

Contents

1	Some useful things	2
2	Data structures	3
2.1	Hash table	3
3	Geometry	3
3.1	Common tangents of two circles	3
3.2	Convex hull 3D in $O(n^2)$	4
3.3	Dynamic convex hull trick	4
3.4	Minimal covering disk	4
3.5	Draw svg pictures	5
4	Graphs	5
4.1	2-Chinese algorithm	5
4.2	Dominator tree	6
4.3	General matching	7
4.4	Hungarian algorithm	8
4.5	Link-Cut Tree	9
4.6	Smith algorithm (Game on cyclic graph)	10
4.7	Stoer-Vagner algorithm (Global min-cut)	11
5	Matroids	11
5.1	Matroids intersection	11
6	Numeric	12
6.1	Berlekamp-Massey Algorithm	12
6.2	Chinese remainder theorem	13
6.3	Miller–Rabin primality test	13
6.4	Multiplication by modulo	13
6.5	Numerical integration	13
6.6	Pollard’s rho algorithm	13
6.7	Polynom division and inversion	14
6.8	Simplex method	15
7	Strings	15
7.1	Duval algorithm (Lyndon factorization)	15
7.2	Palindromic tree	15
7.3	Suffix automaton	16
7.4	Suffix tree	16

1 Some useful things

```
import java.util.*;
import java.io.*;

public class Template {
    | FastScanner in;
    | PrintWriter out;

    | public void solve() throws IOException {
    | | int n = in.nextInt();
    | | out.println(n);
    | }

    | public void run() {
    | | try {
    | | | in = new FastScanner();
    | | | out = new PrintWriter(System.out);

    | | | solve();

    | | | out.close();
    | | } catch (IOException e) {
    | | | e.printStackTrace();
    | | }
    | }

    | class FastScanner {
    | | BufferedReader br;
    | | StringTokenizer st;

    | | FastScanner() {
    | | | br = new BufferedReader(new
    | | |     ↳ InputStreamReader(System.in));
    | | }

    | | String next() {
    | | | while (st == null || !st.hasMoreTokens()) {
    | | | | try {
    | | | | | st = new
    | | | | |     ↳ StringTokenizer(br.readLine());
    | | | | } catch (IOException e) {
    | | | | | e.printStackTrace();
    | | | | }
    | | | }
    | | | return st.nextToken();
    | | }

    | | int nextInt() {
    | | | return Integer.parseInt(next());
    | | }
    | }

    | public static void main(String[] arg) {
    | | new Template().run();
    | }
}
```

```
#include <algorithm>
#include <cstdio>
```

```
/** Interface */

inline int readInt();
inline int readUInt();
inline bool isEof();

/** Read */

static const int buf_size = 100000;
static char buf[buf_size];
static int buf_len = 0, pos = 0;

inline bool isEof() {
    if (pos == buf_len) {
        pos = 0, buf_len = fread(buf, 1, buf_size,
        ↳ stdin);
        if (pos == buf_len)
            return 1;
    }
    return 0;
}

inline int getChar() { return isEof() ? -1 :
    ↳ buf[pos++]; }

inline int readChar() {
    int c = getChar();
    while (c != -1 && c <= 32)
        c = getChar();
    return c;
}

inline int readUInt() {
    int c = readChar(), x = 0;
    while ('0' <= c && c <= '9')
        x = x * 10 + c - '0', c = getChar();
    return x;
}

inline int readInt() {
    int s = 1, c = readChar();
    int x = 0;
    if (c == '-')
        s = -1, c = getChar();
    while ('0' <= c && c <= '9')
        x = x * 10 + c - '0', c = getChar();
    return s == 1 ? x : -x;
}

// 10M int [0..1e9)
// cin 3.02
// scanf 1.2
// cin sync_with_stdio(false) 0.71
// fastRead getchar 0.53
// fastRead fread 0.15

inline void fasterLLDivMod(ull x, uint y, uint
    ↳ &out_d, uint &out_m) {
    | uint xh = (uint)(x >> 32), xl = (uint)x, d, m;
    | #ifdef __GNUC__
    | | asm(
    | | | "divl %4; \n\t"
```

```

| | : "=a" (d), "=d" (m)
| | : "d" (xh), "a" (xl), "r" (y)
| );
#else
| __asm {
|   mov edx, dword ptr[xh];
|   mov eax, dword ptr[xl];
|   div dword ptr[y];
|   mov dword ptr[d], eax;
|   mov dword ptr[m], edx;
| };
#endif
| out_d = d; out_m = m;
}

// have no idea what sse flags are really cool;
→ list of some of them
// -- very good with bitsets
#pragma GCC optimize("O3")
#pragma GCC target(
→ "sse,sse2,sse3,ssse3,sse4,popcnt,abm,mmx")

```

```

#include "ext/pb_ds/assoc_container.hpp"
using namespace __gnu_pbds;

template <typename T> using ordered_set = tree<T,
→ null_type, less<T>, rb_tree_tag,
→ tree_order_statistics_node_update>;
template <typename K, typename V> using
→ ordered_map = tree<K, V, less<K>,
→ rb_tree_tag,
→ tree_order_statistics_node_update>;

// HOW TO USE ::
// -- order_of_key(10) returns the number of
→ elements in set/map strictly less than 10
// -- *find_by_order(10) returns 10-th smallest
→ element in set/map (0-based)

bitset<N> a;
for (int i = a._Find_first(); i != a.size(); i =
→ a._Find_next(i)) {
| cout << i << endl;
}

```

2 Data structures

2.1 Hash table

```

template <const int max_size, class HashType,
→ class Data,
| | | | const Data default_value>
struct hashTable {
| HashType hash[max_size];
| Data f[max_size];
| int size;

| int position(HashType H) const {
|   int i = H % max_size;
|   while (hash[i] && hash[i] != H)

```

```

| | | if (++i == max_size)
| | | i = 0;
|   return i;
| }

Data &operator[] (HashType H) {
|   assert(H != 0);
|   int i = position(H);
|   if (!hash[i]) {
| |   hash[i] = H;
| |   f[i] = default_value;
| |   size++;
|   }
|   return f[i];
| }
};

hashTable<13, int, int, 0> h;

```

3 Geometry

3.1 Common tangents of two circles

```

vector<Line> commonTangents(pt A, dbl rA, pt B,
→ dbl rB) {
|   vector<Line> res;
|   pt C = B - A;
|   dbl z = C.len2();
|   for (int i = -1; i <= 1; i += 2) {
| |   for (int j = -1; j <= 1; j += 2) {
| | |   dbl r = rB * j - rA * i;
| | |   dbl d = z - r * r;
| | |   if (ls(d, 0))
| | | |   continue;
| | |   d = sqrt(max(0.01, d));
| | |   pt magic = pt(r, d) / z;
| | |   pt v(magic % C, magic * C);
| | |   dbl CC = (rA * i - v % A) / v.len2();
| | |   pt O = v * -CC;
| | |   res.pb(Line(O, O + v.rotate()));
| | }
| }
|   return res;
}

```

```

// HOW TO USE ::
// --      *D*-----*F*
// --      *...*-          -*...*
// --      *.....* -      - *.....*
// --      *.....* -      - *.....*
// --      *...A...* --      *...B...*
// --      *.....* -      - *.....*
// --      *.....* -      - *.....*
// --      *...*-          -*...*
// --      *C*-----*E*
// --      res = {CE, CF, DE, DF}

```

3.2 Convex hull 3D in $O(n^2)$

```

struct Plane {
| pt 0, v;
| vector<int> id;
};

vector<Plane> convexHull3(vector<pt> p) {
| vector<Plane> res;
| int n = p.size();
| for (int i = 0; i < n; i++)
| | p[i].id = i;
| for (int i = 0; i < 4; i++) {
| | vector<pt> tmp;
| | for (int j = 0; j < 4; j++)
| | | if (i != j)
| | | | tmp.pb(p[j]);
| | res.pb({tmp[0],
| | | (tmp[1] - tmp[0]) * (tmp[2] -
| | |   tmp[0]),
| | | {tmp[0].id, tmp[1].id, tmp[2].id}});
| | if ((p[i] - res.back().0) % res.back().v > 0)
| | | {
| | | | res.back().v = res.back().v * -1;
| | | | swap(res.back().id[0], res.back().id[1]);
| | | }
| | }
| vector<vector<int>> use(n, vector<int>(n, 0));
| int tmr = 0;
| for (int i = 4; i < n; i++) {
| | int cur = 0;
| | tmr++;
| | vector<pair<int, int>> curEdge;
| | for (int j = 0; j < sz(res); j++) {
| | | if ((p[i] - res[j].0) % res[j].v > 0) {
| | | | for (int t = 0; t < 3; t++) {
| | | | | int v = res[j].id[t];
| | | | | int u = res[j].id[(t + 1) % 3];
| | | | | use[v][u] = tmr;
| | | | | curEdge.pb({v, u});
| | | | }
| | | } else {
| | | | res[cur++] = res[j];
| | | }
| | }
| | res.resize(cur);
| | for (auto x : curEdge) {
| | | if (use[x.S][x.F] == tmr)
| | | | continue;
| | | res.pb({p[i], (p[x.F] - p[i]) * (p[x.S] -
| | |   p[i]), {x.F, x.S, i}});
| | }
| }
| return res;
}

