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Space Reduction of Tentriss Hypertrie with Path Compression

by

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Ort, Datum

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Abstract. In my thesis, I investigate and implement a space reduction approach for the in-memory indexing data structure Hypertrie.

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1

Introduction

Preliminaries and Foundations

This chapter is logically divided into two main parts. The first part presents the tooling and techniques I utilized to implement aspects of my space-reduction solution. I take into consideration the pointer tagging technique (Sec. 2.2) and the utilization of template-meta programming in modern C++ (Sec. 2.3). In addition, the first part introduces common notations and terminologies that I use through out the work (Sec. 2.1).

In the second part, I give a quick overview of the semantic web topic (Sec. 2.4). Afterwards I delve into Tentrism in section 2.5 where I present its concept and implementation. More deeply, I describe how its realized by presenting its main underlying data structure, Hypertrie. My work builds on top of the current Tentrism implementation in an attempt to tackle the excessive memory consumption challenge. **Maybe need to delete the last sentence.**

2.1 Notation and Convention

For a function f , the domain and co-domain of f are denoted by $\text{dom}(f)$ and $\text{codom}(f)$, respectively. The set of natural numbers \mathbb{N} includes zero in this work. Further \mathbb{N}_n with $n \in \mathbb{N}$ is equal to $\{0, 1, \dots, n-1\}$. Let \mathbb{B} be the set of boolean values; i.e. $\mathbb{B} = \{true, false\}$. We map *true* to 1 and *false* to 0. We use angle brackets $\langle \dots \rangle$ to define a tuple t which represents a sequence with fixed order for its elements. The entries $\langle t_0, t_1, \dots, t_{n-1} \rangle$ of a tuple t with length n can be accessed using the square bracket notation (subscript) after the tuple symbol. For example, $t[i] = t_i$ is the tuple t entry at position i . Entries of a tuple t are zero-indexed. The domain of a tuple t , denoted by $\text{dom}(t) = \langle 0, 1, \dots, n-1 \rangle$, is a tuple of t entries' positions.

2.2 Pointer Tagging

Pointer Tagging is a low-level programming technique that uses the spare low bits in a pointer to encode additional information. Using the Pointer tagging technique, pointer value (initially a memory address before tagging) can hold extra information about the point-to heap object or can be used as a meta-data to further describe the usage of the pointer data. Pointer tagging is mainly enabled because of the way heap objects are situated and accessed on modern computer architectures.

metaphorically

2.2.1 Data Structure Alignment

Data alignment (also referred to as data structure padding) is a way in which heap objects are arranged and accessed by the CPU. CPUs in modern computer architecture (say 64-bit architecture) read data from and write data to memory more efficiently when data is aligned.

On an abstract level, computer memory can be seen as an array of words or bytes, each with its own address. Unlike bytes, the term word has ambiguous meaning. In the context of this work, we are targeting the generic term in the context of CPU architecture. That is, a "processor word" refers to the size of a processor register or memory address register. The term word also refers to the size of CPU instruction, or the size of a pointer depending on the exact CPU architecture. For example, in a 64-bit architecture, the word size (also pointer size) is 64 bits = 8 bytes.

Figure need to
added

Generally, when a source program is executed, it is loaded into memory and put into a process p for execution. All data objects in the program are mapped at certain point in time (during compilation or execution) to a physical memory address [ref: operating system concept]. Let us suppose we have the following snippet written in C language:

```
bool *b = new bool(true); // x = x21DE
int* a = new int(123); // a = x21E6
char* c = new char('A'); // c = x21EE
```

According to C language specification, the size of integer value in memory is 4 bytes and size of char value is 1 byte [C spec]. When we execute the previously mentioned statements, however, the compiler (or linker) books 8 bytes of memory to hold the integer value and not 4 bytes as expected. The reason is that, the compiler adds padding to the heap objects in order to align them in memory. The same applies to the character value, as shown in figure 1 (on my notebook).

Why data alignment? The CPU can access the memory only in word-sized chunks. So if our data always starts at a word it can be fetched efficiently. If it were to start somewhere in the middle of a word, the CPU will need to wait two or more memory cycles to fetch data from or write data to memory causing an increase in the CPU stall period which results in a significant performance overhead.

many modern compilers implementations handle data alignment in memory automatically, example includes C, C++, Rust, C# compilers.

2.2.2 Tagged Pointers

Some high-level programming languages, for example C++, offer developers a tool set to work with memory. Using such tool set, developers have access to low level memory abstraction. The main building block that enables memory management is the **pointer data type** and its ecosystem. A variable of type pointer holds a memory address of an object stored in the heap. Due to data alignment (cf. ??), the memory address of any object in the heap memory is always $\alpha \cdot w$ where $w = 8$ (the word size). This implies all addresses held as a pointer value are multiple of 8. A pointer thus can be 8, 16, 24, 109144, etc. But it can not be 7 or 13.

Speaking in binary, example of pointer values are 0b1000 (=8), 0b10000 (=16), 0b11000 (=24), 0b11010101001011000 (=109144). The lower three bits, also called the least significant

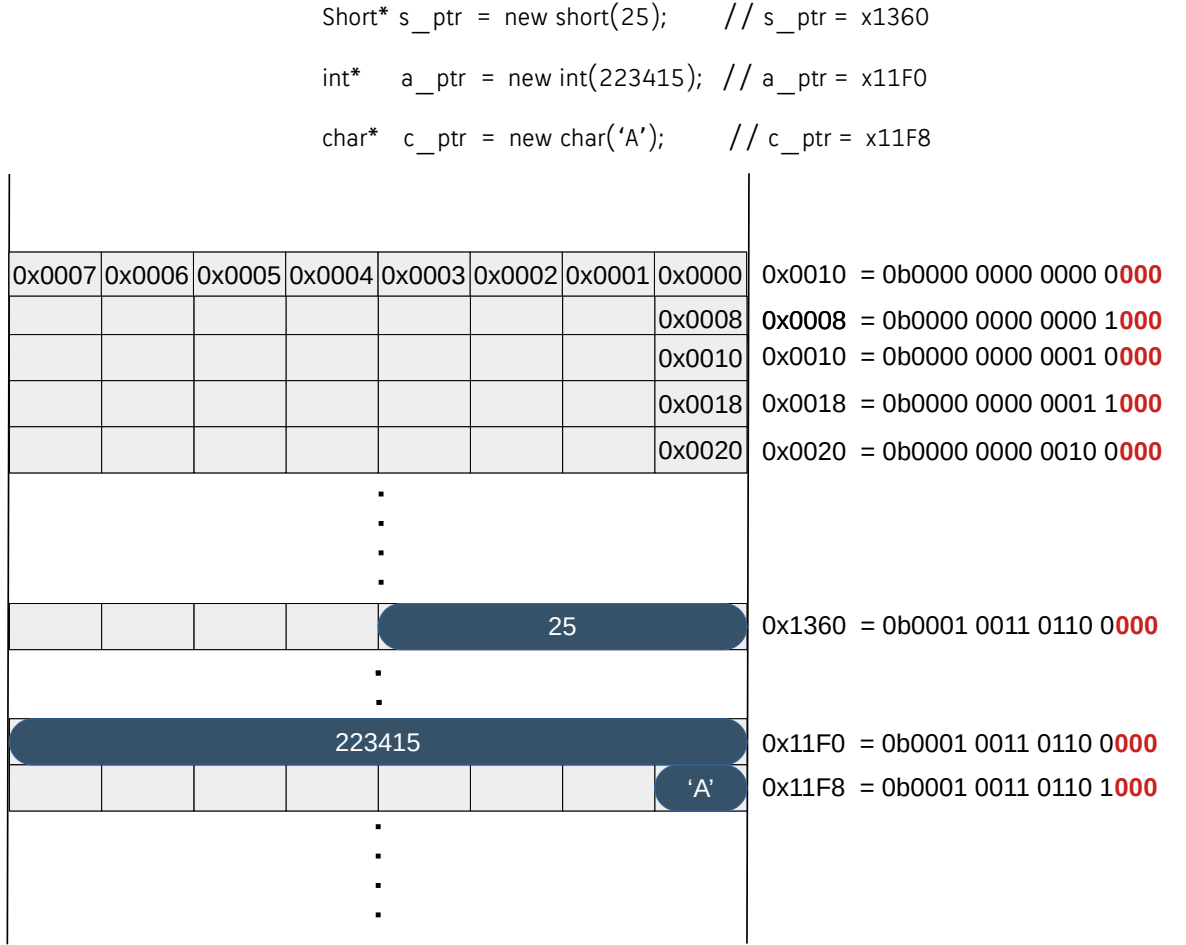


Figure 2.1: Trie representation of the tensor T_g that depicts the RDF graph g in Table ???. A slice $T_g[3, :, :]$ by the first dimension with 3 is shown in the red (inner) box.

