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Some useful things

```
import java.util.*;
import java.io.*;
public class Template {
| FastScanner in;
| PrintWriter out;
| public void solve() throws IOException {
 int n = in.nextInt();
 out.println(n);
| }
| public void run() {
| | try {
| | in = new FastScanner();
| | out = new PrintWriter(System.out);
| | out.close();
| | } catch (IOException e) {
| | e.printStackTrace();
| | }
| }
| class FastScanner {
| BufferedReader br;
| StringTokenizer st;
| | FastScanner() {
| | br = new BufferedReader(new
      | | }
| | String next() {
| | | while (st == null || !st.hasMoreTokens()) {
| | | try {

    StringTokenizer(br.readLine());
| | | | } catch (IOException e) {
| | | | e.printStackTrace();
| | | | }
| | | }
| | return st.nextToken();
| | int nextInt() {
| | return Integer.parseInt(next());
| }
| public static void main(String[] arg) {
| new Template().run();
| }
}
#include <algorithm>
#include <cstdio>
```

```
asm(
```

```
/** Interface */
inline int readInt();
inline int readUInt();
inline bool isEof();
/** Read */
static const int buf_size = 100000;
static char buf[buf_size];
static int buf_len = 0, pos = 0;
inline bool isEof() {
  if (pos == buf_len) {
   pos = 0, buf_len = fread(buf, 1, buf_size,

    stdin);
   if (pos == buf_len)
      return 1;
 }
  return 0;
}
inline int getChar() { return isEof() ? -1 :
→ buf[pos++]; }
inline int readChar() {
 int c = getChar();
 while (c !=-1 \&\& c <= 32)
    c = getChar();
  return c;
inline int readUInt() {
 int c = readChar(), x = 0;
 while ('0' <= c && c <= '9')
    x = x * 10 + c - '0', c = getChar();
  return x;
inline int readInt() {
 int s = 1, c = readChar();
  int x = 0;
  if (c == '-')
   s = -1, c = getChar();
  while ('0' <= c && c <= '9')
    x = x * 10 + c - '0', c = getChar();
 return s == 1 ? x : -x;
}
// 10M int [0..1e9)
// cin 3.02
// scanf 1.2
// cin sync_with_stdio(false) 0.71
// fastRead getchar 0.53
// fastRead fread 0.15
inline void fasterLLDivMod(ull x, uint y, uint
```

```
| uint xh = (uint)(x \Rightarrow 32), xl = (uint)x, d, m;
#ifdef __GNUC__
```

```
| | : "=a" (d), "=d" (m)
| | : "d" (xh), "a" (xl), "r" (y)
| );
#else
| __asm {
  mov edx, dword ptr[xh];
| | mov eax, dword ptr[x1];
| | div dword ptr[y];
| | mov dword ptr[d], eax;
| | mov dword ptr[m], edx;
| };
#endif
out_d = d; out_m = m;
// have no idea what sse flags are really cool;
\rightarrow list of some of them
// -- very good with bitsets
#pragma GCC optimize("03")
#pragma GCC target(|
   "sse,sse2,sse3,ssse3,sse4,popcnt,abm,mmx")
```

```
#include <ext/pb_ds/assoc_container.hpp>
using namespace __gnu_pbds;
template <typename T> using ordered_set = tree<T,</pre>
\hookrightarrow null_type, less<T>, rb_tree_tag,

→ tree_order_statistics_node_update>;

template <typename K, typename V> using
→ ordered_map = tree<K, V, less<K>,

→ rb_tree_tag,

    tree_order_statistics_node_update>;

// HOW TO USE ::
// -- order_of_key(10) returns the number of
\rightarrow elements in set/map strictly less than 10
// -- *find_by_order(10) returns 10-th smallest

→ element in set/map (0-based)

bitset<N> a;
for (int i = a._Find_first(); i != a.size(); i =
→ a._Find_next(i)) {
| cout << i << endl;
}
```

2 Data structures

2.1 Hash table

```
| | | | i = 0;
| return i;
| }
| Data & operator[] (HashType H) {
| | assert(H != 0);
| int i = position(H);
| | if (!hash[i]) {
| | | hash[i] = H;
| | f[i] = default_value;
| | }
| return f[i];
| }
};
hashTable<13, int, int, 0> h;
```

3 Geometry

3.1 Common tangents of two circles

```
vector<Line> commonTangents(pt A, dbl rA, pt B,
\rightarrow dbl rB) {
vector<Line> res;
| pt C = B - A;
| dbl z = C.len2();
| for (int i = -1; i \le 1; i += 2) {
| | for (int j = -1; j \le 1; j += 2) {
| | dbl r = rB * j - rA * i;
 | dbl d = z - r * r;
 | | if (ls(d, 0))
 | | continue;
| \ | \ | \ d = sqrt(max(0.01, d));
| | | pt magic = pt(r, d) / z;
| | pt v(magic % C, magic * C);
| | dbl CC = (rA * i - v \% A) / v.len2();
| | | pt 0 = v * -CC;
| | }
| }
return res;
}
// HOW TO USE ::
// --
         *D*---
// --
         *...*-
// --
       *...A...*
// --
// --
// --
// --
          *C*----*E*
// -- res = {CE, CF, DE, DF}
```

3.2 Convex hull 3D in $O(n^2)$

```
struct Plane {
| pt 0, v;
vector<int> id;
};
vector<Plane> convexHull3(vector<pt> p) {
vector<Plane> res;
int n = p.size();
| for (int i = 0; i < n; i++)
| for (int i = 0; i < 4; i++) {
| vector<pt> tmp;
| | for (int j = 0; j < 4; j++)
| | if (i != j)
| res.pb(\{tmp[0],
\rightarrow tmp[0]),
| | | | | {tmp[0].id, tmp[1].id, tmp[2].id}});
| if ((p[i] - res.back().0) % res.back().v > 0)
| | res.back().v = res.back().v * -1;
| | | swap(res.back().id[0], res.back().id[1]);
   }
| }
vector<vector<int>> use(n, vector<int>(n, 0));
| int tmr = 0;
| for (int i = 4; i < n; i++) {
| | int cur = 0;
 | tmr++;
| vector<pair<int, int>> curEdge;
| | for (int j = 0; j < sz(res); j++) {
| | | | if ((p[i] - res[j].0) % res[j].v > 0) {
| \ | \ | \ |  for (int t = 0; t < 3; t++) {
| | | | int v = res[j].id[t];
| \ | \ | \ | \ |  int u = res[j].id[(t + 1) % 3];
 | | | }
| | | }
| | }
| res.resize(cur);
| | for (auto x : curEdge) {
| | | if (use[x.S][x.F] == tmr)
| | | continue;
| \ | \ | \ res.pb({p[i], (p[x.F] - p[i]) * (p[x.S] - p[i])} | | 
      \rightarrow p[i]), {x.F, x.S, i}});
| }
return res;
}
// plane in 3d
// (A, v) * (B, u) -> (0, n)
pt n = v * u;
pt m = v * n;
double t = (B - A) \% u / (u \% m);
```

```
pt 0 = A - m * t;
```

3.3 Dynamic convex hull trick

```
const ll is_query = -(1LL << 62);</pre>
struct Line {
| 11 m, b;
mutable function<const Line *()> succ;
| bool operator<(const Line &rhs) const {
| | if (rhs.b != is_query)
| | return m < rhs.m;
| const Line *s = succ();
| | if (!s)
| 11 x = rhs.m;
 | return b - s -> b < (s -> m - m) * x;
| }
};
struct HullDynamic : public multiset<Line> {
bool bad(iterator y) {
 | auto z = next(y);
 | if (y == begin()) {
| | | if (z == end())
| | return y->m == z->m && y->b <= z->b;
| | }
\mid auto x = prev(y);
| if (z == end())
| | return y->m == x->m && y->b <= x->b;
| | return (x->b - y->b) * (z->m - y->m) >= (y->b)
    \rightarrow - z->b) * (y->m - x->m);
| }
void insert_line(ll m, ll b) {
| | auto y = insert(\{m, b\});
| y > succ = [=] \{ return next(y) == end() ? 0 :
    \rightarrow &*next(y); };
| | if (bad(y)) {
| | return;
| | }
| | while (next(y) != end() && bad(next(y)))
| | | erase(next(y));
 | while (y != begin() && bad(prev(y)))
 | | erase(prev(y));
| }
\mid ll eval(ll x) {
| | auto 1 = *lower_bound((Line){x, is_query});
| return l.m * x + l.b;
| }
};
```

