

Operating Systems

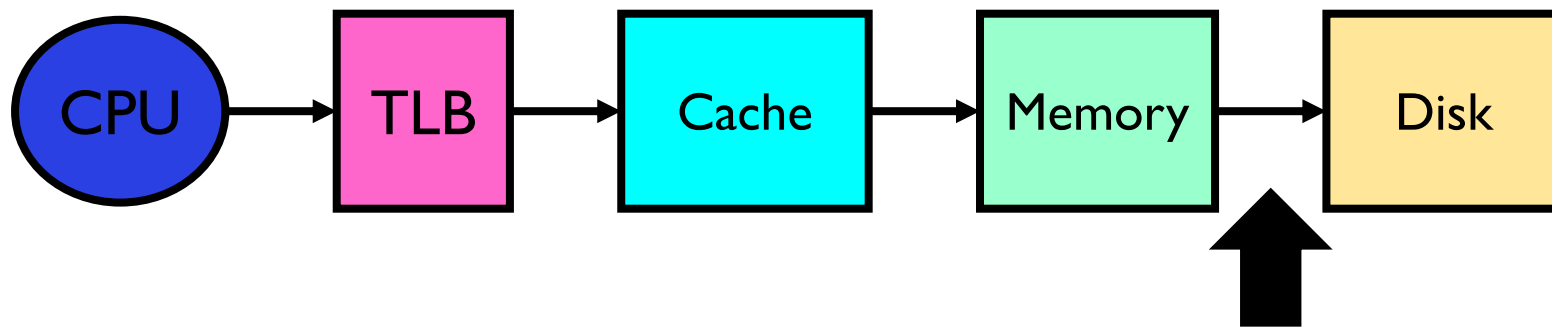
Lecture 9

Scheduling

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Recap: Cache Hierarchy

- Memory as cache for secondary disk



Recap: Demand Paging (需求分页)

- Modern programs require a lot of physical memory, but they don't use all their memory all of the time
 - 90-10 rule: programs spend 90% of their time in 10% of their code
 - Wasteful to require all of user's code to be in memory
- Solution: use main memory as cache for disk
 - “lazy” memory allocation
- An illusion of infinite memory
 - In-use virtual memory can be bigger than physical memory
 - Combined memory of running processes much larger than physical memory
 - ❑ More programs fit into memory, allowing more concurrency
 - Principle: page table for transparent management

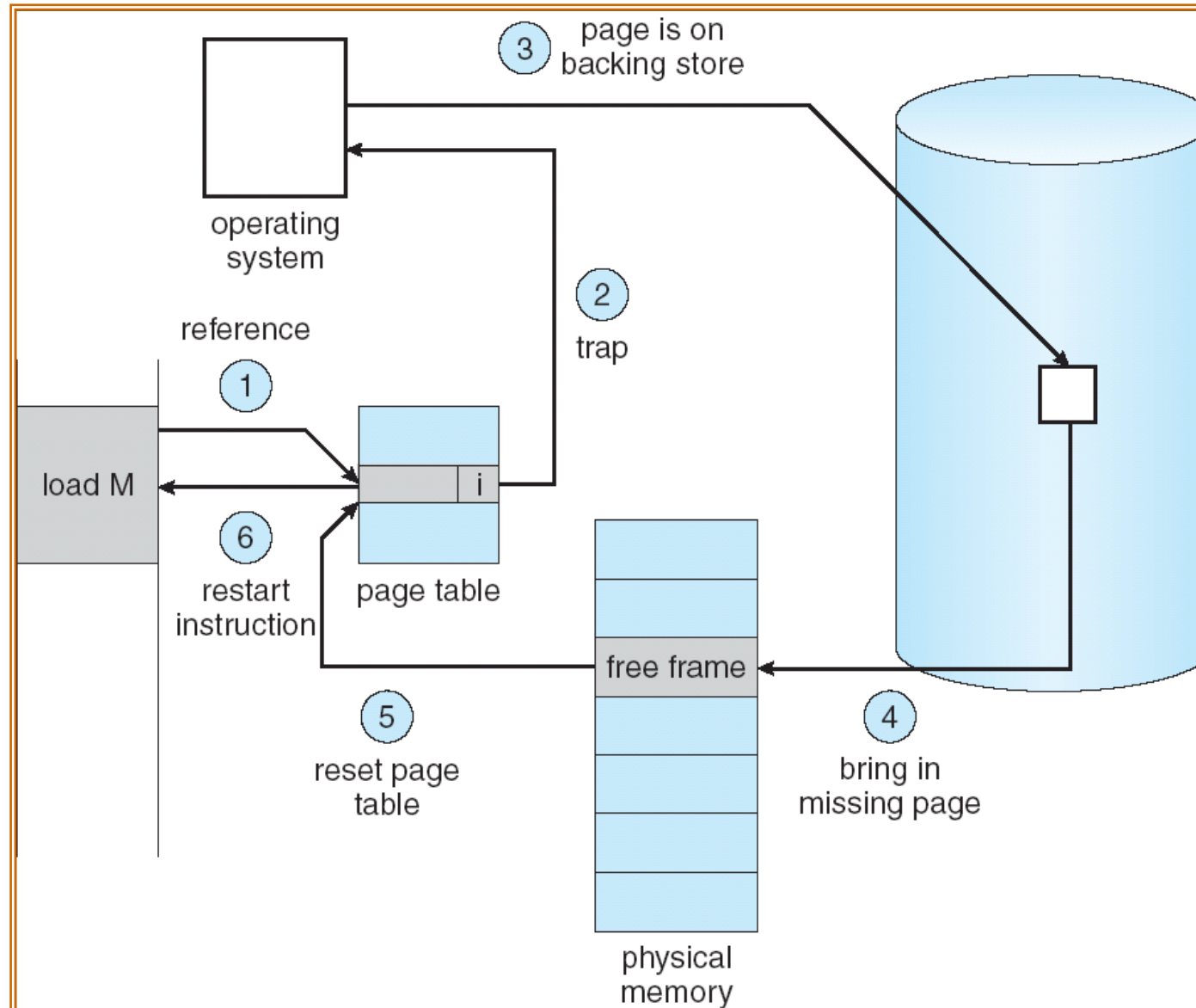
Recap: Demand Paging as Cache

- What is block size?
 - 1 page
- What is organization of this cache (i.e. direct-mapped, set-associative, fully-associative)?
 - Fully associative: arbitrary virtual \rightarrow physical mapping
- How do we find a page in the cache when look for it?
 - First check TLB, then page-table traversal
- What is page replacement policy? (i.e. LRU, Random...)
 - This requires more explanation... (kinda LRU)
- What happens on a miss?
 - Go to lower level to fill miss (i.e. disk)
- What happens on a write? (write-through, write back)
 - Write-back – need dirty bit!

Recap: Implementation of mmap

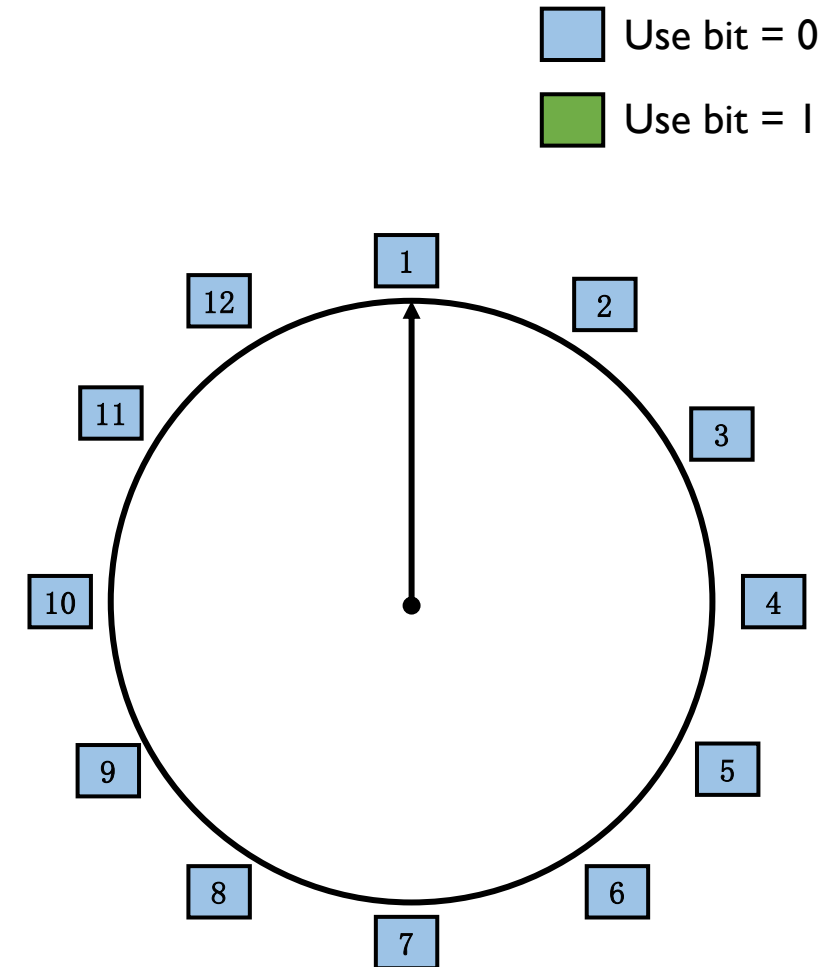
- When program accesses an invalid address
 1. [MMU] TLB miss; full page table lookup
 2. [MMU + OS] Trapping into page fault handler
 3. [OS] Convert virtual address to file offset
 4. [OS] Allocate a new page frame in memory
 5. [OS] Read data from disk to the memory (blocked)
 6. [CPU] Disk interrupt when read completes
 7. [OS] Updating page table by marking the entry as valid
 8. [OS] Resume process
 9. [MMU] TLB miss; full page table lookup
 10. [MMU] TLB update

