

Mecánica de medios continuos

Parcial I-Punto I

- Definimos las constantes y los espacios con los cuales se va a trabajar

```
In[1]:= a = 8.5*^-3;
k = 5.66*^-6;
cr = 3700;
xx = Range[0, 25000, 1];
yy = Range[0, 5000, 1];
tt = Range[0, 50, 0.05];
la = 40*^9;
g = 40*^9;
```

- Definimos los desplazamientos

```
In[9]:= u = Function[{x, y, t},
  a * (Exp[-0.8475*k*y] - 0.5773*Exp[-0.3933*k*y]) * Sin[k*(cr*t - x)]];
v = Function[{x, y, t}, a * (0.8475*Exp[-0.8475*k*y] + 1.4679*Exp[-0.3933*k*y]) *
  Cos[k*(cr*t - x)]];
w = Function[{x, y, t}, 0];
```

- Evaluamos si se puede utilizar el tensor infinitesimal

```
In[679]:= gradU = Grad[{u[x, y, t], v[x, y, t], w[x, y, t]}, {x, y, z}];
Maximize[Norm[gradU], {x, y, t}]
Out[680]= {1.11372*10^-7, {x → 7.5764, y → 39.5354, t → 74.3147}}
```

- Dado que la máxima norma es mucho menor que 1, podemos utilizar la aproximación infinitesimal para el tensor de Green y de Almansi (son lo mismo)

I. Escriba el tensor de Green y Almansi, dado que para desplazamientos infinitesimales son lo mismo

```
In[1215]:= ge = (gradU + Transpose[gradU]) / 2
Out[1215]= { {-4.811*10^-8 (e^-4.79685*10^-6 y - 0.5773 e^-2.22608*10^-6 y) Cos[5.66*10^-6 (3700 t - x)], 1/2 (0.0085 (-4.79685*10^-6 e^-4.79685*10^-6 y + 1.28511*10^-6 e^-2.22608*10^-6 y) Sin[5.66*10^-6 (3700 t - x)] + 4.811*10^-8 (0.8475 e^-4.79685*10^-6 y + 1.4679 e^-2.22608*10^-6 y) Sin[5.66*10^-6 (3700 t - x)]), 0}, {1/2 (0.0085 (-4.79685*10^-6 e^-4.79685*10^-6 y + 1.28511*10^-6 e^-2.22608*10^-6 y) Sin[5.66*10^-6 (3700 t - x)] + 4.811*10^-8 (0.8475 e^-4.79685*10^-6 y + 1.4679 e^-2.22608*10^-6 y) Sin[5.66*10^-6 (3700 t - x)]), 0.0085 (-4.06533*10^-6 e^-4.79685*10^-6 y - 3.26766*10^-6 e^-2.22608*10^-6 y) Cos[5.66*10^-6 (3700 t - x)], 0}, {0, 0, 0} }
```

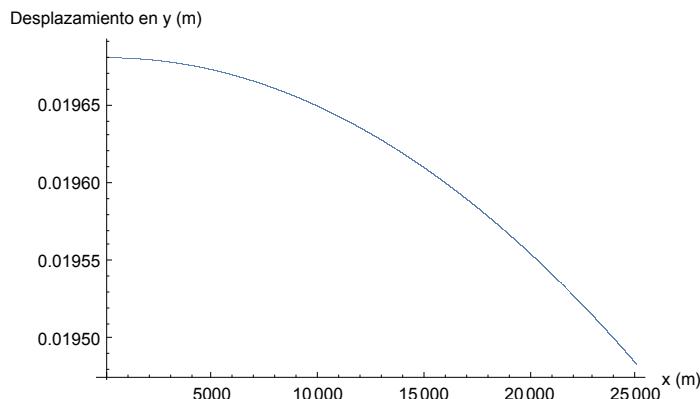
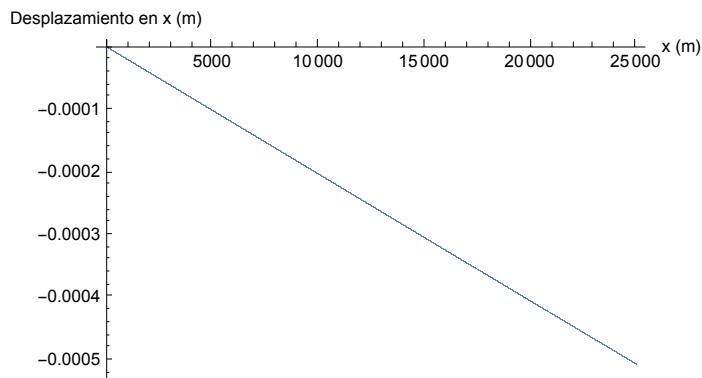
- Encontramos el tensor de esfuerzos

```
In[825]:= sij = 2 * g * ge + Tr[ge] * la * IdentityMatrix[3];
Dimensions[sij]
Out[826]= {3, 3}
```

2. Diagrama la forma de la onda en la superficie libre ($y=0$)

- Para $t=0$

```
uy0t0 = Evaluate[u[x, 0, 0]] /. {x -> xx};
vy0t0 = Evaluate[v[x, 0, 0]] /. {x -> xx};
data1u = Thread[{xx, uy0t0}];
data1v = Thread[{xx, vy0t0}];
ListPlot[data1u, AxesLabel -> {"x (m)", "Desplazamiento en x (m)"}]
ListPlot[data1v, AxesLabel -> {"x (m)", "Desplazamiento en y (m)"}]
```



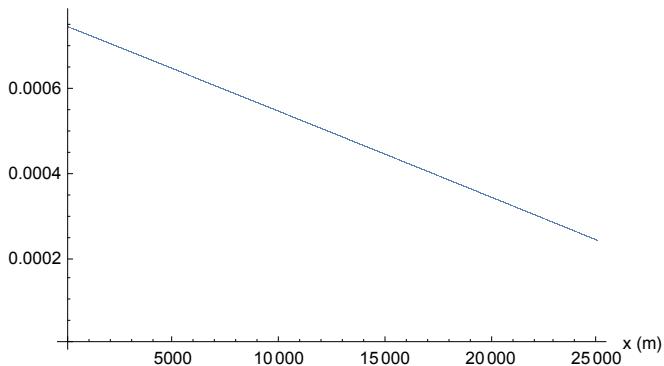
- Para $t=10$ s

```

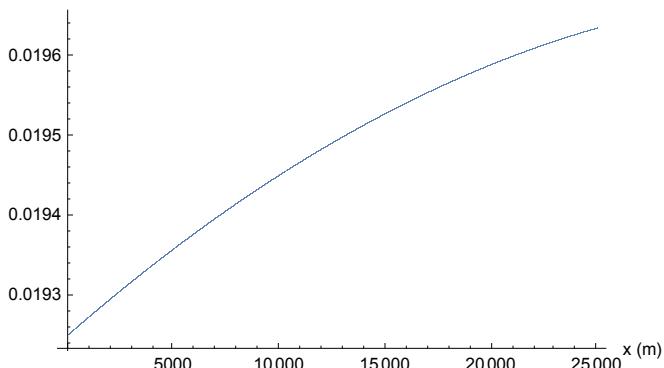
uy0t10 = Evaluate[u[x, 0, 10]] /. {x -> xx};
vy0t10 = Evaluate[v[x, 0, 10]] /. {x -> xx};
data2u = Thread[{xx, uy0t10}];
data2v = Thread[{xx, vy0t10}];
ListPlot[data2u, AxesLabel -> {"x (m)", "Desplazamiento en x (m)"}]
ListPlot[data2v, AxesLabel -> {"x (m)", "Desplazamiento en y (m)"}]

```

Desplazamiento en x (m)



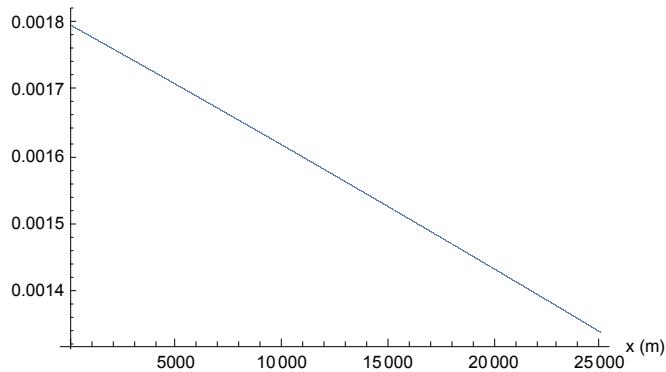
Desplazamiento en y (m)



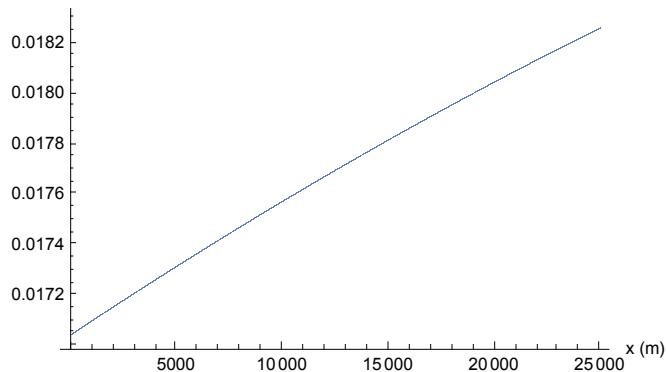
- Para t=25 s

```
uy0t25 = Evaluate[u[x, 0, 25]] /. {x -> xx};
vy0t25 = Evaluate[v[x, 0, 25]] /. {x -> xx};
data3u = Thread[{xx, uy0t25}];
data3v = Thread[{xx, vy0t25}];
ListPlot[data3u, AxesLabel -> {"x (m)", "Desplazamiento en x (m)"}]
ListPlot[data3v, AxesLabel -> {"x (m)", "Desplazamiento en y (m)"}]
```

Desplazamiento en x (m)



Desplazamiento en y (m)



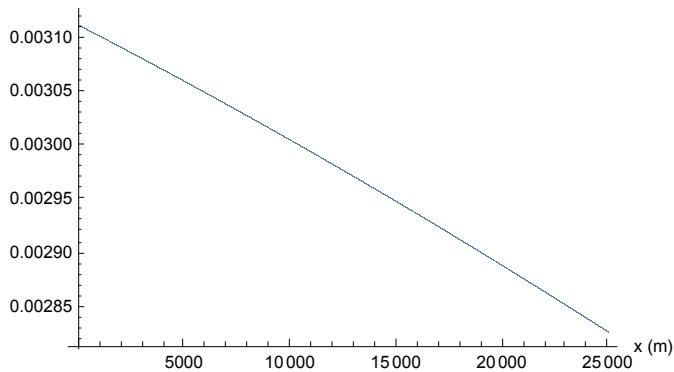
■ Para t=50

```

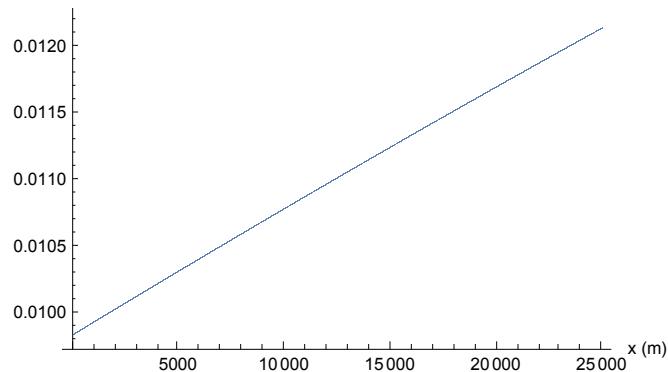
uy0t50 = Evaluate[u[x, 0, 50]] /. {x → xx};
vy0t50 = Evaluate[v[x, 0, 50]] /. {x → xx};
data4u = Thread[{xx, uy0t50}];
data4v = Thread[{xx, vy0t50}];
ListPlot[data4u, AxesLabel → {"x (m)", "Desplazamiento en x (m)"}]
ListPlot[data4v, AxesLabel → {"x (m)", "Desplazamiento en y (m)"}]

```

Desplazamiento en x (m)



Desplazamiento en y (m)

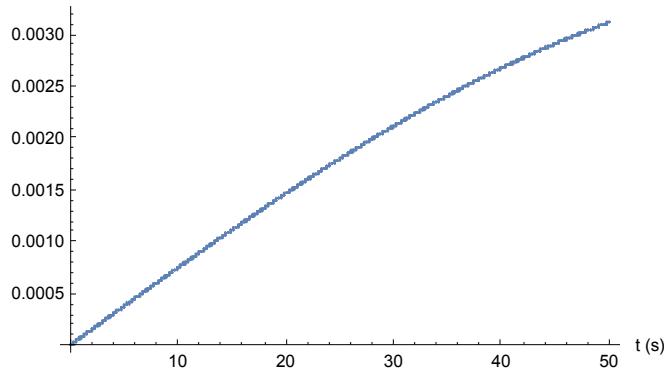


3. Diagrama la trayectoria de movimiento de las partículas en $y=0$ para varios valores de x . Haga lo mismo para varios $y>0$.

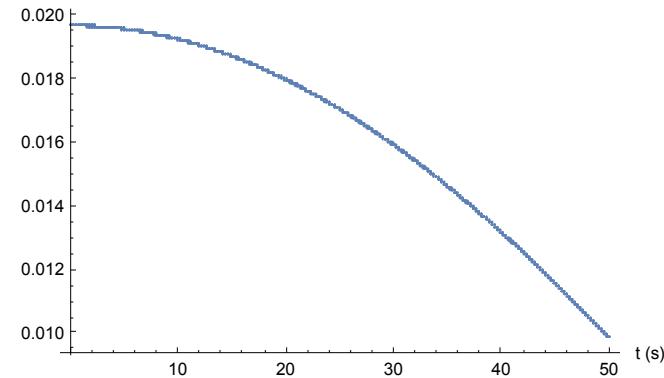
- Para $y=0$ & $x=0$

```
uy0x0 = Evaluate[u[0, 0, t]] /. {t → tt};
vy0x0 = Evaluate[v[0, 0, t]] /. {t → tt};
data5u = Thread[{tt, uy0x0}];
data5v = Thread[{tt, vy0x0}];
ListPlot[data5u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]
ListPlot[data5v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]
```

Desplazamiento en x (m)



Desplazamiento en y (m)



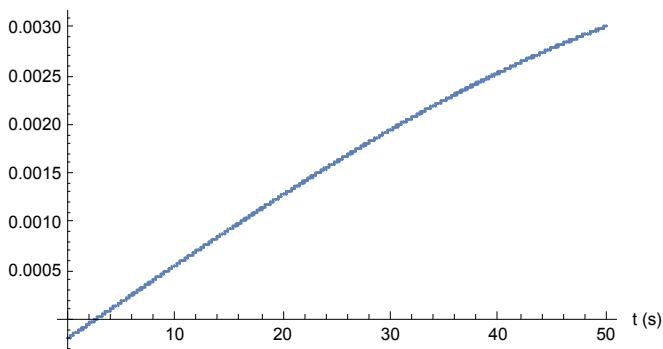
- Para $y=0$ & $x=10000$

```

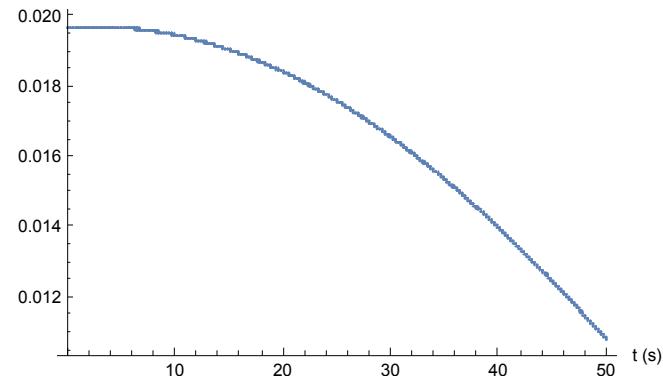
uy0x10 = Evaluate[u[10 000, 0, t]] /. {t → tt};
vy0x10 = Evaluate[v[10 000, 0, t]] /. {t → tt};
data6u = Thread[{tt, uy0x10}];
data6v = Thread[{tt, vy0x10}];
ListPlot[data6u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]
ListPlot[data6v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]

```

Desplazamiento en x (m)

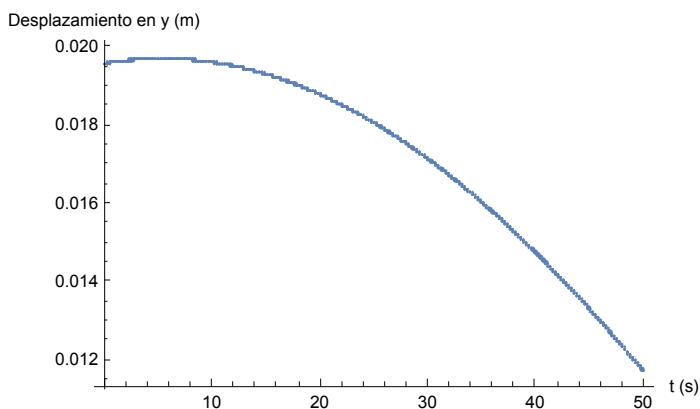
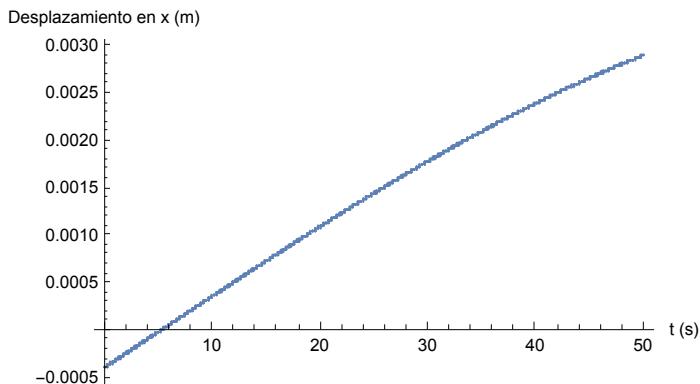


Desplazamiento en y (m)



- Para $y=0$ & $x=20000$

```
uy0x20 = Evaluate[u[20000, 0, t]] /. {t → tt};  
vy0x20 = Evaluate[v[20000, 0, t]] /. {t → tt};  
data7u = Thread[{tt, uy0x20}];  
data7v = Thread[{tt, vy0x20}];  
ListPlot[data7u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]  
ListPlot[data7v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]
```

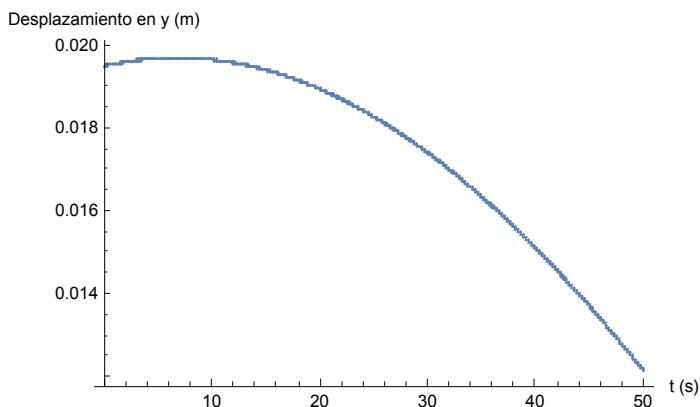
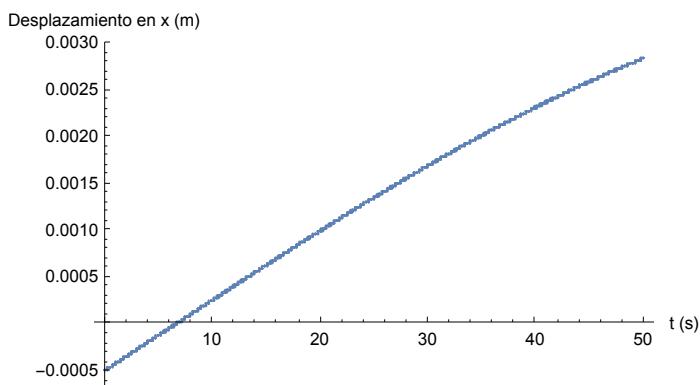


- Para y=0 & x=25000

```

uy0x25 = Evaluate[u[25 000, 0, t]] /. {t → tt};
vy0x25 = Evaluate[v[25 000, 0, t]] /. {t → tt};
data8u = Thread[{tt, uy0x25}];
data8v = Thread[{tt, vy0x25}];
ListPlot[data8u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]
ListPlot[data8v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]

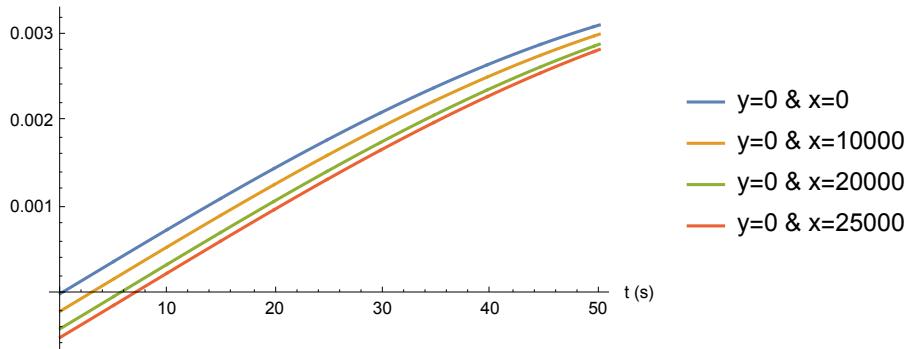
```



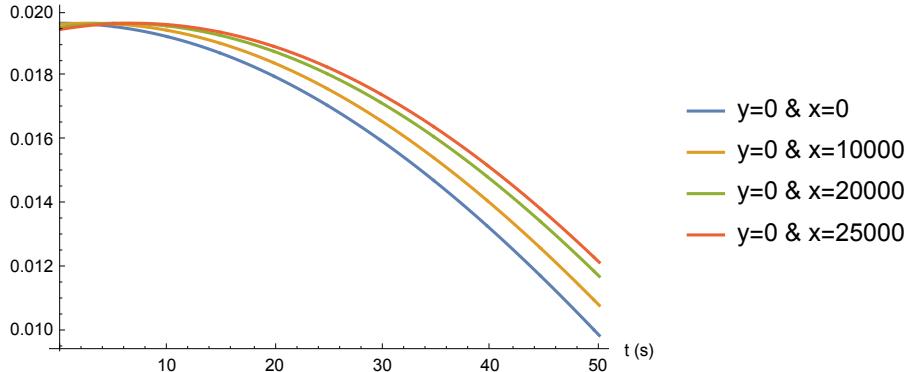
■ Para $y=0$

```
ListPlot[{data5u, data6u, data7u, data8u},
 PlotLegends -> {"y=0 & x=0", "y=0 & x=10000", "y=0 & x=20000", "y=0 & x=25000"}, 
 AxesLabel -> {"t (s)", "Desplazamiento en x (m)"}, Joined -> True]
ListPlot[{data5v, data6v, data7v, data8v},
 PlotLegends -> {"y=0 & x=0", "y=0 & x=10000", "y=0 & x=20000", "y=0 & x=25000"}, 
 AxesLabel -> {"t (s)", "Desplazamiento en y (m)"}, Joined -> True]
```

Desplazamiento en x (m)



Desplazamiento en y (m)



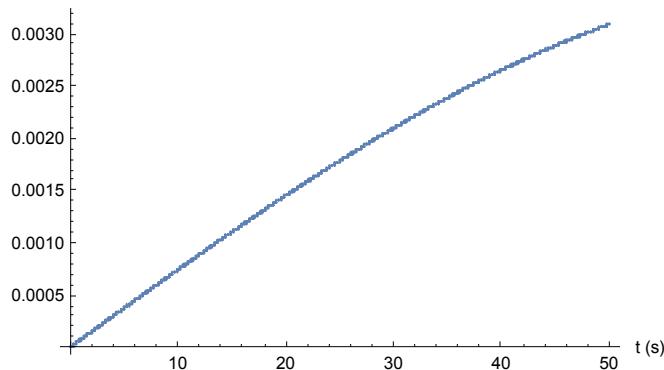
- Para $y=1000 & x=0$

```

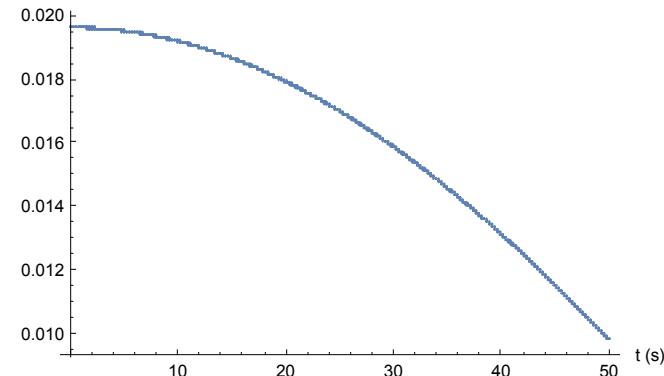
uy1x0 = Evaluate[u[0, 1000, t]] /. {t → tt};
vy1x0 = Evaluate[v[0, 1000, t]] /. {t → tt};
data9u = Thread[{tt, uy1x0}];
data9v = Thread[{tt, vy1x0}];
ListPlot[data9u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]
ListPlot[data9v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]

```

Desplazamiento en x (m)



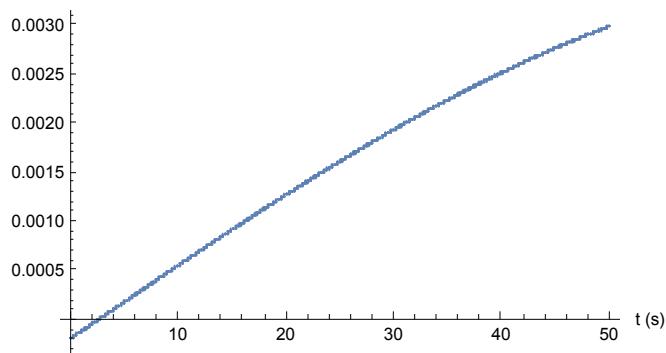
Desplazamiento en y (m)



