

$$1) \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} + \begin{pmatrix} b_{11} & b_{12} & \dots & b_{1n} \\ b_{21} & b_{22} & \dots & b_{2n} \\ \dots & \dots & \dots & \dots \\ b_{m1} & b_{m2} & \dots & b_{mn} \end{pmatrix} +$$

$$\begin{pmatrix} c_{11} & c_{12} & \dots & c_{1n} \\ c_{21} & c_{22} & \dots & c_{2n} \\ \dots & \dots & \dots & \dots \\ c_{m1} & c_{m2} & \dots & c_{mn} \end{pmatrix} = \begin{pmatrix} a_{11}+b_{11} & a_{12}+b_{12} & \dots & a_{1n}+b_{1n} \\ a_{21}+b_{21} & a_{22}+b_{22} & \dots & a_{2n}+b_{2n} \\ \dots & \dots & \dots & \dots \\ a_{m1}+b_{m1} & a_{m2}+b_{m2} & \dots & a_{mn}+b_{mn} \end{pmatrix} +$$

$$\begin{pmatrix} a_{11}+b_{11}+c_{11} & a_{12}+b_{12}+c_{12} & \dots & a_{1n}+b_{1n}+c_{1n} \\ a_{21}+b_{21}+c_{21} & a_{22}+b_{22}+c_{22} & \dots & a_{2n}+b_{2n}+c_{2n} \\ \dots & \dots & \dots & \dots \\ a_{m1}+b_{m1}+c_{m1} & a_{m2}+b_{m2}+c_{m2} & \dots & a_{mn}+b_{mn}+c_{mn} \end{pmatrix} \quad \text{I. 7.}$$

$$\begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} + \begin{pmatrix} b_{11} & b_{12} & \dots & b_{1n} \\ b_{21} & b_{22} & \dots & b_{2n} \\ \dots & \dots & \dots & \dots \\ b_{m1} & b_{m2} & \dots & b_{mn} \end{pmatrix} + \begin{pmatrix} c_{11} & c_{12} & \dots & c_{1n} \\ c_{21} & c_{22} & \dots & c_{2n} \\ \dots & \dots & \dots & \dots \\ c_{m1} & c_{m2} & \dots & c_{mn} \end{pmatrix} =$$

$$= \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} + \begin{pmatrix} b_{11}+c_{11} & b_{12}+c_{12} & \dots & b_{1n}+c_{1n} \\ b_{21}+c_{21} & b_{22}+c_{22} & \dots & b_{2n}+c_{2n} \\ \dots & \dots & \dots & \dots \\ b_{m1}+c_{m1} & b_{m2}+c_{m2} & \dots & b_{mn}+c_{mn} \end{pmatrix} =$$

$$= \begin{pmatrix} a_{11}+b_{11}+c_{11} & a_{12}+b_{12}+c_{12} & \dots & a_{1n}+b_{1n}+c_{1n} \\ a_{21}+b_{21}+c_{21} & a_{22}+b_{22}+c_{22} & \dots & a_{2n}+b_{2n}+c_{2n} \\ \dots & \dots & \dots & \dots \\ a_{m1}+b_{m1}+c_{m1} & a_{m2}+b_{m2}+c_{m2} & \dots & a_{mn}+b_{mn}+c_{mn} \end{pmatrix} \quad \text{— np. 7.}$$

I. 7. = np. 7.

7. m. g.

