

## COMP9024 22T3

1/100

Data Structures and Algorithms



*Michael Thielscher*

Web Site: [www.cse.unsw.edu.au/~cs9024](http://www.cse.unsw.edu.au/~cs9024)

## Course Convenor

2/100

Name: Michael Thielscher

Office: K17-4011 (turn left from lift and dial 57129)

Phone: 9385 7129

Email: [mit@unsw.edu.au](mailto:mit@unsw.edu.au)

Consults: technical (course contents): Forum  
technical/personal: Thur 11am-12pm (online)    personal: Email

Research: Artificial Intelligence, Robotics, General Problem-Solving Systems

Pastimes: Fiction, Films, Food, Football

## ... Course Convenor

3/100

*Tutors:* Kamiyu Hijikata, [k.hijikata@student.unsw.edu.au](mailto:k.hijikata@student.unsw.edu.au)  
Kevin Luong, [kevin.luong@unsw.edu.au](mailto:kevin.luong@unsw.edu.au)  
Daria Schumm, [d.schumm@student.unsw.edu.au](mailto:d.schumm@student.unsw.edu.au)

*Programming Help Labs:* Fri 3pm-4pm (on-campus, [Clavier Lab K14-LG20](#))  
Mon 3pm-4pm (online)  
Tues 11am-12noon (online)

## Course Goals

4/100

COMP9021 ...

- gets you thinking like a *programmer*
- solving problems by developing programs
- expressing your ideas in the language Python

COMP9024 ...

- gets you thinking like a *computer scientist*
- knowing fundamental data structures/algorithms
- able to reason about their applicability/effectiveness
- able to analyse the efficiency of programs
- able to code in C

*Data structures*

- how to store data inside a computer for efficient use

*Algorithms*

- step-by-step process for solving a problem (within finite amount of space and time)
- 

## ... Course Goals

5/100

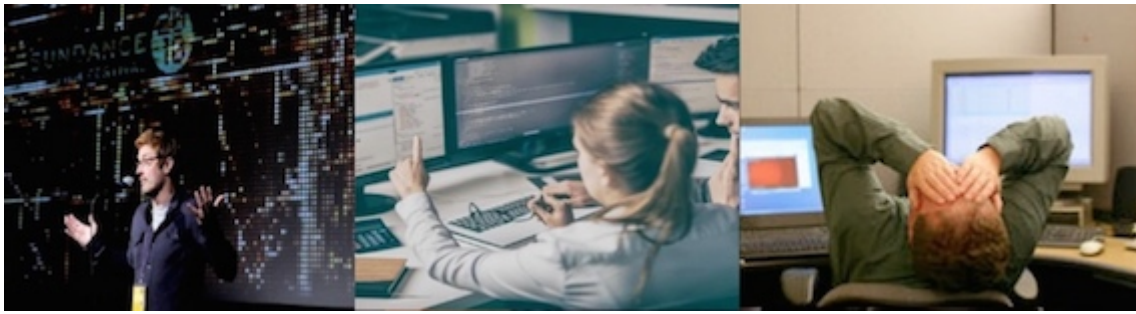
COMP9021 ...



## ... Course Goals

6/100

COMP9024 ...



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## Pre-conditions

7/100

There are no prerequisites for this course.

However we will move at fast pace through the necessary programming fundamentals. You may find it helpful if already you are able to:

- produce correct programs from a specification
- understand the state-based model of computation  
(variables, assignment, function parameters)
- use fundamental data structures  
(characters, numbers, strings, arrays)
- use fundamental control structures (if, while, for)
- know fundamental programming techniques (recursion)
- fix simple bugs in incorrect programs

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## Post-conditions

8/100

At the *end* of this course you should be able to:

- choose/develop effective data structures (DS)  
(graphs, search trees, ...)
- choose/develop algorithms (A) on these DS  
(graph algorithms, tree algorithms, string algorithms, ...)
- analyse performance characteristics of algorithms
- develop and maintain C programs

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## Access to Course Material

9/100

All course information is placed on the main course website:

- [www.cse.unsw.edu.au/~cs9024](http://www.cse.unsw.edu.au/~cs9024)

Need to login to access material, submit homework and assignment, post on the forum, view your marks

Access lecture recordings and quizzes (weeks 2, 4, 7, 9) on Moodle:

- [COMP9024 Data Structures & Algorithms \(T3-2022\)](#)

Always give credit when you use someone else's work.

Ideas for the COMP9024 material are drawn from

- slides by John Shepherd (COMP1927), Hui Wu (COMP9024) and Alan Blair (COMP1917)
- Robert Sedgewick's and Alistair Moffat's books, Goodrich and Tamassia's Java book, Skiena and Revilla's programming challenges book

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## Schedule

10/100

Week	Lectures	Assessment	Notes
1	Introduction, C language	—	
2	Analysis of algorithms	quiz	
3	Dynamic data structures	program	
4	Graph data structures	quiz	
5	Graph algorithms	program	
6	<b>Mid-term test (Wednesday)</b>		Large Assignment
7	Search tree data structures	quiz	
8	Search tree algorithms	program	
9	String algorithms, Approximation	quiz	
10	Randomised algorithms, Review	program	due

