Gerrymandering: Exploring the Data

An, Anderson, and Deck

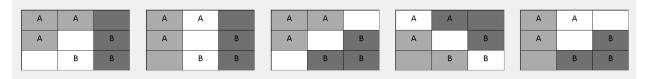
4/4/2021

We are interested in a more reasonable naming device to provide a better way to think about each map.

For the gerrymandered maps we refer to them as $Gerry_i$ for $i \in \{A, B\}$ where i identifies the player for whom the map is gerrymandered (Player A is advantaged in $Gerry_A$). That is, Map 1 will be $Gerry_B$ and Map 5 will be $Gerry_A$.

As the remaining maps are symmetric at the player level we reference $Sym_{d,z}$ for $d \in \{1,3\}$ and $z \in \{1,3\}$ where d denotes the number of competitive districts and z denotes the number of zones within each competitive district. That is, Map 2 will be $Sym_{1,1}$, Map 3 will be $Sym_{1,3}$, and Map 4 will be $Sym_{3,1}$.

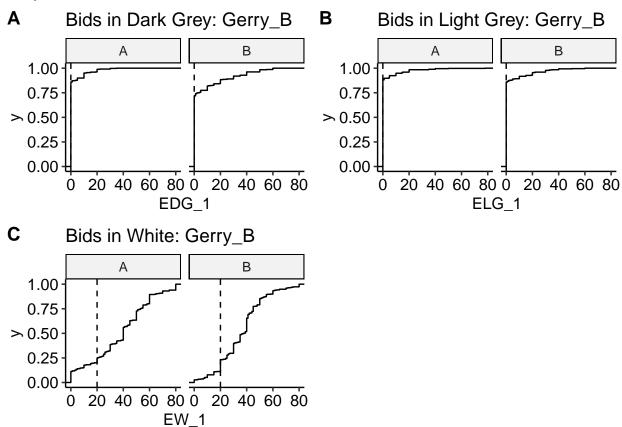
For reference:



Reading from left to right we have Gerry_B, Symm_1_1, Symm_1_3, Symm_3_1, and Gerry_A.

Note that in Gerry_A, Gerry_B, Symm_1_1, and Symm_1_3 the white district is the only competitive district in the sense that only the competition within the white district determines whether a subject wins that Map. The exception is Symm_3_1 in which it is logical to bid in any district as no district is guaranteed a victor.

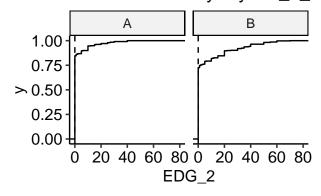
Gerry_B

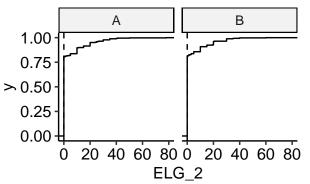


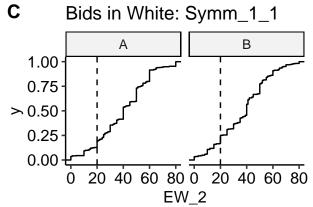
 $Symmetric_{1,1}$

A Bids in Dark Grey: Symm_1_1 B

Bids in Light Grey: Symm_1_1



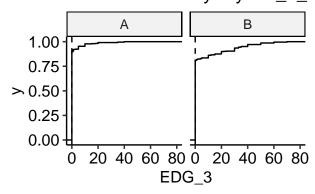


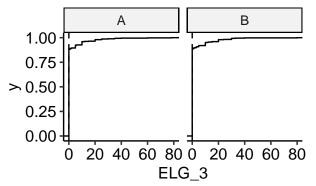


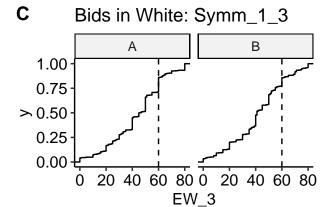
 $Symmetric_{1,3}$

A Bids in Dark Grey: Symm_1_3 B

Bids in Light Grey: Symm_1_3



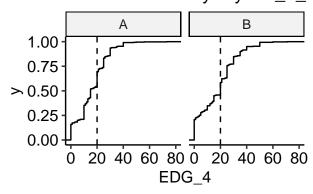


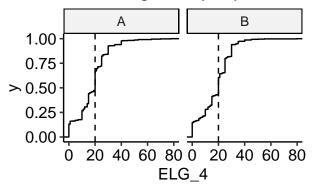


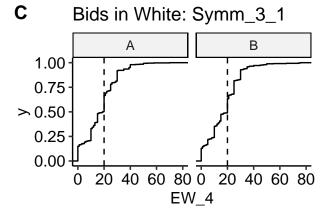
 $Symmetric_{3,1}$

A Bids in Dark Grey: Symm_3_1 B

Bids in Light Grey: Symm_3_1

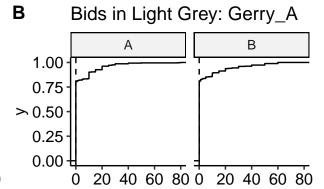




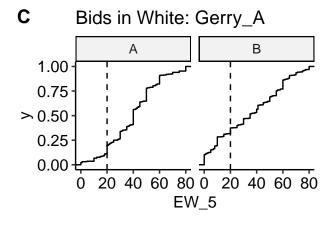


Gerry_A

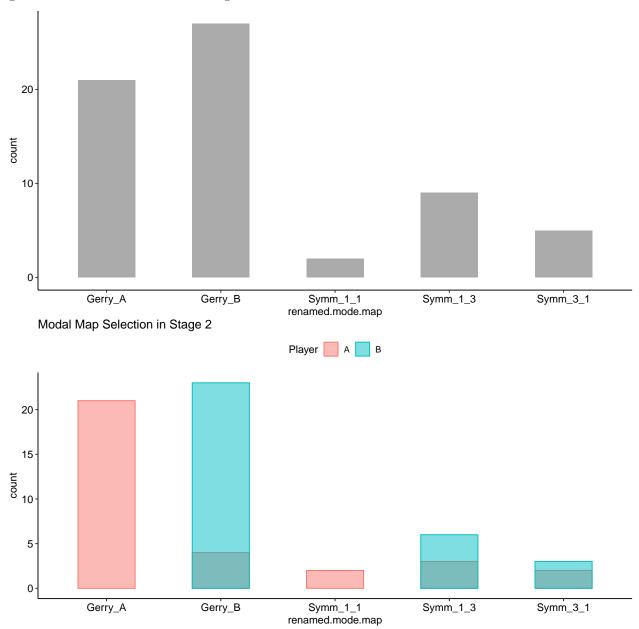
A Bids in Dark Grey: Gerry_A 1.00 0.75 > 0.50 0.25 0.00 0 20 40 60 80 0 20 40 60 80 EDG_5



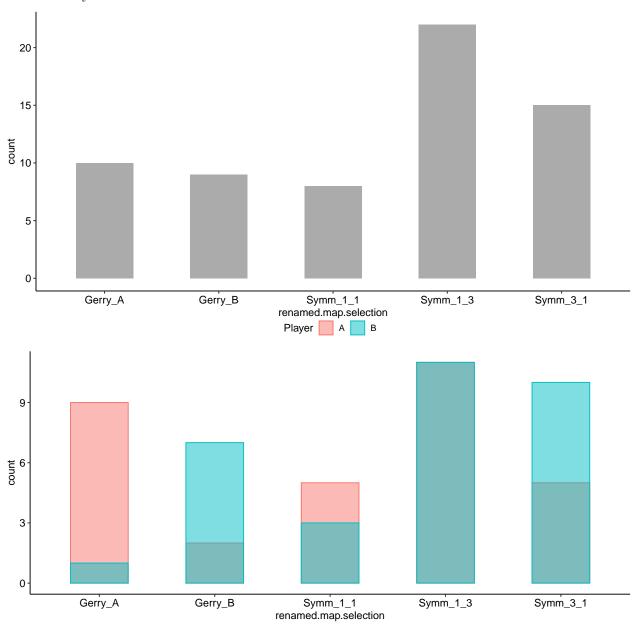
ELG_5



Recall, Player A should pick Gerry_A and Player B should pick Gerry_B if they are choosing the map that gives them the best chance of winning.



