DataStorm Insomniacs Final

May 30, 2024

```
[340]: import numpy as np
       import pandas as pd
       from sklearn import preprocessing
       from sklearn.ensemble import IsolationForest
       from sklearn.preprocessing import StandardScaler
       from sklearn.cluster import KMeans
       from scipy.cluster.hierarchy import dendrogram, linkage
       from sklearn.decomposition import PCA
       try:
           import seaborn as sns
       except ImportError:
           %pip install seaborn
           import seaborn as sns
       try:
           from word2number import w2n
       except ImportError:
           %pip install word2number
           from word2number import w2n
       import matplotlib.pyplot as plt
       from scipy import stats
```

1 Loading Data

```
2
              3
                                  6812
                                                                      2.11
3
              4
                                 38542
                                                                     7.82
              5
                                                                     7.51
                                 48712
   average_monthly_basket_size
                            2.84
0
1
                           33.83
                             NaN
3
                           10.73
                           10.04
```

c:\Users\dell\AppData\Local\Programs\Python\Python39\lib\sitepackages\IPython\core\interactiveshell.py:3553: DtypeWarning: Columns (1,2) have
mixed types.Specify dtype option on import or set low_memory=False.
 exec(code_obj, self.user_global_ns, self.user_ns)

2 Dealing with Non Numeric Data

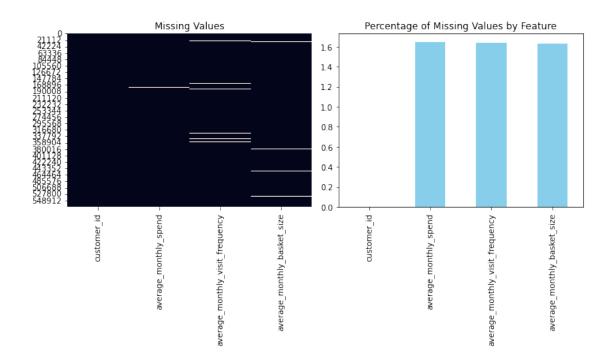
```
[342]: #print all non numeric columns
     print("----")
     for i in dataset.columns:
         if dataset[i].dtype == 'object':
            print(i,end = " ")
     print()
     print("-----")
     #handling non-numeric data converting them to numeric
     def word_to_num(value):
        try:
            return w2n.word_to_num(value)
        except ValueError:
            if value.isdigit():
               return int(value)
            elif value.replace('.', '', 1).isdigit() and value.count('.') < 2:</pre>
               return float(value)
            return None
     for column in dataset.columns:
        dataset[column] = dataset[column].apply(lambda x : word_to_num(str(x)))
```

----- NON NUMERIC COLUMNS-----average_monthly_spend average_monthly_visit_frequency

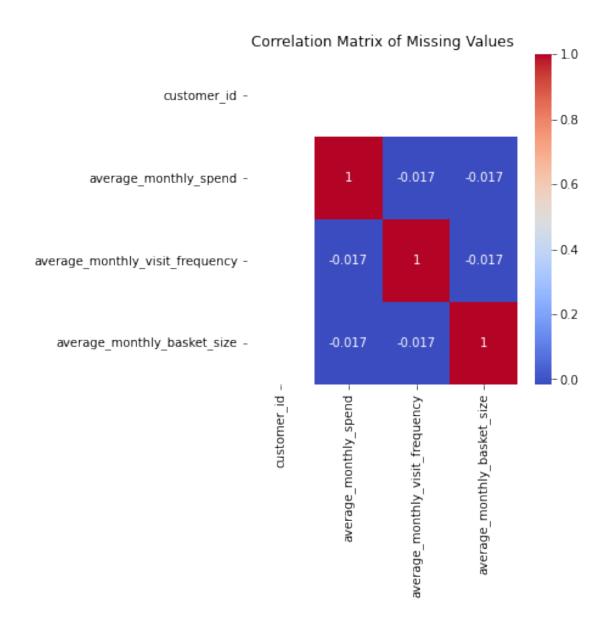
3 Prelimenary Analysis of Missing Values

```
[343]: #missing value analysis
      print("----- MISSING VALUE DETAILS,
      ٠,----")
      #nan count
      print(dataset.isna().sum())
      #length of dataset
      print(f"Length of dataset: {len(dataset)}")
      #count all the rows with nan values
      rows with nan = dataset.isna().any(axis=1).sum()
      print(f"Rows with nan values: {rows_with_nan}")
      #ratio of rows with nan values
      missing_percentage = dataset.isnull().mean() * 100
      print(f"Ratio of rows with nan values: {round(rows with nan/
       \hookrightarrowlen(dataset),2)*100}%")
      plt.figure(figsize=(5,5))
      plt.subplot(1, 2, 1)
      plt.title('Missing Values')
      sns.heatmap(dataset.isnull(), cbar=False)
      plt.subplot(1, 2, 2)
      missing_percentage.plot(kind='bar', figsize=(10, 6), color='skyblue')
      plt.title('Percentage of Missing Values by Feature')
      plt.tight_layout()
      plt.show()
      print("-----
```

```
customer_id 0
average_monthly_spend 9389
average_monthly_visit_frequency 9337
average_monthly_basket_size 9287
dtype: int64
Length of dataset: 570000
Rows with nan values: 28013
Ratio of rows with nan values: 5.0%
```



```
[344]: #correlation matrix to see the missing values are correlated plt.figure(figsize=(5, 5)) corr_matrix = dataset.isnull().corr() sns.heatmap(corr_matrix, annot=True, cmap='coolwarm') plt.title('Correlation Matrix of Missing Values') plt.show()
```



----- EXTRACTED NAN ROWS -----

```
customer_id average_monthly_spend average_monthly_visit_frequency \
      2
                                            6812.0
                                                                                 2.11
      7
                         8
                                           12656.0
                                                                                 2.13
      24
                        25
                                           41329.0
                                                                                 NaN
      52
                                                                                 NaN
                        53
                                          171010.0
      53
                        54
                                          104457.0
                                                                               18.88
      559914
                    559915
                                           45023.0
                                                                                 NaN
      559945
                    559946
                                           49533.0
                                                                                5.87
                    559960
                                                                                5.80
      559959
                                               NaN
      559970
                                           95444.0
                                                                               19.85
                    559971
      559972
                    559973
                                           13981.0
                                                                                2.74
              average_monthly_basket_size
      2
      7
                                        NaN
      24
                                      10.32
                                     35.03
      52
      53
                                        NaN
      559914
                                      9.82
      559945
                                        {\tt NaN}
                                       9.87
      559959
      559970
                                       NaN
      559972
                                       NaN
      [28013 rows x 4 columns]
[346]: def plot_outliers():
         iso_forest = IsolationForest(contamination=0.05, random_state=42)
         features =
        →['average_monthly_spend', 'average_monthly_visit_frequency', 'average_monthly_basket_size']
         data = dataset.copy()
         iso_forest.fit(data[features])
         outliers = iso_forest.predict(data[features])
         data['outlier'] = outliers
         outliers_data = data[data['outlier'] == -1]
         sns.pairplot(data, hue='outlier', palette={1: 'blue', -1: 'red'}, __
        ⇔markers=["o", "s"])
         plt.suptitle('Isolation Forest Outlier Detection', y=1.02)
         plt.show()
[347]: #Handle outliers
       data = dataset.copy()
       Q1 = dataset.quantile(0.25)
       Q3 = dataset.quantile(0.75)
```

```
[347]:
       count 531990.000000
                                       5.319900e+05
                                                                         531990.000000
       mean
              280059.070229
                                       4.825899e+04
                                                                              6.879288
       std
              161689.312262
                                       9.173203e+04
                                                                              5.323171
                                       0.000000e+00
       min
                   1.000000
                                                                              0.000000
       25%
              139927.250000
                                       1.049900e+04
                                                                              2.390000
       50%
              280109.500000
                                       3.195900e+04
                                                                              5.600000
       75%
              420171.750000
                                       8.541800e+04
                                                                              9.850000
              560000.000000
                                       4.833000e+07
                                                                            432.740000
       max
              average_monthly_basket_size
                             531990.000000
       count
                                 13.292845
       mean
       std
                                 12.039045
       min
                                  0.000000
       25%
                                  3.800000
       50%
                                  9.790000
       75%
                                 17.480000
                                385.040000
       max
```