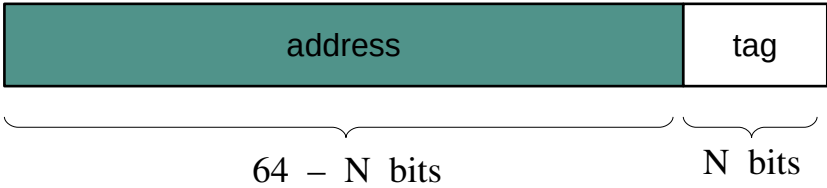


Figure 2.2: Trie representation of the tensor T_g that depicts the RDF graph g in Table ???. A slice $T_g[3, :, :]$ by the first dimension with 3 is shown in the red (inner) box.

bits (LSBs), are always zero. So those three bits are basically free to use. We can use them to store a **tag**, which is an integer between 0 (0b000) and 7 (0b111).

Pointer tagging technique allows a dynamic representation of the value based on the tag. Thus, the actual bits payload of the pointer could represents a memory address for some time during the process execution but can later express the binary representation of a **char** value for example, depending on the execution context and after a change in the tag value during run-time.

An approach to implement a tagged pointer is to develop a wrapper object around a pointer type variable. The wrapper can be equipped with adequate behaviours that govern the tag/payload manipulation and retrieval. An example of pointer tagging implementation can be seen in listing ()

Add the listing

Pointer tagging can be applied in many use cases. In my work, there are a couple of use cases where pointer tagging served perfectly the purpose. Namely: storing integers in pointers and Dynamic de-referencing of void pointers (**void***).

Need to check t

2.2.3 Tagged Pointer Implementation

Tagged pointers technique doesn't compromise address space/ but does affect memory safty
Doesn't add extra overhead of extra space utilization

Integer Tagged Pointer

Type Tagged Pointer Figure

Keep it for the being

2.3 Template Meta-programming

In this section I discuss the C++ meta programming concept.

2.4 Semantic Web

Today World Wide Web (WWW) holds a tremendous amount of different types of data (videos, images, text, geolocation data, books, publications, etc.). Such data comes from different sources (web applications, warehouse systems, GPS devices, smartphones, ATMs, etc.). However, such data are still processed passively by computer system as there is no way to understand its meaning or context. The term **Semantic Web** was coined by Tim Berners-Lee for a *Web of Data* (or *Data Web*) [2] that can be processed by machines. The key technologies of Semantic Web are published by the World Wide Web Consortium (W3C). The Resource Description Framework (RDF), a standard for representing data in the Semantic Web, and SPARQL, a query language for RDF data, are introduced in this section.

2.4.1 Resource Description Framework

The Resource Description Framework (RDF) is part of the W3C standard to define the web of data [1]. Regardless of the nature of the data entity held on the web (blog post, image, publication, newspaper article, list of invoices, etc.), RDF identifies them uniformly as resources. In the standard, each resource is attached to a unique Internationalized Resource Identifier (IRI). IRI is a standard defined by the Internet Engineering Task Force in RFC 3987 [?]. Literals are another sort of resources. A literal comprises a hardcoded value represented as a string; (“Martin,” “true”, “12.3”) are examples of literals. The third resource type is called a blank node. Blank nodes represent anonymous resources and always have local scope where they can be assigned a unique identifier. All definitions in this section are taken from “RDF 1.1 Concepts and Abstract Syntax” [?].

Definition 2.1 (RDF Terms). Let I be the set of *IRIs*, L be the set of *literals* and be B the set of *blank nodes*. Further I , L and B are finite and pair-wise disjoint. Then the set $RT = I \cup L \cup B$ is called the set of RDF terms.

RDF Triple, RDF Graph

On an abstract level, an RDF triple can be seen as a statement that describes the relationship between two resources. An RDF triple can also serve to describe the property of a resource. RDF triple is represented by a sentence composed of three elements in order: *a subject*, *a predicate* and *an object*. The subject is a RDF resource. The subject has a property defined by the predicate and a value for that property set by the object. RDF restricts which RDF terms can be used for subject, predicate and object:

Definition 2.2 (RDF Triple, RDF Graph). An RDF Triple is a triple $(s, p, o) \in (I \cup B) \times I \times RT$ where s is called subject, p is called predicate and o is called object.

A set of of RDF Triples is called RDF graph.

Example 2.1. An example of an RDF graph is given in Table 2.1. The data in the graph presents a list of pioneers along with their occupations and spouses. Table 2.2 defines the abbreviations used in the example.

We use a special language to retrieve data from an RDF graph called SPARQL. SPARQL [?] is a recursive acronym for “SPARQL Protocol And RDF Query Language”.

Listing 2.1 shows a simple example of a SPARQL query against the RDF graph in table 2.1.

| subject | predicate | object |
|--------------------|--------------------|--------------------|
| ex:PresidentOfUS | rdf:type | madsrdf:Occupation |
| ex:Professor | rdf:type | madsrdf:Occupation |
| ex:PoliticalParty | rdf:type | v:Organization |
| ex:RepublicanParty | rdf:type | ex:PoliticalParty |
| ex:DemocraticParty | rdf:type | ex:PoliticalParty |
| ex:AndrewNg | madsrdf:occupation | ex:Professor |
| ex:BarakObama | madsrdf:occupation | ex:PresidentOfUS |
| ex:GeraldFord | madsrdf:occupation | ex:PresidentOfUS |
| ex:BarakObama | ex:party | ex:DemocraticParty |
| ex:GeraldFord | ex:party | ex:RepublicanParty |
| ex:BarakObama | foaf:spouse | ex:DemocraticParty |
| ex:GeraldFord | foaf:spouse | ex:MichelleObama |
| ex:AndrewNg | foaf:spouse | ex:CarolEReiley |

Table 2.1: An RDF graph about a lama and a unicorn, what are their names and what they eat.

| abbr. | IRI |
|----------|--|
| rdf: | http://www.w3.org/1999/02/22-rdf-syntax-ns |
| madsrdf: | http://www.loc.gov/mads/rdf/v1 |
| ex: | https://www.example.com |
| v: | https://www.w3.org/TR/vcard-rdf/ |
| foaf: | http://xmlns.com/foaf/0.1/ |

Table 2.2: The list of abbreviations used in table 2.1.

Listing 2.1: A SPARQL query that returns the spouse of each US president whose party is the democratic.

```
SELECT ?spouse
WHERE {
    ?president madsrdf:occupation ex:PresidentOfUS .
    ?president ex:party ex:DemocraticParty .
    ?president foaf:spouse ?spouse }
```

Triple Stores

Triple Stores are a special kind of data management systems designed to store RDF triple data. It can store one or more RDF graphs. Generally, triple stores provide a standard interface to enable performing queries and other semantic operations on the stored RDF triples using a query language such as SPARQL (Sec. 2.4.1). Triple stores usually expose HTTP-based SPARQL endpoints for querying enablement. A triple store client can send a SPARQL query embedded in an HTTP request to the endpoint. The store evaluates the query against the RDF data it holds and return the results to the client in the body of an HTTP response in a format conforms to the system configuration.

2.5 Tentriss

There is no standard design guideline for triple stores. Hence different implementations of triple stores co-exist. Each subgroup of these implementations utilizes a category of underlying data structures as well as corresponding algorithms that govern the behavior. In production, triple stores are used to store up to billions of RDF triples. To that extent, quality factors like efficiency and scalability are considered first-class citizens during triple stores' construction. And the selection of internal data structures and the behavior definitions greatly influence the overall system efficiency.

Fuseki, Blazegraph, Virtuoso, and RDF-3X are popular implementations of Triple stores. One of the key design characteristics those triple stores have in common is that they all utilize B+ trees to store the indices. Other categories of triple stores use 3D Boolean tensors to store and process RDF data. In such systems, each tensor dimension is mapped to a triple data aspect, i.e., subject, predicate, or object. Examples of tensor-based triple stores include systems like TensorRDF and BitMat. In the following, a novel tensor-based RDF triple store is presented.

Tentris is a triple store variant designed by the data science research group at Paderborn university[3]. Tentris is an in-memory storage solution that represents RDF knowledge graphs as sparse order-3 tensors using a novel data structure, called Hypertire. It then uses tensor algebra to carry out SPARQL queries by mapping SPARQL operations to Einstein summation[?]. At the time of this writing, Tentris' SPARQL engine realizes *SPARQL-BGB* (a subset of the SPARQL-algebra). Consequently, the engine can execute SPARQL queries containing the following keywords: @prefix, SELECT, WHERE, and DISTINCT[?]. *mention that you omit talking about the query aspects: Einstein summation, etc*

Since my work represents a further contribution to the project Tentris, I dedicate this section to deliver a preface for the relevant aspects. In subsection 2.5.1, I specify what tensors are. A way of representing RDF graphs in tensors is showed in subsection 2.5.2. Hypertrie data structure is visited in subsection 2.5.3.

2.5.1 Tensor Algebra

In mathematics, the term Tensor holds a representation-independent meaning. According to [?], Tensors are “objects with many indices that transform in a specific way under a change of Basis”. This mathematical construct has many applications in physics, artificial intelligence, and other fields. However, for tensors to be applied in a practical context, a more concrete definition should be selected. Among other choices, multi-dimensional arrays are widely used as a representation of tensors. Throughout this work, a finite n -dimensional array for tensor representation is adopted. Tensor was defined formally in [3] as the following:

Definition 2.3 (Tensor). A mapping

$$T : \mathbf{K} \rightarrow V$$

from a multi-index \mathbf{K} to a codomain V is called tensor. \mathbf{K} is called *key basis* of dimension $n \in \mathbb{N}$ with

$$\mathbf{K} = K_0 \times K_1 \times \dots \times K_{n-1}, K_i \subset \mathbb{N}$$

The tuple $\mathbf{k} \in \mathbf{K}$ is called *key*, K_i is called a *key part basis* and $k \in K_i$ is called *key part*.

