

CS 383: Machine Learning

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Lecture 02

Outline

- Reading Quiz 1
- K-nearest neighbors
- Featurization (intro)
- Entropy & Decision Trees

Outline

- 1) *Generalization*: ability to answer new questions related to the topic studied
- 2) No! If we look at the test data (either the *features* or the *labels*), then any measurement of the performance of our algorithm becomes inaccurate
- 3) *Multiclass classification*
- 4) *Regression*

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Typical Supervised Learning setup

- X : Input matrix
 - n rows (examples/instances/individuals)
 - m columns (features/attributes)
- y : Label vector
- \hat{y} : Prediction vector

Simple Evaluation

How close is \hat{y} to y ?

Indicator
variable

Accuracy: $\frac{1}{n} \sum_i \mathbb{1}(\hat{y}_i, y_i)$

K-nearest neighbors

Problem: Given a collection of labeled examples, determine the class of a new unlabeled example

Solution: assign the same class as the ***most similar*** examples

Key idea: whats ***most similar***?

K-NN creates implicit decision boundaries

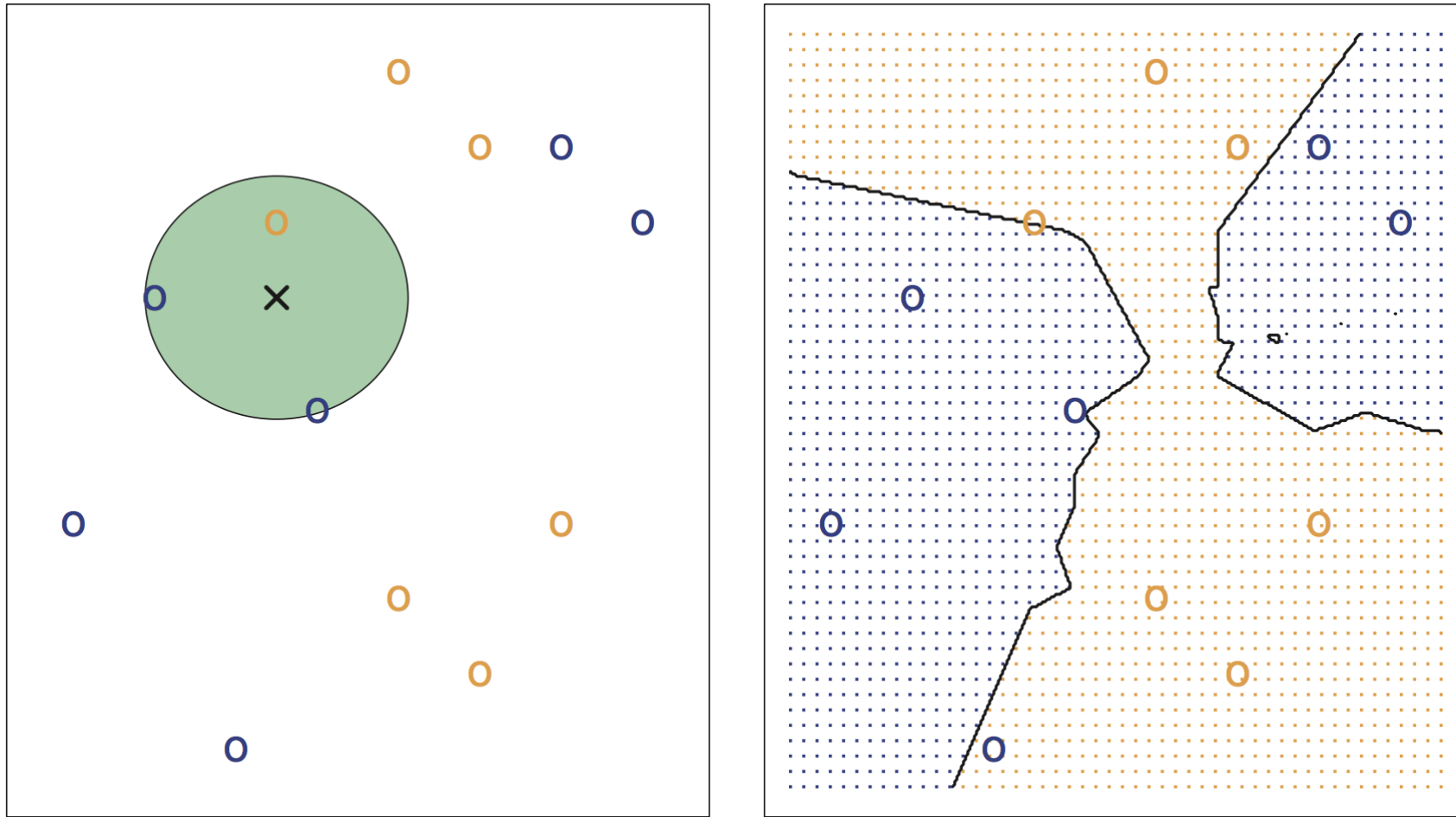


Figure 2.14 from ISL book, KNN with two classes ($C=2$), and $K=3$

HW01 – K-Nearest Neighbor

Implement KNN

Given:

- starter code, unit tests
- Train data with labels, dev data with labels, test data w/o labels

Deliverables:

- Implemented code
- Predictions on test data

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Terminology

Features: feature names

- e.g. shape

Feature values: what values are possible

- e.g. {circle, square, triangle}

Feature vector: values for a particular example

- e.g. $\mathbf{x} = [x_1, x_2, x_3, \dots, x_p]$

Terminology

Decision boundary:

separates regions of the feature space that would be classified as positive or negative (or multiclass)

Underfitting:

“had the opportunity to learn something but didn’t”
(Duame)

Overfitting:

memorized individual training examples (fit to noise) and can’t generalize

Handout 2

(find and work with a partner)