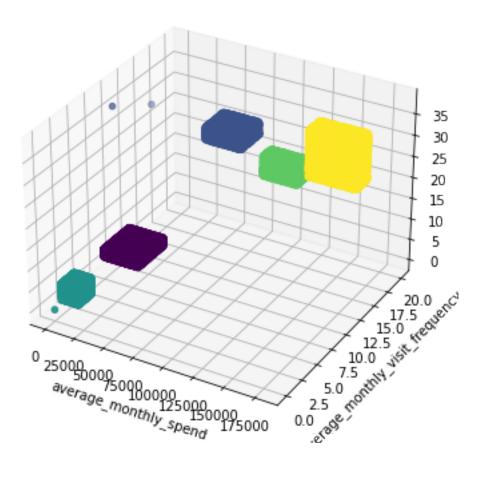
4 Data Visualization and Preliminary Clusterting for Observing the Nature of Decision Boundaries

```
[348]: #scale for cluster visualization
    scaler = StandardScaler()
    scaled_data = scaler.fit_transform(dataset.iloc[:, 1:])
    scaled_data_nan = scaler.transform(nan_rows.iloc[:, 1:])

[349]: #clustering using Kmeans
    kmeans = KMeans(n_clusters=5, random_state=42)
    clusters = kmeans.fit_predict(scaled_data)

c:\Users\dell\AppData\Local\Programs\Python\Python39\lib\site-
    packages\sklearn\cluster\_kmeans.py:870: FutureWarning: The default value of
    `n_init` will change from 10 to 'auto' in 1.4. Set the value of `n_init`
    explicitly to suppress the warning
    warnings.warn(
```

Clusters



Cuboidal shape of the clusters is proof that the Decision boundaries can be represented as a logical

combination of coniditions on eack parameter seperately. (The decision Boundaries are alined with the Vertical and Horizontal Planes). That is the Function for a Decison Boundary for a cluster j, $\phi_j(x_1,x_2,x_2)$ (where x_1,x_2,x_3 are the three features) can be expressed as a logical combination of three simple decision rules.

That is if,

$$\phi_j(x_1,x_2,x_3) = \begin{cases} 1 & \text{If belongs to cluster j} \\ 0 & \text{If does not belongs to cluster j} \end{cases}$$

then,

$$\phi_{i}(x_{1},x_{2},x_{3})=\phi_{1,i}(x_{1})\cdot\phi_{2,i}(x_{2})\cdot\phi3,i(x_{3})$$

where \cdot is the logical and operation fruthemore since there is only one such block per cluster per axis,

$$\phi_{k,j}(x_k) = \begin{cases} 1 & a_k < x_k < b_k \\ 0 & \text{otherwise} \end{cases}$$

Where a_k and b_k are to be determined Finally it can also be observed that these margins are far apart so clustering in each dimension separately is sufficient for identifying these bondaries.

Finally this corrabartes well with the Problem Statement

5 Demonstrating that Rows with Missing Values Belong to One of the Clusters and Can be Fully Determined by Considering the remaining Columns

We will use the fact that if we make one of the features zero, this produces a Projection of one of the Cuboidal Clusters onto one of the planes. Therefore, we will replace the missing values with zero and plot in a 3d space

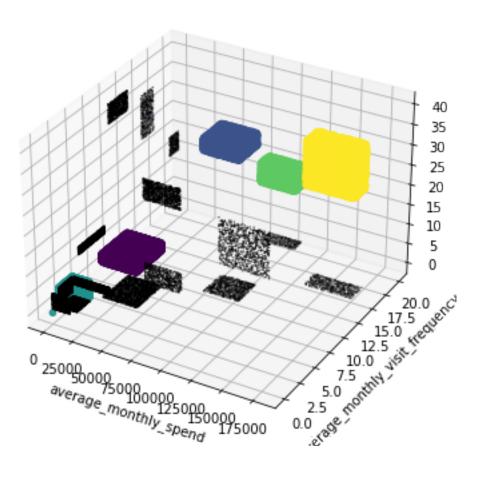
```
[351]: nan rows.fillna(0, inplace=True)
       dataset['Cluster'] = clusters
       fig = plt.figure(figsize=(13, 12))
       ax = fig.add subplot(121, projection='3d')
       ax.scatter(dataset['average_monthly_spend'],__

dataset['average_monthly_visit_frequency'],

        dataset['average_monthly_basket_size'], c=clusters, cmap='viridis')
       ax.set xlabel('average monthly spend')
       ax.set_ylabel('average_monthly_visit_frequency')
       ax.set zlabel('average monthly basket size')
       plt.title('Clusters')
       ax.scatter(nan_rows['average_monthly_spend'],_
        →nan_rows['average_monthly_visit_frequency'],
        anan_rows['average_monthly_basket_size'],
                  c='black', s = 0.1)
       ax.set_xlabel('average_monthly_spend')
       ax.set_ylabel('average_monthly_visit_frequency')
       ax.set_zlabel('average_monthly_basket_size')
```

plt.show()

Clusters

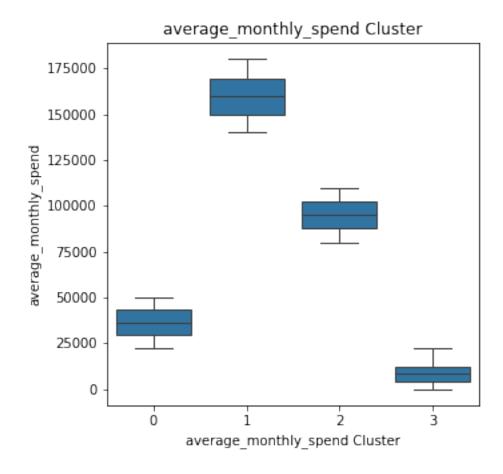


We can easily see that all of the missing value clouds (Black data clouds) are simply projections of the already identified clusters onto on of the planse x_1x_2, x_1x_3, x_2x_3 planes thus proving our claim is correct. We will reinforce this claim in later sections. Finally, since all Black Data clouds are 2 Dimensional it is also clear that there are no columns with two or more missing values.

6 Demonstrating that the Distribution Roughly Follows the Rules given in the Problem Statement

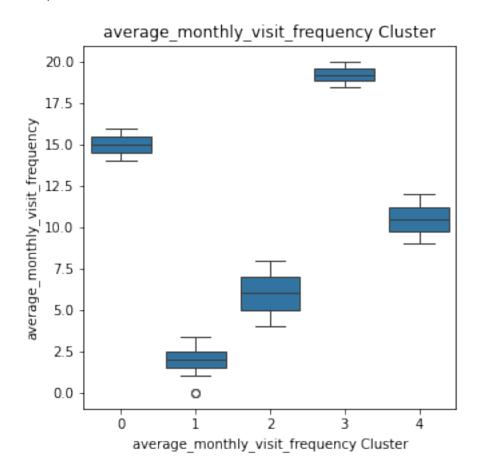
```
[352]: def cluster_visualization_on_feature(feature_name:str):
    feature_dataset = copy_dataset[[feature_name]].dropna()
    n = 5 if feature_name == "average_monthly_visit_frequency" else 4
    kmeans = KMeans(n_clusters=n, random_state=42)
    clusters = kmeans.fit_predict(feature_dataset)
```

c:\Users\dell\AppData\Local\Programs\Python\Python39\lib\sitepackages\sklearn\cluster_kmeans.py:870: FutureWarning: The default value of
`n_init` will change from 10 to 'auto' in 1.4. Set the value of `n_init`
explicitly to suppress the warning
 warnings.warn(

