

Q4

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The problem can be solved by solving following subproblem.

Subproblem: for every single day, find the activity that could achieve maximum accumulated enjoyment, the visitor (You in the context) can get.

\* For Q4 Assume that all the arrays are started from index 1

\* For Q4 Assume the enjoyments of different activities will be stored in a two-dimensional array

For example  $A[1][1]$  ----> the enjoyment of activity 1 on day 1.

Recursion:  $Opt(d,a) = \max\{Sum(Opt(d-1,not\_a\_1)) + A[a][d], Sum(Opt(d-1,not\_a\_2)) + A[a][d]\}$

Base case:  $Opt(0,a) = 0$ , if the day number is reached zero, then just simply return 0 as enjoyment.

1. The variable d is the current day
2. The variable a is the chosen activity
3. The not\_a\_1, and not\_a\_2 means the activities that are not chosen. For example  
 $Opt(4,1) = \max\{Opt(4-1, 2), Opt(4-1, 3)\}$

We will use another recursion function to trace the sequence.

$From(i) = \text{args } \max\{Sum(Opt(d-1,not\_a\_1)) + A[a][d], Sum(Opt(d-1,not\_a\_2)) + A[a][d]\}$

From(i) function will be used to trace of sequence of a of function Opt.

Procedure: we start to apply the Subproblem from the last day, which is day N, for day N we call the subproblems three times, and we want to find the maximum enjoyment obtained among these three  $\max\{Opt(N, 1), Opt(N,2), Opt(N,3)\}$ . And the returned maximum value will be the maximum enjoyment that a, and From(i) function will return the sequence of activity that would achieve this result.

Time complexity: as we can see from the recursion function that every subproblem is calling two other subproblems, and we are calling three subproblems on day N(starting point), then the complexity is  $3 * (n-1)^2$  which is  $O(n^2)$ .