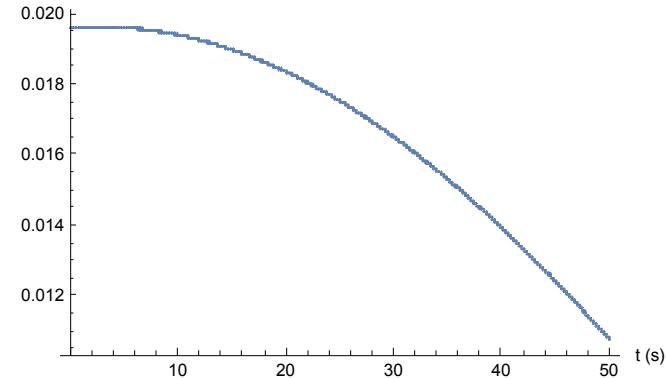
- Para $y=1000$ & $x=10000$

```
uy1x10 = Evaluate[u[10 000, 1000, t]] /. {t → tt};  
vy1x10 = Evaluate[v[10 000, 1000, t]] /. {t → tt};  
data10u = Thread[{tt, uy1x10}];  
data10v = Thread[{tt, vy1x10}];  
ListPlot[data10u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]  
ListPlot[data10v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]
```

Desplazamiento en x (m)



Desplazamiento en y (m)



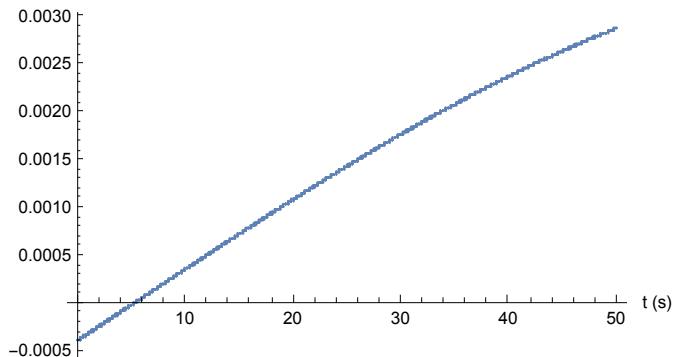
- Para $y=1000$ & $x=20000$

```

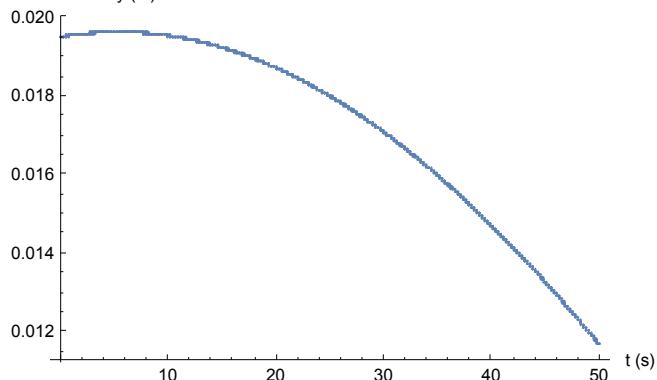
uy1x20 = Evaluate[u[20000, 1000, t]] /. {t → tt};
vy1x20 = Evaluate[v[20000, 1000, t]] /. {t → tt};
data11u = Thread[{tt, uy1x20}];
data11v = Thread[{tt, vy1x20}];
ListPlot[data11u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]
ListPlot[data11v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]

```

Desplazamiento en x (m)



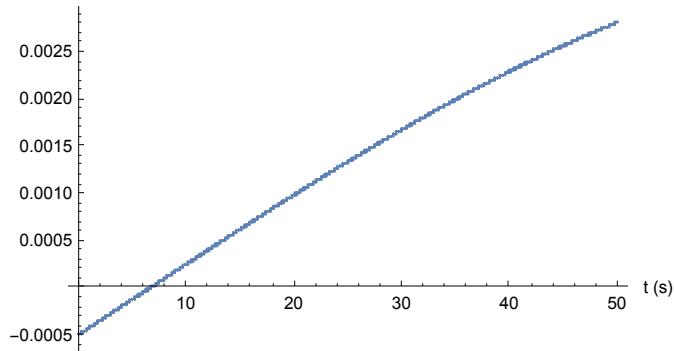
Desplazamiento en y (m)



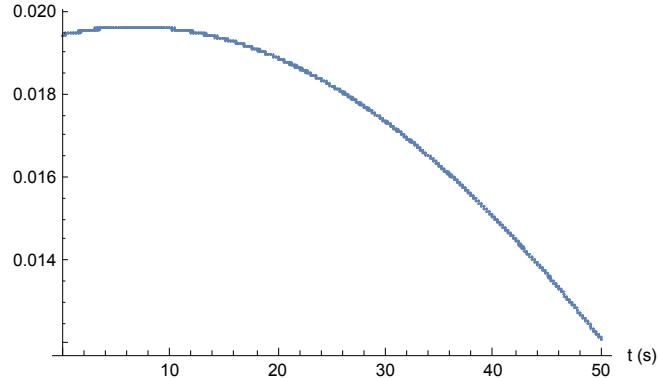
- Para $y=1000$ & $x=25000$

```
uy1x25 = Evaluate[u[25 000, 1000, t]] /. {t → tt};  
vy1x25 = Evaluate[v[25 000, 1000, t]] /. {t → tt};  
data12u = Thread[{tt, uy1x25}];  
data12v = Thread[{tt, vy1x25}];  
ListPlot[data12u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]  
ListPlot[data12v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]
```

Desplazamiento en x (m)

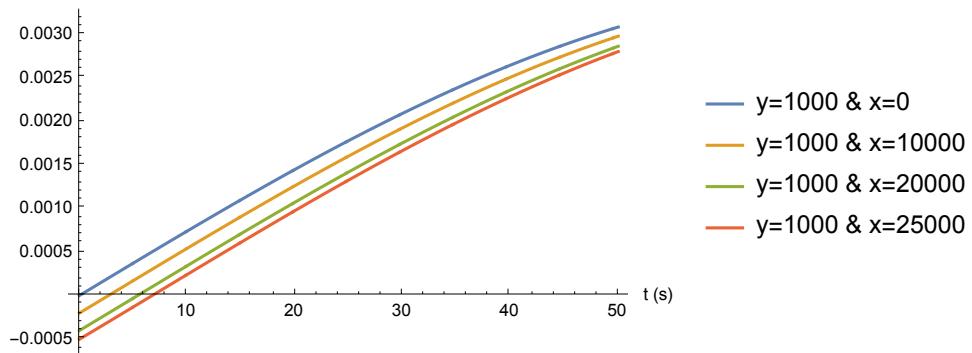


Desplazamiento en y (m)

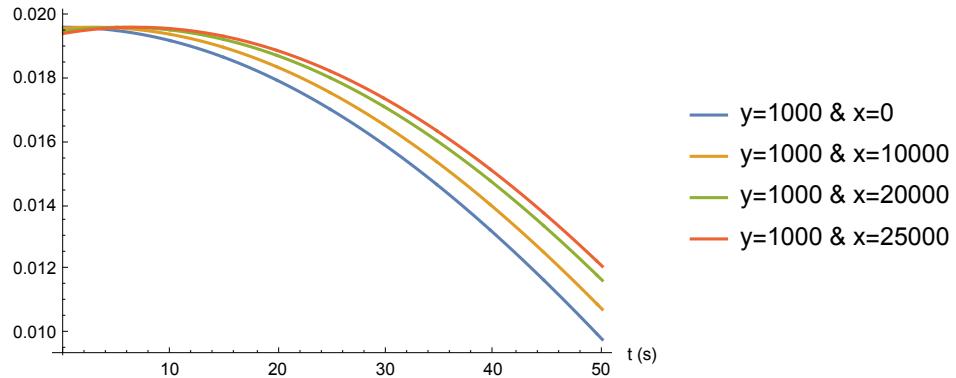


```
ListPlot[{data9u, data10u, data11u, data12u}, PlotLegends ->
 {"y=1000 & x=0", "y=1000 & x=10000", "y=1000 & x=20000", "y=1000 & x=25000"}, 
 AxesLabel -> {"t (s)", "Desplazamiento en x (m)"}, Joined -> True]
ListPlot[{data9v, data10v, data11v, data12v}, PlotLegends ->
 {"y=1000 & x=0", "y=1000 & x=10000", "y=1000 & x=20000", "y=1000 & x=25000"}, 
 AxesLabel -> {"t (s)", "Desplazamiento en y (m)"}, Joined -> True]
```

Desplazamiento en x (m)



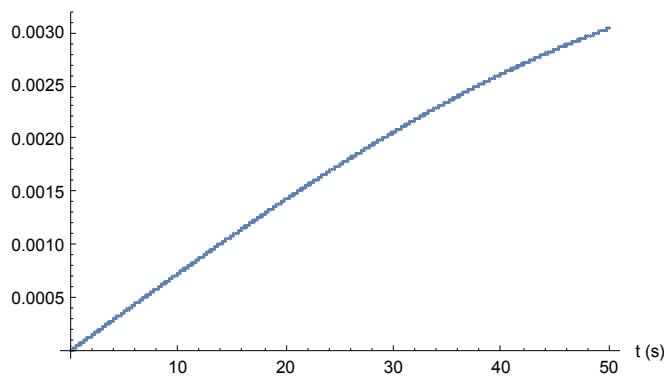
Desplazamiento en y (m)



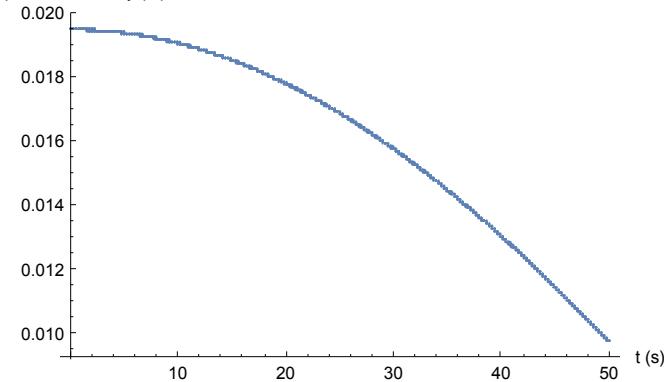
- Para $y=3000$ & $x=0$

```
uy3x0 = Evaluate[u[0, 3000, t]] /. {t → tt};  
vy3x0 = Evaluate[v[0, 3000, t]] /. {t → tt};  
data13u = Thread[{tt, uy3x0}];  
data13v = Thread[{tt, vy3x0}];  
ListPlot[data13u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]  
ListPlot[data13v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]
```

Desplazamiento en x (m)



Desplazamiento en y (m)



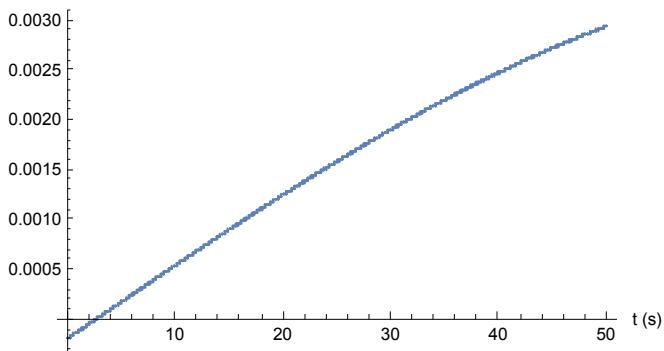
- Para $y=3000$ & $x=10000$

```

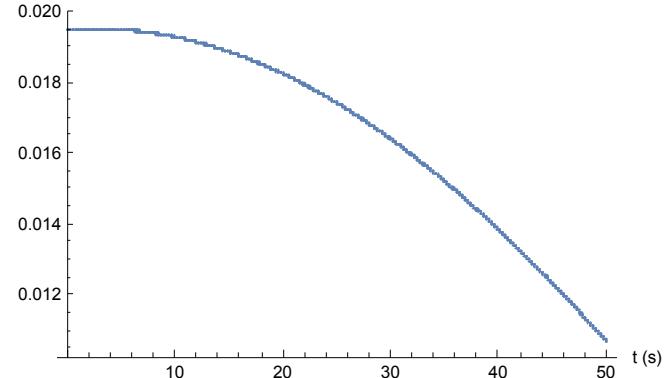
uy3x10 = Evaluate[u[10 000, 3000, t]] /. {t → tt};
vy3x10 = Evaluate[v[10 000, 3000, t]] /. {t → tt};
data14u = Thread[{tt, uy3x10}];
data14v = Thread[{tt, vy3x10}];
ListPlot[data14u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]
ListPlot[data14v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]

```

Desplazamiento en x (m)

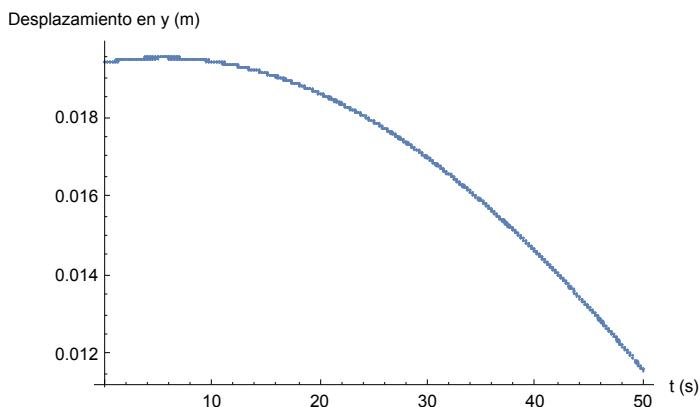
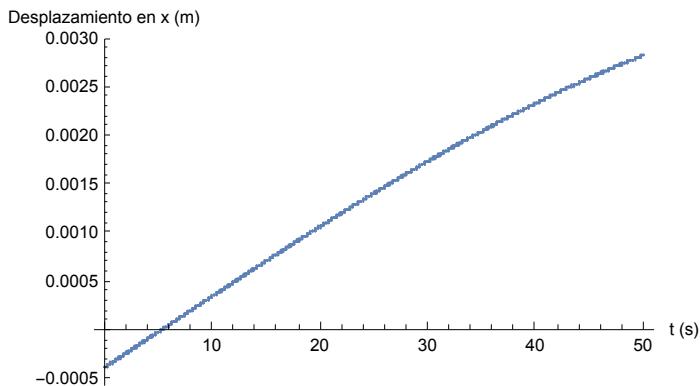


Desplazamiento en y (m)



- Para y=3000 & x=20000

```
uy3x20 = Evaluate[u[20 000, 3000, t]] /. {t → tt};  
vy3x20 = Evaluate[v[20 000, 3000, t]] /. {t → tt};  
data15u = Thread[{tt, uy3x20}];  
data15v = Thread[{tt, vy3x20}];  
ListPlot[data15u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]  
ListPlot[data15v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]
```



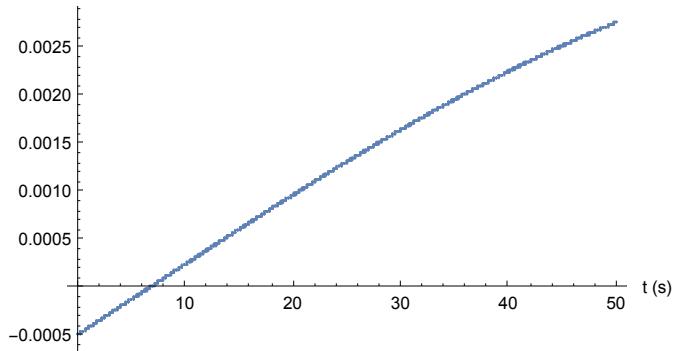
- Para y=3000 & x=25000

```

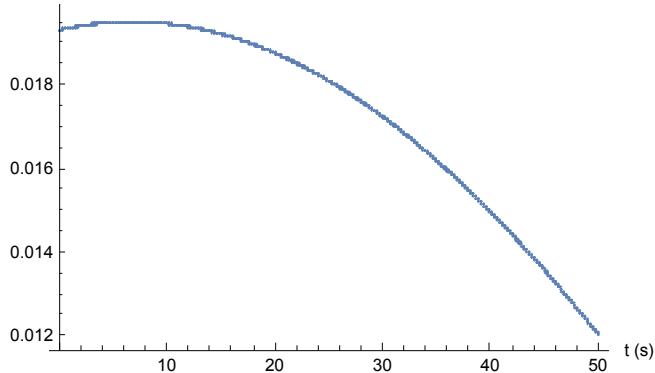
uy3x25 = Evaluate[u[25 000, 3000, t]] /. {t → tt};
vy3x25 = Evaluate[v[25 000, 3000, t]] /. {t → tt};
data16u = Thread[{tt, uy3x25}];
data16v = Thread[{tt, vy3x25}];
ListPlot[data16u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]
ListPlot[data16v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]

```

Desplazamiento en x (m)



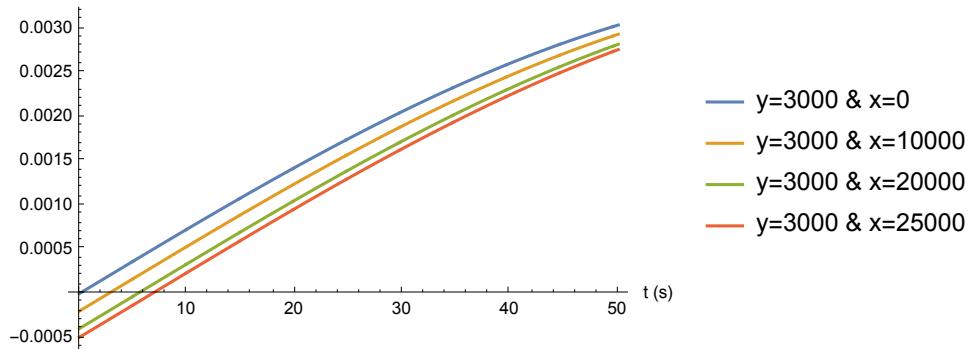
Desplazamiento en y (m)



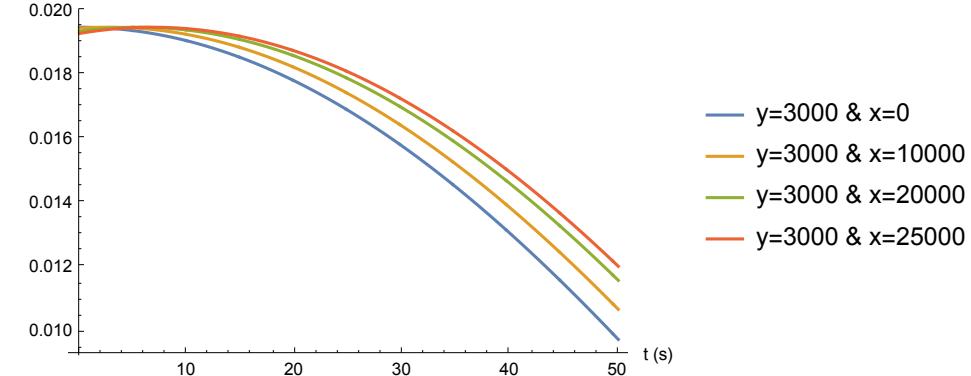
- Para y=3000

```
ListPlot[{data13u, data14u, data15u, data16u}, PlotLegends ->
  {"y=3000 & x=0", "y=3000 & x=10000", "y=3000 & x=20000", "y=3000 & x=25000"}, 
  AxesLabel -> {"t (s)", "Desplazamiento en x (m)"}, Joined -> True]
ListPlot[{data13v, data14v, data15v, data16v}, PlotLegends ->
  {"y=3000 & x=0", "y=3000 & x=10000", "y=3000 & x=20000", "y=3000 & x=25000"}, 
  AxesLabel -> {"t (s)", "Desplazamiento en y (m)"}, Joined -> True]
```

Desplazamiento en x (m)



Desplazamiento en y (m)



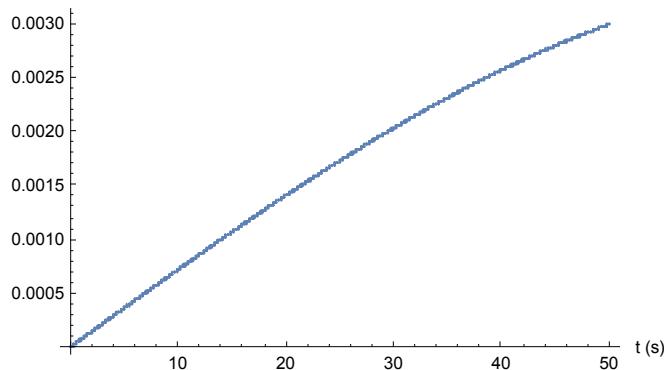
- Para $y=5000$ & $x=0$

```

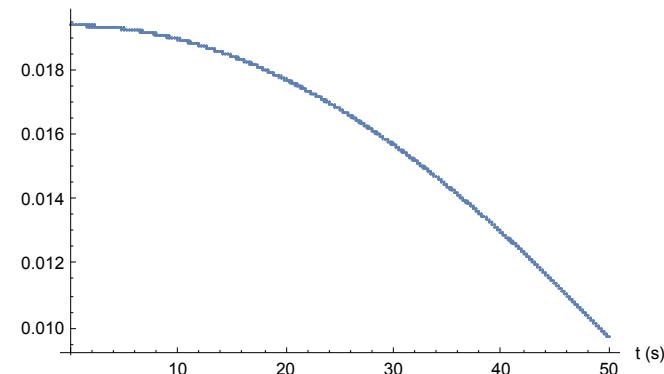
uy5x0 = Evaluate[u[0, 5000, t]] /. {t → tt};
vy5x0 = Evaluate[v[0, 5000, t]] /. {t → tt};
data17u = Thread[{tt, uy5x0}];
data17v = Thread[{tt, vy5x0}];
ListPlot[data17u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]
ListPlot[data17v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]

```

Desplazamiento en x (m)



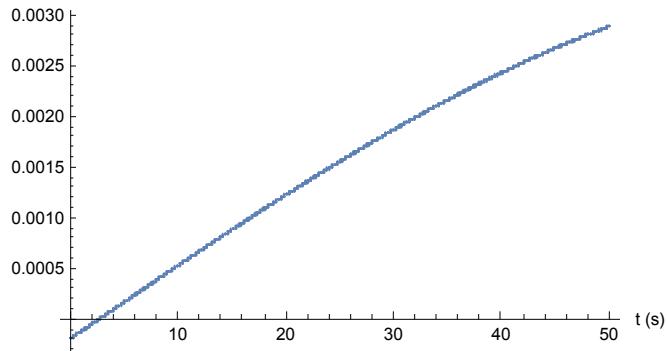
Desplazamiento en y (m)



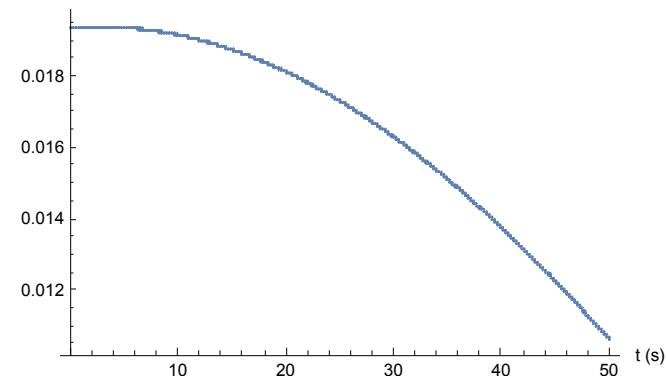
- Para $y=5000$ & $x=10000$

```
uy5x10 = Evaluate[u[10 000, 5000, t]] /. {t → tt};  
vy5x10 = Evaluate[v[10 000, 5000, t]] /. {t → tt};  
data18u = Thread[{tt, uy5x10}];  
data18v = Thread[{tt, vy5x10}];  
ListPlot[data18u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]  
ListPlot[data18v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]
```

Desplazamiento en x (m)



Desplazamiento en y (m)



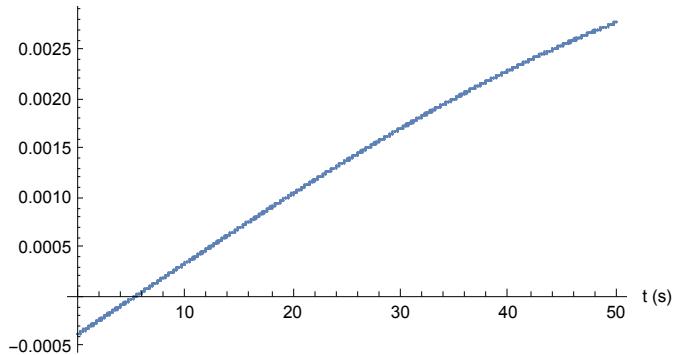
- Para y=5000 & x=20000

```

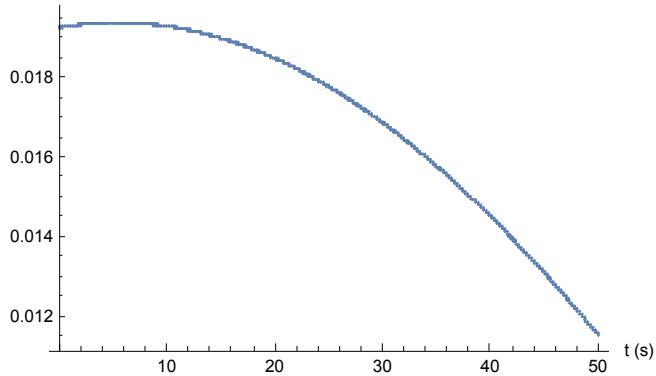
uy5x20 = Evaluate[u[20000, 5000, t]] /. {t → tt};
vy5x20 = Evaluate[v[20000, 5000, t]] /. {t → tt};
data19u = Thread[{tt, uy5x20}];
data19v = Thread[{tt, vy5x20}];
ListPlot[data19u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]
ListPlot[data19v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]

```

Desplazamiento en x (m)



