

Measures of Location and Spread

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Question 1

a

2.75, 5.50

b

$$\begin{aligned}
 &= \frac{\sum MF}{\sum F} \\
 &= \frac{(0.5 * 1) + (1.5 * 6) + (2.25 * 60) + (2.75 * 280) + (3.25 * 820) + (3.75 * 320) + (4.5 * 10) + (5.5 * 3)}{1 + 6 + 60 + 280 + 820 + 320 + 10 + 3} \\
 &= \frac{4841}{1500} \\
 &= 3.23 \text{ kg}
 \end{aligned}$$

d

$$\begin{aligned}
 Q2 &= \frac{n}{2} = \frac{1500}{2} = 750 \\
 Q2 &\rightarrow 3.0 + \frac{750 - 1 - 6 - 60 - 280}{820} * (3.5 - 3) = 3.0 + \frac{403}{820} * 0.5 = 3.25 \text{ kg}
 \end{aligned}$$

Question 2

a

Q1

$$\begin{aligned}
 &= \frac{n+1}{4} = \frac{11+1}{4} = 3 \\
 &\rightarrow 35
 \end{aligned}$$

Q2/Median

$$\begin{aligned}
 &= \frac{n+1}{2} = \frac{11+1}{2} = 6 \\
 &\rightarrow 53
 \end{aligned}$$

Q3

$$\begin{aligned}
 &= \frac{3(n+1)}{4} = \frac{33+3}{4} = 9 \\
 &\rightarrow 60
 \end{aligned}$$

b

$$IQR = Q_3 - Q_1 = 25$$

Lower Bound

$$= Q_3 + 1.5 * IQR = 60 + 1.5 * 25 = 97.5$$

Upper Bound

$$= Q_1 - 1.5 * IQR = 35 - 1.5 * 25 = -2.5$$

The only value that is outside these bounds is 110.

c

Question 3

a

$$\begin{aligned} 30\% &= \frac{30n}{100} = \frac{30 * 100}{100} = 30 \\ &\rightarrow 20.5 + \frac{0.5}{30} * (30.5 - 20.5) = 20.7 \end{aligned}$$

b

$$\begin{aligned} 70\% &= \frac{70n}{100} = \frac{70 * 100}{100} = 70 \\ &\rightarrow 30.5 + \frac{10}{24} * (40.5 - 30.5) = 34.7 \end{aligned}$$