```

```

// plane in 3d
// (A, v) * (B, u) -> (0, n)

```

```

pt n = v * u;
pt m = v * n;
double t = (B - A) % u / (u % m);

```

```
pt 0 = A - m * t;
```

3.3 Dynamic convex hull trick

```

const ll is_query = -(1LL << 62);

struct Line {
| ll m, b;
| mutable function<const Line *(> succ;

| bool operator<(const Line &rhs) const {
| | if (rhs.b != is_query)
| | | return m < rhs.m;
| | const Line *s = succ();
| | if (!s)
| | | return 0;
| | ll x = rhs.m;
| | return b - s->b < (s->m - m) * x;
| }
};

struct HullDynamic : public multiset<Line> {
| bool bad(iterator y) {
| | auto z = next(y);
| | if (y == begin()) {
| | | if (z == end())
| | | | return 0;
| | | return y->m == z->m && y->b <= z->b;
| | }
| | auto x = prev(y);
| | if (z == end())
| | | return y->m == x->m && y->b <= x->b;
| | return (x->b - y->b) * (z->m - y->m) >= (y->b
| |   - z->b) * (y->m - x->m);
| }

| void insert_line(ll m, ll b) {
| | auto y = insert({m, b});
| | y->succ = [=] { return next(y) == end() ? 0 :
| |   &*next(y); };
| | if (bad(y)) {
| | | erase(y);
| | | return;
| | }
| | while (next(y) != end() && bad(next(y)))
| | | erase(next(y));
| | while (y != begin() && bad(prev(y)))
| | | erase(prev(y));
| }

| ll eval(ll x) {
| | auto l = *lower_bound((Line){x, is_query});
| | return l.m * x + l.b;
| }
};

```

3.4 Minimal covering disk

```

pair<pt, dbl> minDisc(vector<pt> p) {
| int n = p.size();

```

```

| pt 0 = pt(0, 0);
| dbl R = 0;
| random_shuffle(all(p));
| for (int i = 0; i < n; i++) {
| | if (ls(R, (0 - p[i]).len())) {
| | | 0 = p[i];
| | | R = 0;
| | | for (int j = 0; j < i; j++) {
| | | | if (ls(R, (0 - p[j]).len())) {
| | | | | 0 = (p[i] + p[j]) / 2;
| | | | | R = (p[i] - p[j]).len() / 2;
| | | | | for (int k = 0; k < j; k++) {
| | | | | | if (ls(R, (0 - p[k]).len())) {
| | | | | | | Line 11((p[i] + p[j]) / 2,
| | | | | | | | (p[i] + p[j]) / 2 + (p[i] -
| | | | | | | | | p[j]).rotate());
| | | | | | | Line 12((p[k] + p[j]) / 2,
| | | | | | | | (p[k] + p[j]) / 2 + (p[k] -
| | | | | | | | | p[j]).rotate());
| | | | | | | 0 = l1 * l2;
| | | | | | | R = (p[i] - 0).len();
| | | | | }
| | | }
| | }
| }
| return {0, R};
}

```

3.5 Draw svg pictures

```

struct SVG {
| FILE *out;
| ld sc = 50;
| void open() {
| | out = fopen("image.svg", "w");
| | fprintf(out, "svg
| |   ↪ xmlns='http://www.w3.org/2000/svg'
| |   ↪ viewBox='-1000 -1000 2000 2000'>\n");
| }
| void line(point a, point b) {
| | a = a * sc, b = b * sc;
| | fprintf(out, "line x1='%f' y1='%f' x2='%f'
| |   ↪ y2='%f' stroke='black'/>\n", a.x, -a.y,
| |   ↪ b.x, -b.y);
| }
| void circle(point a, ld r = -1, string col =
| |   ↪ "red") {
| | r = sc * (r == -1 ? 0.3 : r);
| | a = a * sc;
| | fprintf(out, "circle cx='%f' cy='%f' r='%f'
| |   ↪ fill='%s'/>\n", a.x, -a.y, r,
| |   ↪ col.c_str());
| }
| void text(point a, string s) {
| | a = a * sc;
| | fprintf(out, "text x='%f' y='%f'
| |   ↪ font-size='100px'>s</text>\n", a.x,
| |   ↪ -a.y, s.c_str());
| }
}

```

```

void close() {
| | fprintf(out, "</svg>\n");
| | fclose(out);
| | out = 0;
| }
~SVG() {
| | if (out) {
| | | close();
| | }
| }
} svg;

```

4 Graphs

4.1 2-Chinese algorithm

```

namespace twoc {
struct Heap {
| static Heap *null;
| ll x, xadd;
| int ver, h;
| #ifdef ANS
| int ei;
| #endif
| Heap *l, *r;
| Heap(ll xx, int vv) : x(xx), xadd(0), ver(vv),
|   ↪ h(1), l(null), r(null) {}
| Heap(const char *) : x(0), xadd(0), ver(0),
|   ↪ h(0), l(this), r(this) {}
| void add(ll a) {
| | x += a;
| | xadd += a;
| }
| void push() {
| | if (l != null)
| | | l->add(xadd);
| | if (r != null)
| | | r->add(xadd);
| | xadd = 0;
| }
};
Heap *Heap::null = new Heap("wqeqw");
Heap *merge(Heap *l, Heap *r) {
| if (l == Heap::null)
| | return r;
| if (r == Heap::null)
| | return l;
| l->push();
| r->push();
| if (l->x > r->x)
| | swap(l, r);
| l->r = merge(l->r, r);
| if (l->l->h < l->r->h)
| | swap(l->l, l->r);
| l->h = l->r->h + 1;
| return l;
}
Heap *pop(Heap *h) {
| h->push();
| return merge(h->l, h->r);
}

```

```

const int N = 666666;
struct DSU {
    int p[N];
    void init(int nn) { iota(p, p + nn, 0); }
    int get(int x) { return p[x] == x ? x : p[x] =
        get(p[x]); }
    void merge(int x, int y) { p[get(y)] = get(x);
        }
} dsu;
Heap *eb[N];
int n;
#ifdef ANS
struct Edge {
    int x, y;
    ll c;
};
vector<Edge> edges;
int answer[N];
#endif
void init(int nn) {
    n = nn;
    dsu.init(n);
    fill(eb, eb + n, Heap::null);
    edges.clear();
}
void addEdge(int x, int y, ll c) {
    Heap *h = new Heap(c, x);
#ifdef ANS
    h->ei = sz(edges);
    edges.push_back({x, y, c});
#endif
    eb[y] = merge(eb[y], h);
}
ll solve(int root = 0) {
    ll ans = 0;
    static int done[N], pv[N];
    memset(done, 0, sizeof(int) * n);
    done[root] = 1;
    int tt = 1;
#ifdef ANS
    int cnum = 0;
    static vector<ipair> eout[N];
    for (int i = 0; i < n; ++i)
        eout[i].clear();
#endif
    for (int i = 0; i < n; ++i) {
        int v = dsu.get(i);
        if (done[v])
            continue;
        ++tt;
        while (true) {
            done[v] = tt;
            int nv = -1;
            while (eb[v] != Heap::null) {
                nv = dsu.get(eb[v]->ver);
                if (nv == v) {
                    eb[v] = pop(eb[v]);
                    continue;
                }
                break;
            }
            if (nv == -1)
                return LINF;
            ans += eb[v]->x;
            eb[v]->add(-eb[v]->x);
#ifdef ANS
            int ei = eb[v]->ei;
            eout[edges[ei].x].push_back({++cnum, ei});
#endif
            if (!done[nv]) {
                pv[v] = nv;
                v = nv;
                continue;
            }
            if (done[nv] != tt)
                break;
            int v1 = nv;
            while (v1 != v) {
                eb[v] = merge(eb[v], eb[v1]);
                dsu.merge(v, v1);
                v1 = dsu.get(pv[v1]);
            }
        }
    }
#ifdef ANS
    memset(answer, -1, sizeof(int) * n);
    answer[root] = 0;
    set<ipair> es(all(eout[root]));
    while (!es.empty()) {
        auto it = es.begin();
        int ei = it->second;
        es.erase(it);
        int nv = edges[ei].y;
        if (answer[nv] != -1)
            continue;
        answer[nv] = ei;
        es.insert(all(eout[nv]));
    }
    answer[root] = -1;
#endif
    return ans;
}
/* Usage: twoc::init(vertex_count);
 *         twoc::addEdge(v1, v2, cost);
 *         twoc::solve(root); - returns cost or
 *         LINF
 *         twoc::answer contains index of ingoing edge
 *         for each vertex
 */
} // namespace twoc

```

4.2 Dominator tree

```

namespace domtree {
const int K = 18;
const int N = 1 << K;

int n, root;
vector<int> e[N], g[N];
int sdom[N], dom[N];
int p[N][K], h[N], pr[N];
int in[N], out[N], tmr, rev[N];