3.4 Minimal covering disk

```
pair<pt, dbl> minDisc(vector<pt> p) {
   int n = p.size();
```

```
| pt 0 = pt(0, 0);
| dbl R = 0;
random_shuffle(all(p));
| for (int i = 0; i < n; i++) {
 if (ls(R, (0 - p[i]).len())) {
 | | 0 = p[i];
| \quad | \quad | \quad R = 0;
| | | for (int j = 0; j < i; j++) {
| \ | \ | \ | \ |  if (ls(R, (0 - p[j]).len()))  {
| | | | | | 0 = (p[i] + p[j]) / 2;
| | | | R = (p[i] - p[j]).len() / 2;
    | | | for (int k = 0; k < j; k++) {
          | if (ls(R, (0 - p[k]).len())) {
        | | Line 11((p[i] + p[j]) / 2,
          | | | | | | | (p[i] + p[j]) / 2 + (p[i] -
                        → p[j]).rotate());
        | | | Line 12((p[k] + p[j]) / 2,
      | | | | | | | | | | (p[k] + p[j]) / 2 + (p[k] -
                        → p[j]).rotate());
      | \ | \ | \ | \ 0 = 11 * 12;
    | | | | | | R = (p[i] - 0).len();
| | | | | }
| | | | | }
| | | }
| | | }
| | }
| }
| return {0, R};
```

3.5 Draw svg pictures

```
struct SVG {
| FILE *out;
| double sc = 50;
void open() {
| | out = fopen("image.svg", "w");
| | fprintf(out, "<svg

→ xmlns='http://www.w3.org/2000/svg'

       viewBox='-1000 -1000 2000 2000'>\n");
| }
void line(point a, point b) {
| | a = a * sc, b = b * sc;
| | fprintf(out, "<line x1='%f' y1='%f' x2='%f'
    \rightarrow y2='%f' stroke='black'/>\n", a.x, -a.y,
       b.x, -b.y);
| }
| void circle(point a, double r = -1, string col
  r = sc * (r == -1 ? 0.3 : r);
| a = a * sc;
| | fprintf(out, "<circle cx='%f' cy='%f' r='%f'
    \rightarrow fill='%s'/>\n", a.x, -a.y, r,
       col.c_str());
| }
void text(point a, string s) {
| a = a * sc;
| | fprintf(out, "<text x='%f' y='%f'
    \rightarrow font-size='100px'>%s</text>\n", a.x,
       -a.y, s.c_str());
| }
```

```
| void close() {
| | fprintf(out, "</svg>\n");
| | fclose(out);
| | out = 0;
| }
| ~SVG() {
| | if (out) {
| | close();
| | }
| }
} svg;
```

4 Graphs

4.1 2-Chinese algorithm

```
namespace twoc {
struct Heap {
| static Heap *null;
| ll x, xadd;
int ver, h;
#ifdef ANS
int ei;
#endif
| Heap *1, *r;
| Heap(ll xx, int vv) : x(xx), xadd(0), ver(vv),
  \rightarrow h(1), l(null), r(null) {}
| Heap(const char *) : x(0), xadd(0), ver(0),
  \rightarrow h(0), l(this), r(this) {}
void add(ll a) {
| x += a;
 \mid xadd += a;
 }
void push() {
| | if (1 != null)
| | if (r != null)
| | r -> add(xadd);
| xadd = 0;
| }
Heap *Heap::null = new Heap("wqeqw");
Heap *merge(Heap *1, Heap *r) {
| if (1 == Heap::null)
return r;
| if (r == Heap::null)
 return 1;
| 1->push();
| r->push();
| if (1->x > r->x)
| | swap(1, r);
| 1->r = merge(1->r, r);
| if (1->1->h < 1->r->h)
| | swap(1->1, 1->r);
| 1->h = 1->r->h + 1;
 return 1;
}
Heap *pop(Heap *h) {
| h->push();
 return merge(h->1, h->r);
}
```

```
const int N = 666666;
struct DSU {
int p[N];
void init(int nn) { iota(p, p + nn, 0); }
| int get(int x) \{ return p[x] == x ? x : p[x] =
  \rightarrow get(p[x]); }
void merge(int x, int y) { p[get(y)] = get(x);
  → }
} dsu;
Heap *eb[N];
int n;
#ifdef ANS
struct Edge {
int x, y;
| 11 c;
};
vector<Edge> edges;
int answer[N];
#endif
void init(int nn) {
| n = nn;
dsu.init(n);
| fill(eb, eb + n, Heap::null);
| edges.clear();
}
void addEdge(int x, int y, ll c) {
| Heap *h = new Heap(c, x);
#ifdef ANS
| h->ei = sz(edges);
| edges.push_back({x, y, c});
#endif
| eb[y] = merge(eb[y], h);
}
11 solve(int root = 0) {
| 11 ans = 0;
| static int done[N], pv[N];
| memset(done, 0, sizeof(int) * n);
| done[root] = 1;
| int tt = 1;
#ifdef ANS
| int cnum = 0;
| static vector<ipair> eout[N];
| for (int i = 0; i < n; ++i)
| | eout[i].clear();
#endif
| for (int i = 0; i < n; ++i) {
| int v = dsu.get(i);
| | if (done[v])
| | continue;
| ++tt:
| | while (true) {
| | |  int nv = -1;
| | while (eb[v] != Heap::null) {
| \ | \ | \ |  if (nv == v)  {
| | | | eb[v] = pop(eb[v]);
| | | | continue;
| | | | }
| | | break;
| | | }
| | | if (nv == -1)
```

```
| | | return LINF;
\mid \cdot \mid \cdot \mid ans += eb[v]->x;
| | | eb[v] -> add(-eb[v] -> x);
#ifdef ANS
| | eout[edges[ei].x].push_back({++cnum, ei});
#endif
| | | | pv[v] = nv;
| | | v = nv;
| | | continue;
| | | }
| | break;
\mid \ \mid \ \mid while (v1 != v) {
| | | | eb[v] = merge(eb[v], eb[v1]);
| | | }
   }
| }
#ifdef ANS
| memset(answer, -1, sizeof(int) * n);
answer[root] = 0;
set<ipair> es(all(eout[root]));
| while (!es.empty()) {
| | auto it = es.begin();
 int ei = it->second;
| | es.erase(it);
| int nv = edges[ei].y;
\mid if (answer[nv] != -1)
| | continue;
| | answer[nv] = ei;
es.insert(all(eout[nv]));
| }
\mid answer[root] = -1;
#endif
return ans;
}
/* Usage: twoc::init(vertex_count);
        twoc::addEdge(v1, v2, cost);
         twoc::solve(root); - returns cost or
  LINF
 * twoc::answer contains index of ingoing edge
   for each vertex
 */
} // namespace twoc
```

4.2 Dominator tree

```
namespace domtree {
  const int K = 18;
  const int N = 1 << K;

int n, root;
  vector<int> e[N], g[N];
  int sdom[N], dom[N];
  int p[N][K], h[N], pr[N];
  int in[N], out[N], tmr, rev[N];
```

```
void init(int _n, int _root) {
| n = _n;
root = root;
| tmr = 0;
| for (int i = 0; i < n; i++) {
| | g[i].clear();
| in[i] = -1;
| }
}
void addEdge(int u, int v) {
| e[u].push_back(v);
| g[v].push_back(u);
void dfs(int v) {
| in[v] = tmr++;
| for (int to : e[v]) {
| | if (in[to] != -1)
| | continue;
| | pr[to] = v;
| | dfs(to);
| }
| out[v] = tmr - 1;
}
int lca(int u, int v) {
| if (h[u] < h[v])
\mid \mid swap(u, v);
| for (int i = 0; i < K; i++)
| | if ((h[u] - h[v]) & (1 << i))
| | | u = p[u][i];
| if (u == v)
| return u;
| for (int i = K - 1; i >= 0; i--) {
| | if (p[u][i] != p[v][i]) {
| | | u = p[u][i];
| | | v = p[v][i];
| | }
| }
| return p[u][0];
}
void solve(int _n, int _root, vector<pair<int,</pre>
\hookrightarrow int>> _edges) {
init(_n, _root);
| for (auto ed : _edges)
| | addEdge(ed.first, ed.second);
| dfs(root);
| for (int i = 0; i < n; i++)
| | if (in[i] != -1)
segtree tr(tmr); // a[i] := min(a[i], x) and
  \rightarrow return a[i]
| for (int i = tmr - 1; i >= 0; i--) {
| | <u>int</u> v = rev[i];
| | int cur = i;
| | for (int to : g[v]) {
| | | if (in[to] == -1)
| | | continue;
```

```
| | else
| | }
 | sdom[v] = rev[cur];
| tr.upd(in[v], out[v], in[sdom[v]]);
| }
| for (int i = 0; i < tmr; i++) {
| | int v = rev[i];
| | if (i == 0) {
| | dom[v] = v;
| | h[v] = 0;
| | | h[v] = h[dom[v]] + 1;
| | }
| | p[v][0] = dom[v];
| | for (int j = 1; j < K; j++)
| | | p[v][j] = p[p[v][j - 1]][j - 1];
| }
| for (int i = 0; i < n; i++)
\mid if (in[i] == -1)
| \quad | \quad | \quad dom[i] = -1;
} // namespace domtree
```