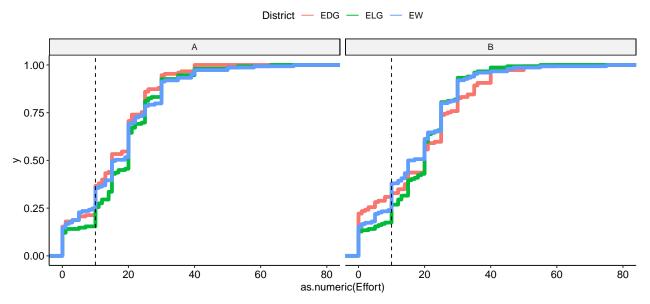
The first figure depicts the map choices during the final stage for all participants. The second figure is of interest because we might have spillover from the previous stage whereby participants choose the map they have been choosing without really paying attention to the implications... or they could just be flipping the coin that they are the "incumbent" after randomization occurs.



Now we are addressing:

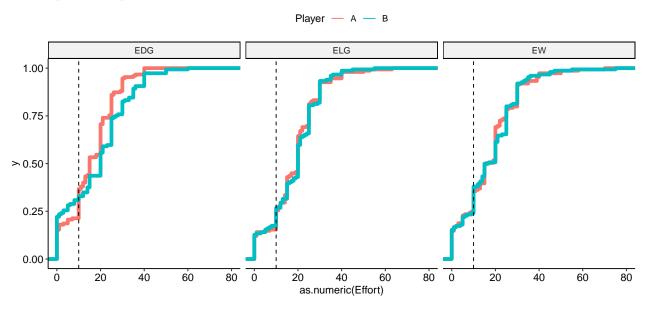
- 1) For the map where they should be bidding on every region, I would like to see player A's 3 CDFs overlaid on top of each other because there's no reason for them to differ but it's hard to tell in the version you sent.
- 2) I would also like to see player B's CDFs overlaid

Symm_3_1



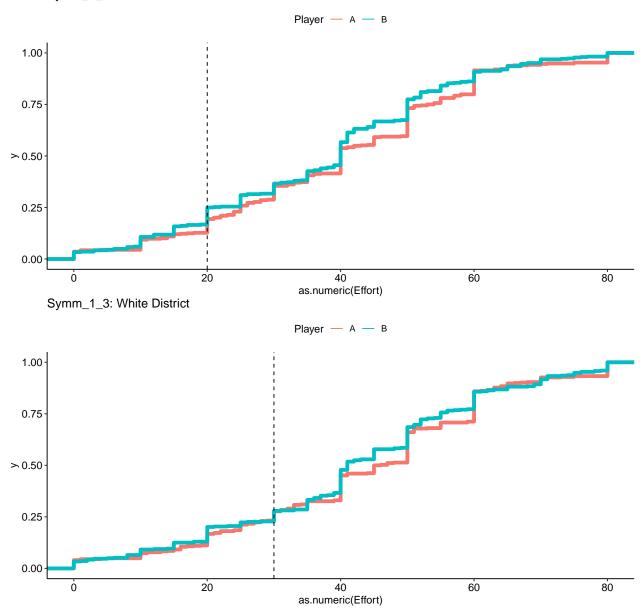
3), 4), & 5) Separately I would like to overlay player A and B's CDFs for districts 1-3 in the map where they bid on all districts since there's no reason for these to differ.

Symm_3_1 by District

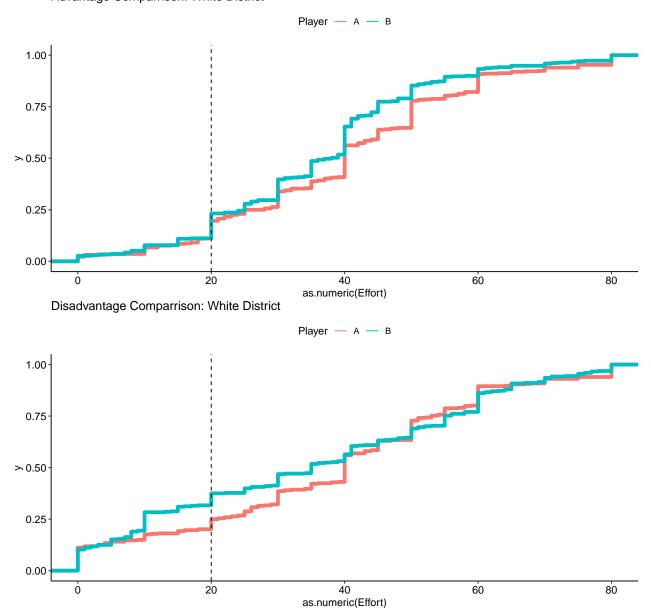


6) & 7) On each of the two maps where the players are symmetric and only bidding on one district I would like to see their CDF's overlaid.

Symm_1_1: White District

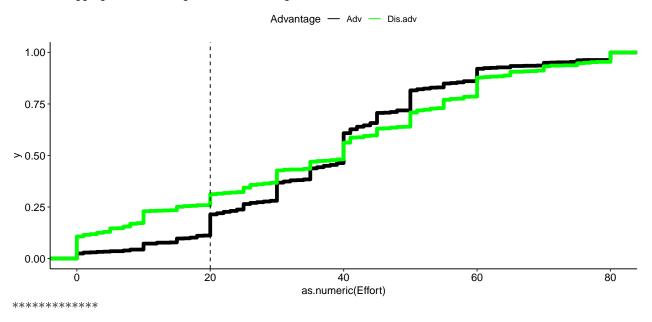


- 8) Overlay the CDFs of the advantage player in Gerry_B and the advantage player in Gerry_A.
- 9) Overlay the CDFs of the disadvantaged player in Gerry_B and the disadvantaged player in Gerry_A. Advantage Comparison: White District



10) Assuming the two CDFs in 8) look the same and the two CDFs in 9) look the same, then make a combined advantaged CDF and a combined disadvantaged CDF and overlay those so we me can easily see how being advantaged matters.

Disaggregated: Advantaged vs Disadvantaged



To be added as of 2021-04-07

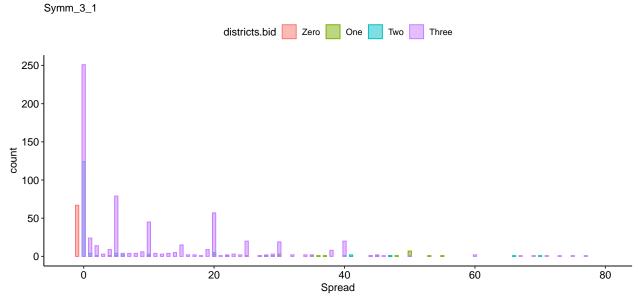
[DONE]- One other small improvement to all the CDF figures would be to add a vertical line at the theoretical prediction for that map.