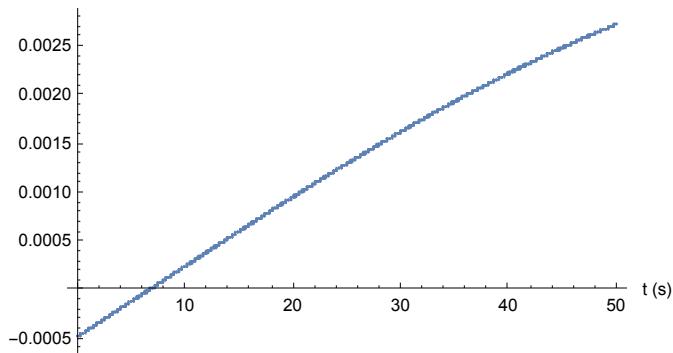
Desplazamiento en y (m)



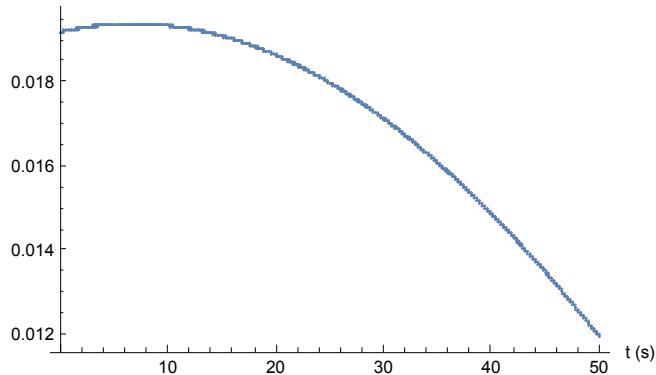
- Para $y=5000$ & $x=25000$

```
uy5x25 = Evaluate[u[25 000, 5000, t]] /. {t → tt};  
vy5x25 = Evaluate[v[25 000, 5000, t]] /. {t → tt};  
data20u = Thread[{tt, uy5x25}];  
data20v = Thread[{tt, vy5x25}];  
ListPlot[data20u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]  
ListPlot[data20v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]
```

Desplazamiento en x (m)



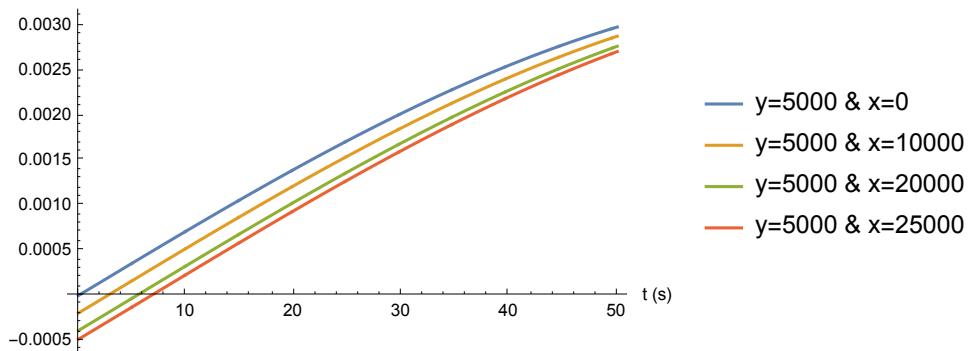
Desplazamiento en y (m)



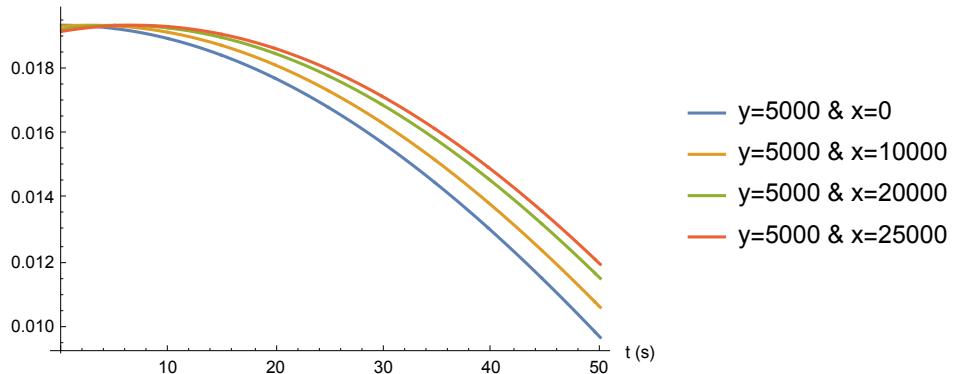
- Para y=5000

```
ListPlot[{data17u, data18u, data19u, data20u}, PlotLegends ->
  {"y=5000 & x=0", "y=5000 & x=10000", "y=5000 & x=20000", "y=5000 & x=25000"}, 
  AxesLabel -> {"t (s)", "Desplazamiento en x (m)"}, Joined -> True]
ListPlot[{data17v, data18v, data19v, data20v}, PlotLegends ->
  {"y=5000 & x=0", "y=5000 & x=10000", "y=5000 & x=20000", "y=5000 & x=25000"}, 
  AxesLabel -> {"t (s)", "Desplazamiento en y (m)"}, Joined -> True]
```

Desplazamiento en x (m)



Desplazamiento en y (m)



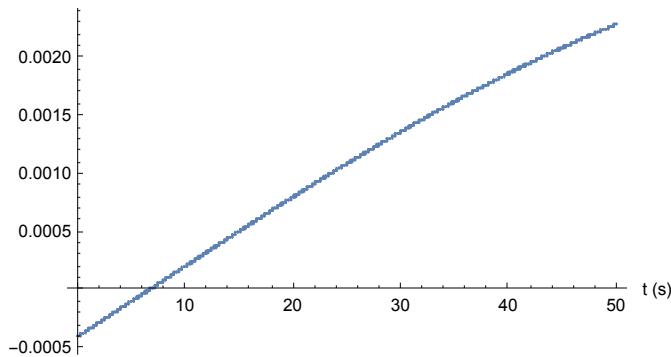
- Para y=25000 & x=0

```

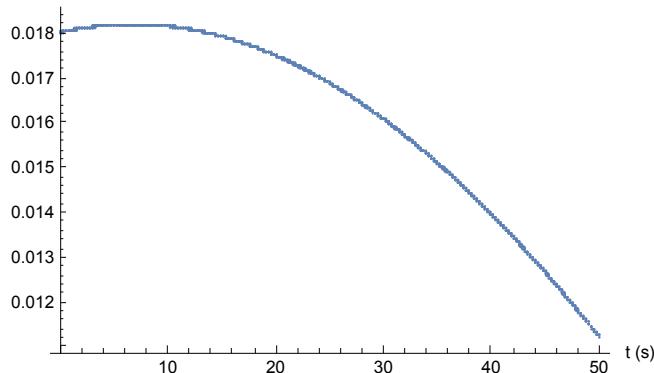
uy25x25 = Evaluate[u[25 000, 25 000, t]] /. {t → tt};
vy25x25 = Evaluate[v[25 000, 25 000, t]] /. {t → tt};
data21u = Thread[{tt, uy25x25}];
data21v = Thread[{tt, vy25x25}];
ListPlot[data21u, AxesLabel → {"t (s)", "Desplazamiento en x (m)"}]
ListPlot[data21v, AxesLabel → {"t (s)", "Desplazamiento en y (m)"}]

```

Desplazamiento en x (m)



Desplazamiento en y (m)



4. Muestre que el movimiento de las partículas es retrógrado a bajas profundidades, ¿qué sucede a grandes profundidades?

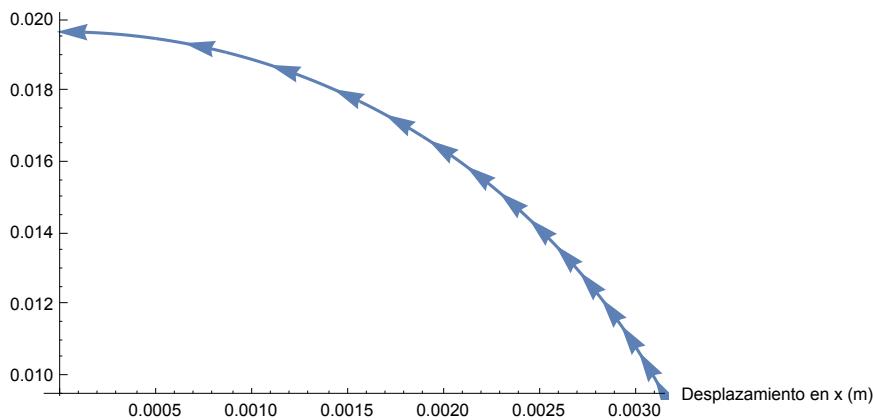
- Para este punto parametrizamos la curva de desplazamiento y mostramos explícitamente la dirección del flujo
- Para una profundidad de $y=100$

```

uu = Evaluate[u[1000, 100, t]] /. {t → tt};
vv = Evaluate[v[1000, 100, t]] /. {t → tt};
data22 = Thread[{uu, vv}];
p0 = ListPlot[data22, Joined → True,
  AxesLabel → {"Desplazamiento en x (m)", "Desplazamiento en y (m)" }];
p0 /. Line[x_] :> {Arrowheads[Table[-0.05, {15}]], Arrow[x]}

```

Desplazamiento en y (m)



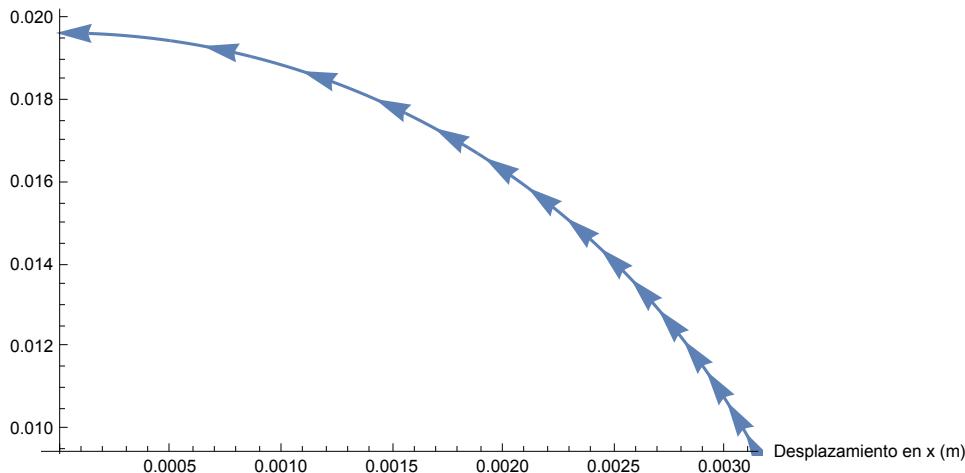
■ Para una profundidad de $y=500$

```

uu = Evaluate[u[1000, 500, t]] /. {t → tt};
vv = Evaluate[v[1000, 500, t]] /. {t → tt};
data22 = Thread[{uu, vv}];
p0 = ListPlot[data22, Joined → True,
  AxesLabel → {"Desplazamiento en x (m)", "Desplazamiento en y (m)" }];
p0 /. Line[x_] :> {Arrowheads[Table[-.05, {15}]], Arrow[x]}

```

Desplazamiento en y (m)

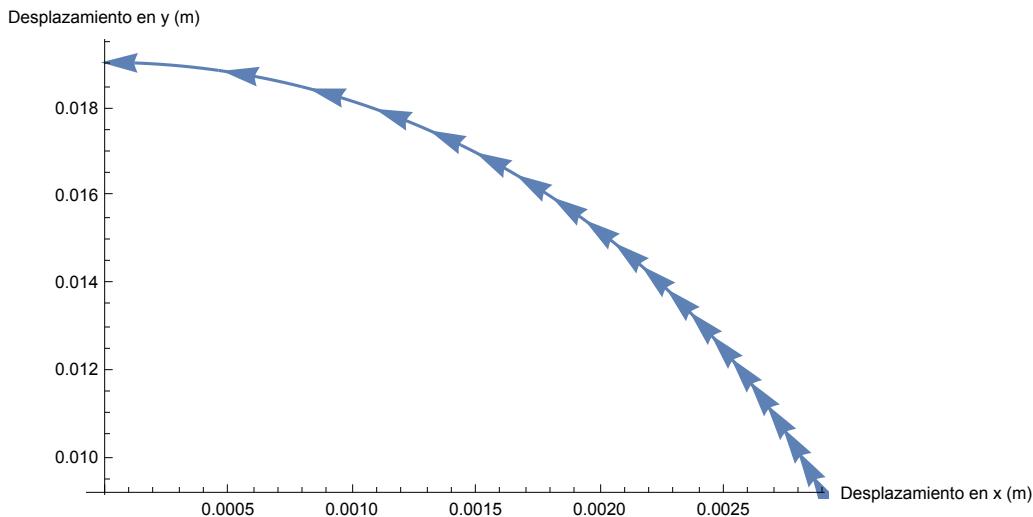


■ Para una profundidad de $y=10000$

```

uu = Evaluate[u[1000, 10000, t]] /. {t → tt};
vv = Evaluate[v[1000, 10000, t]] /. {t → tt};
data22 = Thread[{uu, vv}];
p0 = ListPlot[data22, Joined → True,
  AxesLabel → {"Desplazamiento en x (m)", "Desplazamiento en y (m)" }];
p0 /. Line[x_] → {Arrowheads[Table[-.05, {20}]], Arrow[x]}

```



5. Diagrama los campos de desplazamiento, velocidad y aceleración en la superficie libre ($y=0$) para varios valores de t . Haga lo mismo para varios valores $y>0$.

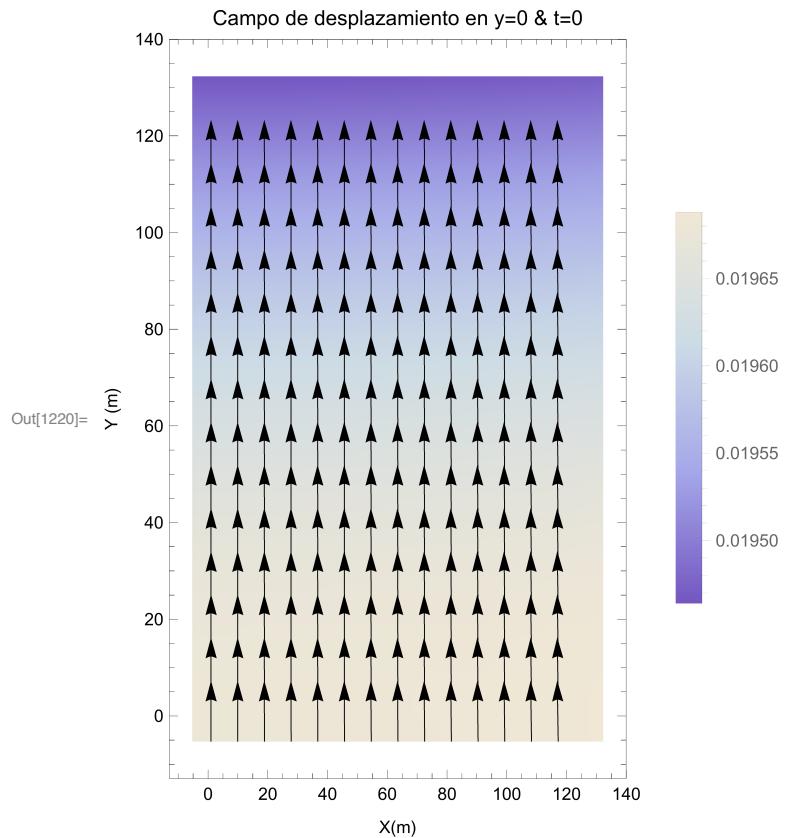
- Para $y=0$ & $t=0$

```

In[1216]:= xx = Range[0, 25000, 200];
uuu = Evaluate[u[x, 0, 0]] /. {x → xx};
vvv = Evaluate[v[x, 0, 0]] /. {x → xx};
data23 = Table[{uuu[[i]], vvv[[j]]}, {i, Length[uuu]}, {j, Length[vvv]}];
ListVectorDensityPlot[data23, AspectRatio → GoldenRatio,
  FrameLabel → {"X(m)", "Y (m)"}, PlotLabel → "Campo de desplazamiento en y=0 & t=0",
  ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
du = D[Evaluate[u[x, 0, t]], t] /. {t → 0, x → xx};
dv = D[Evaluate[v[x, 0, t]], t] /. {t → 0, x → xx};
data24 = Table[{du[[i]], dv[[j]]}, {i, Length[du]}, {j, Length[dv]}];
ListVectorDensityPlot[data24, AspectRatio → GoldenRatio,
  FrameLabel → {"X(m)", "Y (m)"}, PlotLabel → "Campo de velocidades en y=0 & t=0",
  ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
d2u = D[D[Evaluate[u[x, 0, t]], t], t] /. {t → 0, x → xx};
d2v = D[D[Evaluate[v[x, 0, t]], t], t] /. {t → 0, x → xx};
data25 = Table[{d2u[[i]], d2v[[j]]}, {i, Length[d2u]}, {j, Length[d2v]}];
ListVectorDensityPlot[data25, AspectRatio → GoldenRatio,
  FrameLabel → {"X(m)", "Y (m)"}, PlotLabel → "Campo de aceleraciones en y=0 & t=0",
  ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]

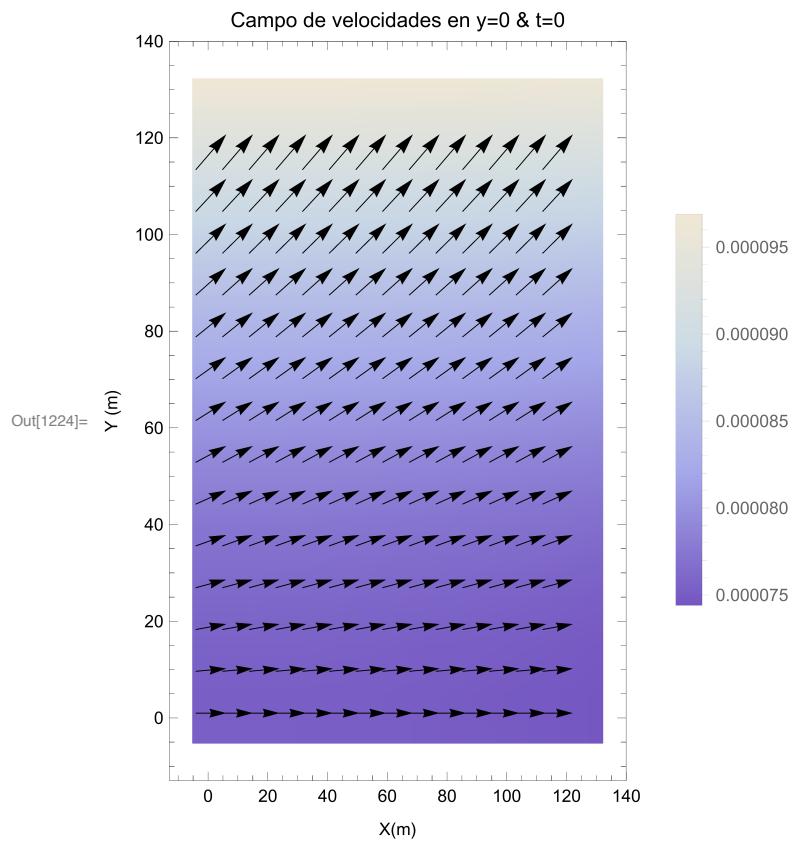
```

ListStreamDensityPlatfun:
Value of optionColorFunction→ RainbowOpacity is not a valid colorfunction or a gradientColorDataentity >>



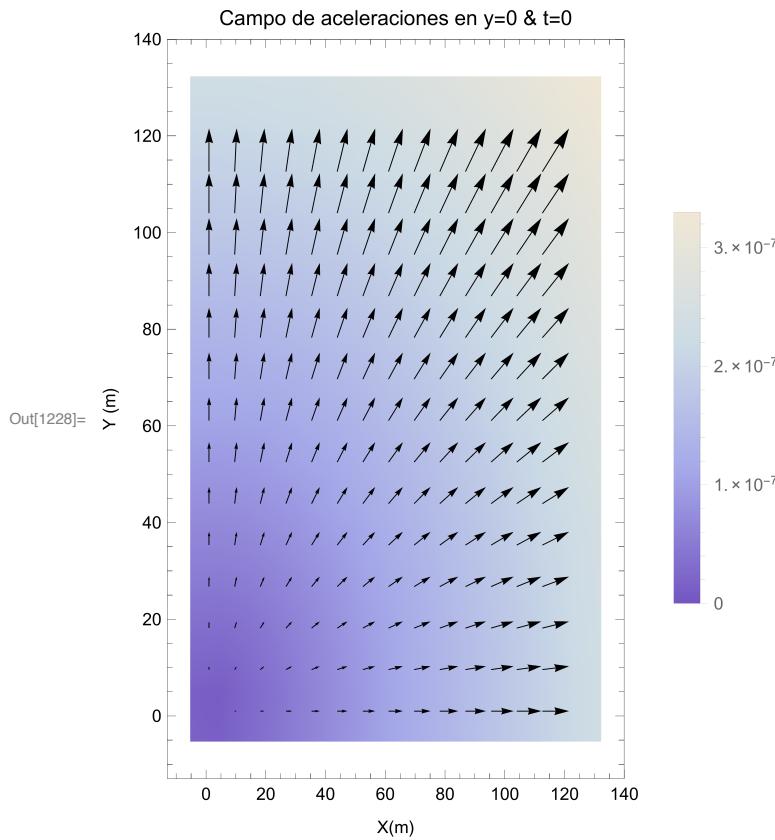
ListStreamDensityPlotfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



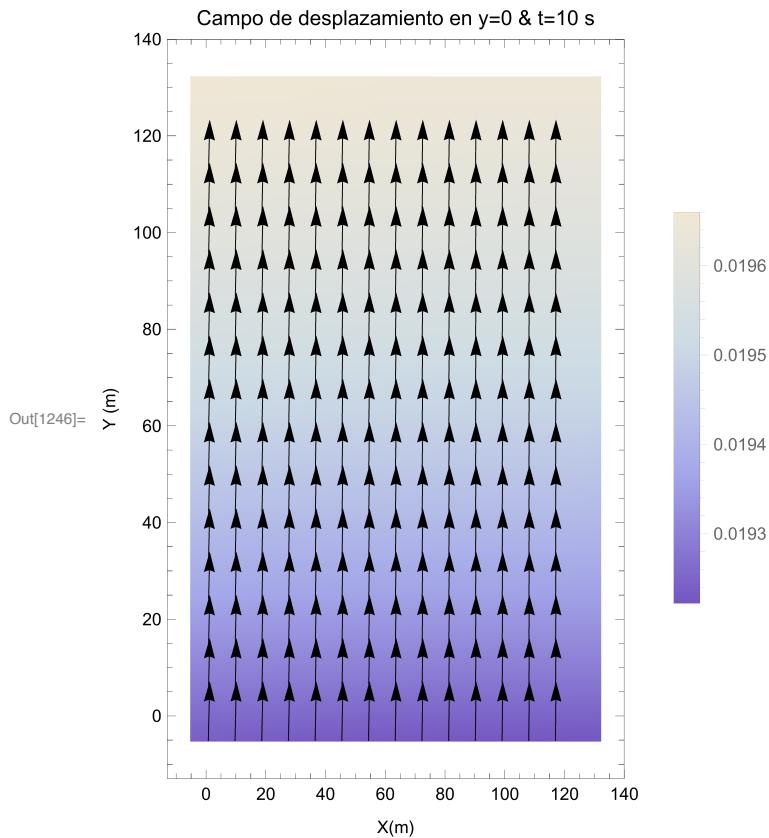
ListStreamDensityPlatfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



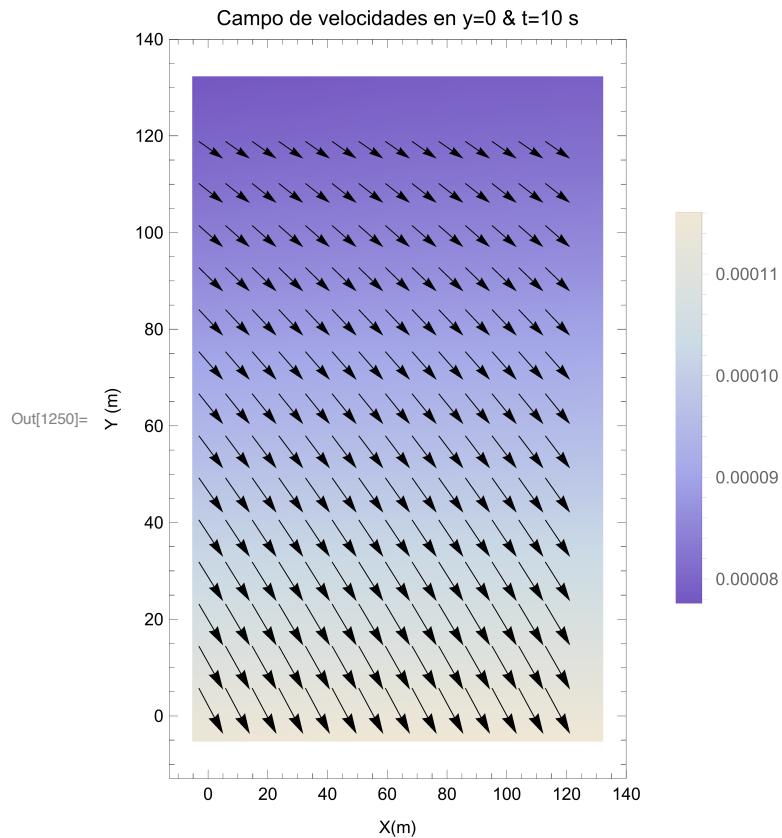
■ Para $y=0$ & $t=10$

```
In[1242]:= xx = Range[0, 25000, 200];
uuu = Evaluate[u[x, 0, 10]] /. {x → xx};
vvv = Evaluate[v[x, 0, 10]] /. {x → xx};
data23 = Table[{uuu[[i]], vvv[[j]]}, {i, Length[uuu]}, {j, Length[vvv]}];
ListVectorDensityPlot[data23,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de desplazamiento en y=0 & t=10 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
du = D[Evaluate[u[x, 0, t]], t] /. {t → 10, x → xx};
dv = D[Evaluate[v[x, 0, t]], t] /. {t → 10, x → xx};
data24 = Table[{du[[i]], dv[[j]]}, {i, Length[du]}, {j, Length[dv]}];
ListVectorDensityPlot[data24,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de velocidades en y=0 & t=10 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
d2u = D[D[Evaluate[u[x, 0, t]], t], t] /. {t → 10, x → xx};
d2v = D[D[Evaluate[v[x, 0, t]], t], t] /. {t → 10, x → xx};
data25 = Table[{d2u[[i]], d2v[[j]]}, {i, Length[d2u]}, {j, Length[d2v]}];
ListVectorDensityPlot[data25,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de aceleraciones en y=0 & t=10 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
ListStreamDensityPlatfun:
Value of optionColorFunction-> RainbowOpacity is not a valid colorfunction or a gradientColorData entity >>
```