4.3 General matching

```
// COPYPASTED FROM E-MAXX
namespace general_matching {
const int MAXN = 256;
int n;
vector<int> g[MAXN];
int match[MAXN], p[MAXN], base[MAXN], q[MAXN];
bool used[MAXN], blossom[MAXN];
int lca(int a, int b) {
bool used[MAXN] = {0};
| for (;;) {
| | a = base[a];
| | used[a] = true;
| | if (match[a] == -1)
| | break;
| | a = p[match[a]];
| }
| for (;;) {
 | b = base[b];
| | if (used[b])
| | return b;
| | b = p[match[b]];
| }
void mark_path(int v, int b, int children) {
| while (base[v] != b) {
| | blossom[base[v]] = blossom[base[match[v]]] =

    true;

| | p[v] = children;
| | children = match[v];
| v = p[match[v]];
```

```
| }
}
int find_path(int root) {
| memset(used, 0, sizeof used);
| memset(p, -1, sizeof p);
| for (int i = 0; i < n; ++i)
used[root] = true;
| int qh = 0, qt = 0;
| q[qt++] = root;
| while (qh < qt) {
| int v = q[qh++];
| | for (size_t i = 0; i < g[v].size(); ++i) {
| | | if (base[v] == base[to] || match[v] == to)
| | | continue;
| | | if (to == root || (match[to] != -1 &&
     \rightarrow p[match[to]] != -1)) {
| | | int curbase = lca(v, to);
| | | memset(blossom, 0, sizeof blossom);
| | | mark_path(v, curbase, to);
| | | mark_path(to, curbase, v);
| \ | \ | \ |  for (int i = 0; i < n; ++i)
| | | base[i] = curbase;
   | | | | if (!used[i]) {
   | | | | | | q[qt++] = i;
   | | | | }
   | | | }
 | \ | \ | \  else if (p[to] == -1) {
| | | | p[to] = v;
| | | if (match[to] == -1)
   | | return to;
   | | | | q[qt++] = to;
| | | }
| | }
| }
return -1;
vector<pair<int, int>> solve(int _n,

    vector<pair<int, int>> edges) {

| n = _n;
| for (int i = 0; i < n; i++)
| | g[i].clear();
| for (auto o : edges) {
| | g[o.first].push_back(o.second);
 g[o.second].push_back(o.first);
| memset(match, -1, sizeof match);
| for (int i = 0; i < n; ++i) {
\mid if (match[i] == -1) {
| | int v = find_path(i);
| \ | \ | while (v != -1) {
| | | match[v] = pv, match[pv] = v;
| | | v = ppv;
```

```
| | | | }
| | | }
| vector<pair<int, int>> ans;
| for (int i = 0; i < n; i++) {
| | if (match[i] > i) {
| | | ans.push_back(make_pair(i, match[i]));
| | }
| return ans;
}
} // namespace general_matching
```

4.4 Gomory-Hu tree

```
// graph has n nodes
// reset() clears all flows in graph
// dinic(s, t) pushes max flow from s to t
// dist[v] is distance from s to v in residual
\hookrightarrow network
vector<vector<long long>> prec;
void buildTree() {
  vector<int> p(n, 0);
  prec = vector<vector<long long>>(n, vector<long</pre>
  → long>(n, inff));
 for (int i = 1; i < n; i++) {
    reset();
    long long f = dinic(i, p[i]);
    for (int j = 0; j < n; j++) {
      if (j != i && dist[j] < inff && p[j] ==</pre>
      → p[i]) {
        p[j] = i;
    }
    prec[p[i]][i] = prec[i][p[i]] = f;
    for (int j = 0; j < i; j++) {
      prec[i][j] = prec[j][i] =

→ min(prec[j][p[i]], f);
    }
      int j = p[i];
      if (dist[p[j]] < inff) {</pre>
        p[i] = p[j];
        p[j] = i;
  }
long long fastFlow(int S, int T) {
| return prec[S][T];
}
```

4.5 Hungarian algorithm

```
namespace hungary {
const int N = 210;
int a[N][N];
```

```
int ans[N];
int calc(int n, int m) {
++n, ++m;
vector<int> u(n), v(m), p(m), prev(m);
| for (int i = 1; i < n; ++i) {
| | p[0] = i;
| int x = 0;
vector<int> mn(m, INF);
| vector<int> was(m, 0);
\mid \mid while (p[x]) {
| | | was[x] = 1;
| | |  int ii = p[x], dd = INF, y = 0;
| | | for (int j = 1; j < m; ++j)
| | | | | int cur = a[ii][j] - u[ii] - v[j];
| | | | | mn[j] = cur, prev[j] = x;
| | | | | if (mn[j] < dd)
| \ | \ | \ | \ | \ | \ dd = mn[j], y = j;
| | | }
| | | for (int j = 0; j < m; ++j) {
| | | | | u[p[j]] += dd, v[j] -= dd;
| | | }
| | x = y;
| | }
\mid \cdot \mid while (x) {
| | p[x] = p[y];
| | x = y;
| | }
| }
| for (int j = 1; j < m; ++j) {
   ans[p[j]] = j;
| }
return -v[0];
}
// How to use:
//* Set values to a[1..n][1..m] (n <= m)
// * Run calc(n, m) to find minimum
//* Optimal\ edges\ are\ (i,\ ans[i])\ for\ i=1..n
// * Everything works on negative numbers
// !!! I don't understand this code, it's
\hookrightarrow copypasted from e-maxx
} // namespace hungary
```

4.6 Link-Cut Tree

```
#include <cassert>
#include <cstdio>
#include <iostream>
using namespace std;
// BEGIN ALGO
const int MAXN = 110000;
```

```
typedef struct _node {
_node *1, *r, *p, *pp;
int size;
| bool rev;
_node();
| explicit _node(nullptr_t) {
| | 1 = r = p = pp = this;
| size = rev = 0;
| }
void push() {
| | if (rev) {
 | | 1->rev ^= 1;
 | | r->rev ^= 1;
| | rev = 0;
| | }
| }
void update();
} * node;
node None = new _node(nullptr);
node v2n[MAXN];
_node::_node() {
| 1 = r = p = pp = None;
\mid size = 1;
| rev = false;
}
void _node::update() {
| size = (this != None) + l->size + r->size;
| 1->p = r->p = this;
void rotate(node v) {
| assert(v != None && v->p != None);
assert(!v->rev);
assert(!v->p->rev);
| node u = v -> p;
| if (v == u -> 1)
| u->1 = v->r, v->r = u;
else
| u->r = v->1, v->1 = u;
| swap(u->p, v->p);
\mid swap(v->pp, u->pp);
| if (v->p != None) {
 | assert(v->p->1 == u || v->p->r == u);
| if (v->p->r == u)
| | v->p->r = v;
| | else
| | v - p - 1 = v;
| }
u->update();
v->update();
void bigRotate(node v) {
assert(v->p != None);
v->p->p->push();
v->p->push();
v->push();
\mid if (v->p->p != None) {
 if ((v->p->1 == v) ^ (v->p->p->r == v->p))
| | else
```

```
| }
| rotate(v);
}
inline void Splay(node v) {
| while (v->p != None)
  | bigRotate(v);
inline void splitAfter(node v) {
| v->push();
| Splay(v);
| v->r->p = None;
| v->r->pp = v;
v->r = None;
v->update();
}
void expose(int x) {
\mid node v = v2n[x];
| splitAfter(v);
| while (v->pp != None) {
| assert(v->p == None);
| | splitAfter(v->pp);
| assert(v->pp->r == None);
| | assert(v->pp->p == None);
| assert(!v->pp->rev);
| v-pp-r = v;
v->pp->update();
| v = v - pp;
| v->r->pp = None;
| }
assert(v->p == None);
\mid Splay(v2n[x]);
}
inline void makeRoot(int x) {
expose(x);
assert(v2n[x]->p == None);
assert(v2n[x]->pp == None);
assert(v2n[x]->r == None);
 v2n[x]->rev ^= 1;
}
inline void link(int x, int y) {
makeRoot(x);
| v2n[x]-pp = v2n[y];
}
inline void cut(int x, int y) {
expose(x);
| Splay(v2n[y]);
| if (v2n[y]->pp != v2n[x]) {
\mid \mid swap(x, y);
expose(x);
| | Splay(v2n[y]);
\mid assert(v2n[y]->pp == v2n[x]);
| }
| v2n[y]->pp = None;
}
inline int get(int x, int y) {
\mid if (x == y)
| return 0;
makeRoot(x);
| expose(y);
| expose(x);
| Splay(v2n[y]);
| if (v2n[y]->pp != v2n[x])
```

```
| return -1;
| return v2n[y]->size;
}
// END ALGO
_node mem[MAXN];
int main() {
| freopen("linkcut.in", "r", stdin);
| freopen("linkcut.out", "w", stdout);
int n, m;
| scanf("%d %d", &n, &m);
| for (int i = 0; i < n; i++)
| v2n[i] = \&mem[i];
| for (int i = 0; i < m; i++) {
| | int a, b;
 | if (scanf(" link %d %d", &a, &b) == 2)
| | | link(a - 1, b - 1);
| | else if (scanf(" cut %d %d", &a, &b) == 2)
| | cut(a - 1, b - 1);
| | else if (scanf(" get %d %d", &a, &b) == 2)
| \cdot | printf("%d\n", get(a - 1, b - 1));
| | else
| | assert(false);
| }
 return 0;
```

