$\operatorname{G53IDS}$ - Final Report

Embedded Domain Specific Language for Describing Recipes in Haskell

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1 Introduction and Motivation

1.1 Overview

Consider the following recipe to make a cup of tea:

- Boil some water
- Pour over a teabag
- Wait for 5 minutes
- Add milk (optional)

This is a very simple but useful recipe that many people will perform, in some cases, many times a day over their lives. What we can realise by looking at this recipe is that it actually consists of many smaller recipes, such as boiling water and combining tea with milk, performed in a certain order. This raises the question, to what extent does the order matter and to what extent can we rearrange things in order to make the recipe more efficient? No doubt you have done this, maybe subconsciously, while cooking at home. Furthermore which steps can be done concurrently in the event that multiple people are cooking e.g. in a professional kitchen with a full brigade?

Perhaps closer to computer science, we could also ask, how could we instruct a robot to do this? After doing some research on robotic chefs it appears that not a huge number exist. There is one home cooking robot [1] which uses motion capture in order to learn recipes. In my opinion this is rather restrictive. It presumes that the human performs the recipe in the optimal manner and it would be very difficult to model a brigade system in this way. In reality there is a limited set of fundamental actions that one becomes able to perform when learning to cook. Recipes can then be performed using a sequence of these actions. Representing recipes like this would allow us to take a robot programmed to perform each of the fundamental actions and tell it how to cook literally anything. This is the same principle as taking code written in a high level language and compiling it down into a sequence of low level actions in assembly language.

What is needed is a consistent way of representing recipes to a computer such that they can be manipulated in various ways for example scheduling, calculation of cost or even generating suggestions on how to improve the recipe. My contributions to solving this problem are the following:

• I have provided a set of combinators as an EDSL in Haskell and show that they can be used to describe a wide variety of recipes

(Section 2).

• I have defined a set of actions needed to actually execute a recipe (Section 3).

- I have defined what it means for two recipes to be equal.
- I have scheduled recipes defined in the EDSL using a representation of a kitchen environment. The schedule is optimised based on the tree-like structure of recipes in the EDSL.

1.2 DSLs and Haskell

Domain Specific Languages (DSLs) are programming languages that are designed for use in a certain problem domain rather than being general purpose. As such they trade range of expression for clarity of expression. A frequently used example of a DSL is the popular database querying language, SQL.

Embedded Domain Specific Languages (EDSLs) are DSLs that are embedded within another language, such as Haskell. This allows for fast development as you no longer need to write your parser or compiler; programs written in your EDSL can just be interpretted as programs written using the language in which it is embedded. Secondly it allows programs written in your language to be manipulated using the full power of the host language. Taking an example from this project, if recipes were specified as a DSL then in order to schedule them, one would have to either expand the DSL to handle scheduling or write something in another language to interpret the recipes so that they can be scheduled. In this case the recipe EDSL is in Haskell and as such a scheduler can just be written in Haskell as it would for any other purpose thus saving both time and unecessary extra code.

Haskell is a very popular language for writing EDSLs, examples range from pretty printing [5] to financial contracts [4]. Reasons for this include that the type checker catches many mistakes and that Haskell has very lightweight function application syntax allowing us to omit symbols such as brackets in many cases [3].

1.3 Deep and Shallow Embedding

When writing an EDSL one must choose between deep and shallow embedding. Deep embedding means that the DSL's abstract syntax tree

(AST) is represented using an algebraic data type. On the other hand, shallow embedding doesn't have an AST and the language constructs exist purely as mappings to their semantics.

Both of these approaches have their advantages. Deep embedding allows us to transform the representation before evaluating it however, every time we want to add a new language construct then we need to add it to the AST and as such our data type can become quite large. Similarly, all functions manipulating the AST must be changed to accommodate the new construct. Shallow embedding avoids these issues as it doesn't have an AST however, it does mean that we are limited to a specific semantic domain.

For the recipe DSL I have decided to borrow some features from both. The fundamental actions which compose a recipe use a deep embedding allowing us to evaluate the recipes in multiple semantic domains for example cost or time. The functions exposed to the user represent more of a shallow embedding which makes the definition of recipes much more concise and means that any new combinator can be added trivially as long as it can be represented as some construction of the deeply embedded actions.

2 Combinators

In this section I shall use various example recipes to demonstrate the different combinators. We started off by boiling down several recipes, if you'll forgive the pun, into their components and then modelling them as combinators. As the project progressed we added, removed and modified the combinators to address various issues we encountered. This is similar to the approach used to write the financial contracts DSL [4].

2.1 Implementing a Cup of Tea

We first need to describe what a cup of tea is. It's boiling water mixed with a teabag for a certain amount of time, possible with milk added. This leads us into the following definition.

```
water, teabag, milk :: Recipe
water = ingredient "water"
teabag = ingredient "teabag"
milk = ingredient "milk"
```

Here we have introduced several things. Firstly our heat combinator which heats an ingredient to a temperature. We then have combine which takes a String as a description of how to combine, followed by the two recipes it combines. wait and ingredient are relatively self-explanatory which leaves >>>. This is our sequencing combinator where a >>> b means "do a then do b". The types for these are as follows.

```
ingredient :: String \rightarrow Recipe heat :: Int \rightarrow Recipe \rightarrow Recipe wait :: Int \rightarrow Recipe combine :: String \rightarrow Recipe \rightarrow Recipe \rightarrow Recipe (>>>) :: Recipe \rightarrow Recipe \rightarrow Recipe
```

In order to keep the recipes as simple as possible when exploring ways to manipulate them we will not concern ourselves with precise measurements or exactly how something is chopping up. We will presume a sort of "cooking show" style where ingredients are already prepared. We will in fact add a measurement combinator in Section 5.3 when discussing the price of a recipe. However, there wasn't a part of the project in which it was obvious that a "chopping" combinator would make much difference to our interpretations and as such it was omitted. It could of course be added if this DSL were to be used in practice.

2.2 Sequencing Problem

As we continued to explore the semantics of the combinators defined above, we began to notice an issue with the sequencing combinator. When considering the topological sorts of a recipe as in Section 3, we make use of the sequencing provided by the tree-like structure of recipes. For example heat 100 r implicitly requires that r be performed before it can be heated. In the case of sequence, things get a little less clear. Consider the recipe r1 >>> r2, that is "r1 then r2". There is no need for r1 to be performed first because r2 doesn't make use of it. Let's say we then apply heat to this sequence, are we heating r1, r2 or both? The reason for this problem is that we have added meaning that doesn't exist, we have forced sequencing in a scenario in which it does not naturally occur. Paul Hudak writes in his paper [2] that a "a DSL should capture the semantics of the domain and nothing more". This was the issue that lead to the first major

rework of our combinators and a significant breakthrough in the form of conditionals.