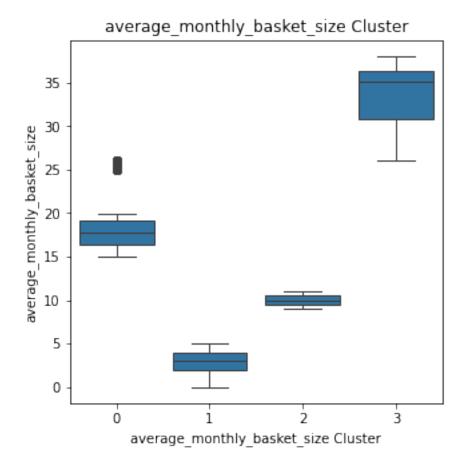


c:\Users\dell\AppData\Local\Programs\Python\Python39\lib\sitepackages\sklearn\cluster_kmeans.py:870: FutureWarning: The default value of
`n_init` will change from 10 to 'auto' in 1.4. Set the value of `n_init`

explicitly to suppress the warning
warnings.warn(



c:\Users\dell\AppData\Local\Programs\Python\Python39\lib\sitepackages\sklearn\cluster_kmeans.py:870: FutureWarning: The default value of
`n_init` will change from 10 to 'auto' in 1.4. Set the value of `n_init`
explicitly to suppress the warning
 warnings.warn(



Plotting Box and Whisker graphs to analyze distinct clusters within features. Considering Average Monthly Spend by Cluster, We can identify there are 4 distinct clusters (cluster 0 and 4 are the same). We could categorize them as, - 3 - LOW - 1 - Average - 0, 4 - High - 2 - Very High

Considering Average Monthly Visit Frequency by cluster, We can identify that there are 5 distinct clusters. We can categorize them as,

- 3 Low
- 1 Average Lower
- 4 Average Higher
- 2 High
- 1 Very High

Note that we can see two well separated clusters in the average range instead of the one as given in the problem statement. It is possible that these two clusters have no bearing on the problem. But we will later show that these have a very high importance for the classification task. Considering Average Monthly Basket Size by cluster. Although we can see 5 clusters in the plot we can see that the two upper clusters are overlapping in terms of the inter quartile ranges. Therefore will only consider four clusters. We can categorize them as ,

- 3 Low
- 1 Average

- 0 High
- 2,4 Very High

The Table is mostly correct however there are some modifications need to be done which we will further verify and update in a later section

7 Analyzing Each Feature Set Independently and Identifying the Percentiles (Ranges in our Case)

Since in the previous section we demonstrated that it is sufficient to analyze each feature independantly we wil analyze them, - first visually through histograms - second using

```
[353]: print("-----")
      data = pd.read_csv('customer_dataset.csv')
      data.head()
                  -----Data Analysis-----
     c:\Users\dell\AppData\Local\Programs\Python\Python39\lib\site-
     packages\IPython\core\interactiveshell.py:3553: DtypeWarning: Columns (1,2) have
     mixed types. Specify dtype option on import or set low_memory=False.
       exec(code_obj, self.user_global_ns, self.user_ns)
[353]:
         customer_id average_monthly_spend average_monthly_visit_frequency \
      0
                  1
                                    790
                                                                 1.11
                  2
      1
                                  176875
                                                                15.74
      2
                  3
                                                                 2.11
                                   6812
      3
                  4
                                   38542
                                                                 7.82
                                   48712
                                                                 7.51
         average_monthly_basket_size
      0
                              2.84
      1
                             33.83
      2
                               NaN
      3
                             10.73
      4
                             10.04
[354]: # Extracting columns from the dataframe
      col_names = data.columns.tolist()
      print(col_names)
      ['customer_id', 'average_monthly_spend', 'average_monthly_visit_frequency',
      'average_monthly_basket_size']
[355]: # Converting words to numerical values
      def convert_word_to_number(amount):
          try:
```

```
return w2n.word_to_num(amount)
except ValueError:
    return amount

for col in col_names:
    data[col] = data[col].apply(convert_word_to_number)
    data[col] = pd.to_numeric(data[col], errors='coerce')
    data = data.dropna(subset=[col])

56]:

def plot_barCharts(column_name, x_axis_label, interval_width : int, min_limit :
    int, max_limit : int):
    max_value = int(data[column_name].max()) + interval_width
```

```
[356]: def plot_barCharts(column_name, x_axis_label, interval_width : int, min_limit :u
int, max_limit : int):
    max_value = int(data[column_name].max()) + interval_width

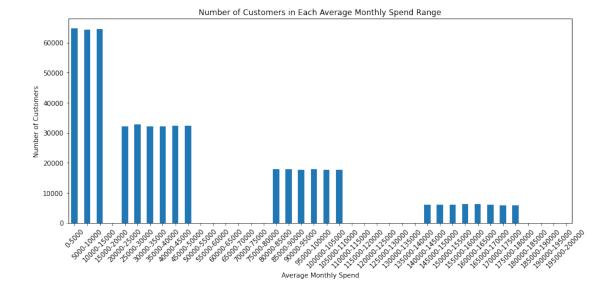
    bins = range(min_limit, max_limit, interval_width)
    labels = [f''{i}-{i+interval_width}' for i in bins[:-1]]

    data['range'] = pd.cut(data[column_name], bins=bins, labels=labels,u
inight=False)
    customer_count = data['range'].value_counts().sort_index()

plt.figure(figsize=(12, 6))
    customer_count.plot(kind='bar')
    plt.ylabel(x_axis_label)
    plt.ylabel('Number of Customers')
    plt.title(f'Number of Customers in Each {x_axis_label} Range')
    plt.xticks(rotation=45)
    plt.tight_layout()
    plt.show()

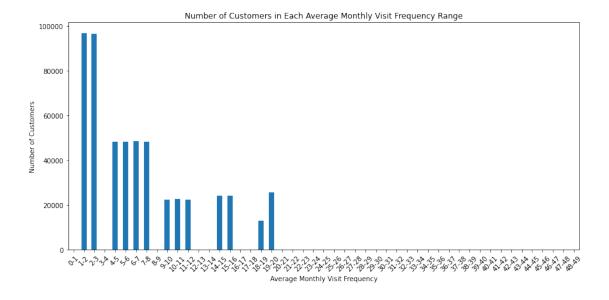
print(customer_count)
```

```
[357]: plot_barCharts('average_monthly_spend', 'Average Monthly Spend', 5000, 0, U $\to 200001)
```



64687
64284
64552
0
32134
32692
32145
32006
32371
32357
0
0
0
0
0
0
17794
17918
17680
17782
17605
17601
0
0
0
0
0
0
6057

```
145000-150000
                  5982
150000-155000
                  6146
155000-160000
                  6188
160000-165000
                  6173
165000-170000
                  6061
170000-175000
                  5856
175000-180000
                  5918
180000-185000
                      0
185000-190000
                      0
190000-195000
                      0
195000-200000
                      0
Name: range, dtype: int64
```

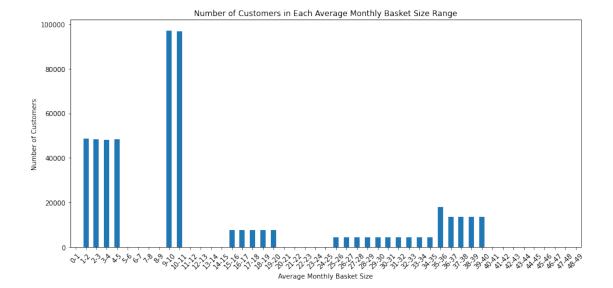


0-1	2
1-2	96944
2-3	96575
3-4	1
4-5	48285
5-6	48346
6-7	48647
7-8	48423
8-9	0
9-10	22447
10-11	22718
11-12	22519
12-13	0

```
14-15
                24151
      15-16
                24235
      16-17
                    0
                    0
      17-18
      18-19
                12928
      19-20
                25766
      20-21
                    0
                    0
      21-22
      22-23
                    1
      23-24
                    0
      24-25
                    0
      25-26
                    0
      26-27
                    0
      27-28
                    0
                    0
      28-29
      29-30
                    0
                    0
      30-31
      31-32
                    0
      32-33
                    0
      33-34
                    0
      34-35
                    0
                    0
      35-36
      36-37
                    0
      37-38
                    0
      38-39
                    0
      39-40
                    0
      40-41
                    0
      41-42
                    0
                    0
      42-43
      43-44
                    0
      44-45
                    0
      45-46
                    0
      46-47
                    0
      47-48
                    0
      48-49
                    0
      Name: range, dtype: int64
[359]: plot_barCharts('average_monthly_basket_size', 'Average Monthly Basket Size', 1, ___
        ⇔0, 50)
```