4.7 Smith algorithm (Game on cyclic graph)

```
const int N = 1e5 + 10;
struct graph {
int n;
| vi v[N];
vi vrev[N];
void read() {
| | int m;
| | scanf("%d%d", &n, &m);
| | forn(i, m) {
| scanf("%d%d", &x, &y);
| | v[x].pb(y);
| | }
| }
int deg[N], cnt[N], used[N], f[N];
int q[N], st, en;
set<int> s[N];
void calc() {
| | for (int x = 0; x < n; ++x)
```

```
| | | f[x] = -1, cnt[x] = 0;
| | int val = 0;
| | while (1) {
| | st = en = 0;
| | | for (int x = 0; x < n; ++x) {
| \ | \ | \ | \ deg[x] = 0;
| | | | used[x] = 0;
| \ | \ | \ | \ |  if (f[y] == -1)
| | | | deg[x]++;
| | | }
| | for (int x = 0; x < n; ++x)
\hookrightarrow val) {
| | | | | q[en++] = x;
| | | | | f[x] = val;
| | | | }
| | if (!en)
| | break;
| | | |  int x = q[st];
| | | st++;
| | | | for (int y : vrev[x]) {
| \ | \ | \ | \ |  if (used[y] == 0 && f[y] == -1) {
| \ | \ | \ | \ | \ | \ used[y] = 1;
| | | | cnt[y]++;
   | | | | deg[z]--;
   \hookrightarrow cnt[z] == val) {
   | | | | | | | f[z] = val;
| | | | | | | | | q[en++] = z;
| | | | | | | }
| | | | | }
| | | | }
| | | | }
| | | }
| | }
| | for (int x = 0; x < n; ++x)
| | eprintf("%d%c", f[x], " \n"[x + 1 == n]);
| | for (int x = 0; x < n; ++x)
| | | if (f[x] == -1) {
| | | | | |  if (f[y] != -1)
| | | | | | s[x].insert(f[y]);
| | | }
| }
} g1, g2;
string get(int x, int y) {
| int f1 = g1.f[x], f2 = g2.f[y];
| if (f1 == -1 \&\& f2 == -1)
| return "draw";
| if (f1 == -1) {
| | if (g1.s[x].count(f2))
| | | return "first";
| return "draw";
| }
| if (f2 == -1) {
| | if (g2.s[y].count(f1))
| | | return "first";
```

```
| return "draw";
| }
| if (f1 ^ f2)
| return "first";
| return "second";
}
```

4.8 Stoer-Vagner algorithm (Global mincut)

```
const int MAXN = 500;
int n, g[MAXN][MAXN];
int best_cost = 1000000000;
vector<int> best_cut;
void mincut() {
vector<int> v[MAXN];
| for (int i = 0; i < n; ++i)
| | v[i].assign(1, i);
int w[MAXN];
bool exist[MAXN], in_a[MAXN];
memset(exist, true, sizeof exist);
| for (int ph = 0; ph < n - 1; ++ph) {
| | memset(in_a, false, sizeof in_a);
| memset(w, 0, sizeof w);
| | for (int it = 0, prev; it < n - ph; ++it) {
| | |  int sel = -1;
| | for (int i = 0; i < n; ++i)
| | | | if (exist[i] && !in_a[i] && (sel == -1 ||
       \rightarrow w[i] > w[sel]))
| | if (it == n - ph - 1) {
| | | if (w[sel] < best_cost)
| | | | best_cost = w[sel], best_cut = v[sel];
| | | v[prev].insert(v[prev].end(),

¬ v[sel].begin(), v[sel].end());
 | | | for (int i = 0; i < n; ++i)
 | | | | g[prev][i] = g[i][prev] += g[sel][i];
| | | exist[sel] = false;
| \ | \ | \ |  for (int i = 0; i < n; ++i)
| | | }
| | }
| }
}
```

5 Matroids

5.1 Matroids intersection

```
// check(ctaken, 1) -- first matroid
// check(ctaken, 2) -- second matroid
vector<char> taken(m);
while (1) {
    vector<vector<int>>> e(m);
    for (int i = 0; i < m; i++) {</pre>
```

```
| | for (int j = 0; j < m; j++) {
| | | auto ctaken = taken;
| | | }
| | | }
| | auto ctaken = taken;
| | | | ctaken[j] = 0;
| | | | }
| | | }
| | }
| }
vector<int> type(m);
| // 0 -- cant, 1 -- can in \2, 2 -- can in \1
| for (int i = 0; i < m; i++) {
| | if (!taken[i]) {
| | auto ctaken = taken;
| | if (check(ctaken, 2))
| | }
| | if (!taken[i]) {
| | auto ctaken = taken;
| | if (check(ctaken, 1))
| | }
| }
vector<int> w(m);
| for (int i = 0; i < m; i++) {
| | w[i] = taken[i] ? ed[i].c : -ed[i].c;
| }
vector<pair<int, int>> d(m, {INF, 0});
| for (int i = 0; i < m; i++) {
| | if (type[i] & 1)
| \ | \ | \ d[i] = \{w[i], 0\};
| }
vector<int> pr(m, -1);
| while (1) {
| vector<pair<int, int>> nd = d;
| | for (int i = 0; i < m; i++) {
| | | continue;
| | | if (nd[to] > make_pair(d[i].first +
     \rightarrow w[to], d[i].second + 1)) {
\rightarrow d[i].second + 1);
| | | | }
| | | }
| | }
| | if (d == nd)
| | break;
| d = nd;
```

6 Numeric

```
// finds first solution of (p + step * x) % mod <
// returns value of (p + step * x), i.e. number
\rightarrow of steps x = (ans - p) / step (mod mod)
int smart_calc(int mod, int step, int 1, int p) {
| if (p < 1) {
| return p;
| }
| int d = (mod - p + step - 1) / step;
| int np = (p + d * step) % mod;
| if (np < 1) {
| return np;
| }
int res = smart_calc(step, mod % step, 1, 1 +
  \rightarrow step - 1 - np);
| return 1 - 1 - res;
}
```

6.1 Berlekamp-Massey Algorithm

```
vector<int> berlekamp(vector<int> s) {
| int 1 = 0;
vector<int> la(1, 1);
| vector<int> b(1, 1);
| for (int r = 1; r <= (int)s.size(); r++) {
| | int delta = 0;
| | for (int j = 0; j \le 1; j++) {
| \ | \ | \ delta = (delta + 1LL * s[r - 1 - j] *
     \rightarrow la[j]) % MOD;
| | }
| b.insert(b.begin(), 0);
| | if (delta != 0) {
vector<int> t(max(la.size(), b.size()));
| | | for (int i = 0; i < (int)t.size(); i++) {

→ + MOD) % MOD;

| | | }
```

```
| | | if (2 * 1 \le r - 1) {
| | | | b = 1a;
| | | int od = inv(delta);
| | | | for (int &x : b)
| \ | \ | \ | \ | \ x = 1LL * x * od % MOD;
| | | | | 1 = r - 1;
| | | }
| | }
| }
| assert((int)la.size() == 1 + 1);
| assert(1 * 2 + 30 < (int)s.size());
reverse(la.begin(), la.end());
return la;
vector<int> mul(vector<int> a, vector<int> b) {
vector<int> c(a.size() + b.size() - 1);
| for (int i = 0; i < (int)a.size(); i++) {
| | for (int j = 0; j < (int)b.size(); j++) {
| | | c[i + j] = (c[i + j] + 1LL * a[i] * b[j]) %

→ MOD;

| | }
| }
vector<int> res(c.size());
| for (int i = 0; i < (int)res.size(); i++)
| | res[i] = c[i] % MOD;
return res;
}
vector<int> mod(vector<int> a, vector<int> b) {
| if (a.size() < b.size())
| a.resize(b.size() - 1);
int o = inv(b.back());
| for (int i = (int)a.size() - 1; i >=
  | | if (a[i] == 0)
| | continue;
int coef = 1LL * o * (MOD - a[i]) % MOD;
| | for (int j = 0; j < (int)b.size(); j++) {
| | | a[i - (int)b.size() + 1 + j] =
| | | | (a[i - (int)b.size() + 1 + j] + 1LL *
          \rightarrow coef * b[j]) % MOD;
| | }
| }
| while (a.size() >= b.size()) {
| | assert(a.back() == 0);
| a.pop_back();
| }
return a;
vector<int> bin(int n, vector<int> p) {
vector<int> res(1, 1);
vector<int> a(2);
| a[1] = 1;
| while (n) {
| | if (n & 1)
| | a = mod(mul(a, a), p);
| | n >>= 1;
```

```
| }
| return res;
}

int f(vector<int> t, int m) {
| vector<int> v = berlekamp(t);
| vector<int> o = bin(m - 1, v);
| int res = 0;
| for (int i = 0; i < (int)o.size(); i++)
| | res = (res + 1LL * o[i] * t[i]) % MOD;
| return res;
}</pre>
```