Recap: Implementation of mmap



Recap: Page Eviction Policy

- **Clocking algorithm**: approximating LRU
- Implementation with the use bit
 - Initialized to 0 in page table
 - Set to 1 whenever there is a page access
- When we need to evict a page, we look at the page under the hand:
 - If its use bit = 1, clear it and move the hand, repeat;
 - If its use bit = 0, evict it



Page reference stream:

Recap: N^{th} Chance Version of Clock Algorithm

- N^{th} chance algorithm: Give page N chances
 - OS keeps counter per page: # sweeps
 - On page fault, OS checks use bit:
 - ❑ 1 \rightarrow clear use and also clear counter (used in last sweep)
 - ❑ 0 \rightarrow increment counter; if count= N , replace page
 - Means that clock hand has to sweep by N times without page being used before page is replaced
- How do we pick N ?
 - Why pick large N ? Better approximation to LRU
 - ❑ If $N \sim 1K$, really good approximation
 - Why pick small N ? More efficient
 - ❑ Otherwise might have to look a long way to find free page
- What about dirty pages?
 - Takes extra overhead to replace a dirty page, so give dirty pages an extra chance before replacing?
 - Common approach:
 - ❑ Clean pages, use $N=1$
 - ❑ Dirty pages, use $N=2$ (and write back to disk when $N=1$)

Recap: Details of Clock Algorithms

- Which bits of a PTE entry are useful to us?
 - **Use**: Set when page is referenced; cleared by clock algorithm
 - **Modified**: set when page is modified, cleared when page written to disk
 - **Valid**: ok for program to reference this page
 - **Read-only**: ok for program to read page, but not modify
 - ☐ For example for catching modifications to code pages!
- Do we really need hardware-supported “modified” bit?
 - No. Can emulate it (BSD Unix) using read-only bit
 - ☐ Initially, mark all pages as read-only, even data pages
 - ☐ On write, trap to OS. OS sets software “modified” bit, and marks page as read-write.
 - ☐ Whenever page comes back in from disk, mark read-only

Scheduling (调度) Concept

- Why we need scheduling? Multitasks and Concurrency.
- Scheduling is only useful when there is not enough resources
- Preemption (抢占) is the basic assumption for fine-grained scheduling
 - Either by timer interrupts or other kinds of interrupts
- Who schedules processes/threads?
 - Mostly by OS.
 - User-level thread libraries schedule the threads by themselves.

Scheduling Policy Goals (1/3)

- Minimize Response Time
 - Minimize elapsed time to do an operation (or job)
 - Response time is what the user sees:
 - ☐ Time to echo a keystroke in editor
 - ☐ Time to compile a program
 - ☐ Real-time tasks: Must meet deadlines imposed by World

Scheduling Policy Goals (2/3)

- Minimize Response Time
- Maximize Throughput
 - Maximize operations (or jobs) per second
 - Throughput related to response time, but not identical:
 - ☐ Minimizing response time will lead to more context switching than if you only maximized throughput
 - Two parts to maximizing throughput
 - ☐ Minimize overhead (for example, context-switching)
 - ☐ Efficient use of resources (CPU, disk, memory, etc)

Scheduling Policy Goals (3/3)

- Minimize Response Time
- Maximize Throughput
- Fairness
 - Share CPU among users in some equitable way
 - Fairness is not minimizing average response time:
 - ❑ Better *average* response time by making system *less* fair

First-Come, First-Served (FCFS) Scheduling

- First-Come, First-Served (FCFS, 先到先服务)
 - Also “First In, First Out” (FIFO, 先进先出) or “Run until done”
 - ❑ In early systems, FCFS meant one program scheduled until done
 - ❑ Now, means keep CPU until thread blocks

- Example:

<u>Process</u>	<u>Burst Time</u>
P_1	24
P_2	3
P_3	3

- Suppose processes arrive in the order: P_1, P_2, P_3
The Gantt Chart (甘特图) for the schedule is:



First-Come, First-Served (FCFS) Scheduling

- Example continued:



- Waiting time for $P_1 = 0$; $P_2 = 24$; $P_3 = 27$
- Average waiting time: $(0 + 24 + 27)/3 = 17$
- Average Completion time: $(24 + 27 + 30)/3 = 27$
- Convoy effect (护航效应): short process behind long process

First-Come, First-Served (FCFS) Scheduling

- Example continued:
 - Suppose that processes arrive in order: P_2, P_3, P_1 . Now, we have:



- Waiting time for $P_1 = 6; P_2 = 0; P_3 = 3$
 - Average waiting time: $(6 + 0 + 3)/3 = 3$
 - Average Completion time: $(3 + 6 + 30)/3 = 13$
- In second case:
 - Average waiting time is much better (before it was 17)
 - Average completion time is better (before it was 27)
- FIFO Pros and Cons:
 - Simple (+)
 - Short jobs get stuck behind long ones (-)
 - ❑ Safeway: Getting milk, always stuck behind cart full of small items

Shortest Job First (SJF) Scheduling

- Shortest Job First (短任务优先) Scheduling
 - Always schedule the job with the shortest remaining time (so sometimes it's also called shortest-remaining-time-first, SRTF)
 - It theoretically minimizes the average response time, why?



Shortest Job First (SJF) Scheduling

- Shortest Job First (短任务优先) Scheduling
 - Always schedule the job with the shortest remaining time (so sometimes it's also called shortest-remaining-time-first, SRTF)
 - It theoretically minimizes the average response time, why?
- Comparison of SRTF with FCFS
 - What if all jobs the same length?
 - ❑ SRTF becomes the same as FCFS (i.e. FCFS is best can do if all jobs the same length)
 - What if jobs have varying length?
 - ❑ SRTF: short jobs not stuck behind long ones

Shortest Job First (SJF) Scheduling

- Shortest Job First (短任务优先) Scheduling
 - Always schedule the job with the shortest remaining time (so sometimes it's also called shortest-remaining-time-first, SRTF)
 - It theoretically minimizes the average response time, why?
- Con#1: starvation (饥饿)
 - If small jobs keep coming, the long jobs will not be served
 - Fairness issue
- Con#2: implementation
 - It's hard to know the task remaining time

Round Robin (RR) Scheduling

- Round Robin (轮询调度) Scheme
 - Each process gets a small unit of CPU time (*time quantum*), usually 10-100 milliseconds
 - After quantum expires, the process is preempted and added to the end of the ready queue.
- n processes in ready queue and time quantum is $q \Rightarrow$
 - ☐ Each process gets $1/n$ of the CPU time
 - ☐ In chunks of at most q time units
 - ☐ No process waits more than $(n-1)q$ time units

Round Robin (RR) Scheduling

- Example:

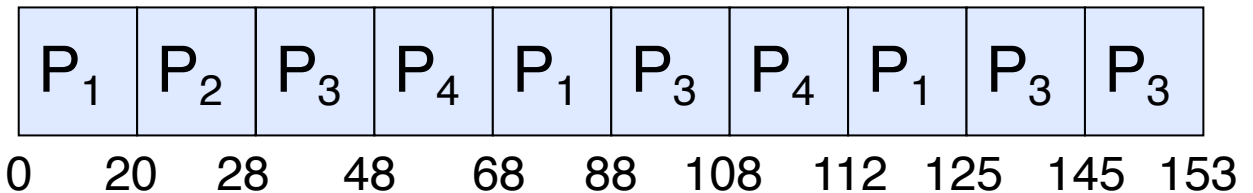
<u>Process</u>	<u>Burst Time</u>
P_1	53
P_2	8
P_3	68
P_4	24
- quantum=20
- Average waiting time?
- Average completion time?