$$2) \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} + \begin{pmatrix} 0 & 0 & \dots & 0 \\ 0 & 0 & \dots & 0 \\ \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & 0 \end{pmatrix} =$$

$$\begin{pmatrix} a_{11}+0 & a_{12}+0 & \dots & a_{1n}+0 \\ a_{21}+0 & a_{22}+0 & \dots & a_{2n}+0 \\ \dots & \dots & \dots & \dots \\ a_{m1}+0 & a_{m2}+0 & \dots & a_{mn}+0 \end{pmatrix} = \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} \quad \text{— I. 7.}$$



$$a_{m1} \ a_{m2} \dots a_{mn} / (1st) a_{m1} \ (1st) a_{m2} \dots (1st) a_{mn}$$

$$\begin{pmatrix} 0 & 0 & \dots & 0 \\ 0 & 0 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & 0 \end{pmatrix} + \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} =$$

$$= \begin{pmatrix} 0+a_{11} & 0+a_{12} & \dots & 0+a_{1n} \\ 0+a_{21} & 0+a_{22} & \dots & 0+a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ 0+a_{m1} & 0+a_{m2} & \dots & 0+a_{mn} \end{pmatrix} = \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} \quad \text{--- np. r.}$$

$$1. r. = \text{np. r.}$$

r. m. g.

$$3) \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} - \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} =$$

$$= \begin{pmatrix} a_{11}-a_{11} & a_{12}-a_{12} & \dots & a_{1n}-a_{1n} \\ a_{21}-a_{21} & a_{22}-a_{22} & \dots & a_{2n}-a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1}-a_{m1} & a_{m2}-a_{m2} & \dots & a_{mn}-a_{mn} \end{pmatrix} = \begin{pmatrix} 0 & 0 & \dots & 0 \\ 0 & 0 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & 0 \end{pmatrix} \quad \text{--- r. m. g.}$$

$$4) \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} + \begin{pmatrix} b_{11} & b_{12} & \dots & b_{1n} \\ b_{21} & b_{22} & \dots & b_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ b_{m1} & b_{m2} & \dots & b_{mn} \end{pmatrix} =$$

$$= \begin{pmatrix} a_{11}+b_{11} & a_{12}+b_{12} & \dots & a_{1n}+b_{1n} \\ a_{21}+b_{21} & a_{22}+b_{22} & \dots & a_{2n}+b_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1}+b_{m1} & a_{m2}+b_{m2} & \dots & a_{mn}+b_{mn} \end{pmatrix} \quad \text{--- 1. r.}$$

$$\begin{pmatrix} b_{11} & b_{12} & \dots & b_{1n} \\ b_{21} & b_{22} & \dots & b_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ b_{m1} & b_{m2} & \dots & b_{mn} \end{pmatrix} + \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} =$$

$$\begin{pmatrix} b_{11}+a_{11} & b_{12}+a_{12} & \dots & b_{1n}+a_{1n} \\ b_{21}+a_{21} & b_{22}+a_{22} & \dots & b_{2n}+a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ b_{m1}+a_{m1} & b_{m2}+a_{m2} & \dots & b_{mn}+a_{mn} \end{pmatrix} = \begin{pmatrix} a_{11}+b_{11} & a_{12}+b_{12} & \dots & a_{1n}+b_{1n} \\ a_{21}+b_{21} & a_{22}+b_{22} & \dots & a_{2n}+b_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1}+b_{m1} & a_{m2}+b_{m2} & \dots & a_{mn}+b_{mn} \end{pmatrix} \quad \text{--- np. r.}$$



$$1. \gamma = \text{np. } \gamma.$$

γ.m.g.

5)

$$k \cdot \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} + \begin{pmatrix} b_{11} & b_{12} & \dots & b_{1n} \\ b_{21} & b_{22} & \dots & b_{2n} \\ \dots & \dots & \dots & \dots \\ b_{m1} & b_{m2} & \dots & b_{mn} \end{pmatrix} =$$

$$= k \cdot \begin{pmatrix} a_{11}+b_{11} & a_{12}+b_{12} & \dots & a_{1n}+b_{1n} \\ a_{21}+b_{21} & a_{22}+b_{22} & \dots & a_{2n}+b_{2n} \\ \dots & \dots & \dots & \dots \\ a_{m1}+b_{m1} & a_{m2}+b_{m2} & \dots & a_{mn}+b_{mn} \end{pmatrix} =$$