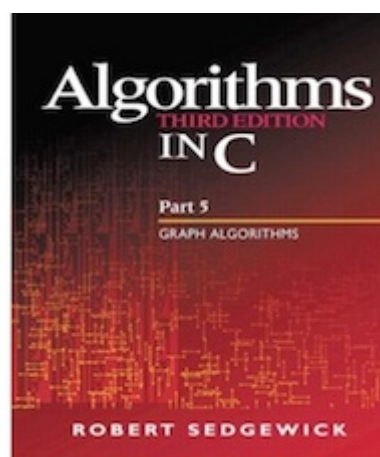
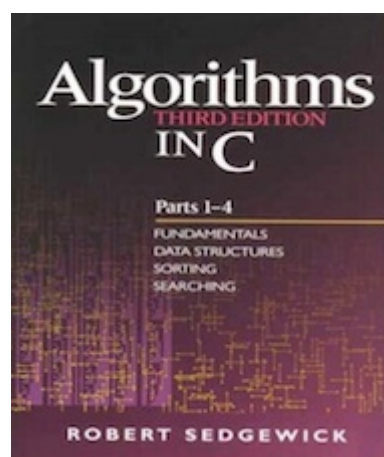
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## Resources

11/100

Textbook is a "double-header"

- Algorithms in C, Parts 1-4, Robert Sedgewick
- Algorithms in C, Part 5, Robert Sedgewick

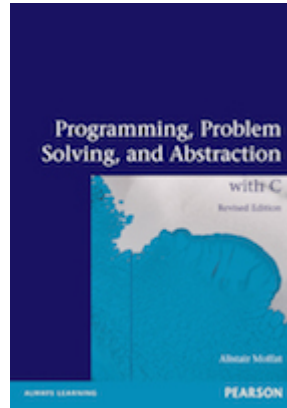


Good books, useful beyond COMP9024 (but coding style ...)

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Supplementary textbook:

- Alistair Moffat  
*Programming, Problem Solving, and Abstraction with C*  
Pearson Educational, Australia, Revised edition 2013, ISBN 978-1-48-601097-4



Also, numerous online C resources are available.

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## Problem Sets

13/100

The weekly homework aims to:

- clarify any problems with lecture material
- work through exercises related to lecture topics
- give practice with algorithm design skills (think before coding)

Problem sets available on web at the time of the lecture

Sample solutions will be posted in the following week

Do them yourself! and Don't fall behind!

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## Weekly Assessments

14/100

In weeks (1), 3, 5, 8, 10:

- you will be asked to submit 1 or 2 (small) programs
- which will be auto-marked against one or more test cases

In weeks 2, 4, 7, 9:

- you will be given a short quiz (4-5 questions)
- with questions related to the exercises and the lecture

Programs and quizzes contribute 8% + 8% to overall mark.

**Strict deadlines** (no late submissions possible, sample solutions posted right after deadline)

- First assessment (week 1) is **programming** practice and will not count
    - Deadline: Tuesday, 20 September, 5:00:00pm
- 

## Large Assignment

15/100

The large assignment gives you experience applying tools/techniques (but to a larger programming problem than the homework)

The assignment will be carried out individually.

The assignment will be released after the mid-term test and is due in week 10.

The assignment contributes 12% to overall mark.

**5% penalty** will be applied for every day late after the deadline, capped at 5 days (120 hrs)

- 2 hours late: 5% reduction
- 2 days and 23 hrs late: 15% reduction
- 5 days and 1 hour late: 0 marks

NB: Late submissions *not* possible for weekly assessments

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## ... Large Assignment

16/100

Advice on doing the large assignment:

Programming assignments always take longer than you expect.

Don't leave them to the last minute.

Organising your time → no late penalty.

If you do leave them to the last minute:

- take the late penalty rather than copying
- 

## Plagiarism

17/100



Just Don't Do it

We get **very annoyed** by people who plagiarise.

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## ... Plagiarism

18/100

Examples of **Plagiarism** ([student.unsw.edu.au/plagiarism](http://student.unsw.edu.au/plagiarism)):

### 1. Copying

Using same or similar idea *without acknowledging the source*  
This includes copying ideas from a website, internet

### 2. Collusion

Presenting work as independent when produced in collusion with others  
This includes *students providing their work to another student*

- which includes using any form of *publicly readable code repository*

Plagiarism will be checked for and **punished** (0 marks for assignment and, in severe cases/repeat offenders, 0 marks for course)

For COMP9024 you will need to complete a short online course on Academic Integrity in Programming Courses

- We will ask for your completion certificate

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## Mid-term Test

19/100

1-hour online test in week 6 (*Wednesday, ~~18~~ 19 October, at time of the lecture*).

Format:

- some multiple-choice questions
- some descriptive/analytical questions with short answers

The mid-term test contributes 12% to overall mark.

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## Final Exam

20/100

2-hour ~~torture~~ online exam during the exam period.

Format:

- some multiple-choice questions
- some descriptive/analytical questions with open answers

The final exam contributes 60% to overall mark.

Must score at least 25/60 in the final exam to pass the course.