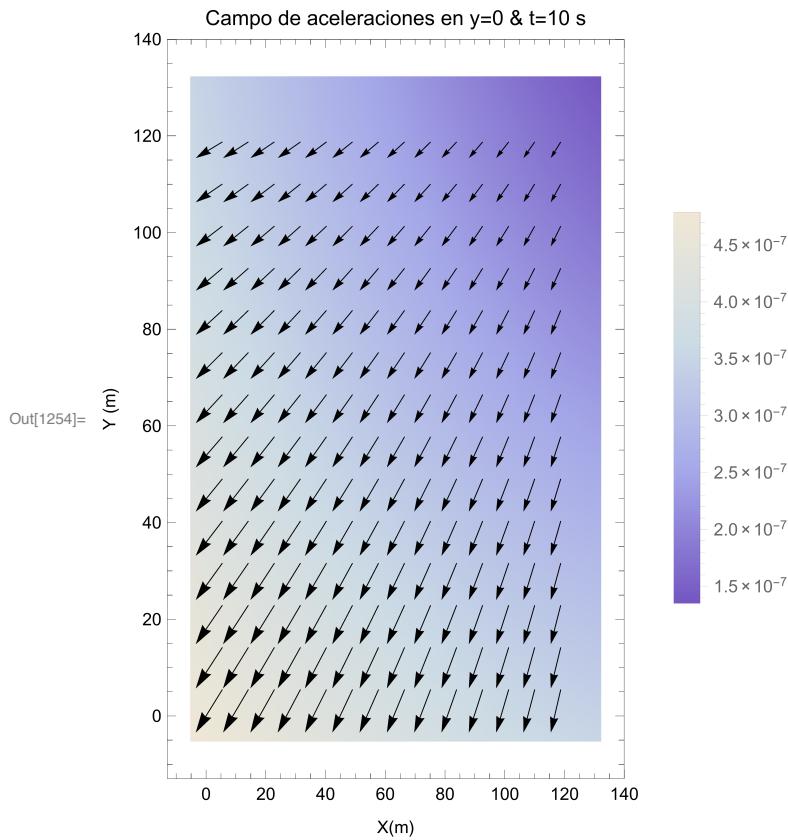
ListStreamDensityPlatcfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



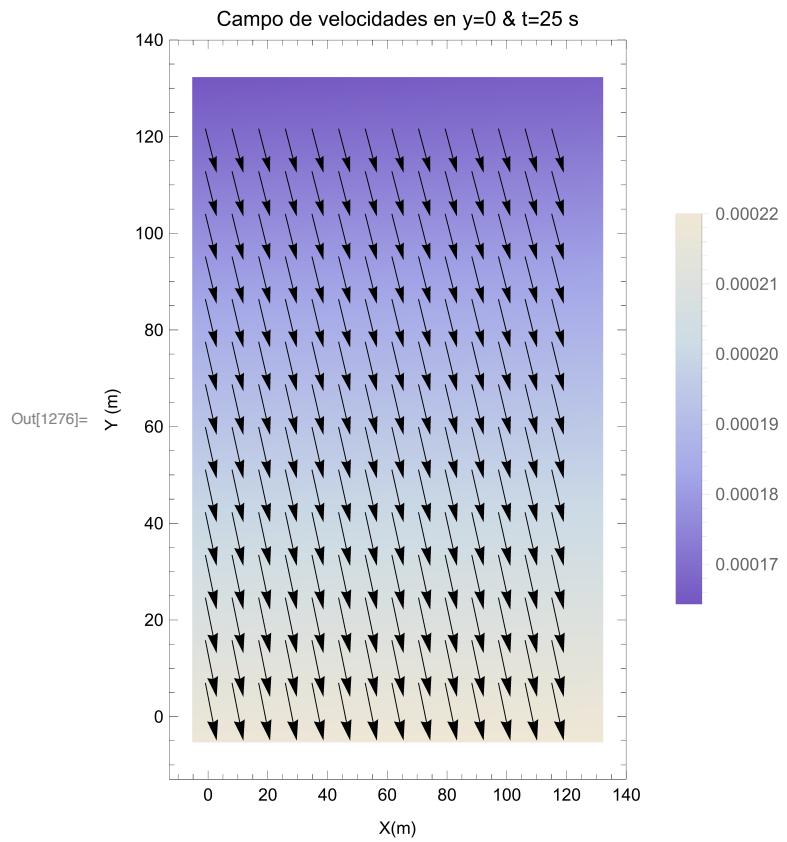
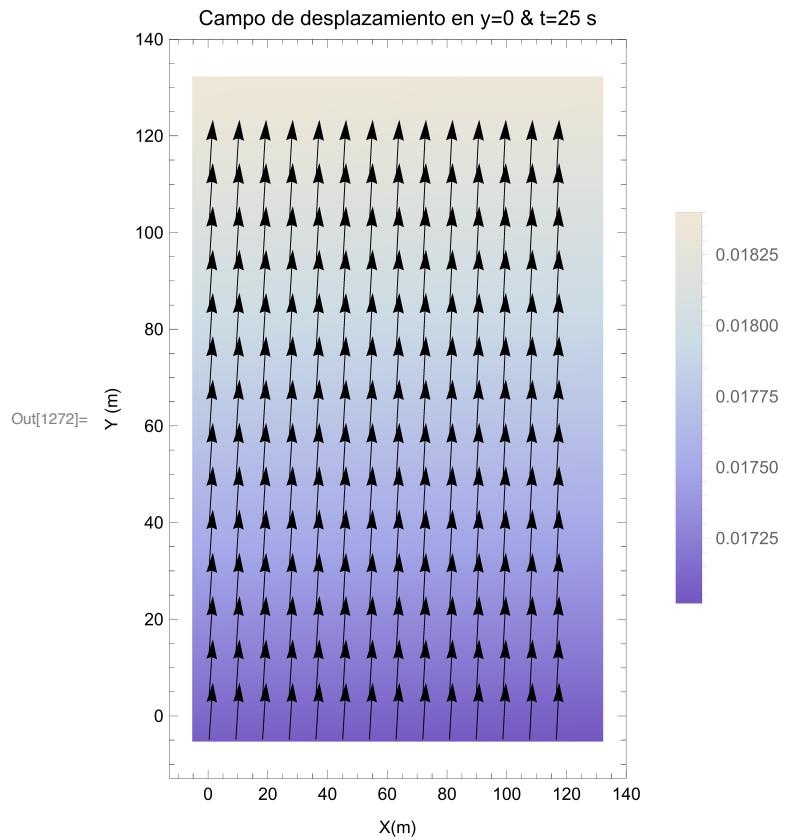
ListStreamDensityPlotfun:

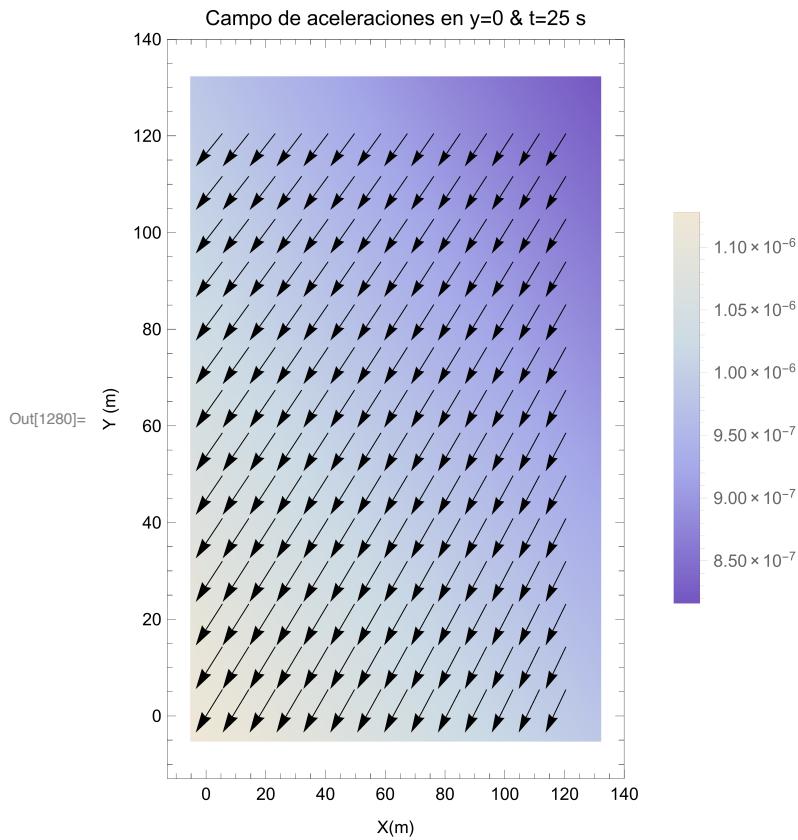
Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



■ Para $y=0$ & $t=25$

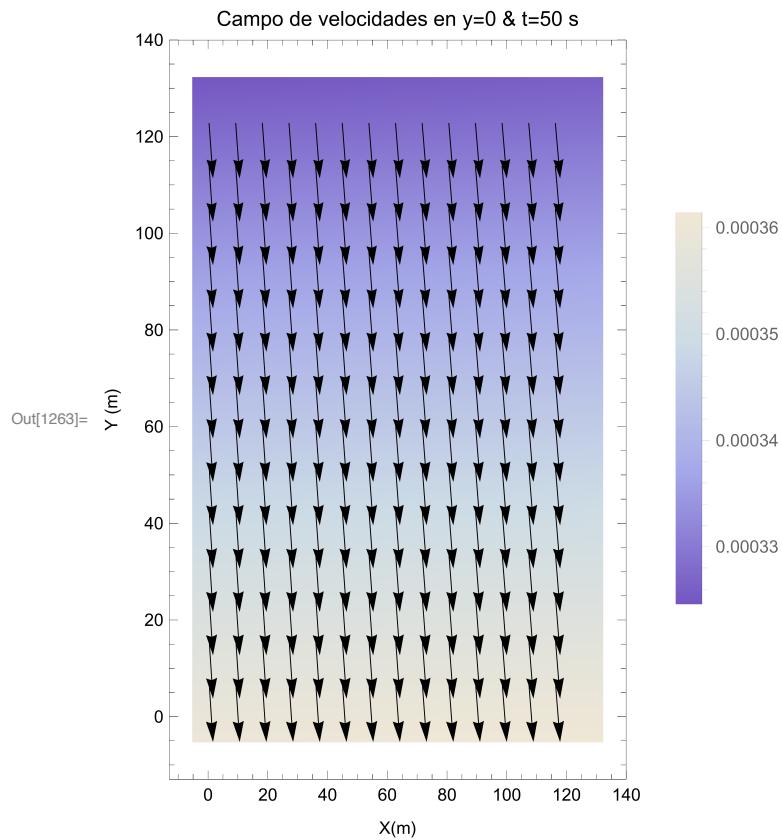
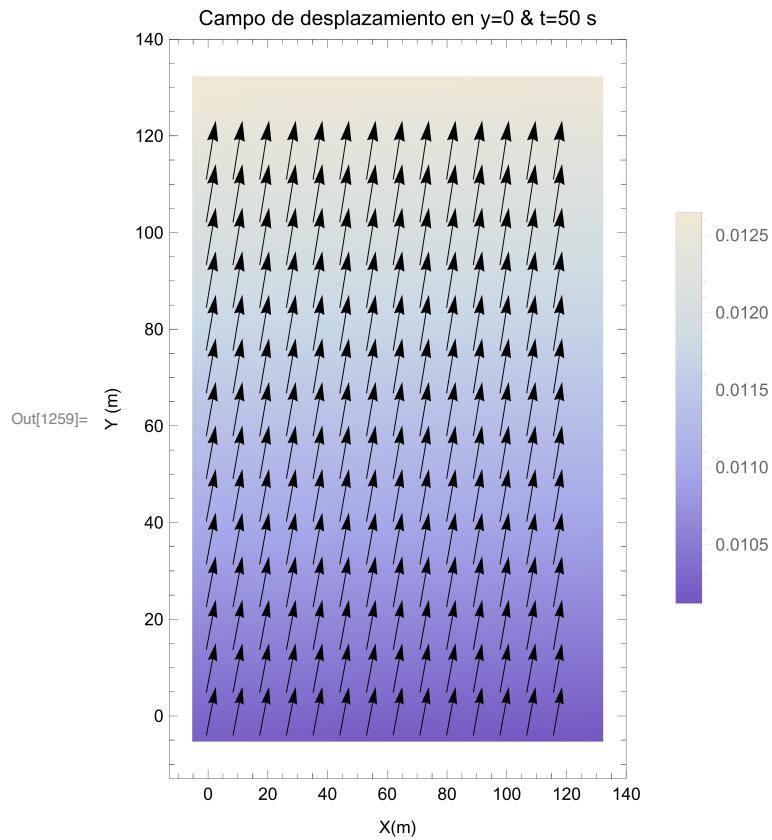
```
In[1268]:= xx = Range[0, 25000, 200];
uuu = Evaluate[u[x, 0, 25]] /. {x → xx};
vvv = Evaluate[v[x, 0, 25]] /. {x → xx};
data23 = Table[{uuu[[i]], vvv[[j]]}, {i, Length[uuu]}, {j, Length[vvv]}];
ListVectorDensityPlot[data23,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de desplazamiento en y=0 & t=25 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
du = D[Evaluate[u[x, 0, t]], t] /. {t → 25, x → xx};
dv = D[Evaluate[v[x, 0, t]], t] /. {t → 25, x → xx};
data24 = Table[{du[[i]], dv[[j]]}, {i, Length[du]}, {j, Length[dv]}];
ListVectorDensityPlot[data24,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de velocidades en y=0 & t=25 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
d2u = D[D[Evaluate[u[x, 0, t]], t], t] /. {t → 25, x → xx};
d2v = D[D[Evaluate[v[x, 0, t]], t], t] /. {t → 25, x → xx};
data25 = Table[{d2u[[i]], d2v[[j]]}, {i, Length[d2u]}, {j, Length[d2v]}];
ListVectorDensityPlot[data25,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de aceleraciones en y=0 & t=25 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
```

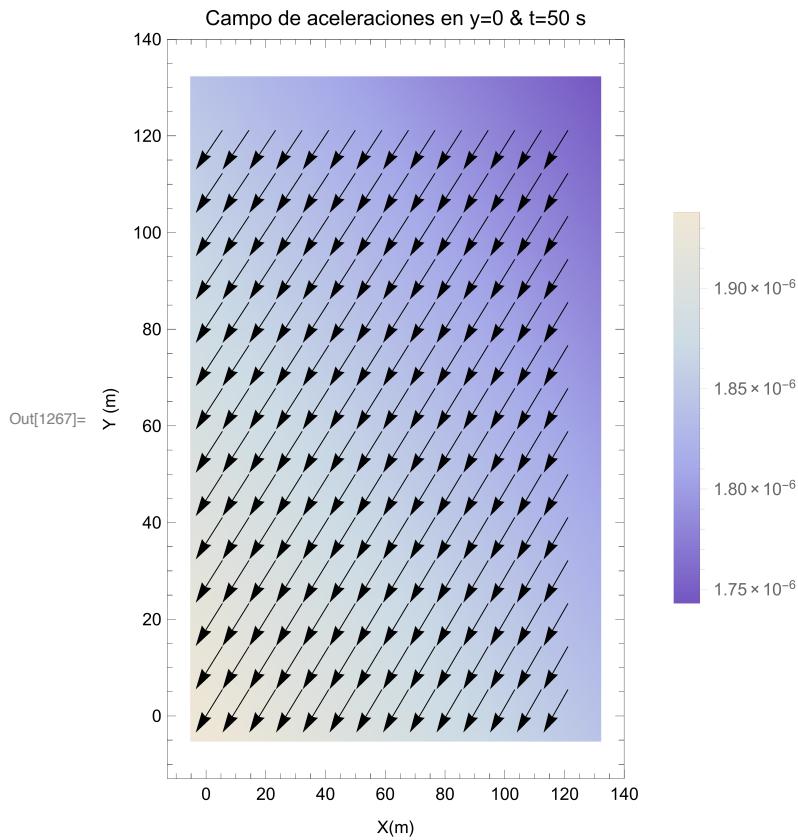




■ Para $y=0$ & $t=50$

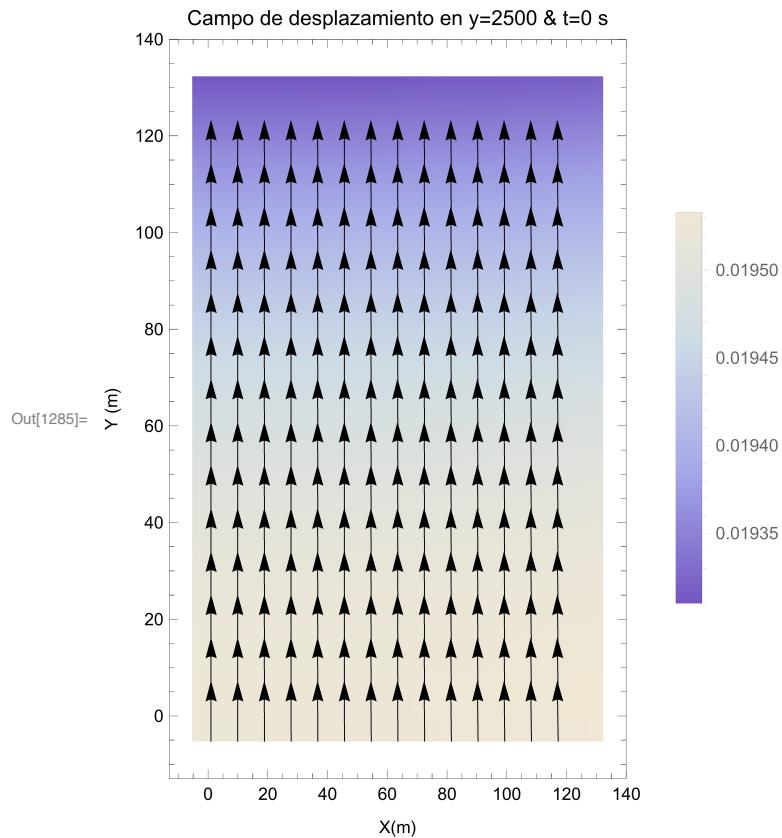
```
In[1255]:= xx = Range[0, 25000, 200];
uuu = Evaluate[u[x, 0, 50]] /. {x → xx};
vvv = Evaluate[v[x, 0, 50]] /. {x → xx};
data23 = Table[{uuu[[i]], vvv[[j]]}, {i, Length[uuu]}, {j, Length[vvv]}];
ListVectorDensityPlot[data23,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de desplazamiento en y=0 & t=50 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
du = D[Evaluate[u[x, 0, t]], t] /. {t → 50, x → xx};
dv = D[Evaluate[v[x, 0, t]], t] /. {t → 50, x → xx};
data24 = Table[{du[[i]], dv[[j]]}, {i, Length[du]}, {j, Length[dv]}];
ListVectorDensityPlot[data24,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de velocidades en y=0 & t=50 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
d2u = D[D[Evaluate[u[x, 0, t]], t], t] /. {t → 50, x → xx};
d2v = D[D[Evaluate[v[x, 0, t]], t], t] /. {t → 50, x → xx};
data25 = Table[{d2u[[i]], d2v[[j]]}, {i, Length[d2u]}, {j, Length[d2v]}];
ListVectorDensityPlot[data25,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de aceleraciones en y=0 & t=50 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
```





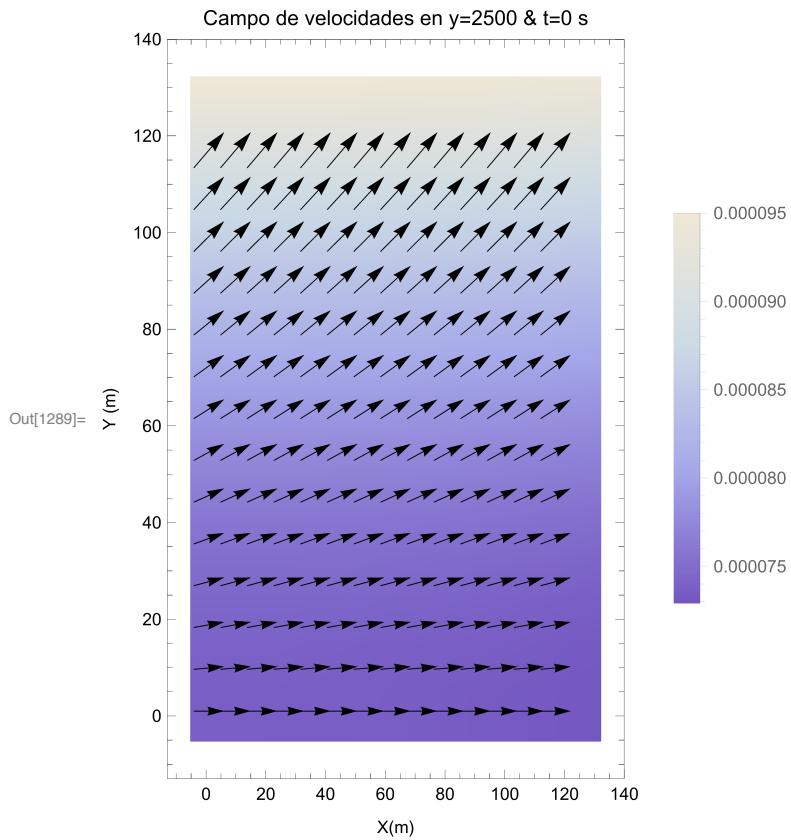
■ Para $y = 2500$ & $t=0$

```
In[1281]:= xx = Range[0, 25000, 200];
uuu = Evaluate[u[x, 2500, 0]] /. {x → xx};
vvv = Evaluate[v[x, 2500, 0]] /. {x → xx};
data23 = Table[{uuu[[i]], vvv[[j]]}, {i, Length[uuu]}, {j, Length[vvv]}];
ListVectorDensityPlot[data23,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de desplazamiento en y=2500 & t=0 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
du = D[Evaluate[u[x, 2500, t]], t] /. {t → 0, x → xx};
dv = D[Evaluate[v[x, 2500, t]], t] /. {t → 0, x → xx};
data24 = Table[{du[[i]], dv[[j]]}, {i, Length[du]}, {j, Length[dv]}];
ListVectorDensityPlot[data24,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de velocidades en y=2500 & t=0 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
d2u = D[D[Evaluate[u[x, 2500, t]], t], t] /. {t → 0, x → xx};
d2v = D[D[Evaluate[v[x, 2500, t]], t], t] /. {t → 0, x → xx};
data25 = Table[{d2u[[i]], d2v[[j]]}, {i, Length[d2u]}, {j, Length[d2v]}];
ListVectorDensityPlot[data25,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de aceleraciones en y=2500 & t=0 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
ListStreamDensityPlatfun:
Value of optionColorFunction→ RainbowOpacityis not a valid colorfunction or a gradientColorDataentity >>
```



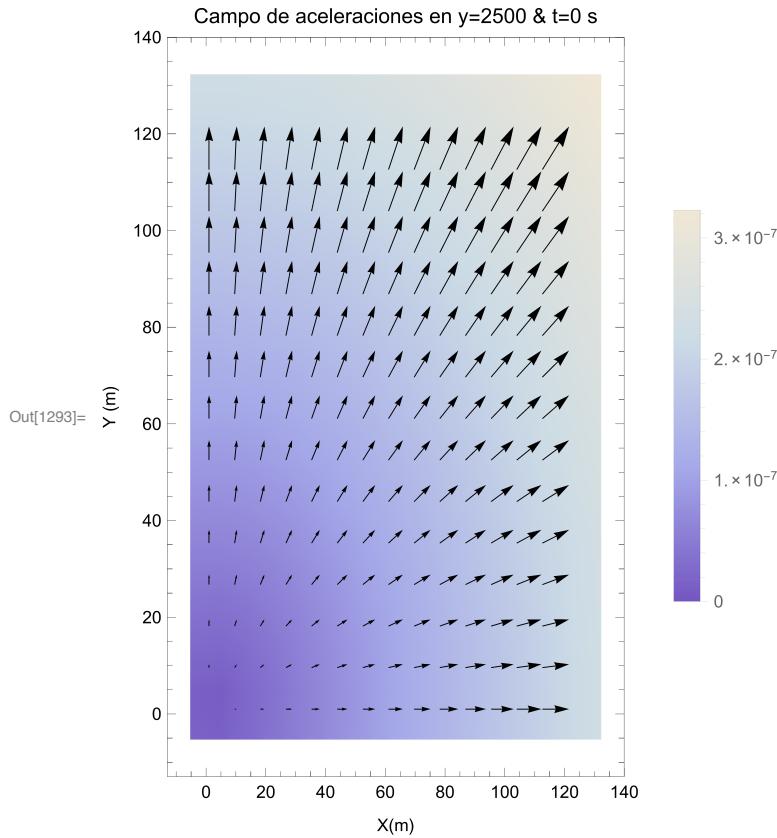
ListStreamDensityPlotfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