The dimension of the key basis is also called dimension of the tensor and is denoted by $\text{ndim}(T)=n$.

Further, $\text{nnz}(T) = |\{\mathbf{k} \in \mathbf{K} | T(\mathbf{k}) \neq 0\}|$ denotes the *number of non-zero entries*.

To resolve a value of a tensor, we use the array subscript notation $T[k_0, \dots, k_{n-1}]$. Moreover, the symbol $V^{\mathbf{K}}$ denotes the set of all mappings $T : \mathbf{K} \rightarrow V$. My work exclusively consider tensors T with \mathbb{B} or \mathbb{N} as codomain and only use multi-indexes $K_1 = \dots = K_n \subset \mathbb{N}$. An n -dimensional tensor is also called *order- n* tensor.

Example 2.2. In the following, some examples to illustrate the Definition 2.3:

1. A tensor $S \in \mathbb{Z}^\emptyset$ is called a *scalar*.

$$S = 1$$

So $S[\emptyset] = S[]$ is 1.

2. A tensor $X \in \mathbb{Z}^{\mathbb{N}_3}$ is called a *vector*.

$$X = \begin{bmatrix} 4 \\ 7 \\ 15 \end{bmatrix}$$

where $X[2]$ is 15.

3. Now, we take a three dimensional tensor $Y \in \mathbb{Z}^{\mathbb{N}_2 \times \mathbb{N}_2 \times \mathbb{N}_2}$. It can be visualized by a vector for the first key part which, in turn, has matrices each with dimensions corresponding to second and third key parts. As an example:

$$Y = \begin{bmatrix} \begin{bmatrix} 1 & 2 \\ 3 & 5 \end{bmatrix} \\ \begin{bmatrix} 7 & 11 \\ 13 & 15 \end{bmatrix} \end{bmatrix}$$

Such that, $Y[1, 0, 1]$ is 11.

Tensor Operations

This section highlights the core operations on tensors. In particular, I describe what tensor slicing and Einstein summations are. In the following, I skip the formal definitions of the operations, instead I present them informally with examples.

Slices Slicing is a useful operation to retrieve a well-defined portion of a tensor $T \in V^K$ in the form of a lower order tensor. Slicing is done by using a *slice key* $\mathbf{s} \in S = (K_0 \cup \{:\}) \times \dots \times (K_{n-1} \cup \{:\})$, and denoted like as we are retrieving a value but with one or more dimensions not bound, e.g. $T[:, x, :]$ (or $T[<:, x, :>]$). When applying the slice key \mathbf{s} to a tensor T , the unbounded dimensions in the slice key (the ones that are marked with $:$) are kept. A slice key part $s_i \neq :$ removes all entries with other key parts at position i and removes K_i from the resultant tensor domain. e.g., $T[:, 2, :]$ or $T[<:, 2, :>]$.

Example 2.3. Back to the third item in Example 2.2, slicing tensor Y by slice keys $s_1 = <:, 1, :>$ results in an order-2 tensor $Z_1 = Y[:, 1, :]$, and with a slice key $s_2 = <0, 1, :>$ results in an order-1 tensor $Z_2 = Y[0, 1, :]$:

$$Z_1 = \begin{bmatrix} 1 & 2 \\ 7 & 11 \end{bmatrix}$$

$$Z_2 = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$$

Worth to mention that, slicing operation is associative, meaning that applying a sequence of slicing operations with different grouping to tensor Y brings the same results:

$$Y[1, 0, :] = (Y[1, :, :])[0, :] = Y[:, 0, :][1, :] = Z_2$$

Einstein Summation Available in many software packages. Allow mutiple operation on different tensors (including vectors, matrices) Einstein Notation Example: Print Three arrays
Calculate the summation result (from the paper)

2.5.2 Storing RDF Graphs in Tensors

Based on [3], let g be an RDF graph with IRIs (I), blank nodes (B) and literals (L) being finite sets, and thus the set of RDF terms RT is also finite (Sec. 2.4.1). We define a bijective function $id_{RT} : RT \rightarrow N_n$ where $|RT| = n$. We call the function *index of resources*. id_{RT} maps each RDF term to a unique identifier. Similarly, we define the *resources by indices* function as $res_{RT} = id_{RT}^{-1}$. We omit the use of the subscript RT with the functions' names id_{RT} and res_{RT} when it is clear from the context.

Every triple $\langle s, p, o \rangle \in g$ is also in $(RT \times RT \times RT)$. For that, we can define an order-3 tensor $T \in \mathbb{B}^{N_n \times N_n \times N_n}$. We store the triple $\langle s, p, o \rangle$ in T by setting $T[id(s), id(p), id(o)] = 1$ and all other entries in T are set to 0. We call T the tensor representation of the RDF graph g and denoted by T_g . In other words:

$$T[i_s, i_p, i_o] = 1 \iff \langle res(i_s), res(i_p), res(i_o) \rangle \in g$$

Example 2.4. Figure 2.3 shows a 3D visualization of 3-dimensional tensor that represents the RDF graph g depicted in table 2.3. We notice that the number of distinct RDF terms in g is 7, so we can represent g with a tensor $T_g \in \mathbb{B}^{N_7 \times N_7 \times N_7}$.

Since T_g has the codomain \mathbb{B} , we describe T_g as a *boolean tensor*. Subject, predicate, and object are associated with one dimension each. In practice, a dimension range ($|RT| = n$) of an RDF tensor T_g fits much more than the bounded resources' IDs in g for that dimension. In [3], however, it is proven that by choosing equal key part basis for enable efficient dimension matching using Einstein notation. As T_g can store a super set of RDF triple in g , we call T_g a *sparse tensor*

| subject | predicate | object |
|---------|----------------|-----------------|
| :e1 (1) | foaf:knows (2) | :e2 (3) |
| :e1 (1) | foaf:knows (2) | :e3 (4) |
| :e2 (3) | foaf:knows (2) | :e3 (4) |
| :e2 (3) | foaf:knows (2) | :e4 (5) |
| :e3 (4) | foaf:knows (2) | :e2 (3) |
| :e3 (4) | foaf:knows (2) | :e4 (5) |
| :e2 (3) | rdf:type (6) | dbr:Unicorn (7) |
| :e4 (5) | rdf:type (6) | dbr:Unicorn (7) |

Table 2.3: An RDF graph example. Resources are printed alogn with their corresponding IDs (enclosed in brackets).

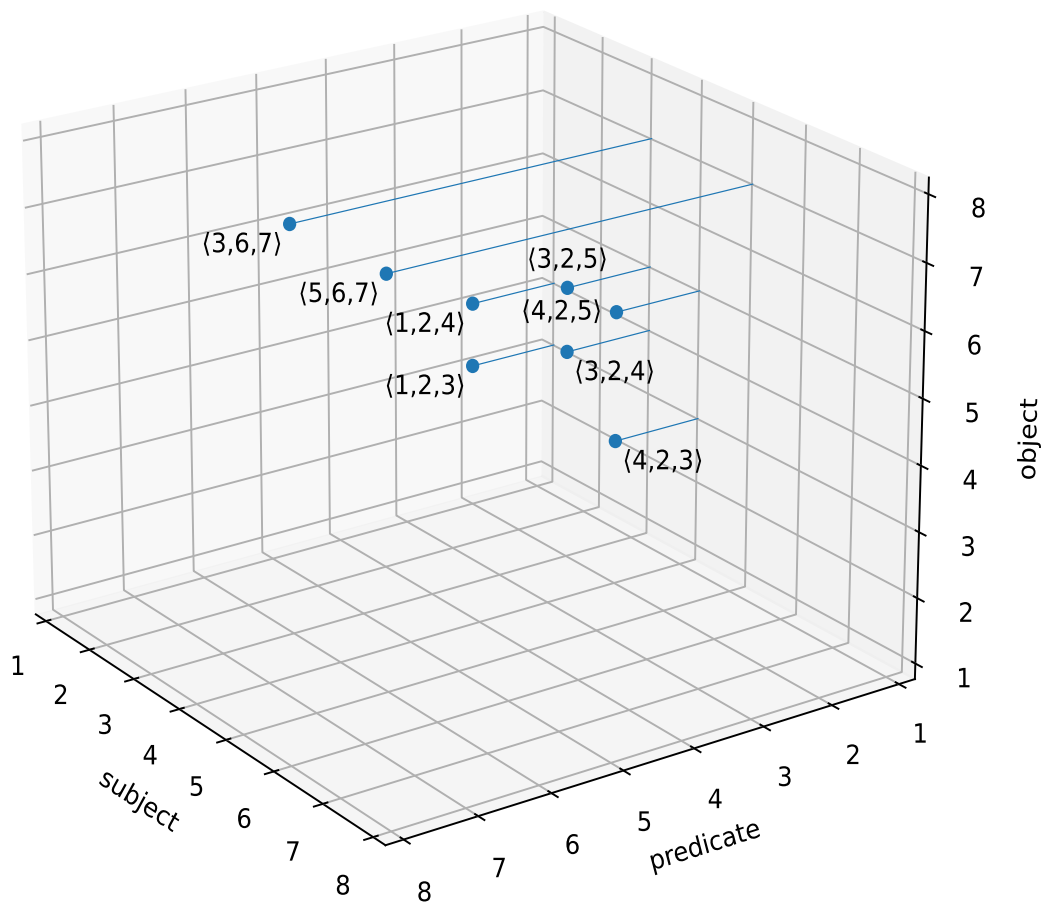


Figure 2.3: A 3D plot of an order-3 RDF tensor representing the RDF graph in table 2.3.