[DONE]- It looks like on Symm_3_1 there is a fair amount of zero bids placed on each map. My guess is that we have lots of instances where people bid on ONLY TWO MAPS. Could you find the proportions of cases (bid tripled by a person in a period) in Symm_3_1 where the person bid 0 on all three districts (that is in a period bid 0,0,0), bid 0 on one district (so 0,x,y or x,0,y, or x,y,0 for x,y>0), bid 0 on two districts, and bid 0 on none of the districts? My guess is that there are lots of cases where they bid 0 on one map.

```
##
   # A tibble: 1 x 9
##
     n.records n.all.zeros n.one.district n.two.districts n.three.distric~
##
         <int>
                      <dbl>
                                     <dbl>
                                                      <dbl>
                                                                        <dbl>
## 1
           896
                         67
                                        29
                                                                          645
                                                        155
## # ... with 4 more variables: pct.zeros <dbl>, pct.bid.one <dbl>,
       pct.bid.two <dbl>, pct.bid.three <dbl>
```

[DONE]- Look at "spread" of own bids across Symm_3_1 (max bid in any district of Symm_3_1 - min bid in any district in Symm_3_1); we'd like to see this overall (graph?) and just in the cases they bid a positive amount on everything then, for the case they only bid on 2, look at the max minus the median

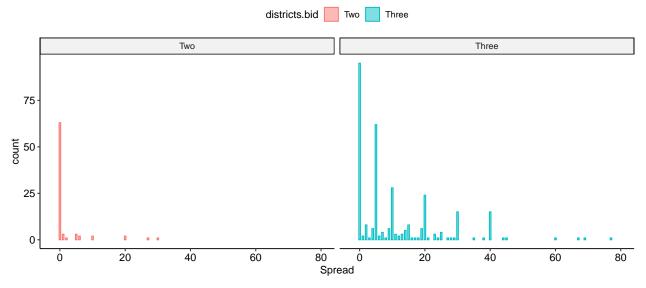
Unadjusted Spread



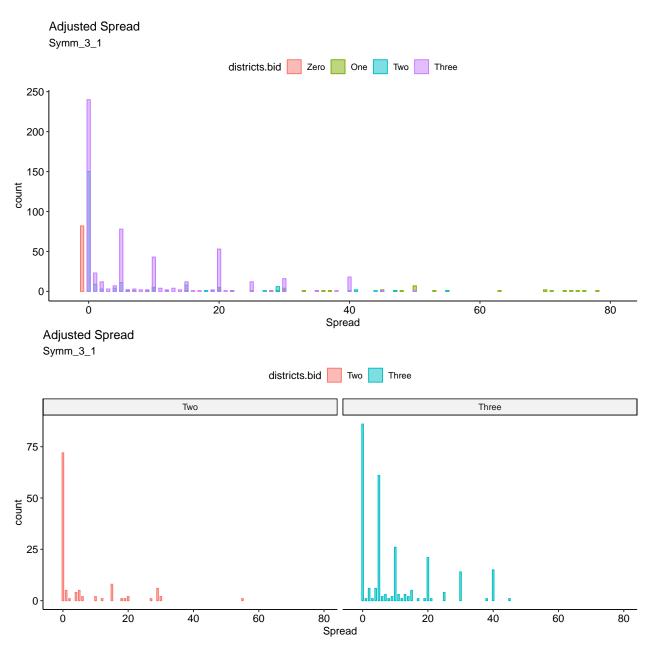
Separate graphs for bidding in two and separate for bidding in three (maybe under table with pct of Zero, One, Two, and Three bids in Symmetric_Map_3,1)

Unadjusted Spread





```
## # A tibble: 1 x 9
##
     n.records n.all.zeros n.one.district n.two.districts n.three.distric~
##
         <int>
                      <dbl>
                                     <dbl>
                                                      <dbl>
                                                                       <dbl>
           896
                         82
                                        47
                                                        218
                                                                         549
## 1
## # ... with 4 more variables: pct.zeros <dbl>, pct.bid.one <dbl>,
       pct.bid.two <dbl>, pct.bid.three <dbl>
```



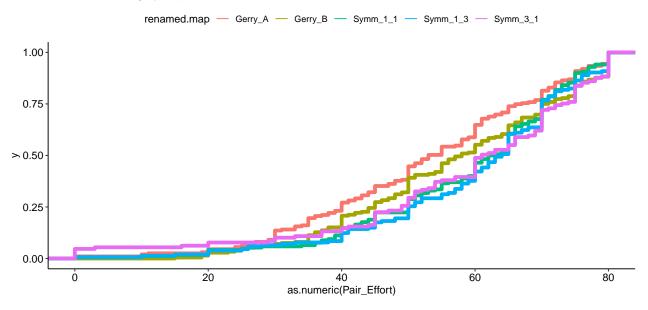
[DONE]- As a first pass, we should run a K-S tests to see if the various pairs of distributions you overlaid are the same.

```
##
## Two-sample Kolmogorov-Smirnov test
##
## data: as.numeric(unlist(EDG4A)) and as.numeric(unlist(EDG4B))
## D = 0.10938, p-value = 0.009408
## alternative hypothesis: two-sided
##
## Two-sample Kolmogorov-Smirnov test
##
## data: as.numeric(unlist(ELG4A)) and as.numeric(unlist(ELG4B))
## D = 0.069196, p-value = 0.2337
## alternative hypothesis: two-sided
```

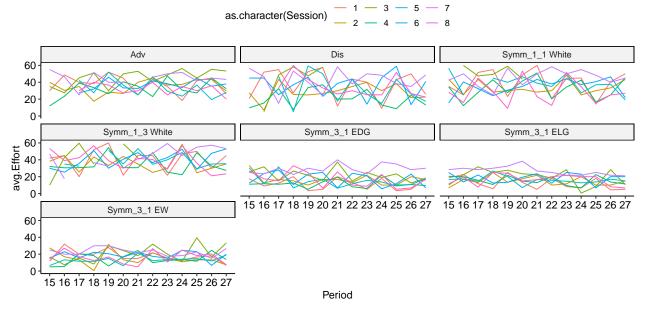
```
##
   Two-sample Kolmogorov-Smirnov test
##
##
## data: as.numeric(unlist(EW4A)) and as.numeric(unlist(EW4B))
## D = 0.035714, p-value = 0.9375
## alternative hypothesis: two-sided
##
##
   Two-sample Kolmogorov-Smirnov test
##
## data: as.numeric(unlist(EW2A)) and as.numeric(unlist(EW2B))
## D = 0.087054, p-value = 0.06707
## alternative hypothesis: two-sided
##
##
   Two-sample Kolmogorov-Smirnov test
##
## data: as.numeric(unlist(EW3A)) and as.numeric(unlist(EW3B))
## D = 0.078125, p-value = 0.1298
## alternative hypothesis: two-sided
##
   Two-sample Kolmogorov-Smirnov test
##
##
## data: as.numeric(unlist(ADV.A)) and as.numeric(unlist(ADV.B))
## D = 0.14286, p-value = 0.000214
## alternative hypothesis: two-sided
##
   Two-sample Kolmogorov-Smirnov test
##
##
## data: as.numeric(unlist(Dis.ADV.A)) and as.numeric(unlist(Dis.ADV.B))
## D = 0.125, p-value = 0.001824
## alternative hypothesis: two-sided
##
   Two-sample Kolmogorov-Smirnov test
## data: as.numeric(unlist(ADV.All)) and as.numeric(unlist(Dis.ADV.All))
## D = 0.15848, p-value = 3.369e-10
## alternative hypothesis: two-sided
```

[DONE]- Also, since it seems that things are symmetric, it would be good to make a single graph that has the cdfs of total pair level investment by map (here a pair in a period is an observation). That way we can see if more is spent on some maps than others.

Pair Total Bidding by Map



[DONE]- One thing that would be good to do is for each kind of choice (advantaged in map 1 or 5, disadvantaged in map 1 or 5, white in map 2, white in map 3, all regions in map 4) take the average across all subjects in a period. Then plot a time series of those averages. This should include phase 1 and 2 so we can see if map selection impacted bidding on maps.



[DONE]- A small cosmetic point is to make sure you keep the x-axis fixed to make comparisons between graphs easier. It is not a big deal for this, just something to do in general. In the first part of the document you have some that include 80 and some that don't.