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How to pass the mid-term test and the Final Exam:

- do the Homework *yourself*
  - do the Homework *every week*
  - practise programming in C *from Week 1*
  - practise programming outside classes
  - read the lecture notes
  - read the corresponding chapters in the textbooks
- 

## Summary

22/100

The goal is for you to become a better Computer Scientist

- more confident in your own ability to choose data structures
  - more confident in your own ability to develop algorithms
  - able to analyse and justify your choices
  - producing a better end-product
  - ultimately, enjoying the software design and development process
- 

## C Programming Language

### Why C?

24/100

- good example of an imperative language
  - gives the programmer great control
  - produces fast code
  - many libraries and resources
  - main language for writing operating systems and compilers; and commonly used for a variety of applications in industry (and science)
- 

### Brief History of C

25/100

- C was originally designed for and implemented on UNIX
  - B (author: **Ken Thompson**, 1970) was the predecessor to C, but there was no A
  - **Dennis Ritchie** was the author of C (around 1971)
  - American National Standards Institute (ANSI) C standard published in 1988
    - this greatly improved source code portability
  - Current standard: C11 (published in 2011)
- 

### Basic Structure of a C Program

26/100

```
// include files
```



```
// global definitions

// function definitions
.
.
.

// main function
int main(arguments) {

    // local variables

    // body of main function

    return 0;
}
```

---

## Exercise #1: What does this program compute?

27/100

```
#include <stdio.h>

int f(int m, int n) {

    while (m != n) {
        if (m > n) {
            m = m-n;
        } else {
            n = n-m;
        }
    }
    return m;
}

int main(void) {

    printf("%d\n", f(30,18));
    return 0;
}
```

---

## Example: Insertion Sort in C

28/100

Insertion Sort algorithm:

```
insertionSort(A):
|   Input array A[0..n-1] of n elements
|
|   for all i=1..n-1 do
|       element=A[i], j=i-1
|       while j≥0 and A[j]>element do
|           A[j+1]=A[j]
|           j=j-1
|       end while
|       A[j+1]=element
|   end for
```

---

## ... Example: Insertion Sort in C

29/100

```

#include <stdio.h> // include standard I/O library defs and functions

#define SIZE 6     // define a symbolic constant

void insertionSort(int array[], int n) { // function headers must provide types
    int i; // each variable must have a type
    for (i = 1; i < n; i++) { // for-loop syntax
        int element = array[i];
        int j = i-1;
        while (j >= 0 && array[j] > element) { // logical AND
            array[j+1] = array[j];
            j--; // abbreviated assignment j=j-1
        }
        array[j+1] = element; // statements terminated by ;
    } // code blocks enclosed in { }
}

int main(void) { // main: program starts here
    int numbers[SIZE] = { 3, 6, 5, 2, 4, 1 }; /* array declaration
                                                and initialisation */

    int i;
    insertionSort(numbers, SIZE);
    for (i = 0; i < SIZE; i++)
        printf("%d\n", numbers[i]); // printf defined in <stdio>

    return 0; // return program status (here: no error) to environment
}

```

---

## Compiling with gcc

30/100

**C source code:** `prog.c`

↓

`a.out`    **(executable program)**

To compile a program `prog.c`, you type the following:

```
prompt$ gcc prog.c
```

To run the program, type:

```
prompt$ ./a.out
```

---

## ... Compiling with gcc

31/100

Command line options:

- The default with `gcc` is not to give you any warnings about potential problems
- Good practice is to be tough on yourself:

```
prompt$ gcc -Wall -Werror prog.c
```

which reports as errors all warnings to anything it finds that is potentially wrong or non ANSI compliant

- The `-o` option tells `gcc` to place the compiled object in the named file rather than `a.out`

## Sidetrack: Printing Variable Values with `printf()`

32/100

Formatted output written to standard output (e.g. screen)

```
printf(format-string, expr1, expr2, ...);
```

`format-string` can use the following placeholders:

<code>%d</code>	decimal	<code>%f</code>	floating-point
<code>%c</code>	character	<code>%s</code>	string
<code>\n</code>	new line	<code>\"</code>	quotation mark

Examples:

```
num = 3;
printf("The cube of %d is %d.\n", num, num*num*num);
```

The cube of 3 is 27.

```
id = 'z';
num = 1234567;
printf("Your \"login ID\" will be in the form of %c%d.\n", id, num);
```

Your "login ID" will be in the form of z1234567.

- Can also use width and precision:

```
printf("%.3f\n", 3.14159);
```

3.142

---

## Algorithms in C

### Basic Elements

34/100

Algorithms are built using

- assignments
- conditionals
- loops
- function calls/return statements

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### Assignments

35/100

- In C, each statement is terminated by a semicolon ;
- Curly brackets { } used to enclose statements in a block
- Usual arithmetic operators: +, -, \*, /, %
- Usual assignment operators: =, +=, -=, \*=, /=, %=

- The operators `++` and `--` can be used to increment a variable (add 1) or decrement a variable (subtract 1)

- It is recommended to put the increment or decrement operator after the variable:

```
// suppose k=6 initially
k++; // increment k by 1; afterwards, k=7
n = k--; // first assign k to n, then decrement k by 1
// afterwards, k=6 but n=7
```

- It is also possible (but NOT recommended) to put the operator before the variable:

```
// again, suppose k=6 initially
++k; // increment k by 1; afterwards, k=7
n = --k; // first decrement k by 1, then assign k to n
// afterwards, k=6 and n=6
```