```

```

void init(int _n, int _root) {
    n = _n;
    root = _root;
    tmr = 0;
    for (int i = 0; i < n; i++) {
        e[i].clear();
        g[i].clear();
        in[i] = -1;
    }
}

void addEdge(int u, int v) {
    e[u].push_back(v);
    g[v].push_back(u);
}

void dfs(int v) {
    in[v] = tmr++;
    for (int to : e[v]) {
        if (in[to] != -1)
            continue;
        pr[to] = v;
        dfs(to);
    }
    out[v] = tmr - 1;
}

int lca(int u, int v) {
    if (h[u] < h[v])
        swap(u, v);
    for (int i = 0; i < K; i++)
        if ((h[u] - h[v]) & (1 << i))
            u = p[u][i];
    if (u == v)
        return u;
    for (int i = K - 1; i >= 0; i--) {
        if (p[u][i] != p[v][i]) {
            u = p[u][i];
            v = p[v][i];
        }
    }
    return p[u][0];
}

void solve(int _n, int _root, vector<pair<int,
    ↪ int>> _edges) {
    init(_n, _root);
    for (auto ed : _edges)
        addEdge(ed.first, ed.second);

    dfs(root);
    for (int i = 0; i < n; i++)
        if (in[i] != -1)
            rev[in[i]] = i;
    segtree tr(tmr); // a[i]:=min(a[i],x) and
    ↪ return a[i]
    for (int i = tmr - 1; i >= 0; i--) {
        int v = rev[i];
        int cur = i;
        for (int to : g[v]) {
            if (in[to] == -1)
                continue;

```

```

            if (in[to] < in[v])
                cur = min(cur, in[to]);
            else
                cur = min(cur, tr.get(in[to]));
        }
        sdom[v] = rev[cur];
        tr.upd(in[v], out[v], in[sdom[v]]);
    }
    for (int i = 0; i < tmr; i++) {
        int v = rev[i];
        if (i == 0) {
            dom[v] = v;
            h[v] = 0;
        } else {
            dom[v] = lca(sdom[v], pr[v]);
            h[v] = h[dom[v]] + 1;
        }
        p[v][0] = dom[v];
        for (int j = 1; j < K; j++)
            p[v][j] = p[p[v][j - 1]][j - 1];
    }
    for (int i = 0; i < n; i++)
        if (in[i] == -1)
            dom[i] = -1;
}
} // namespace domtree

```

4.3 General matching

```

// COPYPASTED FROM E-MAXX
namespace general_matching {
    const int MAXN = 256;
    int n;
    vector<int> g[MAXN];
    int match[MAXN], p[MAXN], base[MAXN], q[MAXN];
    bool used[MAXN], blossom[MAXN];

    int lca(int a, int b) {
        bool used[MAXN] = {0};
        for (;;) {
            a = base[a];
            used[a] = true;
            if (match[a] == -1)
                break;
            a = p[match[a]];
        }
        for (;;) {
            b = base[b];
            if (used[b])
                return b;
            b = p[match[b]];
        }
    }

    void mark_path(int v, int b, int children) {
        while (base[v] != b) {
            blossom[base[v]] = blossom[base[match[v]]] =
                ↪ true;
            p[v] = children;
            children = match[v];
            v = p[match[v]];
        }
    }
}

```

```

    }
}

int find_path(int root) {
    memset(used, 0, sizeof used);
    memset(p, -1, sizeof p);
    for (int i = 0; i < n; ++i)
        base[i] = i;

    used[root] = true;
    int qh = 0, qt = 0;
    q[qt++] = root;
    while (qh < qt) {
        int v = q[qh++];
        for (size_t i = 0; i < g[v].size(); ++i) {
            int to = g[v][i];
            if (base[v] == base[to] || match[v] == to)
                continue;
            if (to == root || (match[to] != -1 &&
                → p[match[to]] != -1)) {
                int curbase = lca(v, to);
                memset(blossom, 0, sizeof blossom);
                mark_path(v, curbase, to);
                mark_path(to, curbase, v);
                for (int i = 0; i < n; ++i)
                    if (blossom[base[i]]) {
                        base[i] = curbase;
                        if (!used[i]) {
                            used[i] = true;
                            q[qt++] = i;
                        }
                    }
            } else if (p[to] == -1) {
                p[to] = v;
                if (match[to] == -1)
                    return to;
                to = match[to];
                used[to] = true;
                q[qt++] = to;
            }
        }
    }
    return -1;
}

vector<pair<int, int>> solve(int _n,
    → vector<pair<int, int>> edges) {
    n = _n;
    for (int i = 0; i < n; ++i)
        g[i].clear();
    for (auto o : edges) {
        g[o.first].push_back(o.second);
        g[o.second].push_back(o.first);
    }
    memset(match, -1, sizeof match);
    for (int i = 0; i < n; ++i) {
        if (match[i] == -1) {
            int v = find_path(i);
            while (v != -1) {
                int pv = p[v], ppv = match[pv];
                match[v] = pv, match[pv] = v;
                v = ppv;
            }
        }
    }
}

```

```

    }
}

vector<pair<int, int>> ans;
for (int i = 0; i < n; i++) {
    if (match[i] > i) {
        ans.push_back(make_pair(i, match[i]));
    }
}
return ans;
}
// namespace general_matching

```

4.4 Hungarian algorithm

```

namespace hungary {
    const int N = 210;

    int a[N][N];
    int ans[N];

    int calc(int n, int m) {
        ++n, ++m;
        vector<int> u(n), v(m), p(m), prev(m);
        for (int i = 1; i < n; ++i) {
            p[0] = i;
            int x = 0;
            vector<int> mn(m, INF);
            vector<int> was(m, 0);
            while (p[x]) {
                was[x] = 1;
                int ii = p[x], dd = INF, y = 0;
                for (int j = 1; j < m; ++j)
                    if (!was[j]) {
                        int cur = a[ii][j] - u[ii] - v[j];
                        if (cur < mn[j])
                            mn[j] = cur, prev[j] = x;
                        if (mn[j] < dd)
                            dd = mn[j], y = j;
                    }
                for (int j = 0; j < m; ++j) {
                    if (was[j])
                        u[p[j]] += dd, v[j] -= dd;
                    else
                        mn[j] -= dd;
                }
                x = y;
            }
            while (x) {
                int y = prev[x];
                p[x] = p[y];
                x = y;
            }
            for (int j = 1; j < m; ++j) {
                ans[p[j]] = j;
            }
            return -v[0];
        }
        // How to use:
        // * Set values to a[1..n][1..m] (n <= m)
    }
}

```



```
// * Run calc(n, m) to find minimum
// * Optimal edges are (i, ans[i]) for i = 1..n
// * Everything works on negative numbers
//
// !!! I don't understand this code, it's
// ↪ cypasted from e-maxx
} // namespace hungary
```