Comparing Decision Boundaries

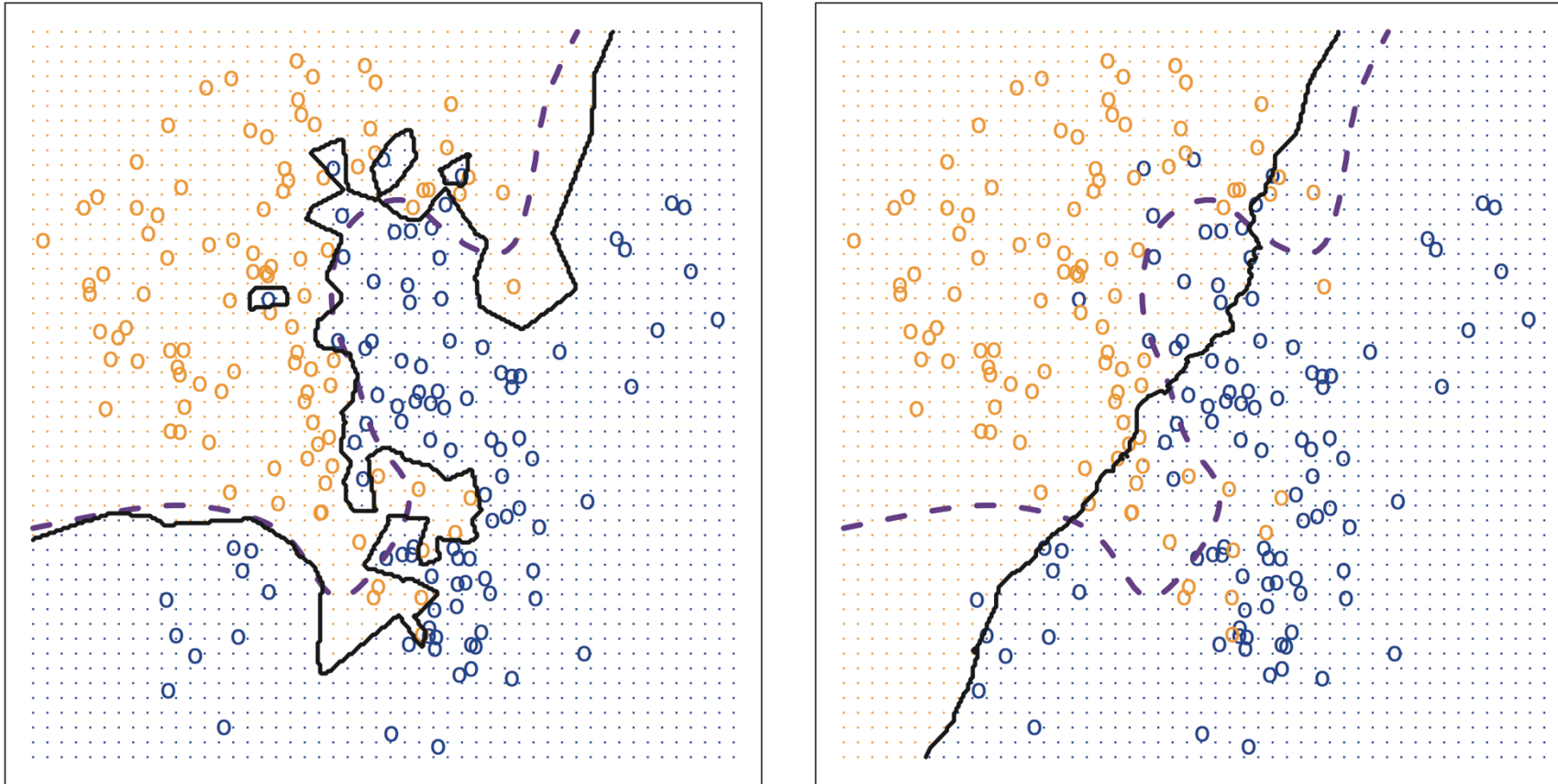
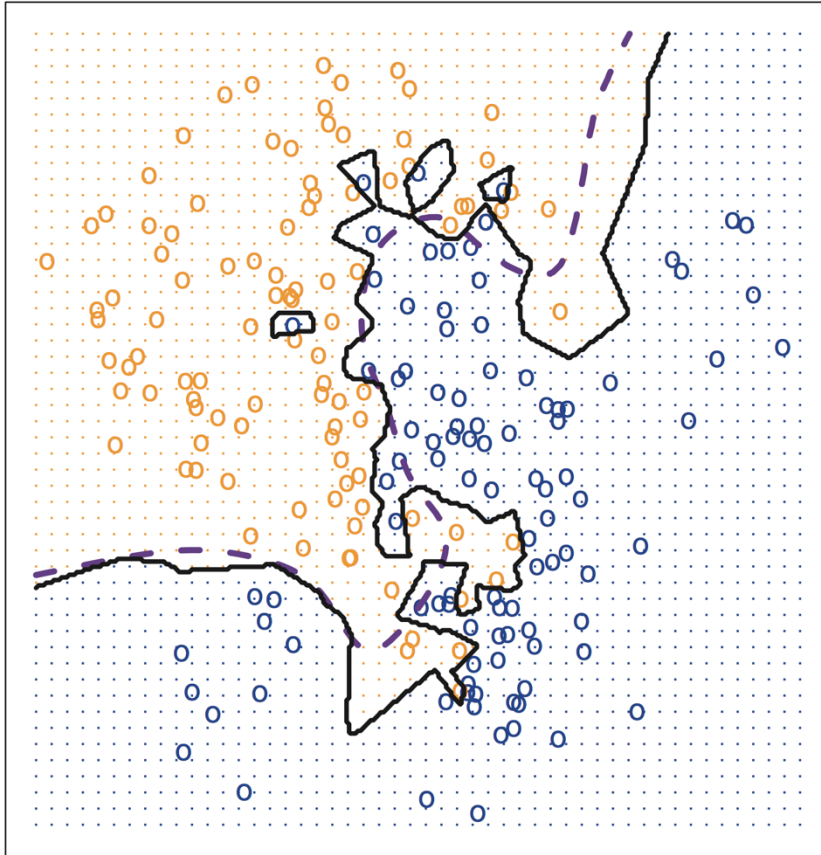


Figure 2.16 from ISL book (dashed line is “ideal” boundary)