[DONE]- Average bid on each district on each map by role

##		Player	Map	District	avg.Effort
##	1	A	1	EDG	1.680804
##	2	A	1	ELG	1.758929
##	3	A	1	EW	37.776786
##	4	Α	1	рEDG	6.495536

##	5	Α	1	pELG	2.662946
##	6	Α	1	pEW	36.203125
##	7	Α	2	EDG	1.968750
##	8	Α	2	ELG	3.379464
##	9	Α	2	EW	39.957589
##	10	Α	2	pEDG	6.176339
##	11	Α	2	pELG	2.901786
##	12	Α	2	pEW	37.515625
##	13	Α	3	EDG	1.008929
##	14	Α	3	ELG	1.671875
##	15	Α	3	EW	43.598214
##	16	Α	3	pEDG	5.017857
##	17	Α	3	pELG	1.669643
##	18	A	3	pEW	42.062500
##	19	A	4	EDG	16.325893
##	20	A	4	ELG	17.897321
##	21	A	4	EW	17.348214
##	22	A	4	pEDG	18.087054
##	23	A	4	pELG	17.917411
##	24	A	4	pEW	17.341518
##	25	A	5	EDG	1.258929
##	26	A	5	ELG	3.261161
##	27	A	5	ELG	40.026786
##	28	A	5	pEDG	4.515625
##	29	A	5	pELG	3.901786
##	30	A	5	pEW	34.750000
##	31	В	1	EDG	6.495536
##	32	В	1	ELG	2.662946
##	33	В	1	EW	36.203125
##	34	В	1	pEDG	1.680804
##	35	В	1	pELG	1.758929
##	36	В	1	pEW	37.776786
##	37	В	2	EDG	6.176339
##	38	В	2	ELG	2.901786
##	39	В	2	EW	37.515625
##	40	В	2	pEDG	1.968750
##	41	В	2	pELG	3.379464
##	42	В	2	pEW	39.957589
##	43	В	3	EDG	5.017857
##	44	В	3	ELG	1.669643
##	45	В	3	EW	42.062500
##	46	В	3	pEDG	1.008929
##	47	В	3	pELG	1.671875
##	48	В	3	pEW	43.598214
##	49	В	4	EDG	18.087054
##	50	В	4	ELG	17.917411
##	51	В	4	EW	17.341518
##	52	В	4	pEDG	16.325893
##	53	В	4	pELG	17.897321
##	54	В	4	pEW	17.348214
##	55	В	5	EDG	4.515625
##	56	В	5	ELG	3.901786
##	57	В	5	ELG	34.750000
##	58	В	5	pEDG	1.258929
##	00	Ď	Э	PEDG	1.256929

```
## 59 B 5 pELG 3.261161
## 60 B 5 pEW 40.026786
```

[DONE]- Percent gerrymandering in stage 2

[1] 0.6875

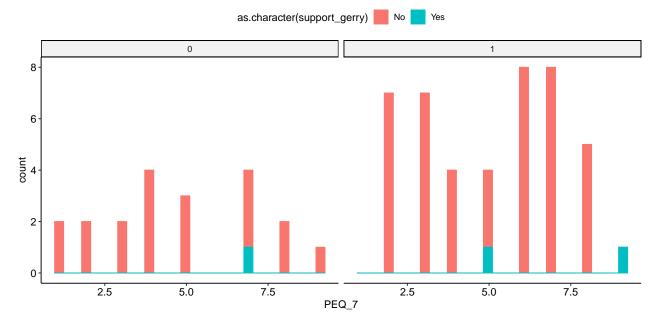
[DONE]- Percentage picking each map in stage 3

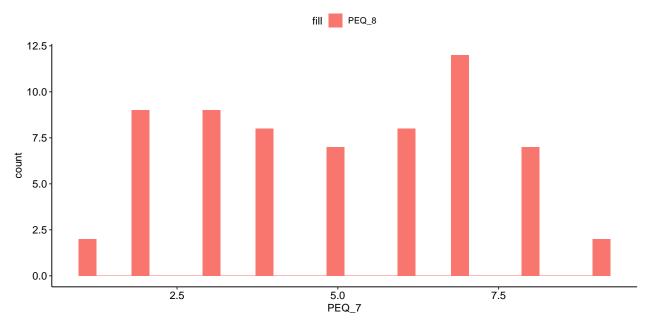
##		Map_Selection	n	<pre>pct.of.pop</pre>
##	1	-99	1	2
##	2	1	9	14
##	3	2	8	12
##	4	3	22	34
##	5	4	15	23
##	6	5	9	14

[DONE]- Rank sum test looking at whether or not their political views influence whether they gerrymander or not...?

Before the rank sum test let's recall the PEQ relevant for the test.

PEQ_7: "On a scale of 1 to 9, how would you describe your political views with 1 being extremely liberal (i.e. to the left of the Democratic Party), 5 being centrist (i.e. falling between the Democratic Party and the Republican Party), and 9 being extremely conservative (i.e. to the right of the Republican party)." (multiple choice; 1 - 9)





```
## [1] 29
## [1] 28
## [1] 0.6875
```

Now, onto the rank sum test.

```
##
## Wilcoxon rank sum test with continuity correction
##
## data: PEQ_7 by as.character(gerry)
## W = 412.5, p-value = 0.693
## alternative hypothesis: true location shift is not equal to 0
```

So we fail to reject the null that the political preference is the same regardless of whether they actually gerrymandered.

What about based on whether they *support* gerrymandering? (a.k.a PEQ_8)

```
##
## Wilcoxon rank sum test with continuity correction
##
## data: PEQ_7 by support_gerry
## W = 44, p-value = 0.1319
## alternative hypothesis: true location shift is not equal to 0
```

Also fail to reject the null that political preference is the same regardless of whether they support gerrymandering.

[DONE]- political beliefs and saying gerrymandering (**done above**; no diff. between gerrymandering and politics)

[DONE]- how either of those answers depend on whether they actually gerrymander (**above** = no diff. b/w support gerry and politics; **below** = no diff in support of gerrymandering based on whether actually gerry)

```
##
## Wilcoxon rank sum test with continuity correction
##
## data: PEQ_8 by as.character(gerry)
```

```
## W = 438, p-value = 0.9527 ## alternative hypothesis: true location shift is not equal to 0
```

[DONE]- Z test of whether observations are same for number of people selecting whether they support gerrymandering or not (same # of people in both camps; probably going to be diff given the distribution between y and n)

(^In Sig.)

[DONE]- Of the people who say they don't support it, what % actually did it

```
nrow(subset(gerry_and_politics, PEQ_8 == 2 & gerry == 1))/nrow(subset(gerry_and_politics, PEQ_8 == 2))
```

[1] 0.6885246

[DONE]- for the same split, did they say they like gerrymandering or not proportionately (are the proportions the same) ???????? Only have 3 that say support gerrymandering... is this enough to make any determination?

(Do you like it as a function of whether you actually did it)

[1] 0.04545455

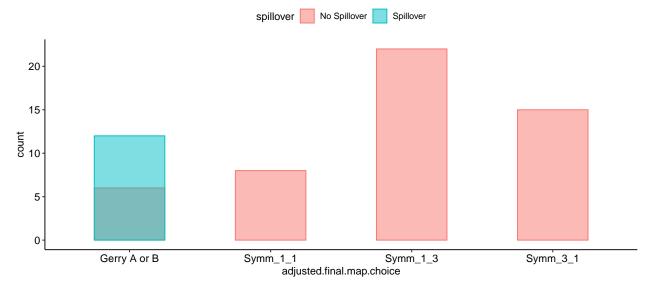
[1] 0.05

This is for the bar graph

- when they don't know who they are which maps are they choosing
- distinguish b/w people choosing gerrymandered map based on if they are choosing it after having chosen it in previous periods
- 4 bars; gerrymander A and B on one column (two colored bars; one color is "gerrymandered for self" other color "gerrymandered for other")
- Some people like gerrymandered maps even not knowing who they are
- Some pick gerrymander for self (have been picking the map for themselves in previous round)

Map Choice in Final Period

Spillover includes only those who actually gerrymandered and chose their previously advantaged map both in stage 2 and stage