2.3 Conditionals

In recipes, one pattern that occures a lot is the notion of performing an action until a certain condition is met. For example in our cup of tea we need to boil water which is the heating of water until the water reaches 100 degrees. We capture this by adding a new combinator as follows. Note that we also add some extra custom combinators to provide a more convenient means of adding each type of condition.

This is incredibly powerful because it allows the simplification of a lot of our other combinators. One particular issue that conditionals helped with was determining the difference between "heat", "heatAt", "heatTo", "heatFor" and their various combinations. Initially we used combine with wait to mean "do for" however, this feels like a bit of a hack. Combinators should only have one purpose in order to keep their semantics concise but here we have given combine an extra use. It not only combines two recipes together in the cooking sense but it also adds functionality to other combinators.

Extracting the end temperature and time from our heat and wait combinators we get the following. Note that the temperature we are heating

"at" isn't extracted because conditionals capture termination coniditions not components of the action itself.

```
\mbox{heatAt} \ :: \ \mbox{Int} \ \rightarrow \mbox{Recipe} \ \rightarrow \mbox{Recipe} \\ \mbox{wait} \ :: \ \mbox{Recipe} \ \rightarrow \mbox{Recipe} \\ \label{eq:Recipe}
```

But what about devices that don't have temperature settings such as kettles? To handle this we add a generic "heat" combinator as follows.

```
\mathtt{heat} :: \mathtt{Recipe} \to \mathtt{Recipe}
```

Now we can define all our other variations of "heat" using these combinators.

```
heatFor :: Time \rightarrow Recipe \rightarrow Recipe heatFor t = forTime t \circ heat heatTo :: Int \rightarrow Recipe \rightarrow Recipe heatTo t = toTemp t \circ heat heatAtFor :: Int \rightarrow Time \rightarrow Recipe \rightarrow Recipe heatAtFor temp time = forTime time \circ heatAt temp waitFor :: Time \rightarrow Recipe \rightarrow Recipe waitFor t r = forTime t (wait r)
```

We're not adding new fundamental combinators here, we're just building on a very small set of core features. This structure makes the language highly extensible. Users could create their own libraries of custom combinators and have them work straight away with the other functions mentioned throughout this report.

2.4 Final Definitions

This leads us into the final definitions of our fundamental combinators.

```
\begin{array}{l} {\rm ingredient} \ :: \ {\rm String} \ \to \ {\rm Recipe} \\ \\ {\rm heat} \ :: \ {\rm Recipe} \ \to \ {\rm Recipe} \\ \\ {\rm heatAt} \ :: \ {\rm Int} \ \to \ {\rm Recipe} \ \to \ {\rm Recipe} \\ \\ {\rm wait} \ :: \ {\rm Recipe} \ \to \ {\rm Recipe} \\ \\ {\rm combine} \ :: \ {\rm String} \ \to \ {\rm Recipe} \ \to \ {\rm Recipe} \\ \\ {\rm addCondition} \ :: \ {\rm Condition} \ \to \ {\rm Recipe} \ \to \ {\rm Recipe} \\ \\ \end{array}
```

```
\mbox{transaction} \ :: \ \mbox{Recipe} \ \to \ \mbox{Recipe} \mbox{measure} \ :: \ \mbox{Measurement} \ \to \ \mbox{Recipe} \ \to \ \mbox{Recipe}
```

The first six combinators have already been described. The transaction combinator shall be formally introduced in Section 4.5 and measure in Section 5.3 so we shall ignore these for now. Using these combinators we can now define our cup of tea as follows.

```
cupOfTea :: Recipe
cupOfTea = optional "milk"
    $ combine "mix" milk
    $ waitFor (minutes 5)
    $ combine "mix" teabag
    $ heatTo 100 water
```

As you can see, our custom combinators like heatTo and optional, as mentioned above, allow us to make the definition very concise. The only function we haven't introduced is minutes which simply constructs a Time with the given number of minutes. Our Time type holds seconds so minutes abstracts away the multiplication by 60. The (\$) operator is Haskell's application operator which "has low, right-associative binding precedence" [12] and as such can allow brackets to be omitted making our definition tidier. What you may also notice is that our definition looks very much like our original set of steps on at the start of the report but written in reverse. This hopefully means that writing recipes in the DSL would be relatively intuitive even for someone who isn't particularly familiar with Haskell or programming in general.

2.5 Tree of Actions

Shortly into the second half of the project, the decision was made to change the underlying implementation of recipes from their own data type that resembled a tree, to an actual tree of actions. Prior to this the recipe type was as follows.

Eventually, after adding conditionals and later, transactions (Section 4.5) we realised that we'd got another problem with sequencing. Conditionals

are intended to wrap an action with a condition however, as you can see above, the way we do that with this representation is the same way we provide sequencing. Heat also wraps a recipe, when visualised as a tree this places Heat above that recipe meaning "perform that recipe then heat it afterwards". The problem is that this results in the intuitive interpretation of Conditional c r being "perform r then evaluate the condition afterwards". This obviously makes no sense as the condition is what decides the completion of "r" in the first place.

A further issue with out current representation is that labelling is a little inconvenient. We could create a labelled recipe by putting a label and a recipe in a tuple as follows.

```
type LRecipe = (Label, Recipe)
```

This might seem like a good solution however, we would need to create a new "labelled" version of all of our combinators that takes an LRecipe instead of a Recipe.

The Haskell package Data. Tree provides the following data structure.

```
data Tree a = Node { rootLabel :: a
    , subForest :: [Tree a] }
```

We can use this to create our recipe type as follows.

With this definition Conditionals and Transactions really do wrap an Action and will therefore appear in the same Node thus removing our problem with implied sequencing. It's also trivial to label our tree as we simply change the type to Tree (Label, Recipe). Now that we've got a way of labelling recipes we can define functions to print a recipe as a sequence of steps.

```
\mbox{type Step} = \mbox{(Label, String)} \mbox{steps} :: \mbox{Recipe} \rightarrow \mbox{Tree Step} \mbox{ppSteps} :: \mbox{Recipe} \rightarrow \mbox{IO ()}
```

Running ppSteps on our cup of tea recipe calls steps to convert the actions at each node of the tree into a step and then prints them out as follows.

```
> ppSteps cupOfTea =
1) Get milk
2) Get teabag
3) Get water
4) Heat (water) until temperature 100
5) Mix (teabag) and (4)
6) Wait for Oh 5m Os
7) Mix (milk) and (6) (optional)
```

We refer to previous steps via their label

Finally Data.Tree provides a pretty printing function that allows us to output an ASCII drawing of the tree. The tree for our cup of tea recipe is as follows.

```
Conditional (Combine "mix") (CondOpt "milk")

GetIngredient "milk"

Conditional Wait (CondTime 0h 5m 0s)

Combine "mix"

GetIngredient "teabag"

Conditional Heat (CondTemp 100)

GetIngredient "water"
```

Figure 1: Cup of tea recipe printed as a tree.

One could of course use any other graphics printing package available in Haskell.