Comparing Decision Boundaries

KNN: $K=1$



KNN: $K=100$

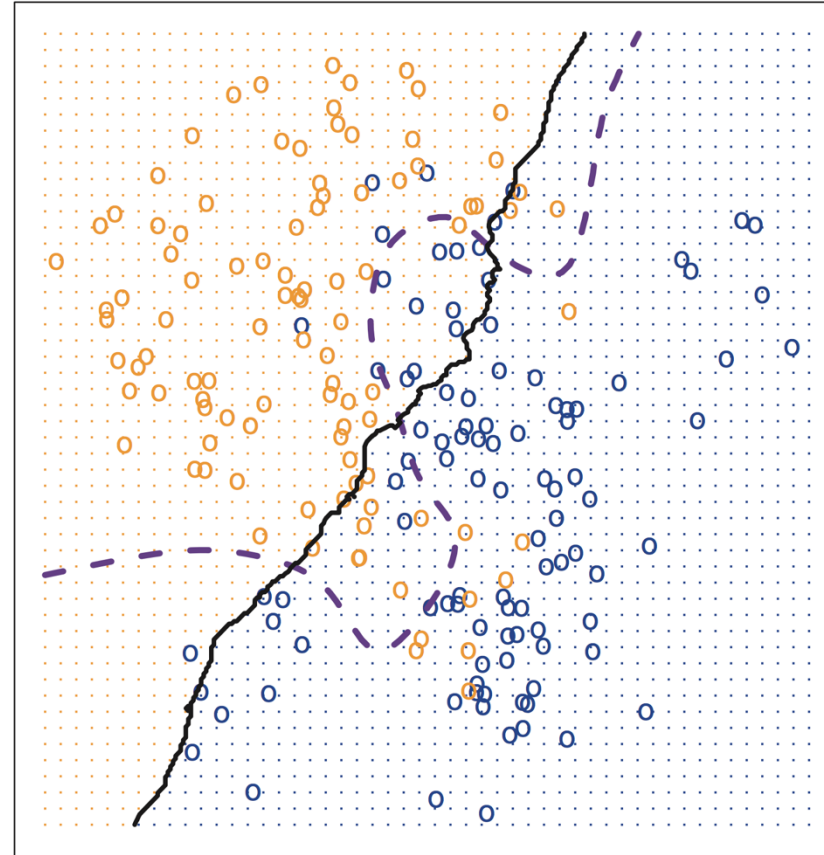
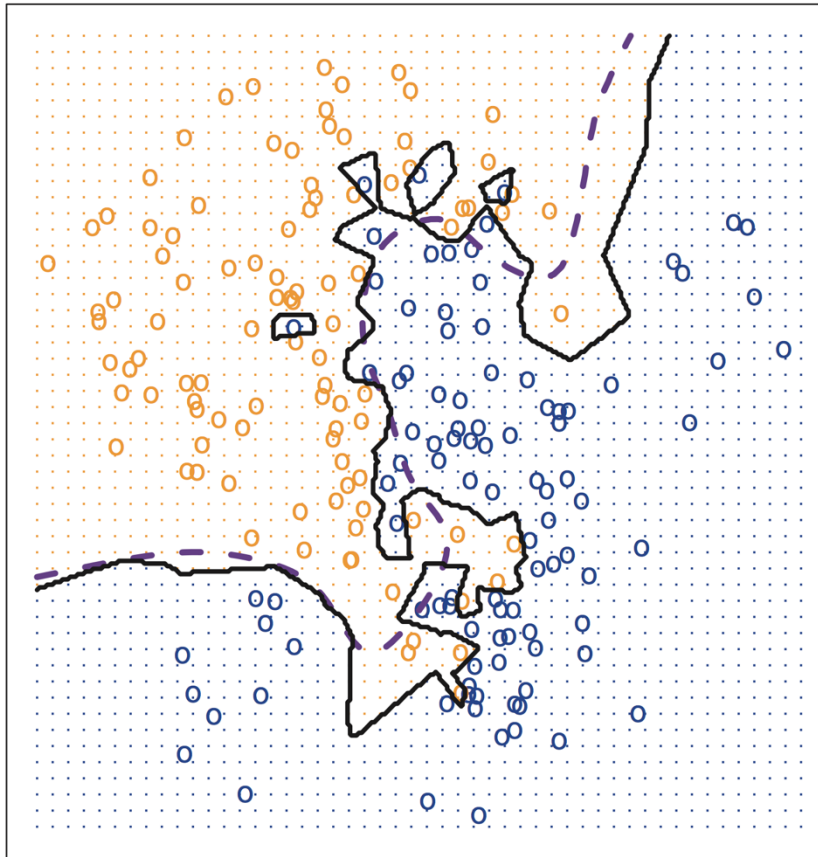


Figure 2.16 from ISL book (dashed line is “ideal” boundary)

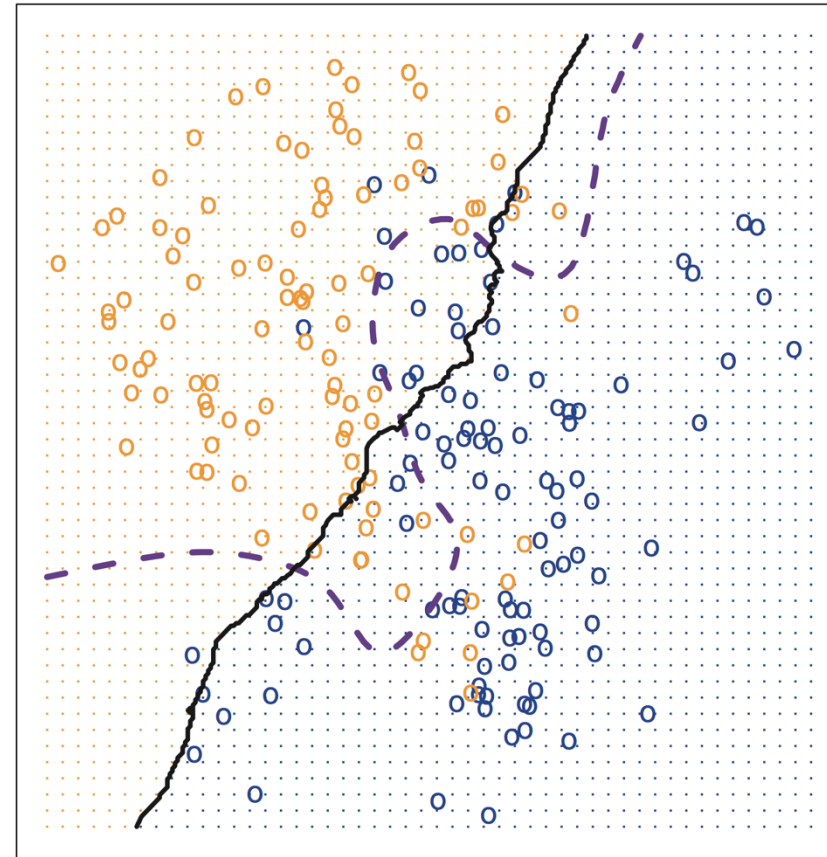
Comparing Decision Boundaries

KNN: $K=1$



Overfitting

KNN: $K=100$



Underfitting

Figure 2.16 from ISL book (dashed line is “ideal” boundary)

Featurization (rule of thumb)

- Real-valued features get copied directly. *Duame, Chap 3*
- Binary features become 0 (for false) or 1 (for true).
- Categorical features with V possible values get mapped to V -many binary indicator features.