[DONE]- Regression from Deck's notes

 $Effort = \alpha + \beta_1 P layer_B + \beta_2 Map_2 + \beta_3 Map_2 P layer_B + \beta_4 Map_3 + \beta_5 Map_3 P layer_B + \beta_6 Map_4 + \beta_7 Map_4 P layer_B + \beta_8 Map_5 + \beta_8 M$

```
##
## Call:
## lm(formula = Effort ~ Player B + Gerry B + Gerry B * Player B +
       Symm_1_3 + Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B +
##
##
       Gerry_A + Gerry_A * Player_B, data = regress_df)
##
## Residuals:
##
     Min
              1Q Median
                            3Q
                                  Max
## -54.80 -14.38
                  1.75 15.62 36.52
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
                                  1.2075 38.964 < 2e-16 ***
## (Intercept)
                      47.0500
                                                   0.6819
## Player_B
                      0.7000
                                  1.7077
                                           0.410
## Gerry_B
                      -3.5656
                                  1.7077 -2.088
                                                   0.0369 *
## Symm_1_3
                      1.2000
                                  1.7077
                                           0.703
                                                   0.4823
## Symm_3_1
                      7.3281
                                           4.291 1.83e-05 ***
                                  1.7077
## Gerry A
                      -1.5281
                                  1.7077 -0.895
                                                   0.3709
## Player_B:Gerry_B
                      2.1531
                                  2.4151
                                          0.892
                                                   0.3727
## Player B:Symm 1 3
                     0.4344
                                  2.4151
                                          0.180
                                                   0.8573
## Player_B:Symm_3_1 -0.2781
                                  2.4151 -0.115
                                                   0.9083
## Player_B:Gerry_A
                      -2.2187
                                  2.4151 -0.919
                                                   0.3583
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 21.6 on 3190 degrees of freedom
## Multiple R-squared: 0.02821,
                                   Adjusted R-squared: 0.02547
## F-statistic: 10.29 on 9 and 3190 DF, p-value: 8.547e-16
The below tells us the role does not really matter.
library(car)
## Loading required package: carData
##
## Attaching package: 'car'
## The following object is masked from 'package:dplyr':
##
##
       recode
#linearHypothesis(map.player.interaction, c("Map_5 + Player_B:Map_5 = 0"))
linearHypothesis(map.player.interaction, c("Player_B + Player_B:Symm_1_3 = 0")) ## in sig at 5%
## Linear hypothesis test
##
## Hypothesis:
## Player B + Player B:Symm 1 3 = 0
##
## Model 1: restricted model
## Model 2: Effort ~ Player_B + Gerry_B + Gerry_B * Player_B + Symm_1_3 +
##
       Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B + Gerry_A +
##
       Gerry_A * Player_B
##
##
                RSS Df Sum of Sq
                                      F Pr(>F)
    Res.Df
      3191 1488684
## 1
```

```
3190 1488478 1
                          205.89 0.4412 0.5066
## 2
linearHypothesis(map.player.interaction, c("Player_B + Player_B:Symm_3_1 = 0")) ## in sig at 5%
## Linear hypothesis test
##
## Hypothesis:
## Player_B + Player_B:Symm_3_1 = 0
## Model 1: restricted model
## Model 2: Effort ~ Player_B + Gerry_B + Gerry_B * Player_B + Symm_1_3 +
       Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B + Gerry_A +
##
       Gerry_A * Player_B
##
                RSS Df Sum of Sq
##
    Res.Df
                                     F Pr(>F)
       3191 1488506
## 1
                          28.477 0.061 0.8049
## 2
       3190 1488478 1
linearHypothesis(map.player.interaction, c("Player_B + Player_B:Symm_1_3 = 0", "Player_B + Player_B:Sym
## Linear hypothesis test
##
## Hypothesis:
## Player_B + Player_B:Symm_1_3 = 0
## Player_B + Player_B:Symm_3_1 = 0
## Player_B = 0
##
## Model 1: restricted model
## Model 2: Effort ~ Player_B + Gerry_B + Gerry_B * Player_B + Symm_1_3 +
##
       Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B + Gerry_A +
       Gerry_A * Player_B
##
##
##
    Res.Df
                RSS Df Sum of Sq
                                      F Pr(>F)
## 1
       3193 1488790
                          312.77 0.2234 0.8802
## 2
       3190 1488478 3
linearHypothesis(map.player.interaction, c("Player_B + Gerry_B + Player_B:Gerry_B = Gerry_A"))
## Linear hypothesis test
##
## Hypothesis:
## Player_B + Gerry_B - Gerry_A + Player_B:Gerry_B = 0
## Model 1: restricted model
## Model 2: Effort ~ Player_B + Gerry_B + Gerry_B * Player_B + Symm_1_3 +
       Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B + Gerry_A +
##
##
       Gerry_A * Player_B
##
##
    Res.Df
                RSS Df Sum of Sq
                                      F Pr(>F)
## 1
      3191 1488584
                        106.44 0.2281 0.633
       3190 1488478 1
linearHypothesis(map.player.interaction, c("Player_B + Gerry_A + Player_B:Gerry_A = Gerry_B"))
## Linear hypothesis test
##
## Hypothesis:
```

```
## Player_B - Gerry_B + Gerry_A + Player_B:Gerry_A = 0
##
## Model 1: restricted model
## Model 2: Effort ~ Player_B + Gerry_B + Gerry_B * Player_B + Symm_1_3 +
       Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B + Gerry_A +
       Gerry A * Player B
##
##
                RSS Df Sum of Sq
##
     Res.Df
                                       F Pr(>F)
## 1
       3191 1488521
       3190 1488478 1
                          43.056 0.0923 0.7613
linearHypothesis(map.player.interaction, c(
  "Player_B + Gerry_B + Player_B:Gerry_B = Gerry_A", "Player_B + Gerry_A + Player_B:Gerry_A = Gerry_B"
## Linear hypothesis test
##
## Hypothesis:
## Player_B + Gerry_B - Gerry_A + Player_B:Gerry_B = 0
## Player_B - Gerry_B + Gerry_A + Player_B:Gerry_A = 0
## Player_B + Player_B:Symm_1_3 = 0
## Player_B + Player_B:Symm_3_1 = 0
## Player_B = 0
##
## Model 1: restricted model
## Model 2: Effort ~ Player_B + Gerry_B + Gerry_B * Player_B + Symm_1_3 +
       Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B + Gerry_A +
##
##
       Gerry A * Player B
##
##
    Res.Df
                RSS Df Sum of Sq
                                       F Pr(>F)
## 1
       3195 1488940
       3190 1488478 5
                          462.26 0.1981 0.9633
Justified ignoring player role in comparing treatments since the joint test (that player A and B play the same)
is not rejected.
regress df <- df %>% dplyr::select(Session, Period, Subject, Player, TE 1:TE 5) %>%
  filter(Period >= 20 & Period < 25) %>%
  gather(Map, Effort, TE 1:TE 5)
regress_df <- regress_df %>% mutate(subject.id = Session*8-(8-Subject),
                                     Player_B = ifelse(Player== "B", 1, 0),
         Gerry_B = ifelse(Map == "TE_1", 1, 0),
         Symm_1_1 = ifelse(Map == "TE_2", 1, 0),
         Symm_1_3 = ifelse(Map == "TE_3", 1, 0),
         Symm_3_1 = ifelse(Map == "TE_4", 1, 0),
         Gerry_A = ifelse(Map == "TE_5", 1, 0),
         Adv = ifelse((Map == "TE 1" & Player == "B") | (Map == "TE 5" & Player == "A"), 1,0),
         Disadv = ifelse((Map == "TE_1" & Player == "A") | (Map == "TE_5" & Player == "B"), 1,0),
         Stage_2_indicator = ifelse((Period > 24 & Period < 28), 1, 0))</pre>
map.adv.interaction <- lm(</pre>
  Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period + Adv*Period + Disadv*Period + Symm_1_3*Period +
  data = regress df
```

```
summary(map.adv.interaction)
##
## Call:
## lm(formula = Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period +
       Adv * Period + Disadv * Period + Symm_1_3 * Period + Symm_3_1 *