Round Robin (RR) Scheduling

- Example:

<u>Process</u>	<u>Burst Time</u>
P_1	53
P_2	8
P_3	68
P_4	24

- The Gantt chart (quantum=20) is:



- Waiting time for
 - $P_1 = (68 - 20) + (112 - 88) = 72$
 - $P_2 = (20 - 0) = 20$
 - $P_3 = (28 - 0) + (88 - 48) + (125 - 108) = 85$
 - $P_4 = (48 - 0) + (108 - 68) = 88$
- Average waiting time = $(72 + 20 + 85 + 88) / 4 = 66\frac{1}{4}$
- Average completion time = $(125 + 28 + 153 + 112) / 4 = 104\frac{1}{2}$

Round Robin (RR) Scheduling

- Thus, Round-Robin Pros and Cons:
 - Better for short jobs, Fair (+)
 - Context-switching time adds up for long jobs (-)

Round Robin (RR) Scheduling

- Thus, Round-Robin Pros and Cons:
 - Better for short jobs, Fair (+)
 - Context-switching time adds up for long jobs (-)
- How do you choose time slice?
 - Too large: Response time suffers
 - What if infinite (∞)? Falls back to FIFO
 - Too small: Throughput suffers

Round Robin (RR) Scheduling

- Thus, Round-Robin Pros and Cons:
 - Better for short jobs, Fair (+)
 - Context-switching time adds up for long jobs (-)
- How do you choose time slice?
- Actual choices of timeslice:
 - Initially, UNIX timeslice one second:
 - ☐ Worked ok when UNIX was used by one or two people.
 - ☐ What if three compilations going on? 3 seconds to echo each keystroke!
 - Need to balance short-job performance and long-job throughput:
 - ☐ Typical time slice today is between 10ms – 100ms
 - ☐ Typical context-switching overhead is 0.1ms – 1ms
 - ☐ Roughly 1% overhead due to context-switching

Comparing FCFS and RR

- Assuming zero-cost context-switching time, is RR always better than FCFS?

- Simple example:

10 jobs, each take 100s of CPU time
RR scheduler quantum of 1s
All jobs start at the same time

- Completion Times:

Job #	FIFO	RR
1	100	991
2	200	992
...
9	900	999
10	1000	1000

- Average response time

❑ Bad when all jobs same length

- Also: Cache state must be shared between all jobs with RR but can be devoted to each job with FIFO

- Total time for RR longer even for zero-cost switch!

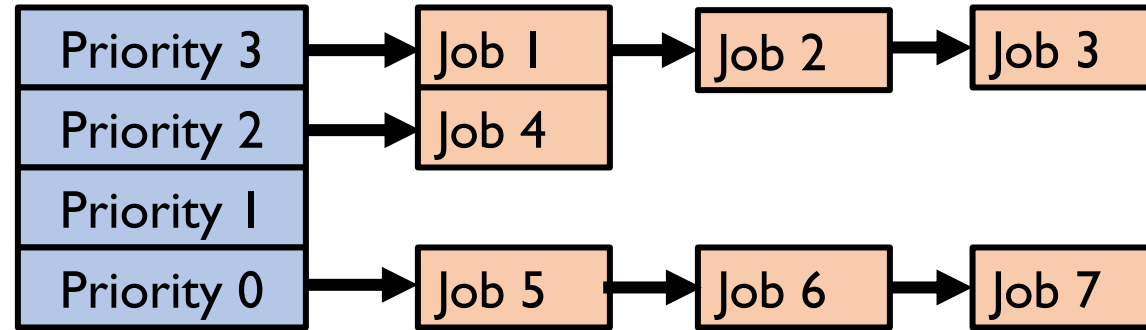
Choice of Time Quantum for RR

Best FCFS:

P ₂ [8]	P ₄ [24]	P ₁ [53]	P ₃ [68]
0	8	32	85
			153

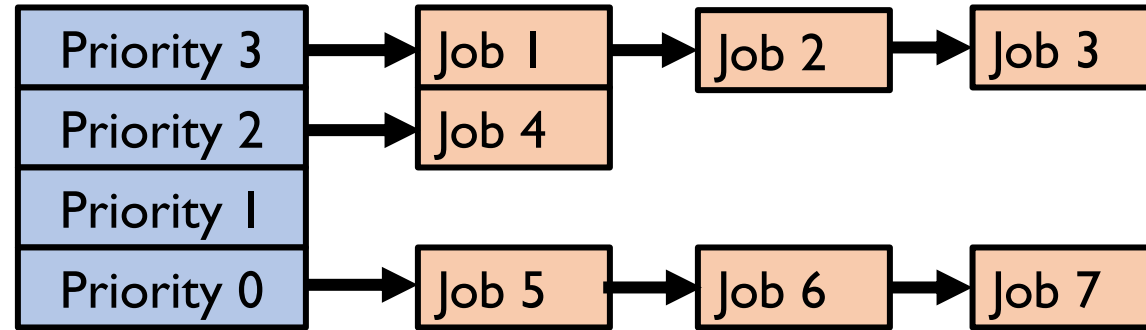
	Quantum	P ₁	P ₂	P ₃	P ₄	Average
Wait Time	Best FCFS	32	0	85	8	31¼
	Q = 1	84	22	85	57	62
	Q = 5	82	20	85	58	61¼
	Q = 8	80	8	85	56	57¼
	Q = 10	82	10	85	68	61¼
	Q = 20	72	20	85	88	66¼
	Worst FCFS	68	145	0	121	83½
Completion Time	Best FCFS	85	8	153	32	69½
	Q = 1	137	30	153	81	100½
	Q = 5	135	28	153	82	99½
	Q = 8	133	16	153	80	95½
	Q = 10	135	18	153	92	99½
	Q = 20	125	28	153	112	104½
	Worst FCFS	121	153	68	145	121¾

Strict Priority Scheduling



- Strict Priority Scheduling (严格优先级调度)
 - Always execute highest-priority runnable jobs to completion
 - Each queue can be processed in RR with some time-quantum
- Problems:
 - Starvation: Lower priority jobs don't get to run because higher priority jobs
 - Deadlock: Priority Inversion (优先级翻转)
 - ❑ Not strictly a problem with priority scheduling, but happens when low priority task has lock needed by high-priority task

