

BSM307 İşaretler ve Sistemler

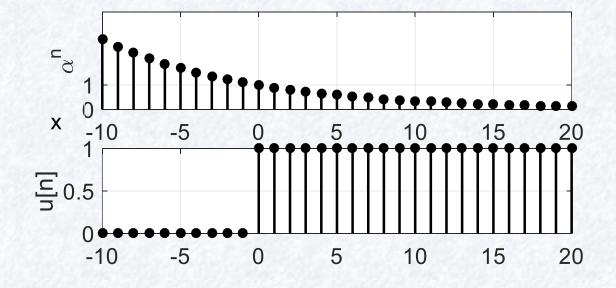
Dr. Seçkin Arı

Konvolüsyon

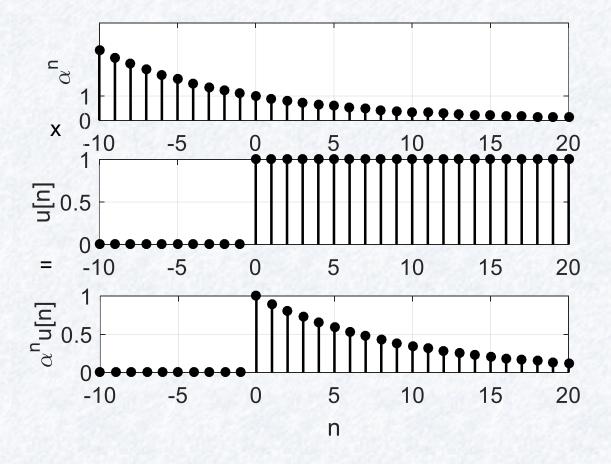
İçerik

- Temel Sistem Özellikleri
- Doğrusal Zamanla Değişmez Sistemler
- Birim Darbe Cevabi

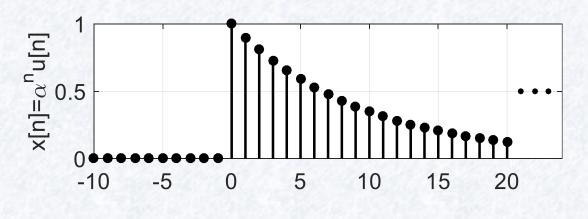
• $x[n] = \alpha^n u[n]$

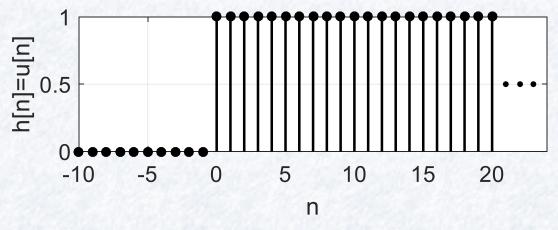


• $x[n] = \alpha^n u[n]$

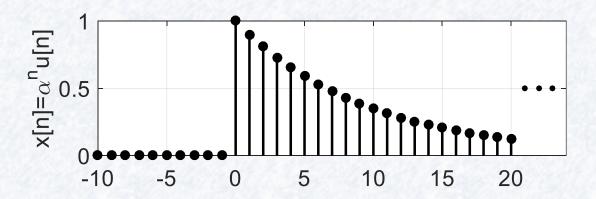


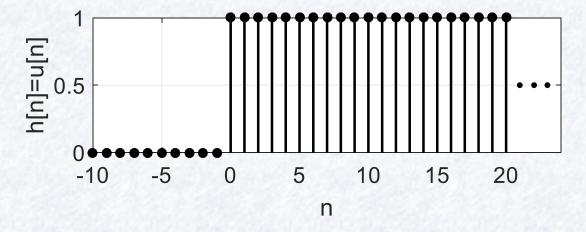
- $x[n] = \alpha^n u[n]$
- h[n] = u[n]
- y[n] = ?



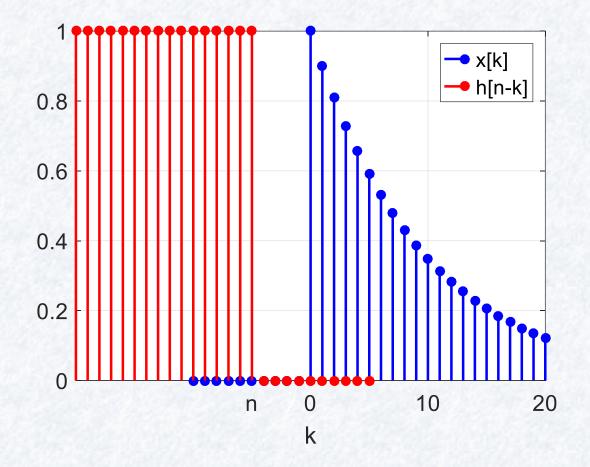


- $x[n] = \alpha^n u[n]$
- h[n] = u[n]
- y[n] = x[n] * h[n]

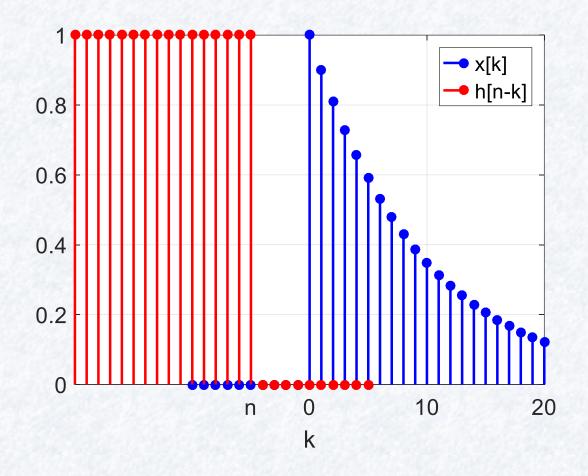




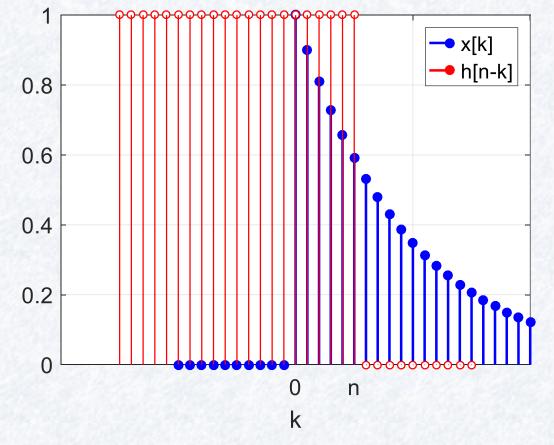
- $x[n] = \alpha^n u[n]$
- h[n] = u[n]
- y[n] = x[n] * h[n]
- n < 0 iken



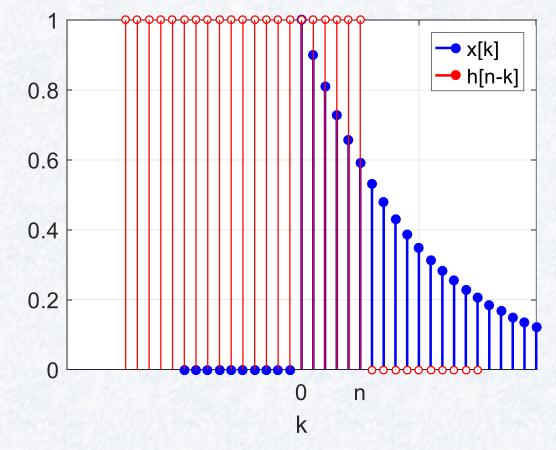
- $x[n] = \alpha^n u[n]$
- h[n] = u[n]
- y[n] = x[n] * h[n]
- n < 0 iken
 - ♦ Çakışma yok
- y[n] = 0



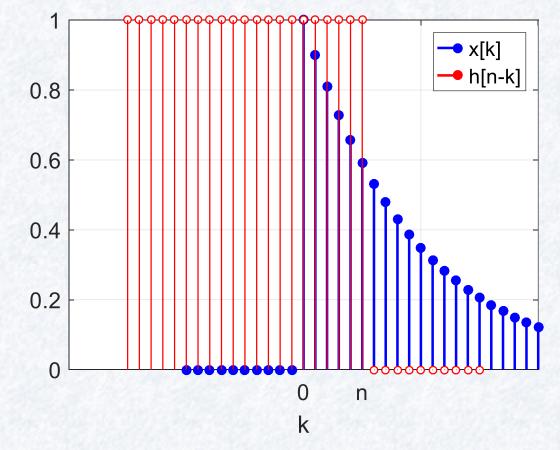
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- $n \ge 0$ iken



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- $n \ge 0$ iken
 - ♦ Çakışma 0-n arası
- $y[n] = \sum_{k=0}^{n} \alpha^k \cdot 1$
- y[n] =



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- $n \ge 0$ iken
 - ♦ Çakışma 0-n arası
- $y[n] = \sum_{k=0}^{n} \alpha^k \cdot 1$
- $\bullet \ y[n] = \frac{1 \alpha^{n+1}}{1 \alpha}$



- $x[n] = \alpha^n u[n]$
- h[n] = u[n]

- n < 0 iken y[n] = 0
- $n \ge 0$ iken $y[n] = \frac{1-\alpha^{n+1}}{1-\alpha}$

- $x[n] = \alpha^n u[n]$
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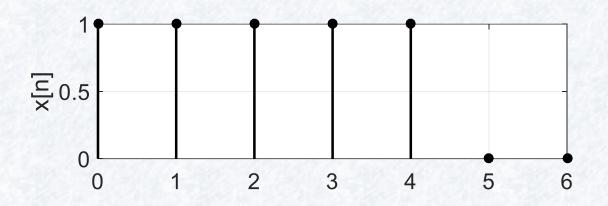
- n < 0 iken y[n] = 0
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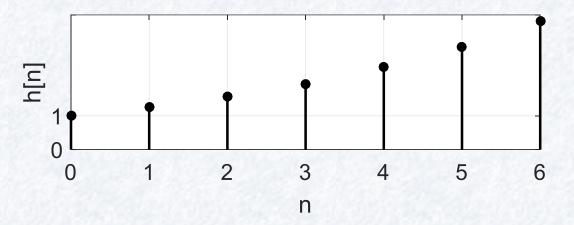
• $y[n] = \frac{1-\alpha^{n+1}}{1-\alpha}u[n]$

•
$$x[n] = \begin{cases} 1, & 0 \le n \le 4 \\ 0, & \text{diğer} \end{cases}$$

•
$$h[n] = \begin{cases} \alpha^n, & 0 \le n \le 6 \\ 0, & \text{diğer} \end{cases}$$