Haven't discussed:

- normalization
- categorical variables on a spectrum

Handout

4. Using your response from the previous question, what would the *feature vector* become for x_1 ?

Day	Outlook	Temperature	Humidity	Wind	PlayTennis (y)
x_1	Sunny	Hot	High	Weak	No
x_2	Sunny	Hot	High	Strong	No
x_3	Overcast	Hot	High	Weak	Yes
x_4	Rain	Mild	High	Weak	Yes
x_5	Rain	Cool	Normal	Weak	Yes
x_6	Rain	Cool	Normal	Strong	No
x_7	Overcast	Cool	Normal	Strong	Yes
x_8	Sunny	Mild	High	Weak	No
x_9	Sunny	Cool	Normal	Weak	Yes
x_{10}	Rain	Mild	Normal	Weak	Yes

Sunny:	{0,1}	
Overcast:	{0,1}	
Rain:	{0,1}	
Temperature:	{0, 1, 2}	(Cool, Mild, Hot)
Humidity:	{0,1}	(Normal, High)
Wind	{0,1}	(Weak, Strong)

Data from Machine Learning by Tom Mitchell (Table 3.2)

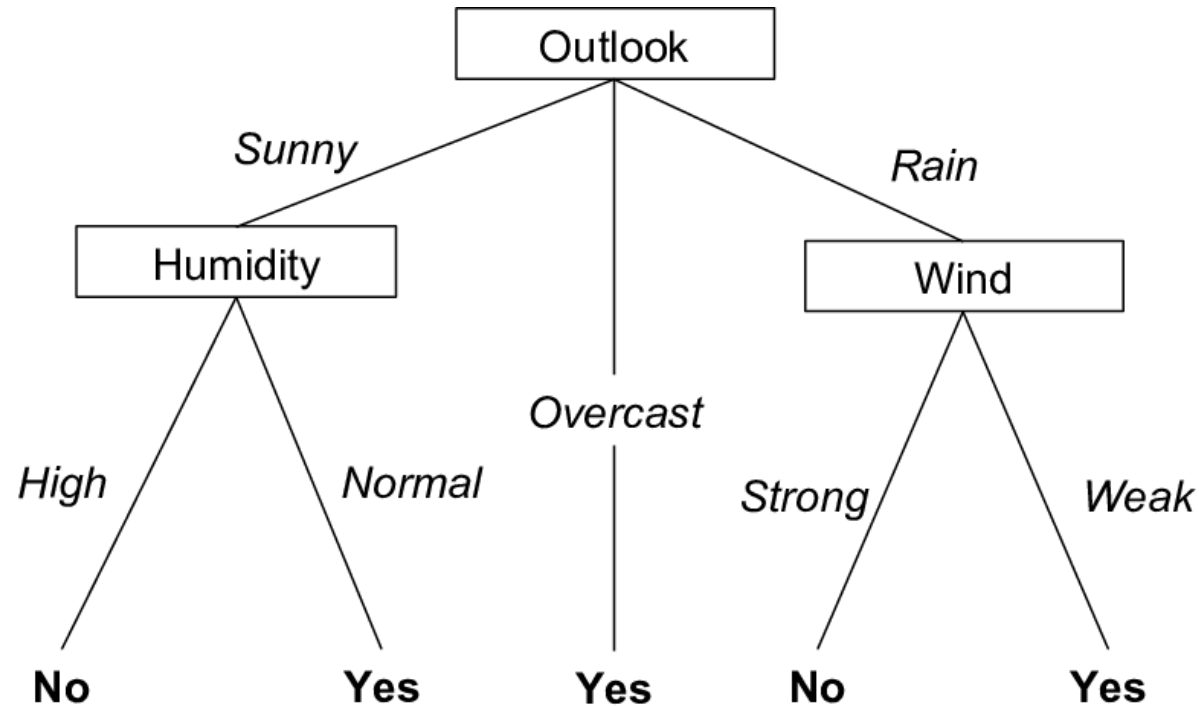
x_1

Sunny	Overcast	Rain	Temp	Humidity	Wind
1	0	0	2	1	0

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Decision Tree example (tennis)