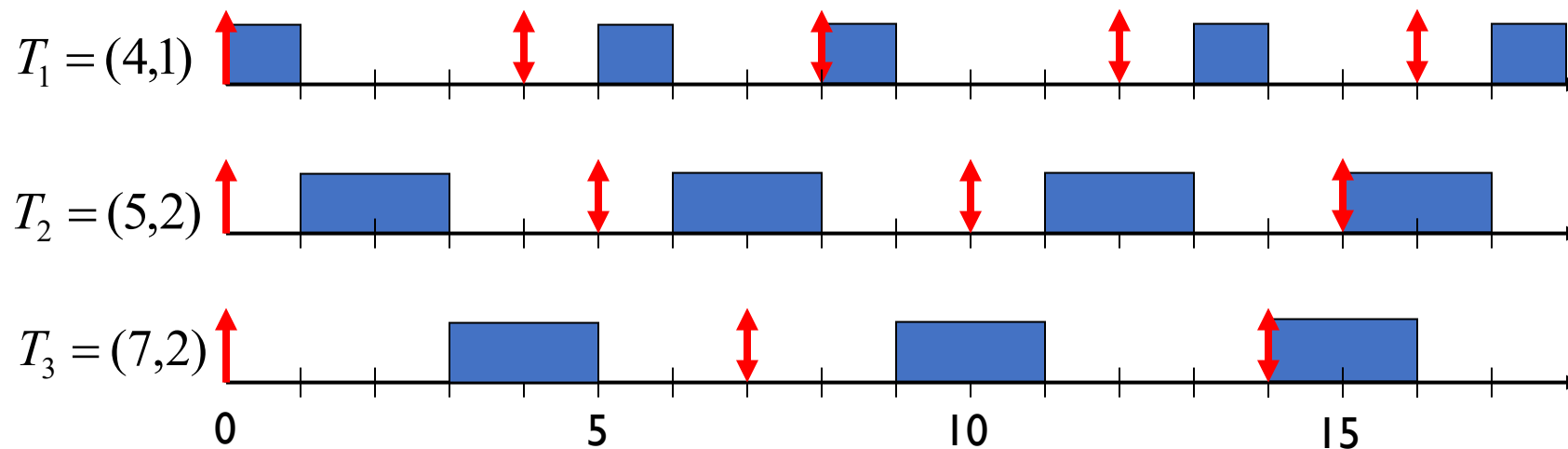
Strict Priority Scheduling



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 - Always execute highest-priority runnable jobs to completion
 - Each queue can be processed in RR with some time-quantum
- Problems:
 - Starvation: Lower priority jobs don't get to run because higher priority jobs
 - Deadlock: Priority Inversion (优先级翻转)
- How to fix? Dynamic priority
 - Dynamic priorities – adjust base-level priority up or down based on heuristics about interactivity, locking, burst behavior, etc...

Earliest Deadline First (EDF)

- Tasks periodic with period P and computation C in each period: (P, C)
- Preemptive priority-based dynamic scheduling
- Each task is assigned a (current) priority based on how close the absolute deadline is
- The scheduler always schedules the active task with the closest absolute deadline



Scheduling Fairness

- What about fairness?
 - Strict fixed-priority scheduling between queues is unfair (run highest, then next, etc):
 - ❑ Long running jobs may never get CPU
 - ❑ In Multics, shut down machine, found 10-year-old job
 - Must give long-running jobs a fraction of the CPU even when there are shorter jobs to run
 - Tradeoff: fairness gained by hurting avg response time!

Scheduling Fairness

- How to implement fairness?
 - Could give each queue some fraction of the CPU
 - ☐ What if one long-running job and 100 short-running ones?
 - ☐ Like express lanes in a supermarket—sometimes express lanes get so long, get better service by going into one of the other lines
 - Could increase priority of jobs that don't get service
 - ☐ What is done in some variants of UNIX
 - ☐ This is ad hoc—what rate should you increase priorities?
 - ☐ And, as system gets overloaded, no job gets CPU time, so everyone increases in priority \Rightarrow Interactive jobs suffer

Scheduling Fairness

- If every tasks need the same resource, fairness is easy: RR.
- Yet, tasks may demand different: compute-bound vs. I/O bound
- Max-Min fairness: iteratively maximize the minimum allocation given to a particular process (or threads/users/applications) until all resources are assigned
 - Mostly used in network

Multi-level Feedback Queue (MFQ) Scheduling

- Multi-level Feedback Queue (MFQ, 多级反馈队列调度)
 - Achieves responsiveness (short jobs quickly as SJF), low overhead (minimizing the preemptions and scheduling decision time), and starvation-free (as RR), and fairness (approximately max-min fair share).
 - Yet, it does not perfectly achieve any of these goals.
 - Widely used in commercial OSes such as Windows, MacOS, and Linux.
- Assuming a mix of two kinds of workloads
 - ① **Interactive tasks** (e.g., waiting for user keyboard input): using CPU for a short time, then yield for I/O waiting. Low latency is critical.
 - ② **CPU-intensive tasks** (e.g., compressing files): using CPU for a long period of time. The response time often does not matter much.

Multi-level Feedback Queue (MFQ) Scheduling

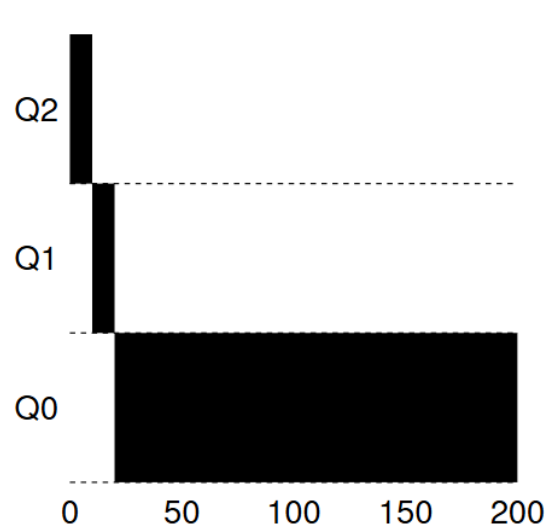
- A naïve version of MFQ: maintaining many tasks queues with different priorities, and use following schedule rules.
 - Rule 1: If $\text{Priority}(A) > \text{Priority}(B)$, A runs (B doesn't).
 - Rule 2: If $\text{Priority}(A) = \text{Priority}(B)$, A & B run in RR.
- The key here is how to set the priority.
 - Intuitively, if a job repeatedly relinquishes the CPU while waiting for input from the keyboard, it shall be kept in high priority.
 - Otherwise, if a job uses CPU intensively for long periods of time, its priority shall be reduced.

Multi-level Feedback Queue (MFQ) Scheduling

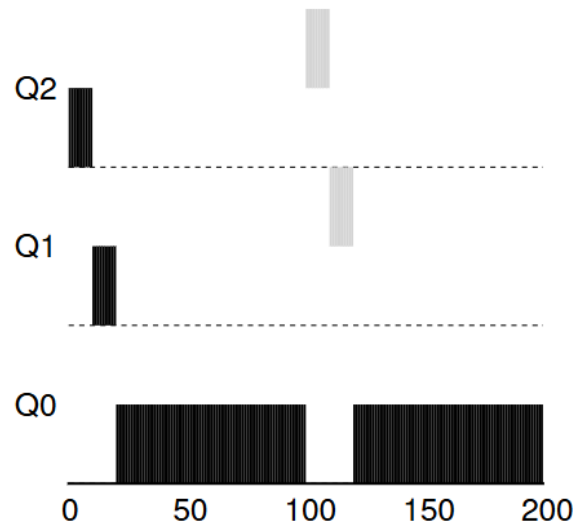
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 - Rule 1: If $\text{Priority}(A) > \text{Priority}(B)$, A runs (B doesn't).
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- Our solution: assign a quota for each job at a given priority level, and reduces its priority once the quota is used up.
 - Rule 3: When a job enters the system, it is placed at the highest priority (the topmost queue).
 - Rule 4a: If a job uses up its allotment while running, its priority is reduced (i.e., it moves down one queue).
 - Rule 4b: If a job gives up the CPU (for example, by performing an I/O operation) before the allotment is up, it stays at the same priority level (i.e., its allotment is reset).

Multi-level Feedback Queue (MFQ) Scheduling

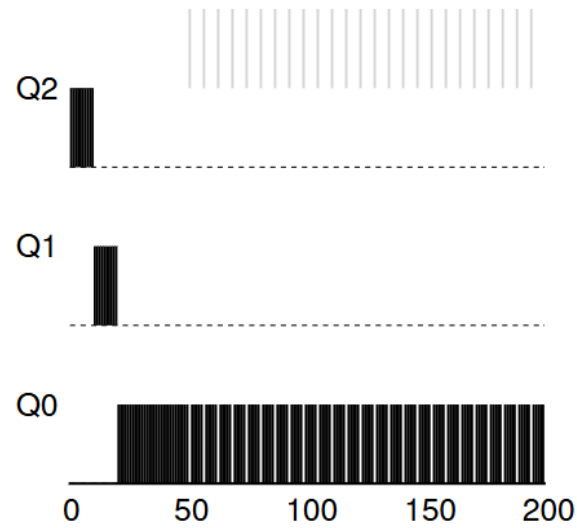
- A few illustrative examples of our naïve MFQ design.



(a) A single long-running job



(b) A single long-running job and a short-running job



(c) A single long-running job and an interactive job that only uses CPU for 1ms per time then waits for I/O

Multi-level Feedback Queue (MFQ) Scheduling

- There are many issues with this naïve version of MFQ.
 - Starvation: if there are “too many” interactive jobs in the system, they will consume all CPU time, and thus long-running jobs will starve.