•
$$y[n] = ?$$



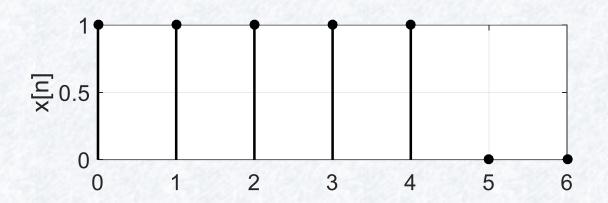


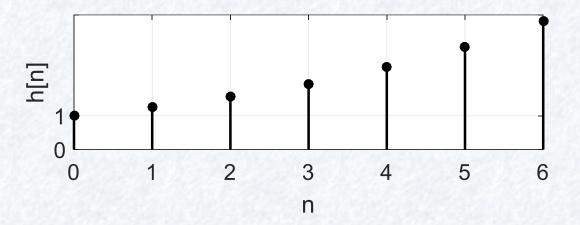
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•
$$y[n] = \sum_{k=-\infty}^{\infty} x[k]h[n-k]$$

• n < 0 iken



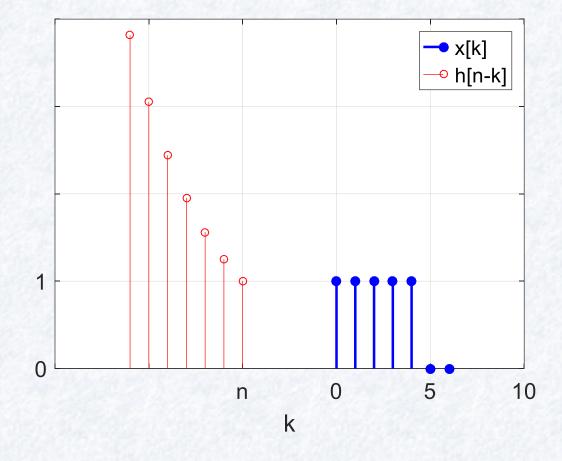


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$$x[n] = \begin{cases} 1, & 0 \le n \le 4 \\ 0, & \text{diğer} \end{cases}$$

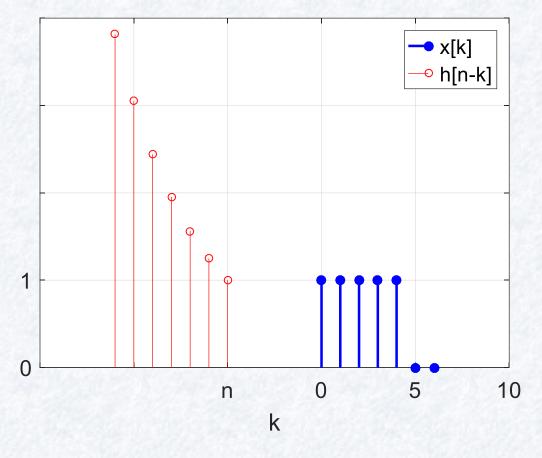
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$$h[n] = \begin{cases} \alpha^n, & 0 \le n \le 6 \\ 0, & \text{diğer} \end{cases}$$

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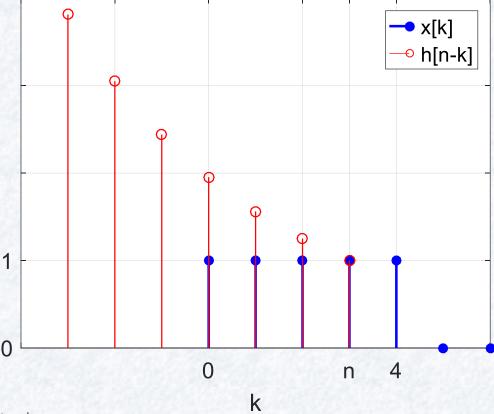
- n < 0 iken
 - ♦ Çakışma yok
- y[n] = 0



• $0 \le n \le 4$ iken



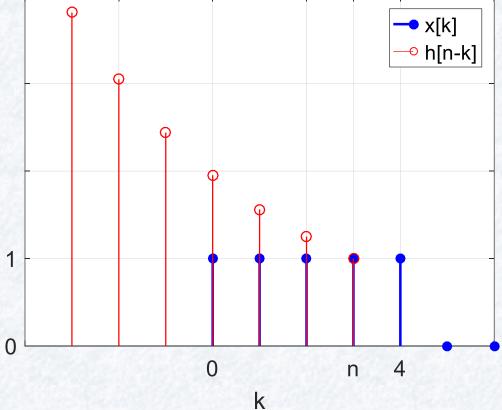
- $0 \le n \le 4$ iken
 - ♦ Çakışma,



- $0 \le n \le 4$ iken
 - ♦ Çakışma, 0-n arası

•
$$y[n] = \sum_{k=0}^{n} x[k]h[n-k]$$

•
$$y[n] = \sum_{k=0}^{n} 1 \cdot \alpha^{n-k}$$

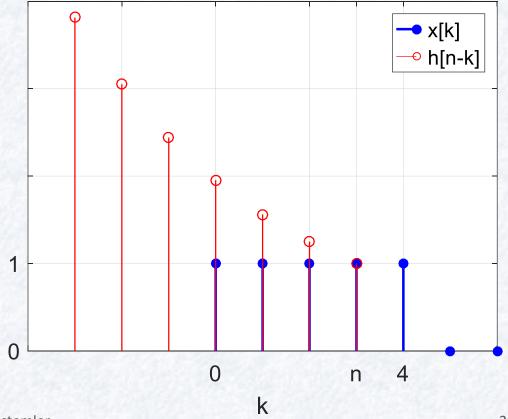


- $0 \le n \le 4$ iken
 - ♦ Çakışma, 0-n arası

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$$y[n] = \sum_{k=0}^{n} x[k]h[n-k]$$

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$$y[n] = \sum_{k=0}^{n} 1 \cdot \alpha^{n-k}$$

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$$y[n] = \sum_{k=0}^{n} 1 \cdot \alpha^n \alpha^{-k}$$



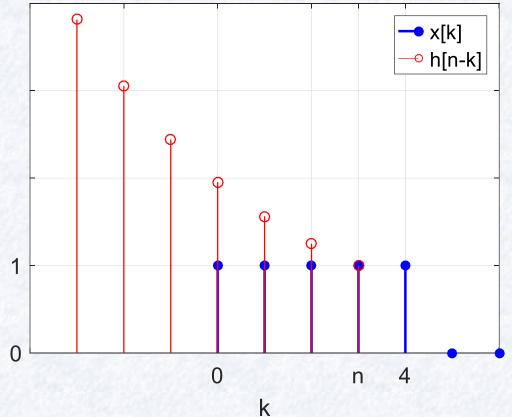
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- $0 \le n \le 4$ iken
 - ♦ Çakışma, 0-n arası

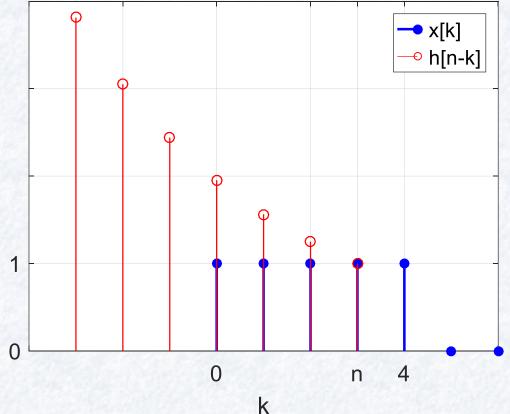
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$$y[n] = \alpha^n \sum_{k=0}^n \alpha^{-k}$$

•
$$y[n] = \alpha^n \sum_{k=0}^n \left(\frac{1}{\alpha}\right)^k$$



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 - ♦ Çakışma, 0-n arası

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$$y[n] = \sum_{k=0}^{n} x[k]h[n-k]$$

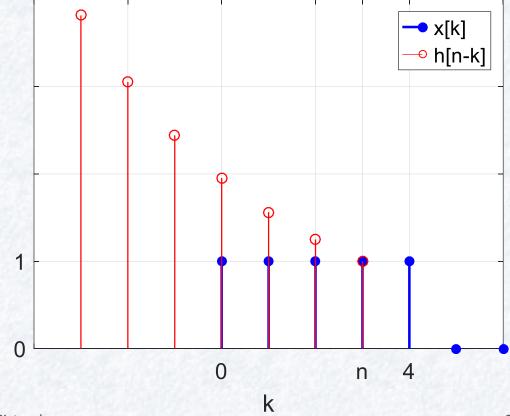
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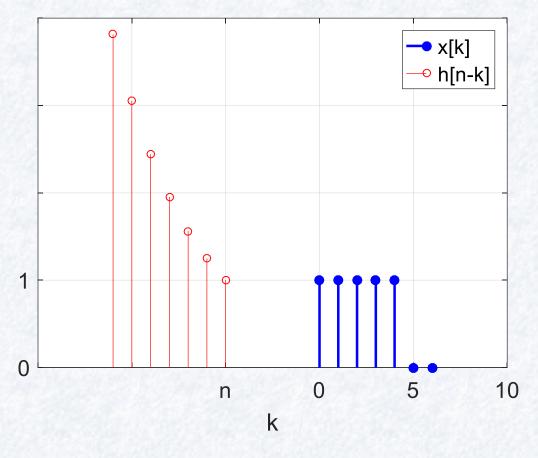
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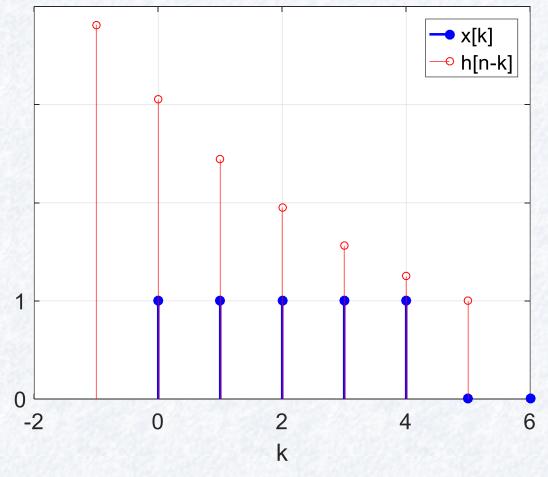
•
$$y[n] = \alpha^n \frac{1 - \left(\frac{1}{\alpha}\right)^{n+1}}{1 - \frac{1}{\alpha}}$$