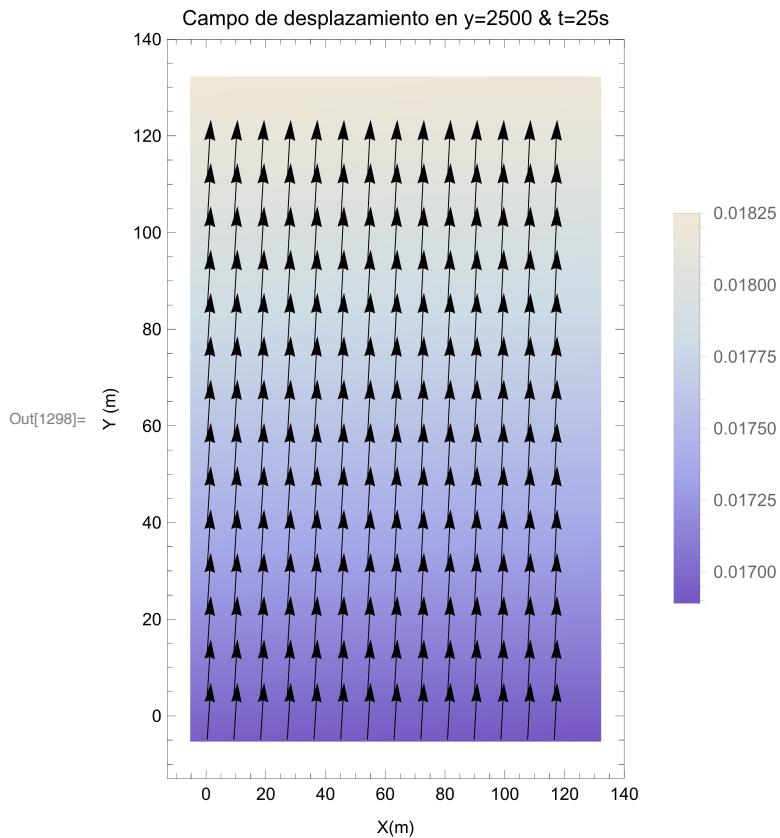
ListStreamDensityPlatfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



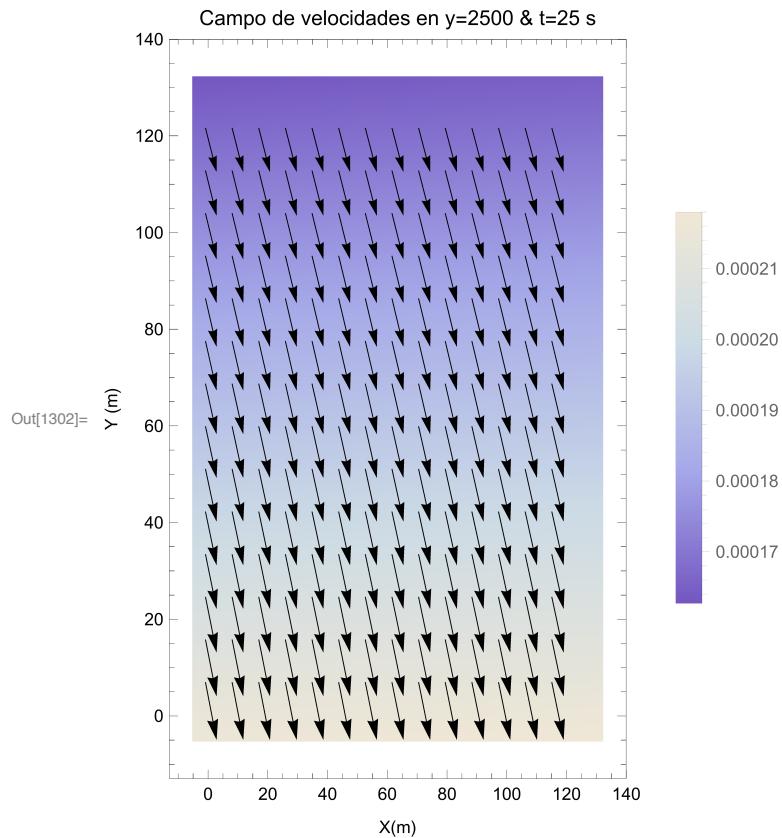
■ Para $y=2500$ & $t=25$

```
In[1294]:= xx = Range[0, 25000, 200];
uuu = Evaluate[u[x, 2500, 25]] /. {x → xx};
vvv = Evaluate[v[x, 2500, 25]] /. {x → xx};
data23 = Table[{uuu[[i]], vvv[[j]]}, {i, Length[uuu]}, {j, Length[vvv]}];
ListVectorDensityPlot[data23,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de desplazamiento en y=2500 & t=25s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
du = D[Evaluate[u[x, 2500, t]], t] /. {t → 25, x → xx};
dv = D[Evaluate[v[x, 2500, t]], t] /. {t → 25, x → xx};
data24 = Table[{du[[i]], dv[[j]]}, {i, Length[du]}, {j, Length[dv]}];
ListVectorDensityPlot[data24,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de velocidades en y=2500 & t=25 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
d2u = D[D[Evaluate[u[x, 2500, t]], t], t] /. {t → 25, x → xx};
d2v = D[D[Evaluate[v[x, 2500, t]], t], t] /. {t → 25, x → xx};
data25 = Table[{d2u[[i]], d2v[[j]]}, {i, Length[d2u]}, {j, Length[d2v]}];
ListVectorDensityPlot[data25,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de aceleraciones en y=2500 & t=25 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
ListStreamDensityPlatfun:
Value of optionColorFunction-> RainbowOpacity is not a valid colorfunction or a gradientColorData entity >>
```



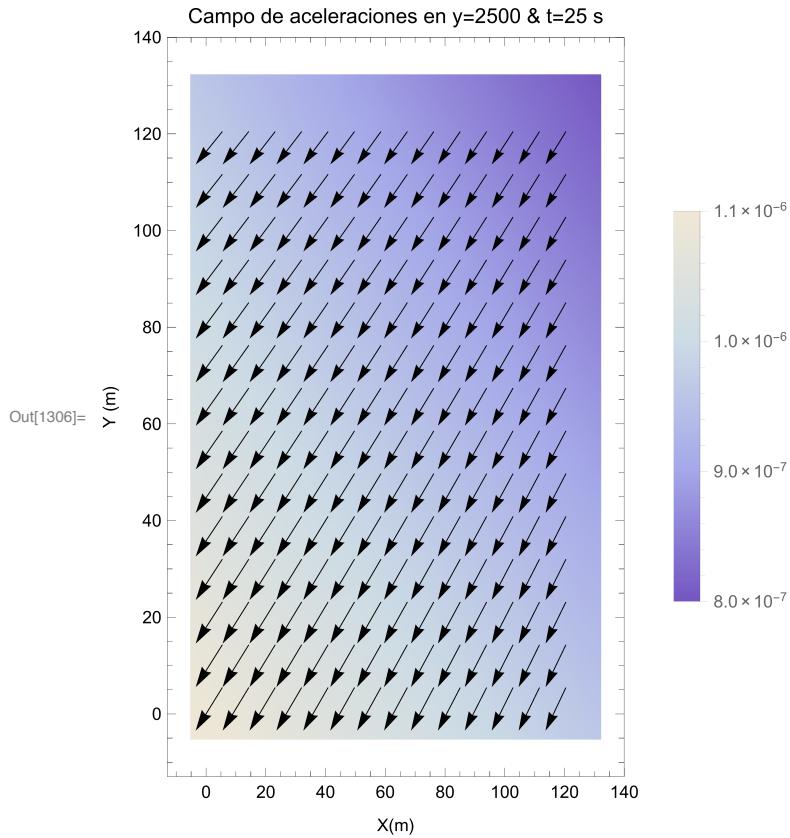
ListStreamDensityPlatcfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



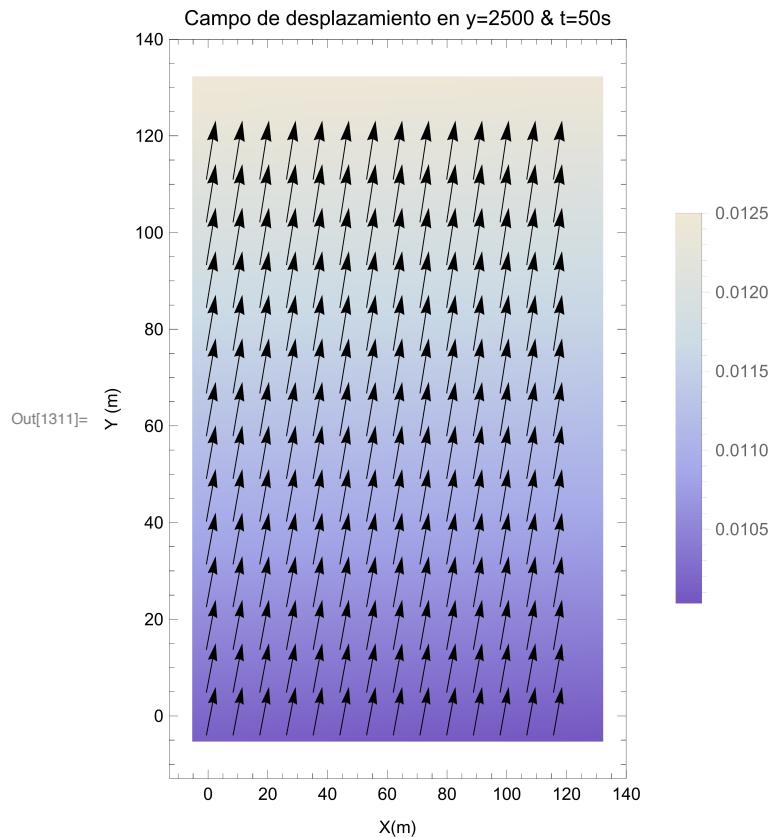
ListStreamDensityPlotfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



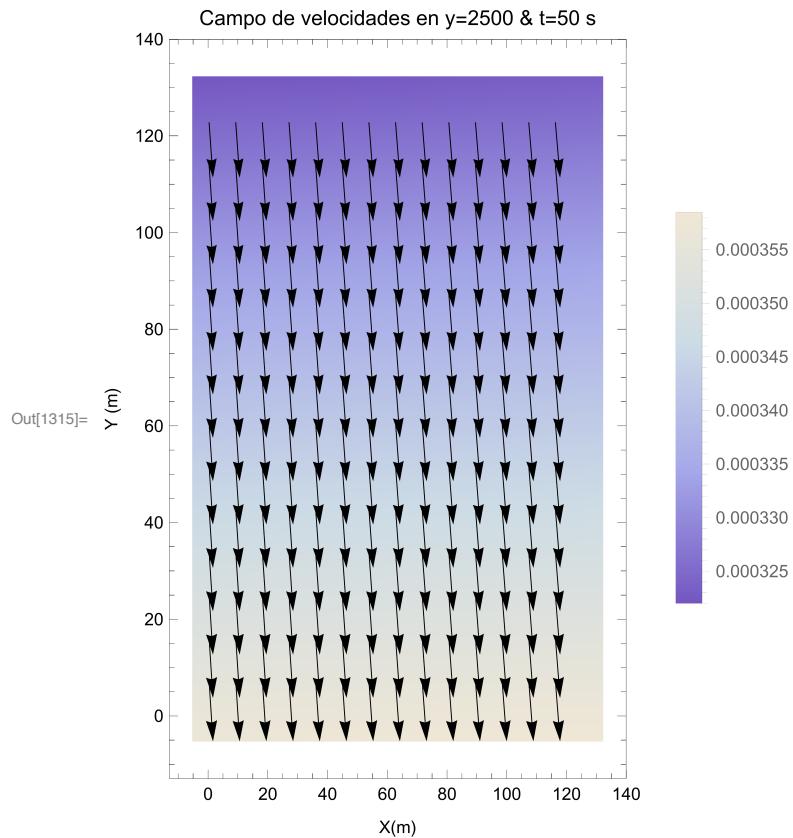
■ Para $y=2500$ & $t=50$

```
In[1307]:= xx = Range[0, 25000, 200];
uuu = Evaluate[u[x, 2500, 50]] /. {x → xx};
vvv = Evaluate[v[x, 2500, 50]] /. {x → xx};
data23 = Table[{uuu[[i]], vvv[[j]]}, {i, Length[uuu]}, {j, Length[vvv]}];
ListVectorDensityPlot[data23,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de desplazamiento en y=2500 & t=50s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
du = D[Evaluate[u[x, 2500, t]], t] /. {t → 50, x → xx};
dv = D[Evaluate[v[x, 2500, t]], t] /. {t → 50, x → xx};
data24 = Table[{du[[i]], dv[[j]]}, {i, Length[du]}, {j, Length[dv]}];
ListVectorDensityPlot[data24,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de velocidades en y=2500 & t=50 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
d2u = D[D[Evaluate[u[x, 2500, t]], t], t] /. {t → 50, x → xx};
d2v = D[D[Evaluate[v[x, 2500, t]], t], t] /. {t → 50, x → xx};
data25 = Table[{d2u[[i]], d2v[[j]]}, {i, Length[d2u]}, {j, Length[d2v]}];
ListVectorDensityPlot[data25,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de aceleraciones en y=2500 & t=50 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
ListStreamDensityPlatfun:
Value of optionColorFunction→ RainbowOpacityis not a valid colorfunction or a gradientColorDataentity >>
```



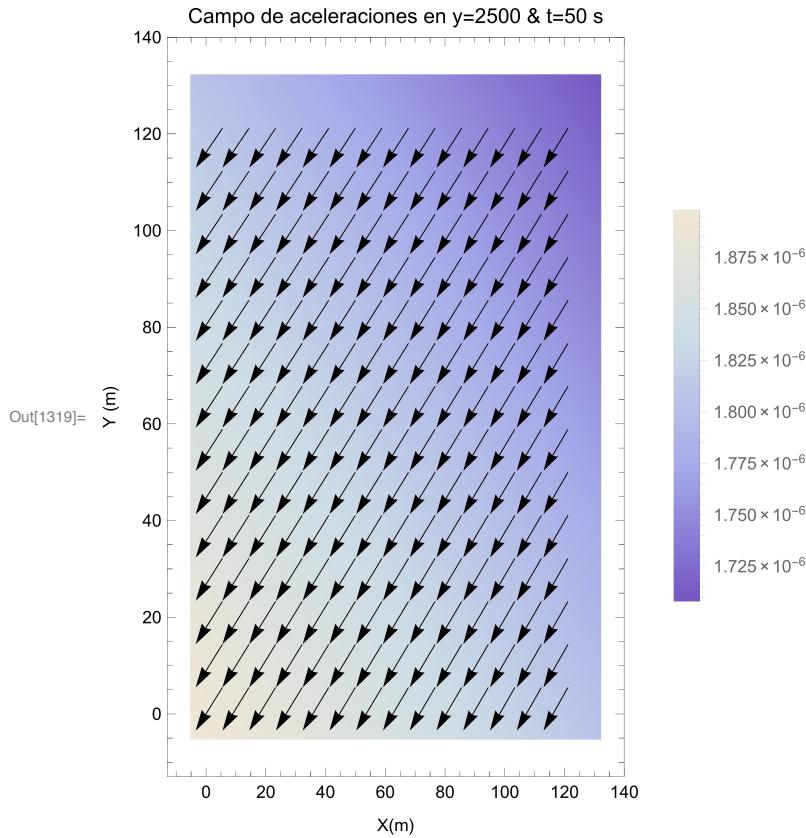
ListStreamDensityPlotfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



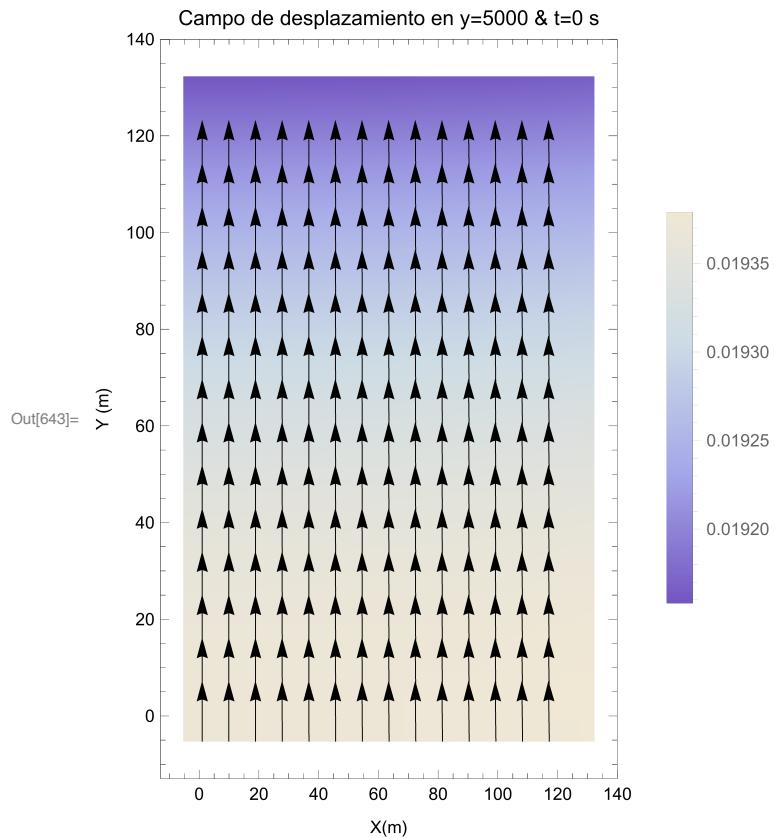
ListStreamDensityPlatfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



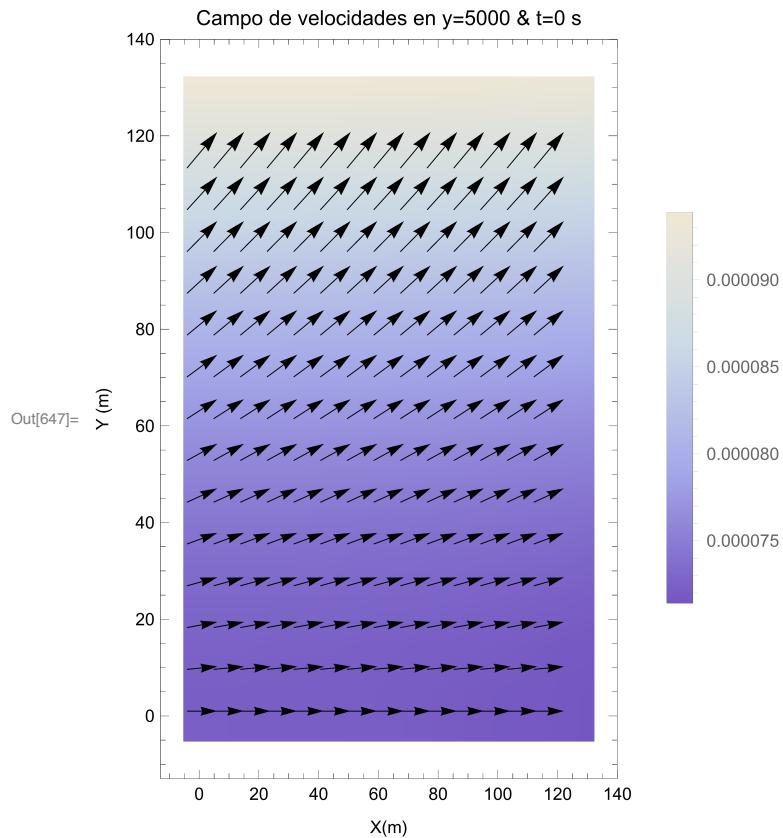
■ Para $y=5000$ & $t=0$

```
In[639]:= xx = Range[0, 25000, 200];
uuu = Evaluate[u[x, 5000, 0]] /. {x → xx};
vvv = Evaluate[v[x, 5000, 0]] /. {x → xx};
data23 = Table[{uuu[[i]], vvv[[j]]}, {i, Length[uuu]}, {j, Length[vvv]}];
ListVectorDensityPlot[data23,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de desplazamiento en y=5000 & t=0 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
du = D[Evaluate[u[x, 5000, t]], t] /. {t → 0, x → xx};
dv = D[Evaluate[v[x, 5000, t]], t] /. {t → 0, x → xx};
data24 = Table[{du[[i]], dv[[j]]}, {i, Length[du]}, {j, Length[dv]}];
ListVectorDensityPlot[data24,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de velocidades en y=5000 & t=0 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
d2u = D[D[Evaluate[u[x, 5000, t]], t], t] /. {t → 0, x → xx};
d2v = D[D[Evaluate[v[x, 5000, t]], t], t] /. {t → 0, x → xx};
data25 = Table[{d2u[[i]], d2v[[j]]}, {i, Length[d2u]}, {j, Length[d2v]}];
ListVectorDensityPlot[data25,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de aceleraciones en y=5000 & t=0 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
ListStreamDensityPlatfun:
Value of optionColorFunction→ RainbowOpacityis not a valid colorfunction or a gradientColorDataentity >>
```



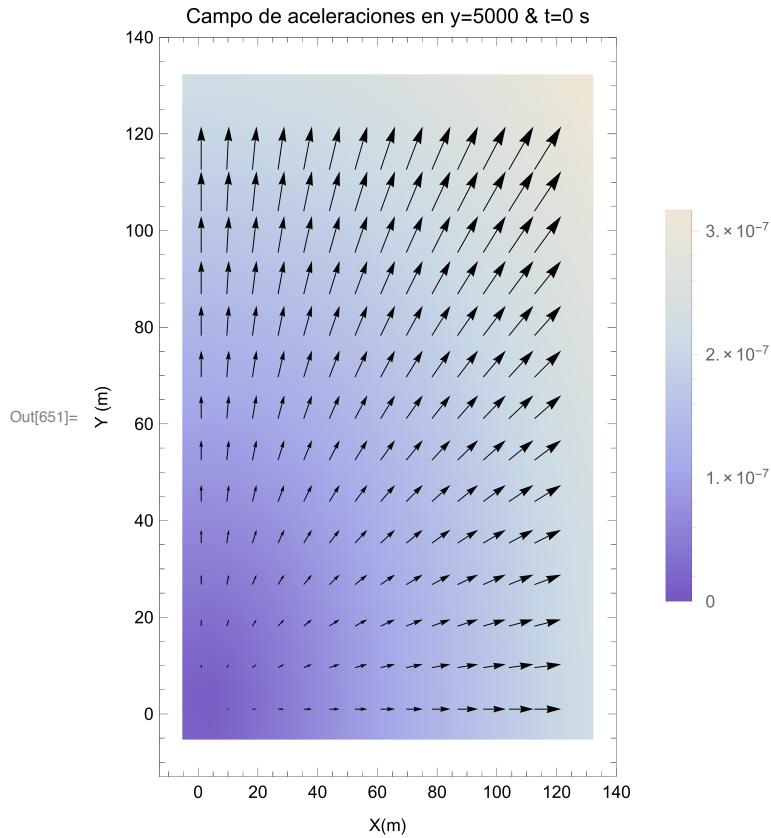
ListStreamDensityPlotfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



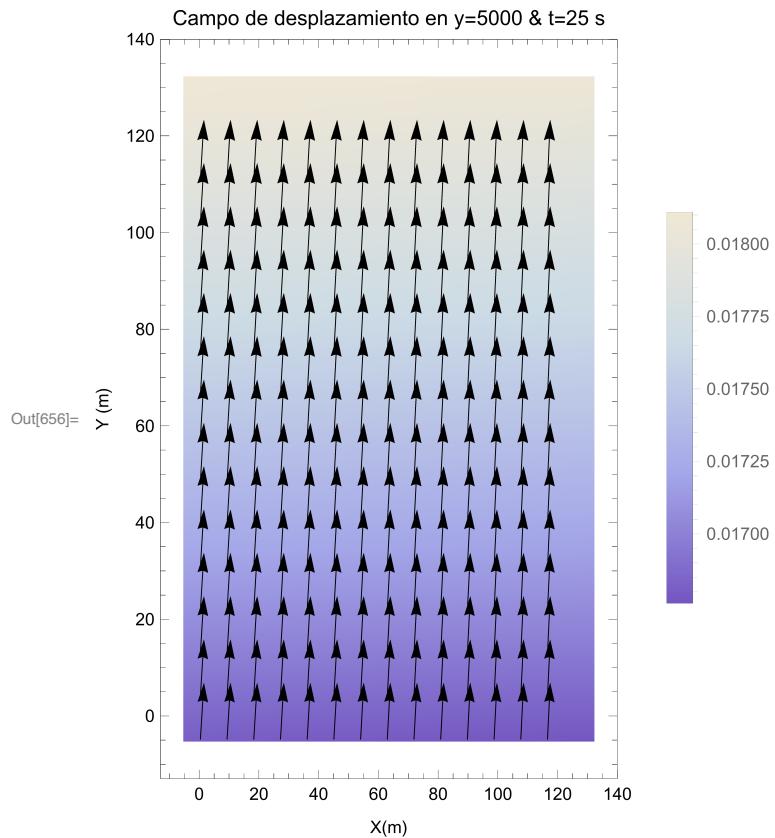
ListStreamDensityPlotfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