##
##
       Period, data = regress_df)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                      Max
## -54.856 -14.291
                    2.741 14.120 40.447
##
## Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   67.9906 18.2584
                                       3.724 0.000203 ***
## Adv
                   -9.5219
                              25.8212 -0.369 0.712354
## Disadv
                              25.8212 -0.038 0.969498
                   -0.9875
## Symm_1_3
                   -10.5156
                              25.8212 -0.407 0.683881
                              25.8212
                                       0.237 0.812808
## Symm_3_1
                    6.1156
## Period
                   -0.9875
                              0.8282 -1.192 0.233313
## Adv:Period
                                       0.309 0.756988
                    0.3625
                               1.1713
## Disadv:Period
                   -0.1562
                               1.1713 -0.133 0.893893
## Symm_1_3:Period 0.5312
                               1.1713
                                       0.454 0.650203
## Symm_3_1:Period
                     0.0250
                               1.1713
                                       0.021 0.982974
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 20.95 on 1590 degrees of freedom
## Multiple R-squared: 0.03311,
                                   Adjusted R-squared: 0.02764
## F-statistic: 6.05 on 9 and 1590 DF, p-value: 2.195e-08
linearHypothesis(map.adv.interaction, c("Symm_1_3 = 10"))
## Linear hypothesis test
## Hypothesis:
## Symm_1_3 = 10
## Model 1: restricted model
## Model 2: Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period + Adv *
       Period + Disadv * Period + Symm_1_3 * Period + Symm_3_1 *
##
##
       Period
##
##
    Res.Df
              RSS Df Sum of Sq
                                    F Pr(>F)
       1591 698291
       1590 698014 1
                        277.13 0.6313 0.427
## 2
linearHypothesis(map.adv.interaction, c("Symm_3_1 = 10")) # so map 4 is pushing expenditure up, but not
## Linear hypothesis test
## Hypothesis:
\#\# Symm_3_1 = 10
##
## Model 1: restricted model
```

```
## Model 2: Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period + Adv *
##
       Period + Disadv * Period + Symm_1_3 * Period + Symm_3_1 *
##
       Period
##
##
    Res.Df
               RSS Df Sum of Sq
                                     F Pr(>F)
## 1
       1591 698024
       1590 698014 1
                         9.9347 0.0226 0.8804
linearHypothesis(map.adv.interaction, c("Symm_1_3 = Symm_3_1")) # map 4 has a larger effect than map 3
## Linear hypothesis test
##
## Hypothesis:
## Symm_1_3 - Symm_3_1 = 0
##
## Model 1: restricted model
## Model 2: Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period + Adv *
##
       Period + Disadv * Period + Symm_1_3 * Period + Symm_3_1 *
##
##
    Res.Df
##
               RSS Df Sum of Sq
                                     F Pr(>F)
## 1
       1591 698196
       1590 698014 1
                         182.12 0.4149 0.5196
linearHypothesis(map.adv.interaction, c("Adv = Disadv"))
## Linear hypothesis test
##
## Hypothesis:
## Adv - Disadv = 0
## Model 1: restricted model
## Model 2: Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period + Adv *
       Period + Disadv * Period + Symm_1_3 * Period + Symm_3_1 *
##
##
       Period
##
               RSS Df Sum of Sq
     Res.Df
                                     F Pr(>F)
       1591 698062
## 1
                         47.958 0.1092 0.7411
## 2
       1590 698014 1
# testing on periods
linearHypothesis(map.adv.interaction, c("Adv:Period = 0", "Disadv:Period = 0", "Symm_1_3:Period = 0", "
## Linear hypothesis test
##
## Hypothesis:
## Adv:Period = 0
## Disadv:Period = 0
## Symm 1 3:Period = 0
## Symm_3_1:Period = 0
## Period = 0
##
## Model 1: restricted model
## Model 2: Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period + Adv *
##
       Period + Disadv * Period + Symm_1_3 * Period + Symm_3_1 *
##
       Period
```

```
##
               RSS Df Sum of Sq
##
     Res.Df
                                      F Pr(>F)
       1595 700451
## 1
       1590 698014
                         2437.4 1.1104 0.3527
## 2
                    5
[Done?]- Regression of average bid as function of period with dummy variable for Map selection phase (periods
(so we just want the impact on the map selection phase on the average map level bids)
## lm(formula = Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Stage_2_indicator +
       Adv * Stage_2_indicator + Disadv * Stage_2_indicator + Symm_1_3 *
       Stage_2_indicator + Symm_3_1 * Stage_2_indicator, data = regress_df)
##
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                        Max
## -52.931 -14.719
                     2.563
                           15.281
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                               46.2656
                                            1.2057 38.374 < 2e-16 ***
                               -1.5469
                                            1.7051 -0.907 0.36438
## Adv
## Disadv
                                -4.4250
                                            1.7051
                                                    -2.595 0.00951 **
## Symm_1_3
                                1.1719
                                            1.7051
                                                     0.687 0.49196
## Symm 3 1
                                6.6656
                                            1.7051
                                                     3.909 9.5e-05 ***
## Stage_2_indicator
                               -4.2708
                                                    -2.169
                                                           0.03016 *
                                            1.9688
## Adv:Stage_2_indicator
                                2.2917
                                            2.7844
                                                     0.823
                                                            0.41056
## Disadv:Stage_2_indicator
                                0.9927
                                            2.7844
                                                     0.357
                                                           0.72147
## Symm_1_3:Stage_2_indicator
                                1.0677
                                            2.7844
                                                     0.383 0.70141
## Symm_3_1:Stage_2_indicator
                               -1.8844
                                            2.7844
                                                    -0.677 0.49861
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 21.57 on 2550 degrees of freedom
## Multiple R-squared: 0.03027,
                                    Adjusted R-squared: 0.02685
## F-statistic: 8.844 on 9 and 2550 DF, p-value: 3.224e-13
linearHypothesis(stage_2_impact, c("Adv:Stage_2_indicator = 0", "Disadv:Stage_2_indicator = 0",
                                    "Symm_1_3:Stage_2_indicator = 0", "Symm_3_1:Stage_2_indicator = 0"))
## Linear hypothesis test
##
## Hypothesis:
## Adv:Stage_2_indicator = 0
## Disadv:Stage_2_indicator = 0
## Symm_1_3:Stage_2_indicator = 0
## Symm_3_1:Stage_2_indicator = 0
##
## Model 1: restricted model
## Model 2: Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Stage_2_indicator +
##
       Adv * Stage_2_indicator + Disadv * Stage_2_indicator + Symm_1_3 *
##
       Stage_2_indicator + Symm_3_1 * Stage_2_indicator
##
##
     Res.Df
                RSS Df Sum of Sq
                                       F Pr(>F)
```