2.5.3 Tetrtris and Hypertrie

Underlying the order-d RDF tensor concept, Tetrtris realizes the concept using a novel data structure called Hypertrie. Before I discuss hypertrie structure, I first clarify how tensors storing RDF graphs can be represented as tries. Then, I show why this is not enough for our use case. **rephrase the concept.**

Trie

A *Trie* is a tree structure used to store *sequences of characters* from an alphabet \mathbb{A} . An example of an alphabet is the ASCII codes set. Sequences, in this case, are strings. A node in a Trie contains potentially one outgoing edge for each possible character. Each node in the tree corresponds to a prefix of some sequences of the set, so if the same prefix occurs several times, there is only one node to represent it.

A possible realization of a Trie node is to use a pointer array of the size $|\mathbb{A}|$. Each pointer points to either another trie node or null. Each array entry corresponds to a character in the alphabet. As an array lookup operation is computationally constant, looking up sequences in the Trie is fast and requires only $O(k)$ time where k is the sequence size. This approach, however, becomes space-inefficient as the size of the alphabet set increases or when it is infinite. An alternative way to represent edges is to maintain a hash table HT whose size will increase as we add distinct edges. The hash table keys corresponds to *edge labels* (characters) and are mapped to the node pointers (edges). Following that, the structure can still be used efficiently to retrieve sequences as accessing keys in a well-implemented sparse hash table is nearly constant.

A *fixed-depth trie* C is a trie that holds sequences of the same length n , termed as *keys*. In that case, a sequence $l = \langle l_0, \dots, l_m \rangle \in \mathbb{A}^m$ of length $m \leq n$ forms a *key prefix*. $C[l]$ is defined as the node that is reached from the root node r by walking along the nodes with edge labels equal to the entries of l . Hence, $C[l]$ could be undefined if no appropriate path exists. Moreover,

We can represent a tensor $T_g \in \mathbb{B}^{\mathbb{N}_n \times \mathbb{N}_n \times \mathbb{N}_n}$ that is used to store an RDF graph g with $|RT| = n$ (Sec. 2.5.2) using a fixed-depth trie C_{T_g} of depth $d = \text{ndim}(T_g) = 3$ with the alphabet \mathbb{N}_n . We call C_{T_g} a *trie tensor or trie representation of T_g* , if:

$$\forall \mathbf{k} \in \mathbb{N}_n \times \mathbb{N}_n \times \mathbb{N}_n, v \neq 0 : T_g[\mathbf{k}] = v \iff C_{T_g}[\mathbf{k}] = v$$

Resolving a tensor trie C_T of depth d by key prefix $l = \langle k_0, \dots, k_m \rangle$ where $m < d$ is equivalent to slicing the corresponding d -order tensor using a slice key $s = \langle k_0, \dots, k_m, e_{m+1}, \dots, e_d \rangle$ with $e_i = \cdot$. Then the resultant tensor slice $T[k_0, \dots, k_m, e_{m+1}, \dots, e_d]$ (d' -order where $d' = d - m$) is represented by an inner trie node or *subtrie* of depth d' .

In the context of this writing, the term *node depth* corresponds to the sequences length that a node holds. For a trie tensor C_T of depth d . The root node is assigned the depth d , an inner node holding prefix of size m , has the depth $d' = d - m$. Leaf nodes share the depth 1. An example of a trie tensor is showed in figure 2.4.

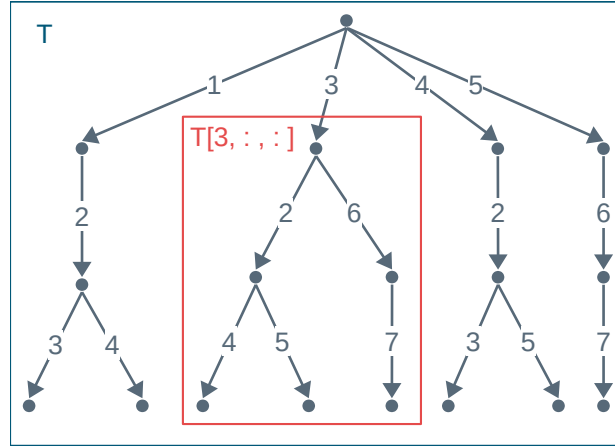


Figure 2.4: Trie representation of the tensor T_g that depicts the RDF graph g in Table 2.3. A slice $T_g[3, :, :]$ by the first dimension with 3 is shown in the red (inner) box.

Hypertrie

In the previous section we defined a trie as a data structure for realizing an order-3 RDF tensor. The structure is memory-efficient as it sparsely encodes a Boolean-valued tensor by storing only the keys that map to 1. As keys with the same key prefixes share the same node, a moderate level of compression is achieved. Slicing is also efficient if the set of edges to children are represented using a well-designed hashtable or search tree[?].

A trie, as defined earlier, however, still lack the ability for flexible slicing, that is by any combination of dimensions. The trie tensor as it is defined so far allows slicing positions to only suffix the slice keys, thus using $s = \langle :, 3, : \rangle$ as a slice key is not possible. Flexible slicing must always be maintained to enable resolving triple patterns (Sec. ???). Tentrism uses *Hypertrie*, a novel trie-based data structure, for holding the keys of an RDF tensor. Hypertrie generalizes the normal trie tensor concept by enabling the efficient slicing by any combination of dimensions. Hypertrie is defined formally based on Tentrism paper [3] in the following:

Definition 2.4. Let $H(d, A, E)$ with $d \geq 0$ be the set of all hypertries with depth d , alphabet A and values E . If A and E are clear from the context, we use $H(d)$. We set $H(0) = E$ per definition. A hypertrie $h \in H(1)$ has an associated partial function $c_1^{(h)} : A \rightarrow E$ that specifies outgoing edges by mapping edge labels to children. For $h' \in H(n), n > 1$, partial functions $c_i^{(h')} : A \rightarrow H(d-1), i \in \mathbb{N}_n$ are defined. Function $c_i^{(h')}$ specifies the edges for resolving the part equivalent to depth i in a trie by mapping edge labels to children. For a hypertrie h , $z(h)$ is the size of the set or mapping it encodes.

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Figure 2.5 shows a hypertrie storing the RDF triples shown in table 2.1. Examples for slicing hypertrie with different slice keys corresponding to various combinations of slicing positions is presented in figure 2.6.

add definition here as needed

Add the concept of node $processed_nodes : \mathbb{B}^3 \rightarrow node$

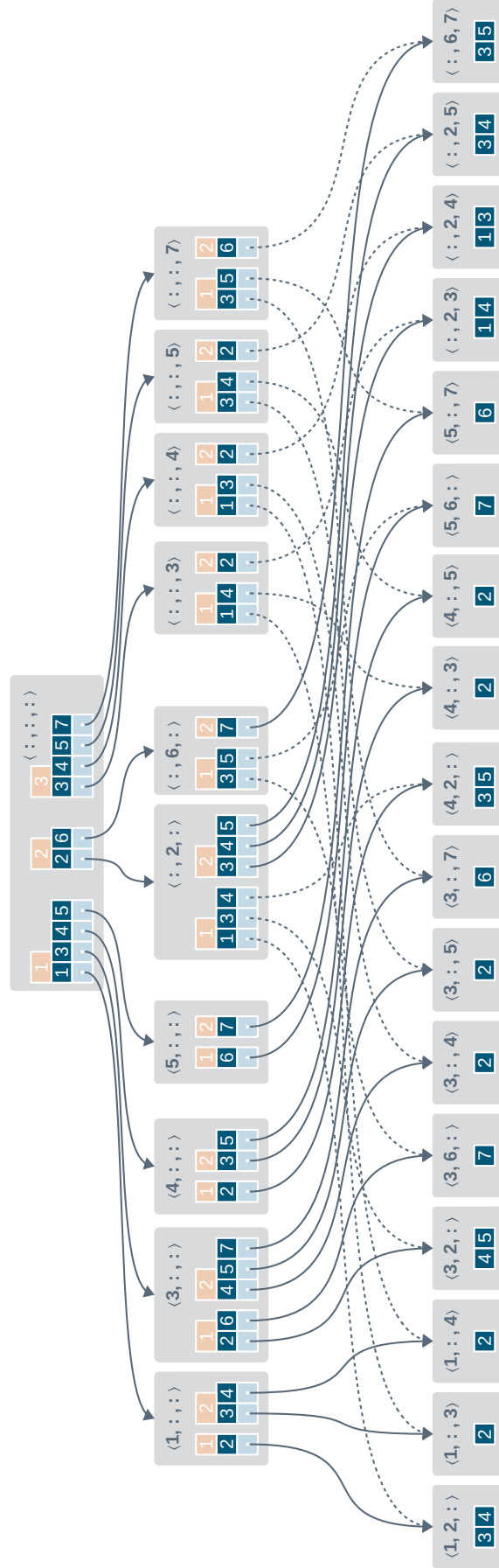


Figure 2.5: Trie representation of the tensor T_g that depicts the RDF graph g in Table 2.3. A slice $T_g[3, :, :]$ by the first dimension with 3 is shown in the red (inner) box.