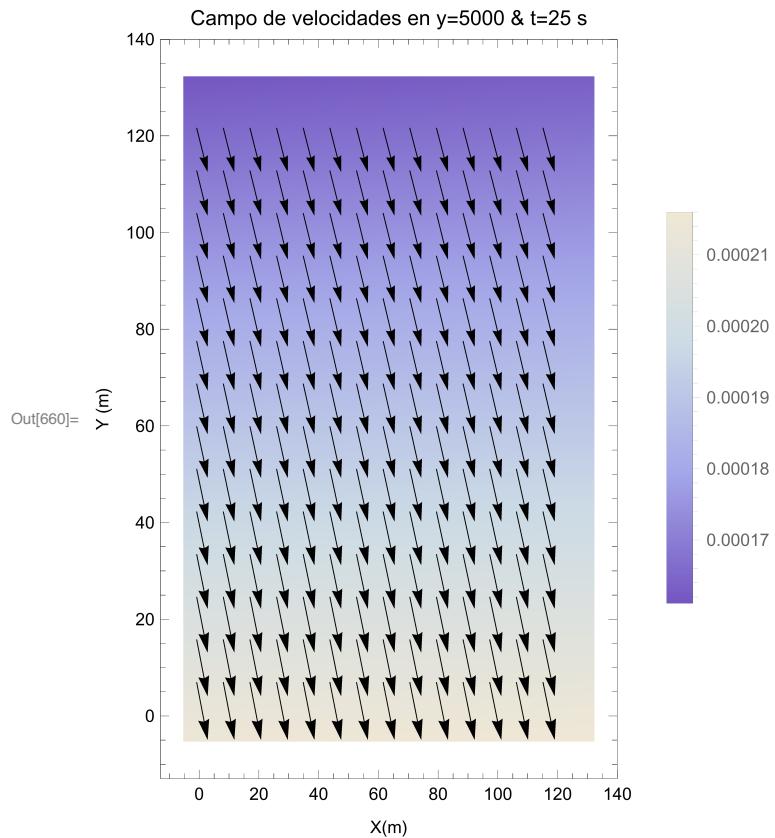
■ Para $y=5000$ & $t=25$

```
In[652]:= xx = Range[0, 25000, 200];
uuu = Evaluate[u[x, 5000, 25]] /. {x → xx};
vvv = Evaluate[v[x, 5000, 25]] /. {x → xx};
data23 = Table[{uuu[[i]], vvv[[j]]}, {i, Length[uuu]}, {j, Length[vvv]}];
ListVectorDensityPlot[data23,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de desplazamiento en y=5000 & t=25 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
du = D[Evaluate[u[x, 5000, t]], t] /. {t → 25, x → xx};
dv = D[Evaluate[v[x, 5000, t]], t] /. {t → 25, x → xx};
data24 = Table[{du[[i]], dv[[j]]}, {i, Length[du]}, {j, Length[dv]}];
ListVectorDensityPlot[data24,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de velocidades en y=5000 & t=25 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
d2u = D[D[Evaluate[u[x, 5000, t]], t], t] /. {t → 25, x → xx};
d2v = D[D[Evaluate[v[x, 5000, t]], t], t] /. {t → 25, x → xx};
data25 = Table[{d2u[[i]], d2v[[j]]}, {i, Length[d2u]}, {j, Length[d2v]}];
ListVectorDensityPlot[data25,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de aceleraciones en y=5000 & t=25 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
ListStreamDensityPlatfun:
Value of option ColorFunction → RainbowOpacity is not a valid colorfunction or a gradientColorData entity >>
```



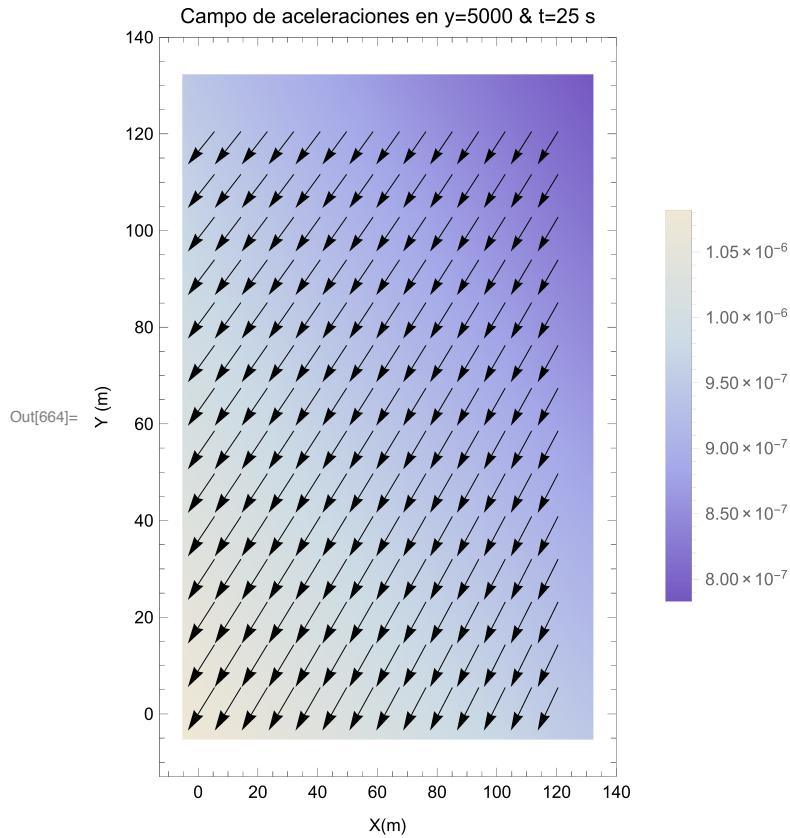
ListStreamDensityPlotfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



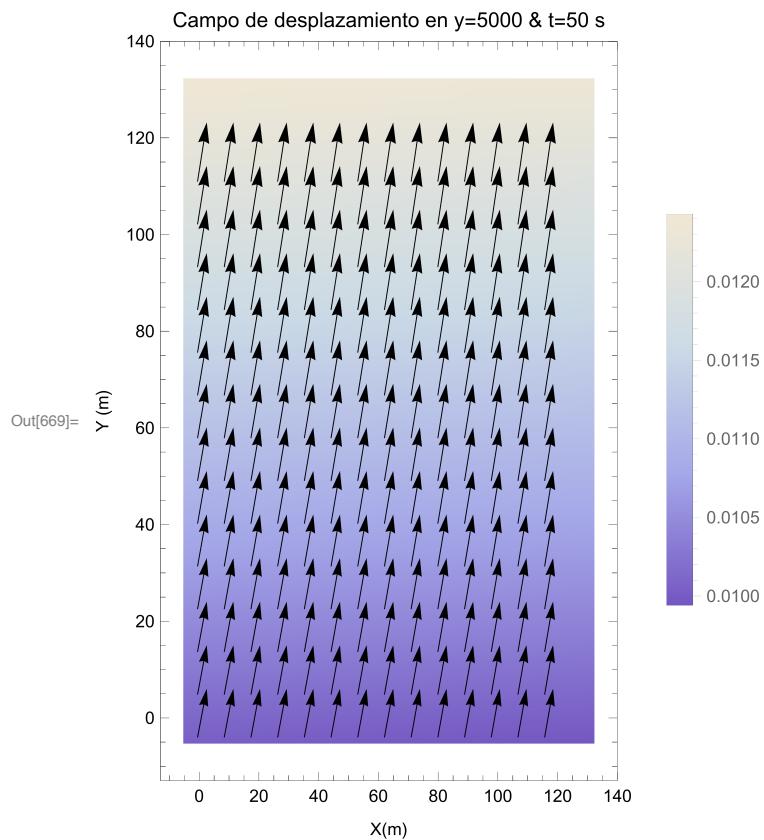
ListStreamDensityPlotfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



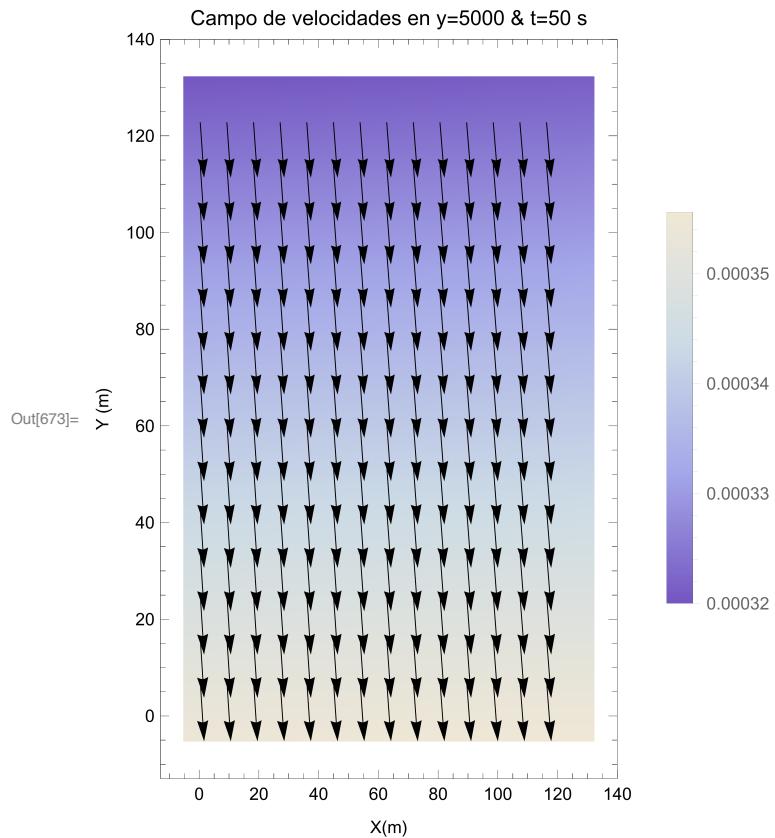
■ Para $y=5000$ & $t=50$

```
In[665]:= xx = Range[0, 25000, 200];
uuu = Evaluate[u[x, 5000, 50]] /. {x → xx};
vvv = Evaluate[v[x, 5000, 50]] /. {x → xx};
data23 = Table[{uuu[[i]], vvv[[j]]}, {i, Length[uuu]}, {j, Length[vvv]}];
ListVectorDensityPlot[data23,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de desplazamiento en y=5000 & t=50 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
du = D[Evaluate[u[x, 5000, t]], t] /. {t → 50, x → xx};
dv = D[Evaluate[v[x, 5000, t]], t] /. {t → 50, x → xx};
data24 = Table[{du[[i]], dv[[j]]}, {i, Length[du]}, {j, Length[dv]}];
ListVectorDensityPlot[data24,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de velocidades en y=5000 & t=50 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
d2u = D[D[Evaluate[u[x, 5000, t]], t], t] /. {t → 50, x → xx};
d2v = D[D[Evaluate[v[x, 5000, t]], t], t] /. {t → 50, x → xx};
data25 = Table[{d2u[[i]], d2v[[j]]}, {i, Length[d2u]}, {j, Length[d2v]}];
ListVectorDensityPlot[data25,
 AspectRatio → GoldenRatio, FrameLabel → {"X(m)", "Y (m)" },
 PlotLabel → "Campo de aceleraciones en y=5000 & t=50 s",
 ColorFunction → "RainbowOpacity", VectorStyle → {Black}, PlotLegends → Automatic]
ListStreamDensityPlatfun:
Value of optionColorFunction→ RainbowOpacityis not a valid colorfunction or a gradientColorDataentity >>
```



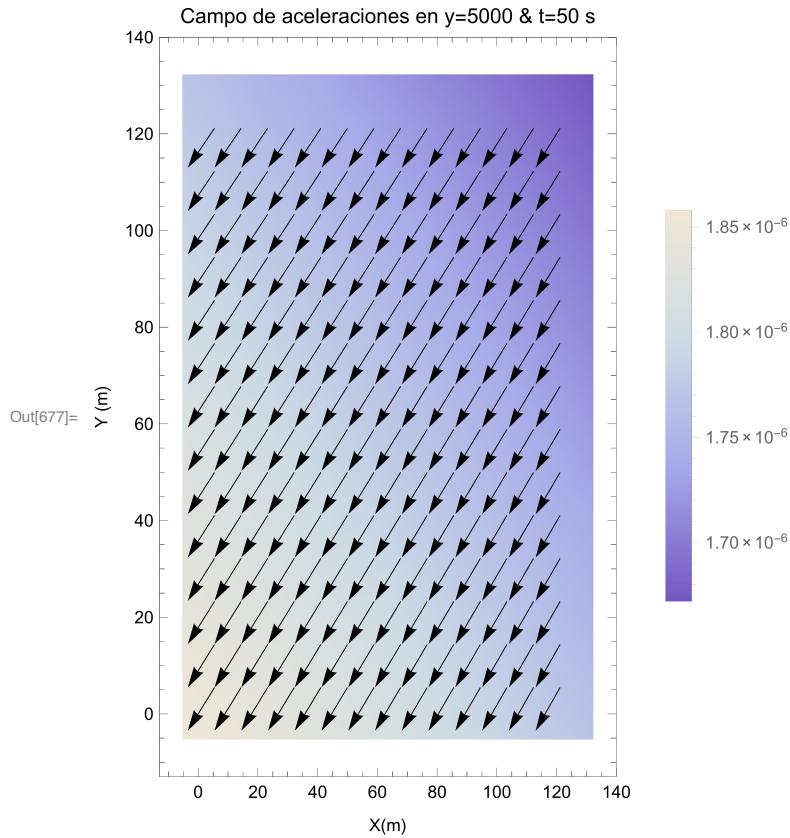
ListStreamDensityPlotfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



ListStreamDensityPlotfun:

Value of optionColorFunction-> RainbowOpacity is not a valid color function or a gradientColorData entity >>



6. Determine los lugares donde ocurre la máxima deformación unitaria principal, en un instante de tiempo dado, ¿cuál es el valor de esta deformación?

```
In[729]:= Clear[x, y, z, t]
Maximize[{Eigenvalues[ge][[1]], x > 0, y > 0, t > 0}, {x, y, t}]
Maximize[{Eigenvalues[ge][[2]], x > 0, y > 0, t > 0}, {x, y, t}]
Maximize[{Eigenvalues[ge][[3]], x > 0, y > 0, t > 0}, {x, y, t}]

Out[730]= {0., {x -> 84, y -> 67, t -> 5.}}

Out[731]= {2.03361 \times 10^{-8}, {x -> 216.364, y -> 1.21596 \times 10^{-22}, t -> 208.491} }

Out[732]= {6.31462 \times 10^{-8}, {x -> 3.64721, y -> 0., t -> 127.494} }
```

7. Diagrame el cambio de volumen del suelo para varios valores de t , en $y=0$ & varios $y>0$.

- Para $y=0$ & $t=0$

```
In[764]:= xx = Range[0, 25000, 1];
epi = Eigenvalues[ge] /. {y -> 0, t -> 0};
dvol = Total[epi] /. {x -> xx};
data26 = Thread[{xx, dvol}];
```

■ Para $y=0$ & $t=25$

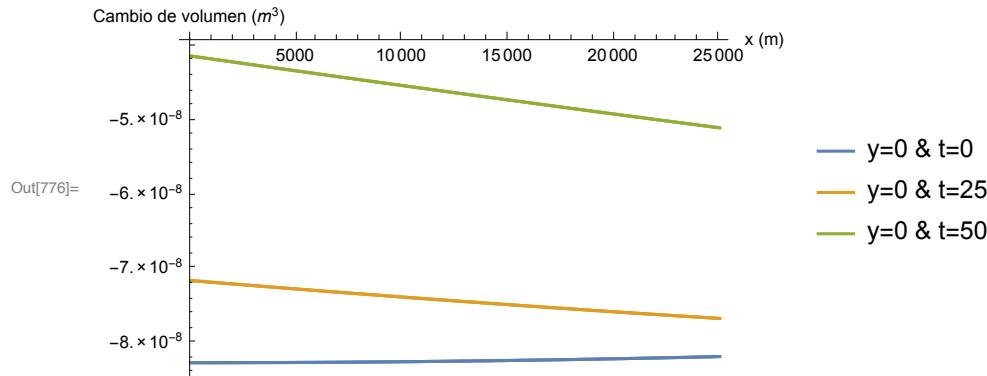
```
In[768]:= xx = Range[0, 25000, 1];
epi = Eigenvalues[ge] /. {y → 0, t → 25};
dvol = Total[epi] /. {x → xx};
data27 = Thread[{xx, dvol}];
```

■ Para $y=0$ & $t=50$

```
In[772]:= xx = Range[0, 25000, 1];
epi = Eigenvalues[ge] /. {y → 0, t → 50};
dvol = Total[epi] /. {x → xx};
data28 = Thread[{xx, dvol}];
```

■ Para $y=0$

```
In[776]:= ListPlot[{data26, data27, data28},
PlotLegends → {"y=0 & t=0", "y=0 & t=25", "y=0 & t=50"}, 
AxesLabel → {"x (m)", "Cambio de volumen (m³)"}, Joined -> True]
```



■ Para $y=1000$ & $t=0$

```
In[781]:= xx = Range[0, 25000, 1];
epi = Eigenvalues[ge] /. {y → 1000, t → 0};
dvol = Total[epi] /. {x → xx};
data29 = Thread[{xx, dvol}];
```

■ Para $y=1000$ & $t=25$

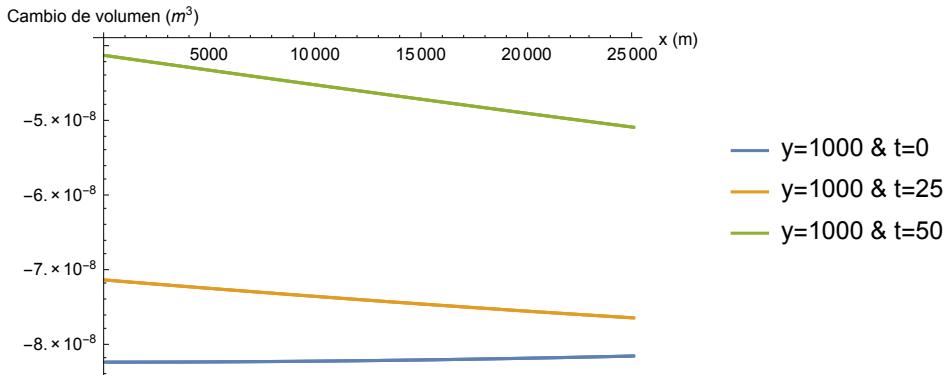
```
In[785]:= xx = Range[0, 25000, 1];
epi = Eigenvalues[ge] /. {y → 1000, t → 25};
dvol = Total[epi] /. {x → xx};
data30 = Thread[{xx, dvol}];
```

■ Para $y=1000$ & $t=50$

```
In[789]:= xx = Range[0, 25000, 1];
epi = Eigenvalues[ge] /. {y → 1000, t → 50};
dvol = Total[epi] /. {x → xx};
data31 = Thread[{xx, dvol}];
```

■ Para $y=1000$

```
In[793]:= ListPlot[{data29, data30, data31},
  PlotLegends -> {"y=1000 & t=0", "y=1000 & t=25", "y=1000 & t=50"},
  AxesLabel -> {"x (m)", "Cambio de volumen (m³)"}, Joined -> True]
```



- Para $y=3000 \& t=0$

```
In[794]:= xx = Range[0, 25000, 1];
epi = Eigenvalues[ge] /. {y -> 3000, t -> 0};
dvol = Total[epi] /. {x -> xx};
data32 = Thread[{xx, dvol}];
```

- Para $y=3000 \& t=25$

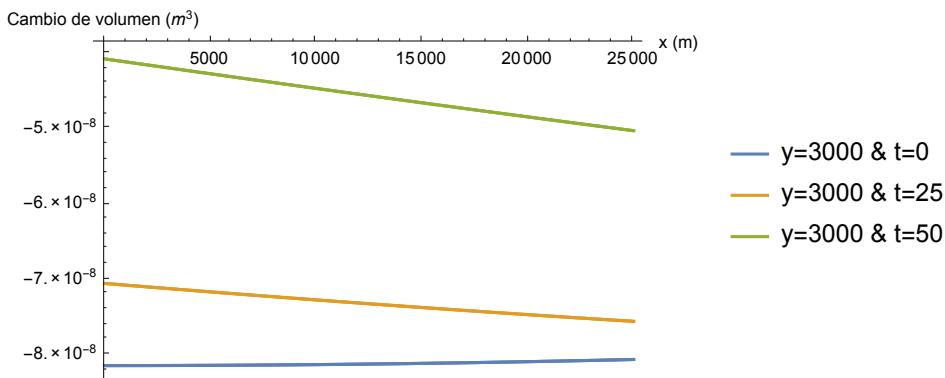
```
In[798]:= xx = Range[0, 25000, 1];
epi = Eigenvalues[ge] /. {y -> 3000, t -> 25};
dvol = Total[epi] /. {x -> xx};
data33 = Thread[{xx, dvol}];
```

- Para $y=3000 \& t=50$

```
In[802]:= xx = Range[0, 25000, 1];
epi = Eigenvalues[ge] /. {y -> 3000, t -> 50};
dvol = Total[epi] /. {x -> xx};
data34 = Thread[{xx, dvol}];
```

- Para $y=3000$

```
In[806]:= ListPlot[{data32, data33, data34},
  PlotLegends -> {"y=3000 & t=0", "y=3000 & t=25", "y=3000 & t=50"},
  AxesLabel -> {"x (m)", "Cambio de volumen (m³)"}, Joined -> True]
```



- Para $y=5000 \& t=0$

```
In[807]:= xx = Range[0, 25000, 1];
epi = Eigenvalues[ge] /. {y → 5000, t → 0};
dvol = Total[epi] /. {x → xx};
data35 = Thread[{xx, dvol}];
```

- Para $y=5000$ & $t=0$

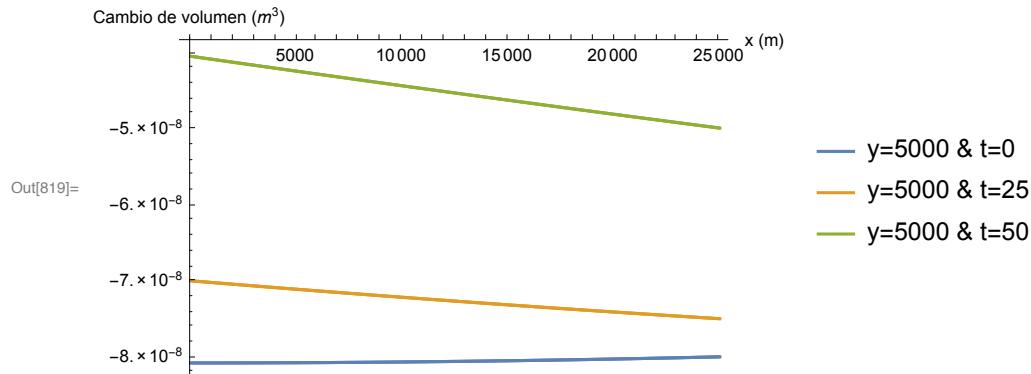
```
In[811]:= xx = Range[0, 25000, 1];
epi = Eigenvalues[ge] /. {y → 5000, t → 25};
dvol = Total[epi] /. {x → xx};
data36 = Thread[{xx, dvol}];
```

- Para $y=5000$ & $t=25$

```
In[815]:= xx = Range[0, 25000, 1];
epi = Eigenvalues[ge] /. {y → 5000, t → 50};
dvol = Total[epi] /. {x → xx};
data37 = Thread[{xx, dvol}];
```

- Para $y=5000$

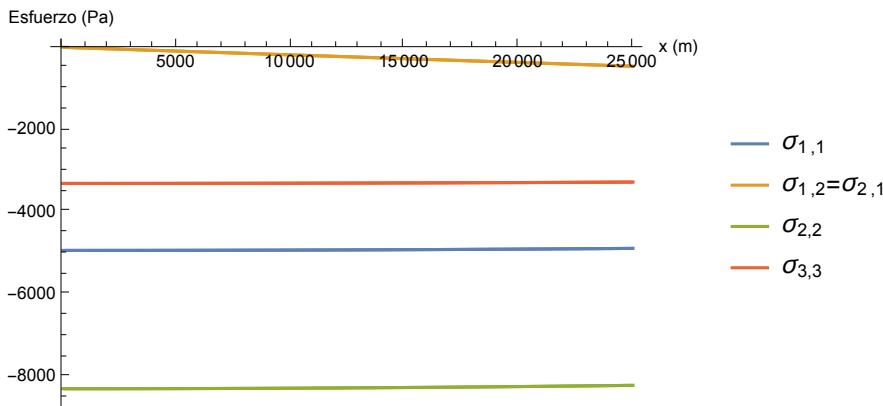
```
In[819]:= ListPlot[{data35, data36, data37},
PlotLegends → {"y=5000 & t=0", "y=5000 & t=25", "y=5000 & t=50"},
AxesLabel → {"x (m)", "Cambio de volumen (m³)"}, Joined -> True]
```



8. Diagrama las componentes del tensor de esfuerzos que son diferentes de 0 en $y = 0$, para varios valores de t . Haga lo mismo para varias partículas para varios $y>0$.