6.2 Chinese remainder theorem

6.3 Miller-Rabin primality test

```
// assume p > 1
bool isprime(ll p) {
| const int a[] = \{2, 3, 5, 7, 11, 13, 17, 19,
  \rightarrow 23, 0};
| 11 d = p - 1;
int cnt = 0;
| while (!(d & 1)) {
| | d >>= 1;
| cnt++;
| }
| for (int i = 0; a[i]; i++) {
| | if (p == a[i]) {
| | return true;
| | }
| | if (!(p % a[i])) {
| | return false;
| | }
| }
| for (int i = 0; a[i]; i++) {
| | ll cur = mpow(a[i], d, p); // a[i] \hat{d} (mod
    \rightarrow p
  | if (cur == 1) {
| | continue;
| | }
| | bool good = false;
| | for (int j = 0; j < cnt; j++) {
| | | if (cur == p - 1) {
| | break;
  | | }
| | cur = mult(cur, cur);
| | }
| | if (!good) {
| | | return false;
| | }
| }
 return true;
```

6.4 Multiplication by modulo

```
11 mul(11 a, 11 b, 11 m) { // works for MOD 8e18
| 11 k = (11)((long double)a * b / m);
| 11 r = a * b - m * k;
| if (r < 0)
| | r += m;
| if (r >= m)
| | r -= m;
| return r;
}
```

6.5 Numerical integration

```
function<dbl(dbl, dbl, function<dbl(dbl)>)> f =
\rightarrow [&](dbl L, dbl R, function<dbl(dbl)> g) {
| const int ITERS = 1000000;
| dbl ans = 0;
| dbl step = (R - L) * 1.0 / ITERS;
| for (int it = 0; it < ITERS; it++) {
| | double xl = L + step * it;
| double xr = L + step * (it + 1);
| dbl x1 = (xl + xr) / 2;
| dbl x0 = x1 - (x1 - x1) * sqrt(3.0 / 5);
| dbl x2 = x1 + (x1 - x1) * sqrt(3.0 / 5);
|  ans += (5 * g(x0) + 8 * g(x1) + 5 * g(x2)) /

→ 18 * step;

| }
return ans;
};
```

6.6 Pollard's rho algorithm

```
namespace pollard {
using math::p;
vector<pair<11, int>> getFactors(11 N) {
vector<ll> primes;
| const int MX = 1e5;
| const 11 MX2 = MX * (11)MX;
| assert(MX <= math::maxP && math::pc > 0);
function<void(11)> go = [&go, &primes](11 n) {
 \mid for (ll x : primes)
   | while (n \% x == 0)
 | | n /= x;
| | if (n == 1)
| | return;
\mid \mid  if (n > MX2) {
| \ | \ | \ auto F = [\&](11 x) {
 | | | | ll k = ((long double)x * x) / n;
    | 11 r = (x * x - k * n + 3) \% n;
 | | return r < 0 ? r + n : r;
| | | };
| | | 11 x = mt19937_64()() \% n, y = x;
```

```
| | | const int C = 3 * pow(n, 0.25);
| \ | \ | \ | ll val = 1;
   forn(it, C) {
      | x = F(x), y = F(F(y));
      | if (x == y)
   | | continue;
 | | | ll delta = abs(x - y);
| \ | \ | \ | ll k = ((long double)val * delta) / n;
 | \cdot | val = (val * delta - k * n) % n;
   | | if (val < 0)
    | | | val += n;
      | if (val == 0) {
        | 11 g = __gcd(delta, n);
        | go(g), go(n / g);
          return;
        }
        if ((it & 255) == 0) {
        | 11 g = __gcd(val, n);
        | if (g != 1) {
          \mid go(g), go(n / g);
          return;
          }
| | | }
| | | }
| | primes.pb(n);
∣ };
| 11 n = N;
| for (int i = 0; i < math::pc && p[i] < MX; ++i)
| | if (n \% p[i] == 0) {
| | | primes.pb(p[i]);
| | | while (n % p[i] == 0)
| | | | n /= p[i];
| | }
| go(n);
| sort(primes.begin(), primes.end());
vector<pair<11, int>> res;
 for (ll x : primes) {
  | int cnt = 0;
 | while (N \% x == 0) {
| | cnt++;
| | N /= x;
| | }
| res.push_back({x, cnt});
| }
 return res;
}
} // namespace pollard
```

6.7 Polynom division and inversion

```
| auto cutPoly = [](poly &from, int l, int r) {
| | poly R;
| | R.v.resize(r - 1);
| | for (int i = 1; i < r; ++i) {
| | }
return R;
| };
| function<int(int, int)> rev = [&rev](int x, int
  \rightarrow m) -> int {
 | if (x == 1)
| | return (1 - rev(m \% x, x) * (11)m) / x + m;
| };
| poly R({rev(A[0], mod)});
| for (int k = 1; k < n; k <<= 1) {
 | poly AO = cutPoly(A, O, k);
 | poly A1 = cutPoly(A, k, 2 * k);
| poly H = AO * R;
\mid H = cutPoly(H, k, 2 * k);
| | poly R1 = (((A1 * R).cut(k) + H) * (poly({0}))
    → - R)).cut(k);
\mid R.v.resize(2 * k);
| | forn(i, k) R[i + k] = R1[i];
| }
return R.cut(n).norm();
pair<poly, poly> divide(poly A, poly B) {
\mid if (sz(A) < sz(B))
| | return {poly({0}), A};
| auto rev = [](poly f) {
| reverse(all(f.v));
| return f;
| };
| poly q =
| | | rev((inv(rev(B), sz(A) - sz(B) + 1) *
      \rightarrow rev(A)).cut(sz(A) - sz(B) + 1));
| poly r = A - B * q;
| return {q, r};
}
```

6.8 Simplex method

```
| | a[x][y] = 1;
| vector<int> vct;
| | for (int j = 0; j \le m; j++) {
| | | a[x][j] /= k;
| | | if (!eq(a[x][j], 0))
| | | vct.push_back(j);
| | }
| | for (int i = 0; i <= n; i++) {
| | | if (eq(a[i][y], 0) || i == x)
| | | continue;
| | | k = a[i][y];
| | for (int j : vct)
| | | | a[i][j] = k * a[x][j];
| | }
| };
| while (1) {
| int x = -1;
| | for (int i = 1; i <= n; i++)
| | | | if (ls(a[i][0], 0) \&\& (x == -1 || a[i][0] <
       \rightarrow a[x][0]))
| | | | x = i;
| | if (x == -1)
| | break;
|  int y = -1;
| | for (int j = 1; j \le m; j++)
| | | | if (ls(a[x][j], 0) && (y == -1 || a[x][j] <
      \rightarrow a[x][y]))
  | | y = j;
| | if (y == -1)
| | assert(0); // infeasible
| | pivot(x, y);
| }
| while (1) {
| | int y = -1;
  | for (int j = 1; j \le m; j++)
| \ | \ | \ | \ if (ls(0, a[0][j]) && (y == -1 \ || \ a[0][j] >
      \rightarrow a[0][y]))
| | | y = j;
| | if (y == -1)
| | break;
| int x = -1;
| | for (int i = 1; i <= n; i++)
| | | if (ls(0, a[i][y]) \&\& (x == -1 || a[i][0] /
      \rightarrow a[i][y] < a[x][0] / a[x][y]))
| | | | x = i;
| | if (x == -1)
| | assert(0); // unbounded
| | pivot(x, y);
| }
vector<double> ans(m + 1);
 for (int i = 1; i <= n; i++)
 | if (left[i] <= m)
| ans[0] = -a[0][0];
return ans;
// j=1..m: x[j]>=0
// i=1..n: sum(j=1..m) A[i][j]*x[j] <= A[i][0]
// \max sum(j=1..m) A[0][j]*x[j]
// res[0] is answer
// res[1..m] is certificate
```

6.9 Some integer sequences

Be	Bell numbers:								
n	B_n	n	B_n						
0	1	10	115975						
1	1	11	678 570						
2	2	12	4213597						
3	5	13	27644437						
4	15	14	190 899 322						
5	52	15	1382958545						
6	203	16	10 480 142 147						
7	877	17	82 864 869 804						
8	4 140	18	682076806159						
9	21 147	19	5832742205057						

Numbers with many divisors:					
$x \leq$	x	d(x)			
20	12	6			
50	48	10			
100	60	12			
1000	840	32			
10 000	9 240	64			
100 000	83 160	128			
10^{6}	720 720	240			
10^{7}	8 648 640	448			
10^{8}	91 891 800	768			
10^{9}	931 170 240	1 344			
10^{11}	97772875200	4032			
10^{12}	963 761 198 400	6720			
10^{15}	866 421 317 361 600	26 880			
10^{18}	897 612 484 786 617 600	103 680			