4.5 Link-Cut Tree

```
#include <cassert>
#include <cstdio>
#include <iostream>

using namespace std;

// BEGIN ALGO

const int MAXN = 110000;

typedef struct _node {
    _node *l, *r, *p, *pp;
    int size;
    bool rev;
    _node();
    explicit _node(nullptr_t) {
        l = r = p = pp = this;
        size = rev = 0;
    }
    void push() {
        if (rev) {
            l->rev ^= 1;
            r->rev ^= 1;
            rev = 0;
            swap(l, r);
        }
    }
    void update();
} * node;

node None = new _node(nullptr);
node v2n[MAXN];
_node::_node() {
    l = r = p = pp = None;
    size = 1;
    rev = false;
}

void _node::update() {
    size = (this != None) + l->size + r->size;
    l->p = r->p = this;
}

void rotate(node v) {
    assert(v != None && v->p != None);
    assert(!v->rev);
    assert(!v->p->rev);
    node u = v->p;
    if (v == u->l)
        u->l = v->r, v->r = u;
    else
        u->r = v->l, v->l = u;
    swap(u->p, v->p);
    swap(v->pp, u->pp);
}
```

```
if (v->p != None) {
    assert(v->p->l == u || v->p->r == u);
    if (v->p->r == u)
        v->p->r = v;
    else
        v->p->l = v;
}
u->update();
v->update();
}

void bigRotate(node v) {
    assert(v->p != None);
    v->p->p->push();
    v->p->push();
    v->push();
    if (v->p->p != None) {
        if ((v->p->l == v) ^ (v->p->p->r == v->p))
            rotate(v->p);
        else
            rotate(v);
    }
    rotate(v);
}

inline void Splay(node v) {
    while (v->p != None)
        bigRotate(v);
}

inline void splitAfter(node v) {
    v->push();
    Splay(v);
    v->r->p = None;
    v->r->pp = v;
    v->r = None;
    v->update();
}

void expose(int x) {
    node v = v2n[x];
    splitAfter(v);
    while (v->pp != None) {
        assert(v->p == None);
        splitAfter(v->pp);
        assert(v->pp->r == None);
        assert(v->pp->p == None);
        assert(!v->pp->rev);
        v->pp->r = v;
        v->pp->update();
        v = v->pp;
        v->r->pp = None;
    }
    assert(v->p == None);
    Splay(v2n[x]);
}

inline void makeRoot(int x) {
    expose(x);
    assert(v2n[x]->p == None);
    assert(v2n[x]->pp == None);
    assert(v2n[x]->r == None);
    v2n[x]->rev ^= 1;
}

inline void link(int x, int y) {
    makeRoot(x);
    v2n[x]->pp = v2n[y];
}
```

```

}
inline void cut(int x, int y) {
| expose(x);
| Splay(v2n[y]);
| if (v2n[y]->pp != v2n[x]) {
| | swap(x, y);
| | expose(x);
| | Splay(v2n[y]);
| | assert(v2n[y]->pp == v2n[x]);
| }
| v2n[y]->pp = None;
}
inline int get(int x, int y) {
| if (x == y)
| | return 0;
| makeRoot(x);
| expose(y);
| expose(x);
| Splay(v2n[y]);
| if (v2n[y]->pp != v2n[x])
| | return -1;
| return v2n[y]->size;
}

// END ALGO

_node mem[MAXN];

int main() {
| freopen("linkcut.in", "r", stdin);
| freopen("linkcut.out", "w", stdout);

| int n, m;
| scanf("%d %d", &n, &m);

| for (int i = 0; i < n; i++)
| | v2n[i] = &mem[i];

| for (int i = 0; i < m; i++) {
| | int a, b;
| | if (scanf(" link %d %d", &a, &b) == 2)
| | | link(a - 1, b - 1);
| | else if (scanf(" cut %d %d", &a, &b) == 2)
| | | cut(a - 1, b - 1);
| | else if (scanf(" get %d %d", &a, &b) == 2)
| | | printf("%d\n", get(a - 1, b - 1));
| | else
| | | assert(false);
| }
| return 0;
}

void read() {
| int m;
| scanf("%d%d", &n, &m);
| for(i, m) {
| | int x, y;
| | scanf("%d%d", &x, &y);
| | --x, --y;
| | v[x].pb(y);
| | vrev[y].pb(x);
| }
}

int deg[N], cnt[N], used[N], f[N];
int q[N], st, en;

set<int> s[N];

void calc() {
| for (int x = 0; x < n; ++x)
| | f[x] = -1, cnt[x] = 0;
| int val = 0;
| while (1) {
| | st = en = 0;
| | for (int x = 0; x < n; ++x) {
| | | deg[x] = 0;
| | | used[x] = 0;
| | | for (int y : v[x])
| | | | if (f[y] == -1)
| | | | | deg[x]++;
| | }
| | for (int x = 0; x < n; ++x)
| | | if (!deg[x] && f[x] == -1 && cnt[x] ==
| | | | val) {
| | | | q[en++] = x;
| | | | f[x] = val;
| | | }
| | if (!en)
| | | break;
| | while (st < en) {
| | | int x = q[st];
| | | st++;
| | | for (int y : vrev[x]) {
| | | | if (used[y] == 0 && f[y] == -1) {
| | | | | used[y] = 1;
| | | | | cnt[y]++;
| | | | | for (int z : vrev[y]) {
| | | | | | deg[z]--;
| | | | | | if (f[z] == -1 && deg[z] == 0 &&
| | | | | | | cnt[z] == val) {
| | | | | | | | f[z] = val;
| | | | | | | | q[en++] = z;
| | | | | }
| | | }
| | }
| | }
| | val++;
| }
| for (int x = 0; x < n; ++x)
| | eprintf("%d%c", f[x], " \n"[x + 1 == n]);
| for (int x = 0; x < n; ++x)

```

4.6 Smith algorithm (Game on cyclic graph)

```
const int N = 1e5 + 10;
```

```

struct graph {
| int n;

| vi v[N];
| vi vrev[N];

```

```

| | | if (f[x] == -1) {
| | | | for (int y : v[x])
| | | | | if (f[y] != -1)
| | | | | s[x].insert(f[y]);
| | | }
| }
} g1, g2;

```

```

string get(int x, int y) {
| int f1 = g1.f[x], f2 = g2.f[y];
| if (f1 == -1 && f2 == -1)
| | return "draw";
| if (f1 == -1) {
| | if (g1.s[x].count(f2))
| | | return "first";
| | return "draw";
| }
| if (f2 == -1) {
| | if (g2.s[y].count(f1))
| | | return "first";
| | return "draw";
| }
| if (f1 ^ f2)
| | return "first";
| return "second";
}

```

4.7 Stoer-Vagner algorithm (Global min-cut)

```

const int MAXN = 500;
int n, g[MAXN][MAXN];
int best_cost = 1000000000;
vector<int> best_cut;

void mincut() {
| vector<int> v[MAXN];
| for (int i = 0; i < n; ++i)
| | v[i].assign(1, i);
| int w[MAXN];
| bool exist[MAXN], in_a[MAXN];
| memset(exist, true, sizeof exist);
| for (int ph = 0; ph < n - 1; ++ph) {
| | memset(in_a, false, sizeof in_a);
| | memset(w, 0, sizeof w);
| | for (int it = 0, prev; it < n - ph; ++it) {
| | | int sel = -1;
| | | for (int i = 0; i < n; ++i)
| | | | if (exist[i] && !in_a[i] && (sel == -1 ||
| | | | | ↪ w[i] > w[sel]))
| | | | | sel = i;
| | | if (it == n - ph - 1) {
| | | | if (w[sel] < best_cost)
| | | | | best_cost = w[sel], best_cut = v[sel];
| | | | v[prev].insert(v[prev].end(),
| | | | | ↪ v[sel].begin(), v[sel].end());
| | | | for (int i = 0; i < n; ++i)
| | | | | g[prev][i] = g[i][prev] += g[sel][i];
| | | | exist[sel] = false;
| | | } else {
| | | | in_a[sel] = true;

```

```

| | | for (int i = 0; i < n; ++i)
| | | | w[i] += g[sel][i];
| | | prev = sel;
| | | }
| | }
| }
}

```

5 Matroids

5.1 Matroids intersection

```

// check(ctaken, 1) -- first matroid
// check(ctaken, 2) -- second matroid
vector<char> taken(m);
while (1) {
| vector<vector<int>> e(m);
| for (int i = 0; i < m; i++) {
| | for (int j = 0; j < m; j++) {
| | | if (taken[i] && !taken[j]) {
| | | | auto ctaken = taken;
| | | | ctaken[i] = 0;
| | | | ctaken[j] = 1;
| | | | if (check(ctaken, 2)) {
| | | | | e[i].push_back(j);
| | | | }
| | | }
| | }
| | if (!taken[i] && taken[j]) {
| | | auto ctaken = taken;
| | | ctaken[i] = 1;
| | | ctaken[j] = 0;
| | | if (check(ctaken, 1)) {
| | | | e[i].push_back(j);
| | | }
| | }
| }
vector<int> type(m);
// 0 -- cant, 1 -- can in \2, 2 -- can in \1
for (int i = 0; i < m; i++) {
| if (!taken[i]) {
| | auto ctaken = taken;
| | ctaken[i] = 1;
| | if (check(ctaken, 2))
| | | type[i] |= 1;
| }
| if (!taken[i]) {
| | auto ctaken = taken;
| | ctaken[i] = 1;
| | if (check(ctaken, 1))
| | | type[i] |= 2;
| }
}
vector<int> w(m);
for (int i = 0; i < m; i++) {
| w[i] = taken[i] ? ed[i].c : -ed[i].c;
}
vector<pair<int, int>> d(m, {INF, 0});
for (int i = 0; i < m; i++) {
| if (type[i] & 1)
| | d[i] = {w[i], 0};

```

```

| }
| vector<int> pr(m, -1);
| while (1) {
| | vector<pair<int, int>> nd = d;
| | for (int i = 0; i < m; i++) {
| | | if (d[i].first == INF)
| | | | continue;
| | | for (int to : e[i]) {
| | | | if (nd[to] > make_pair(d[i].first +
| | | | | ↪ w[to], d[i].second + 1)) {
| | | | | nd[to] = make_pair(d[i].first + w[to],
| | | | | ↪ d[i].second + 1);
| | | | | pr[to] = i;
| | | | }
| | | }
| | }
| | if (d == nd)
| | | break;
| | d = nd;
| }
| int v = -1;
| for (int i = 0; i < m; i++) {
| | if ((d[i].first < INF && (type[i] & 2)) &&
| | | ↪ (v == -1 || d[i] < d[v]))
| | | v = i;
| }
| if (v == -1)
| | break;
| while (v != -1) {
| | sum += w[v];
| | taken[v] ^= 1;
| | v = pr[v];
| }
| ans[--cnt] = sum;
| }

```

6 Numeric

```

// finds first solution of (p + step * x) % mod <
↪ l
// returns value of (p + step * x), i.e. number
↪ of steps x = (ans - p) / step (mod mod)
int smart_calc(int mod, int step, int l, int p) {
| if (p < l) {
| | return p;
| }
| int d = (mod - p + step - 1) / step;
| int np = (p + d * step) % mod;
| if (np < l) {
| | return np;
| }
| int res = smart_calc(step, mod % step, l, l +
| | ↪ step - 1 - np);
| return l - 1 - res;
| }

