

Интегралы и дифференциальные уравнения

Производные (повторение)

$$f'(x_0) = \lim_{\Delta x \rightarrow 0} \frac{f(x_0 + \Delta x) - f(x_0)}{\Delta x} \quad (\ln y)' = \frac{y'}{y}$$

$$(u^v)' = u^v \cdot v' \ln u + u^{v-1} \cdot u' \cdot v \quad \frac{u(x)}{v(x)}$$

Решение задач

~ 1

$$\begin{aligned} y' &= \left(11 \cdot \operatorname{arccotg}^2 \ln \frac{5x + \sqrt{x}}{12x^2 - 5} \right)' = 11 \cdot \left(\operatorname{arccotg}^2 \ln \frac{5x + \sqrt{x}}{12x^2 - 5} \right)' = \\ &= 11 \cdot 2 \operatorname{arccotg}^{2-1} \ln \frac{5x + \sqrt{x}}{12x^2 - 5} \cdot \left(\operatorname{arccotg} \ln \frac{5x + \sqrt{x}}{12x^2 - 5} \right)' = 11 \cdot 2 \cdot \operatorname{arccotg} \ln \frac{5x + \sqrt{x}}{12x^2 - 5} \cdot \\ &\cdot \left(- \frac{1}{1 + \left(\ln \frac{5x + \sqrt{x}}{12x^2 - 5} \right)^2} \right) \cdot \left(\ln \frac{5x + \sqrt{x}}{12x^2 - 5} \right)' = 11 \cdot 2 \cdot \operatorname{arccotg} \ln \frac{5x + \sqrt{x}}{12x^2 - 5} \cdot \\ &\cdot \left(- \frac{1}{1 + \ln^2 \frac{5x + \sqrt{x}}{12x^2 - 5}} \right) \cdot \frac{5x + \sqrt{x}}{12x^2 - 5} \cdot \left(\frac{5x + \sqrt{x}}{12x^2 - 5} \right)' = 11 \cdot 2 \cdot \operatorname{arccotg} \ln \frac{5x + \sqrt{x}}{12x^2 - 5} \cdot \\ &\cdot \left(- \frac{1}{1 + \ln^2 \frac{5x + \sqrt{x}}{12x^2 - 5}} \right) \cdot \frac{12x^2 - 5}{5x + \sqrt{x}} \cdot \frac{(5x + \sqrt{x})' \cdot (12x^2 - 5) - (5x + \sqrt{x}) \cdot (12x^2 - 5)'}{(12x^2 - 5)^2} = \\ &= \frac{(5 + \frac{1}{2\sqrt{x}})(12x^2 - 5) - (5x + \sqrt{x})(24x - 0)}{(12x^2 - 5)^2} = \frac{(5 \cdot 2\sqrt{x} + 1) - 2\sqrt{x}(5x + \sqrt{x}) \cdot 24x}{(12x^2 - 5)^2} = \\ &= \frac{(10\sqrt{x} + 1)(12x^2 - 5) - 48x^2(5\sqrt{x} + 1)}{2\sqrt{x}(12x^2 - 5)^2} = \\ &= \frac{(10\sqrt{x} + 1)(12x^2 - 5) - 48x^2(5\sqrt{x} + 1)}{2\sqrt{x}(12x^2 - 5)^2} = \\ &= \frac{(12x^2 - 5)(10\sqrt{x} + 1)(12x^2 - 5) - 48x^2(5\sqrt{x} + 1)}{(12x^2 - 5)^2} = -22 \cdot \operatorname{arccotg} \ln \frac{5x + \sqrt{x}}{12x^2 - 5} \cdot \frac{1}{1 + \ln^2 \frac{5x + \sqrt{x}}{12x^2 - 5}} \cdot \frac{(12x^2 - 5)(10\sqrt{x} + 1)(12x^2 - 5) - 48x^2(5\sqrt{x} + 1)}{(12x^2 - 5)^2} = \\ &= -22 \cdot \operatorname{arccotg} \ln \frac{5x + \sqrt{x}}{12x^2 - 5} \cdot \frac{1}{1 + \ln^2 \frac{5x + \sqrt{x}}{12x^2 - 5}} \cdot \frac{(12x^2 - 5)(10\sqrt{x} + 1)(12x^2 - 5) - 48x^2(5\sqrt{x} + 1)}{(12x^2 - 5)^2} \end{aligned}$$

$$\cdot \frac{(10\sqrt{x}+1)(12x^2-5) - 48x^2(5\sqrt{x}+1)}{2x(5\sqrt{x}+1)(12x^2-5)} = -11 \cdot \operatorname{arccotg} \ln \frac{5x+\sqrt{x}}{12x^2-5}$$

$$\cdot \frac{1}{1 + \ln^2 \frac{5x+\sqrt{x}}{12x^2-5}} \cdot \frac{(10\sqrt{x}+1)(12x^2-5) - 48x^2(5\sqrt{x}+1)}{(5\sqrt{x}+1)(12x^2-5)x}$$

$$y' = ? \quad y = (x^2 - \sqrt{11}x)^{\operatorname{arcsin}(x^2-1)}$$

$$(\ln y)' = \frac{y'}{y}$$

$$\ln y = (\ln(x^3 - \sqrt{11}x))^{\operatorname{arcsin}(x^2-1)}$$

$$(\ln y)' = (\operatorname{arcsin}(x^2-1))' \cdot (\ln(x^3 - \sqrt{11}x))' = \frac{2x}{\sqrt{1-(x^2-1)^2}} \cdot \ln(x^3 - \sqrt{11}x) + \operatorname{arcsin}(x^2-1) \cdot \frac{1}{x^3 - \sqrt{11}x} \cdot (3x^2 - \frac{\sqrt{11}}{2\sqrt{x}}) \Rightarrow y' = y \cdot * = (x^3 - \sqrt{11}x)^{\operatorname{arcsin}(x^2-1)} \cdot *$$