COEN 240 MACHINE LEARNING HOMEWROK ONE

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PROBLEM ONE:

First of all, since N>>M. there's no need to include a penoty
torm in the error function, which deads with the overfitting problem.

$$\overrightarrow{w} = \arg\min_{\overrightarrow{w} \in \mathbb{R}^m} E(\overrightarrow{w}) = \arg\min_{\overrightarrow{w} \in \mathbb{R}^m} \frac{1}{2} \sum_{n=1}^{\infty} \frac{1}{2} \widehat{w}^T \overrightarrow{x}_n - \widehat{t}_n \right]^2$$

Suppose $X = \begin{bmatrix} -\overrightarrow{x}_1^T \\ -\overrightarrow{x}_2^T \end{bmatrix}$
 $= \frac{1}{2} \begin{bmatrix} X \cdot \overrightarrow{w} - t_n \end{bmatrix}^2$
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 $= \frac{1}{2} \begin{bmatrix} X \cdot \overrightarrow{w} - t_n \end{bmatrix} \begin{bmatrix} X \cdot \overrightarrow$

PROBLEM TWO:

TRAINING SIZE: 320

The prediction accuracy rate on 1000 independent experiments is 0.7294 TRAINING SIZE: 80

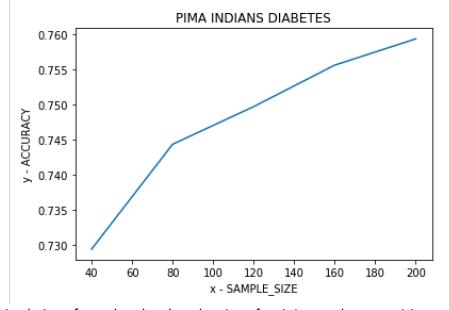
The prediction accuracy rate on 1000 independent experiments is 0.7444 TRAINING SIZE: 160

The prediction accuracy rate on 1000 independent experiments is 0.7497 TRAINING SIZE: 240

The prediction accuracy rate on 1000 independent experiments is 0.7556

The prediction accuracy rate on 1000 independent experiments is 0.7504

The prediction accuracy rate on 1000 independent experiments is 0.7594 TRAINING SIZE: 400



It is obvious from the plot that the size of training set has a positive correlation with the overall accuracy. In other words, the more training data we have, the more accurate our model will be, and vice versa. Even our initial training set size, 80 as 2 times n=40, is substantially bigger than the number of attributes. It tells us having a bigger training set can be considered as an advantage in training our model, but of course within permitted computational power.

ATTACHMENTS

PROBLEM TWO CODE import numpy as np

```
from sklearn.model selection import train test split
import matplotlib.pyplot as plt
import time
# LOADING AND PROCESSING OF DATA
# READ FROM FILE AND ADD BIAS
attributes = {"pregnancies", "glucose", "blood pressure", "bmi", "insulin level", "age",
"attribute7", "attribute8"}
file path = "/Users/bosen/Library/Mobile Documents/com~apple~CloudDocs/Portal/COEN
240/Assignment/Homework1/pima-indians-diabetes.csv"
# file path = ""
diabetes raw = np.genfromtxt(file path, delimiter=',')
N = diabetes raw.shape[0] # N = total number of samples
diabetes plus bias = np.c [np.ones((N,1)), diabetes raw]
# SPLIT DIABETES AND NO DIABETES GROUPS BASED ON TARGET VALUE
columnIndex = 9
target column = diabetes plus bias[:,columnIndex]
sorted_diabetes = diabetes_plus_bias[target_column.argsort()[::-1]]
split result = np.split(sorted_diabetes, np.where(np.diff(sorted_diabetes[:,9]))[0]+1)
class diabetes = split result[0]
class no diabetes = split result[1]
# SPLIT OUT TARGETS FROM ATTRIBUTES
target d = class diabetes[:, 9]
class diabetes = class diabetes[:, 0:9]
num d = class diabetes.shape[0]
target nd = class no diabetes[:, 9]
class no diabetes = class no diabetes[:, 0:9]
num nd = class no diabetes.shape[0]
# TRY DIFFERENT SAMPLE SIZE
samples = []
results = []
for SAMPLE SIZE in range(40, 240, 40):
  # VARIABLES FOR STATISTICS
  COUNT = 1000
  result = 0
  # RUN 1000 EXPERIMENTS
  for i in range(COUNT):
    # MERGE TWO SUBSETS INTO FINAL TRAINING SET
```

```
X train d, X test d, t train d, t test d = \
    train test split(class diabetes, target d, test size=(num d-SAMPLE SIZE)/num d,
random state=time.time ns()%(2**32))
    X train nd, X test nd, t train nd, t test nd = \
    train test split(class no diabetes, target nd, test size=(num nd-SAMPLE SIZE)/num nd,
random state=time.time ns()%(2**32))
    X train = np.concatenate((X train d, X train nd))
    X test = np.concatenate((X test d, X test nd))
   t_train = np.concatenate((t_train_d, t_train_nd)).reshape(-1, 1)
   t test = np.concatenate((t test d, t test nd)).reshape(-1, 1)
    # CALCULATE, ACCELERATED BY REPLACING TENSORFLOW WITH NUMPY
   temp = X train.transpose()
    w val = np.linalg.inv(temp.dot(X train)).dot(temp).dot(t train)
   y test val = np.rint(X test.dot(w val))
    num test
              = X_test.shape[0]
    num match = np.count nonzero(np.equal(y test val, t test))
    result = result + num match/num test
  # RETURN THE AVERAGE RESULT OF THE 1000 EXPERIMENTS
  result averaged = result/COUNT
  results.append(result averaged)
  samples.append(SAMPLE_SIZE)
  print("The prediction accuracy rate on %d independent experiments is %.4f" % (COUNT,
result averaged))
  print("TRAINING SIZE: %d\n" % (SAMPLE SIZE*2))
# PLOTTING
plt.plot(samples, results)
plt.xlabel('x - SAMPLE SIZE')
plt.ylabel('y - ACCURACY')
plt.title('PIMA INDIANS DIABETES')
plt.show()
```