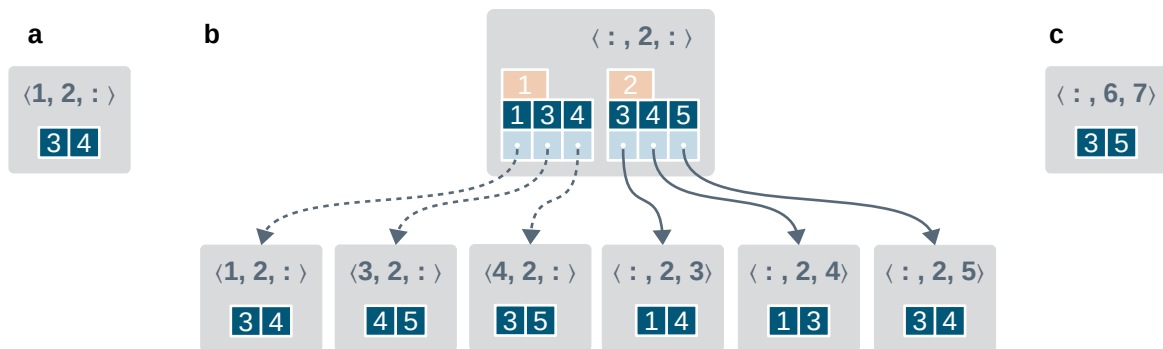


Figure 2.6: Slice.

Related Work

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Space Reduction Approach

This part of the thesis discusses the approach to substantially mitigate the space inefficiency characteristic of Hypertrie. The technique relies mainly on compressing a Hypertrie path with specific characteristics. Worth mentioning that the approach does not neglect the other attempts already realized to minimize Hypertrie memory footprint. In contrast, it can be considered an added feature that further contributes to the space reduction of the overall Hypertrie data structure.

In this chapter, I deliver a motivation to the approach. Afterward, I discuss the new Hypertrie internal nodes' design needed to realize the path compression feature. Finally, algorithms defining the behaviors of the newly designed Hypertrie are also presented.

4.1 Hypertrie Memory Utilization

Despite its operational efficiency, Hypertrie performance comes not without a trade-off. Since Hypertrie is a special kind of a Trie data structure, it inherits some of the fundamental problems of Tries. One of these problems is the excessive space utilization in a worst-case scenario.

The current design and implementation of Hypertrie, however, mitigates the space inefficiency characteristic in two ways. First, for each tensor dimension mapping in each node, the Hypertrie uses custom hash map data structures instead of arrays or linked lists to store the keys. By using a map, Hypertrie's nodes only store keys that form prefixes to already existed paths. In contrast, arrays utilization in normal Tries considers the whole alphabet set in each node with many array entries store pointers that refer to null.

The adoption of maps in Hypertrie also delivers extra performance as looking up keys in a carefully designed map is nearly constant compared to linked list search where it has a linear complexity $O(n)$. The other solution realized by Hypertrie to reduce the overall space requirement is to store equal nodes (Subhypertrie) only once. In this way, Hypertrie achieves a moderate level of compression in practice.

Despite the previously mentioned attempts to minimize the size of Hypertrie, the excessive memory requirement is still a bottleneck. The case can be witnessed when the set of RDF triples needed to be indexed by Hypertrie increases in size with less overlapping between its elements. As a result, many intermediate nodes store map with a single entry for a particular dimension

where the entry hosts a space for key and a pointer. This becomes a space redundancy issue when the leaf node referenced by the pointer has one key only.

The purpose of the following approach is to try to reach a more space-efficient Hypertrie. [Continue here](#)

4.2 Space Reduction Solution

The purpose of this section is to give a better intuition on the idea of path compression.

Assuming we want to store the set of RDF triples in listing 4.1, presented in Turtle syntax, in our space-efficient Hypertrie:

Listing 4.1: An example set of RDF triples

```
@prefix rel: <http://www.example.com/schemas/relationship/> .
@prefix ex: <http://www.example.com/schemas/entities/> .
@prefix xsd: <http://www.w3.org/2001/XMLSchema#> .

ex:Germany rel:capital ex:Berlin .
ex:USA rel:capital ex:Washington_DC
ex:USA rel:political_city ex:Washington_DC
ex:Germany rel:population "82.79e6"^^xsd:integer
```

Tentris do not store the actual values of RDF terms (RTs). Instead, it stores their associated identifiers. For generating identifiers, a bijective function $id : RT \rightarrow N$ is used. For the example of RDF data above, a possible mapping for the terms used is given below:

| <i>RT</i> | <i>id</i> |
|--------------------|-----------|
| ex:Germany | 17 |
| rel:capital | 4 |
| ex:Berlin | 30 |
| ex:USA | 20 |
| ex:Washington_DC | 40 |
| rel:political_city | 5 |
| rel:population | 6 |
| 82.79e6 (integer) | 35 |

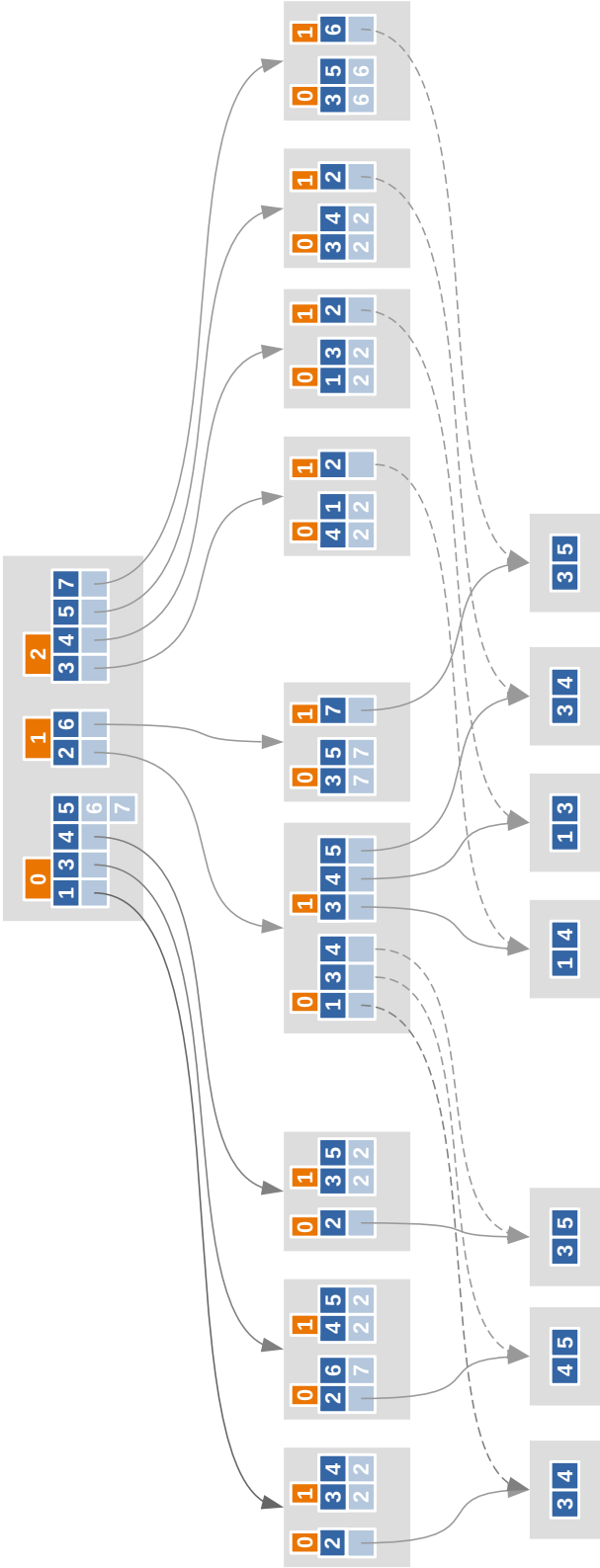


Figure 4.1: Storing RDF in space-efficient Hypertrie.

The Hypertrie will store the triple as shown in Figure ??, when the path compression technique is applied. It is straightforward to notice that many keys stored in the second level nodes (depth=2) do not need to be branched further to point to other nodes in the third level. As a result, the tree height is cut down, and a substantial amount of memory is saved by storing objects in-place instead of storing them on the heap.