Parti	Partitions of n into unordered summands							
n	a(n)	n	a(n)	n	a(n)			
0	1	20	627	40	37338			
1	1	21	792	41	44583			
2	2	22	1 002	42	53174			
3	3	23	1255	43	63261			
4	5	24	1575	44	75175			
5	7	25	1958	45	89 134			
6	11	26	2436	46	105558			
7	15	27	3 010	47	124754			
8	22	28	3 718	48	147273			
9	30	29	4565	49	173525			
10	42	30	5 604	50	204 226			
11	56	31	6 842	51	239 943			
12	77	32	8 349	52	281 589			
13	101	33	10 143	53	329931			
14	135	34	12 310	54	386155			
15	176	35	14883	55	451276			
16	231	36	17977	56	526823			
17	297	37	21637	57	614154			
18	385	38	26015	58	715220			
19	490	39	31 185	59	831 820			
100	190 569 292							

7 Strings

7.1 Duval algorithm (Lyndon factorization)

```
void duval(string s) {
int n = (int)s.length();
| int i = 0;
| while (i < n) {
| int j = i + 1, k = i;
| | while (j < n && s[k] <= s[j]) {
| | | if (s[k] < s[j])
| | | | k = i;
| | else
| | | ++k;
| | ++j;
| | }
| | while (i <= k) {
| | | i += j - k;
| | }
| }
}
```

7.2 Palindromic tree

```
namespace eertree {
const int INF = 1e9;
const int N = 5e6 + 10;
char _s[N];
char *s = _s + 1;
int to[N][2];
int suf[N], len[N];
int sz, last;
const int odd = 1, even = 2, blank = 3;
void go(int &u, int pos) {
| while (u != blank && s[pos - len[u] - 1] !=

    s[pos]) {

| | u = suf[u];
| }
}
int add(int pos) {
| go(last, pos);
int u = suf[last];
| go(u, pos);
| int c = s[pos] - 'a';
| int res = 0;
| if (!to[last][c]) {
| res = 1;
| | to[last][c] = sz;
| len[sz] = len[last] + 2;
| | suf[sz] = to[u][c];
| | sz++;
| }
last = to[last][c];
return res;
}
void init() {
```

```
| to[blank][0] = to[blank][1] = even;
| len[blank] = suf[blank] = INF;
| len[even] = 0, suf[even] = odd;
| len[odd] = -1, suf[odd] = blank;
| last = even;
| sz = 4;
}
} // namespace eertree
```

7.3 Manacher's algorithm

```
// returns vector ret of length (|s| * 2 - 1),
// ret[i * 2] -- maximal length of palindrome
\rightarrow with center in i-th symbol
// ret[i * 2 + 1] -- maximal length of
\hookrightarrow palindrome with center between i-th and (i +
   1)-th symbols
vector<int> find_palindromes(string const& s) {
string tmp;
| for (char c : s) {
| | tmp += c;
| tmp += '!';
| }
tmp.pop_back();
| int c = 0, r = 1;
vector<int> rad(szof(tmp));
\mid rad[0] = 1;
| for (int i = 1; i < szof(tmp); ++i) {
| | if (i < c + r) {
| | | rad[i] = min(c + r - i, rad[2 * c - i]);
| | }
| | while (i - rad[i] >= 0 && i + rad[i] <

    szof(tmp) && tmp[i - rad[i]] == tmp[i +
    \rightarrow rad[i]]) {
| | }
| | if (i + rad[i] > c + r) {
| | c = i;
| | }
| }
| for (int i = 0; i < szof(tmp); ++i) {
| | if (i % 2 == 0) {
| | | rad[i] = (rad[i] + 1) / 2 * 2 - 1;
| | | rad[i] = rad[i] / 2 * 2;
| | }
| }
return rad;
}
```

7.4 Suffix automaton

```
struct state {
| state() { std::fill(next, next + 26, -1); }
| int len = 0, link = -1;
```

```
bool term = false;
| int next[26];
};
vector<state> st;
int last;
void sa_init() {
| last = 0;
| st.clear();
st.resize(1);
void sa_extend(char c) {
int cur = st.size();
| st.resize(st.size() + 1);
| st[cur].len = st[last].len + 1;
int p;
| for (p = last; p != -1 && st[p].next[c - 'a']
  \rightarrow == -1; p = st[p].link)
| | st[p].next[c - 'a'] = cur;
| if (p == -1)
| | st[cur].link = 0;
| else {
| | int q = st[p].next[c - 'a'];
 | if (st[p].len + 1 == st[q].len)
  | | st[cur].link = q;
 | else {
| | int clone = st.size();
| \ | \ |  st[clone].len = st[p].len + 1;
| \ | \ |  std::copy(st[q].next, st[q].next + 26,

    st[clone].next);
| | st[clone].link = st[q].link;
| | for (; p != -1 && st[p].next[c - 'a'] == q;
      \rightarrow p = st[p].link)
| | st[q].link = st[cur].link = clone;
| | }
| }
last = cur;
for (int v = last; v != -1; v = st[v].link) //
→ set termination flag.
\mid st[v].term = 1;
```

7.5 Suffix tree

```
#include \langle bits/stdc++.h \rangle
using namespace std;
#define forn(i, n) for (int i = 0; i < (int)(n);
\rightarrow i++)
const int N = 1e5, VN = 2 * N;
char s[N + 1];
```

```
map<char, int> t[VN];
int l[VN], r[VN], p[VN]; // edge p[v] -> v
\rightarrow matches to [l[v], r[v]) of string
int cc, n, suf[VN], vn = 2, v = 1, pos; // going
\rightarrow by edge from p[v] to v, now standing in pos
void go(int v) {
int no = cc++;
| for (auto p : t[v]) {
| v = p.second;
| | printf("%d %d %d\n", no, l[v], min(n, r[v]));
| | go(v);
| }
}
int main() {
assert(freopen("suftree.in", "r", stdin));
assert(freopen("suftree.out", "w", stdout));
| gets(s);
| forn(i, 127) t[0][i] = 1; // 0 = fictitious, 1
  \rightarrow = root
| 1[1] = -1;
| for (n = 0; s[n]; n++) {
| char c = s[n];
| | auto new_leaf = [&](int v) {
| | | p[vn] = v, l[vn] = n, r[vn] = N, t[v][c] =
      \rightarrow vn++;
| | };
| go:;
| | if (r[v] <= pos) {
| | | | new_leaf(v), v = suf[v], pos = r[v];
| | | }
 | v = t[v][c], pos = l[v] + 1;
 | } else if (c == s[pos]) {
   pos++;
| | |  int x = vn++;
| | | | 1[x] = 1[v], r[x] = pos, 1[v] = pos;
| | | p[x] = p[v], p[v] = x;
   | t[p[x]][s[1[x]]] = x, t[x][s[pos]] = v;
   new_leaf(x);
 | | v = suf[p[x]], pos = l[x];
| | | | v = t[v][s[pos]], pos += r[v] - l[v];
| | | suf[x] = (pos == r[x] ? v : vn);
| | | pos = r[v] - (pos - r[x]);
| | goto go;
| | }
| }
 printf("%d\n", vn - 1);
| go(1);
}
```

Table of Integrals*

Basic Forms

$$\int x^n dx = \frac{1}{n+1} x^{n+1} \tag{1}$$

$$\int \frac{1}{x} dx = \ln|x| \tag{2}$$

$$\int udv = uv - \int vdu \tag{3}$$

$$\int \frac{1}{ax+b} dx = \frac{1}{a} \ln|ax+b| \tag{4}$$

Integrals of Rational Functions

$$\int \frac{1}{(x+a)^2} dx = -\frac{1}{x+a}$$
 (5)

$$\int (x+a)^n dx = \frac{(x+a)^{n+1}}{n+1}, n \neq -1$$
 (6)

$$\int x(x+a)^n dx = \frac{(x+a)^{n+1}((n+1)x-a)}{(n+1)(n+2)}$$
 (7)

$$\int \frac{1}{1+x^2} dx = \tan^{-1} x \tag{8}$$

$$\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a} \tag{9}$$

$$\int \frac{x}{a^2 + x^2} dx = \frac{1}{2} \ln|a^2 + x^2| \tag{10}$$

$$\int \frac{x^2}{a^2 + x^2} dx = x - a \tan^{-1} \frac{x}{a} \tag{11}$$

$$\int \frac{x^3}{a^2 + x^2} dx = \frac{1}{2}x^2 - \frac{1}{2}a^2 \ln|a^2 + x^2| \tag{12}$$

$$\int \frac{1}{ax^2 + bx + c} dx = \frac{2}{\sqrt{4ac - b^2}} \tan^{-1} \frac{2ax + b}{\sqrt{4ac - b^2}}$$
 (13)

$$\int \frac{1}{(x+a)(x+b)} dx = \frac{1}{b-a} \ln \frac{a+x}{b+x}, \ a \neq b$$
 (14)

$$\int \frac{x}{(x+a)^2} dx = \frac{a}{a+x} + \ln|a+x| \tag{15}$$

$$\int \frac{x}{ax^2 + bx + c} dx = \frac{1}{2a} \ln|ax^2 + bx + c| - \frac{b}{a\sqrt{4ac - b^2}} \tan^{-1} \frac{2ax + b}{\sqrt{4ac - b^2}}$$
(16)