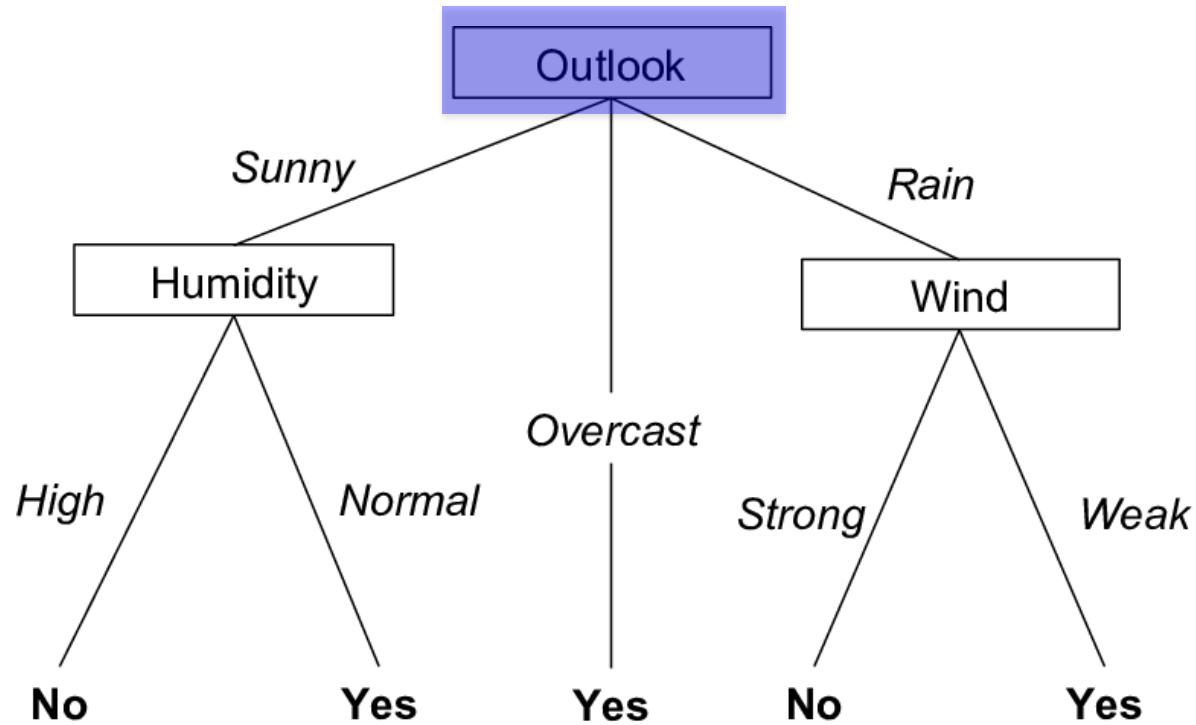


Each internal node: test one feature

Each branch from node: selects one value of the feature

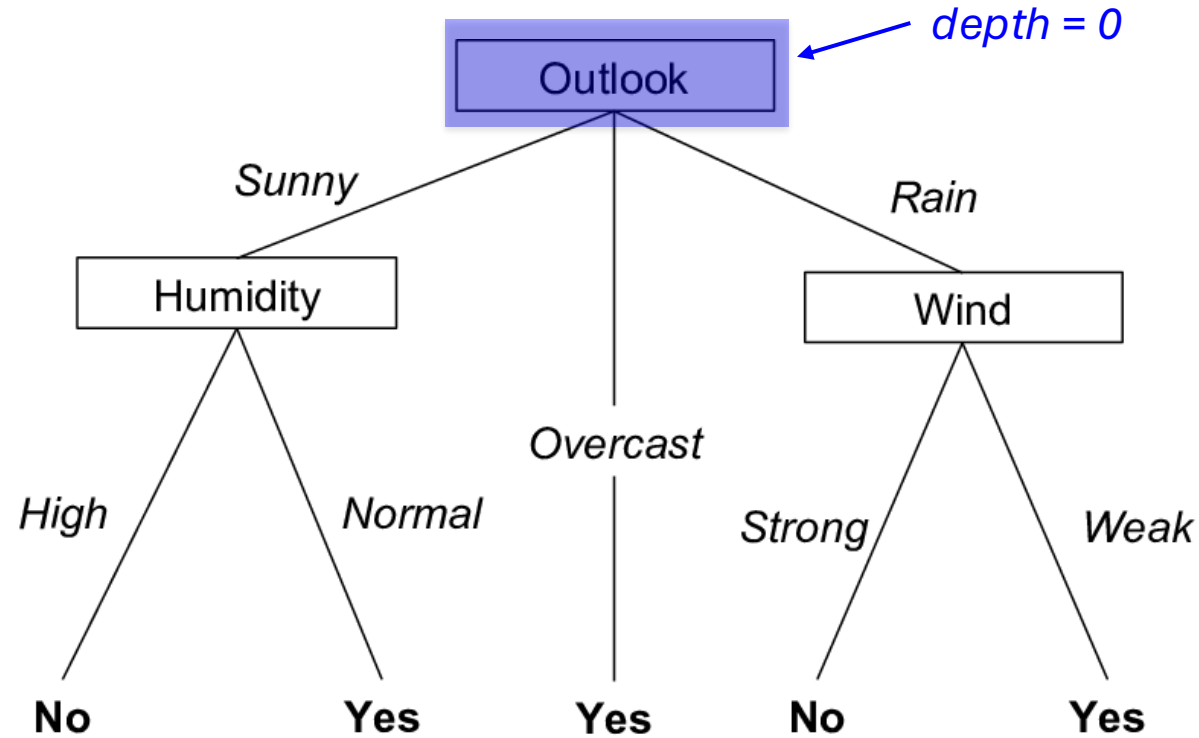
Each leaf node: predict y

Decision Tree example (tennis)



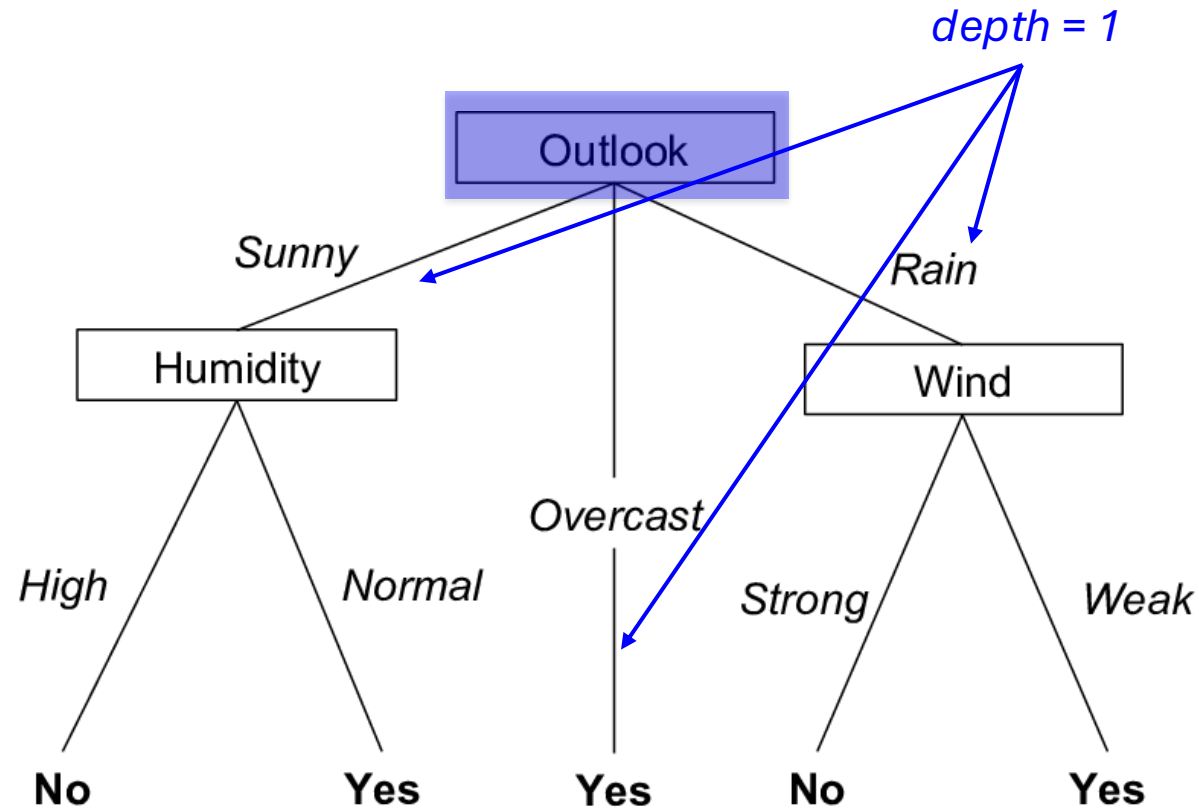
Key term: *depth*

Decision Tree example (tennis)



