

Exercise for Automata session (Part 1)

1 Introduction

In this exercise, we will be familiar with some basic concepts and definitions in automata: language, regular expression, finite automata and NFA (nondeterministic finite automata). Students should review the slide and related theoretical documents before doing the exercises below.

2 Example

Question 1.

Let $\Sigma = \{a, b\}$ and $L = \{ab, aa, baa\}$.

Which of the following strings are in L^* : *abaabaaabaa*, *aaaabaaaa*, *baaaaabaaaab*, *baaaaabaa*?

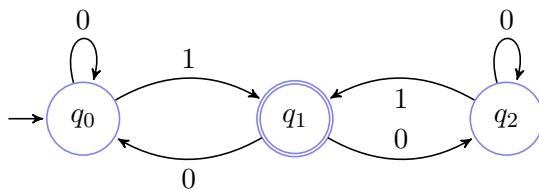
Solution.

abaabaaabaa, aaaabaaaa, baaaaabaa

□

Question 2.

Which of the strings 0001, 01001, 0000110 are accepted by the following automata:



Solution.

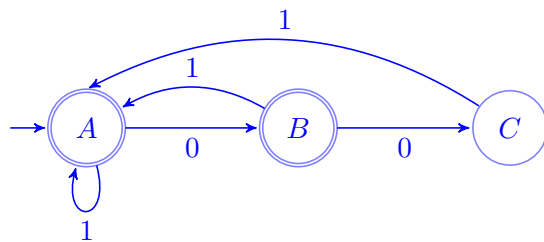
0001, 01001

□

Question 3.

Consider the set of strings on $\{0, 1\}$ in which every 00 is followed immediately by 1. For example 101, 0010, 0010011001 are in the language, but 0001 and 00100 are not. Construct an accepting automata.

Solution.



□

3 Homework

Question 4.

Let $\Sigma = \{a, b\}$.

Find all strings in $L = ((a + b)^*b(a + ab)^*)$ of length less than four.

Question 5.

Let $\Sigma = \{a, b\}$.

For which language it is true that $L = L^*$?

- a) $L = a^n b^{n+1} : n \geq 0$
b) $L = w : n_a(w) = n_b(w)$

Question 6.

Give a finite automata for the language $L = \{a, ba, aba, bab, bbba\}$.

Question 7.

Let $\Sigma = \{a\}$. Give finite automata for the sets consisting of

- a) all strings with exactly one a .
b) all strings with no more than three a 's.

Question 8.

Let $\Sigma = \{a, b\}$.

Give finite automata for the sets consisting of

- a) all strings with exactly one a .
b) all strings with no more than three a 's.

Question 9.

Let $\Sigma = \{a, b, c\}$. Give finite automata for the sets consisting of

- a) all strings with exactly one a .
b) all strings with no more than three a 's.
c) all strings with no more than three a 's and at least one b .

Question 10.

Give an automata for the language $L = \{ab^5wb^4 : w \in \{a, b\}^*\}$.

Question 11.

Find automatas for the following languages on $\Sigma = \{a, b\}$

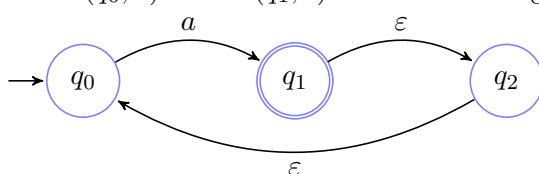
- a) $L_1 = \{w : |w| \bmod 3 = 0\}$
b) $L_2 = \{w : |w| \bmod 5 \neq 0\}$
c) $L_3 = \{w : n_a(w) \bmod 3 > 1\}$

Question 12.

Show that the language $L = a^n : n \geq 0, n \neq 4$ is regular.

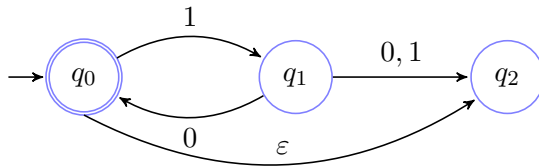
Question 13.

Find $\delta^*(q_0, a)$ and $\delta^*(q_1, \varepsilon)$ for the following automata



Question 14.

For the following automata, find $\delta^*(q_0, 1010)$ and $\delta^*(q_1, 00)$.

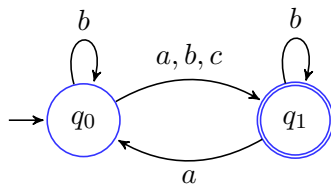


Question 15.

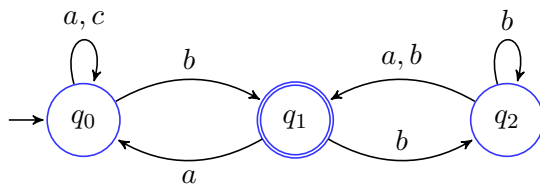
Find an automata with three states that accepts the language $\{ab, abc\}^*$

Question 16.

Give regular expression for the following finite automata



a)



b)

Question 17.

Let $\Sigma = \{a, b, c\}$.

Give complete automatas for the sets consisting of

- all strings with exactly one 'a'.
- all strings of even length.
- all strings which the number of appearances of 'b' is divisible by 3.
- all strings ending with 'a'.
- all strings not ending with 'a'.
- all non-empty strings not ending with 'a'.
- all strings with at least one 'a'.
- all strings with at most one 'a'.
- all strings without any 'a'.
- all strings including at least one 'a' and whose the first appearance of 'a' is not followed by a 'c'.

Complete automata: a finite automata in which from each state, it is defined precisely when receiving any event.