Optimization and Computational Linear Algebra for Data Science
Outline

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1. Vector spaces

1. General definitions
2. Linear dependency
3. Proof of Theorem 2.1

2. Linear transformations

1. Linear transformations
2. Matrix representation
3. Kernel and image

3. Rank

1. More on basis
2. Definition of the rank
3. Properties of the rank
4. Transpose of a matrix, symmetric matrices

4. Norm and dot product

1. Norm
2. Dot product
3. Orthogonality
4. Orthogonal projection and distance to a subspace

5. Matrices and orthogonality

1. Gram-Schmidt orthogonalisation method
2. Orthogonal matrices

6. Eigenvalues, eigenvectors and Markov chains

1. Eigenvalues and eigenvectors
2. Application to Markov chains
3. First definitions and properties
4. Invariant measures and the Perron-Frobenius Theorem
5. Proof of Theorem 2.1
6. Example: Google's PageRank algorithm

7. Singular value decomposition

1. Spectral Theorem
2. Singular value decomposition
3. Best-fitting subspace
4. Properties
5. Conclusion
6. Geometric interpretation of SVD
7. Another interpretation of the singular vectors