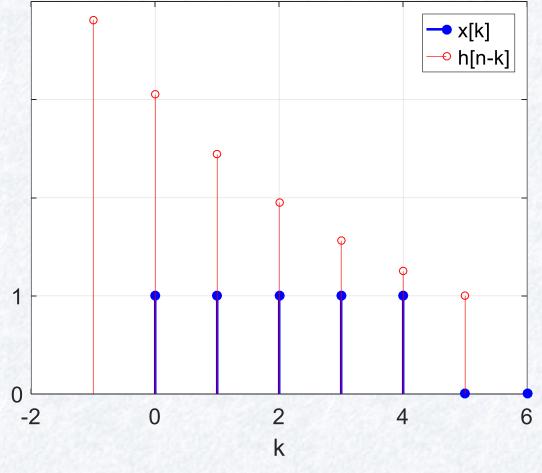
• $4 < n \le 6$ iken



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 - ◆ Çakışma,



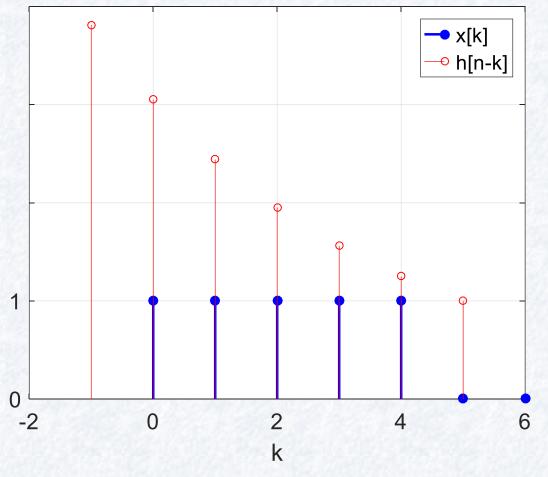
- $4 < n \le 6$ iken
 - ♦ Çakışma, 0-4 arası
- $y[n] = \sum_{k=0}^{4} x[k]h[n-k]$



- $4 < n \le 6$ iken
 - ♦ Çakışma, 0-4 arası

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$$y[n] = \sum_{k=0}^{4} x[k]h[n-k]$$

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$$y[n] = \alpha^n \sum_{k=0}^4 \alpha^{-k}$$

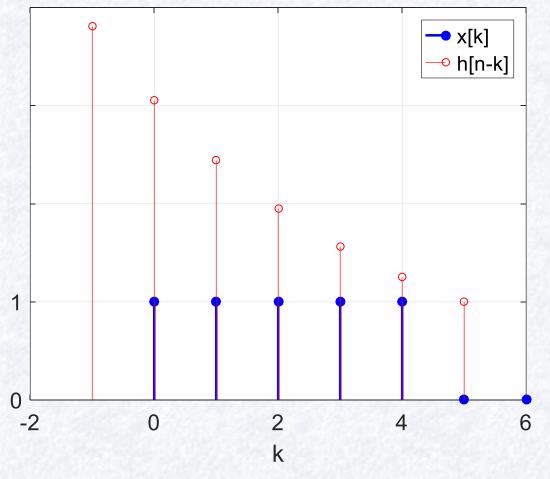


- $4 < n \le 6$ iken
 - ♦ Çakışma, 0-4 arası

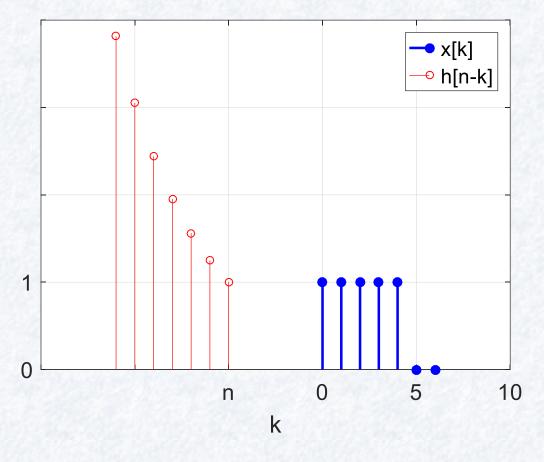
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$$y[n] = \sum_{k=0}^{4} x[k]h[n-k]$$

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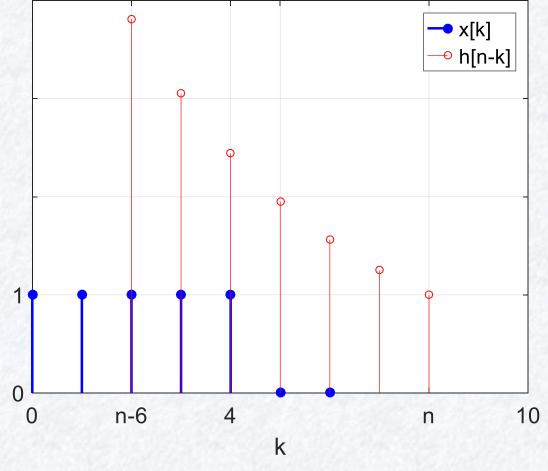
•
$$y[n] = \alpha^n \frac{1 - \left(\frac{1}{\alpha}\right)^5}{1 - \frac{1}{\alpha}}$$



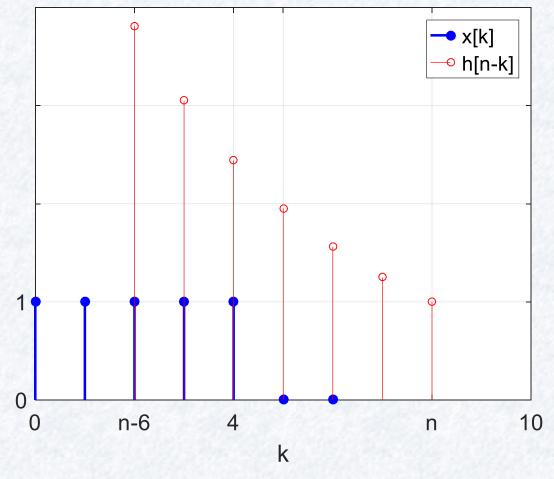
• $6 < n \le 10$ iken



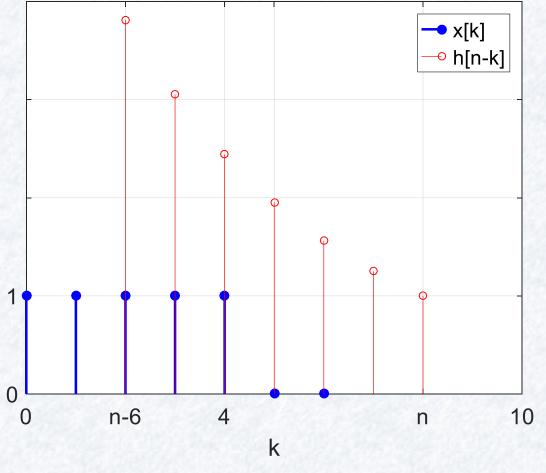
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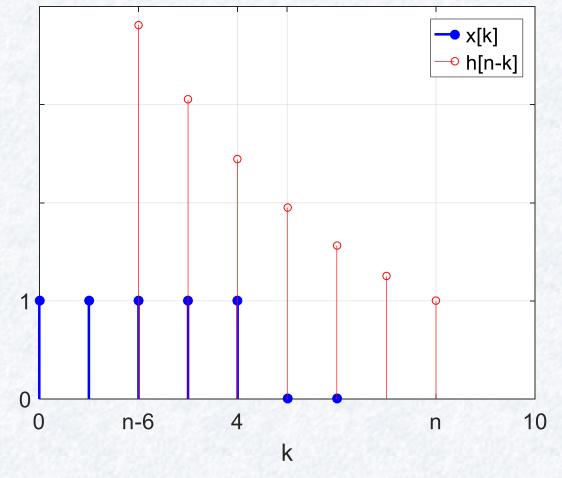
- $6 < n \le 10$ iken
 - ♦ Çakışma, n-6 4 arası



- $6 < n \le 10$ iken
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- $y[n] = \sum_{k=n-6}^{4} x[k]h[n-k]$



- $6 < n \le 10$ iken
 - ♦ Çakışma, n-6 4 arası
- $y[n] = \sum_{k=n-6}^{4} x[k]h[n-k]$
- $y[n] = \alpha^n \sum_{k=n-6}^4 \alpha^{-k}$
 - $\bullet l = k n + 6$



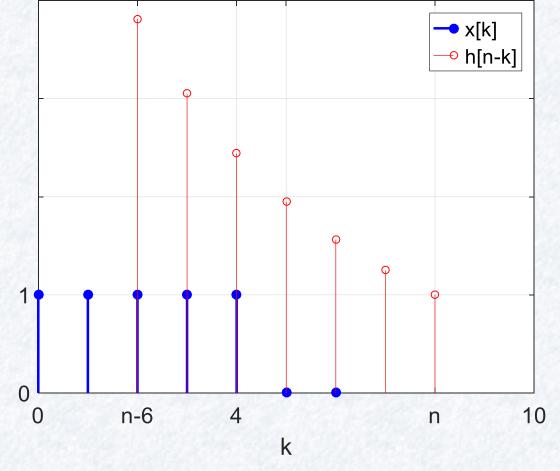
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$$y[n] = \sum_{k=n-6}^{4} x[k]h[n-k]$$

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$$y[n] = \alpha^n \sum_{k=n-6}^4 \alpha^{-k}$$