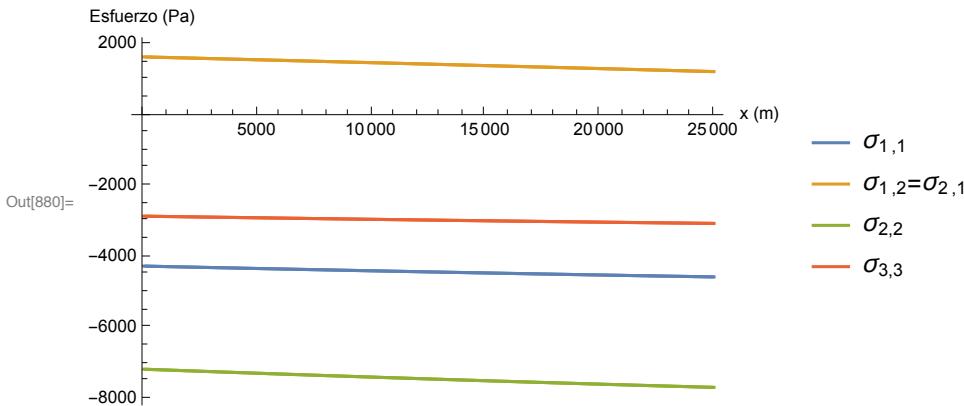
- Para $y=0$ & $t=0$

```
In[869]:= sijx = sij /. {y → 0, t → 0};
s11 = Thread[{xx, sijx[[1, 1]] /. {x → xx}}];
s12 = Thread[{xx, sijx[[1, 2]] /. {x → xx}}];
s22 = Thread[{xx, sijx[[2, 2]] /. {x → xx}}];
s33 = Thread[{xx, sijx[[3, 3]] /. {x → xx}}];
ListPlot[{s11, s12, s22, s33}, PlotLegends → {"σ1,1", "σ1,2=σ2,1", "σ2,2", "σ3,3"}, Joined → True, AxesLabel → {"x (m)", "Esfuerzo (Pa)"}]
```



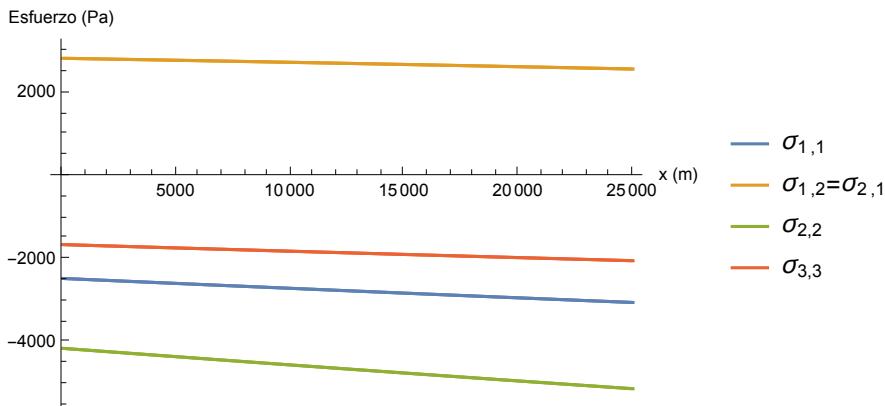
■ Para y=0 & t=25

```
In[875]:= sijx = sij /. {y → 0, t → 25};
s11 = Thread[{xx, sijx[[1, 1]] /. {x → xx}}];
s12 = Thread[{xx, sijx[[1, 2]] /. {x → xx}}];
s22 = Thread[{xx, sijx[[2, 2]] /. {x → xx}}];
s33 = Thread[{xx, sijx[[3, 3]] /. {x → xx}}];
ListPlot[{s11, s12, s22, s33}, PlotLegends → {"σ1,1", "σ1,2=σ2,1", "σ2,2", "σ3,3"}, Joined → True, AxesLabel → {"x (m)", "Esfuerzo (Pa)"}]
```



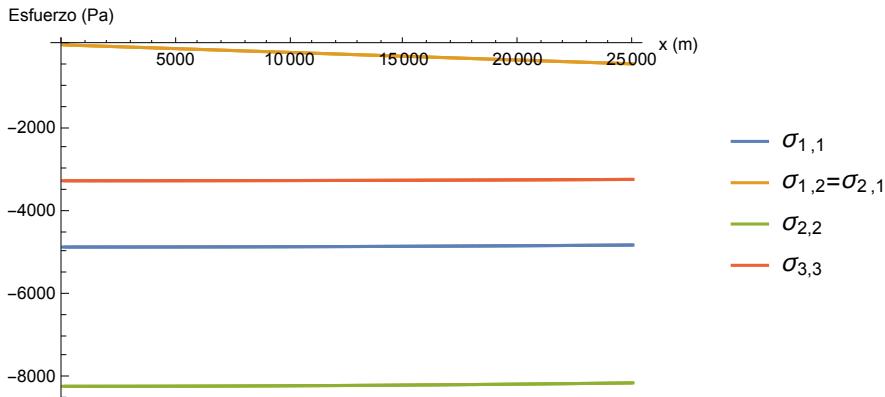
■ Para y=0 & t=50

```
In[881]:= sijx = sij /. {y → 0, t → 50};
s11 = Thread[{xx, sijx[[1, 1]] /. {x → xx}}];
s12 = Thread[{xx, sijx[[1, 2]] /. {x → xx}}];
s22 = Thread[{xx, sijx[[2, 2]] /. {x → xx}}];
s33 = Thread[{xx, sijx[[3, 3]] /. {x → xx}}];
ListPlot[{s11, s12, s22, s33}, PlotLegends → {"σ1,1", "σ1,2=σ2,1", "σ2,2", "σ3,3"},
Joined → True, AxesLabel → {"x (m)", "Esfuerzo (Pa)"}]
```



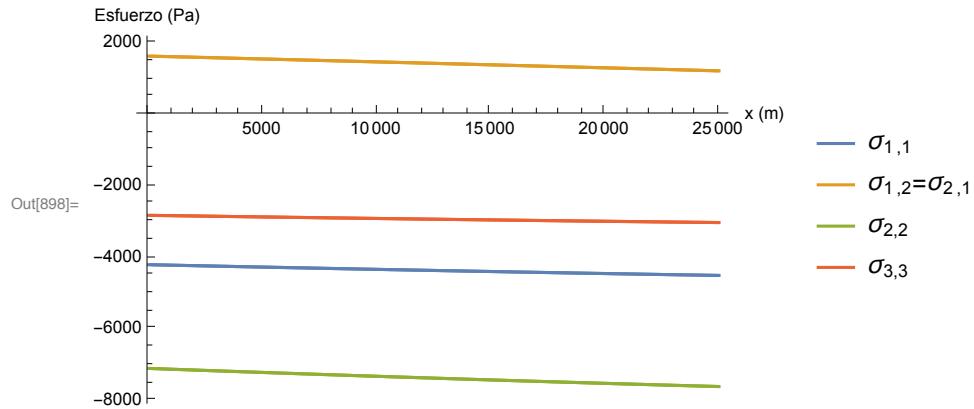
■ Para y=2500 & t=0

```
In[887]:= sijx = sij /. {y → 2500, t → 0};
s11 = Thread[{xx, sijx[[1, 1]] /. {x → xx}}];
s12 = Thread[{xx, sijx[[1, 2]] /. {x → xx}}];
s22 = Thread[{xx, sijx[[2, 2]] /. {x → xx}}];
s33 = Thread[{xx, sijx[[3, 3]] /. {x → xx}}];
ListPlot[{s11, s12, s22, s33}, PlotLegends → {"σ1,1", "σ1,2=σ2,1", "σ2,2", "σ3,3"},
Joined → True, AxesLabel → {"x (m)", "Esfuerzo (Pa)"}]
```



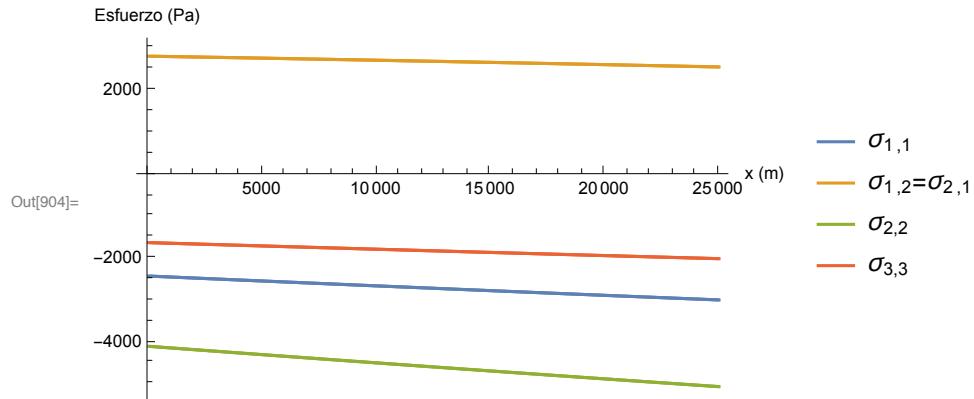
■ Para y=2500 & t=25

```
In[893]:= sijx = sij /. {y → 2500, t → 25};
s11 = Thread[{xx, sijx[[1, 1]] /. {x → xx}}];
s12 = Thread[{xx, sijx[[1, 2]] /. {x → xx}}];
s22 = Thread[{xx, sijx[[2, 2]] /. {x → xx}}];
s33 = Thread[{xx, sijx[[3, 3]] /. {x → xx}}];
ListPlot[{s11, s12, s22, s33}, PlotLegends → {"σ1,1", "σ1,2=σ2,1", "σ2,2", "σ3,3"}, Joined → True, AxesLabel → {"x (m)", "Esfuerzo (Pa)"}]
```



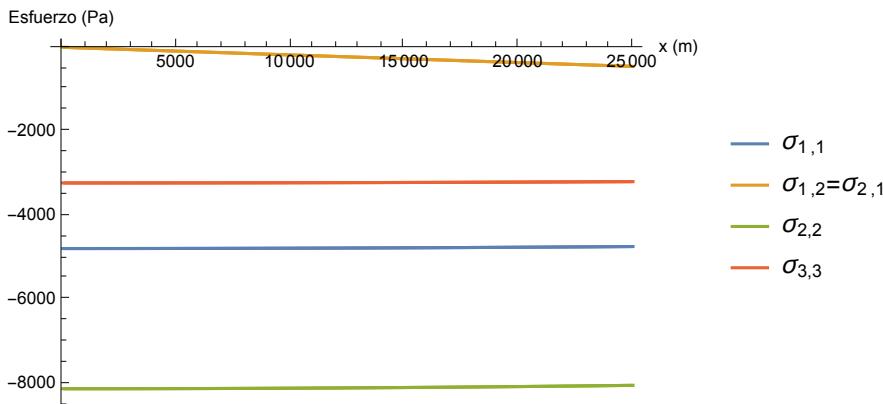
■ Para y=2500 & t=50

```
In[899]:= sijx = sij /. {y → 2500, t → 50};
s11 = Thread[{xx, sijx[[1, 1]] /. {x → xx}}];
s12 = Thread[{xx, sijx[[1, 2]] /. {x → xx}}];
s22 = Thread[{xx, sijx[[2, 2]] /. {x → xx}}];
s33 = Thread[{xx, sijx[[3, 3]] /. {x → xx}}];
ListPlot[{s11, s12, s22, s33}, PlotLegends → {"σ1,1", "σ1,2=σ2,1", "σ2,2", "σ3,3"}, Joined → True, AxesLabel → {"x (m)", "Esfuerzo (Pa)"}]
```



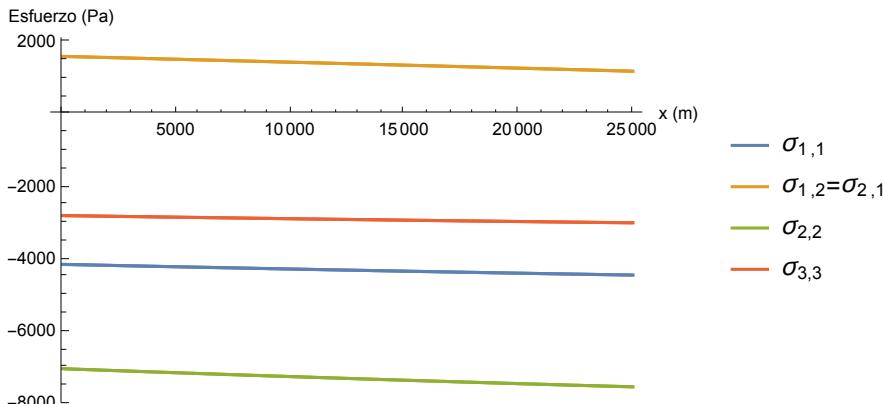
■ Para y=5000 & t=0

```
In[905]:= sijx = sij /. {y → 5000, t → 0};
s11 = Thread[{xx, sijx[[1, 1]] /. {x → xx}}];
s12 = Thread[{xx, sijx[[1, 2]] /. {x → xx}}];
s22 = Thread[{xx, sijx[[2, 2]] /. {x → xx}}];
s33 = Thread[{xx, sijx[[3, 3]] /. {x → xx}}];
ListPlot[{s11, s12, s22, s33}, PlotLegends → {"σ1,1", "σ1,2=σ2,1", "σ2,2", "σ3,3"},
Joined → True, AxesLabel → {"x (m)", "Esfuerzo (Pa)"}]
```



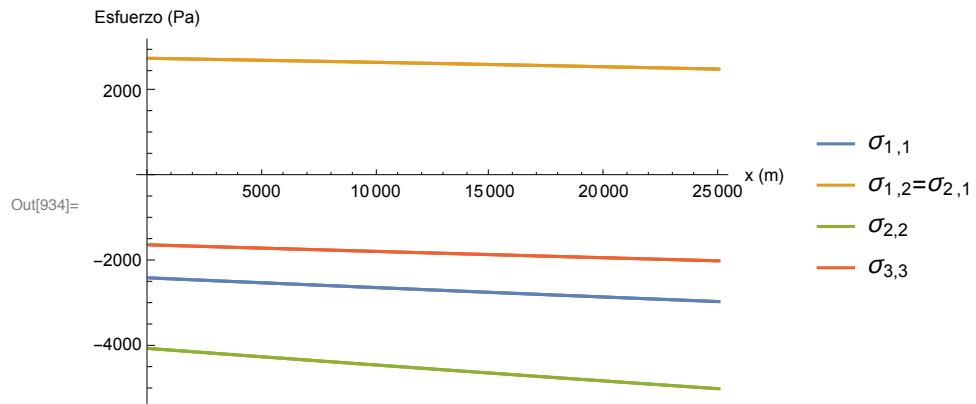
■ Para y=5000 & t=25

```
In[911]:= sijx = sij /. {y → 5000, t → 25};
s11 = Thread[{xx, sijx[[1, 1]] /. {x → xx}}];
s12 = Thread[{xx, sijx[[1, 2]] /. {x → xx}}];
s22 = Thread[{xx, sijx[[2, 2]] /. {x → xx}}];
s33 = Thread[{xx, sijx[[3, 3]] /. {x → xx}}];
ListPlot[{s11, s12, s22, s33}, PlotLegends → {"σ1,1", "σ1,2=σ2,1", "σ2,2", "σ3,3"},
Joined → True, AxesLabel → {"x (m)", "Esfuerzo (Pa)"}]
```



■ Para y=5000 & t=50

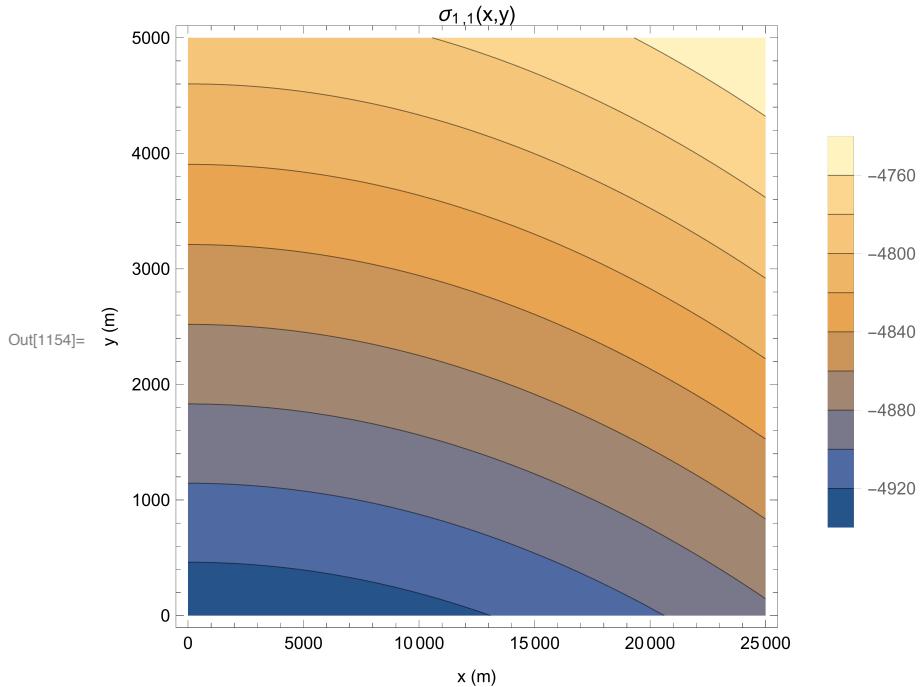
```
In[929]:= sijx = sij /. {y → 5000, t → 50};
s11 = Thread[{xx, sijx[[1, 1]] /. {x → xx}}];
s12 = Thread[{xx, sijx[[1, 2]] /. {x → xx}}];
s22 = Thread[{xx, sijx[[2, 2]] /. {x → xx}}];
s33 = Thread[{xx, sijx[[3, 3]] /. {x → xx}}];
ListPlot[{s11, s12, s22, s33}, PlotLegends → {"σ1,1", "σ1,2=σ2,1", "σ2,2", "σ3,3"},
 Joined → True, AxesLabel → {"x (m)", "Esfuerzo (Pa)"}]
```



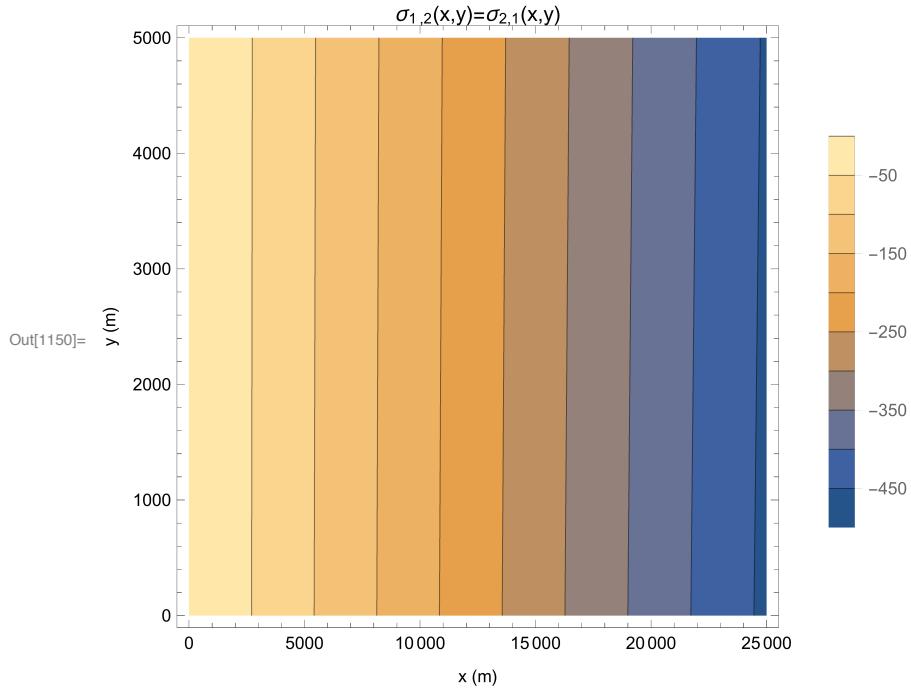
9. Para un tiempo dado, diagrame las componentes del tensor de esfuerzos que son diferentes de 0, como una función de x & y. Haga lo mismo para varios tiempos.

- Para t=0

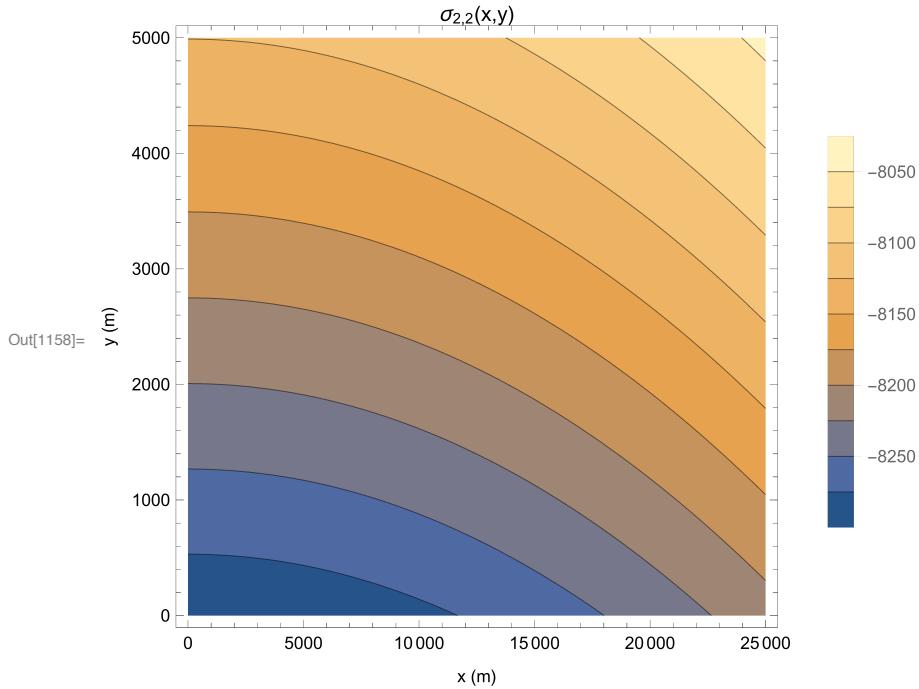
```
In[1151]:= sijxy = sij /. {t → 0};  
sijxy11 = sijxy[[1, 1]];  
f[x_, y_] := Evaluate[sijxy11];  
ContourPlot[f[x, y], {x, 0, 25000}, {y, 0, 5000}, PlotLegends → Automatic,  
PlotLabel → "σ_{1,1}(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```



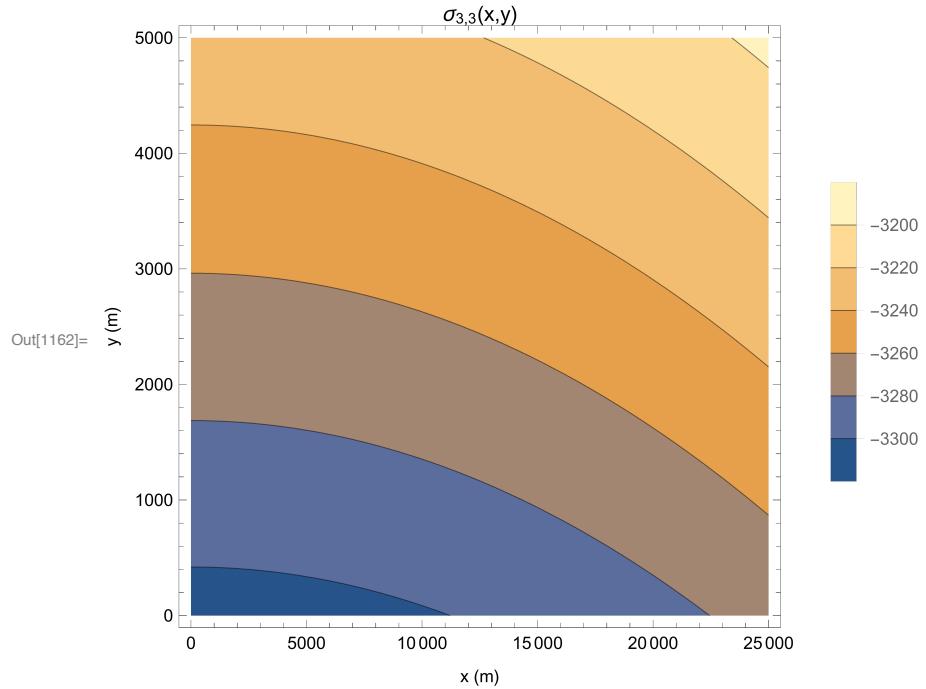
```
In[1147]:= sijxy = sij /. {t → 0};
sijxy12 = sijxy[[1, 2]];
f[x_, y_] := Evaluate[sijxy12];
ContourPlot[f[x, y], {x, 0, 25000}, {y, 0, 5000}, PlotLegends → Automatic,
PlotLabel → "σ1,2(x,y)=σ2,1(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```



```
In[1155]:= sijxy = sij /. {t → 0};  
sijxy22 = sijxy[[2, 2]];  
f[x_, y_] := Evaluate[sijxy22];  
ContourPlot[f[x, y], {x, 0, 25000}, {y, 0, 5000}, PlotLegends → Automatic,  
PlotLabel → "σ<sub>2,2</sub>(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```

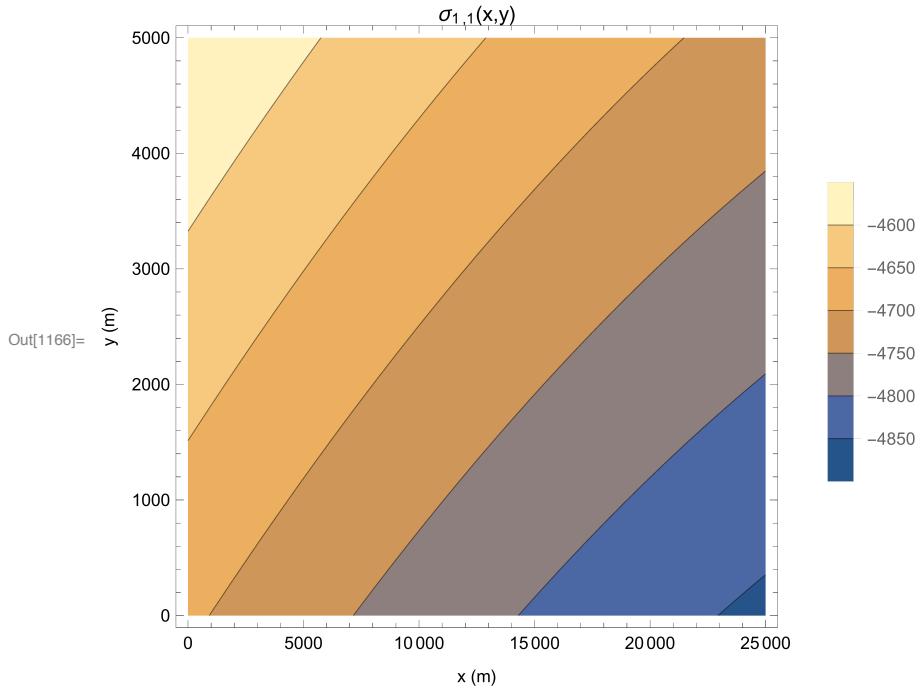


```
In[1159]:= sijxy = sij /. {t → 0};
sijxy33 = sijxy[[3, 3]];
f[x_, y_] := Evaluate[sijxy33];
ContourPlot[f[x, y], {x, 0, 25000}, {y, 0, 5000}, PlotLegends → Automatic,
PlotLabel → "σ3,3(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```