1 2554 1187327 ## 2 2550 1186162 4 1165.2 0.6262 0.6438

Redo the regressions and tests with the data from only 20 through 24 (second half of stage 1) to account for potential learning. this is because the period coefficient shows a downward trend over time.

Below are the regressions and tests using only the last 5 periods from the first stage:

```
##
## Call:
## lm(formula = Effort ~ Player B + Gerry B + Gerry B * Player B +
       Symm_1_3 + Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B +
##
       Gerry_A + Gerry_A * Player_B, data = regress_df)
##
## Residuals:
##
      Min
                1Q Median
                                3Q
                                       Max
## -53.088 -14.325
                     3.125
                           14.344
                                    38,669
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                   1.659 27.529 < 2e-16 ***
                       45.656
## Player B
                       1.219
                                   2.345
                                           0.520 0.60339
## Gerry_B
                       -4.325
                                   2.345 -1.844 0.06537
## Symm 1 3
                        0.575
                                   2.345
                                           0.245 0.80637
                       7.431
## Symm_3_1
                                   2.345
                                           3.168 0.00156 **
## Gerry A
                       -1.331
                                   2.345 -0.568 0.57039
                                           0.773 0.43990
## Player_B:Gerry_B
                       2.562
                                   3.317
                                           0.360 0.71897
## Player B:Symm 1 3
                       1.194
                                   3.317
## Player_B:Symm_3_1
                       -1.531
                                   3.317 -0.462 0.64440
## Player_B:Gerry_A
                       -3.194
                                   3.317 -0.963 0.33576
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 20.98 on 1590 degrees of freedom
## Multiple R-squared: 0.03074,
                                    Adjusted R-squared:
## F-statistic: 5.603 on 9 and 1590 DF, p-value: 1.2e-07
and the tests for this regression:
library(car)
#linearHypothesis(map.player.interaction, c("Map_5 + Player_B:Map_5 = 0"))
linearHypothesis(map.player.interaction, c("Player_B + Player_B:Symm_1_3 = 0")) ## in siq at 5%
## Linear hypothesis test
##
## Hypothesis:
## Player_B + Player_B:Symm_1_3 = 0
## Model 1: restricted model
## Model 2: Effort ~ Player_B + Gerry_B + Gerry_B * Player_B + Symm_1_3 +
##
       Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B + Gerry_A +
##
       Gerry_A * Player_B
##
##
     Res.Df
               RSS Df Sum of Sq
                                    F Pr(>F)
       1591 700192
## 1
       1590 699726 1
                         465.61 1.058 0.3038
linearHypothesis(map.player.interaction, c("Player_B + Player_B:Symm_3_1 = 0")) ## in sig at 5%
## Linear hypothesis test
```

```
##
## Hypothesis:
## Player_B + Player_B:Symm_3_1 = 0
## Model 1: restricted model
## Model 2: Effort ~ Player_B + Gerry_B + Gerry_B * Player_B + Symm_1_3 +
       Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B + Gerry_A +
##
       Gerry_A * Player_B
##
                                     F Pr(>F)
##
     Res.Df
               RSS Df Sum of Sq
## 1
       1591 699734
       1590 699726 1
                         7.8125 0.0178 0.894
## 2
linearHypothesis(map.player.interaction, c("Player_B + Player_B:Symm_1_3 = 0", "Player_B + Player_B:Sym
## Linear hypothesis test
##
## Hypothesis:
## Player_B + Player_B:Symm_1_3 = 0
## Player_B + Player_B:Symm_3_1 = 0
## Player_B = 0
##
## Model 1: restricted model
## Model 2: Effort ~ Player_B + Gerry_B + Gerry_B * Player_B + Symm_1_3 +
##
       Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B + Gerry_A +
##
       Gerry_A * Player_B
##
##
    Res.Df
               RSS Df Sum of Sq
                                     F Pr(>F)
## 1
       1593 700319
       1590 699726 3
                         592.25 0.4486 0.7183
linearHypothesis(map.player.interaction, c("Player_B + Gerry_B + Player_B:Gerry_B = Gerry_A"))
## Linear hypothesis test
##
## Hypothesis:
## Player_B + Gerry_B - Gerry_A + Player_B:Gerry_B = 0
## Model 1: restricted model
## Model 2: Effort ~ Player_B + Gerry_B + Gerry_B * Player_B + Symm_1_3 +
##
       Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B + Gerry_A +
##
       Gerry_A * Player_B
##
##
    Res.Df
               RSS Df Sum of Sq
                                     F Pr(>F)
## 1
       1591 699776
                         49.613 0.1127 0.7371
       1590 699726
                   1
linearHypothesis(map.player.interaction, c("Player_B + Gerry_A + Player_B:Gerry_A = Gerry_B"))
## Linear hypothesis test
##
## Hypothesis:
## Player_B - Gerry_B + Gerry_A + Player_B:Gerry_A = 0
## Model 1: restricted model
## Model 2: Effort ~ Player_B + Gerry_B + Gerry_B * Player_B + Symm_1_3 +
```

```
##
       Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B + Gerry_A +
##
       Gerry_A * Player_B
##
               RSS Df Sum of Sq
##
    Res.Df
                                    F Pr(>F)
## 1
       1591 699809
                         83.028 0.1887 0.6641
## 2
       1590 699726 1
linearHypothesis(map.player.interaction, c(
  "Player_B + Gerry_B + Player_B:Gerry_B = Gerry_A", "Player_B + Gerry_A + Player_B:Gerry_A = Gerry_B"
## Linear hypothesis test
##
## Hypothesis:
## Player_B + Gerry_B - Gerry_A + Player_B:Gerry_B = 0
## Player_B - Gerry_B + Gerry_A + Player_B:Gerry_A = 0
## Player_B + Player_B:Symm_1_3 = 0
## Player_B + Player_B:Symm_3_1 = 0
## Player_B = 0
## Model 1: restricted model
## Model 2: Effort ~ Player_B + Gerry_B + Gerry_B * Player_B + Symm_1_3 +
       Symm_1_3 * Player_B + Symm_3_1 + Symm_3_1 * Player_B + Gerry_A +
##
       Gerry_A * Player_B
##
##
    Res.Df
               RSS Df Sum of Sq
                                     F Pr(>F)
## 1
       1595 700451
                         724.89 0.3294 0.8954
       1590 699726 5
```

The above tests allow us to ignore player role given the null hypothesis that players A and B do not differ in their behavior.

