

Q3

First, sort the array by carrying out advanced sorting algorithms(i.e. The algorithms which takes $O(n \cdot \log n)$ to sort an integer list, like merge sort or quick sort etc). Allocate an array of size of n integers.then for every pairs of integers using the variation of binary search(find the position a of first element smaller or equals to the given number, find the position b of last element greater or equals to the given number) to obtain the elements within the range($b - a + 1$), and store this number into the array in the form of($\text{result}[n] = \text{the number of elements of array A within the range the tuple } n$).

Time complexity : $n \cdot \log(n)$ (sort the array) + $n * (2 * \log n)$, therefore the overall time complexity is $n * \log(n)$.

```
binary _search_last_upper_bound(A,n,U)
  ans = -1
  low = 1
  high = n
  while (low <= high) do
    int mid = low + (high - low + 1) / 2
    int midVal = a[mid]
    if (midVal <= key)
      ans = mid
      low = mid + 1
    else if (midVal > key)
      high = mid - 1
  end loop
  return ans;
```

```
binary_search_first_lower_bound(A,n,L)
ans = -1
  low = 1
  high = n
  while (low <= high) do
    int mid = low + (high - low + 1) / 2
    int midVal = a[mid]
    if (midVal <= key)
      low = mid + 1
    else if (midVal > key)
      ans = mid
      high = mid - 1
  end loop
  return ans;
```