So, the memory for the pointer to the object on the heap is saved. The same method is applied for the root node where keys for a specific dimension are branched by a *lonely path*, i.e. a key path where each element has a single child element.

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4.3 Compressed Hypertrie Nodes

In order to achieve path compression in Hypertrie, fundamental design changes need to take place. By that, we can enable the node to store the entire key suffix. Concretely, each group of Hypertrie nodes in certain tree depth will have their own internal node representation.

define key suffix

We create **Adaptive Hypertrie nodes**.

Concretely, each node must hold internal **containers** where key suffixes can be stored.

We reduce the space requirement of Hypertrie by collapsing Hypertrie nodes to.

From programming point of view, the redesign of Hypertrie nodes' structures is low level. Thanks to C++17 template meta-programming feature, we could separate the compressed nodes realization from the Hypertrie data structure interface. By that, we can still insure a smooth integrity of Hypertrie with other components in Tentris system.

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4.3.1 Internal Node Representations

Now I come to the part where the internal structure of space-efficient Hypertrie nodes are discussed. In my approach, it is a requirement to realize the container concept for each node¹. As a result, each inner node should still be able to expand at certain edges to sub Hypertrie nodes while maintaining a compressed key path in its bounded container for other edges.

The compressed key path container implementation varies depending on the node depth. The idea of having different internal representations comes from the fact that, based on the current structure of nodes on depth two, I found that there is no need to add an additional structure that serves as a container for the key path. Instead, I exploit the space dedicated to pointer value existed as a value in the hash table of store the compressed key path.

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Since Hypertrie's internal nodes can be either a root node or depth two nodes, we can distinguish two variants of internal node representations:

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structure

Depth 3 Node (root node)

In addition to the set of edges (hash tables) $HT_{3,p}$ for each position $p \in P = \{0, 1, 2\}$, the root node also holds another array of hash tables $CommHT_p$ that maps key parts k_j to static arrays

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Answer: Yes)

¹Leaf nodes are not considered.

arr_j . Each array will serve as the container for the key path prefixed by the associated key part k_j at the corresponding position p as depicted in Fig. 4.2. We call the edges k_j stored in $CommHT_p$ **compressed edges**. Clearly, a key part at a particular position p can either represent a compressed or non-compressed edge at a time, so it exists in either HT_p or $CommHT_p$. The remaining key path $k_S = \langle k_1, k_2 \rangle$ associated with each compressed edge k_j holds the key part chain ordered by their presence in the key.

Worth to mention that the key path associated with each compressed edge still represents a $2D$ sparse tensor S that results from slicing tensor T represented by the root node at position p with key part k_j . The resultant tensor S has a single entry $\langle k_1, k_2 \rangle$ that evaluates to 1. As a result, it is important to maintain the order of the elements in the compressed path arr_j as each key $arr[i]$ represents the single edge at position i in S whose child is the other array entry.

Depth 2 Node

Internal nodes with $d = 2$ realize the static container concept associated with compressed edges differently than for the root node. Considering the number of internal nodes, it becomes unfeasible, assigning an extra set of hash tables for each node that serve as key part chains containers.

To realize the container concept, we exploit the fact that key suffixes for edges in $d = 2$ $Node_2$ node comprise a single key part. Hence, we could reuse the space already booked to store the pointers to child nodes (leafs) to hold the suffixed key part. For the pointer ptr_j associated with the edge k_j to serve the purpose of either pointing to a child node or holding an integer value, we make it a tagged pointer (cf. 2.2).

Consequently, pointers to children that corresponds to edges k_j in $Node_2$ are denoted by $ptr_j = (value, tag)$. Such pointers carry two pieces of information. (1) A *value* is the actual payload of bits, which can be viewed as either a memory address or a raw integer value depending on the tag value. (2) A *tag* is the value held in the least significant bits (LSB) indicating whether the associated edge k_j is compressed or non-compressed. Figure 4.3 visualizes the structure.

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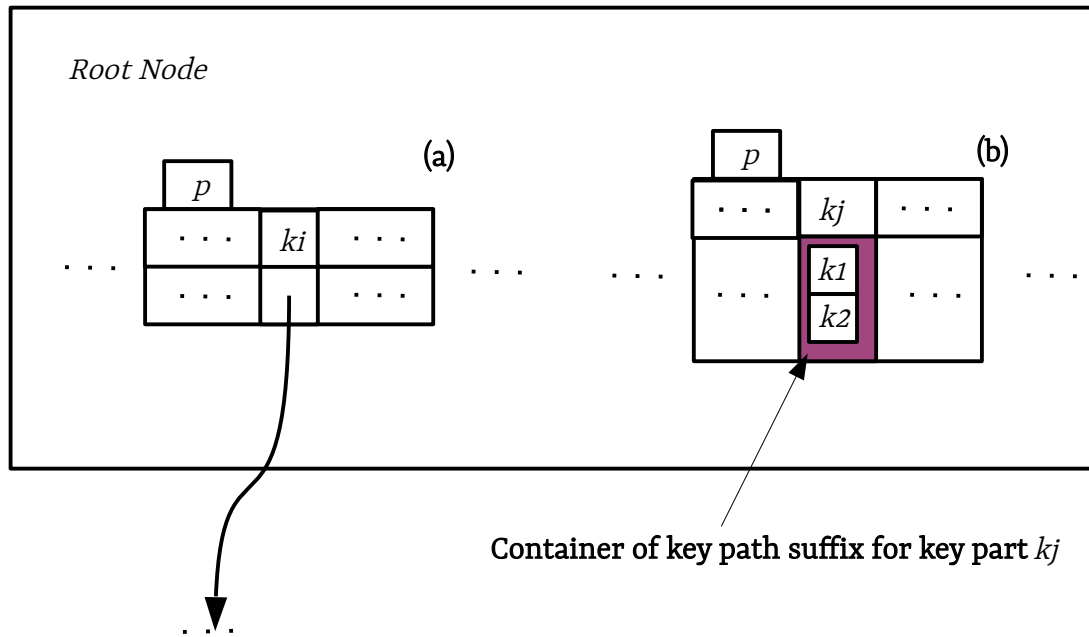


Figure 4.2: Depth 3 Node

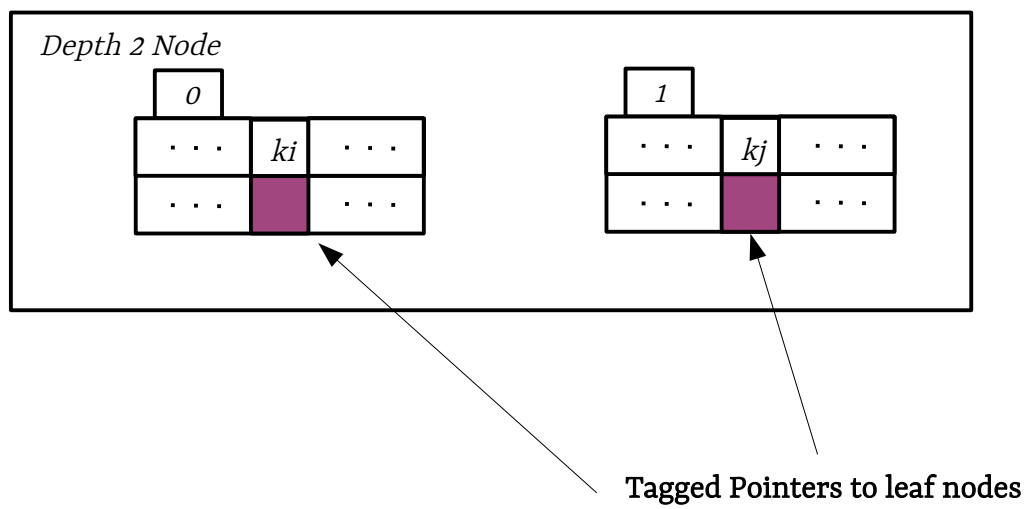


Figure 4.3: Depth 2 Node

4.3.2 Node Expansion

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4.3.3 Virtual Nodes

Due to the fact that some key paths in Hypertrie are collapsed into a single node of depth d , we still need to maintain the concept that collapsed path still represents a tensor of the order $d - 1$ with a single entry that evaluates to 1. Maintaining the concept becomes very important when we implement Hypertrie programmatically. In particular, when we want to perform slicing in the position of the collapsed path.

A straight forward solution is to return the container representation of the collapsed path (array, int value) from the slicing call. However, that contradicts with slicing function contract defined in the Hypertrie interface which states that slicing always return a child node. Also, following this approach will add extra code complexity in the context of handling the different types of returned values from slicing. It will also force us to define a different behavior for each returned type from slicing resulting in substantial amount of code redundancy.

A clean solution is to encapsulate the defined key path containers in a special type of Hypertrie nodes. Those nodes realize all the methods defined in the Hypertrie interface. As a result, we treat slicing operations uniformly. I call these wrappers **virtual nodes** to discriminate them from the actual Hypertrie nodes which I call **concrete nodes**.