13-14

0



0-1	3
1-2	48568
2-3	48458
3-4	48130
4-5	48366
5-6	0
6-7	0
7-8	0
8-9	0
9-10	97051
10-11	96656
11-12	0
12-13	0
13-14	0
14-15	0
15-16	7824
16-17	7632
17-18	7771
18-19	7709
19-20	7758
20-21	0
21-22	0
22-23	0
23-24	0
24-25	0
25-26	4400
26-27	4505
27-28	4346
28-29	4374

```
29-30
          4480
30-31
          4440
31-32
          4356
32-33
          4408
33-34
          4343
34-35
          4352
35-36
         17985
36-37
         13562
37-38
         13471
38-39
         13460
39-40
         13587
40-41
             0
41-42
             0
42-43
             0
43-44
             0
             0
44-45
45-46
             0
46-47
             0
47-48
             0
             0
48-49
Name: range, dtype: int64
```

8 Further Proving that rows with Missing Values Follow the Same Distribution as the other ones

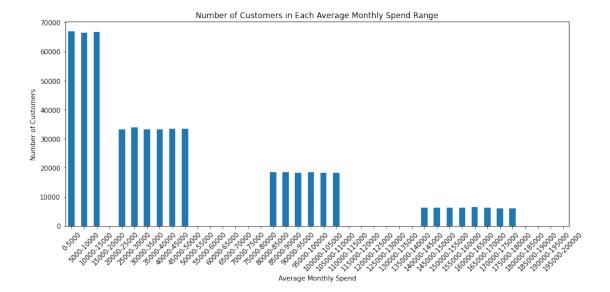
```
[363]: def plot_barCharts_2(column_name, x_axis_label, interval_width : int, min_limit_
        →: int, max_limit : int):
         data = dataset.dropna(subset=[column name])
         max value = int(data[column name].max()) + interval width
         bins = range(min_limit, max_limit, interval_width)
         labels = [f'{i}-{i+interval_width}' for i in bins[:-1]]
         data['range'] = pd.cut(data[column_name], bins=bins, labels=labels,__
        →right=False)
         customer_count = data['range'].value_counts().sort_index()
        plt.figure(figsize=(12, 6))
         customer_count.plot(kind='bar')
        plt.xlabel(x_axis_label)
        plt.ylabel('Number of Customers')
        plt.title(f'Number of Customers in Each {x_axis_label} Range')
        plt.xticks(rotation=45)
        plt.tight_layout()
        plt.show()
         print(customer_count)
```

```
[364]: plot_barCharts_2('average_monthly_spend', 'Average Monthly Spend', 5000, 0, u \( \times 200001 \)
```

C:\Users\dell\AppData\Local\Temp/ipykernel_26116/4100806091.py:8:
SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame. Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy data['range'] = pd.cut(data[column_name], bins=bins, labels=labels, right=False)



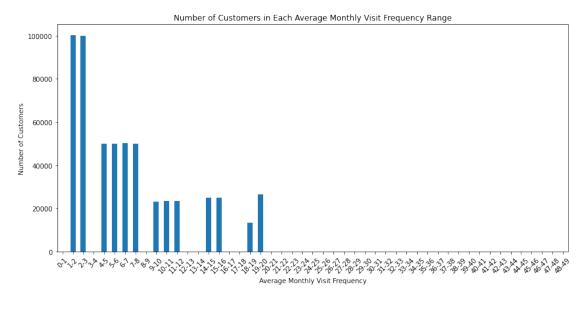
0-5000	66892
5000-10000	66494
10000-15000	66722
15000-20000	0
20000-25000	33268
25000-30000	33795
30000-35000	33218
35000-40000	33105
40000-45000	33501
45000-50000	33424
50000-55000	0
55000-60000	0
60000-65000	0
65000-70000	0
70000-75000	0
75000-80000	0
80000-85000	18421
85000-90000	18560
90000-95000	18285
95000-100000	18413
100000-105000	18226
105000-110000	18248
110000-115000	0
115000-120000	0
120000-125000	0
125000-130000	0
130000-135000	0
135000-140000	0
140000-145000	6254

```
6205
145000-150000
150000-155000
                   6355
155000-160000
                   6380
160000-165000
                   6394
165000-170000
                   6270
170000-175000
                   6058
175000-180000
                   6115
180000-185000
                      0
185000-190000
                      0
190000-195000
                      0
195000-200000
                      0
Name: range, dtype: int64
```

C:\Users\dell\AppData\Local\Temp/ipykernel_26116/4100806091.py:8:
SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame. Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy data['range'] = pd.cut(data[column_name], bins=bins, labels=labels, right=False)



0-1 2 1-2 100263 2-3 99976

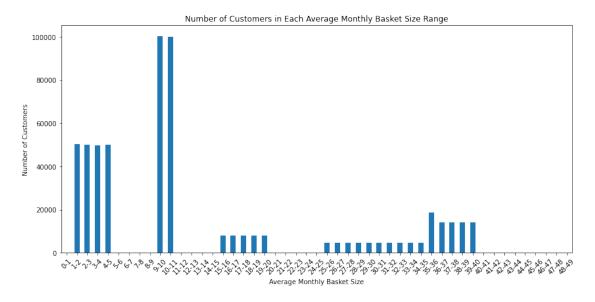
3-4	1
4-5	49959
5-6	49982
6-7	50306
7-8	50022
8-9	0
9-10	23255
10-11	23506
11-12	23352
12-13	0
13-14	0
14-15	25007
15-16	25036
16-17	0
17-18	0
18-19	13356
19-20	26636
20-21	0
21-22	0
22-23	1
23-24	0
24-25	0
25-26	0
26-27	0
27-28	0
28-29	0
	0
29-30 30-31	0
	0
31-32 32-33	0
33-34	0
34-35	0
	0
35-36	_
36-37	0
37-38	0
38-39	0
39-40	0
40-41	0
41-42	0
42-43	0
43-44	0
44-45	0
45-46	0
46-47	0
47-48	0
48-49	0

Name: range, dtype: int64

C:\Users\dell\AppData\Local\Temp/ipykernel_26116/4100806091.py:8:
SettingWithCopyWarning:

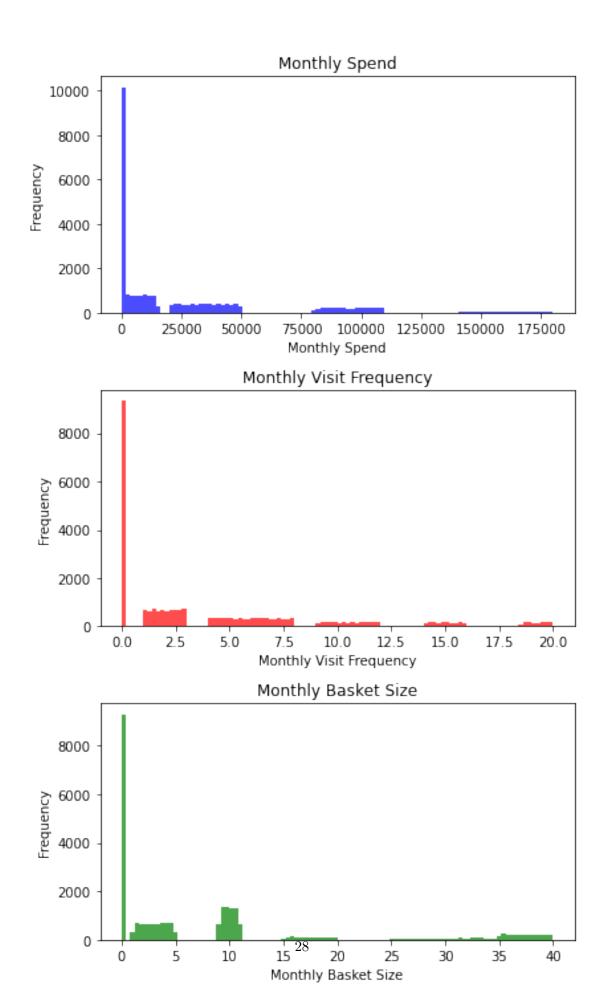
A value is trying to be set on a copy of a slice from a DataFrame. Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy data['range'] = pd.cut(data[column_name], bins=bins, labels=labels, right=False)