---

## ... Assignments

36/100

C assignment statements are really expressions

- they return a result: the value being assigned
- the return value is generally ignored

Frequently, assignment is used in loop continuation tests

- to combine the test with collecting the next value
- to make the expression of such loops more concise

Example: The pattern

```
v = readNextItem();
while (v != 0) {
    process(v);
    v = readNextItem();
}
```

is often written as

```
while ((v = readNextItem()) != 0) {
    process(v);
}
```

---

## Exercise #2: What are the final values of `a` and `b`?

37/100

1.

```
a = 1; b = 5;
while (a < b) {
    a++;
    b--;
}
```

2.

```
a = 1; b = 5;
while ((a += 2) < b) {
    b--;
}
```

- 
1. `a == 3, b == 3`
  2. `a == 5, b == 4`
- 

## Conditionals

39/100

### Relational and logical operators

<code>a &gt; b</code>	<code>a</code> greater than <code>b</code>
<code>a &gt;= b</code>	<code>a</code> greater than or equal <code>b</code>
<code>a &lt; b</code>	<code>a</code> less than <code>b</code>
<code>a &lt;= b</code>	<code>a</code> less than or equal <code>b</code>
<code>a == b</code>	<code>a</code> equal to <code>b</code>
<code>a != b</code>	<code>a</code> not equal to <code>b</code>
<code>a &amp;&amp; b</code>	<code>a</code> logical <b>and</b> <code>b</code>
<code>a    b</code>	<code>a</code> logical <b>or</b> <code>b</code>
<code>! a</code>	logical <b>not</b> <code>a</code>

A relational or logical expression evaluates to **1** if true, and to **0** if false

---

### ... Conditionals

40/100

```
if (expression) {  
    some statements;  
}
```

```
if (expression) {  
    some statements1;  
} else {  
    some statements2;  
}
```

- some statements executed if, and only if, the evaluation of **expression** is non-zero
  - some statements<sub>1</sub> executed when the evaluation of **expression** is non-zero
  - some statements<sub>2</sub> executed when the evaluation of **expression** is zero
  - Statements can be single instructions or blocks enclosed in `{ }`
- 

### ... Conditionals

41/100

*Indentation* is very important in promoting the readability of the code

Each logical block of code is indented:

```
// Style 1           // Style 2 (my preference)           // Preferred else-if style
```

<pre>if (x) {     statements; }</pre>	<pre>if (x) {     statements; }</pre>	<pre>if (expression1) {     statements1; } else if (exp2) {     statements2; } else if (exp3) {     statements3; } else {     statements4; }</pre>
---------------------------------------	---------------------------------------	--

## Exercise #3: Conditionals

42/100

1. What is the output of the following program fragment?

```
if ((x > y) && !(y-x <= 0)) {
    printf("Aye\n");
} else {
    printf("Nay\n");
}
```

2. What is the resulting value of `x` after the following assignment?

```
x = (x >= 0) + (x < 0);
```

1. The condition is unsatisfiable, hence the output will always be

Nay

2. No matter what the value of `x`, one of the conditions will be true (`==1`) and the other false (`==0`)

Hence the resulting value will be `x == 1`

## Loops

44/100

C has two different "while loop" constructs

<pre>// while loop while (expression) {     some statements; }</pre>	<pre>// do .. while loop do {     some statements; } while (expression);</pre>
--	--

The `do .. while` loop ensures the statements will be executed at least once

## ... Loops

45/100

The "for loop" in C

```
for (expr1; expr2; expr3) {
    some statements;
}
```

- `expr1` is evaluated before the loop starts

- `expr2` is evaluated at the beginning of each loop
  - if it is non-zero, the loop is repeated
- `expr3` is evaluated at the end of each loop

Example: 

```
for (i = 1; i < 10; i++) {
    printf("%d %d\n", i, i * i);
}
```

---

## Exercise #4: What is the output of this program?

46/100

```
int i, j;
for (i = 8; i > 1; i /= 2) {
    for (j = i; j >= 1; j--) {
        printf("%d%d\n", i, j);
    }
    printf("\n");
}
```

---

```
88
87
..
81

44
..
41

22
21
```

---

## Functions

48/100

Functions have the form

```
return-type function-name(parameters) {
    local variable declarations

    statements

    return ...;
}
```

- if `return_type` is `void` then the function does not return a value
- if `parameters` is `void` then the function has no arguments

---

## ... Functions

49/100

When a function is called:

1. memory is allocated for its parameters and local variables
  2. the arguments in the calling function are evaluated
  3. C uses "call-by-value" parameter passing ...
    - o the function works only on its own local copies of the parameters, not the ones in the calling function
  4. local variables need to be assigned before they are used (otherwise they will have "garbage" values)
  5. function code is executed, until the first `return` statement is reached
- 

## ... Functions

50/100

When a `return` statement is executed, the function terminates:

`return expression;`

1. the returned `expression` will be evaluated
2. all local variables and parameters will be thrown away when the function terminates
3. the calling function is free to use the returned value, or to ignore it

Example:

```
// Euclid's gcd algorithm (recursive version)
int euclid_gcd(int m, int n) {
    if (n == 0) {
        return m;
    } else {
        return euclid_gcd(n, m % n);
    }
}
```

The `return` statement can also be used to terminate a function of return-type `void`:

`return;`

---

# Data Structures in C

## Basic Data Types

52/100

- In C each variable must have a type
- C has the following generic data types:

<code>char</code>	character	'A', 'e', '#', ...
<code>int</code>	integer	2, 17, -5, ...
<code>float</code>	floating-point number	3.14159, ...
<code>double</code>	double precision floating-point	3.14159265358979, ...