```

6.1 Berlekamp-Massey Algorithm

```

vector<int> berlekamp(vector<int> s) {
| int l = 0;
| vector<int> la(1, 1);
| vector<int> b(1, 1);
| for (int r = 1; r <= (int)s.size(); r++) {
| | int delta = 0;
| | for (int j = 0; j <= l; j++) {
| | | delta = (delta + 1LL * s[r - 1 - j] *
| | | | ↪ la[j]) % MOD;
| | }
| | b.insert(b.begin(), 0);
| | if (delta != 0) {
| | | vector<int> t(max(la.size(), b.size()));
| | | for (int i = 0; i < (int)t.size(); i++) {
| | | | if (i < (int)la.size())
| | | | | t[i] = (t[i] + la[i]) % MOD;
| | | | if (i < (int)b.size())
| | | | | t[i] = (t[i] - 1LL * delta * b[i] % MOD
| | | | | ↪ + MOD) % MOD;
| | | }
| | | if (2 * l <= r - 1) {
| | | | b = la;
| | | | int od = inv(delta);
| | | | for (int &x : b)
| | | | | x = 1LL * x * od % MOD;
| | | | l = r - 1;
| | | }
| | | la = t;
| | }
| }
| assert((int)la.size() == l + 1);
| assert(l * 2 + 30 < (int)s.size());
| reverse(la.begin(), la.end());
| return la;
| }

```

```

vector<int> mul(vector<int> a, vector<int> b) {
| vector<int> c(a.size() + b.size() - 1);
| for (int i = 0; i < (int)a.size(); i++) {
| | for (int j = 0; j < (int)b.size(); j++) {
| | | c[i + j] = (c[i + j] + 1LL * a[i] * b[j]) %
| | | | ↪ MOD;
| | }
| }
| vector<int> res(c.size());
| for (int i = 0; i < (int)res.size(); i++)
| | res[i] = c[i] % MOD;
| return res;
| }

```

```

vector<int> mod(vector<int> a, vector<int> b) {
| if (a.size() < b.size())
| | a.resize(b.size() - 1);

| int o = inv(b.back());
| for (int i = (int)a.size() - 1; i >=
| | ↪ (int)b.size() - 1; i--) {
| | | if (a[i] == 0)
| | | | continue;
| | | int coef = 1LL * o * (MOD - a[i]) % MOD;

```

```

| | for (int j = 0; j < (int)b.size(); j++) {
| | | a[i - (int)b.size() + 1 + j] =
| | | | (a[i - (int)b.size() + 1 + j] + 1LL *
| | | |   ↪ coef * b[j]) % MOD;
| | }
| }
| while (a.size() >= b.size()) {
| | assert(a.back() == 0);
| | a.pop_back();
| }
| return a;
}

```

```

vector<int> bin(int n, vector<int> p) {
| vector<int> res(1, 1);
| vector<int> a(2);
| a[1] = 1;
| while (n) {
| | if (n & 1)
| | | res = mod(mul(res, a), p);
| | a = mod(mul(a, a), p);
| | n >>= 1;
| }
| return res;
}

```

```

int f(vector<int> t, int m) {
| vector<int> v = berlekamp(t);
| vector<int> o = bin(m - 1, v);
| int res = 0;
| for (int i = 0; i < (int)o.size(); i++)
| | res = (res + 1LL * o[i] * t[i]) % MOD;
| return res;
}

```

6.2 Chinese remainder theorem

```

int CRT(int a1, int m1, int a2, int m2) {
| return (a1 - a2 % m1 + m1) * (ll)rev(m2, m1) %
|   ↪ m1 * m2 + a2;
}

```

6.3 Miller–Rabin primality test

```

// assume p > 1
bool isprime(ll p) {
| const int a[] = {2, 3, 5, 7, 11, 13, 17, 19,
|   ↪ 23, 0};
| ll d = p - 1;
| int cnt = 0;
| while (!(d & 1)) {
| | d >>= 1;
| | cnt++;
| }
| for (int i = 0; a[i]; i++) {
| | if (p == a[i]) {
| | | return true;
| | }
| | if (!(p % a[i])) {
| | | return false;
| | }
| }

```

```

| | }
| }
| for (int i = 0; a[i]; i++) {
| | ll cur = mpow(a[i], d, p); // a[i]^d (mod
| |   ↪ p)
| | if (cur == 1) {
| | | continue;
| | }
| | bool good = false;
| | for (int j = 0; j < cnt; j++) {
| | | if (cur == p - 1) {
| | | | good = true;
| | | | break;
| | | }
| | | cur = mult(cur, cur);
| | }
| | if (!good) {
| | | return false;
| | }
| }
| return true;
}

```

6.4 Multiplication by modulo

```

ll mul(ll a, ll b, ll m) { // works for MOD 8e18
| ll k = (ll)((long double)a * b / m);
| ll r = a * b - m * k;
| if (r < 0)
| | r += m;
| if (r >= m)
| | r -= m;
| return r;
}

```

6.5 Numerical integration

```

function<dbl>(dbl, dbl, function<dbl>(dbl))> f =
|   ↪ [&](dbl L, dbl R, function<dbl>(dbl) g) {
| | const int ITERS = 1000000;
| | dbl ans = 0;
| | dbl step = (R - L) * 1.0 / ITERS;
| | for (int it = 0; it < ITERS; it++) {
| | | double x1 = L + step * it;
| | | double xr = L + step * (it + 1);
| | | dbl x1 = (x1 + xr) / 2;
| | | dbl x0 = x1 - (x1 - x1) * sqrt(3.0 / 5);
| | | dbl x2 = x1 + (x1 - x1) * sqrt(3.0 / 5);
| | | ans += (5 * g(x0) + 8 * g(x1) + 5 * g(x2)) /
| | |   ↪ 18 * step;
| | }
| | return ans;
| }
};

```

6.6 Pollard's rho algorithm

```

namespace pollard {
using math::p;

```

```

vector<pair<ll, int>> getFactors(ll N) {
| vector<ll> primes;

| const int MX = 1e5;
| const ll MX2 = MX * (ll)MX;

| assert(MX <= math::maxP && math::pc > 0);

| function<void(ll)> go = [&go, &primes](ll n) {
| | for (ll x : primes)
| | | while (n % x == 0)
| | | | n /= x;
| | | if (n == 1)
| | | | return;
| | | if (n > MX2) {
| | | | auto F = [&](ll x) {
| | | | | ll k = ((long double)x * x) / n;
| | | | | ll r = (x * x - k * n + 3) % n;
| | | | | return r < 0 ? r + n : r;
| | | | };
| | | | ll x = mt19937_64()() % n, y = x;
| | | | const int C = 3 * pow(n, 0.25);

| | | | ll val = 1;
| | | | forn(it, C) {
| | | | | x = F(x), y = F(F(y));
| | | | | if (x == y)
| | | | | | continue;
| | | | | ll delta = abs(x - y);
| | | | | ll k = ((long double)val * delta) / n;
| | | | | val = (val * delta - k * n) % n;
| | | | | if (val < 0)
| | | | | | val += n;
| | | | | if (val == 0) {
| | | | | | ll g = __gcd(delta, n);
| | | | | | go(g), go(n / g);
| | | | | | return;
| | | | | }
| | | | | if ((it & 255) == 0) {
| | | | | | ll g = __gcd(val, n);
| | | | | | if (g != 1) {
| | | | | | | go(g), go(n / g);
| | | | | | | return;
| | | | | | }
| | | | | }
| | | }
| | }
| primes.pb(n);
| };

| ll n = N;

| for (int i = 0; i < math::pc && p[i] < MX; ++i)
| | if (n % p[i] == 0) {
| | | primes.pb(p[i]);
| | | while (n % p[i] == 0)
| | | | n /= p[i];
| | }

| go(n);

| sort(primes.begin(), primes.end());

```

```

| vector<pair<ll, int>> res;
| for (ll x : primes) {
| | int cnt = 0;
| | while (N % x == 0) {
| | | cnt++;
| | | N /= x;
| | }
| | res.push_back({x, cnt});
| }
| return res;
| }
| } // namespace pollard

```

6.7 Polynom division and inversion

```

poly inv(poly A, int n) // returns  $A^{-1} \bmod x^n$ 
{
| assert(sz(A) && A[0] != 0);
| A.cut(n);

| auto cutPoly = [](poly &from, int l, int r) {
| | poly R;
| | R.v.resize(r - l);
| | for (int i = l; i < r; ++i) {
| | | if (i < sz(from))
| | | | R[i - l] = from[i];
| | }
| | return R;
| };

| function<int(int, int)> rev = [&rev](int x, int
|   ↪ m) -> int {
| | if (x == 1)
| | | return 1;
| | return (1 - rev(m % x, x) * (ll)m) / x + m;
| };

| poly R({rev(A[0], mod)});
| for (int k = 1; k < n; k <= 1) {
| | poly A0 = cutPoly(A, 0, k);
| | poly A1 = cutPoly(A, k, 2 * k);
| | poly H = A0 * R;
| | H = cutPoly(H, k, 2 * k);
| | poly R1 = (((A1 * R).cut(k) + H) * (poly({0})
|   ↪ - R)).cut(k);
| | R.v.resize(2 * k);
| | forn(i, k) R[i + k] = R1[i];
| | }
| return R.cut(n).norm();
| }

pair<poly, poly> divide(poly A, poly B) {
| if (sz(A) < sz(B))
| | return {poly({0}), A};

| auto rev = [](poly f) {
| | reverse(all(f.v));
| | return f;
| };

```

```

| poly q =
| | rev((inv(rev(B), sz(A) - sz(B) + 1) *
| |   ↪ rev(A)).cut(sz(A) - sz(B) + 1));
| poly r = A - B * q;

| return {q, r};
}