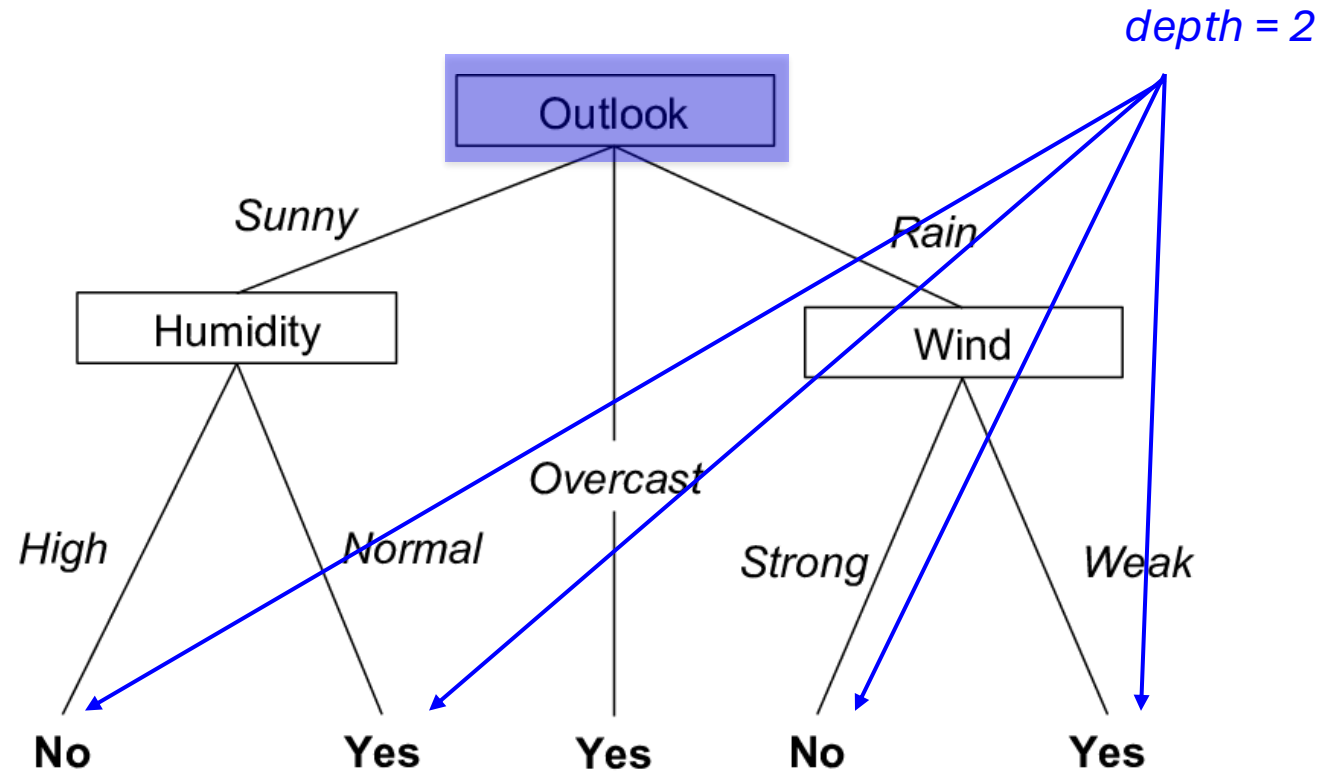
Key term: *depth*

Decision Tree example (tennis)



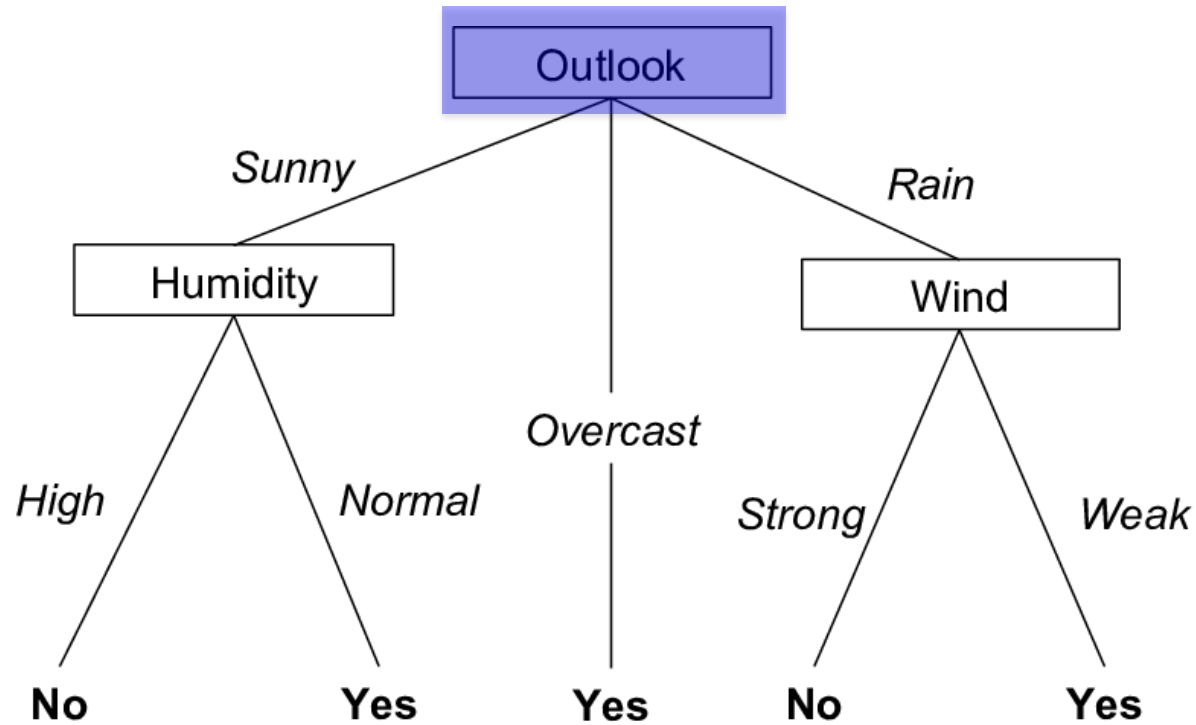
Key term: *depth*

Decision Tree example (tennis)



Key term: *depth*

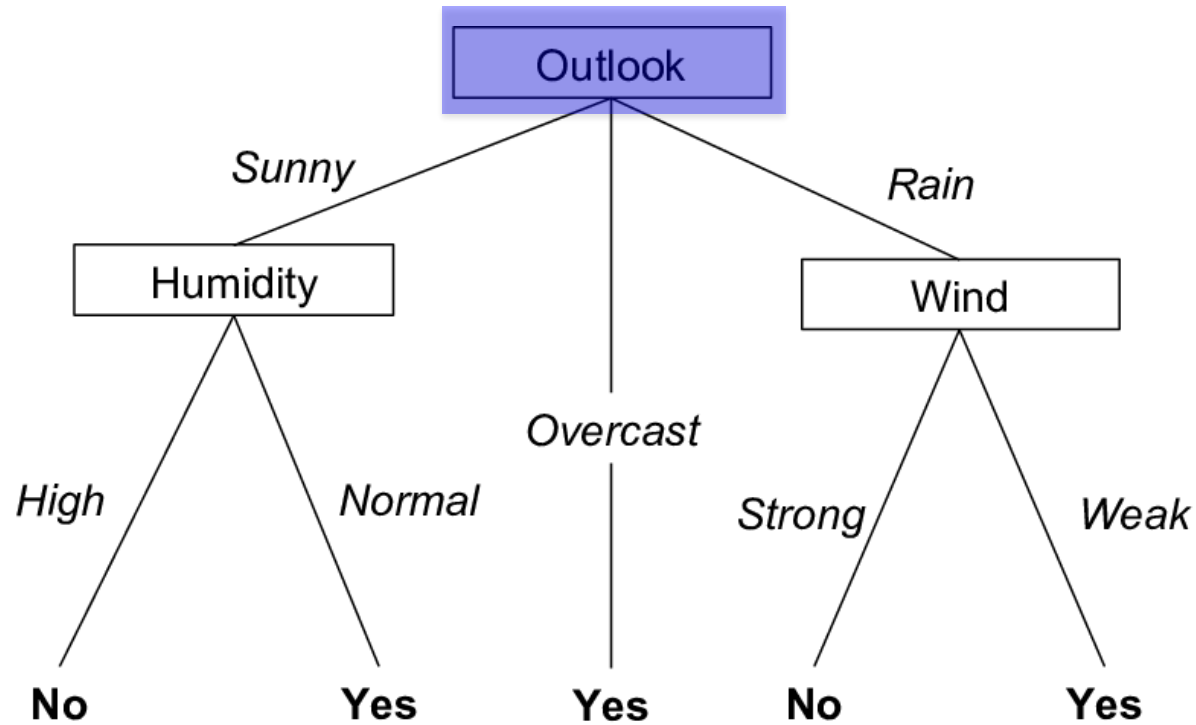
Decision Tree example (tennis)