Back to the previous sub section 4.3.1, I defined two types of key chain static containers. Concretely, a static array of length 2 representing the key suffix of compressed edges in the root node. A tagged pointer that bounds the key suffix (a single key part) of compressed edges in internal depth 2 nodes. Hence, we now have two variants of nodes for each depth (except for the root node). Concrete nodes and virtual nodes.

In the original Hypertrie implementation, slicing method gives enough information about the child node being returned from its execution as shown in listing 4.4. As we conceptually expanded the set of Hypertrie nodes to include virtual nodes, the pointer to a child node of a certain depth returned from a slicing must carry information about the nature of the node being concrete or virtual.

Listing 4.2: Slicing method signature defined for node where $d = \text{depth}$ in original Hypertrie

```
#include <array>

template<int depth>
class hypertrie_node {
    ....
    template<typename key_part_type>
    using SliceKey = std::array<std::optional<key_part_type>, depth>;
    ....
    template<int slice_depth>
    hypertrie_node<slice_count>* slice(SliceKey slice_key) {
        ....
    }
    ....
}
```

To accomplish this, we again use tagged pointers. This time, the pointer holds only a memory address of type `void *`. However, the tag here is used to distinguish between the referenced node being concrete or virtual. Accordingly, we can cast the the pointer value to the appropriate type based on the tag value. It becomes the responsibility of the slicing method to create and return that pointer properly. Listing 4.3 shows the structure of the tagged pointer I developed to reference different node types in our space-friendly Hypertrie.

Listing 4.3: Node pointer structure

```
template<typename VirtualNodePtr, typename ConcreteNodePtr, int alignedTo>
class NodePointer {
private:
    static const intptr_t tagMask = alignedTo - 1;
    static const intptr_t pointerMask = ~tagMask;

public:
    static constexpr int VIRTUAL = 1;

    static constexpr int CONCRETE = 0;

protected:
    union {
        void *asPointer;
        uintptr_t asBits;
    }

public:
    inline NodePointer(VirtualNodePtr ptr) {
        // Safer to clear the tag as we set a fresh tag in the setter method
        clearTag();
        asPointer = ptr;
        asBits |= VIRTUAL;
    }

    inline void clearTag() {
        asBits &= pointerMask;
    }

    inline NodePointer(ConcreteNodePtr ptr) {
        clearTag();
        asPointer = ptr;
        asBits |= CONCRETE;
    }

    /**
     * @param ptr it is already a tagged pointer
     */
    inline NodePointer(void *ptr) {
        asPointer = ptr;
    }

    inline NodePointer() {
        asPointer = nullptr;
    }
}
```

Listing 4.4: Slicing method signature defined for node where $d = \text{depth}$ in the space-friendly Hypertrie

```
#include <array>
```

```

template<int depth, bool virtual>
class hypertrie_node {
    ...
    template<typename key_part_type>
    using SliceKey = std::array<std::optional<key_part_type>, depth>;
    ....
    template<int depth>
    using NodePointer =
        TaggedPointer<hypertrie_node<depth, false>, hypertrie_node<depth, true>>;
    ....
    template<int slice_depth>
    NodePointer<slice_depth> slice(SliceKey slice_key) {
        ....
    }
    ....
}

```

4.4 Algorithms

The change in the internal nodes representations in the compressed version of Hypertrie leads to change in how we define its behavior. Hence, the new realization add the logic necessary to consider the compressed paths containers. At the same time, the logic has to have the same contract defined in the original Hypertrie interface. Following that approach will allow us to integrate the new Hypertrie implementation into the Tentris system efficiently.

Next, I list the main algorithms that realize the core behaviors of Hypertrie when the space reduction approach is applied. The great proportion of my work was on expanding the code base of Hypertrie project to adapt the key path compression approach including the implementation of the accompanying algorithms².

4.4.1 Key Search

A basic operation in Hypertrie is to check if a given $key \in N^d$ represents a path from a $Node_d$ to a leaf node where d is the node depth. In other words, if key is a non-zero entry in the tensor $T = h^{-1}(Node_d)$. Due to the presence of key path containers in internal nodes, the logic should be expanded to consider the children paths of both the compressed and non-compressed edges in each node.

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²In this section, I list only the main algorithms

Input: *node3*: a depth 3 node, *depth*: current node depth, *key*: array of key parts
 $k_i \in K_i$ of size 3

Output: a boolean if a key represents a path in Hypertrie

```

1 node3_key_retrieval(node3, depth, key)
2 begin
3    $p_{min} \leftarrow \text{minCardPos}(\text{node3})$ 
4    $k_i \leftarrow \text{key}[p_{min}]$ 
5    $\text{arr}_i \leftarrow \text{HTComm}_{p_{min}}[k_i]$ 
6   if  $\text{arr}_i \neq \text{NULL}$  then
7      $l \leftarrow 0$ 
8      $c \leftarrow 0$ 
9     while  $l < \text{depth}$  do
10      if  $l == p_{min}$  then
11         $l = l + 1$ 
12      else
13        if  $\text{arr}_i[c] \neq \text{key}[l]$  then
14          return false
15        end
16         $l = l + 1$ 
17         $c = c + 1$ 
18      end
19    end
20    return true
21  end
22   $\text{child}_i \leftarrow \text{HT}_{p_{min}}[k_i]$ 
23  if  $\text{child}_i \neq \text{NULL}$  then
24     $\text{subkey} \leftarrow \langle 0, 0 \rangle$ 
25     $l \leftarrow 0$ 
26     $c \leftarrow 0$ 
27    while  $l < \text{depth}$  do
28      if  $l == p_{min}$  then
29         $l = l + 1$ 
30      else
31         $\text{subkey}[c] \leftarrow \text{key}[l]$ 
32         $l = l + 1$ 
33         $c = c + 1$ 
34      end
35    end
36    return node2_key_retrieval( $\text{child}_i$ , 2, subkey)
37  else
38    return false
39  end
40 end

```

Algorithm 1: KEY RETRIEVAL IN THE ROOT NODE

Input: *node2*: a depth 2 node

depth: current node depth

key: array of key parts $k_i \in K_i$ of size 2 representing a sub key

Output: a boolean if a key represents a path in Hypertrie

```

1 node2_key_retrieval(node2, depth, key)
2 begin
3    $p_{min} \leftarrow \text{minCardPos}(\text{node3})$ 
4    $k_i \leftarrow \text{key}[p_{min}]$ 
5    $ptr_i \leftarrow HTp_{min}[k_i]$ 
6   if  $ptr_i == NULL$  then return false
7    $(value_i, tag_i) \leftarrow ptr_i$ 
8    $next\_pos \leftarrow (p_{min} + 1) \% 2$ 
9   if  $tag_i == INT\_TAG$  then
10    | return  $value_i == \text{key}[next\_pos]$ 
11  else
12    |  $subkey \leftarrow \langle \text{key}[next\_pos] \rangle$ 
13    |  $child_i \leftarrow \text{getPointer}(value_i)$ 
14    | return node1_key_retrieval( $child_i$ , 1,  $subkey$ )
15  end
16 end

```

Algorithm 2: KEY RETRIEVAL IN DEPTH 2 NODES

4.4.2 Key Insertion

Similar to other tree-based data structures, the key insertion operation is recursive. Due to the fact that nodes at certain depth enjoys a unique internal structure, the algorithm for adding keys will change depending on the target node in the recursion sequence. To achieve key insertion, two auxiliary constructs must be implemented. First, the algorithm should utilize a mechanism that keeps track of the processed key parts so far for each key path in hypertrie. A way to maintain such state information is to use a tuple $processed \in \mathbb{B}^3$, such that:

$$\forall i \in \mathbb{N}_3, processed[i] = \begin{cases} 1, & \text{key part at position } i \text{ is processed} \\ 0, & \text{otherwise} \end{cases}$$

Utilizing the state tuple $processed$ while processing a hypertrie node, we know the *sub key*, the remaining key parts to be added. Hence, the state tuple is updated as we proceed in the construction of the key path during insertion; i.e. processing more key parts.

For that, a couple of utility functions are used to map the main key to sub keys. That is, they map key part indices of the inserted key to dimensions represented by the succeeding child node and vice versa. By that, we know which key part should be inserted at which position. $pos2ids$ maps node positions to key part indices, and $id2pos$ maps key part indices to node positions. Both functions are defined in the following:

$$pos2id(pos, processed) = pos + |\{e | e \in \text{dom}(processed), e \leq pos, processed[e] = 1\}|$$

$$id2pos(id, processed) = id - |\{e | e \in \text{dom}(processed), e \leq id, processed[e] = 1\}|$$

The second requirement to achieve efficient insertion similar to the original hypertrie insertion method is to preserve the concept of pointing to equal child nodes only once. This is done by setting up a dictionary $processed_nodes : \mathbb{B}^3 \rightarrow \text{node}$ for each key insertion call. $processed_nodes$ maps instances of the state tuple $processed$ to inform which hypertrie nodes were already created for which combination of dimensions.