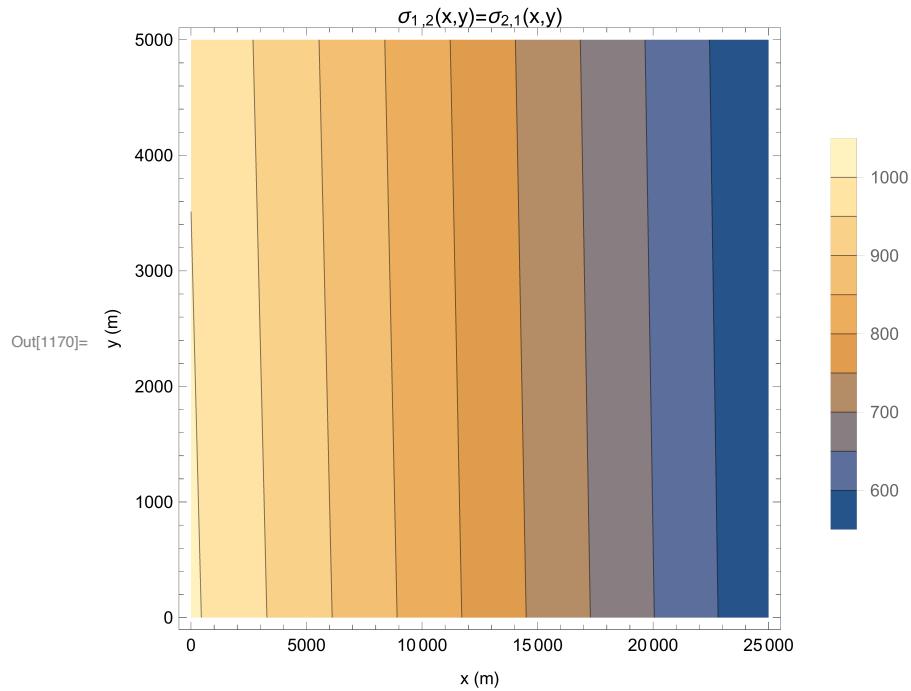


■ Para t=15

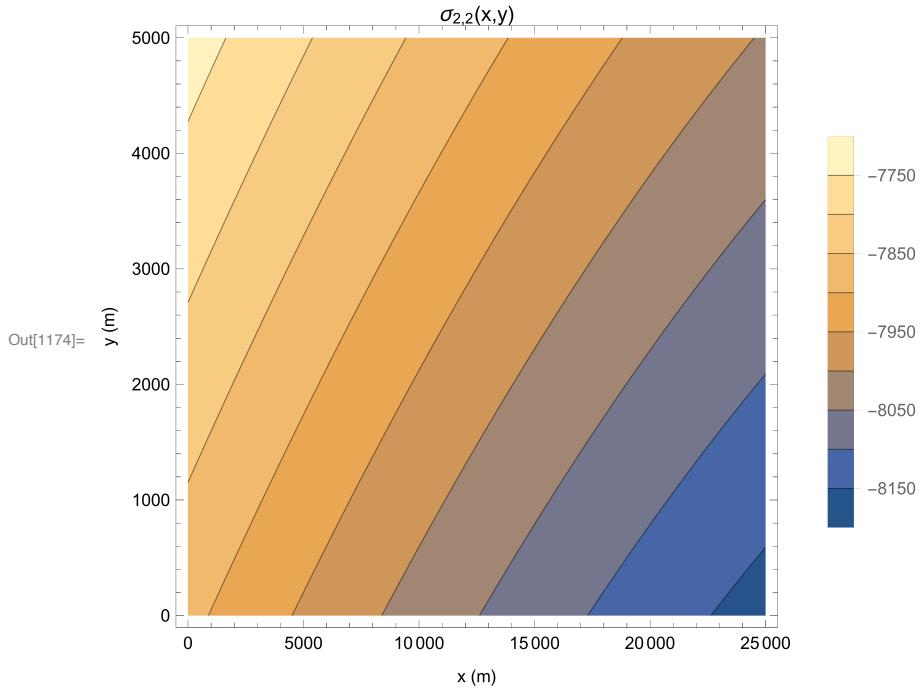
```
In[1163]:= sijxy = sij /. {t → 15};  
sijxy11 = sijxy[[1, 1]];  
f[x_, y_] := Evaluate[sijxy11];  
ContourPlot[f[x, y], {x, 0, 25 000}, {y, 0, 5000}, PlotLegends → Automatic,  
PlotLabel → "σ1,1(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```



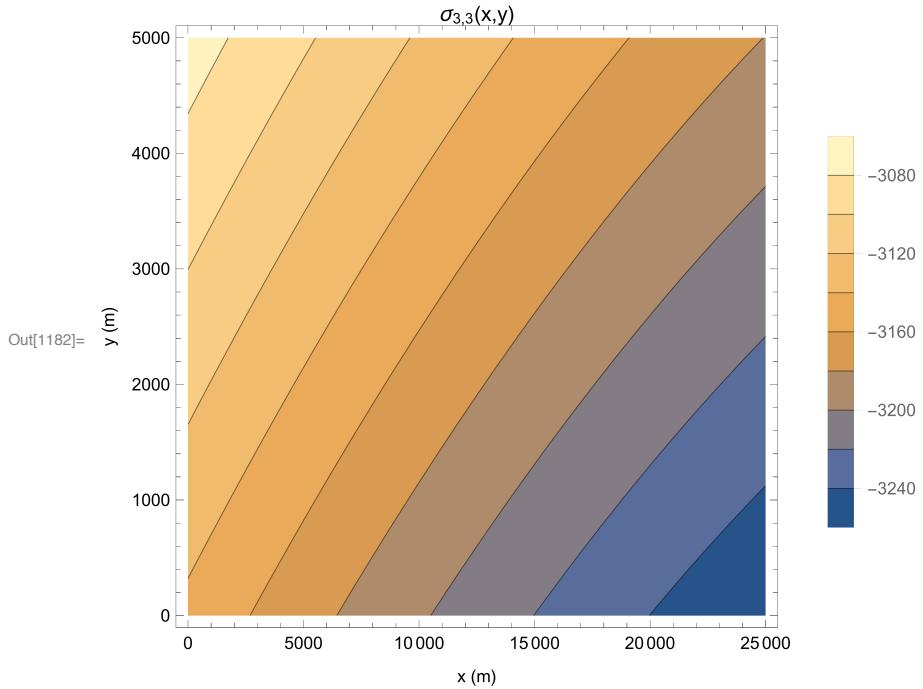
```
In[1167]:= sijxy = sij /. {t → 15};  
sijxy12 = sijxy[[1, 2]];  
f[x_, y_] := Evaluate[sijxy12];  
ContourPlot[f[x, y], {x, 0, 25000}, {y, 0, 5000}, PlotLegends → Automatic,  
PlotLabel → "σ1,2(x,y)=σ2,1(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```



```
In[1171]:= sijxy = sij /. {t → 15};  
sijxy22 = sijxy[[2, 2]];  
f[x_, y_] := Evaluate[sijxy22];  
ContourPlot[f[x, y], {x, 0, 25 000}, {y, 0, 5000}, PlotLegends → Automatic,  
PlotLabel → "σ<sub>2,2</sub>(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```

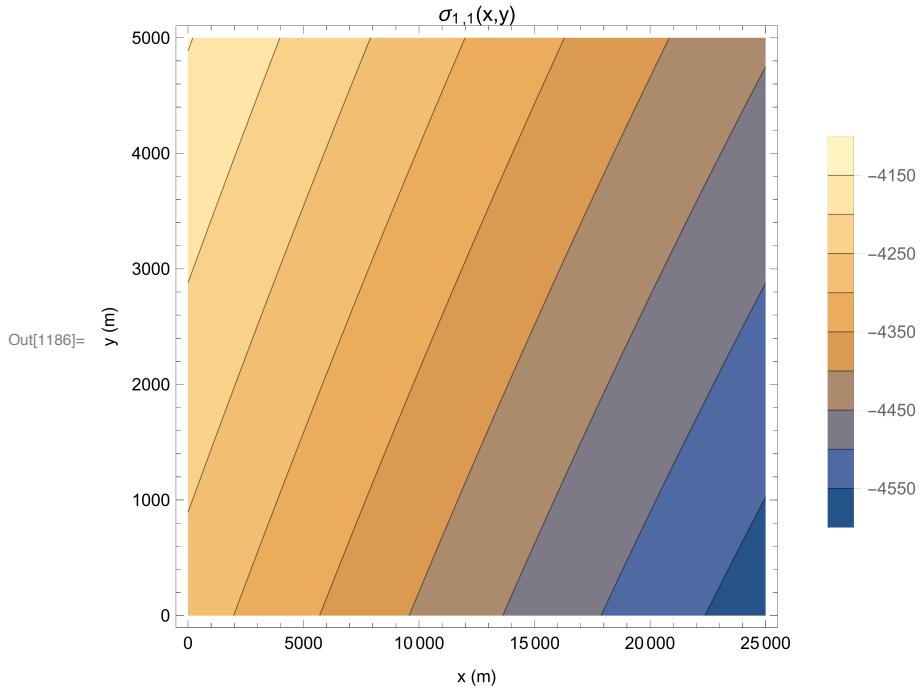


```
In[1179]:= sijxy = sij /. {t → 15};  
sijxy33 = sijxy[[3, 3]];  
f[x_, y_] := Evaluate[sijxy33];  
ContourPlot[f[x, y], {x, 0, 25000}, {y, 0, 5000}, PlotLegends → Automatic,  
PlotLabel → "σ3,3(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```

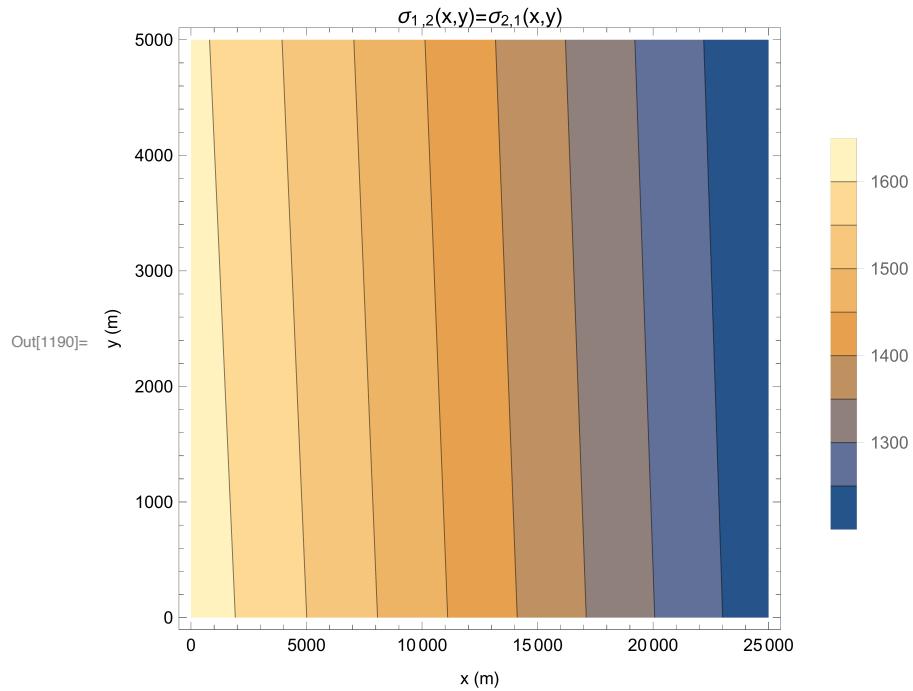


■ Para t=25

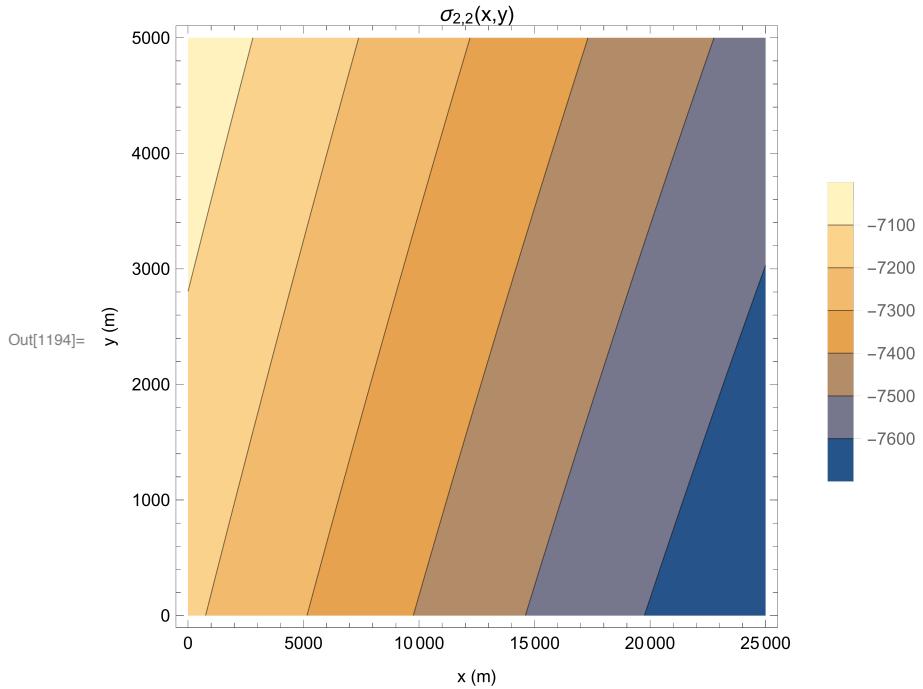
```
In[1183]:= sijxy = sij /. {t → 25};  
sijxy11 = sijxy[[1, 1]];  
f[x_, y_] := Evaluate[sijxy11];  
ContourPlot[f[x, y], {x, 0, 25 000}, {y, 0, 5000}, PlotLegends → Automatic,  
PlotLabel → "σ1,1(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```



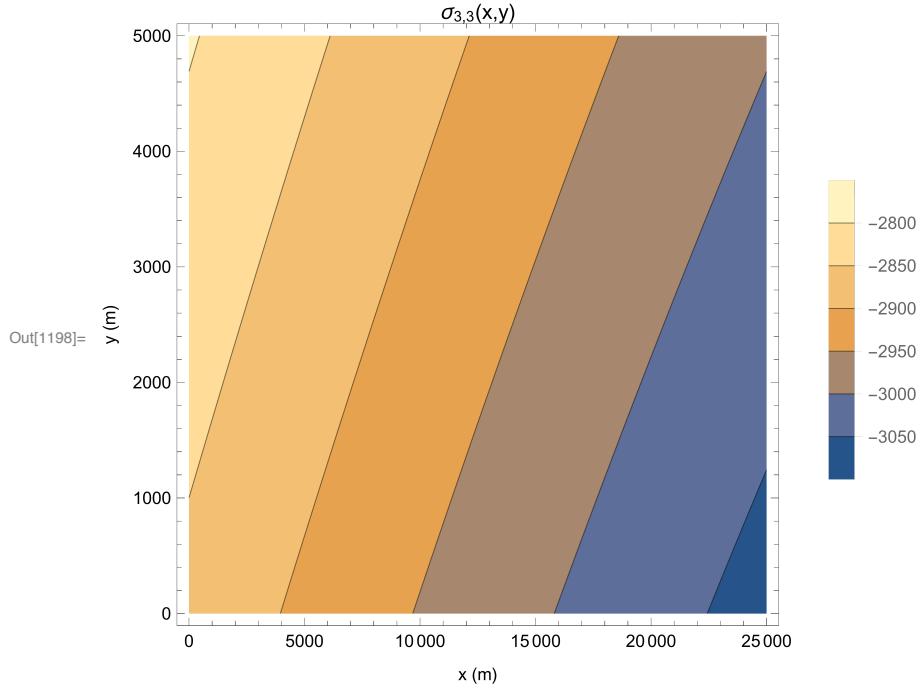
```
In[1187]:= sijxy = sij /. {t → 25};  
sijxy12 = sijxy[[1, 2]];  
f[x_, y_] := Evaluate[sijxy12];  
ContourPlot[f[x, y], {x, 0, 25000}, {y, 0, 5000}, PlotLegends → Automatic,  
PlotLabel → "σ1,2(x,y)=σ2,1(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```



```
In[1191]:= sijxy = sij /. {t → 25};  
sijxy22 = sijxy[[2, 2]];  
f[x_, y_] := Evaluate[sijxy22];  
ContourPlot[f[x, y], {x, 0, 25000}, {y, 0, 5000}, PlotLegends → Automatic,  
PlotLabel → "σ<sub>2,2</sub>(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```

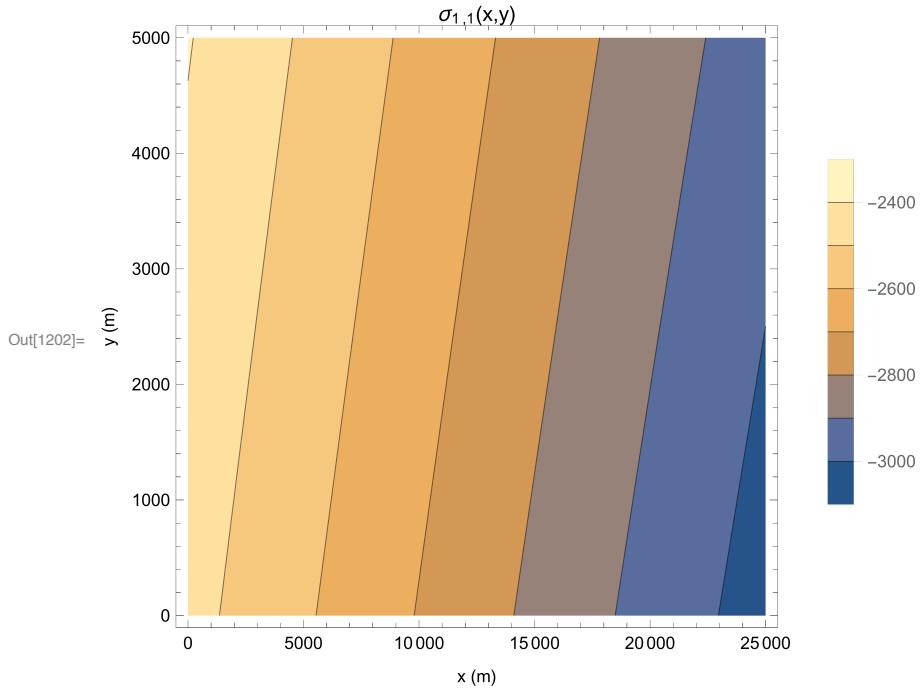


```
In[1195]:= sijxy = sij /. {t → 25};  
sijxy33 = sijxy[[3, 3]];  
f[x_, y_] := Evaluate[sijxy33];  
ContourPlot[f[x, y], {x, 0, 25000}, {y, 0, 5000}, PlotLegends → Automatic,  
PlotLabel → "σ3,3(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```

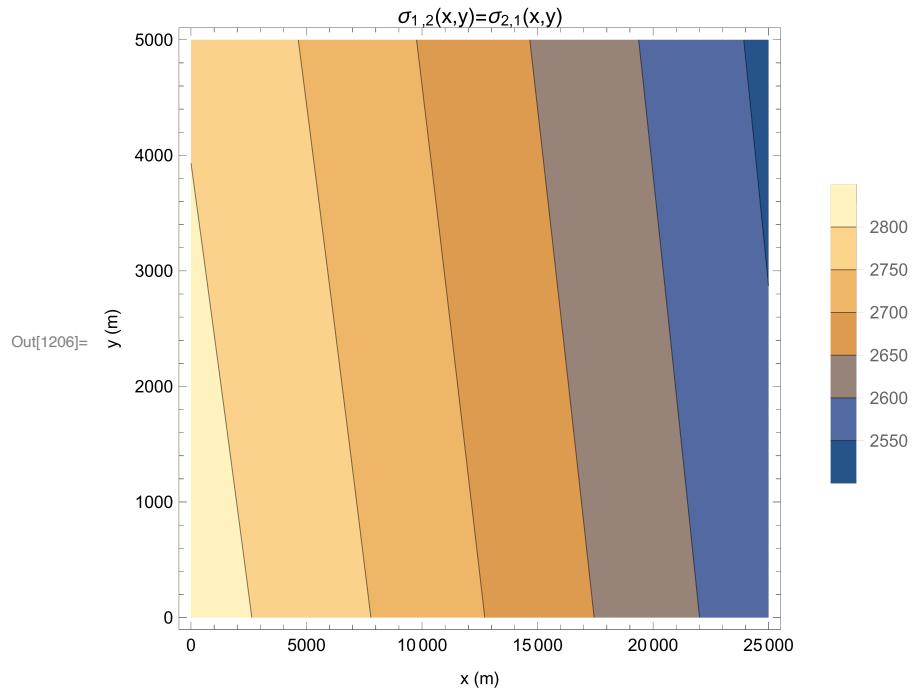


■ t=50

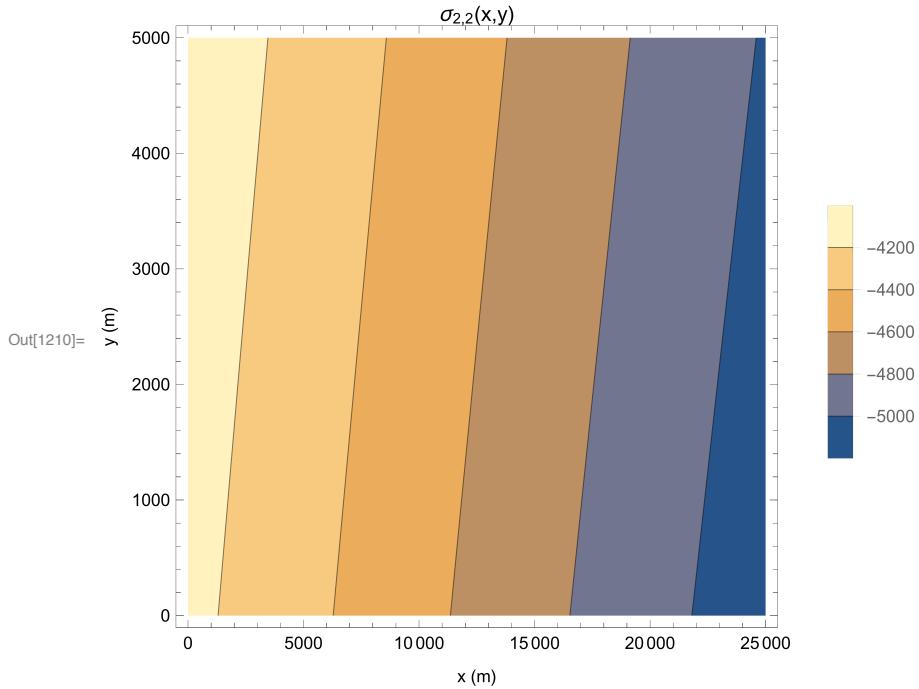
```
In[1199]:= sijxy = sij /. {t → 50};  
sijxy11 = sijxy[[1, 1]];  
f[x_, y_] := Evaluate[sijxy11];  
ContourPlot[f[x, y], {x, 0, 25 000}, {y, 0, 5000}, PlotLegends → Automatic,  
PlotLabel → "σ1,1(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```



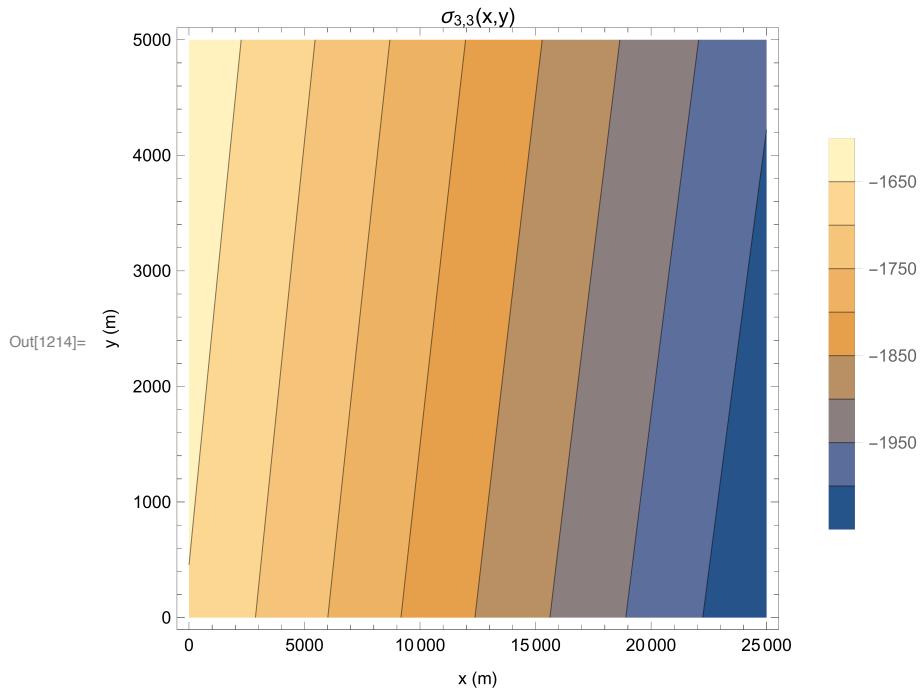
```
In[1203]:= sijxy = sij /. {t → 50};  
sijxy12 = sijxy[[1, 2]];  
f[x_, y_] := Evaluate[sijxy12];  
ContourPlot[f[x, y], {x, 0, 25000}, {y, 0, 5000}, PlotLegends → Automatic,  
PlotLabel → "σ1,2(x,y)=σ2,1(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```



```
In[1207]:= sijxy = sij /. {t → 50};  
sijxy22 = sijxy[[2, 2]];  
f[x_, y_] := Evaluate[sijxy22];  
ContourPlot[f[x, y], {x, 0, 25000}, {y, 0, 5000}, PlotLegends → Automatic,  
PlotLabel → "σ<sub>2,2</sub>(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```



```
In[1211]:= sijxy = sij /. {t → 50};
sijxy33 = sijxy[[3, 3]];
f[x_, y_] := Evaluate[sijxy33];
ContourPlot[f[x, y], {x, 0, 25000}, {y, 0, 5000}, PlotLegends → Automatic,
PlotLabel → "σ3,3(x,y)", FrameLabel → {"x (m)", "y (m)"}]
```



I0. Diagrama el esfuerzo cortante máximo del suelo en $y = 0$, para varios valores de t . Haga lo mismo para varias partículas en $y > 0$, ¿dónde ocurre este esfuerzo?

I1. Lo mismo que 9.