0-1	3
1-2	50256
2-3	50105
3-4	49792
4-5	50098
5-6	0
6-7	0
7-8	0
8-9	0
9-10	100359
10-11	99922
11-12	0
12-13	0
13-14	0
14-15	0
15-16	8092

```
16-17
                  7899
      17-18
                  8084
      18-19
                  7970
      19-20
                  8032
      20-21
                     0
      21-22
                     0
      22-23
                     0
      23-24
                     0
      24-25
                     0
      25-26
                  4553
      26-27
                  4639
      27-28
                  4499
      28-29
                  4526
      29-30
                  4619
      30-31
                  4598
      31-32
                  4519
      32-33
                  4598
      33-34
                  4519
      34-35
                  4493
      35-36
                18557
      36-37
                14019
      37-38
                13959
      38-39
                13938
      39-40
                14061
      40-41
                     0
      41-42
                     0
      42-43
                     0
      43-44
                     0
      44-45
                     0
      45-46
                     0
      46-47
                     0
      47-48
                     0
      48-49
                     0
      Name: range, dtype: int64
[367]: plt.figure(figsize=(6, 10))
       plt.subplots_adjust(hspace=1)
       plt.subplot(3, 1, 1)
       plt.hist(nan_rows['average_monthly_spend'], bins=100, color='blue', alpha=0.7)
       plt.title('Monthly Spend')
       plt.xlabel('Monthly Spend')
       plt.ylabel('Frequency')
       plt.subplot(3, 1, 2)
       plt.hist(nan_rows['average_monthly_visit_frequency'], bins=100, color='red', __
        ⇒alpha=0.7)
```



9 Feature Selection

9.1 Loading Data

```
[368]: import pandas as pd
       import numpy as np
       import matplotlib.pyplot as plt
       from word2number import w2n
       dataset_og = pd.read_csv("customer_dataset.csv")
       CUS_ID = 'customer_id'
       AVG_SPEND = 'average_monthly_spend'
       AVG_VISIT = 'average_monthly_visit_frequency'
       AVG_BASKET_SIZE = 'average_monthly_basket_size'
       #handling non-numeric data converting them to numeric
       def word_to_num(value):
           try:
               return w2n.word to num(value)
           except ValueError:
               if value.isdigit():
                   return int(value)
               elif value.replace('.', '', 1).isdigit() and value.count('.') < 2:</pre>
                   return float(value)
               return None
       for column in dataset_og.columns:
           dataset_og[column] = dataset_og[column].apply(lambda x :_u
        →word_to_num(str(x)))
       dataset = dataset og.drop duplicates().dropna()
       dataset.head()
```

c:\Users\dell\AppData\Local\Programs\Python\Python39\lib\sitepackages\IPython\core\interactiveshell.py:3553: DtypeWarning: Columns (1,2) have
mixed types.Specify dtype option on import or set low_memory=False.
exec(code obj, self.user global ns, self.user ns)

```
[368]:
          customer_id average_monthly_spend average_monthly_visit_frequency \
       0
                                                                          1.11
       1
                    2
                                    176875.0
                                                                         15.74
                    4
                                                                          7.82
       3
                                     38542.0
                    5
       4
                                     48712.0
                                                                          7.51
       5
                                    172333.0
                                                                         14.16
```

average_monthly_basket_size

```
0 2.84
1 33.83
3 10.73
4 10.04
5 35.06
```

9.2 Defining Cluster Thresholds Identified Preivously

```
[369]: class Basket_Sizes:
          LOW = (0,7)
          AVERAGE = (7,13)
          HIGH = (13,22)
          VERY_HIGH = (22,50)
          ranges = [LOW, AVERAGE, HIGH, VERY_HIGH]
          ranges_good = [LOW,AVERAGE,HIGH,VERY_HIGH]
          Oclassmethod
          def filter_set(cls,dataset,range):
              assert(range in cls.ranges)
              return dataset[(dataset[AVG_BASKET_SIZE] >= range[0]) &__
       Oclassmethod
          def get_mask(cls,dataset,range):
              assert(range in cls.ranges)
              return ((dataset[AVG_BASKET_SIZE] >= range[0]) &__
       class Monthly_Spend:
          LOW = (0, 17500)
          AVERAGE = (17500, 65000)
          HIGH = (65000, 125000)
          VERY_HIGH = (125000, 200000)
          ranges = [LOW, AVERAGE, HIGH, VERY_HIGH]
          ranges_good = [LOW, AVERAGE, HIGH, VERY_HIGH]
          Oclassmethod
          def filter_set(cls,dataset,range):
              assert(range in cls.ranges)
              return dataset[(dataset[AVG_SPEND] >= range[0]) & (dataset[AVG_SPEND] <_

¬range[1])]
          Oclassmethod
          def get_mask(cls,dataset,range):
              assert(range in cls.ranges)
```

```
return ((dataset[AVG_SPEND] >= range[0]) & (dataset[AVG_SPEND] <_
 →range[1]))
class Average_Visit:
    LOW = (0,3.7)
    AVERAGE LOWER = (3.7, 8.5)
    AVERAGE_HIGHER = (8.5, 13)
    AVERAGE = (3.7, 13)
    HIGH = (13, 17)
    VERY_HIGH = (17,21)
    ranges = [LOW, AVERAGE_LOWER, AVERAGE_HIGHER, HIGH, VERY_HIGH, AVERAGE]
    ranges good = [LOW, AVERAGE LOWER, AVERAGE HIGHER, HIGH, VERY HIGH]
    @classmethod
    def filter_set(cls,dataset,range):
        assert(range in cls.ranges)
        return dataset[(dataset[AVG_VISIT] >= range[0]) & (dataset[AVG_VISIT] <__
 →range[1])]
    @classmethod
    def get_mask(cls,dataset,range):
        assert(range in cls.ranges)
        return ((dataset[AVG_VISIT] >= range[0]) & (dataset[AVG_VISIT] <__
 →range[1]))
```

9.3 Checking Limiting and Borderline Cases in Threholds Manually

While the Clusters boarder that we have identified programatically (and verified by visual inspection) have good clear boarders there are a few data points that is better if closely and manually verified to ensure it has been given the correct group

```
[370]: data[(data[AVG_VISIT]>3) & (data[AVG_VISIT] < 4)]
               customer_id average_monthly_spend average_monthly_visit_frequency
[370]:
       569999
                    244801
                                           4225.0
                                                                                3.4
               average_monthly_basket_size range
       569999
                                      1.92
[371]: data[(data[AVG_VISIT]>3) & (data[AVG_VISIT] < 4)]
               customer_id average_monthly_spend average_monthly_visit_frequency \
[371]:
                    244801
       569999
                                           4225.0
                                                                                3.4
               average_monthly_basket_size range
       569999
                                      1.92
                                             1-2
```

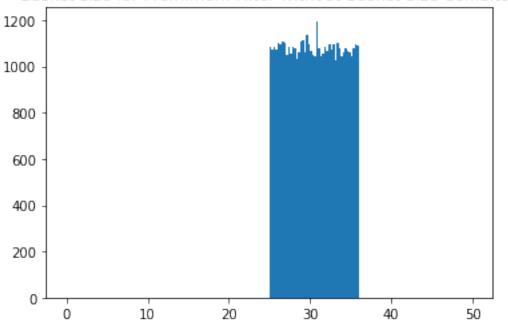
9.4 Fitering Using the Exact Rules Given in the Problem Statement

