

Channel Assignment Optimisation Using a Hyper-heuristic

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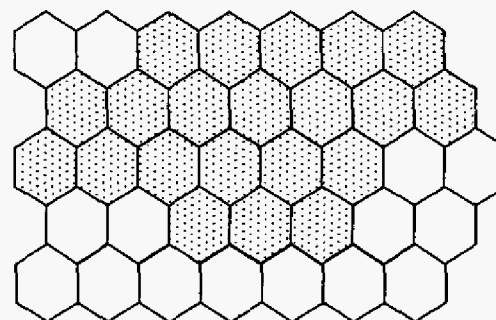
Abstract - The channel assignment problem is a real world problem from the mobile communications industry. The primary objective is to find the minimum frequency bandwidth given different traffic demand distribution within the mobile network. Besides fulfilling the channel demand requirement, we must also consider the minimum channel reuse distance in order to avoid the effect of call interference within the same cell or adjacent cells. Previous approaches have used graph-colouring algorithms, heuristic search, neural networks, simulated annealing and genetic algorithms (GA). In this paper, we propose a hyper-heuristic methodology and compare our approach against channel assignment problems from the literature.

Index Terms— Channel Assignment, Mobile communication, Adaptive heuristic Search, hyper-heuristic, optimisation.

1. INTRODUCTION

The technology supporting mobile communications has grown tremendously and continues to do so. The key aspect of this growth is due to the popularity of mobile communications, which is the ability to provide instant connectivity anytime and to anywhere in the world. Starting from an analog standard (known as 1st generation), we can see the full migration from an analog into a digital standard (known as 2nd generation) throughout the world. The 2nd generation mobile standard (GSM, D-APMS and CDMA), with high quality voice and the capability to provide high-speed data services to the mobile user as an additional service, are the driving factors behind the high growth of sales in communication technology. The mobile communication has recently introduced a 3rd generation mobile wireless technology with the aim to have a global standard for all applications and countries.

The Federal Communications Commission (FCC), in their respective countries, controls the operating of mobile telephone networks and they issue licenses to mobile operators, which means the mobile operators, are allowed to use only the frequency bandwidth allocated to them. The allocated frequency bandwidth is divided into sets of carriers or channels using different techniques such as frequency division (FD), time division (TD), or code division (CD), which each channel uses for call establishment.



n : Cell Number; d : Channel demand

Fig. 1 : Typical 21 Cells Mobile Network [1]

Mobile users in a particular cell use the channel that is allocated at the base station. A channel can simultaneously be used at another base station, subject to a minimum reuse distance, i.e., there is enough distance between the base stations in order to provide interference free communication.

In mobile communication, all the information from mobile sets (MS) to the base stations (BS) travels via radio channels. The geographical area covered by a BS is a cell. This can be represented as a hexagonal network (refer to Figure 1 [1]). A mobile communication network consists of thousand of cells in order to cover the required region, each with a BS at the centre. Each BS will have a dedicated radio channel and the number of the channels assigned will be based on the traffic requirement for the particular cell (for example, there will be a higher channel demand in metropolitan areas compared to suburban areas).

Besides the traffic demand requirement, the assignment of radio channels is subject to the three types of interference constraints;

a) **channel constraint.** The same channel cannot be allocated to certain pairs of radio cells simultaneously. For example consider Fig. 1. Assuming we have mobile set i , that uses channel k in cell 17; the same channel, k can simultaneously be used in cell 17' by another mobile set j , if mobile set, i and mobile set, j are separated by minimum reuse distance (in this case 3).

b) **Adjacent channel constraint.** The same adjacent channel cannot be allocated to adjacent radio cells simultaneously. Assuming we have mobile set i , that uses channel k in cell 17, if, we have mobile set, l , that uses channel g in an adjacent cell (say cell 9), we can comply with adjacent channel constraint if channel k and channel g are separated by a minimum channel separation distance.

c) **Cosite constraint.** Any pair of channels assigned in the same cell must be separated by a minimum channel separation distance.

The channel demand distribution over the whole region of a mobile network varies from cell to cell, according to a nonuniform distribution of business and social activities [1]. In Fig.1, we can see the highest channel demand is 77 channels at cell 9 and the lowest channel demand is 8 for several cells (1,3,4,etc). Mobile operators have to fully utilise a given limited spectrum bandwidth, which can satisfy mobile customers by avoiding or minimising call blocking especially in high channel demand cells (cell 9,16,etc.). With a limited frequency spectrum allocated to the system, the efficiency in which of radio channels are assigned is very important to overcome congestion problems in the network.