2.6 Custom Combinators

As mentioned previously, the combinators are highly extensible. We will now explore this further while constructing a more complex recipe, chicken jalfrezi with rice. For conciseness I shall omit the ingredient definitions. First of all, let's create a marinate combinator for our chicken. This can also make use of the fact that we may frequently want to combine many things at once.

```
\mathtt{multiCombine} \ :: \ \mathtt{String} \ \to \ \mathtt{Recipe} \ \to \ \mathtt{[Recipe]} \ \to \ \mathtt{Recipe}
```

```
multiCombine s r [] = r multiCombine s r rs = foldr (combine s) r rs marinate :: Recipe \rightarrow Recipe \rightarrow Time \rightarrow Recipe marinate r m t = waitFor t $ heatTo 4 $ combine "cover in" r m
```

The heatTo 4 step implies that recipe must be left to marinate in the fridge, or somewhere else that can keep it cool. Secondly we can create a "preheat oil" combinator for use when frying our onions and chicken.

```
preheatOil :: Recipe
preheatOil = heatForM 2 oliveOil
```

Note that heatForM is just a variation of heatFor that takes time as minutes rather than seconds for convenience. We can now start to create all the components of our chicken jalfrezi.

```
spiceMix :: Recipe
spiceMix = multiCombine "mix" cumin
    [coriander, turmeric]
spicedChicken :: Recipe
spicedChicken = marinate chicken
    spiceMix (minutes 10)
cookedChicken :: Recipe
cookedChicken = heatForM 15
    $ combine "place in" spicedChicken
    $ preheatOil
jalfreziSauce :: Recipe
jalfreziSauce = combine "mix" tinnedTomatoes
    $ heatForM 10
    $ combine "place in" garlic
    $ combine "place in" onion
    $ preheatOil
```

Moving onto the rice, we can abstract the notion of boiling "something" in water as we may want to reuse this in the future, for example when cooking vegetables.

```
\label{eq:boilInWaterForM} \begin{array}{l} \text{boilInWaterForM} \ :: \ \text{Time} \ \to \ \text{Recipe} \ \to \ \text{Recipe} \\ \text{boilInWaterForM} \ \text{t} \ r = \text{forTime} \ (\text{minutes t}) \\ \text{\$ combine "place in" r} \\ \text{\$ heatTo 100 water} \end{array}
```

Now we can finish by combining our chicken and sauce with a few more ingredients, heating it for a few more minutes and then placing it on top of some boiled rice.

3 Deriving Equality

When considering what it means for two recipes to be equal one might consider that they must have the same ingredients and the same actions must be performed on those ingredients, in the same order.

Our recipe tree already encodes the ingredients and the actions performed on them, they are nodes in the tree. Ordering of actions in our tree is captured by their level in the tree. We can see that the actions we could choose to perform first are the leaves of the tree. If we then remove a leaf and perform that action then the actions we can perform next are the new leaves of the tree. We can use this to generate a list of all the different orders that the actions of a recipe can be performed in while creating the same recipe. We want a way of generating all combinations of nodes such that nodes higher in the tree appear after their children in the list thus preserving the order of our actions. In other words we want a method of enumerating all valid execution paths through our recipe.

This is known as topological sorting. I have implemented a function in Haskell below which, given a recipe, returns a list of all topological sorts of that recipe.

```
topologicals :: Recipe → [[Action]]
topologicals (Node a []) = [[a]]
topologicals t = concat
    [map (a:) (topologicals' 1) | 1@(Node a _) ← 1s]
    where
        topologicals' 1 = topologicals $ removeFrom t 1
        ls = leaves t
```

This is similar to the operational semantics given by unfolding a term to provide a list of execution paths [8]. As an example, consider this alternate definition for our cup of tea recipe.

In this version we combine our tea with milk rather than combing milk with our tea. Printing the tree for this recipe gives a different result from our original recipe. But fundamentally we know it to be a variation of the same recipe.

```
Conditional (Combine "mix") (CondOpt "milk")

Conditional Wait (CondTime 0h 5m 0s)

Combine "mix"

Combine "mix"

GetIngredient "teabag"

Conditional Heat (CondTemp 100)

GetIngredient "water"
```

Figure 2: Alternate cup of tea recipe printed as a tree.

In Haskell one must make their type an instance of the Eq typeclass in order to make use of the == operator. In order to run QuickSpec on recipes as discussed in a later section, we also need an instance of Ord. This means implementing a function compare, which, when given two recipes, returns an ordering for example "less than" (LT).

What we're doing here is taking the list of topological sorts of each recipe, sorting those lists so that we have some consistent or and then comparing them. The compare function is already implemented for lists of topological sorts as they have type [[Action]] and thus they use the ordering instance already defined for Haskell lists. We do however, need to define ordering for Action and all the types that Action uses for example

Condition for this to work. For this we just let GHC derive them for us as they don't need to have any special meaning, they just need to provide a consistent way of sorting the lists.

What this results in is recipes being equal if and only if their topological sorts are identical. Recipe a will be less than recipe b if the list of recipe a's topological sorts is shorter than recipe b's. Similarly the inverse is true of recipe a being greater than recipe b. Things become a little less clear when the two lists are the same length. Ordering is then deferred to which lists of actions consists of actions with lower ordering as defined by the derived ordering instance for actions. Once again this has no actual meaning but provides the list comparison we need. With ordering defined for recipes, defining (==) becomes trivial as we just check if compare evaluates to EQ.

```
instance {-# OVERLAPPING #-} Eq Recipe where
    (==) r1 r2 = compare r1 r2 == EQ
```

Because Recipe = Tree Action it naturally uses the equality instance for Tree but we want to use our compare function which makes use of topological sorting. That's what the "overlapping" annotation is for. Using the above definition, the expression cupOfTea == cupOfTea' evaluates to True showing that, as desired, our two recipes are equal.

4 Scheduling Recipes

Now that we have a solid representation of our recipes in Haskell we can think about how these could be scheduled.

4.1 Modelling a Kitchen

The first step of scheduling a recipe is to consider some representation of the environment within which it is scheduled. Abstracting from the details we can break a kitchen down into a set of stations for example an oven and a kettle. We also need some sort of global observables for example, time.

```
{ stName :: String
, stConstrF :: ConstraintF
, stObs :: [IO Obs]
}
type ConstraintF = Recipe → Maybe [Process]
```

Stations consist of a name, a constraint function and a set of local observables such as temperature. The constraint function takes a recipe and returns a list of processes required to perform that recipe. In the event that the station cannot handle that particular recipe then Nothing is returned. Observables are represented as follows. I have also provided the function that checks whether a condition is true given a list of observables.