There are other types, which are variations on these

- Variable declaration must specify a data type and a name; they can be initialised when they are declared:



```
float x;  
char ch = 'A';  
int j = i;
```

---

## Arrays

53/100

An *array* is

- a collection of same-type variables
- arranged as a linear sequence
- accessed using an integer subscript
- for an array of size  $N$ , valid subscripts are  $0..N-1$

Examples:

```
int a[20];    // array of 20 integer values/variables  
char b[10];   // array of 10 character values/variables
```

---

## ... Arrays

54/100

Larger example:

```
#define MAX 20  
  
int i;           // integer value used as index  
int fact[MAX];   // array of 20 integer values  
  
fact[0] = 1;  
for (i = 1; i < MAX; i++) {  
    fact[i] = i * fact[i-1];  
}
```

---

## Sidetrack: C Style

55/100

We can define a [symbolic constant](#) at the top of the file

```
#define SPEED_OF_LIGHT 299792458.0  
#define ERROR_MESSAGE "Out of memory.\n"
```

Symbolic constants make the code easier to understand and maintain

```
#define NAME replacement_text
```

- The compiler's pre-processor will replace all occurrences of `NAME` with `replacement_text`
  - it will **not** make the replacement if `NAME` is inside quotes ("...") or part of another name
- 

## ... Sidetrack: C Style

56/100

UNSW Computing provides a style guide for C programs:

Not strictly mandatory for COMP9024, but very useful guideline

Style considerations that *do* matter for your COMP9024 assignments:

- use proper layout, including consistent indentation
  - 3 spaces throughout, or 4 spaces throughout
  - do *not* use TABs
- keep functions short and break into sub-functions as required
- use meaningful names (for variables, functions etc)
- use symbolic constants to avoid burying "magic numbers" in the code
- comment your code

## ... Sidetrack: C Style

57/100

C has a reputation for allowing obscure code, leading to ...

The International Obfuscated C Code Contest

- Run each year since 1984
- Goal is to produce
  - a working C program
  - whose appearance is obscure
  - whose functionality unfathomable
- Web site: [www.ioccc.org](http://www.ioccc.org)
- 100's of examples of bizarre C code  
(understand these → you are a C master)

## ... Sidetrack: C Style

58/100

Most artistic code (Eric Marshall, 1986)

```

extern int
errno
;char
grrr
r,
;main(
int argc
argv, argc )
r ;
#define x int i,
x ;if (P( !
& P(j )>2 ?
; for (i=
_exit(argv[argc- 2 / cc[1*argc] |-1<4 ] ) ;printf("%d",P("")));}
P ( a ) char a ; { a ; while( a > " B "
/* - by E ricM arsh all- */); }
```

## ... Sidetrack: C Style

59/100

Just plain obscure (Ed Lycklama, 1985)

```

#define o define
#o __o write
#o ooo (unsigned)
#o o_o_ 1
#o _o_ char
#o _oo goto
#o _oo_ read
#o o_o for
#o o_ main
#o o__ if
#o oo_ 0
#o _o_(, __, __)(void) __o(, __, ooo(__))
#o __o (o_o_<<((o_o_<<(o_o_<<o_o_))+o_o_<<o_o_))+o_o_<<(o_o_<<(o_o_<<o_o_)))
o_(){o_ _=oo_, __, __, __[_o_];__oo __;__:__=o_o_o_;__:
_o(o_o_, __, __=(_o_o_<__?_o_o_:__));o_o(;;_o(o_o_, "\b", o_o_), __--);
_o(o_o_, " ", o_o_);o_(__--)_oo __;_o(o_o_, "\n", o_o_);__:o_(_=oo_(
oo_, __, __o))_oo __;};

```

---

## Strings

60/100

"String" is a special word for an array of characters

- end-of-string is denoted by `'\0'` (of type `char` and always implemented as 0)

Example:

If a character array `s[11]` contains the string "hello", this is how it would look in memory:

0	1	2	3	4	5	6	7	8	9	10
h	e	l	l	o	\0					

---

## Array Initialisation

61/100

Arrays can be initialised by code, or you can specify an initial set of values in declaration.

Examples:

```
char s[6] = {'h', 'e', 'l', 'l', 'o', '\0'};
```

```
char t[6] = "hello";
```

```
int fib[20] = {1, 1};
```

```
int vec[] = {5, 4, 3, 2, 1};
```

In the third case, `fib[0] == fib[1] == 1` while the initial values `fib[2] .. fib[19]` are undefined.

In the last case, C infers the array length (as if we declared `vec[5]`).

