

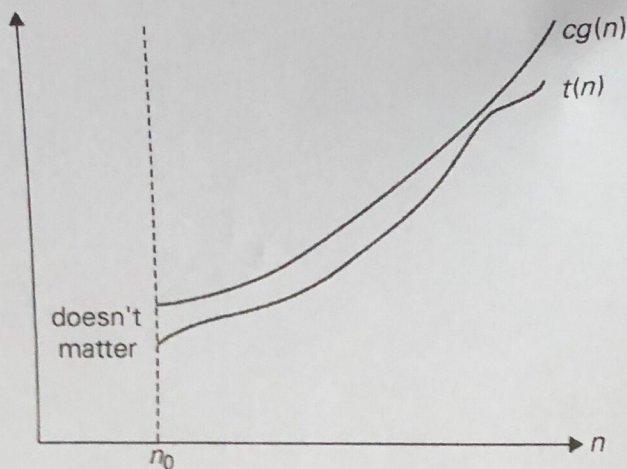
Student No:

07.11.2018

Name- Surname:

### ALGORITHM ANALYSIS MIDTERM EXAM

- 1) What is the "worst case analysis" of the function  $f(n) = 100n + 5$  for different values of  $n$ ?
- 2) Give 3 statements about big-oh notation and prove these statements by using the graphic below.



Big-oh notation:  $t(n) \in O(g(n))$ .

3) Sort the numbers in the below list with

- a) merge sort
- b) quick sort.

What are the worst cases of these two sorting algorithms with this number list?

2-5-9-8-15-6-3-10

1. Question: 40 pts, 2. Question: 30 pts, 3. Question: 40 pts.

You have 60 minutes. Good Luck.

Assoc. Prof. Dr. Ruya SAMLI

## Vize Çözümleri

- 1) What are the worst cases of the algorithms given below?
- computing the sum of  $n$  numbers,
  - computing  $n!$
  - finding the largest element in a list of  $n$  numbers.

(Exercises 2.1 Kitapta)

- $n$  sayısının çok büyük olması
  - $10^3$  ten büyük sayıların hesaplanması çok zor olması ve recursion düşer
  - Listenin çok büyük olması
- 2) Find the big- $O$  notation of the algorithm given by  $f(n) = 100n + 5$ .

a) for all  $n \geq 5$

b) for all  $n \leq 1$

You must find the  $C$  and  $g(n)$  for both situations.

a)  $f(x) \leq C \cdot g(x) \quad \underline{n \geq 5}$

$$100n + 5 \leq C \cdot g(x)$$

$$100n + 5 \leq 100n + n$$

$$100n + 5 \leq 101n$$

$$g(x) = O(n)$$

$$C = 101$$

b)  $f(x) \leq C \cdot g(x) \quad \underline{n \geq 1}$

$$100n + 5 \leq C \cdot g(x)$$

$$100n + 5 \leq 100n + 5n$$

$$100n + 5 \leq 105n$$

$$g(x) = O(n)$$

$$C = 105$$

(Kitapta olan bir soru).

- 3) Prove that bubble sort uses a brute-force algorithm approach.  
Algoritmayı açıklayarak kanıtlamak doğru cevap.

## Algorithms

Choosing between Exact and Approximate Problem Solving

Exact solving <sup>generally</sup> have an exact formula.

Approximate solving Examples; Square root, evaluating definite integrals