

静电场中的电介质

一、电介质

二、电极化

分子等效电偶极子模型

无极分子(电介质)

有极分子(电介质)

无极分子电子位移极化

有极分子取向极化

极化强度矢量 $\vec{P} = \frac{\sum \vec{p}}{\Delta V}$

$$\vec{E} = \vec{E}_0 + \vec{E}'$$

$$\vec{P} = \epsilon_0 \chi_e \vec{E} \quad \text{极化规律}$$

χ_e 极化率

$$q'_{in} = -\oint_S \vec{P} \cdot d\vec{z}$$

三、D高斯定律 *

$$\oint_S \vec{E} \cdot d\vec{z} = \frac{1}{\epsilon_0} (\sum q_{oin} + q'_{in})$$

$$\oint_S \vec{E} \cdot d\vec{z} = \sum q_{oin} + \left(\oint_S \vec{P} \cdot d\vec{z} \right)$$

$$\oint_S (\epsilon_0 \vec{E} + \vec{P}) \cdot d\vec{z} = \sum q_{oin}$$

令 $\vec{D} = \epsilon_0 \vec{E} + \vec{P}$ 电位移矢量

$$\oint_S \vec{D} \cdot d\vec{z} = \sum q_{oin} \quad (\text{D的高斯定律})$$

$$\vec{D} = \epsilon_0 \vec{E} + \epsilon_0 \chi_e \vec{E} = \epsilon_0 (1 + \chi_e) \vec{E}$$

令 $1 + \chi_e = \epsilon_r$ 相对介电常数

$$\vec{D} = \epsilon_0 \epsilon_r \vec{E} \quad \epsilon = \epsilon_0 \epsilon_r \quad (\epsilon \text{ 介电常量, 电容率})$$

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四、电容器. 电容.

均匀导体球: $U = \frac{Q}{4\pi\epsilon_0 R}$

$$C = \frac{Q}{U} = 4\pi\epsilon_0 R$$

C单位: $1F = \frac{1C}{1V} = 1C/V$ $1\mu F = 10^{-6}F$ $1pF = 10^{-12}F$.

$$C = \frac{Q}{U_A - U_B}$$

平行板电容器: $C = \frac{\epsilon_0 \epsilon_r S}{d} = \frac{\epsilon S}{d}$

柱形电容器:

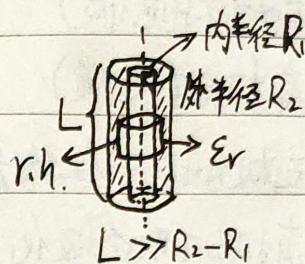
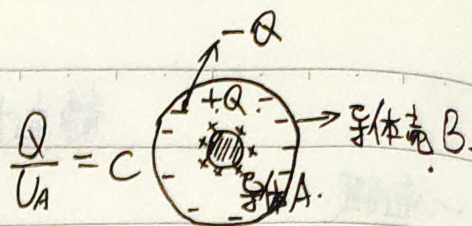
$$\phi_0 = \oint_S \vec{D} \cdot d\vec{S} = D 2\pi r h = \lambda h$$

$$D = \frac{\lambda}{2\pi r} \quad (R_1 < r < R_2)$$

$$E = \frac{D}{\epsilon_0 \epsilon_r} = \frac{\lambda}{2\pi \epsilon_0 \epsilon_r r}$$

$$U_A - U_B = \int_{R_1}^{R_2} \frac{\lambda}{2\pi \epsilon_0 \epsilon_r r} dr = \frac{\lambda}{2\pi \epsilon_0 \epsilon_r} \ln \frac{R_2}{R_1}$$

$$C = \frac{Q}{U_A - U_B} = \frac{\frac{\lambda L}{2\pi \epsilon_0 \epsilon_r \ln \frac{R_2}{R_1}}}{\frac{\lambda L}{2\pi \epsilon_0 \epsilon_r \ln \frac{R_2}{R_1}}} = \frac{2\pi \epsilon_0 \epsilon_r L}{\ln \frac{R_2}{R_1}}$$



五、电场容量.

电容器储能公式

$$W_e = \frac{1}{2} C U^2 = \frac{Q^2}{2C} = \frac{1}{2} U Q$$

电能密度 $W_e = \frac{1}{2} D E = \frac{1}{2} \epsilon E^2$

$$W_e = \int dW_e = \int_V W_e dv = \int_V \frac{1}{2} \epsilon E^2 dv$$