A process is an intermediate translation of our recipes. One might say it's our sort of assembly language, sitting between our high level combinators and some device specific instructions that the developer of a robot chef might write.

```
data Process =
    Input
    | Output
    | Preheat Int
    | DoNothing
    | PCombine String
    | EvalCond Condition
    | MeasureOut Measurement
```

Most of these are self explanatory, PCombine and MeasureOut are just renamings of the actions Combine and Measure. EvalCond is inserted after

Input which when interpreted will check the condition, if true then skip to Output else it will run all processes up until Output before jumping back to the condition again. As an example, here is part of our cup of tea recipe translated into a list of processes.

```
Conditional (CondTemp 100) Heat \rightarrow [Input, EvalCond (CondTemp 100), Output]
```

The water is put into the kettle which then heats it until the temperature is 100 degrees before the water is taken out. You might be wondering why there is no "heat" process. That's because something is heated as a side effect of being placed in a device which becomes hot rather than as an explicit action of that device. Device specific details such as the kettle turning on when the water is added or turning off on output is not covered here as these details can be abstracted away being Input and Output.

Now let's consider what stations we require to make our cup of tea. At the most basic level we need a kettle and a chef. For conciseness I shall only discuss the kettle.

```
\label{eq:kettle} \begin{tabular}{ll} kettle :: Station \\ kettle = let kettleConstr r@(Node a ts) \\ & | r == heatTo 100 \mbox{ (ingredient "water")} = Just [Input, Output] \\ & | otherwise = case a of \\ & Transaction a \rightarrow kettleConstr \$ popT r \\ & \_ \rightarrow Nothing \\ & kettleTemp = return \$ \mbox{ ObsTemp 100} \\ & in Station "kettle" kettleConstr [kettleTemp] \end{tabular}
```

Here we're creating a station with a name of "kettle", creating the constraint function and also providing a temperature observable. We have no actual kettle to retrieve the temperature from so for now we are just providing a constant temperature of 100 degrees. The constraint function simply checks if the recipe passed is "boiling water" or "boiling water" wrapped in a transaction (Section 4.5), returning Nothing if it's not.

We can now speicfy our environment as follows. I have added an extra uneeded station, a toaster, to demonstrate that it remains unused when scheduling making a cup of tea.

```
env :: Env
env = Env { eStations = [kettle, chef, toaster]
    , eObs = [ getTime
    , return $ ObsOpt "milk" True ] }
```

The function getTime simply returns the UTC time converted to ObsTime. We then need to provide a value for our optional "add milk" step. The observables are wrapped in IO meaning they can come from external sources for example, the command line if we so desired.

4.2 Scheduling Methods

Now that we have a model of a cooking environment we need to choose a method for scheduling the recipes. Scheduling is in itself a complex problem and therefore the solution used for this project is by now means suggested as a well refined solution but merely a demonstration of using the recipe system for a more concrete purpose.

4.2.1 Linear Programming

The first consideration was linear programming (LP). LP works by taking a linear function, called the objective function, which is minimised or maximised according to a set of linear constraints. For our recipes the objective function would be the end time of the final step which we would then want to minimise in order to make the recipe as efficient as possible. We then might consider the following constraints.

$$end_r = start_r + dur_r \quad \forall r$$

$$start_r \ge end_d \quad \forall d, r \quad | \quad d \in dependencies(r)$$

That is the end time of each recipe is equal to its start time plus its duration and a recipe must start at or after the end time of its dependencies. The problem arose with choosing which station to schedule each action on. For any action we have a set of stations that can perform that action. We can then expand our first constraint to handle this.

$$end_{r_s} = start_{r_s} + dur_{r_s} \quad \forall r, s \quad | \quad s \in validStations(r)$$

But we only want one of the valid stations to be selected which leaves us with the problem of modelling logical OR in this context. One potential way is to use a set of binary variables as follows.

$$end_r = \sum (end_{r_s} * bin_{r_s}) \quad \forall r, s \mid s \in validStations(r)$$

$$\sum_{s}^{validStations(r)}end_{r_{s}}=1 \quad \forall r$$

The issue with the above is that it involves the multiplication of two variables. As such this is no longer a linear constraint. A long time was spent considering whether or not our recipes could in fact be expressed as linear systems. After reformulating the problem several times and not finding a solution I decided to move on from linear programming and find something else.

4.2.2 Bin Packing

Bin packing is a much more general optimisation problem. It is the problem of packing a number of objects with fixed dimensions into a number of bins of fixed dimensions such that the number of bins is minimised. This problem as it is doesn't bare much resemblance to our recipes however, adjusting the problem as follows provides something more useful.

Given a number of objects of fixed height and a number of bins of infinite height where each bin can only hold certain types of object. Pack the objects into the bins such that the height of the tallest stack is minimised and a set of constraints regarding order of objects is met. We can model our stations as a stack of actions which they must perform, these are our bins. Our objects are either the station performing one of our actions or being idle for a certain time. We can then say that the height an action begins on the stack must be greater than or equal to the height that its dependencies end on their respective stacks.

As an abstract example, imagine a recipe, r1, which has sub-recipes: r2, r3 and r4. All the recipes must be scheduled on station 2, except r3 which must be scheduled on station 1. Below is a diagram showing r1 and a potential stack setup.

4.3 Optimisations and Heuristics

Now that we have a way to translate our recipes into a form of schedule we need to consider optimisations we can apply during the scheduling process. As mentioned in the introduction, you have no doubt done this while cooking at home. In the case of making a cup of tea you may start the kettle boiling before you get the milk out of the fridge. That way, you and the kettle are working in parallel and thus saving time.

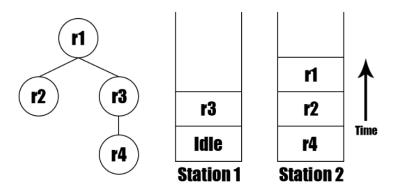


Figure 3: Recipe tree and stack schedule for r1.

Heuristics are "rules of thumb" that are applied to a problem solver in order to guide it in the decision making process. An everyday example might be preferring motorways over country roads when planning a journey; they have a higher speed limit and traffic capacity thus making them a faster route in the general case. There are two decisions we can apply heuristics to when scheduling recipes. The first is which leaf of the recipe tree to schedule first. Referring back to the section on topological sorting, the leaves of the tree at a given time are comprise the set of actions we can choose to perform next. The second decision is which of the available stations to schedule this action on.

4.3.1 Leaf Choice Heuristics

The first heuristic used in leaf choice is "shortest task first". This may seem counter intuitive however, if we think about the way in which recipes are typically structured, it makes sense. It is frequent to have a small task such as "get water" followed by a longer task performed by another station for example "boil water". Let's say that "get milk" was a long task to complete. It would make more sense to do the short "get water" task first, start the kettle boiling, then use that time to "get milk". If we "get milk" first then we're performing a long task, meanwhile the kettle is idle waiting for some water.

The second heuristic is applied in the event that multiple leaves contain a task of the shortest length. It is based on the same principle as above, that if we have short task such as "get water" followed by a lengthy task such as "boil water" we want to "get water" as soon as possible so that

the kettle can be boiling while we do the other tasks. This is formalised as "longest branch first". In the event that there are multiple "shortest tasks" then the task on the longest branch will be chosen to try and ensure that if we have a long task that depends on a short task, it will be started as soon as possible.