```

6.8 Simplex method

```

vector<double> simplex(vector<vector<double>> a)
↪ {
| int n = a.size() - 1;
| int m = a[0].size() - 1;
| vector<int> left(n + 1), up(m + 1);
| iota(up.begin(), up.end(), 0);
| iota(left.begin(), left.end(), m);
| auto pivot = [&](int x, int y) {
| | swap(left[x], up[y]);
| | double k = a[x][y];
| | a[x][y] = 1;
| | vector<int> vct;
| | for (int j = 0; j <= m; j++) {
| | | a[x][j] /= k;
| | | if (!eq(a[x][j], 0))
| | | | vct.push_back(j);
| | }
| | for (int i = 0; i <= n; i++) {
| | | if (eq(a[i][y], 0) || i == x)
| | | | continue;
| | | k = a[i][y];
| | | a[i][y] = 0;
| | | for (int j : vct)
| | | | a[i][j] -= k * a[x][j];
| | }
| };
| while (1) {
| | int x = -1;
| | for (int i = 1; i <= n; i++)
| | | if (ls(a[i][0], 0) && (x == -1 || a[i][0] <
| | |   ↪ a[x][0]))
| | | | x = i;
| | | if (x == -1)
| | | | break;
| | | int y = -1;
| | | for (int j = 1; j <= m; j++)
| | | | if (ls(a[x][j], 0) && (y == -1 || a[x][j] <
| | | |   ↪ a[x][y]))
| | | | | y = j;
| | | if (y == -1)
| | | | assert(0); // infeasible
| | | pivot(x, y);
| | }
| while (1) {
| | int y = -1;
| | for (int j = 1; j <= m; j++)
| | | if (ls(0, a[0][j]) && (y == -1 || a[0][j] >
| | |   ↪ a[0][y]))
| | | | y = j;
| | | if (y == -1)
| | | | break;

```

```

| | int x = -1;
| | for (int i = 1; i <= n; i++)
| | | if (ls(0, a[i][y]) && (x == -1 || a[i][0] /
| | |   ↪ a[i][y] < a[x][0] / a[x][y]))
| | | | x = i;
| | | if (x == -1)
| | | | assert(0); // unbounded
| | | pivot(x, y);
| | }
| vector<double> ans(m + 1);
| for (int i = 1; i <= n; i++)
| | if (left[i] <= m)
| | | ans[left[i]] = a[i][0];
| ans[0] = -a[0][0];
| return ans;
}
// j=1..m: x[j]>=0
// i=1..n: sum(j=1..m) A[i][j]*x[j] <= A[i][0]
// max sum(j=1..m) A[0][j]*x[j]
// res[0] is answer
// res[1..m] is certificate

```

7 Strings

7.1 Duval algorithm (Lyndon factorization)

```

void duval(string s) {
| int n = (int)s.length();
| int i = 0;
| while (i < n) {
| | int j = i + 1, k = i;
| | while (j < n && s[k] <= s[j]) {
| | | if (s[k] < s[j])
| | | | k = i;
| | | else
| | | | ++k;
| | | ++j;
| | }
| | while (i <= k) {
| | | cout << s.substr(i, j - k) << ' ';
| | | i += j - k;
| | }
| }
}

```

7.2 Palindromic tree

```

namespace eertree {
const int INF = 1e9;
const int N = 5e6 + 10;
char _s[N];
char *s = _s + 1;
int to[N][2];
int suf[N], len[N];
int sz, last;

const int odd = 1, even = 2, blank = 3;

void go(int &u, int pos) {

```

```

| while (u != blank && s[pos - len[u] - 1] !=
  ↳ s[pos]) {
| | u = suf[u];
| }
}

int add(int pos) {
| go(last, pos);
| int u = suf[last];
| go(u, pos);
| int c = s[pos] - 'a';
| int res = 0;
| if (!to[last][c]) {
| | res = 1;
| | to[last][c] = sz;
| | len[sz] = len[last] + 2;
| | suf[sz] = to[u][c];
| | sz++;
| }
| last = to[last][c];
| return res;
}

void init() {
| to[blank][0] = to[blank][1] = even;
| len[blank] = suf[blank] = INF;
| len[even] = 0, suf[even] = odd;
| len[odd] = -1, suf[odd] = blank;
| last = even;
| sz = 4;
}
} // namespace eertree

```

7.3 Suffix automaton

```

struct state {
| state() { std::fill(next, next + 26, -1); }

| int len = 0, link = -1;
| bool term = false;

| int next[26];
};

vector<state> st;
int last;

void sa_init() {
| last = 0;
| st.clear();
| st.resize(1);
}

void sa_extend(char c) {
| int cur = st.size();
| st.resize(st.size() + 1);

| st[cur].len = st[last].len + 1;
| int p;
| for (p = last; p != -1 && st[p].next[c - 'a']
  ↳ == -1; p = st[p].link)

```

```

| | st[p].next[c - 'a'] = cur;
| if (p == -1)
| | st[cur].link = 0;
| else {
| | int q = st[p].next[c - 'a'];
| | if (st[p].len + 1 == st[q].len)
| | | st[cur].link = q;
| | else {
| | | int clone = st.size();
| | | st.resize(st.size() + 1);
| | | st[clone].len = st[p].len + 1;
| | | std::copy(st[q].next, st[q].next + 26,
  ↳ st[clone].next);
| | | st[clone].link = st[q].link;
| | | for (; p != -1 && st[p].next[c - 'a'] == q;
  ↳ p = st[p].link)
| | | | st[p].next[c - 'a'] = clone;
| | | st[q].link = st[cur].link = clone;
| | }
| }
| last = cur;
}

for (int v = last; v != -1; v = st[v].link) //
  ↳ set termination flag.
| st[v].term = 1;

```

7.4 Suffix tree

```

#include <bits/stdc++.h>

using namespace std;

#define forn(i, n) for (int i = 0; i < (int)(n);
  ↳ i++)

const int N = 1e5, VN = 2 * N;

char s[N + 1];
map<char, int> t[VN];
int l[VN], r[VN], p[VN]; // edge p[v] -> v
  ↳ matches to [l[v], r[v]] of string
int cc, n, suf[VN], vn = 2, v = 1, pos; // going
  ↳ by edge from p[v] to v, now standing in pos

void go(int v) {
| int no = cc++;
| for (auto p : t[v]) {
| | v = p.second;
| | printf("%d %d %d\n", no, l[v], min(n, r[v]));
| | go(v);
| }
}

int main() {
| assert(freopen("suftree.in", "r", stdin));
| assert(freopen("suftree.out", "w", stdout));

| gets(s);
| forn(i, 127) t[0][i] = 1; // 0 = fictitious, 1
  ↳ = root

```



```
| l[1] = -1;
| for (n = 0; s[n]; n++) {
| | char c = s[n];
| | auto new_leaf = [&](int v) {
| | | p[vn] = v, l[vn] = n, r[vn] = N, t[v][c] =
| | |     ↪ vn++;
| | };
| go;;
| if (r[v] <= pos) {
| | if (!t[v].count(c)) {
| | | new_leaf(v), v = suf[v], pos = r[v];
| | | goto go;
| | }
| | v = t[v][c], pos = l[v] + 1;
| } else if (c == s[pos]) {
| | pos++;
| } else {
| | int x = vn++;
| | l[x] = l[v], r[x] = pos, l[v] = pos;
| | p[x] = p[v], p[v] = x;
| | t[p[x]][s[l[x]]] = x, t[x][s[pos]] = v;
| | new_leaf(x);
| | v = suf[p[x]], pos = l[x];
| | while (pos < r[x])
| | | v = t[v][s[pos]], pos += r[v] - l[v];
| | suf[x] = (pos == r[x] ? v : vn);
| | pos = r[v] - (pos - r[x]);
| | goto go;
| }
| }
| printf("%d\n", vn - 1);
| go(1);
| }
```

Table of Integrals*

Basic Forms

$$\int x^n dx = \frac{1}{n+1} x^{n+1} \quad (1)$$

$$\int \frac{1}{x} dx = \ln |x| \quad (2)$$

$$\int u dv = uv - \int v du \quad (3)$$

$$\int \frac{1}{ax+b} dx = \frac{1}{a} \ln |ax+b| \quad (4)$$

Integrals of Rational Functions

$$\int \frac{1}{(x+a)^2} dx = -\frac{1}{x+a} \quad (5)$$

$$\int (x+a)^n dx = \frac{(x+a)^{n+1}}{n+1}, n \neq -1 \quad (6)$$

$$\int x(x+a)^n dx = \frac{(x+a)^{n+1}((n+1)x-a)}{(n+1)(n+2)} \quad (7)$$

$$\int \frac{1}{1+x^2} dx = \tan^{-1} x \quad (8)$$

$$\int \frac{1}{a^2+x^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a} \quad (9)$$

$$\int \frac{x}{a^2+x^2} dx = \frac{1}{2} \ln |a^2+x^2| \quad (10)$$

$$\int \frac{x^2}{a^2+x^2} dx = x - a \tan^{-1} \frac{x}{a} \quad (11)$$

$$\int \frac{x^3}{a^2+x^2} dx = \frac{1}{2} x^2 - \frac{1}{2} a^2 \ln |a^2+x^2| \quad (12)$$

$$\int \frac{1}{ax^2+bx+c} dx = \frac{2}{\sqrt{4ac-b^2}} \tan^{-1} \frac{2ax+b}{\sqrt{4ac-b^2}} \quad (13)$$

$$\int \frac{1}{(x+a)(x+b)} dx = \frac{1}{b-a} \ln \frac{a+x}{b+x}, a \neq b \quad (14)$$

$$\int \frac{x}{(x+a)^2} dx = \frac{a}{a+x} + \ln |a+x| \quad (15)$$

$$\int \frac{x}{ax^2+bx+c} dx = \frac{1}{2a} \ln |ax^2+bx+c| - \frac{b}{a\sqrt{4ac-b^2}} \tan^{-1} \frac{2ax+b}{\sqrt{4ac-b^2}} \quad (16)$$