$$= \begin{pmatrix} k(a_{11}+b_{11}) & k(a_{12}+b_{12}) & \dots & k(a_{1n}+b_{1n}) \\ k(a_{21}+b_{21}) & k(a_{22}+b_{22}) & \dots & k(a_{2n}+b_{2n}) \\ \dots & \dots & \dots & \dots \\ k(a_{m1}+b_{m1}) & k(a_{m2}+b_{m2}) & \dots & k(a_{mn}+b_{mn}) \end{pmatrix} =$$

$$= \begin{pmatrix} ka_{11}+kb_{11} & ka_{12}+kb_{12} & \dots & ka_{1n}+kb_{1n} \\ ka_{21}+kb_{21} & ka_{22}+kb_{22} & \dots & ka_{2n}+kb_{2n} \\ \dots & \dots & \dots & \dots \\ ka_{m1}+kb_{m1} & ka_{m2}+kb_{m2} & \dots & ka_{mn}+kb_{mn} \end{pmatrix} - 1. \gamma$$

$$k \cdot \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} + k \begin{pmatrix} b_{11} & b_{12} & \dots & b_{1n} \\ b_{21} & b_{22} & \dots & b_{2n} \\ \dots & \dots & \dots & \dots \\ b_{m1} & b_{m2} & \dots & b_{mn} \end{pmatrix} =$$

$$= \begin{pmatrix} ka_{11} & ka_{12} & \dots & ka_{1n} \\ ka_{21} & ka_{22} & \dots & ka_{2n} \\ \dots & \dots & \dots & \dots \\ ka_{m1} & ka_{m2} & \dots & ka_{mn} \end{pmatrix} + \begin{pmatrix} kb_{11} & kb_{12} & \dots & kb_{1n} \\ kb_{21} & kb_{22} & \dots & kb_{2n} \\ \dots & \dots & \dots & \dots \\ kb_{m1} & kb_{m2} & \dots & kb_{mn} \end{pmatrix} =$$

$$= \begin{pmatrix} ka_{11}+kb_{11} & ka_{12}+kb_{12} & \dots & ka_{1n}+kb_{1n} \\ ka_{21}+kb_{21} & ka_{22}+kb_{22} & \dots & ka_{2n}+kb_{2n} \\ \dots & \dots & \dots & \dots \\ ka_{m1}+kb_{m1} & ka_{m2}+kb_{m2} & \dots & ka_{mn}+kb_{mn} \end{pmatrix} - \text{np. } \gamma$$

$$1. \gamma = \text{np. } \gamma.$$

γ.m.g.

6)

$$(s+t) \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \dots & \dots \\ a_{m1} & a_{m2} & \dots & a_{mn} \end{pmatrix} = \begin{pmatrix} (s+t)a_{11} & (s+t)a_{12} & \dots & (s+t)a_{1n} \\ (s+t)a_{21} & (s+t)a_{22} & \dots & (s+t)a_{2n} \\ \dots & \dots & \dots & \dots \\ (s+t)a_{m1} & (s+t)a_{m2} & \dots & (s+t)a_{mn} \end{pmatrix} =$$