Multi-level Feedback Queue (MFQ) Scheduling

- There are many issues with this naïve version of MFQ.
 - Starvation: if there are “too many” interactive jobs in the system, they will consume all CPU time, and thus long-running jobs will starve.
- Solution# 1: priority boost
 - Rule 5: After some time period S , move all the jobs in the system to the topmost queue.

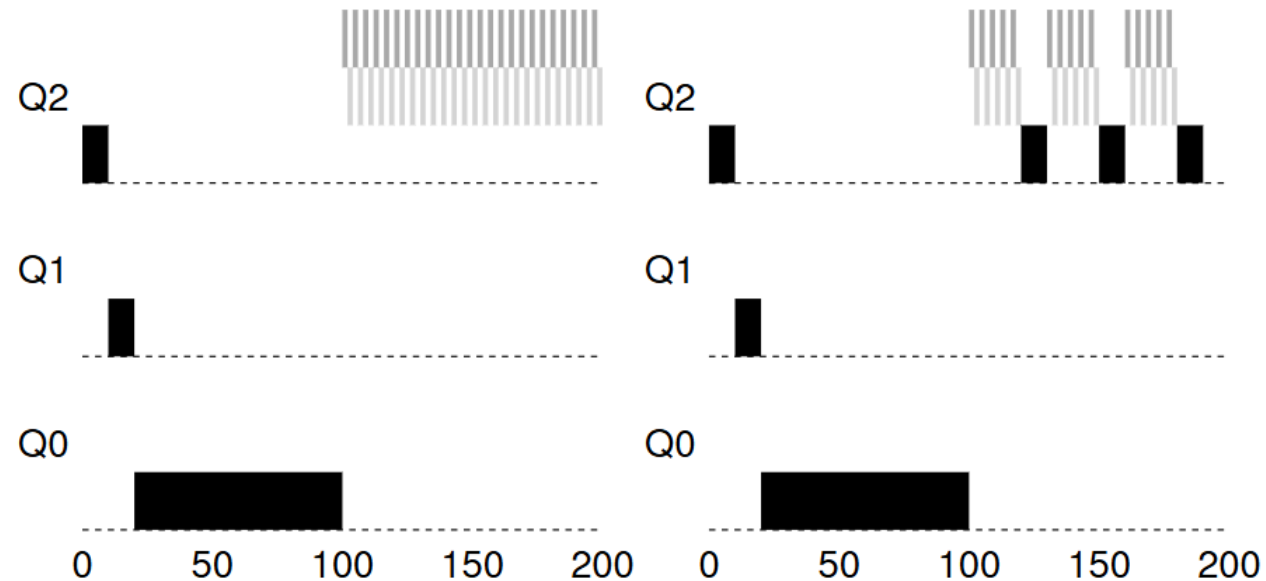


Figure 8.4: Without (Left) and With (Right) Priority Boost

Multi-level Feedback Queue (MFQ) Scheduling

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 - S shall be neither too large or too small. Why?

Multi-level Feedback Queue (MFQ) Scheduling

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- Solution#1: priority boost
 - Rule 5: After some time period S , move all the jobs in the system to the topmost queue.
 - S shall be neither too large or too small. Why?
- Solution#2: time slice across queues
 - each queue gets a certain amount of CPU time
 - e.g., 70% to highest, 20% next, 10% lowest
- More solutions..

Multi-level Feedback Queue (MFQ) Scheduling

- There are many issues with this naïve version of MFQ.
 - Starvation: if there are “too many” interactive jobs in the system, they will consume all CPU time, and thus long-running jobs will starve.
 - Countermeasure: user action that can foil intent of OS designers, e.g., put in a bunch of meaningless I/O to keep job’s priority high.
 - How to parameterize the scheduler: how many queues should there be? How big should the time slice be per queue?
 - More..
- Think of possible solutions to them?

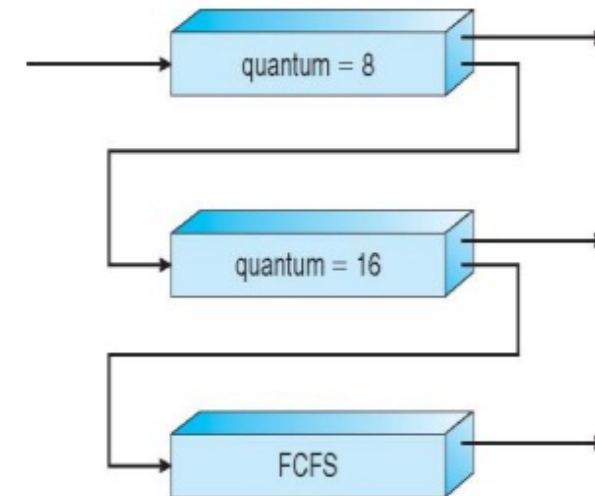
Multi-level Feedback Queue (MFQ) Scheduling

- To further extend the MFQ design: Each queue has its own scheduling parameters or even different algorithms!
 - ❑ e.g. foreground – RR, background – FCFS
 - ❑ Sometimes multiple RR priorities with quantum increasing exponentially (highest: 1ms, next: 2ms, next: 4ms, etc)
- Adjust each job's priority as follows (details vary)
 - Job starts in highest priority queue
 - If timeout expires, drop one level
 - If timeout doesn't expire, push up one level (or stay at the same one)

Multi-level Feedback Queue (MFQ) Scheduling

- A test
 - Assume we have 4 processes in a system with multilevel feedback queue scheduling policy. All the processes arrived at time 0 and located in the highest level queue in the order of their IDs (1 to 4) a) Calculate the average waiting time and average turnaround time.

<u>Process</u>	<u>Burst Time</u>
P_1	11
P_2	26
P_3	31
P_4	45



b) If a new process P_5 enters the system at time 35 how the gantt chart is going to change?

Fair-share Scheduler

- This type of scheduler aims to guarantee that each job obtain a certain percentage of CPU time.
 - Also known as “proportional-share scheduler.
- Next, we will discuss two types of fair-share scheduler.
 - Lottery scheduling
 - The Linux Completely Fair Scheduler (CFS)

Lottery Scheduling

- Lottery Scheduling
 - Give each job some number of lottery tickets
 - On each time slice, randomly pick a winning ticket
 - On average, CPU time is proportional to number of tickets given to each job (but **not deterministically!**)
- Assuming there are two jobs: A with 75 tickets, B with 25 tickets
 - Here, B gets run 4 out of 20 time slices (20%).
 - With more tries, B is more likely to get 25% slices.

Here is an example output of a lottery scheduler's winning tickets:

63 85 70 39 76 17 29 41 36 39 10 99 68 83 63 62 43 0 49 12

Here is the resulting schedule:

A		A	A		A	A	A	A	A		A		A	A	A	A	A	A
	B			B						B			B					

Lottery Scheduling

- Lottery Scheduling
 - Give each job some number of lottery tickets
 - On each time slice, randomly pick a winning ticket
 - On average, CPU time is proportional to number of tickets given to each job
- How to assign tickets?
 - To approximate SRTF, short running jobs get more, long running jobs get fewer
 - To avoid starvation, every job gets at least one ticket (everyone makes progress)
- Advantage over strict priority scheduling: behaves gracefully as load changes
 - Adding or deleting a job affects all jobs proportionally, independent of how many tickets each job possesses

Lottery Scheduling

- Lottery Scheduling Example
 - Assume short jobs get 10 tickets, long jobs get 1 ticket

# short jobs/ # long jobs	% of CPU each short jobs gets	% of CPU each long jobs gets
1/1	??	??
0/2	??	??
2/0	??	??
10/1	??	??
1/10	??	??