$$\bullet l = k - n + 6$$

•
$$y[n] = \alpha^n \sum_{l=0}^{10-n} \alpha^{-l-n+6}$$



- $6 < n \le 10$ iken
 - ◆ Çakışma, n-6 4 arası

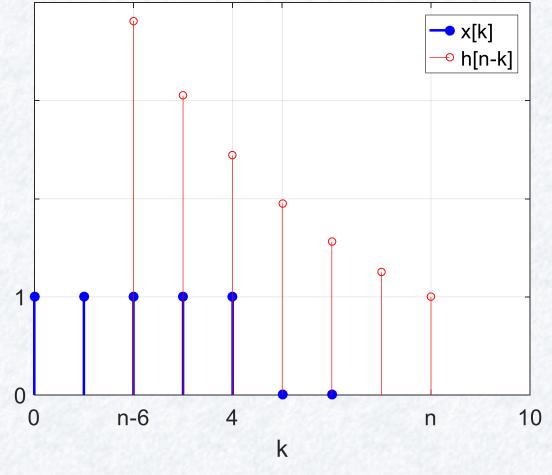
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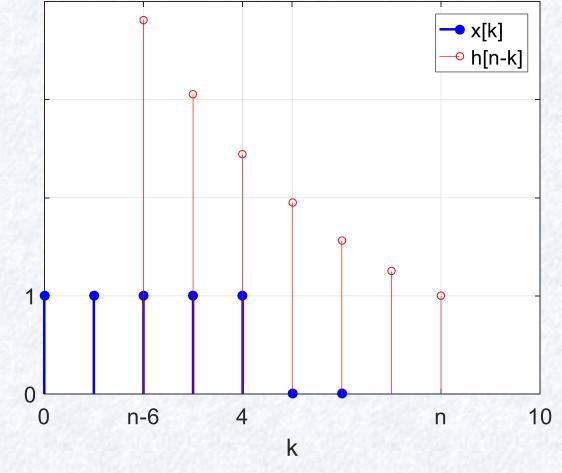
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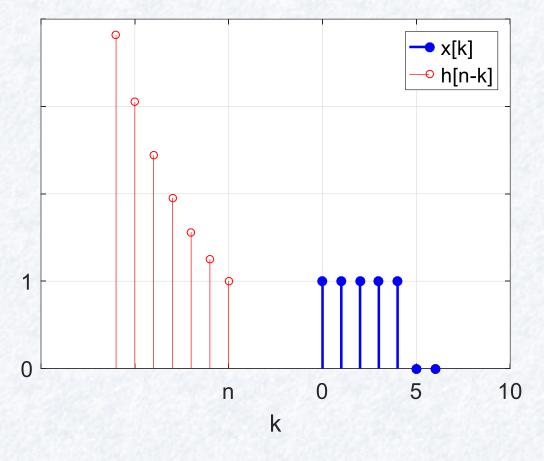
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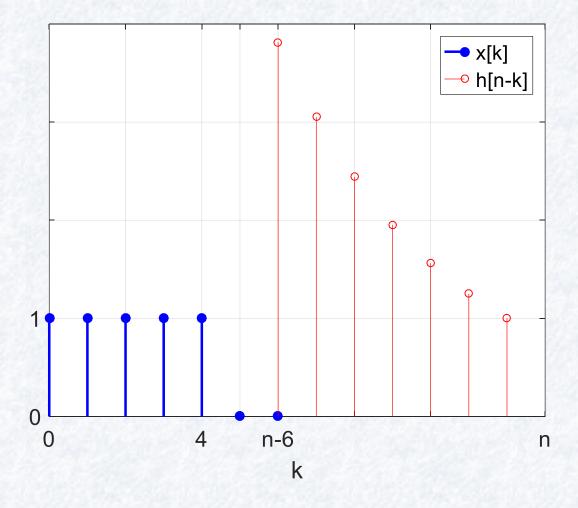
•
$$y[n] = \alpha^6 \frac{1 - \left(\frac{1}{\alpha}\right)^{11 - n}}{1 - \frac{1}{\alpha}}$$



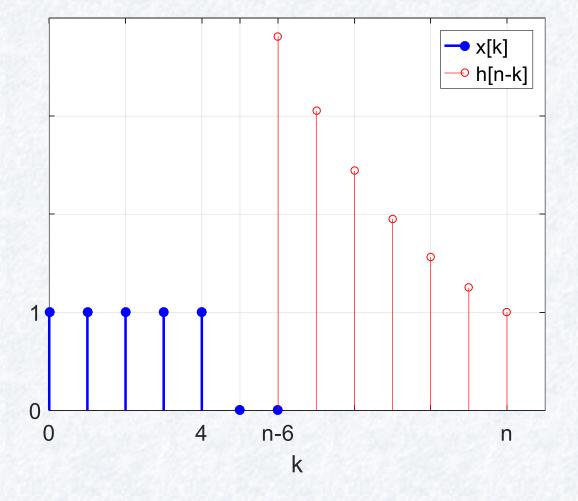
• 10 < n iken



- 10 < n iken
 - ♦ Çakışma yok.



- 10 < n iken
 - ♦ Çakışma yok.
- y[n] = 0



- n < 0 iken y[n] = 0
- $0 \le n \le 4$ iken $y[n] = \alpha^n \frac{1 \left(\frac{1}{\alpha}\right)^{n+1}}{1 \frac{1}{\alpha}}$
- $4 < n \le 6$ iken $y[n] = \alpha^n \frac{1 \left(\frac{1}{\alpha}\right)^5}{1 \frac{1}{\alpha}}$
- $6 < n \le 10$ iken $y[n] = \alpha^6 \frac{1 \left(\frac{1}{\alpha}\right)^{11 n}}{1 \frac{1}{\alpha}}$
- 10 < n iken y[n] = 0
- y[n] = ?

- n < 0 iken y[n] = 0

- $0 \le n \le 4$ iken $y[n] = \alpha^n \frac{1 \left(\frac{1}{\alpha}\right)^{n+1}}{1 \frac{1}{\alpha}}$ $4 < n \le 6$ iken $y[n] = \alpha^n \frac{1 \left(\frac{1}{\alpha}\right)^5}{1 \frac{1}{\alpha}}$ $6 < n \le 10$ iken $y[n] = \alpha^6 \frac{1 \left(\frac{1}{\alpha}\right)^{11 n}}{1 \frac{1}{\alpha}}$
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- $6 < n \le 10 \text{ iken } y[n] = \alpha^6 \frac{1 \left(\frac{1}{\alpha}\right)^{11 n}}{1 \frac{1}{\alpha}}$
- 10 < n iken y[n] = 0
- $y[n] = \left(\alpha^n \frac{1 \left(\frac{1}{\alpha}\right)^{n+1}}{1 \frac{1}{\alpha}}\right) \left(u(n) u(n-5)\right) + \left(\alpha^n \frac{1 \left(\frac{1}{\alpha}\right)^5}{1 \frac{1}{\alpha}}\right) ($

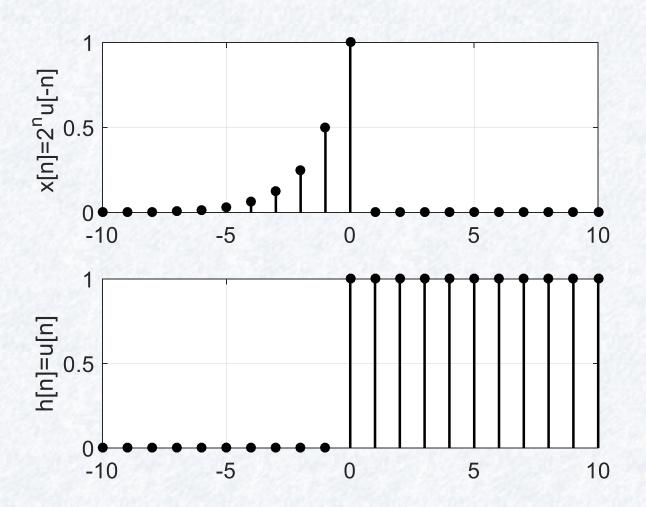
- n < 0 iken y[n] = 0
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- $6 < n \le 10 \text{ iken } y[n] = \alpha^6 \frac{1 \left(\frac{1}{\alpha}\right)^{11 n}}{1 \frac{1}{\alpha}}$
- 10 < n iken y[n] = 0

•
$$y[n] = \left(\alpha^n \frac{1 - \left(\frac{1}{\alpha}\right)^{n+1}}{1 - \frac{1}{\alpha}}\right) \left(u(n) - u(n-5)\right) + \left(\alpha^n \frac{1 - \left(\frac{1}{\alpha}\right)^5}{1 - \frac{1}{\alpha}}\right) \left(u(n-5) - u(n-7)\right) + \left(\alpha^6 \frac{1 - \left(\frac{1}{\alpha}\right)^{11-n}}{1 - \frac{1}{\alpha}}\right) (1)$$

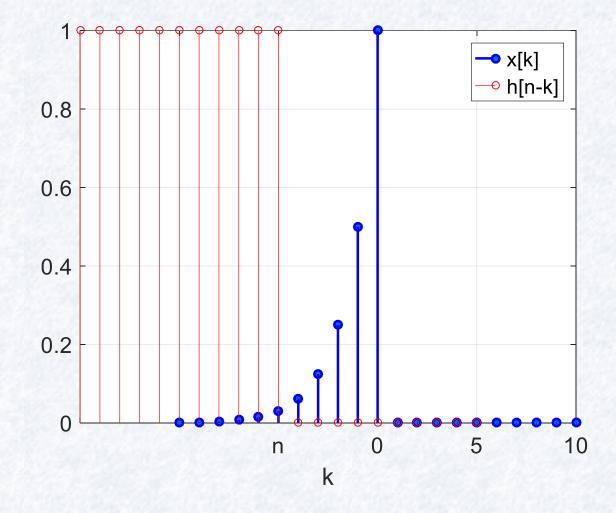
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- $4 < n \le 6$ iken $y[n] = \alpha^n \frac{1 \left(\frac{1}{\alpha}\right)^5}{1 \frac{1}{\alpha}}$
- $6 < n \le 10 \text{ iken } y[n] = \alpha^6 \frac{1 \left(\frac{1}{\alpha}\right)^{11 n}}{1 \frac{1}{\alpha}}$
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$$y[n] = \left(\alpha^{n} \frac{1 - \left(\frac{1}{\alpha}\right)^{n+1}}{1 - \frac{1}{\alpha}}\right) \left(u(n) - u(n-5)\right) + \left(\alpha^{n} \frac{1 - \left(\frac{1}{\alpha}\right)^{5}}{1 - \frac{1}{\alpha}}\right) \left(u(n-5) - u(n-7)\right) + \left(\alpha^{6} \frac{1 - \left(\frac{1}{\alpha}\right)^{11-n}}{1 - \frac{1}{\alpha}}\right) \left(u(n-7) - u(n-11)\right)$$

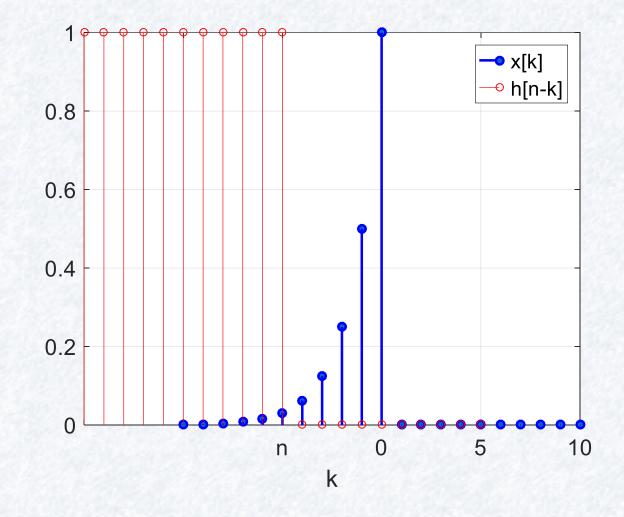
- $x[n] = 2^n u[-n]$
- h[n] = u[n]
- y[n] = ?