Integrals with Roots

$$\int \sqrt{x-a} dx = \frac{2}{3} (x-a)^{3/2}$$
 (17)

$$\int \frac{1}{\sqrt{x \pm a}} dx = 2\sqrt{x \pm a} \tag{18}$$

$$\int \frac{1}{\sqrt{a-x}} dx = -2\sqrt{a-x} \tag{19}$$

$$\int x\sqrt{x-a}dx = \frac{2}{3}a(x-a)^{3/2} + \frac{2}{5}(x-a)^{5/2}$$
 (20)

$$\int \sqrt{ax+b}dx = \left(\frac{2b}{3a} + \frac{2x}{3}\right)\sqrt{ax+b}$$
 (21)

$$\int (ax+b)^{3/2} dx = \frac{2}{5a} (ax+b)^{5/2}$$
 (22)

$$\int \frac{x}{\sqrt{x+a}} dx = \frac{2}{3} (x \mp 2a) \sqrt{x \pm a}$$
 (23)

$$\int \sqrt{\frac{x}{a-x}} dx = -\sqrt{x(a-x)} - a \tan^{-1} \frac{\sqrt{x(a-x)}}{x-a}$$
 (2)

$$\int \sqrt{\frac{x}{a+x}} dx = \sqrt{x(a+x)} - a \ln \left[\sqrt{x} + \sqrt{x+a} \right]$$
 (25)

$$\int x\sqrt{ax+b}dx = \frac{2}{15a^2}(-2b^2 + abx + 3a^2x^2)\sqrt{ax+b}$$
 (26)

$$\int \sqrt{x(ax+b)}dx = \frac{1}{4a^{3/2}} \left[(2ax+b)\sqrt{ax(ax+b)} -b^2 \ln \left| a\sqrt{x} + \sqrt{a(ax+b)} \right| \right]$$
(27)

$$\int \sqrt{x^3(ax+b)}dx = \left[\frac{b}{12a} - \frac{b^2}{8a^2x} + \frac{x}{3}\right] \sqrt{x^3(ax+b)} + \frac{b^3}{8a^{5/2}} \ln\left|a\sqrt{x} + \sqrt{a(ax+b)}\right| \quad (28)$$

$$\int \sqrt{x^2 \pm a^2} dx = \frac{1}{2} x \sqrt{x^2 \pm a^2} \pm \frac{1}{2} a^2 \ln \left| x + \sqrt{x^2 \pm a^2} \right|$$
(29)

$$\int \sqrt{a^2 - x^2} dx = \frac{1}{2} x \sqrt{a^2 - x^2} + \frac{1}{2} a^2 \tan^{-1} \frac{x}{\sqrt{a^2 - x^2}}$$
(30)

$$\int x\sqrt{x^2 \pm a^2} dx = \frac{1}{3} \left(x^2 \pm a^2\right)^{3/2}$$
 (31)

$$\int \frac{1}{\sqrt{x^2 \pm a^2}} dx = \ln \left| x + \sqrt{x^2 \pm a^2} \right|$$
 (32)

$$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a} \tag{33}$$

$$\int \frac{x}{\sqrt{x^2 + a^2}} dx = \sqrt{x^2 \pm a^2} \tag{34}$$

$$\int \frac{x}{\sqrt{a^2 - x^2}} dx = -\sqrt{a^2 - x^2} \tag{35}$$

$$\int \frac{x^2}{\sqrt{x^2 \pm a^2}} dx = \frac{1}{2} x \sqrt{x^2 \pm a^2} \mp \frac{1}{2} a^2 \ln \left| x + \sqrt{x^2 \pm a^2} \right|$$
(36)

$$\int \sqrt{ax^2 + bx + c} dx = \frac{b + 2ax}{4a} \sqrt{ax^2 + bx + c} + \frac{4ac - b^2}{8a^{3/2}} \ln \left| 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right|$$
(37)

$$\int x\sqrt{ax^2 + bx + c} = \frac{1}{48a^{5/2}} \left(2\sqrt{a}\sqrt{ax^2 + bx + c} \right)$$
$$\times \left(-3b^2 + 2abx + 8a(c + ax^2) \right)$$

$$+3(b^3 - 4abc) \ln \left| b + 2ax + 2\sqrt{a}\sqrt{ax^2 + bx + c} \right|$$
 (38)

$$\int \frac{1}{\sqrt{ax^2 + bx + c}} dx = \frac{1}{\sqrt{a}} \ln \left| 2ax + b + 2\sqrt{a(ax^2 + bx + c)} \right|$$
(39)

$$\int \frac{x}{\sqrt{ax^2 + bx + c}} dx = \frac{1}{a} \sqrt{ax^2 + bx + c}$$

$$-\frac{b}{2a^{3/2}}\ln\left|2ax+b+2\sqrt{a(ax^2+bx+c)}\right|$$
 (40)

$$\int \frac{dx}{(a^2 + x^2)^{3/2}} = \frac{x}{a^2 \sqrt{a^2 + x^2}} \tag{41}$$

Integrals with Logarithms

$$\int \ln ax dx = x \ln ax - x \tag{42}$$

$$\int \frac{\ln ax}{x} dx = \frac{1}{2} (\ln ax)^2 \tag{43}$$

$$\int \ln(ax+b)dx = \left(x+\frac{b}{a}\right)\ln(ax+b) - x, a \neq 0 \quad (44)$$

$$\int \ln(x^2 + a^2) \, dx = x \ln(x^2 + a^2) + 2a \tan^{-1} \frac{x}{a} - 2x \quad (45)$$

$$\int \ln(x^2 - a^2) \, dx = x \ln(x^2 - a^2) + a \ln \frac{x + a}{x - a} - 2x \quad (46)$$

$$\int \ln (ax^2 + bx + c) dx = \frac{1}{a} \sqrt{4ac - b^2} \tan^{-1} \frac{2ax + b}{\sqrt{4ac - b^2}} - 2x + \left(\frac{b}{2a} + x\right) \ln (ax^2 + bx + c)$$
(47)

$$\int x \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4}x^2 + \frac{1}{2}\left(x^2 - \frac{b^2}{a^2}\right) \ln(ax+b)$$
 (48)

$$\int x \ln \left(a^2 - b^2 x^2\right) dx = -\frac{1}{2} x^2 + \frac{1}{2} \left(x^2 - \frac{a^2}{b^2}\right) \ln \left(a^2 - b^2 x^2\right)$$
(49)

Integrals with Exponentials

$$\int e^{ax} dx = \frac{1}{a} e^{ax} \tag{50}$$

$$\int \sqrt{x}e^{ax}dx = \frac{1}{a}\sqrt{x}e^{ax} + \frac{i\sqrt{\pi}}{2a^{3/2}}\operatorname{erf}\left(i\sqrt{ax}\right),$$
where $\operatorname{erf}(x) = \frac{2}{\sqrt{\pi}}\int_{a}^{x}e^{-t^{2}}dt$ (51)

$$\int xe^x dx = (x-1)e^x \tag{52}$$

$$\int xe^{ax}dx = \left(\frac{x}{a} - \frac{1}{a^2}\right)e^{ax} \tag{53}$$

$$\int x^2 e^x dx = (x^2 - 2x + 2) e^x$$
 (54)

$$\int x^2 e^{ax} dx = \left(\frac{x^2}{a} - \frac{2x}{a^2} + \frac{2}{a^3}\right) e^{ax}$$
 (55)

$$\int x^3 e^x dx = (x^3 - 3x^2 + 6x - 6) e^x$$
 (56)

$$\int x^n e^{ax} dx = \frac{x^n e^{ax}}{a} - \frac{n}{a} \int x^{n-1} e^{ax} dx$$
 (57)

$$\int x^n e^{ax} dx = \frac{(-1)^n}{a^{n+1}} \Gamma[1+n, -ax],$$
where $\Gamma(a, x) = \int_x^\infty t^{a-1} e^{-t} dt$ (58)

$$\int e^{ax^2} dx = -\frac{i\sqrt{\pi}}{2\sqrt{a}} \operatorname{erf}\left(ix\sqrt{a}\right)$$
 (59)

$$\int e^{-ax^2} dx = \frac{\sqrt{\pi}}{2\sqrt{a}} \operatorname{erf}(x\sqrt{a})$$
(60)

$$\int xe^{-ax^2} \, \mathrm{dx} = -\frac{1}{2a}e^{-ax^2} \tag{61}$$

$$\int x^2 e^{-ax^2} dx = \frac{1}{4} \sqrt{\frac{\pi}{a^3}} \operatorname{erf}(x\sqrt{a}) - \frac{x}{2a} e^{-ax^2}$$
 (62)