Lottery Scheduling

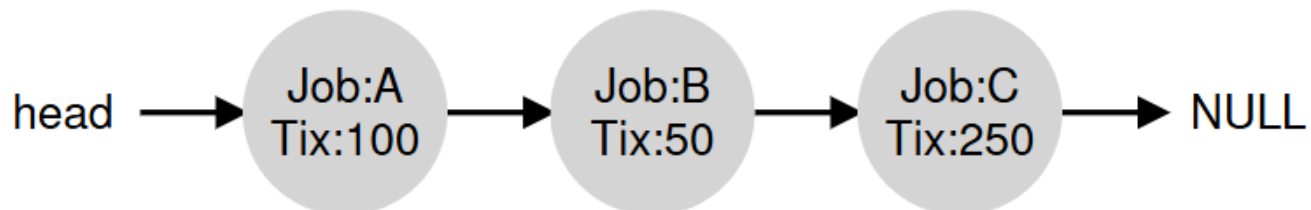
- Lottery Scheduling Example
 - Assume short jobs get 10 tickets, long jobs get 1 ticket

# short jobs/ # long jobs	% of CPU each short jobs gets	% of CPU each long jobs gets
1/1	91%	9%
0/2	N/A	50%
2/0	50%	N/A
10/1	9.9%	0.99%
1/10	50%	5%

Lottery Scheduling

- Implementing lottery scheduling is amazingly easy!
 - One of the important feature of it.
- You only need
 1. A good random number generator
 2. A data structure to track the processes of the system and the total number of tickets

Lottery Scheduling



```
1 // counter: used to track if we've found the winner yet
2 int counter = 0;
3
4 // winner: call some random number generator to
5 //           get a value >= 0 and <= (totaltickets - 1)
6 int winner = getrandom(0, totaltickets);
7
8 // current: use this to walk through the list of jobs
9 node_t *current = head;
10 while (current) {
11     counter = counter + current->tickets;
12     if (counter > winner)
13         break; // found the winner
14     current = current->next;
15 }
16 // 'current' is the winner: schedule it...
```

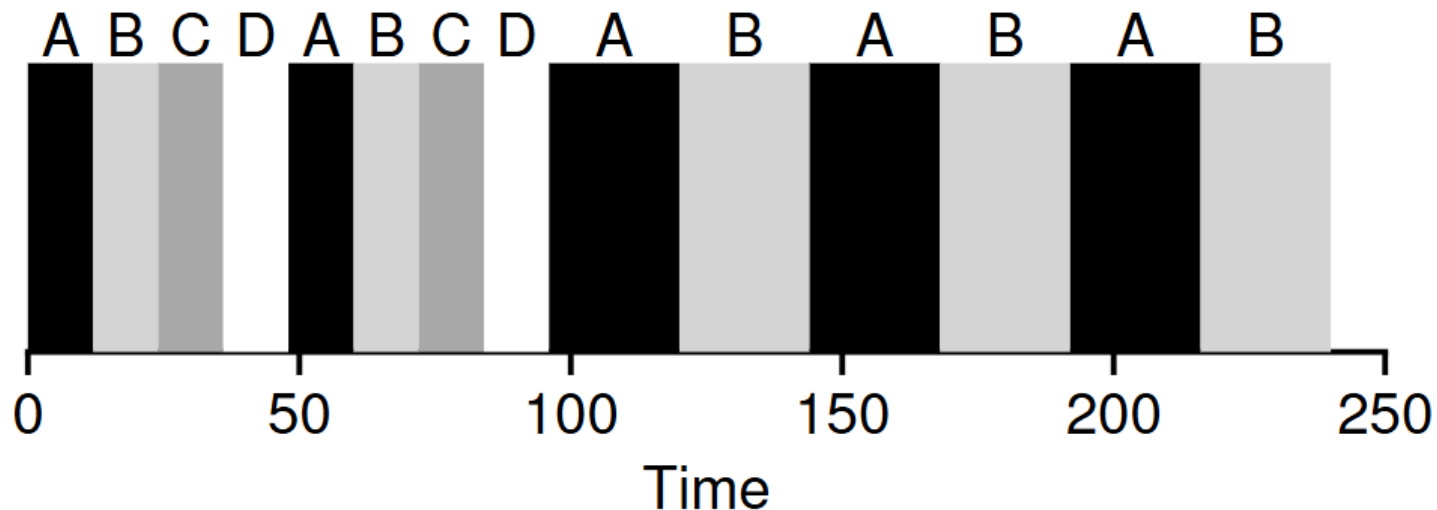
*An optimization:
organize the list
in sorted order*

Completely Fair Scheduler (CFS)

- The default Linux scheduler since v2.6.23 (2007).
 - The goal of **CFS**: to fairly divide a CPU evenly among all competing processes.
- CFS uses a counting-based technique known as **virtual runtime** (**vruntime**)
 - As each process runs, it accumulates **vruntime**, e.g., in proportion with the physical (real) time.
 - When a scheduling decision occurs, CFS will pick the process with the lowest **vruntime** to run next.
- How does **CFS** know when to stop the running process?
 - The scheduling time slice. Either too large or small. Why?

Completely Fair Scheduler (CFS)

- CFS decides the scheduling interval based on the number of currently running processes.
 - `sched_latency` divided by the number of processes
 - why?
 - E.g., 48 milliseconds / 4 processes = 12 milliseconds
 - What if there are too many processes? Set a minimal value of time slice: `min_granularity`.



Completely Fair Scheduler (CFS)

- CFS also enables controls over process priority, enabling users to give some processes a higher share of the CPU.
 - Using a UNIX mechanism known as the **nice** level of a process.
 - Larger **nice**, lower priority.

```
static const int prio_to_weight[40] = {  
    /* -20 */ 88761, 71755, 56483, 46273, 36291,  
    /* -15 */ 29154, 23254, 18705, 14949, 11916,  
    /* -10 */ 9548, 7620, 6100, 4904, 3906,  
    /* -5 */ 3121, 2501, 1991, 1586, 1277,  
    /* 0 */ 1024, 820, 655, 526, 423,  
    /* 5 */ 335, 272, 215, 172, 137,  
    /* 10 */ 110, 87, 70, 56, 45,  
    /* 15 */ 36, 29, 23, 18, 15,  
};
```

Two jobs: A with nice value of -5, B with nice value of 0. sched_latency is 48ms. What is the time slice of A and B?

$$\text{time_slice}_k = \frac{\text{weight}_k}{\sum_{i=0}^{n-1} \text{weight}_i} \cdot \text{sched_latency}$$

Completely Fair Scheduler (CFS)

$$vruntime_i = vruntime_i + \frac{weight_0}{weight_i} \cdot runtime_i$$

$weight_0$ is the weight of process with default priority (1024)

```
static const int prio_to_weight[40] = {  
    /* -20 */ 88761, 71755, 56483, 46273, 36291,  
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$$time_slice_k = \frac{weight_k}{\sum_{i=0}^{n-1} weight_i} \cdot sched_latency$$

Completely Fair Scheduler (CFS)

$$vruntime_i = vruntime_i + \frac{weight_0}{weight_i} \cdot runtime_i$$

$weight_0$ is the weight of process with default priority (1024)

How those “magic numbers are determined”?