## Exercise #5: What is the output of this program?

62/100

```

1  #include <stdio.h>
2
3  int main(void) {
4      int arr[3] = {10,10,10};
5      char str[] = "Art";
6      int i;
7
8      for (i = 1; i < 3; i++) {
9          arr[i] = arr[i-1] + arr[i] + 1;
10         str[i] = str[i+1];
11     }
12     printf("Array[2] = %d\n", arr[2]);
13     printf("String = \"%s\"\n", str);
14     return 0;
15 }

```

---

```

Array[2] = 32
String = "At"

```

---

## Sidetrack: Reading Variable Values with `scanf()` and `atoi()`

64/100

Formatted input read from standard input (e.g. keyboard)

```
scanf(format-string, expr1, expr2, ...);
```

Converting string into integer

```
int value = atoi(string);
```

Example:

```

#include <stdio.h> // includes definition of and scanf()
#include <stdlib.h> // includes definition of atoi()

#define INPUT_STRLEN 20

...

char str[INPUT_STRLEN];
int n;

printf("Enter a string: ");
scanf("%19s", str);
n = atoi(str);
printf("You entered: \"%s\". This converts to integer %d.\n", str, n);

```

```

Enter a string: 9024
You entered: "9024". This converts to integer 9024.

```

---

## Arrays and Functions

65/100

When an array is passed as a parameter to a function

- the address of the start of the array is actually passed

→ an exception to the 'call-by-value' parameter passing in C!

Example:

```
int total, vec[20];  
...  
total = sum(vec);
```

Within the function ...

- the types of elements in the array are known
- the size of the array is unknown

---

## ... Arrays and Functions

66/100

Since functions do not know how large an array is:

- pass in the size of the array as an extra parameter, or
- include a "termination value" to mark the end of the array

So, the previous example would be more likely done as:

```
int total, vec[20];  
...  
total = sum(vec, 20);
```

Also, since the function doesn't know the array size, it can't check whether we've written an invalid subscript (e.g. in the above example 100 or 20).

---

## Exercise #6: Arrays and Functions

67/100

Implement a function that sums up all elements in an array.

Use the *prototype*

```
int sum(int[], int)
```

---

```
int sum(int vec[], int dim) {  
    int i, total = 0;  
  
    for (i = 0; i < dim; i++) {  
        total += vec[i];  
    }  
    return total;  
}
```

---

## Multi-dimensional Arrays

69/100

Examples:

<code>float q[2][2];</code>	<code>int r[3][4];</code>
$\begin{bmatrix} 0.5 & 2.7 \\ 3.1 & 0.1 \end{bmatrix}$	$\begin{bmatrix} 5 & 10 & -2 & 4 \\ 0 & 2 & 4 & 8 \\ 21 & 2 & 1 & 42 \end{bmatrix}$

**Note:** `q[0][1]==2.7`   `r[1][3]==8`   `q[1]=={3.1, 0.1}`

Multi-dimensional arrays can also be initialised:

```
float q[][] = {
    { 0.5, 2.7 },
    { 3.1, 0.1 }
};
```

---

## Sidetrack: Defining New Data Types

70/100

C allows us to define new data type (names) via `typedef`:

```
typedef ExistingDataType NewTypeName;
```

Examples:

```
typedef float Temperature;
```

```
typedef int Matrix[20][20];
```

---

## ... Sidetrack: Defining New Data Types

71/100

Reasons to use `typedef`:

- give meaningful names to value types (documentation)
  - is a given number Temperature, Dollars, Volts, ...?
- allow for easy changes to underlying type

```
typedef float Real;
Real complex_calculation(Real a, Real b) {
    Real c = log(a+b); ... return c;
}
```

- "package up" complex type definitions for easy re-use
  - many examples to follow; `Matrix` is a simple example

---

## Structures

72/100

A *structure*

- is a collection of variables, perhaps of different types, grouped together under a single name

- helps to organise complicated data into manageable entities
- exposes the connection between data within an entity
- is defined using the `struct` keyword

Example:

```
typedef struct {
    char name[30];
    int zID;
} StudentT;
```

---

## ... Structures

73/100

One structure can be *nested* inside another:

```
typedef struct {
    int day, month;
} DateT;

typedef struct {
    int hour, minute;
} TimeT;

typedef struct {
    char plate[7]; // e.g. "DSA42X"
    double speed;
    DateT d;
    TimeT t;
} TicketT;
```

---

## ... Structures

74/100

Possible memory layout produced for `TicketT` object:

D   S   A   4   2   X   \0	7 bytes + 1 padding
68.4	8 bytes
2   6	8 bytes
20   45	8 bytes

Note: padding is needed to ensure that `plate` lies on an 8-byte block.

Don't normally care about internal layout, since fields are accessed by name.