The assignment of radio channel is generally called the Channel Assignment Problem (CAP). The CAP can be viewed as a combinatorial optimisation problem, with the difficulty of CAP increasing exponentially with the problem size. There are three kinds of channel assignment; Fixed Channel Assignment (FCA), Dynamic Channel Assignment (DCA) and Hybrid Channel Assignment (HCA) [2]. In FCA, the radio channels are assigned permanently to each cell based on a predefined channel demand. In DCA the channels are dynamically assigned to cells based on channel requests. DCA provides flexibility and traffic adaptability at the cost of higher complexity, but under heavy traffic conditions, DCA strategies are less efficient compared to FCA [3]. Since heavy traffic condition is expected in the future, the efficiency of an FCA scheme is highly desirable [2]. HCA is a combination between FCA and DCA. In this paper, we will consider only FCA schemes.

Mobile customers can make a call using a channel of the cell in which the user is currently situated. Under heavy traffic conditions, the network planning engineers have to reduce the cell size (cell splitting) and use advanced antenna technology in order to cater for the increase in channel demand. This causes the number of base stations to increase. Under FCA, the CAP objective is to optimise the assignment of the limited channel resources to a base station without ignoring service quality such as cochannel and adjacent interference. Using an exhaustive search strategy, the optimum result could be obtained, but as the number of base station increases, finding an optimum solution is extremely difficult [4].

In this paper, we will introduce a hyper-heuristic approach to tackle this problem and present computational results.

II. RELATED WORK

The channel assignment problem continues to be an active research area [5]. Previous approaches to solve CAP can be categorised as approaches using graph theory [6], heuristics [1,7, 8, 9], local search [10], neural networks [11, 12, 13], the utilisation of simulated annealing [14] and genetic algorithms [15].

Graph theory approaches used the sequential assignment of channels based on assignment difficulty. Zoellner and Bell [6] used a frequency-exhaustive strategy or a requirement-exhaustive strategy to assign a channel to cells which were ranked in node-degree order or node-colouring order.

Using an heuristic approach, Box [7], used the principle of *assignment difficulty* to arrange the cell sequence or ordering. With this sequence, he used a simple iterative method to assign the channel. Sivarajan *et. al* [9], produced eight CAP algorithms by ranking the calls in row-wise ordering or column-wise ordering and the cells in node-degree order or node-colouring order. With each rank, they used a requirement exhaustive strategy and a frequency exhaustive strategy to assign the channel. Chakraborty [1] proposed an algorithm for generating a pool of valid solutions. He claimed that the algorithm is very fast and could find optimum or near optimum solutions.

Wang and Rushforth [10] used a local search approach. In the feasible region R with the current solution X_c , the next solution X_{c+1} will be accepted if the cost function $f(X_{c+1}) < f(X_c)$. Based on benchmark test results, this approach produced superior results to those reported in the literature.

A neural network approach was proposed by Kunz [11] and the result was improved by Funabiki and Takefuji [12]. Subsequently, Kim *et. al* [13], proposed a modified discrete Hopfield neural network in order to escape from local optima. They formulated CAP as an energy-minimisation problem and claimed that the performance is better when compared to previous approaches. The simulated annealing approach [14], guarantees to find the global optimum but with the disadvantage that the rate of convergence is slow.

A genetic algorithm approach was proposed by Lai and Coghil [15] who investigated the channel assignment problem using a computational technique that mimics the evolutionary process. The primary goal in solving CAP is to satisfy cosite and cochannel constraints and satisfy all channel demands required by each cell. They used a string structure to represent the channel required for each base station, where the total length of each string is the sum of channels required. The evolutionary process uses partially matched (PMX) crossover and basic mutation, with two extra parameters in order to bias cosite and cochannel constraints in their fitness function. They claim that their approach is elegant and simple.

III. PROBLEM DEFINITION

Frequency bandwidths are allocated to cellular service providers with a range of $[b_{min}, b_{max}]$ [16]. The bandwidth is partitioned into a set of channels, F (or often called frequencies) and can be represented as positive integers 1, 2,

3, ..., f_{max} where f_{max} is a maximum channel number. A basic channel assignment problem for radio network planning consists of (mostly adopted from [9] and [10])

- N : The number of cells in the network.
- D : demand vector, $D = (d_1, d_2, \dots, d_N)$ where d_i : the number of radio channel required in cell i in order to satisfy channel demand.
- C : Compatibility matrix, $C = (c_{ij})_{N \times N}$ denotes the frequency separation required between cell i and cell j .
- $Call_{ik}$: Cell i with call k where $1 \leq i \leq N$, $1 \leq k \leq d_i$.
- f_{ik} : A radio channel is assigned to $Call_{ik}$, where $f_{ik} \in F$.
- Frequency separation constraint - $|f_{ik} - f_{jm}| \geq c_{ij}$, for all i, j, k, m ($i \neq j, k \neq m$), c_{ij} is defined in Compatibility Matrix, C . If $i=j$, it's become co-site constraint.