Integrals with Roots

$$\int \sqrt{x-a} dx = \frac{2}{3} (x-a)^{3/2} \quad (17)$$

$$\int \frac{1}{\sqrt{x \pm a}} dx = 2\sqrt{x \pm a} \quad (18)$$

$$\int \frac{1}{\sqrt{a-x}} dx = -2\sqrt{a-x} \quad (19)$$

$$\int x\sqrt{x-a} dx = \frac{2}{3} a(x-a)^{3/2} + \frac{2}{5} (x-a)^{5/2} \quad (20)$$

$$\int \sqrt{ax+bd} dx = \left(\frac{2b}{3a} + \frac{2x}{3} \right) \sqrt{ax+b} \quad (21)$$

$$\int (ax+b)^{3/2} dx = \frac{2}{5a} (ax+b)^{5/2} \quad (22)$$

$$\int \frac{x}{\sqrt{x \pm a}} dx = \frac{2}{3} (x \mp 2a) \sqrt{x \pm a} \quad (23)$$

$$\int \sqrt{\frac{x}{a-x}} dx = -\sqrt{x(a-x)} - a \tan^{-1} \frac{\sqrt{x(a-x)}}{x-a} \quad (24)$$

$$\int \sqrt{\frac{x}{a+x}} dx = \sqrt{x(a+x)} - a \ln [\sqrt{x} + \sqrt{x+a}] \quad (25)$$

$$\int x\sqrt{ax+bd} dx = \frac{2}{15a^2} (-2b^2 + abx + 3a^2x^2) \sqrt{ax+b} \quad (26)$$

$$\int \sqrt{x(ax+b)} dx = \frac{1}{4a^{3/2}} \left[(2ax+b) \sqrt{ax(ax+b)} - b^2 \ln |a\sqrt{x} + \sqrt{a(ax+b)}| \right] \quad (27)$$

$$\int \sqrt{x^3(ax+b)} dx = \left[\frac{b}{12a} - \frac{b^2}{8a^2x} + \frac{x}{3} \right] \sqrt{x^3(ax+b)} + \frac{b^3}{8a^{5/2}} \ln |a\sqrt{x} + \sqrt{a(ax+b)}| \quad (28)$$

$$\int \sqrt{x^2 \pm a^2} dx = \frac{1}{2} x \sqrt{x^2 \pm a^2} \pm \frac{1}{2} a^2 \ln |x + \sqrt{x^2 \pm a^2}| \quad (29)$$

$$\int \sqrt{a^2 - x^2} dx = \frac{1}{2} x \sqrt{a^2 - x^2} + \frac{1}{2} a^2 \tan^{-1} \frac{x}{\sqrt{a^2 - x^2}} \quad (30)$$

$$\int x\sqrt{x^2 \pm a^2} dx = \frac{1}{3} (x^2 \pm a^2)^{3/2} \quad (31)$$

$$\int \frac{1}{\sqrt{x^2 \pm a^2}} dx = \ln |x + \sqrt{x^2 \pm a^2}| \quad (32)$$

$$\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a} \quad (33)$$

$$\int \frac{x}{\sqrt{x^2 \pm a^2}} dx = \sqrt{x^2 \pm a^2} \quad (34)$$

$$\int \frac{x}{\sqrt{a^2 - x^2}} dx = -\sqrt{a^2 - x^2} \quad (35)$$

$$\int \frac{x^2}{\sqrt{x^2 \pm a^2}} dx = \frac{1}{2} x \sqrt{x^2 \pm a^2} \mp \frac{1}{2} a^2 \ln |x + \sqrt{x^2 \pm a^2}| \quad (36)$$

$$\int \sqrt{ax^2+bx+cd} dx = \frac{b+2ax}{4a} \sqrt{ax^2+bx+c} + \frac{4ac-b^2}{8a^{3/2}} \ln |2ax+b+2\sqrt{a(ax^2+bx+c)}| \quad (37)$$

$$\int x\sqrt{ax^2+bx+c} dx = \frac{1}{48a^{5/2}} \left(2\sqrt{a}\sqrt{ax^2+bx+c} \times (-3b^2+2abx+8a(c+ax^2)) + 3(b^3-4abc) \ln |b+2ax+2\sqrt{a}\sqrt{ax^2+bx+c}| \right) \quad (38)$$

$$\int \frac{1}{\sqrt{ax^2+bx+c}} dx = \frac{1}{\sqrt{a}} \ln |2ax+b+2\sqrt{a(ax^2+bx+c)}| \quad (39)$$

$$\int \frac{x}{\sqrt{ax^2+bx+c}} dx = \frac{1}{a} \sqrt{ax^2+bx+c} - \frac{b}{2a^{3/2}} \ln |2ax+b+2\sqrt{a(ax^2+bx+c)}| \quad (40)$$

$$\int \frac{dx}{(a^2+x^2)^{3/2}} = \frac{x}{a^2\sqrt{a^2+x^2}} \quad (41)$$

Integrals with Logarithms

$$\int \ln ax dx = x \ln ax - x \quad (42)$$

$$\int \frac{\ln ax}{x} dx = \frac{1}{2} (\ln ax)^2 \quad (43)$$

$$\int \ln(ax+b) dx = \left(x + \frac{b}{a} \right) \ln(ax+b) - x, a \neq 0 \quad (44)$$

$$\int \ln(x^2+a^2) dx = x \ln(x^2+a^2) + 2a \tan^{-1} \frac{x}{a} - 2x \quad (45)$$

$$\int \ln(x^2-a^2) dx = x \ln(x^2-a^2) + a \ln \frac{x+a}{x-a} - 2x \quad (46)$$

$$\int \ln(ax^2+bx+c) dx = \frac{1}{a} \sqrt{4ac-b^2} \tan^{-1} \frac{2ax+b}{\sqrt{4ac-b^2}} - 2x + \left(\frac{b}{2a} + x \right) \ln(ax^2+bx+c) \quad (47)$$

$$\int x \ln(ax+b) dx = \frac{bx}{2a} - \frac{1}{4} x^2 + \frac{1}{2} \left(x^2 - \frac{b^2}{a^2} \right) \ln(ax+b) \quad (48)$$

$$\int x \ln(a^2-b^2x^2) dx = -\frac{1}{2} x^2 + \frac{1}{2} \left(x^2 - \frac{a^2}{b^2} \right) \ln(a^2-b^2x^2) \quad (49)$$

Integrals with Exponentials

$$\int e^{ax} dx = \frac{1}{a} e^{ax} \quad (50)$$

$$\int \sqrt{x} e^{ax} dx = \frac{1}{a} \sqrt{x} e^{ax} + \frac{i\sqrt{\pi}}{2a^{3/2}} \operatorname{erf}(i\sqrt{ax}),$$

where $\operatorname{erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$ (51)

$$\int x e^x dx = (x-1)e^x \quad (52)$$

$$\int x e^{ax} dx = \left(\frac{x}{a} - \frac{1}{a^2} \right) e^{ax} \quad (53)$$

$$\int x^2 e^x dx = (x^2 - 2x + 2) e^x \quad (54)$$

$$\int x^2 e^{ax} dx = \left(\frac{x^2}{a} - \frac{2x}{a^2} + \frac{2}{a^3} \right) e^{ax} \quad (55)$$

$$\int x^3 e^x dx = (x^3 - 3x^2 + 6x - 6) e^x \quad (56)$$

$$\int x^n e^{ax} dx = \frac{x^n e^{ax}}{a} - \frac{n}{a} \int x^{n-1} e^{ax} dx \quad (57)$$

$$\int x^n e^{ax} dx = \frac{(-1)^n}{a^{n+1}} \Gamma[1+n, -ax],$$

where $\Gamma(a, x) = \int_x^\infty t^{a-1} e^{-t} dt$ (58)

$$\int e^{ax^2} dx = -\frac{i\sqrt{\pi}}{2\sqrt{a}} \operatorname{erf}(i\sqrt{a}x) \quad (59)$$

$$\int e^{-ax^2} dx = \frac{\sqrt{\pi}}{2\sqrt{a}} \operatorname{erf}(x\sqrt{a}) \quad (60)$$

$$\int x e^{-ax^2} dx = -\frac{1}{2a} e^{-ax^2} \quad (61)$$

$$\int x^2 e^{-ax^2} dx = \frac{1}{4} \sqrt{\frac{\pi}{a^3}} \operatorname{erf}(x\sqrt{a}) - \frac{x}{2a} e^{-ax^2} \quad (62)$$