---

## ... Structures

75/100

Defining a structured data type itself does not allocate any memory

We need to declare a variable in order to allocate memory

```
DateT christmas;
```

The components of the structure can be accessed using the "dot" operator

```
christmas.day    = 25;
christmas.month  = 12;
```

---

## ... Structures

76/100

With the above TicketT type, we declare and use variables as ...

```
#define NUM_TICKETS 1500

typedef struct {...} TicketT;

TicketT tickets[NUM_TICKETS]; // array of structs

// Print all speeding tickets in a readable format
for (i = 0; i < NUM_TICKETS; i++) {
    printf("%s %6.2f %d/%d at %d:%d\n", tickets[i].plate,
        tickets[i].speed,
        tickets[i].d.day,
        tickets[i].d.month,
        tickets[i].t.hour,
        tickets[i].t.minute);
}

// Sample output:
//
// DSA42X  68.40 2/6 at 20:45
```

---

## ... Structures

77/100

A structure can be passed as a parameter to a function:

```
void print_date(DateT d) {
    printf("%d/%d\n", d.day, d.month);
}

int is_winter(DateT d) {
    return ( (d.month >= 6) && (d.month <= 8) );
}
```

---

# Data Abstraction

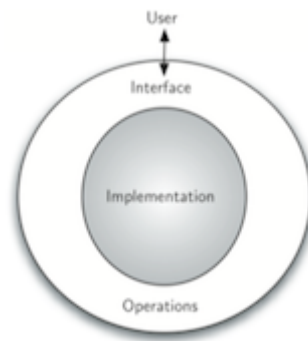
## Abstraction

79/100

An *abstract data structure* ...



- is a logical description of how we view the data and operations
- without regard to how they will be implemented
- creates an *encapsulation* around the data
- is a form of *information hiding*




---

## ... Abstraction

80/100

Users of an abstract data structure see only the *interface*

Builders of the abstract data structure provide an *implementation*

*Interface* provides

- a user-view of the data structure
- function signatures (prototypes) for all operations
- semantics of operations (via documentation)

*Implementation* gives

- concrete definition of the data structures
- function implementations for all operations

---

## ... Abstraction

81/100

Interfaces are *opaque*

- clients *cannot* see the implementation via the interface

Abstraction is important because ...

- it facilitates decomposition of complex programs
- makes implementation changes invisible to clients
- improves readability and structuring of software
- allows for reuse of modules in other systems

---

## Example: A Stack as an Abstract Data Object (ADO)

82/100

Stack, aka *pushdown stack* or *LIFO data structure* (last in, first out)

Assume (for the time being) a stack of `char` values

Operations:

- *create* empty stack
- insert (*push*) an item onto stack
- remove (*pop*) most recently pushed item
- check whether stack *is empty*

Applications:

- undo sequence in a text editor
- bracket matching algorithm
- ...

---

## ... Example: A Stack as an Abstract Data Object (ADO)

83/100

Example of use:

Stack	Operation	Return value
?	create	-
-	isempty	true
-	push a	-
a	push b	-
a b	push c	-
a b c	pop	c
a b	isempty	false

---

## Stack vs Queue

84/100

Queue, aka *FIFO data structure* (first in, first out)

Insert and delete are called *enqueue* and *dequeue*

Applications:

- the checkout at a supermarket
- objects flowing through a pipe (where they cannot overtake each other)
- chat messages
- printing jobs arriving at a printer
- ...

---

## Exercise #7: Stack vs Queue

85/100

Consider the previous example but with a queue instead of a stack.

Which element would have been taken out ("dequeued") first?

---

a

---

## Stack as ADO

87/100

**Interface** (a file named `Stack.h`)

`// Stack ADO header file`

```
#define MAXITEMS 10
```

```
void StackInit();      // set up empty stack
int  StackIsEmpty();   // check whether stack is empty
void StackPush(char);  // insert char on top of stack
char StackPop();       // remove char from top of stack
```

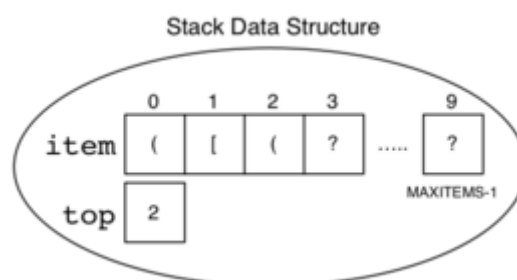
Note:

- no explicit reference to Stack object
  - this makes it an *Abstract Data Object* (ADO)
  - gives you *one* stack to work with
- 

## ... Stack as ADO

88/100

Implementation may use the following data structure:



```
typedef struct {
    char item[MAXITEMS];
    int top;
} stackRep;
```

---

## ... Stack as ADO

89/100

**Implementation** (a file named `Stack.c`):

```
#include "Stack.h"
#include <assert.h>
```

```
// define the Data Structure
typedef struct {                      // insert char on top of stack
```

```

char item[MAXITEMS];
int top;
} stackRep;

// define the Data Object
static stackRep stackObject;

// set up empty stack
void StackInit() {
    stackObject.top = -1;
}

// check whether stack is empty
int StackIsEmpty() {
    return (stackObject.top < 0);
}

void StackPush(char ch) {
    assert(stackObject.top < MAXITEMS-1);
    stackObject.top++;
    int i = stackObject.top;
    stackObject.item[i] = ch;
}

// remove char from top of stack
char StackPop() {
    assert(stackObject.top > -1);
    int i = stackObject.top;
    char ch = stackObject.item[i];
    stackObject.top--;
    return ch;
}

```

- `assert(test)` terminates program with error message if *test* fails
- `static` Type Var declares Var as *local* to Stack.c

## Exercise #8: Bracket Matching

90/100

Bracket matching ... check whether all opening brackets such as '(', '[', '{' have matching closing brackets ')', ']', '}'

Which of the following expressions are balanced?