4.3.2 Stack Choice Heuristics

Now that we have selected which leaf to schedule, we need to choose which station to schedule it on. In many cases this is a simple task as many actions can only be performed by one station. In the event that multiple stations can be used then we use three heuristics to choose, each shortening the list of potential stations.

The first is to pick whichever station is in least demand. This is done by scanning through all unscheduled actions and calculating their time divided by the number of stations that action could be performed on. For example if an action a had a time of 10 and could be performed on either of 2 stations then the demand that a would create for each station would be 5. The reason for this heuristic is rather intuitive. If we have a choice between a station which a lot of other actions need and a relatively uneeded station, we should choose the uneeded station to reduce the load on the high demand station. This heuristic could obviously be inverted if the goal was to minimise stations used rather than time taken.

The second heuristic is "least idle time". One's first thought might be to add the action to the emptiest stack however, in the event that the action is waiting on a long dependency, it could cause lots of idle time to be added to an otherwise empty stack. Therefore we choose the stack which allows the action to be started closest to the end time of its dependencies which may mean placing it on a fuller stack rather than an emptier one. We also might consider that choosing an a stack with "high demand" could be worth it if it avoids a significant amount of idle time. To model this we implement these two heuristics as one by simply adding the idle time and demand of a station together. We can then choose or choose from the station(s) with the lowest idle time and demand.

It is unlikely that the first two heuristics didn't filter the potential stations down to one, but if they didn't then we select the stack that is least full. Providing there are no caveats like idle time, as mentioned above, then placing an action on an emptier stack should result in a shorter overall time in most cases.

4.4 Implementation

In the interest of space, I shalln't go into the details of the code here as there is quite a lot of it However, below is some pseudo-code to demonstrate the general flow of the scheduling functions.

```
data Task = Active Label | Idle Time
type Stack = [Task]
type Schedule = Map StName Stack
\mathtt{schedule} \; :: \; \mathtt{Recipe} \; \rightarrow \; \mathtt{Env} \; \rightarrow \; \mathtt{Schedule}
schedule r env = do
    tree = labelRecipe r
    schedule' env tree tree emptySch
    where
         schedule' env fullTree tree sch = do
              l = chooseLeaf tree
              st = chooseStation fullTree 1 env sch
              stack = lookup st sch
              stack' = Active 1 : stack
             newSch = insert st stack' sch
              if l == root fullTree
                  then
                       newSch
                  else
                       tree' = removeFrom tree 1
                       schedule' env fullTree tree' newSch
```

The main function schedule takes a recipe and an environment then returns a schedule. It first labels the recipe, this is to avoid issues with a set of actions appearing on multiple branches. It then passes the environment, two copies of the recipe tree and an empty initial schedule to the subroutine schedule'. The reason for passing two copies of the tree is that one is maintained as the full tree in order to maintain access to the children of the node we are scheduling even after those child nodes have been scheduled and removed from the other tree. The functions chooseLeaf and chooseStation apply the various heuristics and return the best leaf and best station respectively. Next we add the leaf to the stack of the chosen station and update the schedule. We then check to see if the node we just scheduled is the root of the tree, if it is, then we have finished and can return our new schedule otherwise we pass our new schedule and updated tree to the next iteration of schedule'.

The function scheduleAndPrint schedules a recipe on a given environment and prints the result in a more readable way, showing each action as a step rather than a collection of the more low level processes. Below is the result of running scheduleAndPrint on our cup of tea and the environment created above.

```
> scheduleAndPrint cupOfTea env =

chef:
Oh Om Os: 3) Get water
Oh Om 10s: 2) Get teabag
Oh Om 20s: 1) Get milk
Oh Om 30s: Idle: Oh 3m Os
Oh 3m 30s: 5) mix (2) and (4)
Oh 3m 40s: 6) Wait for Oh 5m Os
Oh 8m 40s: 7) mix (1) and (6) (optional)

kettle:
Oh Om Os: Idle: Oh Om 10s
Oh Om 10s: 4) Heat (3) until temperature 100
```

As you can see the scheduling function tells the chef to get the water first so that the kettle can start boiling it as soon as possible. After 10 seconds the kettle can start boiling the water, meanwhile the chef acquires the other ingredients before becoming idle until the kettle has finished. Once the water is boiled the chef adds the teabag before waiting for 5 minutes. After that they optionally add milk. Meanwhile our uneeded toaster does nothing. While this scheduling function seems effective, it is also rather inefficient. When running it on larger recipes like our chicken jalfrezi, which contains over 30 steps, it runs for a long time before running out of memory. As mentioned before, the scheduling function isn't the focus of the project and as such not a lot of time was spent on it.

4.5 Transactions

toaster:

This method of scheduling seems to work however, there is one problem that arises from us reordering steps in order to optimise them. Consider the following recipe for tea and buttered toast, for conciseness I have omitted the ingredient definitions.

```
cupOfTea :: Recipe
cupOfTea = optional $ combine "mix" milk
```

```
$ waitFor (minutes 5)
$ combine "mix" teabag
$ heatTo 100 water

butteredToast :: Recipe
butteredToast = combine "spread" butter
$ heatFor (minutes 3) bread

teaWithToast :: Recipe
teaWithToast = combine "place next to"
   butteredToast
   cupOfTea
```

It could be the case that, when scheduling, first the bread is toasting, then the cup of tea is made, then the butter is added to the toast. The problem with this is that by the time we come to spread the butter on the toast, it has gone cold. We need some way to ensure that the butter is added immediately after the toast is finished. To do this we have a new combinator called Transaction which wraps any other action. This can then be interpretted by the scheduling function to mean that the action which it wraps and it's immediate children should be scheduled together meaning that no other actions can end up in between. Our buttered toast recipe is now as follows.

5 Recipe Properties

In this section we will explore recipes across various semantic domains and how this can help us to create new recipes.

5.1 Folding Over Recipes

One function that is particularly useful in exploring semantics is fold. Folding is the process of taking some whole made up of parts and creating a single value from it. For example folding texttt(+) over a list of numbers [1,2,3] returns 6. We can use folding to create denotational semantics for our recipes [8]. Denotational semantics involves terms being evaluated via a mapping to a value in a certain semantic domain. There are multiple

semantic domains of interest in recipes hence the choice of a deep embedding (Section 1.3). Abstracting the traversal of the recipe from the semantic mapping functions, into a fold function results in conciser definitions and less repetition.

```
foldRecipe :: Monoid a \Rightarrow (Action \rightarrow a) \rightarrow Recipe \rightarrow a foldRecipe f (Node a ts) =

let vs = map (foldRecipe f) ts

in f a 'mappend' (mconcat vs)
```

Now that we have defined folding over recipes, we can take any function which maps actions to some value and use it to evaluate our recipe. The one caveat is that the values must form a monoid. This simply means that the values should have some "empty" value and that there should be some natural way of appending them. As an example the Monoid instance of Time is given below.

```
instance Monoid Time where
  mempty = 0
  mappend = (+)
```