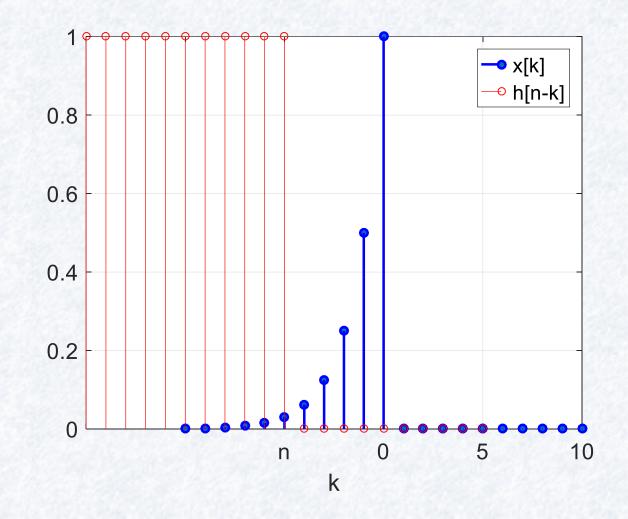
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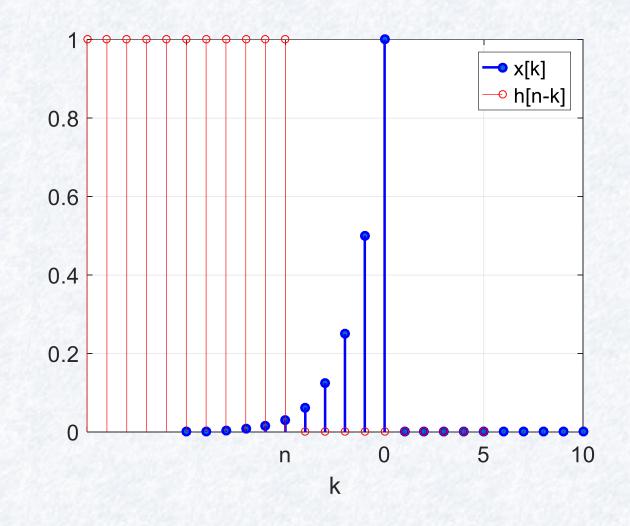
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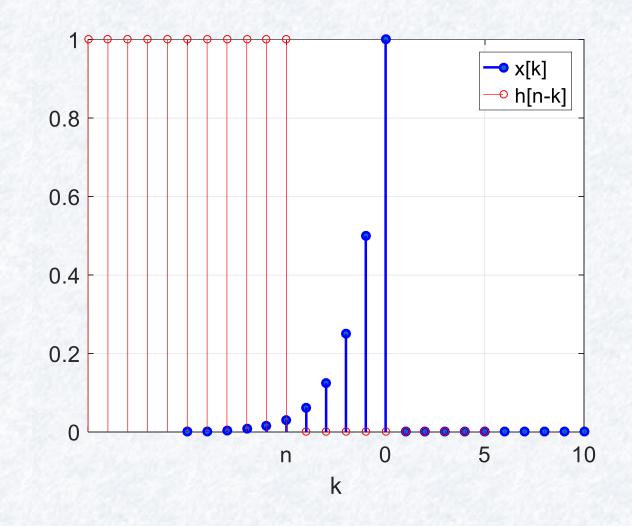
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 - ◆ Çakışma, -∞ n arası
- $y[n] = \sum_{k=-\infty}^{n} x[k]h[n-k]$



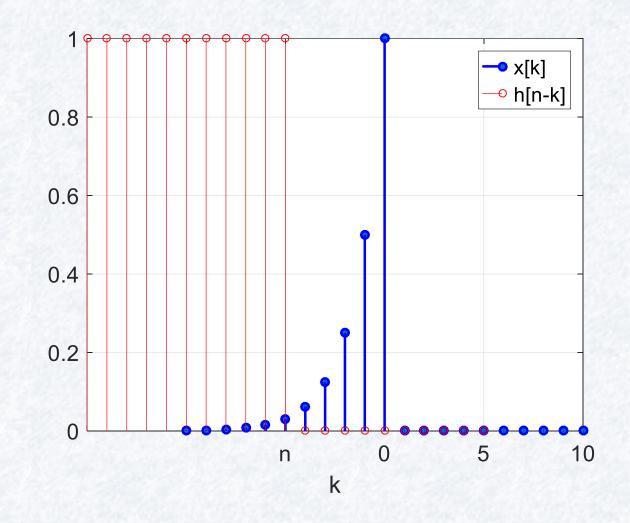
- $x[n] = 2^n u[-n]$
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- $y[n] = \sum_{k=-\infty}^{n} 2^{k} 1$



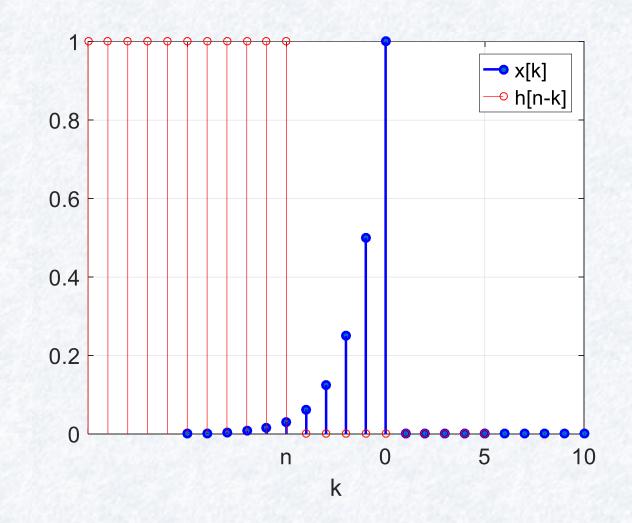
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 - $\bullet l = -k + n$



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•
$$x[n] = 2^n u[-n]$$

- h[n] = u[n]
- n < 0 iken
 - Çakışma, -∞ n arası

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$$y[n] = \sum_{k=-\infty}^{n} x[k]h[n-k]$$

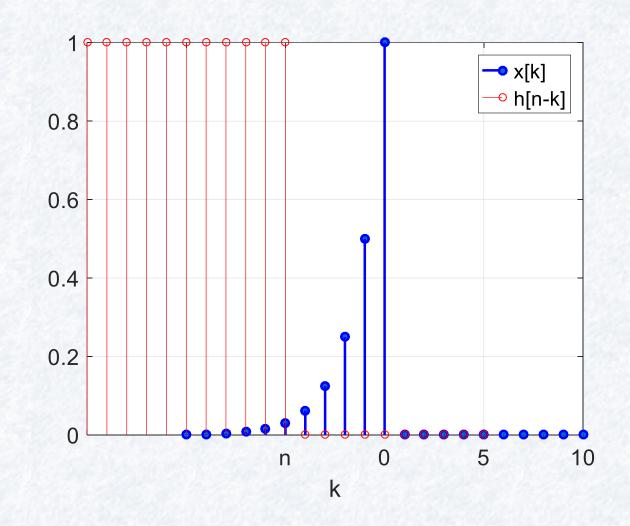
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$$\bullet$$
 $l = -k + n$

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$$y[n] = \sum_{l=\infty}^{0} 2^{n-l} 1$$

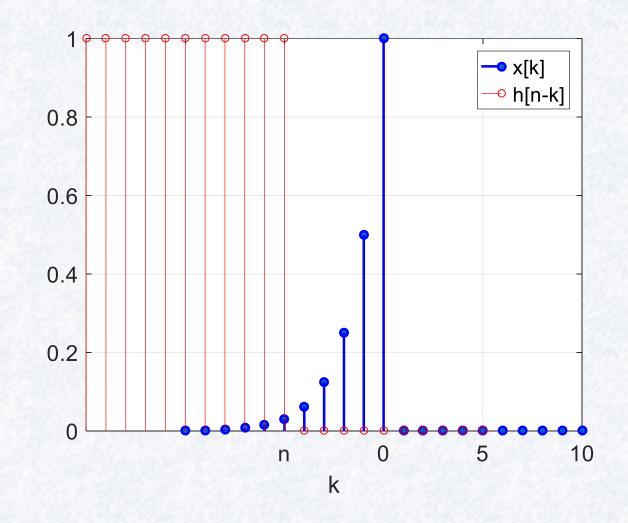
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$$y[n] = \sum_{l=0}^{\infty} 2^{n} 2^{-l} 1$$

•
$$y[n] = 2^n \sum_{l=0}^{\infty} \left(\frac{1}{2}\right)^l$$



- $x[n] = 2^n u[-n]$
- h[n] = u[n]
- *n* < 0 iken

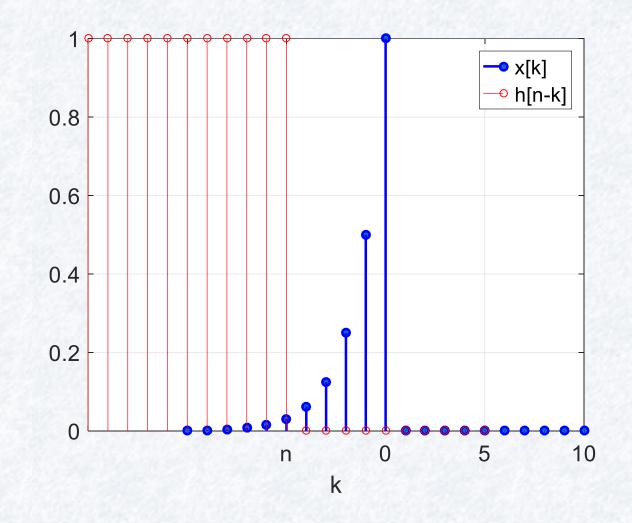
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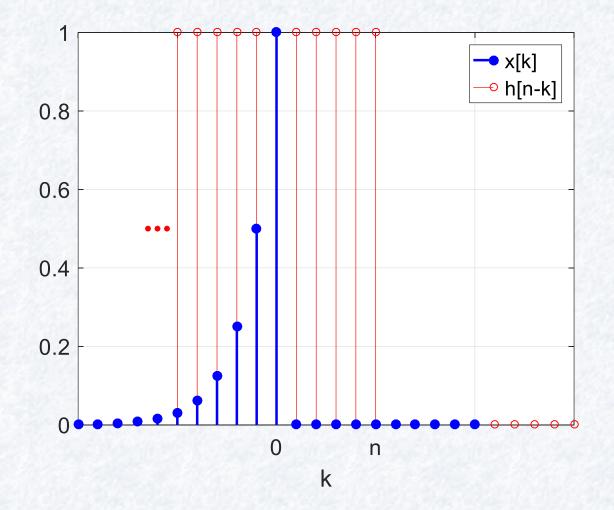
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$$y[n] = 2^n \sum_{l=0}^{\infty} \left(\frac{1}{2}\right)^l$$