That is, we can run:

```
regress_df <- df %>% dplyr::select(Session, Period, Subject, Player, TE_1:TE_5) %>%
  filter(Period >= 20 & Period < 25) %>%
  gather(Map, Effort, TE_1:TE_5)
regress_df <- regress_df %>% mutate(subject.id = Session*8-(8-Subject),
                                     Player_B = ifelse(Player== "B", 1, 0),
         Gerry_B = ifelse(Map == "TE_1", 1, 0),
         Symm_1_1 = ifelse(Map == "TE_2", 1, 0),
         Symm_1_3 = ifelse(Map == "TE_3", 1, 0),
         Symm_3_1 = ifelse(Map == "TE_4", 1, 0),
         Gerry_A = ifelse(Map == "TE_5", 1, 0),
         Adv = ifelse((Map == "TE_1" & Player == "B") | (Map == "TE_5" & Player == "A"), 1,0),
         Disadv = ifelse((Map == "TE_1" & Player == "A") | (Map == "TE_5" & Player == "B"), 1,0),
         Stage_2_indicator = ifelse((Period > 24 & Period < 28), 1, 0))</pre>
map.adv.interaction <- lm(</pre>
 Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period + Adv*Period + Disadv*Period + Symm_1_3*Period +
  data = regress_df
  )
summary(map.adv.interaction)
```

```
##
## Call:
## lm(formula = Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period +
       Adv * Period + Disadv * Period + Symm_1_3 * Period + Symm_3_1 *
##
       Period, data = regress_df)
##
## Residuals:
       Min
##
                1Q Median
                                3Q
                                       Max
## -54.856 -14.291
                     2.741 14.120 40.447
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
                   67.9906
                              18.2584
                                       3.724 0.000203 ***
## (Intercept)
                              25.8212 -0.369 0.712354
## Adv
                   -9.5219
## Disadv
                              25.8212 -0.038 0.969498
                   -0.9875
## Symm_1_3
                  -10.5156
                              25.8212 -0.407 0.683881
                              25.8212
## Symm_3_1
                    6.1156
                                       0.237 0.812808
## Period
                   -0.9875
                              0.8282 -1.192 0.233313
                               1.1713
## Adv:Period
                    0.3625
                                       0.309 0.756988
## Disadv:Period
                   -0.1562
                                1.1713 -0.133 0.893893
## Symm_1_3:Period 0.5312
                                1.1713
                                       0.454 0.650203
## Symm_3_1:Period
                   0.0250
                                       0.021 0.982974
                                1.1713
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 20.95 on 1590 degrees of freedom
## Multiple R-squared: 0.03311,
                                    Adjusted R-squared: 0.02764
## F-statistic: 6.05 on 9 and 1590 DF, p-value: 2.195e-08
with tests:
linearHypothesis(map.adv.interaction, c("Symm 1 3 = 10"))
## Linear hypothesis test
##
## Hypothesis:
## Symm_1_3 = 10
## Model 1: restricted model
## Model 2: Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period + Adv *
       Period + Disadv * Period + Symm_1_3 * Period + Symm_3_1 *
##
##
       Period
##
              RSS Df Sum of Sq
                                    F Pr(>F)
##
    Res.Df
## 1
       1591 698291
       1590 698014 1
                        277.13 0.6313 0.427
linear Hypothesis (map.adv.interaction, c("Symm_3_1 = 10")) # so map 4 is pushing expenditure up, but not
## Linear hypothesis test
##
## Hypothesis:
\#\# Symm_3_1 = 10
## Model 1: restricted model
## Model 2: Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period + Adv *
```

```
##
       Period + Disadv * Period + Symm_1_3 * Period + Symm_3_1 *
##
       Period
##
##
    Res.Df
               RSS Df Sum of Sq
                                     F Pr(>F)
## 1
       1591 698024
## 2
       1590 698014 1
                         9.9347 0.0226 0.8804
linearHypothesis(map.adv.interaction, c("Symm_1_3 = Symm_3_1")) # map 4 has a larger effect than map 3
## Linear hypothesis test
## Hypothesis:
## Symm_1_3 - Symm_3_1 = 0
## Model 1: restricted model
## Model 2: Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period + Adv *
       Period + Disadv * Period + Symm_1_3 * Period + Symm_3_1 *
##
       Period
##
##
    Res.Df
               RSS Df Sum of Sq
                                     F Pr(>F)
       1591 698196
                         182.12 0.4149 0.5196
## 2
       1590 698014 1
linearHypothesis(map.adv.interaction, c("Adv = Disadv"))
## Linear hypothesis test
## Hypothesis:
## Adv - Disadv = 0
##
## Model 1: restricted model
## Model 2: Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period + Adv *
##
       Period + Disadv * Period + Symm_1_3 * Period + Symm_3_1 *
##
       Period
##
##
     Res.Df
               RSS Df Sum of Sq
                                     F Pr(>F)
       1591 698062
       1590 698014 1
                         47.958 0.1092 0.7411
# testing on periods
linearHypothesis(map.adv.interaction, c("Adv:Period = 0", "Disadv:Period = 0", "Symm_1_3:Period = 0", "
## Linear hypothesis test
##
## Hypothesis:
## Adv:Period = 0
## Disadv:Period = 0
## Symm_1_3:Period = 0
## Symm 3 1:Period = 0
## Period = 0
## Model 1: restricted model
## Model 2: Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Period + Adv *
##
       Period + Disadv * Period + Symm_1_3 * Period + Symm_3_1 *
##
       Period
##
```

```
Res.Df
               RSS Df Sum of Sq
                                     F Pr(>F)
## 1
       1595 700451
       1590 698014 5
                         2437.4 1.1104 0.3527
Now, let's look specifically at the effect of map selection:
##
## Call:
## lm(formula = Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Stage_2_indicator +
       Adv * Stage_2_indicator + Disadv * Stage_2_indicator + Symm_1_3 *
##
       Stage_2_indicator + Symm_3_1 * Stage_2_indicator, data = regress_df)
##
## Residuals:
       Min
                10 Median
                                30
## -52.931 -14.719
                     2.563 15.281
##
## Coefficients:
                              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                               46.2656
                                           1.2057 38.374 < 2e-16 ***
                                           1.7051 -0.907 0.36438
## Adv
                               -1.5469
## Disadv
                               -4.4250
                                           1.7051
                                                   -2.595 0.00951 **
## Symm_1_3
                                1.1719
                                           1.7051
                                                    0.687 0.49196
## Symm_3_1
                                           1.7051
                                                    3.909 9.5e-05 ***
                                6.6656
## Stage_2_indicator
                               -4.2708
                                                   -2.169 0.03016 *
                                           1.9688
## Adv:Stage_2_indicator
                                2.2917
                                           2.7844
                                                    0.823 0.41056
                                                    0.357 0.72147
## Disadv:Stage_2_indicator
                                0.9927
                                           2.7844
## Symm_1_3:Stage_2_indicator
                                1.0677
                                           2.7844
                                                    0.383 0.70141
## Symm_3_1:Stage_2_indicator
                                           2.7844
                                                   -0.677 0.49861
                              -1.8844
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 21.57 on 2550 degrees of freedom
## Multiple R-squared: 0.03027,
                                    Adjusted R-squared: 0.02685
## F-statistic: 8.844 on 9 and 2550 DF, p-value: 3.224e-13
with joint test:
linearHypothesis(stage_2_impact, c("Adv:Stage_2_indicator = 0", "Disadv:Stage_2_indicator = 0",
                                   "Symm_1_3:Stage_2_indicator = 0", "Symm_3_1:Stage_2_indicator = 0"))
## Linear hypothesis test
##
## Hypothesis:
## Adv:Stage_2_indicator = 0
## Disadv:Stage_2_indicator = 0
## Symm_1_3:Stage_2_indicator = 0
## Symm_3_1:Stage_2_indicator = 0
##
## Model 1: restricted model
## Model 2: Effort ~ Adv + Disadv + Symm_1_3 + Symm_3_1 + Stage_2_indicator +
##
       Adv * Stage_2_indicator + Disadv * Stage_2_indicator + Symm_1_3 *
##
       Stage_2_indicator + Symm_3_1 * Stage_2_indicator
##
##
     Res.Df
                RSS Df Sum of Sq
                                      F Pr(>F)
## 1
       2554 1187327
       2550 1186162 4
                          1165.2 0.6262 0.6438
```

Now, we need to verify the other tests still hold with this sub-sample. We might also be interested in comparing a few tables.

To start:

```
summarize(map_four_bidding, n.records = n(),
          n.all.zeros = sum(all.zeros.bids),
          n.one.district = sum(one.bids),
          n.two.districts = sum(two.bids),
          n.three.districts = sum(all.three.bids),
          pct.zeros = n.all.zeros/n.records,
          pct.bid.one = n.one.district/n.records,
          pct.bid.two = n.two.districts/n.records,
          pct.bid.three = n.three.districts/n.records,
## # A tibble: 1 x 9
   n.records n.all.zeros n.one.district n.two.districts n.three.distric~
##
         <int>
                     dbl>
                                    <dbl>
                                                    dbl>
                                                                      <dbl>
## 1
           896
                        67
                                       29
                                                       155
                                                                        645
## # ... with 4 more variables: pct.zeros <dbl>, pct.bid.one <dbl>,
     pct.bid.two <dbl>, pct.bid.three <dbl>
# compared to
summarize(subset(map_four_bidding, Period > 19), n.records = n(),
          n.all.zeros = sum(all.zeros.bids),
          n.one.district = sum(one.bids),
          n.two.districts = sum(two.bids),
          n.three.districts = sum(all.three.bids),
          pct.zeros = n.all.zeros/n.records,
          pct.bid.one = n.one.district/n.records,
          pct.bid.two = n.two.districts/n.records,
          pct.bid.three = n.three.districts/n.records,
## # A tibble: 1 x 9
    n.records n.all.zeros n.one.district n.two.districts n.three.distric~
##
         <int>
                     <dbl>
                                    <dbl>
                                                    <dbl>
                                                                      <dbl>
## 1
           576
                        54
                                       20
                                                                        414
## # ... with 4 more variables: pct.zeros <dbl>, pct.bid.one <dbl>,
      pct.bid.two <dbl>, pct.bid.three <dbl>
# the above have very little difference
Now, the K-S tests:
##
   Two-sample Kolmogorov-Smirnov test
##
## data: as.numeric(unlist(EDG4A)) and as.numeric(unlist(EDG4B))
## D = 0.13889, p-value = 0.007732
## alternative hypothesis: two-sided
##
##
   Two-sample Kolmogorov-Smirnov test
##
## data: as.numeric(unlist(ELG4A)) and as.numeric(unlist(ELG4B))
```

```
## D = 0.10764, p-value = 0.0711
## alternative hypothesis: two-sided
   Two-sample Kolmogorov-Smirnov test
##
##
## data: as.numeric(unlist(EW4A)) and as.numeric(unlist(EW4B))
## D = 0.0625, p-value = 0.6272
## alternative hypothesis: two-sided
##
   Two-sample Kolmogorov-Smirnov test
##
## data: as.numeric(unlist(EW2A)) and as.numeric(unlist(EW2B))
## D = 0.11111, p-value = 0.05713
## alternative hypothesis: two-sided
## Two-sample Kolmogorov-Smirnov test
## data: as.numeric(unlist(EW3A)) and as.numeric(unlist(EW3B))
## D = 0.059028, p-value = 0.6973
## alternative hypothesis: two-sided
##
## Two-sample Kolmogorov-Smirnov test
##
## data: as.numeric(unlist(ADV.A)) and as.numeric(unlist(ADV.B))
## D = 0.13889, p-value = 0.007732
## alternative hypothesis: two-sided
##
##
   Two-sample Kolmogorov-Smirnov test
## data: as.numeric(unlist(Dis.ADV.A)) and as.numeric(unlist(Dis.ADV.B))
## D = 0.13194, p-value = 0.01329
## alternative hypothesis: two-sided
##
## Two-sample Kolmogorov-Smirnov test
## data: as.numeric(unlist(ADV.All)) and as.numeric(unlist(Dis.ADV.All))
## D = 0.18576, p-value = 4.663e-09
## alternative hypothesis: two-sided
```