(test example) $x =$

Outlook	Temp	Humidity	Wind
Rain	Hot	High	Strong

Decision Tree example (tennis)

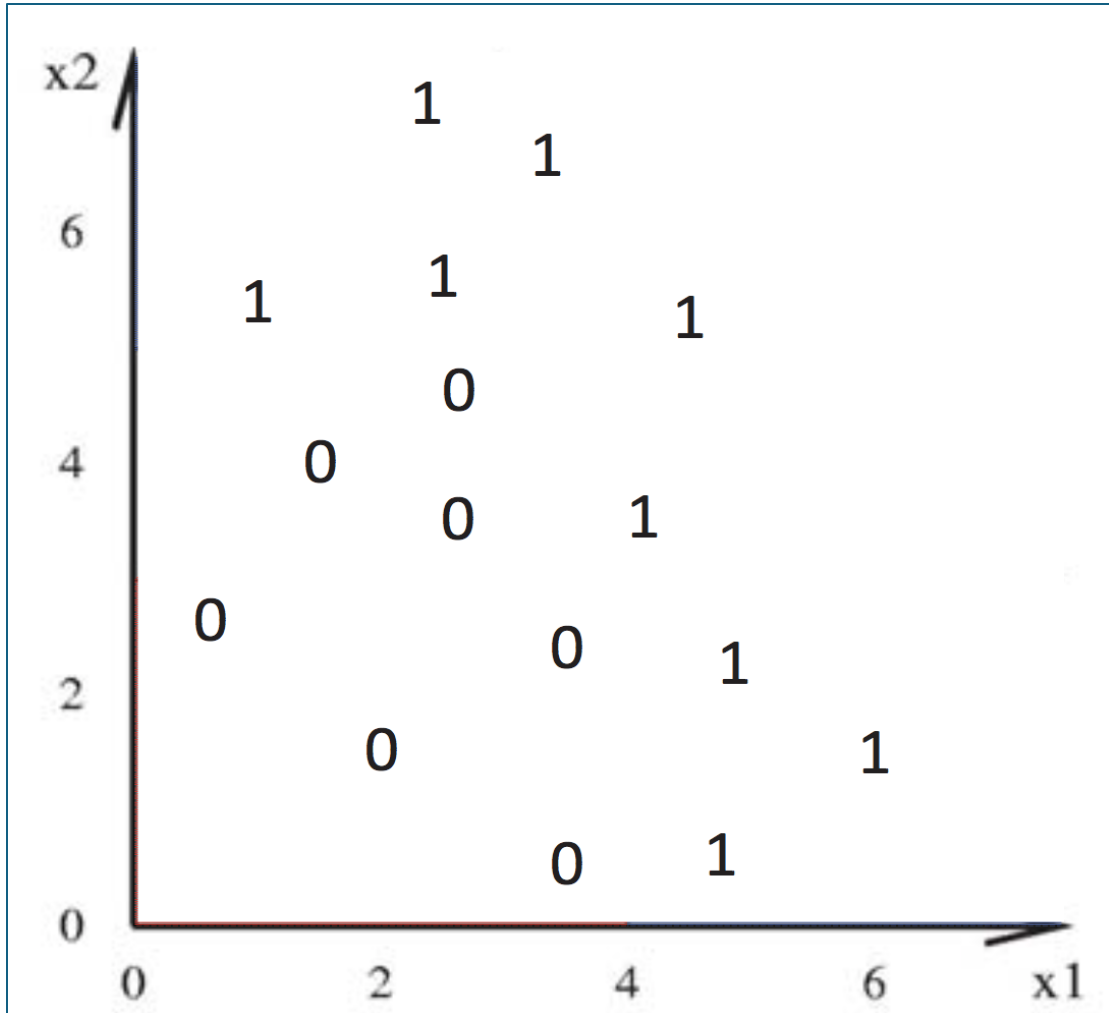


(test example) $x =$

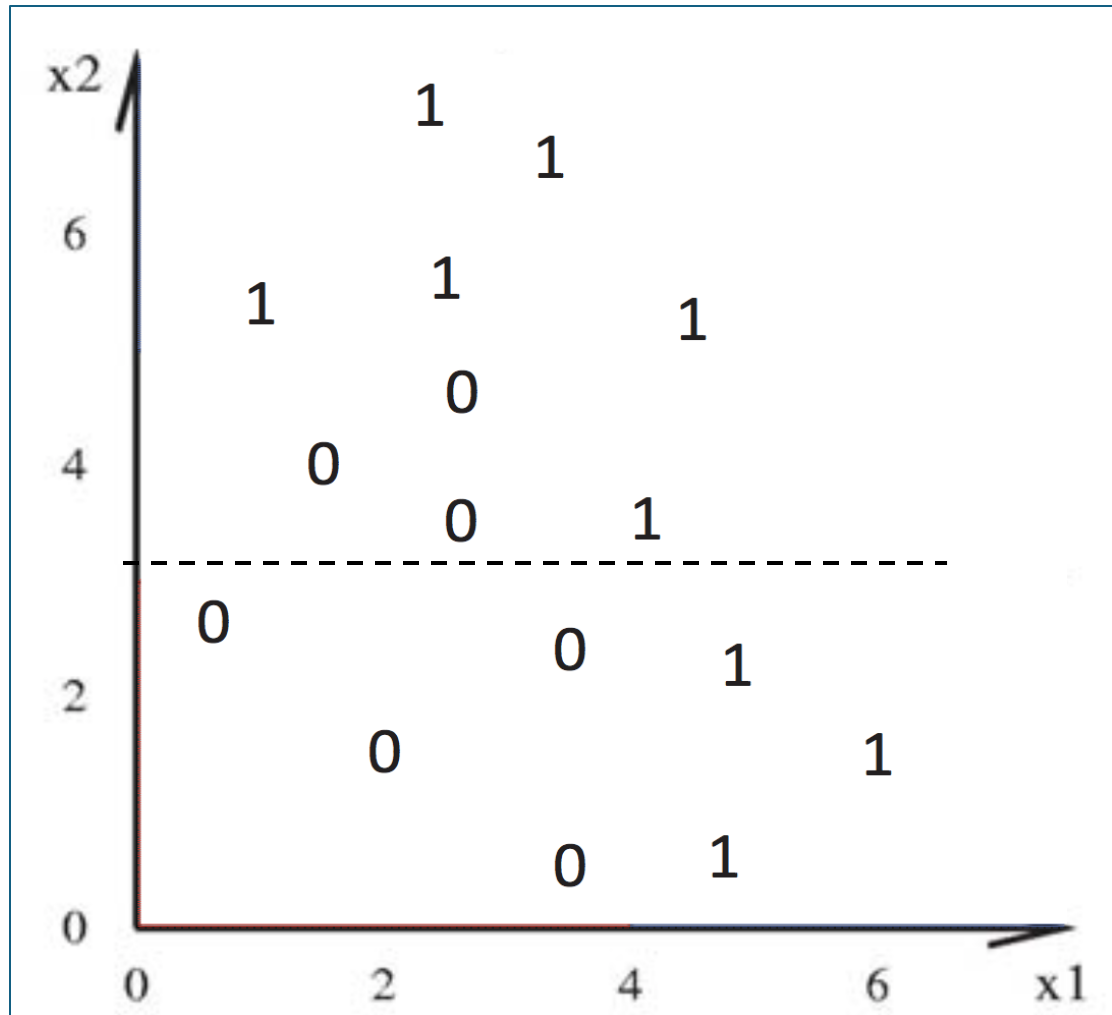
Outlook	Temp	Humidity	Wind
Rain	Hot	High	Strong

$\hat{y} = \text{No}$

Continuous Features

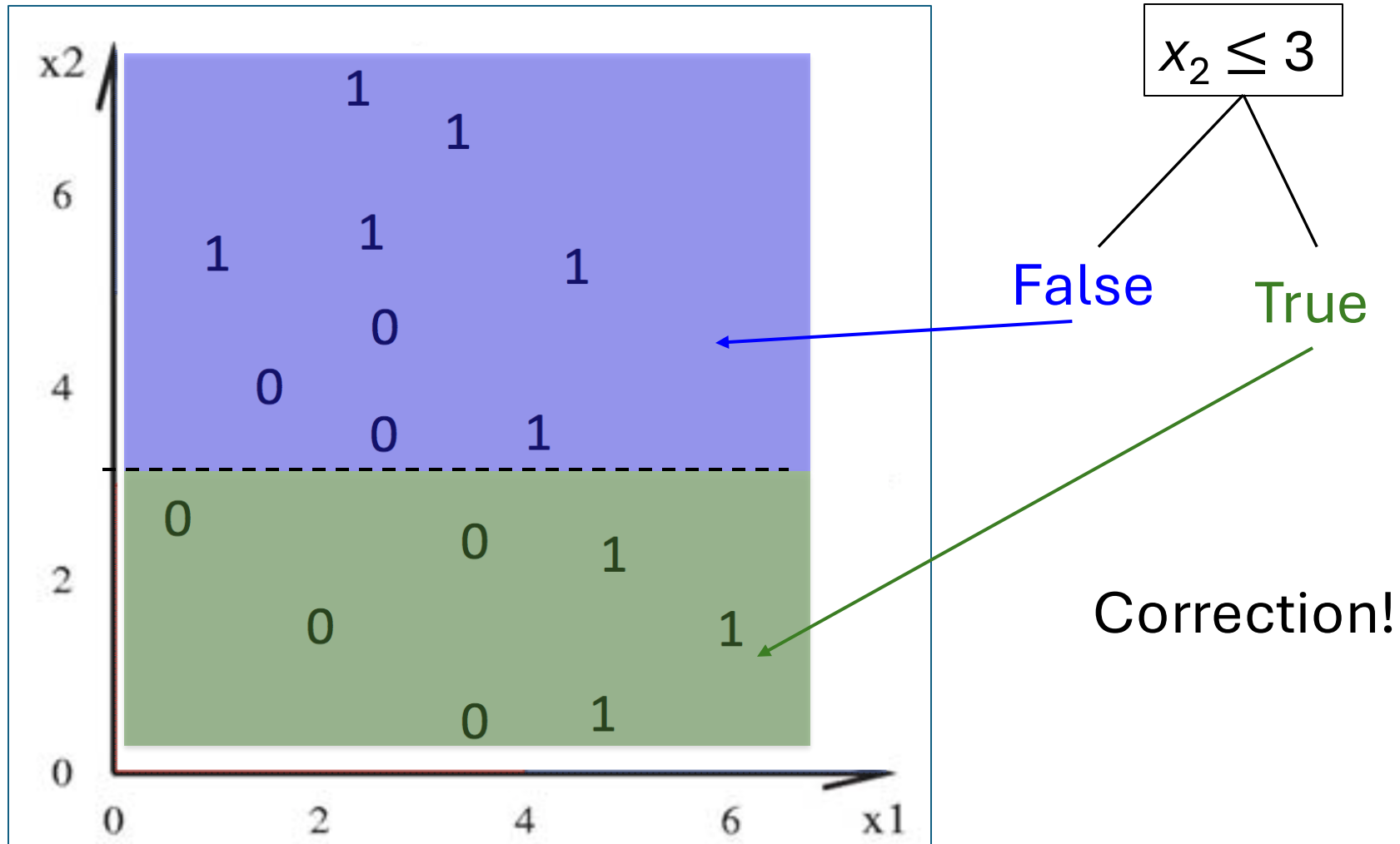


Continuous Features



$$x_2 \leq 3$$

Continuous Features



Decision Trees: Pros vs Cons

Discuss with a partner! Think about:

- * training and testing
- * featurization
- * runtime
- * human factors

Decision Trees: Pros vs Cons

- Very interpretable! Easy to say *why* we made a classification (can point to which features)
- Compact representation and fast predictions
- Can be brittle (not looking at each example holistically)
- Featurization and implementation difficulties

Next class

- Algorithm to create decision trees
- HW01 due Friday night
- Wednesday's Lab will be a lecture
- Thursday lecture back on schedule
 - Reading quiz on Thursday