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Integrals with Trigonometric Functions

$$\int \sin ax dx = -\frac{1}{a} \cos ax \tag{63}$$

$$\int \sin^2 ax dx = \frac{x}{2} - \frac{\sin 2ax}{4a} \tag{64}$$

$$\int \sin^n ax dx = -\frac{1}{a} \cos ax \, _2F_1 \left[\frac{1}{2}, \frac{1-n}{2}, \frac{3}{2}, \cos^2 ax \right]$$
 (65)

$$\int \sin^3 ax dx = -\frac{3\cos ax}{4a} + \frac{\cos 3ax}{12a} \tag{66}$$

$$\int \cos ax dx = -\frac{1}{a} \sin ax \tag{67}$$

$$\int \cos^2 ax dx = \frac{x}{2} + \frac{\sin 2ax}{4a} \tag{68}$$

$$\int \cos^p ax dx = -\frac{1}{a(1+p)} \cos^{1+p} ax \times {}_{2}F_{1} \left[\frac{1+p}{2}, \frac{1}{2}, \frac{3+p}{2}, \cos^2 ax \right]$$
(69)

$$\int \cos^3 ax dx = \frac{3\sin ax}{4a} + \frac{\sin 3ax}{12a} \tag{70}$$

$$\int \cos ax \sin bx dx = \frac{\cos[(a-b)x]}{2(a-b)} - \frac{\cos[(a+b)x]}{2(a+b)}, a \neq b$$
(71)

$$\int \sin^2 ax \cos bx dx = -\frac{\sin[(2a-b)x]}{4(2a-b)} + \frac{\sin bx}{2b} - \frac{\sin[(2a+b)x]}{4(2a+b)}$$
(72)

$$\int \sin^2 x \cos x dx = \frac{1}{3} \sin^3 x \tag{73}$$

$$\int \cos^2 ax \sin bx dx = \frac{\cos[(2a-b)x]}{4(2a-b)} - \frac{\cos bx}{2b} - \frac{\cos[(2a+b)x]}{4(2a+b)}$$
(74)

$$\int \cos^2 ax \sin ax dx = -\frac{1}{3a} \cos^3 ax \tag{75}$$

$$\int \sin^2 ax \cos^2 bx dx = \frac{x}{4} - \frac{\sin 2ax}{8a} - \frac{\sin[2(a-b)x]}{16(a-b)} + \frac{\sin 2bx}{8b} - \frac{\sin[2(a+b)x]}{16(a+b)}$$
(76)

$$\int \sin^2 ax \cos^2 ax dx = \frac{x}{8} - \frac{\sin 4ax}{32a} \tag{77}$$

$$\int \tan ax dx = -\frac{1}{a} \ln \cos ax \tag{78}$$

$$\int \tan^2 ax dx = -x + \frac{1}{a} \tan ax \tag{79}$$

$$\int \tan^{n} ax dx = \frac{\tan^{n+1} ax}{a(1+n)} \times {}_{2}F_{1}\left(\frac{n+1}{2}, 1, \frac{n+3}{2}, -\tan^{2} ax\right)$$
(80)

$$\int \tan^3 ax dx = \frac{1}{a} \ln \cos ax + \frac{1}{2a} \sec^2 ax \tag{81}$$

$$\int \sec x dx = \ln|\sec x + \tan x| = 2\tanh^{-1}\left(\tan\frac{x}{2}\right) \quad (82)$$

$$\int \sec^2 ax dx = \frac{1}{a} \tan ax \tag{83}$$

$$\int \sec^3 x \, dx = \frac{1}{2} \sec x \tan x + \frac{1}{2} \ln|\sec x + \tan x| \quad (84)$$

$$\int \sec x \tan x dx = \sec x \tag{85}$$

$$\int \sec^2 x \tan x dx = \frac{1}{2} \sec^2 x \tag{86}$$

$$\int \sec^n x \tan x dx = \frac{1}{n} \sec^n x, n \neq 0$$
 (87)

$$\int \csc x dx = \ln\left|\tan\frac{x}{2}\right| = \ln|\csc x - \cot x| + C \qquad (88)$$

$$\int \csc^2 ax dx = -\frac{1}{a} \cot ax \tag{89}$$

$$\int \csc^3 x dx = -\frac{1}{2} \cot x \csc x + \frac{1}{2} \ln|\csc x - \cot x| \quad (90)$$

$$\int \csc^n x \cot x dx = -\frac{1}{n} \csc^n x, n \neq 0$$
 (91)

$$\int \sec x \csc x dx = \ln|\tan x| \tag{92}$$

Products of Trigonometric Functions and Monomials

$$\int x \cos x dx = \cos x + x \sin x \tag{93}$$

$$\int x \cos ax dx = \frac{1}{a^2} \cos ax + \frac{x}{a} \sin ax \tag{94}$$

$$\int x^2 \cos x dx = 2x \cos x + \left(x^2 - 2\right) \sin x \tag{95}$$

$$\int x^2 \cos ax dx = \frac{2x \cos ax}{a^2} + \frac{a^2 x^2 - 2}{a^3} \sin ax$$
 (96)

$$\int x^{n} \cos x dx = -\frac{1}{2} (i)^{n+1} \left[\Gamma(n+1, -ix) + (-1)^{n} \Gamma(n+1, ix) \right]$$
(97)

$$\int x^n \cos ax dx = \frac{1}{2} (ia)^{1-n} \left[(-1)^n \Gamma(n+1, -iax) - \Gamma(n+1, ixa) \right]$$

$$(98)$$

$$\int x \sin x dx = -x \cos x + \sin x \tag{99}$$

$$\int x \sin ax dx = -\frac{x \cos ax}{a} + \frac{\sin ax}{a^2} \tag{100}$$

$$\int x^2 \sin x dx = (2 - x^2) \cos x + 2x \sin x \tag{101}$$

$$\int x^2 \sin ax dx = \frac{2 - a^2 x^2}{a^3} \cos ax + \frac{2x \sin ax}{a^2}$$
 (102)

$$\int x^n \sin x dx = -\frac{1}{2} (i)^n \left[\Gamma(n+1, -ix) - (-1)^n \Gamma(n+1, -ix) \right]$$
(103)

Products of Trigonometric Functions and Exponentials

$$\int e^x \sin x dx = \frac{1}{2} e^x (\sin x - \cos x) \tag{104}$$

$$\int e^{bx} \sin ax dx = \frac{1}{a^2 + b^2} e^{bx} (b \sin ax - a \cos ax) \quad (105)$$

$$\int e^x \cos x dx = \frac{1}{2} e^x (\sin x + \cos x) \tag{106}$$

$$\int e^{bx} \cos ax dx = \frac{1}{a^2 + b^2} e^{bx} (a \sin ax + b \cos ax) \quad (107)$$

$$\int xe^x \sin x dx = \frac{1}{2}e^x (\cos x - x\cos x + x\sin x) \qquad (108)$$

$$\int xe^x \cos x dx = \frac{1}{2}e^x (x\cos x - \sin x + x\sin x) \qquad (109)$$

Integrals of Hyperbolic Functions

$$\int \cosh ax dx = \frac{1}{a} \sinh ax \tag{110}$$

$$\int e^{ax} \cosh bx dx =$$

$$\begin{cases} \frac{e^{ax}}{a^2 - b^2} [a\cosh bx - b\sinh bx] & a \neq b\\ \frac{e^{2ax}}{4a} + \frac{x}{2} & a = b \end{cases}$$
(111)

$$\int \sinh ax dx = -\frac{1}{a} \cosh ax \tag{112}$$

$$\int e^{ax} \sinh bx dx =$$

$$\begin{cases}
\frac{e^{ax}}{a^2 - b^2} [-b \cosh bx + a \sinh bx] & a \neq b \\
\frac{e^{2ax}}{4a} - \frac{x}{2} & a = b
\end{cases}$$
(113)

$$\int e^{ax} \tanh bx dx = \begin{cases} \frac{e^{(a+2b)x}}{(a+2b)} {}_{2}F_{1} \left[1 + \frac{a}{2b}, 1, 2 + \frac{a}{2b}, -e^{2bx} \right] \\ -\frac{1}{a} e^{ax} {}_{2}F_{1} \left[\frac{a}{2b}, 1, 1E, -e^{2bx} \right] & a \neq b \end{cases}$$
(114)
$$\frac{e^{ax} - 2 \tan^{-1}[e^{ax}]}{a} \qquad a = b$$

$$\int \tanh ax \, dx = \frac{1}{a} \ln \cosh ax \tag{115}$$

$$\int \cos ax \cosh bx dx = \frac{1}{a^2 + b^2} \left[a \sin ax \cosh bx + b \cos ax \sinh bx \right]$$

$$(116)$$

$$\int \cos ax \sinh bx dx = \frac{1}{a^2 + b^2} \left[b \cos ax \cosh bx + a \sin ax \sinh bx \right]$$
 (117)

$$\int \sin ax \cosh bx dx = \frac{1}{a^2 + b^2} \left[-a \cos ax \cosh bx + b \sin ax \sinh bx \right] \tag{118}$$

$$\int \sin ax \sinh bx dx = \frac{1}{a^2 + b^2} \left[b \cosh bx \sin ax - a \cos ax \sinh bx \right]$$
(119)

$$\int \sinh ax \cosh ax dx = \frac{1}{4a} \left[-2ax + \sinh 2ax \right]$$
 (120)

$$\int \sinh ax \cosh bx dx = \frac{1}{b^2 - a^2} [b \cosh bx \sinh ax -a \cosh ax \sinh bx]$$
(121)