5.2 Time

An important semantic domain for recipes is time. In order to calculate the time of a recipe using foldRecipe we first need a function of type Action -> Time.

```
timeAction :: Action \rightarrow Time timeAction (GetIngredient _) = 10 timeAction Heat = 0 timeAction (HeatAt t) = preheatTime t timeAction Wait = 0 timeAction (Combine _) = 10 timeAction (Conditional _ c) = foldCond f c where  f \text{ (CondTime t)} = t \\ f \text{ (CondTemp t)} = tempToTime t \\ f \text{ (CondOpt s)} = 0 \\ timeAction (Transaction a) = timeAction a timeAction (Measure m) = 10
```

These times are just intended to be estimates, note that most of the "time" is contained within conditionals. This is intentional as most of the duration of a recipe is made up of performing an action for a given time rather than actions that have a set time. A more complex function might also

take into account which station each action is scheduled on. The only other point of note here is foldCond. This function allows us to abstract the details of "and" and "or" conditions to a more general case as follows.

If the condition we are handling is logical and over two conditions then we can simply apply our function to each of the sub-conditions and join the results, hence the requirement that the value we're creating have a monoid instance. In the that event we're dealing with the logical or of two conditions then we apply our function to each of the sub-conditions as before, except this time we take the largest value. This provides us with a "worst case scenario" as it would take whichever condition would take the longest duration to be met. This works in other semantic domains too. Imagine we added a condition of mass and thus extracted the measurement from our Measure combinator (Section 5.3). If we calculated the cost of a recipe, as we shall do in the next section, we would need to quantify the ingredients. Using foldCond on logical or over two conditions in the domain of mass would provide us with the largest mass possible leading to the highest price and once again the "worst case scenario". Our use of max also holds when evaluating conditions to boolean values as max True False = True thus holding the meaning of logical or.

We can now define our function time for a recipe as follows.

```
\begin{array}{ll} \mathtt{time} \ :: \ \mathtt{Recipe} \ \to \ \mathtt{Time} \\ \mathtt{time} \ = \ \mathtt{foldRecipe} \ \mathtt{timeAction} \end{array}
```

We can also define a function **schLength** which tells us the length of a schedule.

```
\begin{array}{l} {\rm schLength} \ :: \ {\rm Schedule} \ \to \ {\rm Recipe} \ \to \ {\rm Time} \\ {\rm schLength} \ {\rm sch} \ r = \\ {\rm let} \ r {\rm Map} = {\rm mkLabelMap} \ \$ \ {\rm labelRecipeR} \ r \\ {\rm stacks} = {\rm Map.elems} \ {\rm sch} \\ {\rm ts} = {\rm map} \ (\lambda {\rm s} \ \to \ {\rm stackHeight} \ {\rm s} \ r {\rm Map}) \ {\rm stacks} \\ {\rm in} \ {\rm maximum} \ {\rm ts} \end{array}
```

One of the great things about Haskell is that it allows us to keep the recipe labelling functions pure. As such we can recreate the map of labels to recipes that was used in scheduling at any point and know it will be the

same; we need not worry that some side effect has caused it to be different.

If we run the above functions on our cup of tea then we see that our scheduling has saved us 20 seconds off the estimated time by parallelising certain steps. Naturally this benefit would potentially be much larger for a recipe with a larger number of steps.

```
> time cupOfTea = 0h 9m 10s 
 > schLength (scheduleRecipe cupOfTea env) cupOfTea = 0h 8m 50s
```

5.3 Price

Another semantic domain to consider for recipes is their price. For this we need to quantify our ingredients with the Measure combinator.

```
data Measurement = Count Int | Grams Int | Milliletres Int measure :: Measurement \to Recipe \to Recipe measure m r = Node (Measure m) [r]
```

Below is our cup of tea recipe, updated with quantified ingredients.

```
cupOfTeaQ :: Recipe
cupOfTeaQ = optional "milk"
    $ combine "mix" (measure (Milliletres 10) milk)
    $ waitFor (minutes 5)
    $ combine "mix" (measure (Count 1) teabag)
    $ heatTo 100
$ measure (Milliletres 300) water
```

We now need some representation of the price of the individual ingredients. Below is an implementation of a PriceList which itself is based on a more generic PropertyList.

```
type PropertyList v = [(String, v)]
type PriceList = PropertyList (Price, Measurement)
```

Finally we need to get a list of our quantified ingredients and check them against the price list.

```
\label{eq:continuous} \begin{array}{c} \text{evalPropsQ} :: (\text{Integral } v, \, \text{Monoid } v) \Rightarrow \text{PropertyList } (v, \, \text{Measurement}) \\ & \rightarrow \, [(\text{String}, \, \text{Measurement})] \, \rightarrow \, v \\ \\ \text{evalPropsQ ps } \text{xs} = \text{mconcat } \$ \text{ map } \text{evalPropsQ'} \text{xs} \\ \\ \text{where} \end{array}
```

```
evalPropsQ' (s,m) = case lookup s ps of Nothing \rightarrow mempty

Just (v,m') \rightarrow applyQuant m (v,m')
```

The function evalPropsQ takes a list of properties, that have a Measurement component, and a list of String keys that also have a Measurement. We then lookup each key in our list, use applyQuant which calculates the ratio of measurements returning the actual price (or other value) for our quantity, and finally join the results together making use of our value's monoid instance.

We can now define price for our recipes. Note ingredientsQ takes a recipe and returns a list of ingredient names paired with their measurements.

```
\begin{array}{l} \texttt{price} \ :: \ \texttt{PriceList} \ \to \ \texttt{Recipe} \ \to \ \texttt{Price} \\ \texttt{price} \ \texttt{ps} \ \texttt{r} = \texttt{evalPropsQ} \ \texttt{ps} \ (\texttt{ingredientsQ} \ \texttt{r}) \end{array}
```

Returning to our quantified cup of tea, we get the following.

5.4 QuickSpec

QuickSpec [9, 10] is a Haskell library for automatically generating laws about your program. In order to do this QuickSpec requires a way of generating random values of the relevant type. We can provide this by making our recipe type an instance of the Arbitrary typeclass.

```
instance {-# OVERLAPPING #-} Arbitrary Recipe where arbitrary = sized $ \lambdan \rightarrow let bin = resize (n 'div' 2) genRecipe un = resize (n-1) genRecipe in case n of 1 \rightarrow genIng _ \rightarrow oneof [genUnRec un, genBinRec bin bin] genIng :: Gen Recipe genIng = liftM (ingredient \circ show) (choose (1, 100) :: Gen Int)
```

```
genUnRec :: Gen Recipe → Gen Recipe
genUnRec un = oneof
   [ liftM heat un
   , liftM2 heatAt genTemp un
   , liftM wait un
   , liftM2 addCondition arbitrary un
   , liftM transaction un
   , liftM2 measure arbitrary un ]

genBinRec :: Gen Recipe → Gen Recipe → Gen Recipe
genBinRec r1 r2 = liftM3 combine genMethod r1 r2
```

The first point of note is that our recipes are generated as sized values meaning that they have a number of sub-recipes. If a recipe is size 1 then we should generate an ingredient. Random ingredients are just provided as a random number between 1 and 100. If the size of the recipe is greater than 1 then we can either generate a unary recipe or a binary recipe. This refers to how many children the recipe should have. The only valid binary recipe we have is combine, the rest are all unary as they only apply to one sub-recipe. Instances of Arbitrary are also required for all the other types needed to make recipes such as Time and Measurement. In the interest of space I shalln't go into them here, they are relatively straightforward compared to the above.