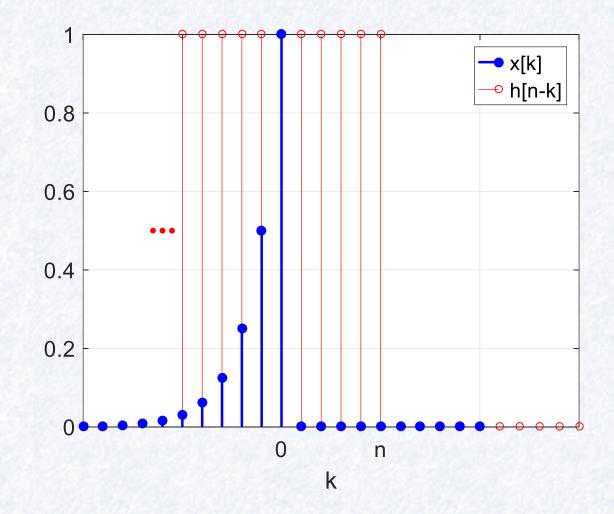
•
$$y[n] = 2^n \frac{1}{1 - \frac{1}{2}} = 2^{n+1}$$



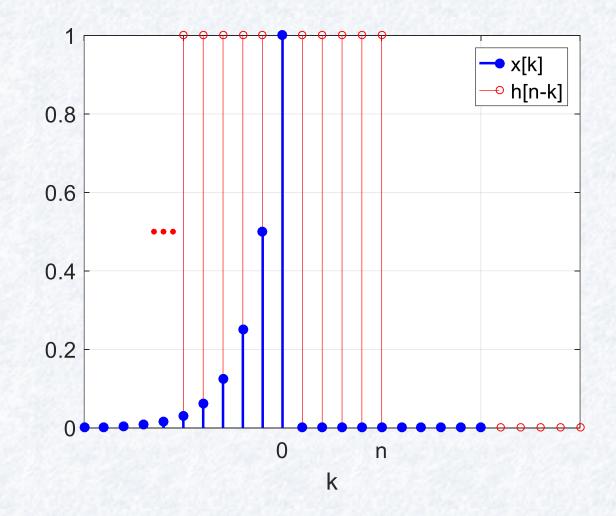
- $\bullet \ x[n] = 2^n u[-n]$
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 - ◆ Çakışma,



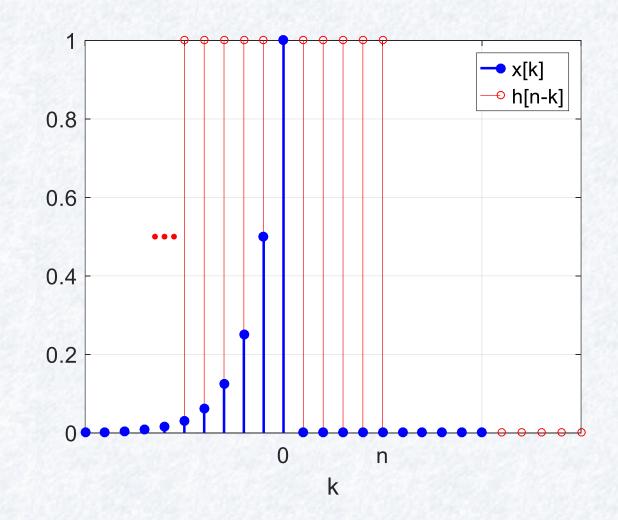
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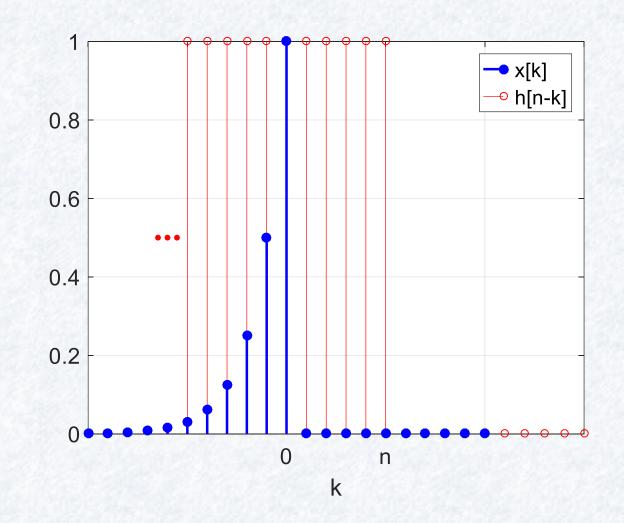
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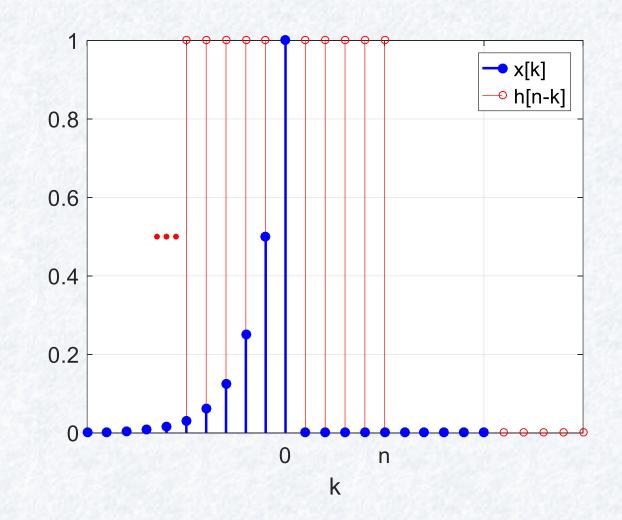
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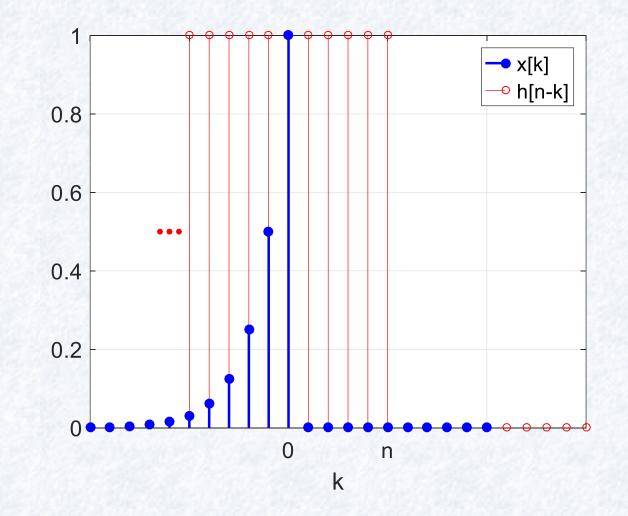
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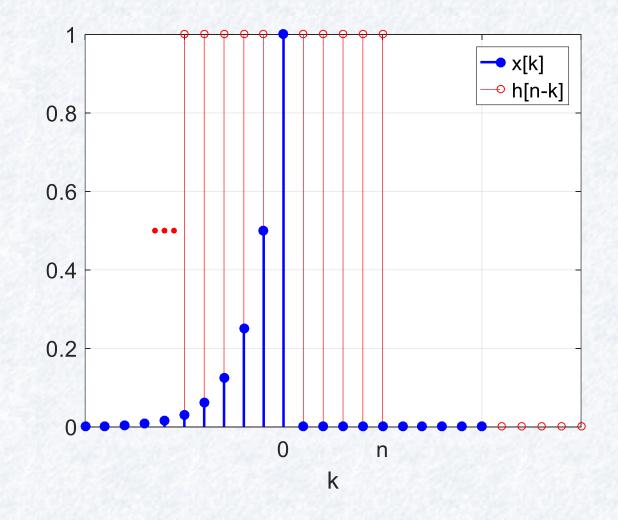
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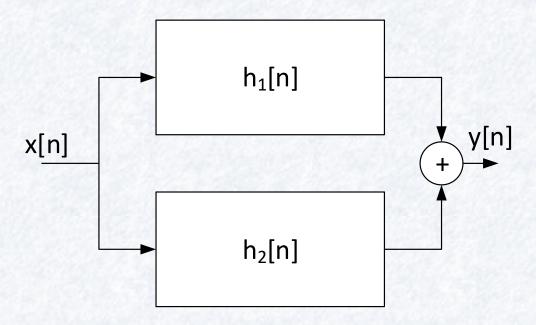
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- $y[n] = 2^{n+1}u[-n-1] + 2u[n]$

- Değişme Özelliği
 - $\star x[n] * h[n] = h[n] * x[n]$

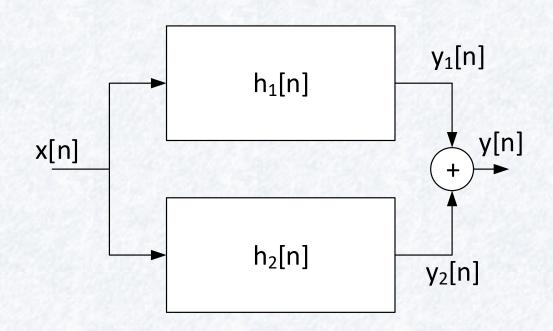
- Değişme Özelliği
 - $\star x[n] * h[n] = h[n] * x[n]$
- Dağılma Özelliği

- Değişme Özelliği
 - $\star x[n] * h[n] = h[n] * x[n]$
- Dağılma Özelliği
- Birleşme Özelliği

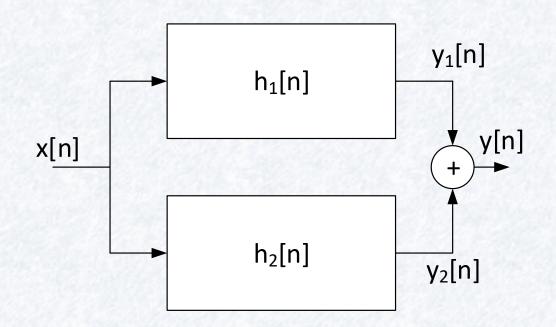
- Dağılma Özelliği
- y[n] = ?