```
static const int prio_to_weight[40] = {
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};
```

Think about 2 case:

- (1) A with nice value 0, B with nice value -5
 - (2) A with nice value 5, B with nice value 0
- Calculate how they will be scheduled

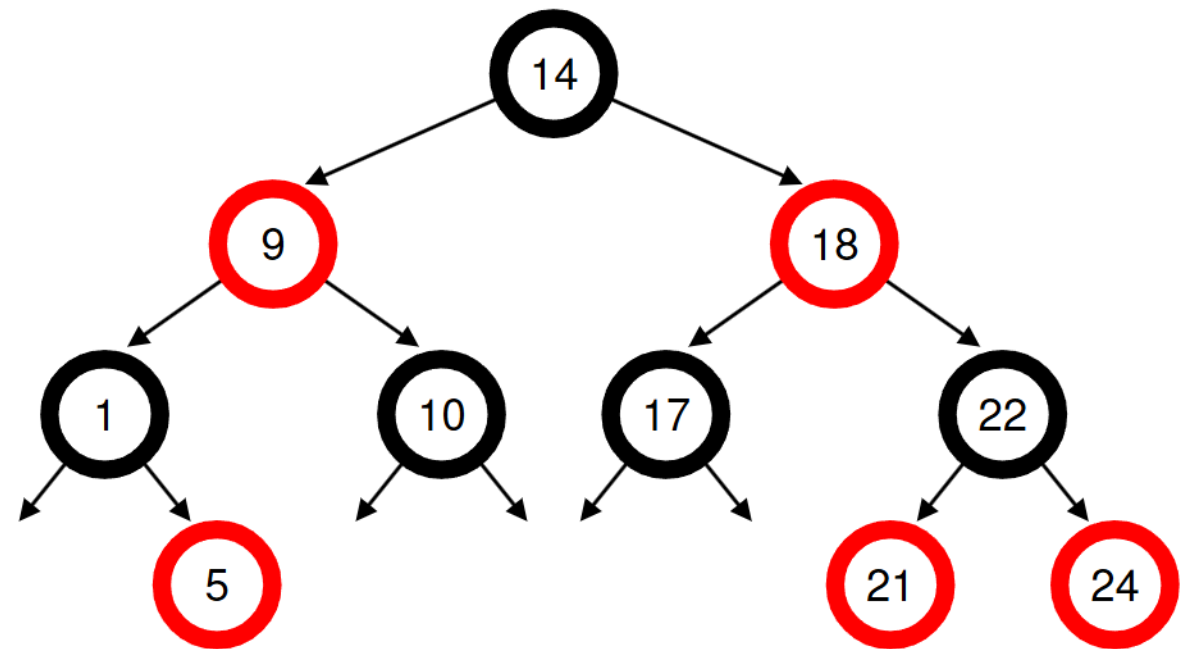
$$time_slice_k = \frac{weight_k}{\sum_{i=0}^{n-1} weight_i} \cdot sched_latency$$

Completely Fair Scheduler (CFS)

- Implementing CFS
 - The ops to be supported: (1) finding the process with lowest **vruntime**; (2) insert/delete a process
- Approach#1: Ordered List
 - Finding the next job: $O(1)$
 - Insert/delete: $O(n)$

Completely Fair Scheduler (CFS)

- Implementing CFS
 - The ops to be supported: (1) finding the process with lowest **vruntime**; (2) insert/delete a process
- Approach#1: Ordered List
 - Finding the next job: $O(1)$
 - Insert/delete: $O(n)$
- Approach#2: Red-Black Tree
 - Finding the next job: $O(\log n)$
 - Insert/delete: $O(\log n)$
 - ❑ A node is either red or black
 - ❑ The root is black
 - ❑ All leaves (NULL) are black
 - ❑ Both children of every red node are black
 - ❑ Every simple path from root to leaves contains the same number of black nodes.

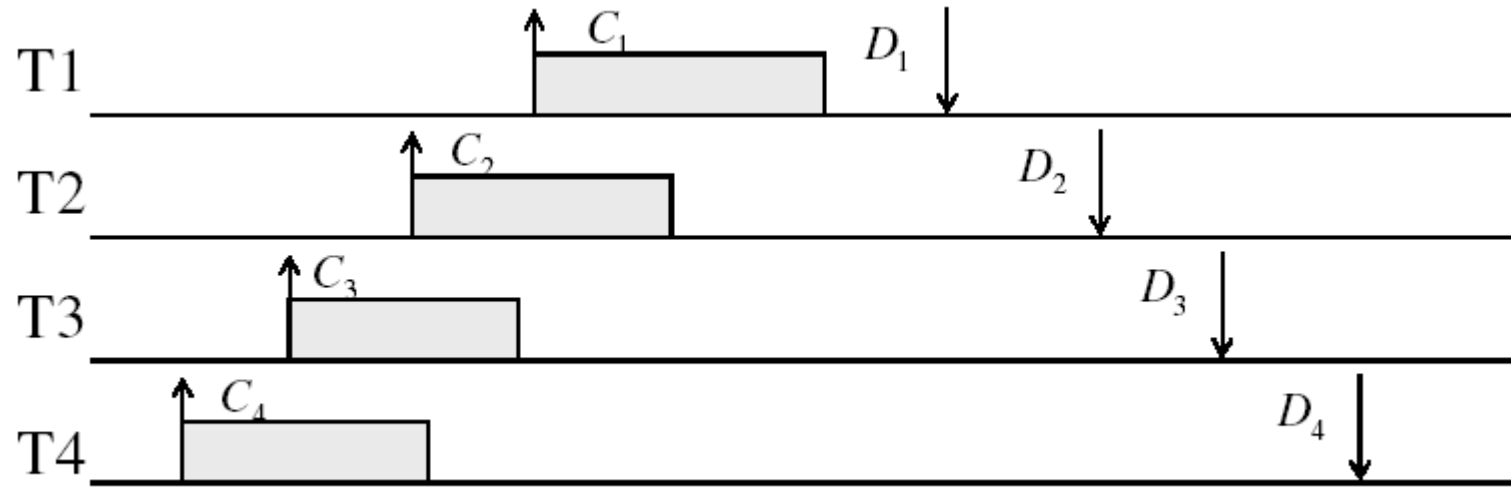


Real-Time Scheduling (RTS)

- Efficiency is important but **predictability** is essential:
 - We need to predict with confidence worst case response times for systems
 - In RTS, performance guarantees are:
 - Task- and/or class centric and often ensured a priori
 - In conventional systems, performance is:
 - System/throughput oriented with post-processing (... wait and see ...)
 - Real-time is about enforcing predictability, and does not equal fast computing!!!
- Hard Real-Time
 - *Attempt to meet all deadlines*
 - **EDF (Earliest Deadline First), LLF (Least Laxity First), RMS (Rate-Monotonic Scheduling), DM (Deadline Monotonic Scheduling)**
- Soft Real-Time
 - *Attempt to meet deadlines with high probability*
 - Minimize miss ratio / maximize completion ratio (firm real-time)
 - Important for multimedia applications
 - **CBS (Constant Bandwidth Server)**

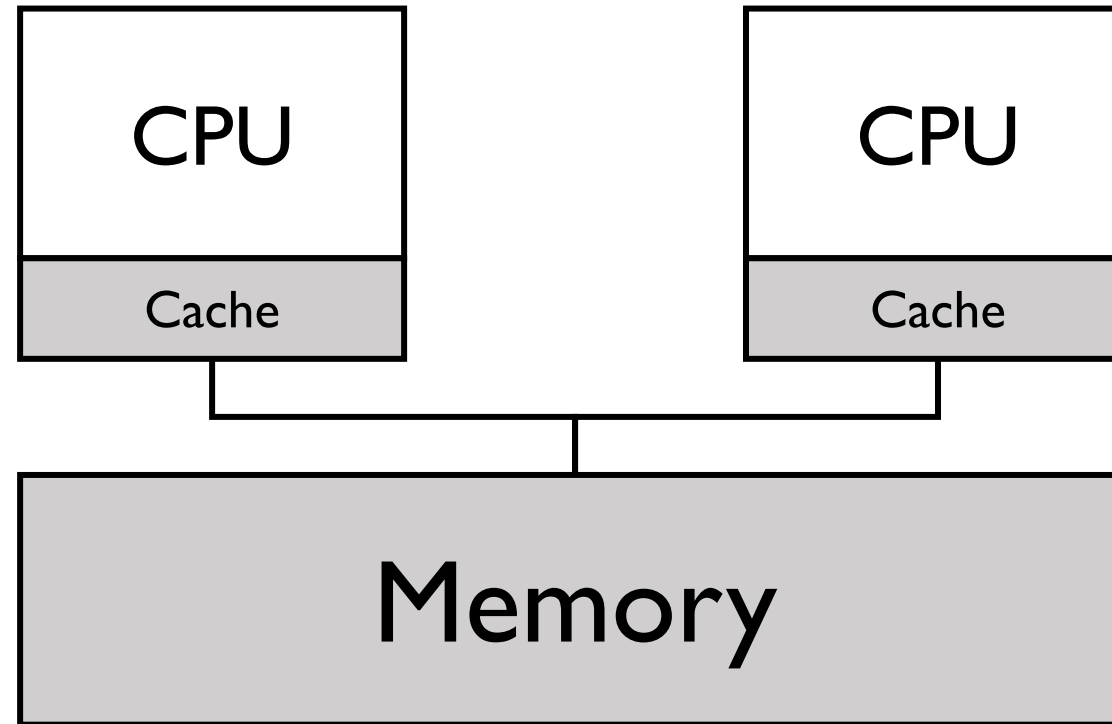
Real-Time Scheduling (RTS)

- Tasks are preemptable, independent with arbitrary arrival (=release) times
- Tasks have deadlines (D) and known computation times (C)
- Example Setup:



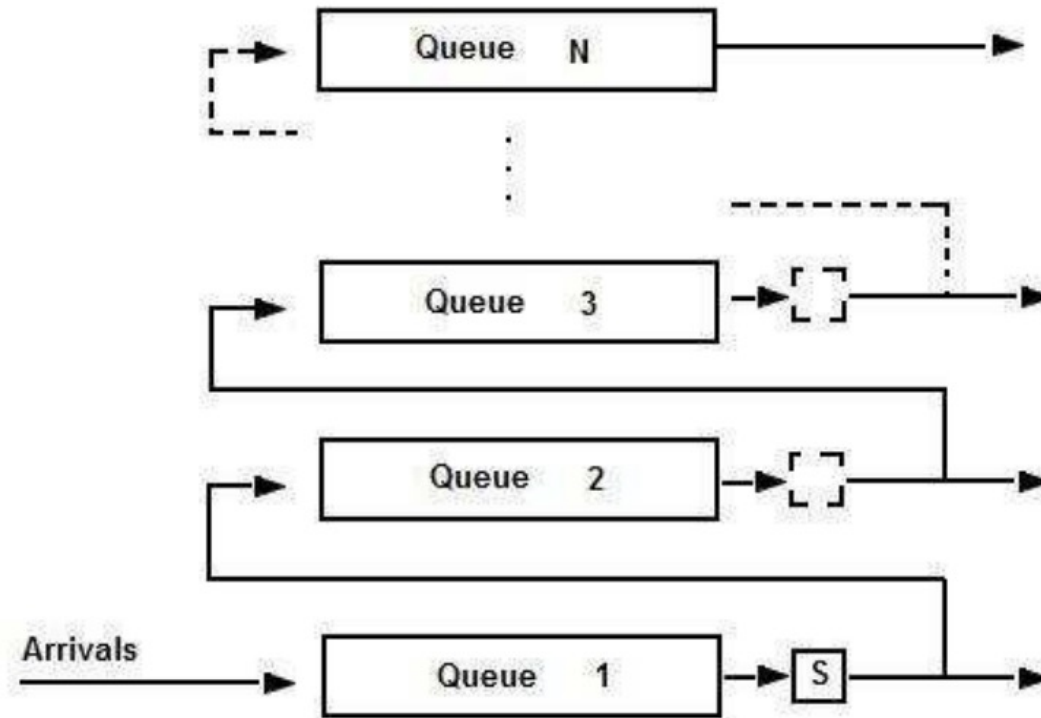
Scheduling on Multiprocessor

- Recall: the cache-memory system, and cache consistency (or coherency) (缓存一致性)



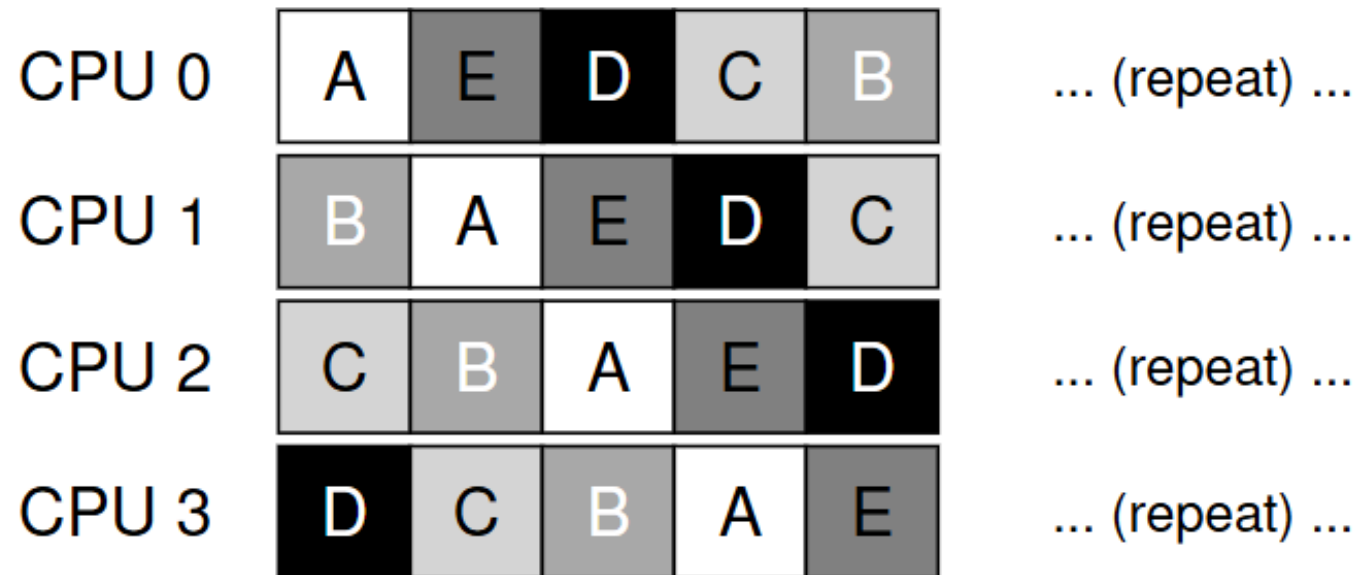
Scheduling on Multiprocessor

- What's wrong with a centralized MFQ?



Scheduling on Multiprocessor

- What's wrong with a centralized MFQ?
 - Contention for the MFQ lock
 - ❑ The lock could become a bottleneck especially with large number of processors
 - Cache coherence overhead
 - ❑ The MFQ data structure will be modified often and cause cache miss when a processor gets its lock to use MFQ



Assuming we have 5 jobs (A, B, C, D, E) running repeatedly in order on 4 CPUs.

Bad cache hit ratio!

Scheduling on Multiprocessor

- What's wrong with a centralized MFQ?
 - Contention for the MFQ lock