$$\begin{aligned}
 &= \begin{pmatrix} s_{d_{11}} + t_{d_{11}} & s_{d_{12}} + t_{d_{12}} & \dots & s_{d_{1n}} + t_{d_{1n}} \\ s_{d_{21}} + t_{d_{21}} & s_{d_{22}} + t_{d_{22}} & \dots & s_{d_{2n}} + t_{d_{2n}} \\ \dots & \dots & \dots & \dots \\ s_{d_{m1}} + t_{d_{m1}} & s_{d_{m2}} + t_{d_{m2}} & \dots & s_{d_{mn}} + t_{d_{mn}} \end{pmatrix} - \text{д.т.} \\
 &= s \cdot \begin{pmatrix} d_{11} & d_{12} & \dots & d_{1n} \\ d_{21} & d_{22} & \dots & d_{2n} \\ \dots & \dots & \dots & \dots \\ d_{m1} & d_{m2} & \dots & d_{mn} \end{pmatrix} + t \cdot \begin{pmatrix} d_{11} & d_{12} & \dots & d_{1n} \\ d_{21} & d_{22} & \dots & d_{2n} \\ \dots & \dots & \dots & \dots \\ d_{m1} & d_{m2} & \dots & d_{mn} \end{pmatrix} = \\
 &= \begin{pmatrix} s_{d_{11}} & s_{d_{12}} & \dots & s_{d_{1n}} \\ s_{d_{21}} & s_{d_{22}} & \dots & s_{d_{2n}} \\ \dots & \dots & \dots & \dots \\ s_{d_{m1}} & s_{d_{m2}} & \dots & s_{d_{mn}} \end{pmatrix} + \begin{pmatrix} t_{d_{11}} & t_{d_{12}} & \dots & t_{d_{1n}} \\ t_{d_{21}} & t_{d_{22}} & \dots & t_{d_{2n}} \\ \dots & \dots & \dots & \dots \\ t_{d_{m1}} & t_{d_{m2}} & \dots & t_{d_{mn}} \end{pmatrix} = \\
 &= \begin{pmatrix} s_{d_{11}} + t_{d_{11}} & s_{d_{12}} + t_{d_{12}} & \dots & s_{d_{1n}} + t_{d_{1n}} \\ s_{d_{21}} + t_{d_{21}} & s_{d_{22}} + t_{d_{22}} & \dots & s_{d_{2n}} + t_{d_{2n}} \\ \dots & \dots & \dots & \dots \\ s_{d_{m1}} + t_{d_{m1}} & s_{d_{m2}} + t_{d_{m2}} & \dots & s_{d_{mn}} + t_{d_{mn}} \end{pmatrix} - \text{нр.т.}
 \end{aligned}$$

$$\text{д.т.} = \text{нр.т.}$$

(т.н.г.)

$$\begin{aligned}
 \gamma) \quad (V \cdot \Gamma) \cdot \begin{pmatrix} d_{11} & d_{12} & \dots & d_{1n} \\ d_{21} & d_{22} & \dots & d_{2n} \\ \dots & \dots & \dots & \dots \\ d_{m1} & d_{m2} & \dots & d_{mn} \end{pmatrix} &= \begin{pmatrix} v\Gamma d_{11} & v\Gamma d_{12} & \dots & v\Gamma d_{1n} \\ v\Gamma d_{21} & v\Gamma d_{22} & \dots & v\Gamma d_{2n} \\ \dots & \dots & \dots & \dots \\ v\Gamma d_{m1} & v\Gamma d_{m2} & \dots & v\Gamma d_{mn} \end{pmatrix} - \text{д.т.} \\
 &= v \cdot \left( \Gamma \cdot \begin{pmatrix} d_{11} & d_{12} & \dots & d_{1n} \\ d_{21} & d_{22} & \dots & d_{2n} \\ \dots & \dots & \dots & \dots \\ d_{m1} & d_{m2} & \dots & d_{mn} \end{pmatrix} \right) = v \cdot \begin{pmatrix} \Gamma d_{11} & \Gamma d_{12} & \dots & \Gamma d_{1n} \\ \Gamma d_{21} & \Gamma d_{22} & \dots & \Gamma d_{2n} \\ \dots & \dots & \dots & \dots \\ \Gamma d_{m1} & \Gamma d_{m2} & \dots & \Gamma d_{mn} \end{pmatrix} = \\
 &= \begin{pmatrix} v\Gamma d_{11} & v\Gamma d_{12} & \dots & v\Gamma d_{1n} \\ v\Gamma d_{21} & v\Gamma d_{22} & \dots & v\Gamma d_{2n} \\ \dots & \dots & \dots & \dots \\ v\Gamma d_{m1} & v\Gamma d_{m2} & \dots & v\Gamma d_{mn} \end{pmatrix} - \text{нр.т.}
 \end{aligned}$$

$$\text{д.т.} = \text{нр.т.}$$

(нр.г.)