The other interesting definition is that for Condition as conditions don't have a natural ordering instance. Instead, QuickSpec allows us to test for observational equality. That is we must specify a function observe test a for which the following property holds: $two\ values\ x\ and\ y\ are\ considered\ equal,$ if for many random values of type test, observe test $x == observe\ test\ y$.

Below we are generating random lists of our Obs type and evaluating our condition against them (Section 4.1). Now that we have all of our in-

stances, we can pass our recipe functions to QuickSpec and see what laws it finds.

5.5 Generating Recipes

While QuickSpec deals with recipes generated arbitrarily, we could also consider how we might generate recipes in a more structured way. This could then be combined with the semantics discussed above to work out the cheapest or most time efficient meals that meet certain criteria. If we want a dish to have certain properties then we first need to create a list of our available ingredients and map them to their properties. As a simple example, here is a list of ingredients given a property called FoodType which simply lables whether the ingredient is a meat or a vegetable.

We also need to know how to cook each ingredient so we will create another list which maps the ingredient to a recipe. There are, of course, many different ways that one could cook each ingredient and this could easily be adapted to map ingredients to a list of recipes. For simplicity though, we shall just stick with one.

Now we need some structured way of selecting ingredients and then combining them. We call this a "cuisine". The type of cuisine that we are

making provides the structure that the ingredients will be placed into. To demonstrate this concept we will use the very simple and traditional "meat and two veg".

```
type Cuisine = PropertyList FoodType \rightarrow PropertyList Recipe \rightarrow Recipe meatTwoVeg :: Cuisine meatTwoVeg is rs = let meats = filter (\lambda(\_,t) \rightarrow t = \text{Meat}) is vegs = filter (\lambda(\_,t) \rightarrow t = \text{Veg}) is ings = map fst $ head ms : take 2 vs parts = map (\lambda s \rightarrow case \ lookup \ s \ rs \ of \ Just \ r \rightarrow r \ Nothing \rightarrow ingredient \ s) is in foldr1 (combine "next to") parts
```

Here we are simply seleting a meat and two vegetables, applying their recipes from the list and then combining them in an appropriate way. Running this example we get the following recipe tree.



Figure 4: Recipe tree for generated recipe example.

This is of course a very simple example, one could imagine modelling much more complex cuisines in this method, maybe even handling the cooking methods for each type of ingredient in the cuisine function itself rather than having a list. Below is an example of a "roast dinner" function which adapts the measurements and cooking times based upon how many it must serve.

5.6 Improving Recipes

We have looked into how we can generate new recipes but what about improving recipes that already exist, or indeed that we have generated? One of the easiest ways to improve a dish is to ensure it has been properly seasoned. Typically people think of salt and pepper when seasoning but there is actually a seasoning triangle [13], consisting of salt, sugar (sweetness) and acid. A dish will taste better if these flavours are all in balance.

Let's start by modelling these seasonings as a data type. We can also model a "flavour profile" as a list of seasonings paired with the frequency they appear in our recipe.

```
data Seasoning = Salt | Sweet | Acid
    deriving (Eq, Ord, Show)

type Profile = [(Seasoning, Int)]
```

Next we can write a function profile that, given a list of seasonings, turns them into a flavour profile.

```
profile :: [Seasoning] → Profile
profile [] = [(Salt, 0), (Sweet, 0), (Acid, 0)]
profile (s:ss) =
   let m = profile ss
        i = fromJust $ lookup s m
   in insert s (i+1) m
```

Finally we can write a function balance which, given a recipe and a mapping from ingredients to the seasoning that they bring to a dish, profiles the seasonings it contains before suggesting what needs to be done to balance them. If there are no seasonings at all, it will suggest we add one of everything. On the other hand, if the seasonings are out of balance, it will suggest the amount of each type of seasoning that is required to balance the dish.

```
balance :: Recipe \rightarrow PropertyList Seasoning \rightarrow [(Seasoning, Int)] balance r ss =

let is = ingredients r

flavours = catMaybes $ map (\lambdai \rightarrow lookup i ss) ings

p = profile flavours

(_,maxI) = maximumBy (\lambda(_,i) (_,i') \rightarrow compare i i')

in case p of

[(Salt, 0), (Sweet, 0), (Acid, 0)] \rightarrow map (\lambda(s,_) \rightarrow

(s,1)) p

\rightarrow [(s, maxI - i) | (s,i) \leftarrow p]
```

This could be combined with the recipe generation functions from the previous section to actually suggest which ingredients could be added to provide each seasoning. To add acid in Thai cuisine, one might add lime juice whereas in Italian cuisine, red wine might be more appropriate.

As an example, let's consider the following, most basic of recipes, an avocado. Avocado is often eaten on its own and has a slightly sweet, creamy flavour. Passing this to our balance function we get the following.

As you can see, we need to add some salt and some acid to our avocado in order to balance the flavours. Adding some salt and a sequeeze of lime juice as follows puts our flavours in balance. This is actually a basic version of the popular dip, guacamole.

```
guacamole :: Recipe
guacamole = multiCombine "mix" avocado
    [salt, limeJuice]

> balance guacamole seasonings = [(Salt,0),(Sweet,0),(Acid,0)]
```

6 Development Process

6.1 Project Management

The project has been managed using the scrum development method with the time between supervisor meetings actings as the sprints, typically two weeks in length. This allowed lots of flexibility regarding the prioritisation of project components and the length of time spent on them. Due to the research nature of the project it wasn't clear from the outset exactly which parts would take the longest or be the most challenging. An example of this is that quite a significant amount of time was spent in the first part of the project considering various semantics for recipes before other parts of the language were started. In the second part of the project a lot of time was spent with scheduling recipes. Trying to express the constraints in linear form was a huge challenge and in the end it seems as though it wasn't actually possible hence the move to bin packing.

Throughout the project, a Trello board was used to keep track of tasks and prioritise them appropriately. The files for the project were stored on GitLab providing version control and backups. Furthermore, GitLab's continuous integration (CI) servers were used to compile the code and run some examples to ensure any issues were found as soon as possible.