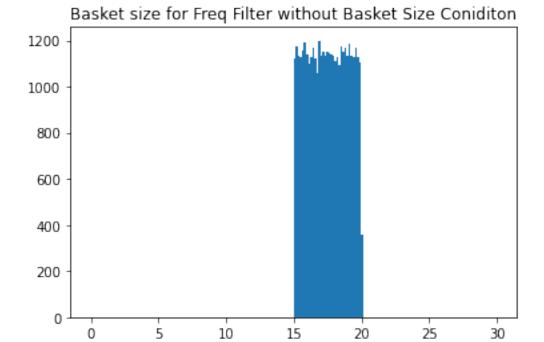
```
[372]: low_level_mask = Monthly_Spend.get_mask(dataset, Monthly_Spend.LOW) &__
        →Average Visit.get mask(dataset, Average Visit.LOW) & Basket Sizes.
        →get_mask(dataset,Basket_Sizes.LOW)
       medium level mask = Monthly Spend.get mask(dataset, Monthly Spend.AVERAGE) & ...
        Average_Visit.get_mask(dataset,Average_Visit.AVERAGE) & Basket_Sizes.
        ⇒get mask(dataset, Basket Sizes.AVERAGE)
       high_frequent_mask = Monthly_Spend.get_mask(dataset,Monthly_Spend.HIGH) &_ 
        Average Visit.get mask(dataset, Average Visit. VERY HIGH) & Basket Sizes.

→get_mask(dataset,Basket_Sizes.AVERAGE)
       high_loyal_mask = Monthly_Spend.get_mask(dataset,Monthly_Spend.HIGH) &_
        Average_Visit.get_mask(dataset,Average_Visit.AVERAGE) & Basket_Sizes.
        ⇒get_mask(dataset,Basket_Sizes.VERY_HIGH)
       high_premium_mask = Monthly_Spend.get_mask(dataset,Monthly_Spend.VERY_HIGH) &_
        Average_Visit.get_mask(dataset, Average_Visit.HIGH) & Basket_Sizes.
        →get_mask(dataset,Basket_Sizes.HIGH)
       print(low level mask.sum())
       print(medium_level_mask.sum())
       print(high frequent mask.sum())
       print(high_loyal_mask.sum())
       print(high_premium_mask.sum())
```

From this we have verified the calim that we have made before that the basket value for the "High-end-frequent" and "High-end-premium" needs to be changed from the values given in the table in the problem statement. This can be verified by taking the datasets that do not fit the rules and plotting the distribution of the datasets that do not follow the rules and apply the rules for these two datasets except for the Basket size dataset and observing the distribution

Basket size for Premimum Filter without Basket Size Coniditon





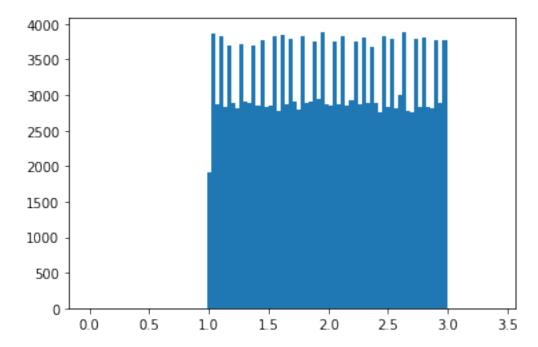
[374]:

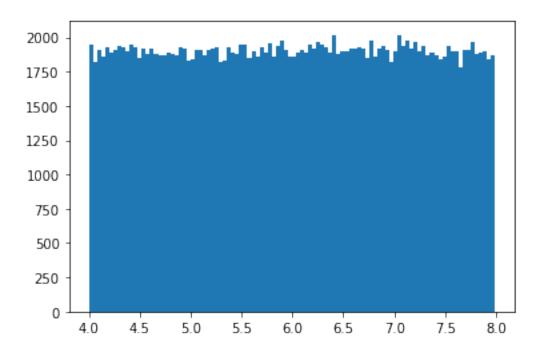
```
[374]:
                customer_id average_monthly_spend
                                                      average_monthly_visit_frequency
               37975.000000
                                        37975.000000
                                                                           37975.000000
       count
              281239.489849
                                        94997.415036
       mean
                                                                              19.247284
       std
              161976.207837
                                         8660.220172
                                                                               0.434948
       min
                  74.000000
                                        80000.000000
                                                                              18.500000
       25%
              140928.000000
                                        87549.500000
                                                                              18.870000
       50%
              281125.000000
                                        95004.000000
                                                                              19.250000
       75%
              421880.000000
                                       102523.000000
                                                                              19.630000
       max
              559984.000000
                                       109999.000000
                                                                              19.990000
              average_monthly_basket_size
                              37975.000000
       count
                                 17.492247
       mean
       std
                                  1.443141
                                 15.000000
       min
       25%
                                 16.240000
       50%
                                 17.500000
       75%
                                 18.750000
                                 19.990000
       max
```

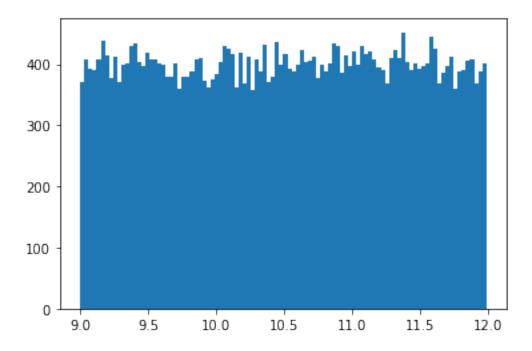
9.5 Proving additional clusters Identified in the Average Frequency correspond to actual features

Although the problem statement only identifies one average cluster for Frequency parameter from out prelimenary investigations we have shown that two seperate clusters are observable and furthermore that they actually can be effectively used to identify customer type. Now we will prove this claim. By applying the other two rules for a dataset with outliers removed and plotting the histograms

```
data = remove_outliers(data,AVG_BASKET_SIZE)
```







In fact keeping these two as seperate clusters is highly benegicial especially since this alone can be used to identify between Medium and High-End Loyal Customers even if the two other parameters (Average Spending and Average Basket size) are missing.

This leads us to conclude that the table should be updated as | Customer Category | Monthly Spend

```
| \  \, Monthly \  \, Visit \  \, Frequency \  \, | \  \, Monthly \  \, Basket \  \, Size \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \  \, | \
```

10 Analyzing Nature of Outliers and their Following of Rules

Now we will consider the dataset without the outliers to see if they obey the patterns observed

[377]:		customer_id	average_monthly_spend	average_monthly_visit_frequency	\
	count	18.000000	1.800000e+01	18.000000	
	mean	354434.666667	4.934703e+06	46.058333	
	std	159311.270356	1.293920e+07	100.784055	
	min	252.000000	0.00000e+00	1.250000	
	25%	322879.500000	9.543150e+04	11.930000	
	50%	325078.000000	1.489220e+05	15.310000	
	75%	515194.750000	1.612676e+06	19.630000	
	max	558101.000000	4.833000e+07	432.740000	

```
average_monthly_basket_size
                           18.000000
count
                           69.655000
mean
                          110.472051
std
min
                            2.160000
25%
                           12.427500
50%
                           29,285000
75%
                           37.470000
max
                          385.040000
```

Most of the values that do not follow the rules are due to outliers so we will get rid of the outliers and see if there are columns which follow the rules

```
[378]: spend_anomaly = other_data[AVG_SPEND]>Monthly_Spend.VERY_HIGH[1]
basket_anomaly = other_data[AVG_BASKET_SIZE]>Basket_Sizes.VERY_HIGH[1]
visit_anomaly = other_data[AVG_VISIT]>Average_Visit.VERY_HIGH[1]
other_data[~(spend_anomaly | basket_anomaly | visit_anomaly)]
```

```
[378]: customer_id average_monthly_spend average_monthly_visit_frequency \ 325525 325526 0.0 9.36 515037 515038 0.0 15.35
```