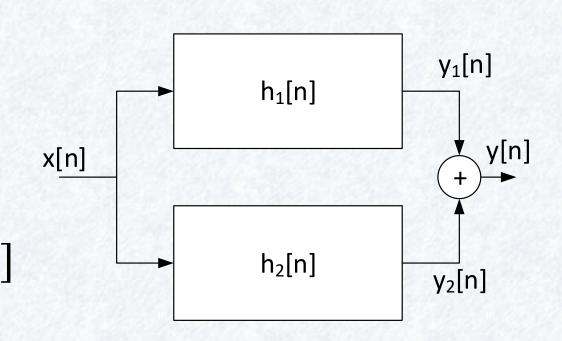
- Dağılma Özelliği
- y[n] = ?
- $y[n] = y_1[n] + y_2[n]$
- $y_1[n] = ?$
- $y_2[n] = ?$



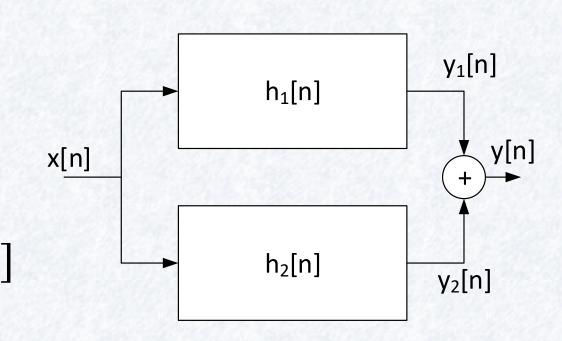
- Dağılma Özelliği
- y[n] = ?
- $y[n] = y_1[n] + y_2[n]$
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- $y_2[n] = x[n] * h_2[n]$



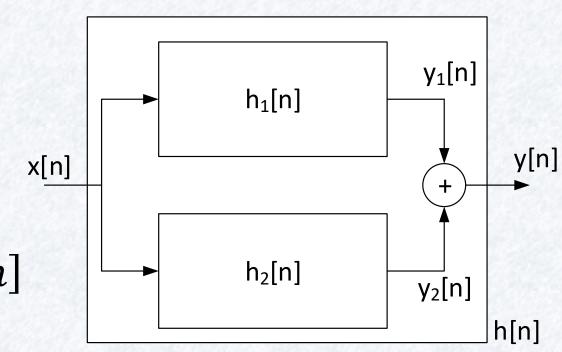
- Dağılma Özelliği
- y[n] = ?
- $y[n] = y_1[n] + y_2[n]$
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- $y_2[n] = x[n] * h_2[n]$
- $y[n] = x[n] * h_1[n] + x[n] * h_2[n]$



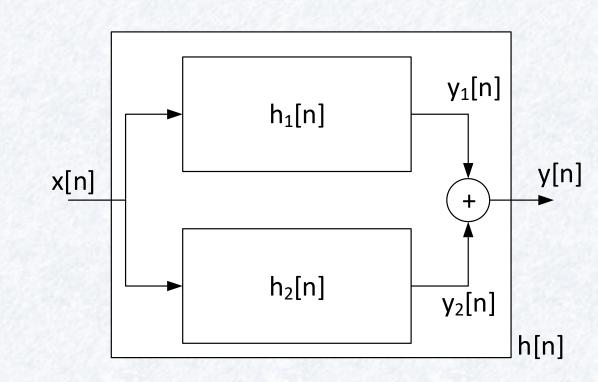
- Dağılma Özelliği
- y[n] = ?
- $y[n] = y_1[n] + y_2[n]$
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- $y_2[n] = x[n] * h_2[n]$
- $y[n] = x[n] * h_1[n] + x[n] * h_2[n]$



- Dağılma Özelliği
- y[n] = ?
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- $y_1[n] = x[n] * h_1[n]$
- $y_2[n] = x[n] * h_2[n]$
- $y[n] = x[n] * h_1[n] + x[n] * h_2[n]$
- y[n] =
- h[n] = ?



- Dağılma Özelliği
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- $y[n] = y_1[n] + y_2[n]$
- $y_1[n] = x[n] * h_1[n]$
- $y_2[n] = x[n] * h_2[n]$
- $y[n] = x[n] * h_1[n] + x[n] * h_2[n]$
- y[n] =
- y[n] = x[n] * h(n)
- h[n] = ?



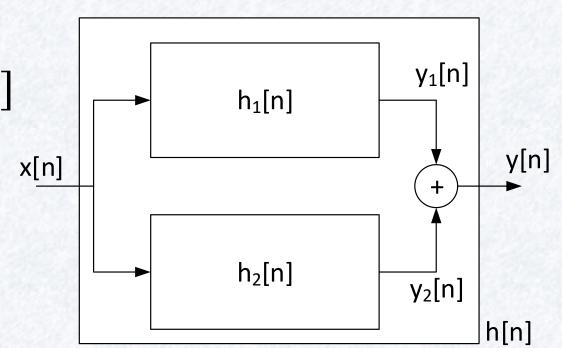
Dağılma Özelliği

•
$$y[n] = ?$$

•
$$y[n] = x[n] * h_1[n] + x[n] * h_2[n]$$

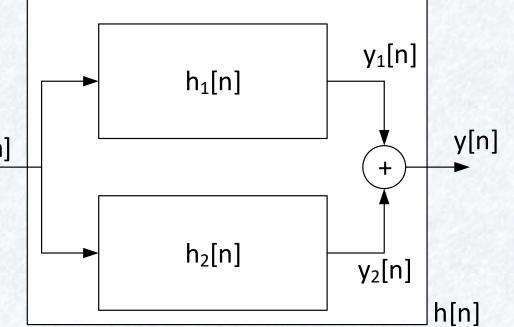
•
$$y[n] = x[n] * (h_1[n] + h_2[n])$$

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- h[n] = ?



Dağılma Özelliği

• h[n] = ?



Dağılma Özelliği

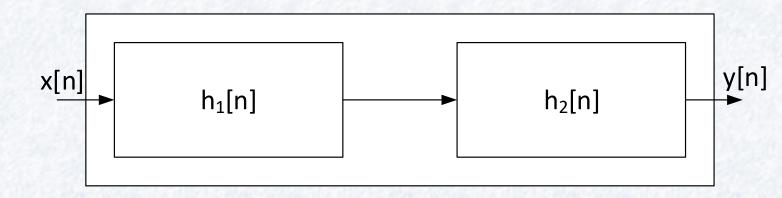
•
$$y[n] = ?$$
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• $y[n] = x[n] * (h_1[n] + h_2[n])$
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Dağılma Özelliği

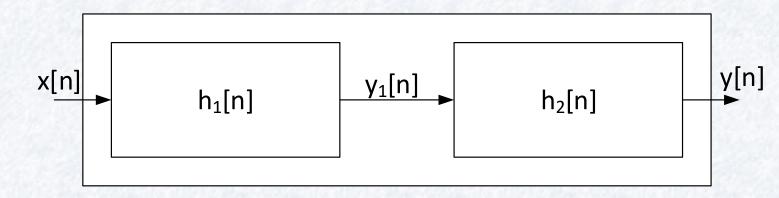
•
$$y[n] = ?$$
• $y[n] = x[n] * h_1[n] + x[n] * h_2[n]$
• $y[n] = x[n] * (h_1[n] + h_2[n])$
• $y[n] = x[n] * h(n)$
• $x[n] * h[n] = x[n] * (h_1[n] + h_2[n])$

 $h_1[n]$ $y_1[n]$ y[n] $h_2[n]$ $y_2[n]$ h[n]

- Birleşme Özelliği
 - $\star x[n] * (h_1[n] * h_2[n]) = (x[n] * h_1[n]) * h_2[n]$
- y[n] = ?



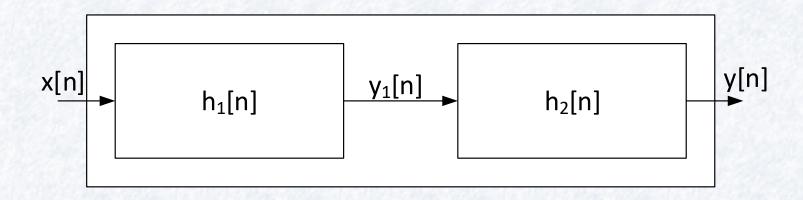
- Birleşme Özelliği
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- $y[n] = y_1[n] * h_2[n]$
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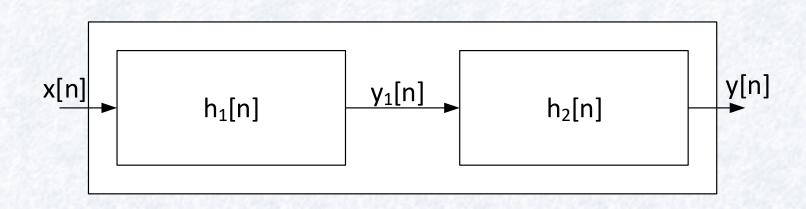
• Birleşme Özelliği

$$\star x[n] * (h_1[n] * h_2[n]) = (x[n] * h_1[n]) * h_2[n]$$

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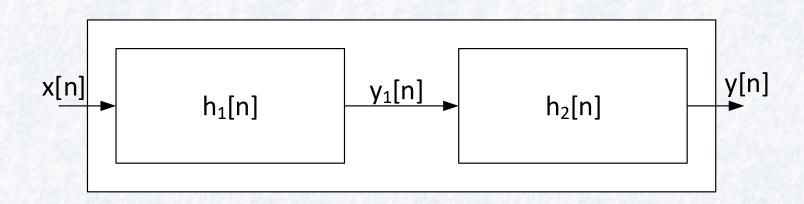
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Birleşme Özelliği

$$\star x[n] * (h_1[n] * h_2[n]) = (x[n] * h_1[n]) * h_2[n]$$

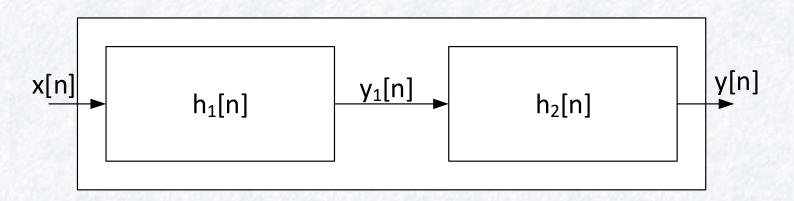
- $y[n] = y_1[n] * h_2[n]$
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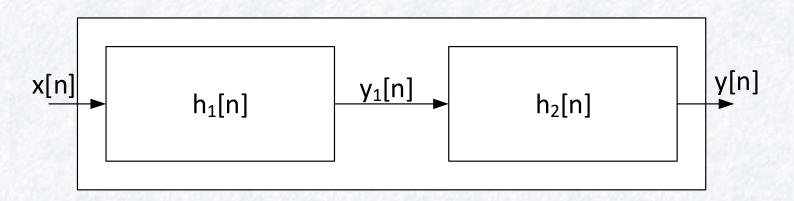
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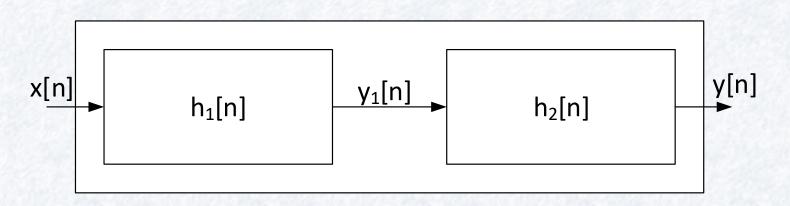
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• Birleşme Özelliği

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- Hafızalılık
- Hafızasız
 - ♦ Sistem çıkışının, giriş işaretinin zamanın sadece o andaki bilgisine bağlı olması
- Hafızalı
 - ♦ Sistem çıkışının, giriş işaretinin ötelenmiş hallerine bağlı olması
- $y[n] = \sum_{k=-\infty}^{\infty} x[k]h[n-k] = \sum_{k=-\infty}^{\infty} h[k]x[n-k]$
- $y[n] = \cdots + h[-1]x[n+1] + h[0]x[n] + h[1]x[n-1] + \cdots$

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Hafızalılık

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- $\forall n \neq 0$ iken h[n] = 0 olursa Hafızasız.

