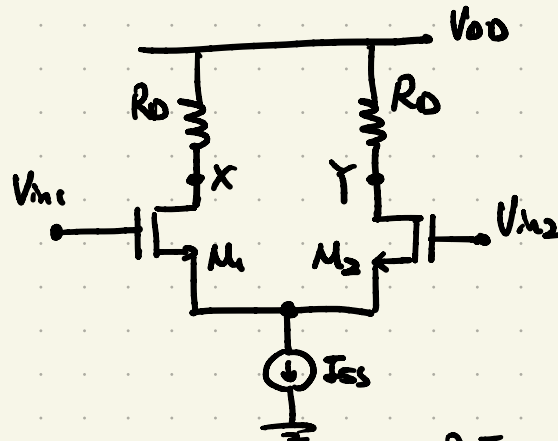
The equilibrium overdrive voltage:

$$V_{GS1} - V_{TH} = \sqrt{\frac{I_{SS}}{\mu_n C_{ox} \frac{W}{L}}}$$

- If $V_{cm,in}$ changes, what quantities in the circuit change?

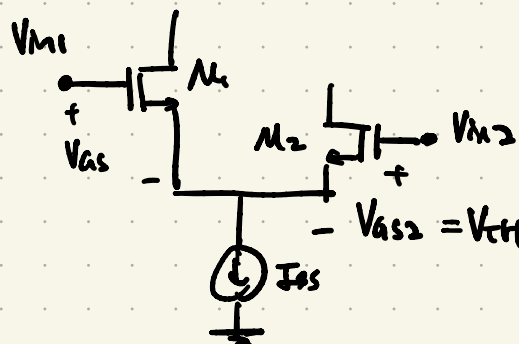
Nothing changes

② Differential behavior



Example

What is the minimum value of $V_{in1} - V_{in2}$ at which one transistor turns off?

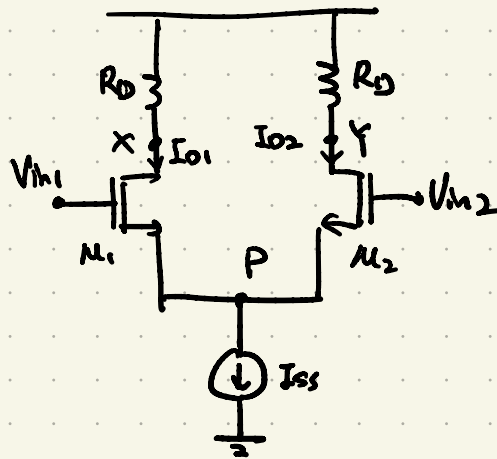


$$V_{GS1} = \sqrt{\frac{2I_{SS}}{\mu_n C_{ox} \frac{W}{L}}} + V_{TH}$$

$$V_{in1} - V_{in2} = V_{GS1} - V_{GS2}$$

$$= \sqrt{\frac{2I_{SS}}{\mu_n C_{ox} \frac{W}{L}}}$$

Large-Signal Analysis



$$V_{in1} - V_{in2} = V_{GS1} - V_{GS2}$$

$$V_{in1} - V_{in2} = \sqrt{\frac{2I_{01}}{\mu_n C_{ox} \frac{W}{L}}} + V_{TH}$$

$$- \left(\sqrt{\frac{2I_{02}}{\mu_n C_{ox} \frac{W}{L}}} + V_{TH} \right)$$

$$I_{01} + I_{02} = I_{SS}$$

$$V_X - V_Y = -R_D (I_{01} - I_{02})$$

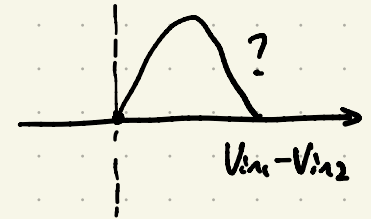
$$(V_{in1} - V_{in2})^2 = \frac{2I_{01}}{\mu_n C_{ox} \frac{W}{L}} + \frac{2I_{02}}{\mu_n C_{ox} \frac{W}{L}} - \frac{2\sqrt{4I_{01}I_{02}}}{\mu_n C_{ox} \frac{W}{L}}$$

$$(V_{in1} - V_{in2})^2 - \frac{2I_{SS}}{\mu_n C_{ox} \frac{W}{L}} = -4 \sqrt{\frac{I_{01}(I_{SS} - I_{01})}{\mu_n C_{ox} \frac{W}{L}}}$$

$$I_{01} - I_{02} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{in1} - V_{in2}) \sqrt{\frac{4I_{SS}}{\mu_n C_{ox} \frac{W}{L}} - (V_{in1} - V_{in2})^2}$$

Observations

① $I_{01} - I_{02} = 0$ if $V_{in1} = V_{in2}$



② Equation (A) is valid

only if M_1 and M_2 are on or at the edge of turning off; up to

$$|V_{in1} - V_{in2}| = \sqrt{\frac{2I_{SS}}{\mu_n C_{ox} \frac{W}{L}}}$$