Therefore, the channel assignment problem (CAP) is a task to find the minimum bandwidth (span) required by the system i.e.:

Given N, D, C ,

Span, $f(s) = (f_{ik_{max}} - f_{ik_{min}})$ is minimised.

where $f_{ik_{max}} = \text{maximum channel used}$

$f_{ik_{min}} = \text{minimum channel used}$

IV. THE ALGORITHM

A. Hyper-heuristic

We propose using a hyper-heuristic approach to solve the channel assignment problem. A hyper-heuristic is a knowledge poor meta-heuristic that does not use problem specific information [17]. Based on non-domain information, such as CPU time, change in the objective function etc., a hyper-heuristic will decide which low level heuristic to call at each decision point. In order to implement the search, we may use simple neighbourhood heuristics such as delete, add and swap. The advantages of using a hyper-heuristics for practical scheduling and indeed optimisation problems are (mostly adapted from [18]):

- It is easy for the problem owner to consider their problem by modeling it using simple heuristics.
- Simple heuristics are typically faster to implement compared to some other approaches.
- It is robust enough to effectively handle a wide range of problem instances by small modifications or additions.

Hyper-heuristics operate at a higher level of abstraction than meta-heuristics by managing a set of low level heuristics (LLH). The general framework can be shown in figure 2 [17].

Hyper-heuristics are problem independent and have been successfully applied to various optimisation and scheduling problems [19,20,21,22]. For example, a genetic algorithm hyper-heuristic [20] used an allele in a chromosome to represent each LLH. The quality of the solution is evaluated based on the sequence of calls within the chromosome. In [21], a Monte Carlo hyper-heuristic approach is used to optimise the scheduling of electrical component placement on

a printed circuit board. They used an acceptance criteria to determine solution quality returned by each LLH.

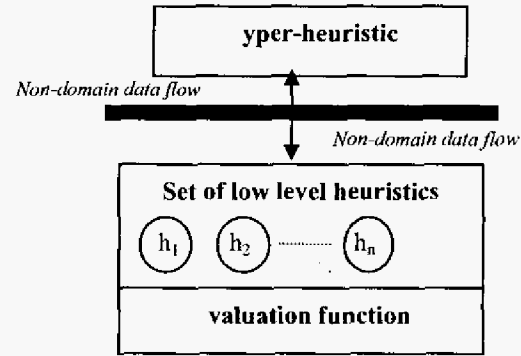


Figure 2: A Hyper-heuristic Framework

Another approach has used a tabu list to monitor the performance of each LLH in solving an examination timetabling problem [22]. The choice function hyper-heuristic [23] ranks the solution quality performance of each LLH. Based on the quality of the previous result; the hyper-heuristic will decide which LLH should be called next.

Let us use the local search framework to define:

Solution Space, S : The set of possible ordered list of calls.

Objective function: $f(S_{max}) \in F$, the maximum frequency for solution $S_{max} \in S$.

N : neighbourhood structure.

H : A set of Low Level Heuristic (h_1, h_2, \dots, h_n)

The hyper-heuristic algorithms is as follows:

Step 1: (Initialisation)

(A) Choose Initial solution $S_0 \in S$;

(B) Record the best obtained solution, $S_{best} = S_0$ and $f(S_{best}) = f(S_0)$;

Step 2: (Choice and termination)

(A) Randomly choose an $h_c \in H$;

(B) Apply h_c to produce $S_c \in N(S_0)$;

(C) Compute $\delta = f(S_c) - f(S_0)$;

(D) If the acceptance criteria is true, then accept S_c (and proceed to Step 3);

(E) If S_c is rejected and stopping condition=false, then return to Step2(A);

(F) Terminate by a stopping condition.

Step 3: (Update)

Re-set $S_0 = S_c$, and if $f(S_c) < f(S_{best})$, perform Step1(C).

Return to Step2 if stopping condition=false.

B. List of Low level heuristic (LLHs)

Low level heuristics are defined as simple local search operators, which are problem dependent. In this work, we randomly call LLHs to generate a unique move from the current solution to the new solution. The list of LLHs that we use are shown below:

quadnary representation $[0,+1,-1,+9]$, which means [assignable,used,unassignable,unused].

Another comparison is with recent work by Ghosh *et al.* [26], in which they use a genetic algorithm based on geometric symmetry. We run our experiments for 400 seconds for each benchmark problem.