1.  $(a+b) * c$
2.  $a[i]+b[j]*c[k])$
3.  $(a[i]+b[j])*c[k]$
4.  $a(a+b)*c$
5. `void f(char a[], int n) {int i; for(i=0;i<n;i++) { a[i] = (a[i]*a[i])*(i+1); }}`
6.  $a(a+b * c$

1. **balanced**
2. **not balanced** (case 1: an opening bracket is missing)
3. **balanced**
4. **not balanced** (case 2: closing bracket doesn't match opening bracket)
5. **balanced**
6. **not balanced** (case 3: missing closing bracket)

## ... Stack as ADO

92/100

Bracket matching algorithm, to be implemented as a *client* for **Stack ADO**:

```

bracketMatching(s):
|   Input  stream s of characters
|   Output true if parentheses in s balanced, false otherwise
|
|   for each ch in s do
|       if ch = open bracket then
|           push ch onto stack
|       else if ch = closing bracket then
|           if stack is empty then
|               return false
|               // opening bracket missing (case 1)

```

```

else
    pop top of stack
    if brackets do not match then
        return false // wrong closing bracket (case 2)
    end if
end if
end if
end for
if stack is not empty then return false // some brackets unmatched (case 3)
else return true

```

### ... Stack as ADO

93/100

Execution trace of client on sample input:

( [ { } ] )

Next char	Stack	Check
-	empty	-
(	(	-
[	( [	-
{	( [ {	-
}	( [	{ vs } ✓
]	(	[ vs ] ✓
)	empty	( vs ) ✓
eof	empty	-

### Exercise #9: Bracket Matching Algorithm

94/100

Trace the algorithm on the input

```

void f(char a[], int n) {
    int i;
    for(i=0;i<n;i++) { a[i] = a[i]*a[i] }*(i+1); }
}

```

Next bracket	Stack	Check
start	empty	-
(	(	-
[	( [	-
]	(	✓
)	empty	✓
{	{	-

(	{ (	-
)	{	✓
{	{{	-
[	{{[	-
]	{{	✓
[	{{[	-
]	{{	✓
[	{{[	-
]	{{	✓
)	{	false

## Exercise #10: Implement Bracket Matching Algorithm in C

96/100

- Use Stack ADO

```
#include "Stack.h"
```

- *Sidetrack: Character I/O Functions in C* (requires `<stdio.h>`)

```
int getchar(void);
```

- returns character read from standard input as an `int`, or returns `EOF` on end of file (keyboard: CTRL-D on Unix, CTRL-Z on Windows)

```
int putchar(int ch);
```

- writes the character `ch` to standard output
- returns the character written, or `EOF` on error

## Managing Abstract Data Structures in C

## Compilers

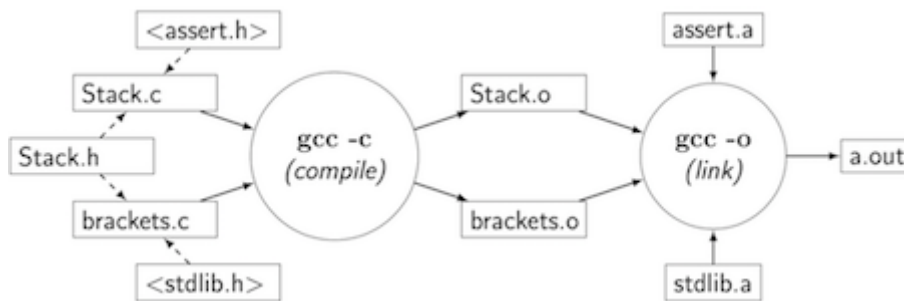
98/100

*Compilers* are programs that

- convert program source code to executable form
- "executable" might be machine code or bytecode

The Gnu C compiler (`gcc`)

- applies source-to-source transformation (pre-processor)
- compiles *source code* to produce *object files*
- links object files and *libraries* to produce *executables*



---

## ... Compilers

99/100

### Compilation/linking with `gcc`

`gcc -c Stack.c`  
produces `Stack.o`, from `Stack.c` (and `Stack.h`)

`gcc -c brackets.c`  
produces `brackets.o`, from `brackets.c` (and `Stack.h`)

`gcc -o prog brackets.o Stack.o`  
links `brackets.o`, `Stack.o` and libraries  
producing executable program called `prog`

**Note** `stdio`, `assert` are included implicitly.

`gcc` is a multi-purpose tool

- compiles (`-c`), links, makes executables (`-o`)

---

## Summary

100/100

- Introduction to Algorithms and Data Structures
- C programming language, compiling with `gcc`
  - Basic data types (`char`, `int`, `float`)
  - Basic programming constructs (`if ... else` conditionals, `while` loops, `for` loops)
  - Basic data structures (atomic data types, arrays, structures)
- Introduction to Abstract Data Structures
  - Compilation
- Suggested reading (Moffat):
  - introduction to C ... Ch. 1; Ch. 2.1-2.3, 2.5-2.6;
  - conditionals and loops ... Ch. 3.1-3.3; Ch. 4.1-4.4
  - arrays ... Ch. 7.1, 7.5-7.6
  - structures ... Ch. 8.1
- Suggested reading (Sedgewick):
  - introduction to ADTs ... Ch. 4.1-4.3
- Coming up ...
  - Principles of algorithm analysis ([S] 2.1-2.4, 2.6)