 ${\tt average_monthly_basket_size}$

325525	36.42
515037	30.02

From simple observation alone we can see that these two simply correspond to an entering error in the average monthly spend and actually belong to two clear categories if we consider the other two features

11 Feature Engineering

Now we will give a numeric lable to each of the ranges for each of the parameters (known as the score) Outliers and Nan values are marked as known as (-1). (These can actually later be estimated at least the range of them by considering the cluster that it belongs to)

```
[379]: classification_data = dataset_og.copy()
       VISIT_SCORE = 'VISIT_SCORE'
       BASKET_SCORE = 'BASKET_SCORE'
       SPEND SCORE = 'SPEND SCORE'
       classification_data[VISIT_SCORE] = -1
       classification_data[BASKET_SCORE] = -1
       classification_data[SPEND_SCORE] = -1
       for i,rr in enumerate(Monthly_Spend.ranges_good):
           mask = Monthly_Spend.get_mask(classification_data,rr)
           classification_data.loc[mask,SPEND_SCORE] = i
       #do the same for other two
       for i,rr in enumerate(Basket_Sizes.ranges_good):
           mask = Basket_Sizes.get_mask(classification_data,rr)
           classification_data.loc[mask,BASKET_SCORE] = i
       for i,rr in enumerate(Average_Visit.ranges_good):
           mask = Average_Visit.get_mask(classification_data,rr)
           classification_data.loc[mask,VISIT_SCORE] = i
       classification_data
```

```
[379]:
                                                       average_monthly_visit_frequency
                customer_id
                              average_monthly_spend
                                                790.0
                                                                                     1.11
       1
                                            176875.0
                                                                                    15.74
       2
                           3
                                              6812.0
                                                                                     2.11
       3
                           4
                                             38542.0
                                                                                     7.82
       4
                           5
                                                                                     7.51
                                             48712.0
                                             27428.0
       569995
                     341740
                                                                                     4.91
```

56999	96 2152	76	1./	1241.0		15.47
56999		515		9183.0		2.09
56999				5541.0		4.22
56999				4225.0		3.40
5099	99 2440	501		4225.0		3.40
	average_r	nonthly_1	oasket_size	VISIT_SCORE	BASKET_SCORE	SPEND_SCORE
0			2.84	0	0	0
1			33.83	3	3	3
2			NaN	0	-1	0
3			10.73	1	1	1
4			10.04	1	1	1
 56999	25		 9.42	 1	 1	1
5699			31.13	3	3	3
5699			4.61	0	0	0
5699			9.65	1	1	1
5699			1.92	0	0	0
prin	t(classifica	tion_data	a[SPEND_SCOR	E].value_coun E].value_coun RE].value_cou	ts())	
1	200269					
0	200242					
2	70113					
3	50043					
4	39992					
-1	9341					
Name:	VISIT_SCORE	, dtype:	int64			
1	200311					
0	200108					
2	110153					
3	50031					
-1	9397					
Name:	SPEND_SCORE	, dtype:	int64			

Name: SPEND_SCORE, dtype: int64

1 200281 0 200254 3 120097 2 40077 -1 9291

Name: BASKET_SCORE, dtype: int64

Demonstrate that There are no data points that have all feautres unknown

[381]:

```
no_data_mask = (classification_data[VISIT_SCORE] == -1) & 

⇔(classification_data[SPEND_SCORE] == -1) & 

⇔(classification_data[BASKET_SCORE] == -1) classification_data[no_data_mask]
```

[381]: Empty DataFrame

Columns: [customer_id, average_monthly_spend, average_monthly_visit_frequency, average_monthly_basket_size, VISIT_SCORE, BASKET_SCORE, SPEND_SCORE]

Index: []

Our Final Algorithm of Classifiation is very simple.

We have already identified the rules for each cluster by consdering the Problem Statement Table, The K-means Cluster Whisker plots. Fact that the decision boundaris can be written as logistic boundaries using and combination of decision inequalities for components idependantly (demonstrated using the cuboid shape of the cluster). The Nan Values also follow the same Law since they can clearly be seen to be projections of these cubes. Therefore we can simply collapse all feature by assiging a number as for each range. Then we find the similarity to a certain Cluster rules using the following formula.

Let the similarity between a customer and a Cluster be define by $S(\mathbf{x_i}, \mathbf{c_j})$ Where $\mathbf{x_i}$ is the feature vector defined for the i^{th} customer, and $\mathbf{c_i}$ for the j^{th} cluster. A feature vector is defined as [Average Spend Cluster Index, Average Basket Size Cluster Index, Average Visit Frequeny Index]

Now,

$$S(x_i, c_j) = \sum_{k=0}^3 \left(x_i[k] == c_j[k] \right)$$

where k stands for the k^{th} feature

That is the count of the entires where the cluster and customer has equal feature Indexes Now the Cluster of the i^{th} customer is given as,

Cluster of the
$$i^{th}$$
 customer = $\arg\max_{j=0}^5 S(x_i,c_j)$

11.1 Calculating Cluster Similarities

```
[382]: score_given_data =classification_data.copy()

PREMIUM = 'PREMIUM'
LOYAL = 'LOYAL'
FREQ = 'FREQ'
MED = 'MED'
LOW = 'LOW'

PREMIUM_VEC = {SPEND_SCORE:3, VISIT_SCORE:3, BASKET_SCORE:3}
LOYAL_VEC = {SPEND_SCORE:2, VISIT_SCORE:2, BASKET_SCORE:3}
```

```
FREQ_VEC = {SPEND_SCORE:2, VISIT_SCORE:4, BASKET_SCORE:2}
      MED_VEC = {SPEND_SCORE:1,VISIT_SCORE:1,BASKET_SCORE:1}
      LOW_VEC = {SPEND_SCORE:0,VISIT_SCORE:0,BASKET_SCORE:0}
      Types = [PREMIUM,LOYAL,FREQ,MED,LOW]
      Vecs = [PREMIUM_VEC,LOYAL_VEC,FREQ_VEC,MED_VEC,LOW_VEC]
      for ct,vec in zip(Types,Vecs):
          scores = (score_given_data[SPEND_SCORE] == vec[SPEND_SCORE]).astype(int)__
       print(ct)
         score_given_data[ct] = scores
      #qet the column name that has the maximum value or values out of Types
      MAX_CUSTOMER_TYPE_SCORE = 'MAX_SCORE'
      score_given_data[MAX_CUSTOMER_TYPE_SCORE] =_
       ⇒score_given_data[[PREMIUM,LOYAL,FREQ,MED,LOW]].max(axis=1)
     PREMIUM
     LOYAL
     FREQ
     MED
     LOW
     11.2 Calculaing the Cluster Type
[383]: final_result = score_given_data.copy()
      CUSTOMER_TYPE = 'CUSTOMER_TYPE'
      final result[CUSTOMER TYPE] = final result[[PREMIUM,LOYAL,FREQ,MED,LOW]].
       →idxmax(axis=1)
      final_result[CUSTOMER_TYPE].value_counts()
[383]: MED
                203581
      LOW
                203542
      LOYAL
                 71275
      PREMIUM
                 50887
                 40715
      FREQ
      Name: CUSTOMER_TYPE, dtype: int64
[384]: final_result[[CUS_ID,CUSTOMER_TYPE]]
[384]:
             customer id CUSTOMER TYPE
      0
                                 LOW
```

PREMIUM

1

```
2
                    3
                                 LOW
3
                    4
                                 MED
4
                   5
                                 MED
569995
              341740
                                 MED
569996
              215276
                            PREMIUM
569997
                                 LOW
               11515
569998
              205260
                                 MED
569999
                                 LOW
              244801
```

[570000 rows x 2 columns]