Input: $node3$: a depth 3 node, $depth$: current node depth, key : array of key parts

```

1 insert( $node3$ ,  $depth$ ,  $key$ )
2 begin
3    $processed \leftarrow \langle 0, 0, 0 \rangle$ 
4    $processed\_nodes \leftarrow \{\}$ 
5    $node3\_insert(node3, depth, key, processed, processed\_nodes)$ 
6 end
```

Algorithm 3: KEY INSERTION MAIN METHOD

Input: *node3*: a depth 3 node, *depth*: current node depth, *key*: array of key parts, *processed*: state of processed keyparts, *processed_nodes*: dictionary of processed nodes

```

1 node3_insert(node3, depth, key, processed, processed_nodes)
2 begin
3   foreach key_pos in {e | e ∈ dom(processed), processed[e] = 0} do
4     key_part ← key[key_pos]
5     pos ← id2pos(key_pos, processed)
6     next_processed ← processed
7     next_processed[key_pos] = 1
8     child_ptr ← get(node3, pos, key_part)
9     (child, tag) ← child_ptr
10    if child is empty then
11      arr ← [0, 0]
12      for i in [0, 1] do
13        | arr[i] = key[pos2id(i, next_processed)]
14      end
15      HTComm_pos[key_part] = arr
16    else if tag == NON_COMPRESSED then
17      | node2_insert(child, 2, key, next_processed, processed_nodes)
18    else if tag == COMPRESSED then
19      | new_node ← create a new concrete hypertrie child node of depth 2
20      | HT_pos[key_part] = ptr(new_node)
21      | node2_insert(new_node, 2, key, next_processed, processed_nodes)
22      | reconstructed_key ← < 0, 0, 0 >
23      | arr ← HTComm_pos[key_part]
24      | for i in [0, 1, 2] do
25        | if i == key_pos then
26        | | reconstructed_key[i] = key_part
27        | else
28        | | reconstructed_key[i] = arr[id2pos(i, next_processed)]
29        | end
30      | end
31      | erase HTComm_pos[key_part]
32      | node2_insert(new_node, 2, reconstructed_key, next_processed, processed_nodes)
33    end
34  end
35 end

```

Algorithm 4: KEY INSERTION FOR DEPTH 3 NODE

4.4.3 Slicing

| Dataset | #T | #S | #P | #O | Type |
|---------|-------|------|------|-------|------------|
| SWDF | 372 k | 32 k | 185 | 96 k | real-world |
| DBpedia | 681 M | 40 M | 63 k | 178 M | real-world |
| WatDiv | 1 G | 52 M | 186 | 92 M | synthetic |

Table 4.1: Numbers of distinct triples (T), subjects (S), predicates (P) and objects (O) of each dataset. Additionally, Type classifies the datasets as real-world or synthetic.

4.4.4 Diagonal

4.5 Storage Discussion

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ation

Best case is easy. all triples are stored in the root node??? During the evaluation phase, I will prove that the performance of the space efficient Hypertrie is at least as much as the performance of the base (reference) Hypertrie. The compressed Hypertrie is **cache-conscious**. That is the frequently accessed compressed key paths suffixes stored at the root node in array-based containers will increase the probability that those paths resides within cache.

]

How much data compression does the Hypertrie achieve due to applying the space reduction approach presented earlier? Does the new data structure compromise the overall efficiency, more specifically, the query processing speed? On the one side, this chapter describes the space-friendliness of Hypertrie by presenting the compression ratio achieved w.r.t. the original Hypertrie after the bulk loading with different RDF data sets is done for both Hypertrie variants. On the other side, we have a look at how the space enhanced Tentrism can still maintain its proven efficiency. For that, I ran a series of benchmark experiments on real RDF data and queries.

As this work's effort is mainly toward enhancing the Tentrism system in the context of space cost, all the experiments consider only the original Tentrism's Hypertrie as the reference for comparison opting out other triple store systems. The experimental setup is described in section 5.1. In the succeeding section 5.2, the results are presented.

5.1 Experimental Setup

5.1.1 Data Sets and Queries

I used three different RDF data sets to assess the performance (load time/ size) of the compressed Hypertrie. Concretely, I used Semantic Web Dog Food SWDF (372K triples) as well as the English DBpedia 2015-10 (681 M triples) as real-world data sets. I also chose the 1 billion-triple synthetic data set from WatDiv (see Table 5.1). All the three data sets were used during the size/load speed assessment. However, only SWDF and DBpedia data set were incorporated into the benchmarks.

5.1.2 Test Environment

I used the server machine "Geiser" provisioned and maintained by the data science research group at Paderborn university to run all the experiments. The server machine has two Xeon E5-2683 v4 CPUs and 512 GB of RAM. Geiser runs Ubuntu 18.04.4 LTS 64-bit on Linux Kernel 4.15.0-112-generic with Python 3.6.9 and OpenJDK Java 11.0.8 installed¹. The benchmark tool and the Tentrism triple stores (compressed/ non-compressed) were installed locally on a single

¹The server specification may change in the future. However, by the time of the document submission date, the spec mentioned here holds.

| Dataset | #T | #S | #P | #O | Type |
|---------|-------|------|------|-------|------------|
| SWDF | 372 k | 32 k | 185 | 96 k | real-world |
| DBpedia | 681 M | 40 M | 63 k | 178 M | real-world |
| WatDiv | 1 G | 52 M | 186 | 92 M | synthetic |

Table 5.1: RDF datasets which were used throughout the evaluation phase. Numbers of distinct triples (T), subjects (S), predicates (P) and objects (O) of each dataset. Additionally, Type classifies the datasets as real-world or synthetic.

server instance to avoid network latency. Data sets held in N-Triples format (`.nt` files) were uploaded to the server and stored on disk.

5.1.3 Bulk Loading

Generally, bulk loading is the activity of loading a large volume of data into a data storage system (database, triple store, etc.) mainly in one call, thus in a relatively small amount of time. There are many use cases in which bulk loading could apply; one example is data import/ export. In this work context, bulk loading is used to load an entire RDF graph into Tentriss; thus, it can calculate its memory footprint and the time to load. During the bulk loading experiment, all the three RDF datasets (Sec. 5.1.1) were involved for each variant of the triple stores (compressed, non-compressed). I also expanded the load test to check the space utilization performance of the compressed Hypertrie as the dataset scales. For that, I used generated WatDiv synthetic datasets with increasing scale factors: [10, 100, 1000, 10000]. The bulk loading tests' results were calculated using a set of utility methods inside the Tentriss project. Those utilities rely on built-in functions inside C++ language, which interface low-level system services and data to their clients.

Calculating Size

There are many methods to calculate memory utilization of processes or data structures residents. Each method fits a set of use cases and they can vary with accuracy. For the case at hand, I relied on the `proc` virtual file system in the server instance that ran the experiments. Given that, "The `proc` filesystem is a pseudo-filesystem which provides an interface to kernel data structures. It is commonly mounted at `/proc`. Typically, it is mounted automatically by the system, but it can also be mounted manually" ². The content of the files inside `proc` has mostly the status of *read-only* as the files are written by the kernel. For each process (with a process id *pid*) currently running in the linux system, there exists a subdirectory `/proc/[pid]`. Underneath each subdirectory `/proc/[pid]`, there are a set of files and subdirectories disclosing meta-information about process with *pid*. The file `/proc/[pid]/status` provides status information about the process including various memory consumption information. The information are provided in a human-readable fashion.

After a single bulk load experiment is finished, Tentriss access the corresponding status file; i.e. `/proc/self/status` where the magic symbolic link `self` is automatically evaluated to Tentriss' process ID. The field `VmRSS` inside `Status` file provide the current memory utilization of the resident Tentriss process including the sizes of resident anonymous memory, resident file mappings and resident shared memory.

²<https://man7.org/linux/man-pages/man5/proc.5.html>

Calculating Load Time

A simple tic-toc approach is adopted to calculate the load speed of RDF graphs into Tentriss. More specifically, two start and end time flags are setup immediately before and after the actual loading of keys. The difference between the time checkpoints is then calculated to capture the load speed.

The time checkpoints calculation utilized `steady_clock` instead of `system_clock`. As `system_clock` talks periodically to machine clock to correct itself, it might make minor timing mistakes. As `steady_clock` is independent from the system clock, thus providing more reliable timing insights.

5.1.4 Benchmark Execution

For executing the benchmark, I used the generic SPARQL benchmark execution framework IGUANA v3.0.0-alpha2 [4]. IGUANA is a benchmark suite for executing benchmarks. It takes a benchmark, namely a data set and a possible list of SPARQL queries/updates, as input. Then it simulates a SPARQL user that pushes a series of queries repeatedly in a stress test scenario to a SPARQL endpoint where the next request is sent immediately after returning the last response. IGUANA can execute both synthetic benchmarks and benchmarks based on real data. As part of its execution, the suite returns information on the respective triple store's different behavioral aspects, such as query processing speed for each query and the query result's size. The framework enables different benchmark execution options and fashions (measure performance of triple stores under updates, parallel user requests, etc ...). As Tentriss provides an HTTP-based SPARQL interface, I used the HTTP-based benchmark with one user as a benchmark setup. The suite returned the average response time for each query, and the query result's size to consider later for comparison.

5.2 Results

Conclusion

Parallelization Different types of containers Different types of compression methods

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