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Integrals with Trigonometric Functions

$$\int \sin ax dx = -\frac{1}{a} \cos ax \quad (63)$$

$$\int \sin^2 ax dx = \frac{x}{2} - \frac{\sin 2ax}{4a} \quad (64)$$

$$\int \sin^n ax dx = -\frac{1}{a} \cos ax {}_2F_1 \left[\frac{1}{2}, \frac{1-n}{2}, \frac{3}{2}, \cos^2 ax \right] \quad (65)$$

$$\int \sin^3 ax dx = -\frac{3 \cos ax}{4a} + \frac{\cos 3ax}{12a} \quad (66)$$

$$\int \cos ax dx = \frac{1}{a} \sin ax \quad (67)$$

$$\int \cos^2 ax dx = \frac{x}{2} + \frac{\sin 2ax}{4a} \quad (68)$$

$$\int \cos^p ax dx = -\frac{1}{a(1+p)} \cos^{1+p} ax \times {}_2F_1 \left[\frac{1+p}{2}, \frac{1}{2}, \frac{3+p}{2}, \cos^2 ax \right] \quad (69)$$

$$\int \cos^3 ax dx = \frac{3 \sin ax}{4a} + \frac{\sin 3ax}{12a} \quad (70)$$

$$\int \cos ax \sin bxdx = \frac{\cos[(a-b)x]}{2(a-b)} - \frac{\cos[(a+b)x]}{2(a+b)}, a \neq b \quad (71)$$

$$\int \sin^2 ax \cos bxdx = -\frac{\sin[(2a-b)x]}{4(2a-b)} + \frac{\sin bx}{2b} - \frac{\sin[(2a+b)x]}{4(2a+b)} \quad (72)$$

$$\int \sin^2 x \cos x dx = \frac{1}{3} \sin^3 x \quad (73)$$

$$\int \cos^2 ax \sin bxdx = \frac{\cos[(2a-b)x]}{4(2a-b)} - \frac{\cos bx}{2b} - \frac{\cos[(2a+b)x]}{4(2a+b)} \quad (74)$$

$$\int \cos^2 ax \sin ax dx = -\frac{1}{3a} \cos^3 ax \quad (75)$$

$$\int \sin^2 ax \cos^2 bxdx = \frac{x}{4} - \frac{\sin 2ax}{8a} - \frac{\sin[2(a-b)x]}{16(a-b)} + \frac{\sin 2bx}{8b} - \frac{\sin[2(a+b)x]}{16(a+b)} \quad (76)$$

$$\int \sin^2 ax \cos^2 ax dx = \frac{x}{8} - \frac{\sin 4ax}{32a} \quad (77)$$

$$\int \tan ax dx = -\frac{1}{a} \ln \cos ax \quad (78)$$

$$\int \tan^2 ax dx = -x + \frac{1}{a} \tan ax \quad (79)$$

$$\int \tan^n ax dx = \frac{\tan^{n+1} ax}{a(1+n)} \times {}_2F_1 \left(\frac{n+1}{2}, 1, \frac{n+3}{2}, -\tan^2 ax \right) \quad (80)$$

$$\int \tan^3 ax dx = \frac{1}{a} \ln \cos ax + \frac{1}{2a} \sec^2 ax \quad (81)$$

$$\int \sec x dx = \ln |\sec x + \tan x| = 2 \tanh^{-1} \left(\tan \frac{x}{2} \right) \quad (82)$$

$$\int \sec^2 ax dx = \frac{1}{a} \tan ax \quad (83)$$

$$\int \sec^3 x dx = \frac{1}{2} \sec x \tan x + \frac{1}{2} \ln |\sec x + \tan x| \quad (84)$$

$$\int \sec x \tan x dx = \sec x \quad (85)$$

$$\int \sec^2 x \tan x dx = \frac{1}{2} \sec^2 x \quad (86)$$

$$\int \sec^n x \tan x dx = \frac{1}{n} \sec^n x, n \neq 0 \quad (87)$$

$$\int \csc x dx = \ln \left| \tan \frac{x}{2} \right| = \ln |\csc x - \cot x| + C \quad (88)$$

$$\int \csc^2 ax dx = -\frac{1}{a} \cot ax \quad (89)$$

$$\int \csc^3 x dx = -\frac{1}{2} \cot x \csc x + \frac{1}{2} \ln |\csc x - \cot x| \quad (90)$$

$$\int \csc^n x \cot x dx = -\frac{1}{n} \csc^n x, n \neq 0 \quad (91)$$

$$\int \sec x \csc x dx = \ln |\tan x| \quad (92)$$

Products of Trigonometric Functions and Monomials

$$\int x \cos x dx = \cos x + x \sin x \quad (93)$$

$$\int x \cos ax dx = \frac{1}{a^2} \cos ax + \frac{x}{a} \sin ax \quad (94)$$

$$\int x^2 \cos x dx = 2x \cos x + (x^2 - 2) \sin x \quad (95)$$

$$\int x^2 \cos ax dx = \frac{2x \cos ax}{a^2} + \frac{a^2 x^2 - 2}{a^3} \sin ax \quad (96)$$

$$\int x^n \cos x dx = -\frac{1}{2} (i)^{n+1} [\Gamma(n+1, -ix) + (-1)^n \Gamma(n+1, ix)] \quad (97)$$

$$\int x^n \cos ax dx = \frac{1}{2} (ia)^{1-n} [(-1)^n \Gamma(n+1, -iax) - \Gamma(n+1, iax)] \quad (98)$$

$$\int x \sin x dx = -x \cos x + \sin x \quad (99)$$

$$\int x \sin ax dx = -\frac{x \cos ax}{a} + \frac{\sin ax}{a^2} \quad (100)$$

$$\int x^2 \sin x dx = (2 - x^2) \cos x + 2x \sin x \quad (101)$$

$$\int x^2 \sin ax dx = \frac{2 - a^2 x^2}{a^3} \cos ax + \frac{2x \sin ax}{a^2} \quad (102)$$

$$\int x^n \sin x dx = -\frac{1}{2} (i)^n [\Gamma(n+1, -ix) - (-1)^n \Gamma(n+1, -ix)] \quad (103)$$

Products of Trigonometric Functions and Exponentials

$$\int e^x \sin x dx = \frac{1}{2} e^x (\sin x - \cos x) \quad (104)$$

$$\int e^{bx} \sin ax dx = \frac{1}{a^2 + b^2} e^{bx} (b \sin ax - a \cos ax) \quad (105)$$

$$\int e^x \cos x dx = \frac{1}{2} e^x (\sin x + \cos x) \quad (106)$$

$$\int e^{bx} \cos ax dx = \frac{1}{a^2 + b^2} e^{bx} (a \sin ax + b \cos ax) \quad (107)$$

$$\int x e^x \sin x dx = \frac{1}{2} e^x (\cos x - x \cos x + x \sin x) \quad (108)$$

$$\int x e^x \cos x dx = \frac{1}{2} e^x (x \cos x - \sin x + x \sin x) \quad (109)$$

Integrals of Hyperbolic Functions

$$\int \cosh ax dx = \frac{1}{a} \sinh ax \quad (110)$$

$$\int e^{ax} \cosh bxdx = \begin{cases} \frac{e^{ax}}{a^2 - b^2} [a \cosh bx - b \sinh bx] & a \neq b \\ \frac{e^{2ax}}{4a} + \frac{x}{2} & a = b \end{cases} \quad (111)$$

$$\int \sinh ax dx = \frac{1}{a} \cosh ax \quad (112)$$

$$\int e^{ax} \sinh bxdx = \begin{cases} \frac{e^{ax}}{a^2 - b^2} [-b \cosh bx + a \sinh bx] & a \neq b \\ \frac{e^{2ax}}{4a} - \frac{x}{2} & a = b \end{cases} \quad (113)$$

$$\int e^{ax} \tanh bxdx = \begin{cases} \frac{e^{(a+2b)x}}{(a+2b)} {}_2F_1 \left[1 + \frac{a}{2b}, 1, 2 + \frac{a}{2b}, -e^{2bx} \right] - \frac{1}{a} e^{ax} {}_2F_1 \left[\frac{a}{2b}, 1, 1E, -e^{2bx} \right] & a \neq b \\ \frac{e^{ax} - 2 \tanh^{-1}[e^{ax}]}{a} & a = b \end{cases} \quad (114)$$

$$\int \tanh ax dx = \frac{1}{a} \ln \cosh ax \quad (115)$$

$$\int \cos ax \cosh bxdx = \frac{1}{a^2 + b^2} [a \sin ax \cosh bx + b \cos ax \sinh bx] \quad (116)$$

$$\int \cos ax \sinh bxdx = \frac{1}{a^2 + b^2} [b \cos ax \cosh bx + a \sin ax \sinh bx] \quad (117)$$

$$\int \sin ax \cosh bxdx = \frac{1}{a^2 + b^2} [-a \cos ax \cosh bx + b \sin ax \sinh bx] \quad (118)$$

$$\int \sin ax \sinh bxdx = \frac{1}{a^2 + b^2} [b \cosh bx \sin ax - a \cos ax \sinh bx] \quad (119)$$

$$\int \sinh ax \cosh ax dx = \frac{1}{4a} [-2ax + \sinh 2ax] \quad (120)$$

$$\int \sinh ax \cosh bxdx = \frac{1}{b^2 - a^2} [b \cosh bx \sinh ax - a \cosh ax \sinh bx] \quad (121)$$