12 Saving the Data

```
[385]: customer_id CUSTOMER_TYPE
0 1 Low level
1 2 High end - Premium
2 3 Low level
3 4 Medium level
4 5 Medium level
```

13 Checking the Results

```
[386]: validating_set = final_result.copy()
```

13.1 Proving that there are no Customers who have more than one compatible cluster

```
[387]: 1 570000
dtype: int64
Since all results have only one Max score there is no ambiguity

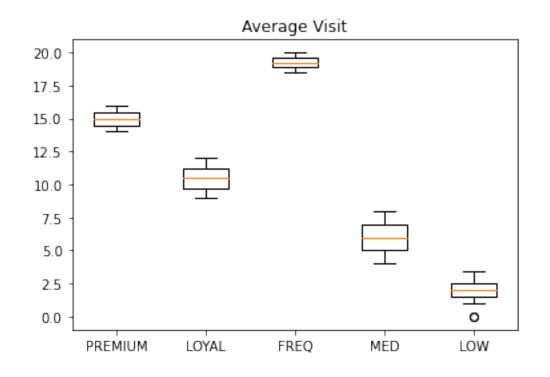
[]:
```

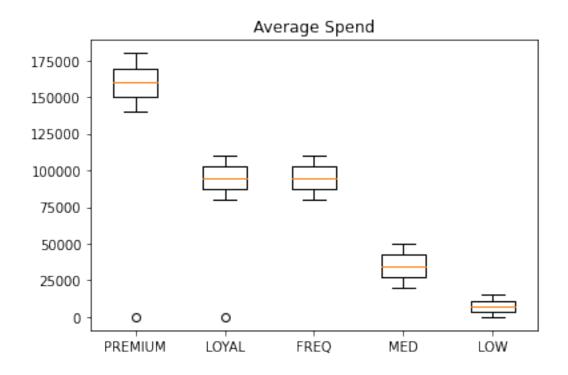
13.2 Checking that the Distributions of Feature Values with the Final Classification Match with Expectation

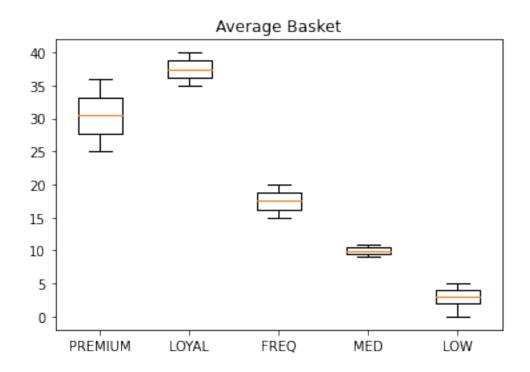
```
[388]: plt.title("Average Visit")
       plt.boxplot(
           [validating_set[validating_set[CUSTOMER_TYPE] == type] [AVG_VISIT].
        dropna() [validating_set[validating_set[CUSTOMER_TYPE] ==type] [AVG_VISIT].
        dropna().between(0,Average_Visit.VERY_HIGH[1])] for type in Types],
           labels=Types
       plt.show()
       plt.title("Average Spend")
       plt.boxplot(
           [validating_set[validating_set[CUSTOMER_TYPE] == type] [AVG_SPEND].
        dropna() [validating_set[validating_set[CUSTOMER_TYPE] ==type] [AVG_SPEND] .
        ⇒dropna().between(0,Monthly_Spend.VERY_HIGH[1])] for type in Types],
           labels=Types
       plt.show()
       plt.title("Average Basket")
       plt.boxplot(
           [validating_set[validating_set[CUSTOMER_TYPE] == type] [AVG_BASKET_SIZE] .

¬dropna() [validating_set[validating_set[CUSTOMER_TYPE] == type] [AVG_BASKET_SIZE] .

        dropna().between(0,Basket_Sizes.VERY_HIGH[1])] for type in Types],
           labels=Types
       plt.show()
```







14 Checking the Nature of the customers who had only similarity of 2

	customer_id	average_monthly	spend	avera	ge monthly vis	it frequency
2	- 3	•	6812.0		0 = 7 =	2.11
7	8	1	2656.0			2.13
24	25	4	1329.0			NaN
52	53	17	1010.0			NaN
53	54	10	4457.0			18.88
••	•••		•			•••
559914	559915	4	5023.0			NaN
559945	559946	4	9533.0			5.87
559959	559960		NaN			5.80
559970	559971	9	5444.0			19.85
559972	559973	1	3981.0			2.74
	average_mont	hly_basket_size	VISIT_S	SCORE	BASKET_SCORE	SPEND_SCORE
2		NaN		0	-1	0
7		NaN		0	-1	0
24		10.32		-1	1	1

52				35.0	3	-1	3	3
53				Na	.N	4	-1	2
				•••		•••	•••	•••
559914				9.8	2	-1	1	1
559945				Na	.N	1	-1	1
559959				9.8	7	1	1	-1
559970				Na	.N	4	-1	2
559972				Na	.N	0	-1	0
	PREMIUM	LOYAL	FREQ	MED	LOW	MAX_SCORE	CUSTOMER_TYPE	
2	0	0	0	0	2	2	LOW	
7	0	0	0	0	2	2	LOW	
24	0	0	0	2	0	2	MED	
52	2	1	0	0	0	2	PREMIUM	
53	0	1	2	0	0	2	FREQ	
					•••	•••		
559914	0	0	0	2	0	2	MED	
559945	0	0	0	2	0	2	MED	
559959	0	0	0	2	0	2	MED	
559970	0	1	2	0	0	2	FREQ	
559972	0	0	0	0	2	2	LOW	

[28031 rows x 14 columns]

	[390] :	score	is	2.dropna()	describe ((`)
1		PCOTE	T 12	Z · ur opna ()	, deperties	٠,	,

[390]:	score_is_2.dropna().describe()										
[390]:		customer_id	average_monthly_spend av		verage_monthly_visit_frequency \						
	count	18.000000	1.80	0000e+01		18.000000					
	mean	354434.666667	4.93	4703e+06		46.058333					
	std	159311.270356	1.29	3920e+07		100.784055 1.250000					
	min	252.000000	0.00	0000e+00							
	25%	322879.500000	9.54	9.543150e+04		11.930000					
	50%	325078.000000	1.48	9220e+05		15.310000 19.630000 432.740000					
	75%	515194.750000	1.61	2676e+06							
	max	558101.000000	4.83	3000e+07							
		average_monthl	y_basket_size	VISIT_SCORE	BASKET_SCORE	SPEND_SCORE \					
	count		18.000000	18.000000	18.000000	18.000000					
	mean		69.655000	1.666667	1.277778	0.388889					
	std		110.472051	1.847096	1.673515	1.539247					
	min		2.160000	-1.000000	-1.000000	-1.000000					
	25%		12.427500	0.000000	0.000000	-1.000000					
	50%		29.285000	2.500000	1.500000	0.000000					
	75%		37.470000	3.000000	3.000000	2.000000					
	max		385.040000	4.000000	3.000000	3.000000					
		PREMIUM	LOYAL F	REQ MI	ED LOW	MAX_SCORE					

count	18.000000	18.000000	18.000000	18.000000	18.000000	18.0
mean	0.888889	0.722222	0.44444	0.222222	0.44444	2.0
std	0.963382	0.751904	0.783823	0.646762	0.783823	0.0
min	0.000000	0.000000	0.000000	0.000000	0.000000	2.0
25%	0.000000	0.000000	0.000000	0.000000	0.000000	2.0
50%	0.500000	1.000000	0.000000	0.000000	0.000000	2.0
75%	2.000000	1.000000	0.750000	0.000000	0.750000	2.0
max	2.000000	2.000000	2.000000	2.000000	2.000000	2.0

We see that the ones that have given a similarity score of 2 is the ones that are outliers the, two entires which had zero as spending be mistake (This is the above 18 rows), and entires with NA. Since we already know that the ones with NA only have one NA it is reasonable that all have a similarity score of 2. Furthermore it shows that even there there is no ambiguity

Thus our classification is Justified