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 - \bullet $h[n] = A\delta[n]$

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- $\forall n \neq 0$ iken h[n] = 0 olursa Hafızasız.
 - \bullet $h[n] = A\delta[n]$
- $\exists n \neq 0$ iken $h[n] \neq 0$ olursa Hafızalı.
 - $h[n] \neq A\delta[n]$

• $h[n] = a^n u[n]$, Hafızalı mıdır?

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- $n \neq 0$ iken $h[n] \neq 0$
 - n = 1 iken h[n] = a
 - n = 2 iken $h[n] = a^2$
 - **♦**

- $h[n] = a^n u[n]$, Hafızalı mıdır?
- $n \neq 0$ iken $h[n] \neq 0$
 - $\bullet n = 1 \text{ iken } h[n] = a$
 - n = 2 iken $h[n] = a^2$
 - *****
- Hafızalı

• $h[n] = \delta[n - n_0]$, Hafızalı mıdır?

- $h[n] = \delta[n n_0]$, Hafızalı mıdır?
- $n \neq 0$ iken h[n] = ?

- $h[n] = \delta[n n_0]$, Hafızalı mıdır?
- $n \neq 0$ iken h[n]

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$$h[n] = \delta[n - n_0] = \begin{cases} 0, & n \neq n_0 \\ 1, & n = n_0 \end{cases}$$

- $h[n] = \delta[n n_0]$, Hafızalı mıdır?
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 - $n_0 = 0$ ise

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- $n_0 = 0$ ise Hafizasiz
- $n_0 \neq 0$ ise

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- $n_0 \neq 0$ ise Hafızalı

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 - $\bullet n = 1 \text{ iken } h[n] = 1$
 - $\bullet n = 2 \text{ iken } h[n] = 1$
 - *****

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 - *****
- Hafızalı

- Nedensellik
- $y[n] = \cdots + h[-1]x[n+1] + h[0]x[n] + h[1]x[n-1] + \cdots$
 - \bullet Nedensel: y[n], sadece

Nedensellik

- $y[n] = \cdots + h[-1]x[n+1] + h[0]x[n] + h[1]x[n-1] + \cdots$
 - ullet Nedensel: y[n], sadece x[n] ve/veya x[n-k] 'ya bağlı olması
- $y[n] = \underbrace{\cdots + h[-1]x[n+1]}_{0} + h[0]x[n] + h[1]x[n-1] + \cdots$
- $\forall n < 0$ iken h[n] = 0 ise Nedensel.

Nedensellik

- $y[n] = \cdots + h[-1]x[n+1] + h[0]x[n] + h[1]x[n-1] + \cdots$
 - ullet Nedensel: y[n], sadece x[n] ve/veya x[n-k] 'ya bağlı olması
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- $\forall n < 0$ iken h[n] = 0 ise Nedensel.
- $\exists n < 0$ iken $h[n] \neq 0$ ise Nedensel değil.

- $h[n] = a^n u[n]$, Nedensel midir?
 - ♦ Hafızalı

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 - ♦ Hafızalı
- n < 0 iken h[n] = 0
 - n < 0 iken u[n] = 0
- Nedensel

- $h[n] = \delta[n n_0]$, Nedensel midir?
 - \bullet $n_0 \neq 0$ ise Hafızalı, $n_0 = 0$ ise Hafızasız

- $h[n] = \delta[n n_0]$, Nedensel midir?
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- n < 0 iken h[n] = ?

Dr. Ari

- $h[n] = \delta[n n_0]$, Nedensel midir?
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- $\delta[n-n_0] = \begin{cases} 0, & n \neq n_0 \\ 1, & n = n_0 \end{cases}$

- $h[n] = \delta[n n_0]$, Nedensel midir?
 - \bullet $n_0 \neq 0$ ise Hafızalı, $n_0 = 0$ ise Hafızasız
- n < 0 iken h[n] = ?
- $\delta[n-n_0] = \begin{cases} 0, & n \neq n_0 \\ 1, & n = n_0 \end{cases}$
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 - ♦ Nedensel değil.

- $h[n] = \delta[n n_0]$, Nedensel midir?
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$$\delta[n-n_0] = \begin{cases} 0, & n \neq n_0 \\ 1, & n = n_0 \end{cases}$$

- $n = n_0 < 0$ iken h[n] = 1
 - ♦ Nedensel değil.
- $n = n_0 \ge 0$ iken h[n] = 1
- n < 0 iken h[n] = 0
 - ♦ Nedensel.

- h[n] = u[n], Nedensel midir?
 - ♦ Hafızalı

- h[n] = u[n], Nedensel midir?
 - ♦ Hafızalı
- n < 0 iken h[n] = ?

- h[n] = u[n], Nedensel midir?
 - ♦ Hafızalı
- n < 0 iken h[n] = 0

- h[n] = u[n], Nedensel midir?
 - ♦ Hafızalı
- n < 0 iken h[n] = 0
 - n < 0 iken u[n] = 0

- h[n] = u[n], Nedensel midir?
 - ♦ Hafızalı
- n < 0 iken h[n] = 0
 - n < 0 iken u[n] = 0
- Nedensel

- Kararlılık
- $\sum_{n=-\infty}^{\infty} |h[n]| < \infty$ ise Kararlı.

- Kararlılık
- $\sum_{n=-\infty}^{\infty} |h[n]| < \infty$ ise Kararlı.
- $\sum_{n=-\infty}^{\infty} |h[n]| \to \infty$ ise Kararsız.

- $h[n] = a^n u[n]$, Kararlı mıdır?
 - ♦ Hafızalı
 - ♦ Nedensel

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 - ♦ Hafızalı
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- $\sum_{n=-\infty}^{\infty} |h[n]| = ?$

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 - ♦ Nedensel
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- $\sum_{n=-\infty}^{\infty} a^n u[n] = ?$

- $h[n] = a^n u[n]$, Kararlı mıdır?
 - ♦ Hafızalı
 - ♦ Nedensel
- $\sum_{n=-\infty}^{\infty} |h[n]| = ?$
- $\bullet \ \sum_{n=0}^{\infty} a^n = \begin{cases} \infty, & a \ge 1 \end{cases}$

- $h[n] = a^n u[n]$, Kararlı mıdır?
 - ♦ Hafızalı
 - ♦ Nedensel

•
$$\sum_{n=-\infty}^{\infty} |h[n]| = ?$$

•
$$\sum_{n=0}^{\infty} a^n = \begin{cases} \infty, & |a| \ge 1 \\ \frac{1}{1-a} & |a| < 1 \end{cases}$$

- $h[n] = a^n u[n]$, Kararlı mıdır?
 - ♦ Hafızalı
 - ♦ Nedensel
- $\sum_{n=-\infty}^{\infty} |h[n]| = ?$

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$$\sum_{n=0}^{\infty} a^n = \begin{cases} \infty, & |a| \ge 1 \\ \frac{1}{1-a} & |a| < 1 \end{cases}$$

• $|a| \ge 1$ iken Kararsız

- $h[n] = a^n u[n]$, Kararlı mıdır?
 - ♦ Hafızalı
 - ♦ Nedensel
- $\sum_{n=-\infty}^{\infty} |h[n]| = ?$

- $|a| \ge 1$ iken Kararsız
- |a| < 1 iken Kararlı

- $h[n] = \delta[n n_0]$, Kararlı mıdır?
 - $n_0 \neq 0$ ise Hafızalı, $n_0 = 0$ ise Hafızasız
 - \bullet $n_0 \ge 0$ ise Nedensel, $n_0 < 0$ ise Nedensel değil

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- $\sum_{n=-\infty}^{\infty} |h[n]| = ?$

- $h[n] = \delta[n n_0]$, Kararlı mıdır?
 - $n_0 \neq 0$ ise Hafızalı, $n_0 = 0$ ise Hafızasız
 - \bullet $n_0 \ge 0$ ise Nedensel, $n_0 < 0$ ise Nedensel değil
- $\sum_{n=-\infty}^{\infty} |h[n]| = ?$
- $\sum_{n=-\infty}^{\infty} \delta[n-n_0] =$

- $h[n] = \delta[n n_0]$, Kararlı mıdır?
 - $n_0 \neq 0$ ise Hafızalı, $n_0 = 0$ ise Hafızasız
 - \bullet $n_0 \ge 0$ ise Nedensel, $n_0 < 0$ ise Nedensel değil
- $\sum_{n=-\infty}^{\infty} |h[n]| = ?$
- $\sum_{n=-\infty}^{\infty} \delta[n-n_0] = 1$

- $h[n] = \delta[n n_0]$, Kararlı mıdır?
 - \bullet $n_0 \neq 0$ ise Hafızalı, $n_0 = 0$ ise Hafızasız
 - \bullet $n_0 \ge 0$ ise Nedensel, $n_0 < 0$ ise Nedensel değil
- $\sum_{n=-\infty}^{\infty} |h[n]| = ?$
- $\sum_{n=-\infty}^{\infty} \delta[n-n_0] = 1 < \infty$
- Kararlı

- h[n] = u[n], Kararlı mıdır?
 - ♦ Hafızalı
 - ♦ Nedensel

- h[n] = u[n], Kararlı mıdır?
 - ♦ Hafızalı
 - ♦ Nedensel
- $\sum_{n=-\infty}^{\infty} |h[n]| = ?$

- h[n] = u[n], Kararlı mıdır?
 - ♦ Hafızalı
 - ♦ Nedensel
- $\sum_{n=-\infty}^{\infty} |h[n]| = ?$
- $\sum_{n=-\infty}^{\infty} u[n] =$

- h[n] = u[n], Kararlı mıdır?
 - ♦ Hafızalı
 - ♦ Nedensel
- $\sum_{n=-\infty}^{\infty} |h[n]| = ?$
- $\sum_{n=-\infty}^{\infty} u[n] = \sum_{n=0}^{\infty} 1$

- h[n] = u[n], Kararlı mıdır?
 - ♦ Hafızalı
 - ♦ Nedensel
- $\sum_{n=-\infty}^{\infty} |h[n]| = ?$
- $\sum_{n=-\infty}^{\infty} u[n] = \sum_{n=0}^{\infty} 1 = \infty$

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- $\sum_{n=-\infty}^{\infty} |h[n]| = ?$
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- Kararsız