Using a random constructive heuristic to generate an initial solution and using 'runtime expired' as our stopping criteria, we ran each experiment 10 times. By applying our approach we were able to achieve promising results as presented in table III (*AM* and *OI*) and table IV (*MC* and *RRT*).

Test	C_Matric(C)/ Demand(D)	Trivial Lower Bound	Initial solution	Chakraborty [1]	Ghosh et al. [26]	AM Hyper-heuristic (span/ % improvement)	OI Hyper-heuristic (span/ % improvement)
1	C4_21/D1_21	457	622	457	-	457/26.5	457/26.5
2	C4_21/D2_21	265	337	280	-	272/19.2	270/19.8
3	C6_21/D1_21	381	595	463	427	448/24.7	446/25.4
4	C6_21/D2_21	221	316	273	253	268/15.2	266/15.8
5	C7_21/D1_21	305	353	305	-	305/13.6	305/13.6
6	C7_21/D2_21	177	226	197	-	185/18.1	184/18.5
7	C8_21/D1_21	305	507	465	-	447/11.8	442/12.8
8	C8_21/D2_21	177	320	278	-	275/14.1	272/15.0
9	C1_25/D3_25	21	78	73	-	73/6.4	73/6.4
10	C1_25/D4_25	89	209	121	-	200/4.3	200/4.3
11	C1_55/D5_55	309	336	309	-	309/8.0	309/8.0
12	C1_55/D6_55	71	98	79	-	73/25.5	72/26.5

TABLE III : AN AVERAGE RESULT OF TEN RUNS FOR *ALL MOVES* AND *ONLY IMPROVING*

Test	C_Matric(C)/ Demand(D)	Trivial Lower Bound	Initial solution	Chakraborty [1]	Ghosh et al. [26]	MC Hyper-heuristic (span/ % improvement)	RRT Hyper-heuristic (span/ % improvement)
1	C4_21/D1_21	457	622	457	-	457/26.5	.
2	C4_21/D2_21	265	337	280	-	270/19.8	.
3	C6_21/D1_21	381	595	463	427	443/25.5	.
4	C6_21/D2_21	221	316	273	253	266/15.8	.
5	C7_21/D1_21	305	353	305	-	305/13.6	.
6	C7_21/D2_21	177	226	197	-	184/18.6	.
7	C8_21/D1_21	305	507	465	-	444/12.4	.
8	C8_21/D2_21	177	320	278	-	274/14.4	.
9	C1_25/D3_25	21	78	73	-	73/6.4	.
10	C1_25/D4_25	89	209	121	-	200/4.3	.
11	C1_55/D5_55	309	336	309	-	309/8.0	.
12	C1_55/D6_55	71	98	79	-	72/26.5	.

TABLE IV : AN AVERAGE RESULT OF TEN RUNS FOR *MONTÉ CARLO* AND *RECORD-TO-RECORD TRAVEL*

VI. DISCUSSION

When we compare the results in Table III and table IV, we can see that the performance of the *RRT* hyper-heuristic is superior compared to the other approaches. This suggests that by controlling the margin of the acceptance solution quality, it will lead to better results. In *RRT*, if the solution quality is worse, compared to the incumbent solution, but within the 'margin limit', it will become a new configuration for the next iteration.

When we compare test 3 and test 4 which are the most difficult benchmark problems, even though our proposed algorithms cannot beat the existing result from [26], their solution took between 16-80 hours to produce such good quality solutions. Our result is promising especially for *RRT*,

which is achieving an improvement of 26% and 17% when compared to the initial solution.

For other test problems, when we compare our result with constructive heuristics as proposed in [1], all our proposed hyper-heuristic manage to find a better solution except for test 10.

VII. CONCLUSIONS AND FUTURE WORK

The channel assignment problem is a real world problem from the mobile communications industry. The primary objective is to find the minimum frequency bandwidth given different traffic demand distribution within the mobile network. Besides fulfilling the channel demand requirement, we must also consider the minimum channel

reuse distance in order to avoid the effect of call interference within the same cell or adjacent cells.

In this work, we have proposed a hyper-heuristic methodology which is problem independent. Unlike other meta-heuristic approaches such as variable neighbourhood search; we can freely move from one neighbourhood to another neighbourhood structure. Therefore, we see the motivation of using a hyper-heuristics as a rapid development tool for optimisation problems.

We have proposed a hyper-heuristic with four different acceptance criteria. Based on experimental result, the *RRT* hyper-heuristics is superior compared to the other proposed hyper-heuristics. Our future interest is to use different strategies to produce initial solutions, using intelligent LLHs (LLHs which themselves have an acceptance criteria, based on random descent and steepest descent local search).

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