$$8) \begin{pmatrix} d_{11} & d_{12} & \dots & d_{1n} \\ d_{21} & d_{22} & \dots & d_{2n} \\ \dots & \dots & \dots & \dots \\ d_{m1} & d_{m2} & \dots & d_{mn} \end{pmatrix} + \begin{pmatrix} 0 & 0 & \dots & 0 \\ 0 & 0 & \dots & 0 \\ \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & 0 \end{pmatrix} = J \cdot \pi$$

$$= \begin{pmatrix} d_{11}+0 & d_{12}+0 & \dots & d_{1n}+0 \\ d_{21}+0 & d_{22}+0 & \dots & d_{2n}+0 \\ \dots & \dots & \dots & \dots \\ d_{m1}+0 & d_{m2}+0 & \dots & d_{mn}+0 \end{pmatrix} = \begin{pmatrix} d_{11} & d_{12} & \dots & d_{1n} \\ d_{21} & d_{22} & \dots & d_{2n} \\ \dots & \dots & \dots & \dots \\ d_{m1} & d_{m2} & \dots & d_{mn} \end{pmatrix} = \pi \cdot \pi$$

$$J \cdot \pi = \pi \cdot \pi$$

$\pi \cdot m \cdot g$

$$9) \begin{pmatrix} d_{11} & d_{12} & \dots & d_{1n} \\ d_{21} & d_{22} & \dots & d_{2n} \\ \dots & \dots & \dots & \dots \\ d_{m1} & d_{m2} & \dots & d_{mn} \end{pmatrix} = J \cdot \pi$$

$$= \begin{pmatrix} 1 \cdot d_{11} & 1 \cdot d_{12} & \dots & 1 \cdot d_{1n} \\ 1 \cdot d_{21} & 1 \cdot d_{22} & \dots & 1 \cdot d_{2n} \\ \dots & \dots & \dots & \dots \\ 1 \cdot d_{m1} & 1 \cdot d_{m2} & \dots & 1 \cdot d_{mn} \end{pmatrix} =$$

$$= \begin{pmatrix} d_{11} & d_{12} & \dots & d_{1n} \\ d_{21} & d_{22} & \dots & d_{2n} \\ \dots & \dots & \dots & \dots \\ d_{m1} & d_{m2} & \dots & d_{mn} \end{pmatrix} = \pi \cdot \pi$$

$$J \cdot \pi = \pi \cdot \pi$$

$\pi \cdot m \cdot g$

$$10) \begin{pmatrix} d_{11} & d_{12} & \dots & d_{1n} \\ d_{21} & d_{22} & \dots & d_{2n} \\ \dots & \dots & \dots & \dots \\ d_{m1} & d_{m2} & \dots & d_{mn} \end{pmatrix} = J \cdot \pi$$

$$= \begin{pmatrix} 0 \cdot d_{11} & 0 \cdot d_{12} & \dots & 0 \cdot d_{1n} \\ 0 \cdot d_{21} & 0 \cdot d_{22} & \dots & 0 \cdot d_{2n} \\ \dots & \dots & \dots & \dots \\ 0 \cdot d_{m1} & 0 \cdot d_{m2} & \dots & 0 \cdot d_{mn} \end{pmatrix} =$$

$$= \begin{pmatrix} 0 & 0 & \dots & 0 \\ 0 & 0 & \dots & 0 \\ \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & 0 \end{pmatrix} = \pi \cdot \pi$$

$$J \cdot \pi = \pi \cdot \pi$$

$\pi \cdot m \cdot g$