

(Hw01 Question-3) for Question 4 on book

Let $f(x) = -x^3 - \cos(x)$. With $p_0 = -1$ and $p_1 = 0$, find p_3 .

a. Use the Secant method.

$$\rightarrow p_n = p_{n-1} - f(p_{n-1}) \frac{(p_{n-1} - p_{n-2})}{f(p_{n-1}) - f(p_{n-2})}$$

$$\rightarrow p_2 = p_1 - f(p_1) \frac{(p_1 - p_0)}{f(p_1) - f(p_0)} = \frac{-f(0)}{f(0) - f(-1)} = -0.6851$$

$$\rightarrow p_3 = p_2 - f(p_2) \frac{(p_2 - p_1)}{f(p_2) - f(p_1)} = -0.6851 - \frac{f(-0.6851)(-0.6851 - 0)}{f(-0.6851) - f(0)} = -1.252$$

b. Use the method of False Position.

I did 'nt know how to solve this so I write a solution that I found on Internet. So it 's not my own

By using p_2 and p_0 in the secant method, we can solve it according to false Position. answer

$$\rightarrow p_3 = p_2 - \frac{f(p_2)(p_2 - p_0)}{f(p_2) - f(p_0)}$$

$$\rightarrow p_3 = \frac{1}{\cos(-1) - 2} - \frac{\frac{-1}{(\cos(-1) - 2)^3} - \cos(\frac{1}{\cos(-1) - 2})(\frac{1}{\cos(-1) - 2})}{\frac{-1}{(\cos(-1) - 2)^3} - \cos(\frac{-1}{(\cos(-1) - 2)^3}) + 1}$$

$$\rightarrow p_3 = -0.84136$$