 - ❑ The lock could become a bottleneck especially with large number of processors
 - Cache coherence overhead
 - ❑ The MFQ data structure will be modified often and cause cache miss when a processor gets its lock to use MFQ
 - Limited cache reuse
 - ❑ A thread is likely to be scheduled on different processors, so the L1 cache needs to be fetched from the memory again

Scheduling on Multiprocessor

- What's wrong with a centralized MFQ?
 - Contention for the MFQ lock
 - Cache coherence overhead
 - Limited cache reuse
- Modern OSes use per-processor MFQ
- Affinity scheduling (亲和性调度): a thread is always (re)scheduled to the same processor
 - Rebalancing across processors only happens when necessary

How to Evaluate a Scheduling algorithm?

- Deterministic modeling
 - Takes a predetermined workload and compute the performance of each algorithm for that workload
- Queueing models (排队论/模型)
 - Mathematical approach for handling stochastic workloads
 - Commonly used in a variety of fields, including computer science, telecommunications, operations research, and industrial engineering
- Implementation/Simulation:
 - Build system which allows actual algorithms to be run against actual data – most flexible/general

Summary of Scheduling Algorithms

- Round-Robin Scheduling:
 - Give each thread a small amount of CPU time when it executes; cycle between all ready threads
 - Pros: Better for short jobs
- Shortest Job First (SJF) / Shortest Remaining Time First (SRTF):
 - Run whatever job has the least amount of computation to do/least remaining amount of computation to do
 - Pros: Optimal (average response time)
 - Cons: Hard to predict future, Unfair
- Multi-Level Feedback Scheduling:
 - Multiple queues of different priorities and scheduling algorithms
 - Automatic promotion/demotion of process priority in order to approximate SJF/SRTF

Summary of Scheduling Algorithms

- Lottery Scheduling:
 - Give each thread a priority-dependent number of tokens (short tasks \Rightarrow more tokens)
- Linux CFS
 - Completely fair across processes (always assign to the one with least running time)
 - Dynamically adjust time slice of each process
 - Using priority (nice level) to control the assignment
- Real-time scheduling
 - Need to meet a deadline, predictability essential
 - Earliest Deadline First (EDF) and Rate Monotonic (RM) scheduling

Summary of Scheduling Algorithms

- This course only covers very basic knowledge of scheduling
 - The schedulers used in real OSes are more complex
 - Choosing a proper schedule depends on many factors: hardware, workloads, etc..
 - Note: almost every hardware resource needs scheduler..
 - ☐ GPU, disk, network, etc..
 - Scheduling is common in real-world life
 - ☐ Use what you learned to solve them!
 - ☐ Example #1: Hospital emergencies?
 - ☐ Example #2: Air traffic control?
 - ☐ Example #3: Supermarket checkout?
 - ☐ Example #4: Print jobs in a printer?
 - ☐ Example #5: Control system in a rocket?
 - ☐ Example #6: Engine control unit in an automotive application

Homework

- Some simple code about MLFQ. Check out our website.