6.2 Evaluation and Testing

6.2.1 Test Recipes

6.2.2 QuickCheck

7 Summary

7.1 Contributions

While DSLs are a widely explored field, nothing along the lines of a recipe DSL currently exists. My contributions to filling this gap are the following:

- A small set of extensible combinators that can be used to describe a wide variety of recipes.
- Interpretations of recipes specified using these combinators within various semantic domains.
- A concrete implementation of the recipes in the form of stations in an environment.
- A demonstration of how operational semantics (topological sorting) can be used in scheduling to optimise a recipe via parallelisation.
- Mapping of various properties to recipes potentially leading to the ability to suggest improvements or substitutions.
- Exploration into how, given a certain model (cuisine), one can write functions that generate recipes.

7.2 Future Work

As mentioned above, there does not currently exist much, if any, work in the area of a recipe DSL and as such there is huge scope for future work. More work is needed to perfect and further refine the combinators. There is currently no way to "remove" a recipe from another recipe for example removing the teabag from our cup of tea. An unsafe version of this may just presume that way was added can in fact be removed and that it was even added in the first place however, creating a sensible remove combinator would no doubt require more thought. A further consideration, briefly mentioned above, is that the Measurement passed to the Measure action should potentially be extracted into a condition. This would allow the

modelling of a "reduce" combinator that could be implemented as something along the lines of the following.

```
reduce r t m = addCondition (CondMeasure m) (heatAt t r)
```

In other words: "heat r at temp t until it has reduced to the given measurement".

There is also one rather difficult issue of handling recipes that have multiple outputs. For example let's say we roasted some meat and then wanted to take out the meat juices to make gravy but also do something with the meat. This completely breaks our tree structure as we would have the roast meat node branching up into two nodes, roasted meat and meat juices.

It goes without saying that further optimisations and research could be done into the scheduling part of this project; scheduling is, itself, a huge area of research. The scheduling solutions expressed above were mainly to demonstrate a use of the operational semantics of recipes.

Our model of a cooking environment was rather simple and didn't consider any requirement of transferring recipes between stations. For example, once something has been heated by an oven, it is then immediately available to any other station that needs to perform an action on it regardless of whether a chef is available to take it out of the oven or not.

There is also the task of translating our processes to actual instructions specific to a certain robot. It would be interesting to see what sort of issues would arise from this as they could then be used to direct attention to which areas of the project are most in need of further development.

7.3 Reflections

Being a research oriented project this was certainly different from anything I'd ever done before. Throughout the project there were times when I noticed that I was focusing too much on perfecting certain areas of the project, as if I was developing an actual piece of software, rather than exploring the key parts of each area. For example, rather than taking the combinators I already had and exploring different ways to interpret them, I sometimes wanted to ensure that every feature that could ever be wanted could be expressed. This got easier to deal with as the project continued and my supervisor also helped to keep me focused on the important things when we discussed which tasks should be focused on before the following meeting.

8 Related Work

While a recipe DSL is something that has not previously been researched, there exist many great examples of DSLs for other purposes.

8.1 Financial Contracts

Composing contracts [4] was the first paper I read while doing research for this project. The topic of the paper was to create a DSL in Haskell to describe and process financial contracts. The paper was a huge inspiration as it provided the very basis for my approach to the recipe DSL. The authors of the paper describe boiling down "the immense soup of actively-traded contracts into a reasonably small set of combinators". A similar approach was applied to recipes, we boiled down a number of recipes into their components. Then, while trying to express other recipes and interpret them in various ways, we experienced various issues which then resulted in adjustments to the combinators.

Once the authors had developed their set of combinators, they started modelling a set of evaluation semantics for their contracts. This was a mapping from a contract to a value process where a value process is a "partial function from time to a random variable" [4]. There is some mathematical theory underpinning these value processes but, as stated in the paper, it is unlikely to be familiar to computer scientists and as such I won't go into it further. All that is needed is the notion that a random variable is some representation of the values a contract could hold. This is then used to reason about contracts, one can determine equality by comparing the valuation semantics of two contracts. We took a similar approach to recipes in terms of topological sorting (Section 3).

In the world of financial contracts there are, many different models for predicting change of value over time. This is supported by the contracts DSL by passing a model to the evaluation function. The model contains all the underlying information necessary to evaluate the contract. This is similar to the way in which we pass an environment when scheduling our recipes. As mentioned previously, we could also modify our evaluation functions, for example time, to be based on various information stored in the environment. Perhaps a certain station is capable of performing an action quicker than another. This is however, moving more towards modelling kitchen appliances and away from modelling recipes.

8.2 DSL Development Method

In his paper *Domain Specific Languages* [2], Hudak covers DSLs in a wider context. He mentions commonly used DSLs such as SQL, for accessing databases and HTML for laying out web pages. What has been of particular importance throughout this project is his work on "The DSL Software Development Method" which is outlined as follows.

- Define your domain.
- Design a DSL that accurately captures the domain semantics.
- Build software tools to support the DSL.
- Develop applications (domain instances) using the new DSL infrastructure.

We defined our domain as that of describing recipes. We then designed our combinators in such a way that we captured the semantics of recipes. We could then build tools to support the DSL for example our model of a cooking environment and our scheduling function. The next step might be to develop some more polished applications that make use of the DSL. For example one might consider a "drag and drop" GUI to create recipes using a visual tree structure.

Another piece of valuable information found within Hudak's paper is that one should focus on the semantics of the DSL and not worry too much about the syntax. The only significant change that was made regarding syntax was to ensure that, for combinators that are passed a recipe, the recipe is the final argument thus allowing convenient use of Haskell's (\$) operator. Hudak then goes on to make note of the advantages of embedded DSLs. We discuss the choice to embed our recipe DSL in Haskell in Section 1.2. Michael Snoyman, creator of Yesod, a Haskell web development framework, made a webcast in which he discusses DSLs in Haskell [3].

8.3 Regions

One EDSL mentioned by Hudak in his paper [2] that I found particularly interesting is the DSL to support a "Geometric Region Server" for the Navy [14]. The authors of [14] prototyped the EDSL in various programming languages including Haskell and C++. A committee chosen by the

Navy reviewed the prototypes and determined that the Haskell version was the best as it "took significantly less time to develop and was considerably more concise and easier to understand". This supports our choice of Haskell as the host language for our recipe DSL.

What made the region DSL so interesting is its remarkable simplicity along with the use of a shallow embedding (Section 1.3). The Haskell implementation represents regions as a function which, given a point, returns a boolean value indicating whether or not the point is within the region.

```
type Region = Point \rightarrow Bool
```

Various supporting functions were then created such as the logical negation of a region and the intersection of two regions. Below are the type signatures for various functions as written in [14].

```
circle :: Radius \to Region -- creates a region with given radius outside :: Region \to Region -- the logical negation of a region (/\lambda) :: Region \to Region \to Region -- the intersection of two regions
```

With just a few functions, the DSL is able to express much more complex regions concisely. The following is the definition given by the authors for a function annulus which is "used to define an engageability zone".

```
annulus :: Radius 
ightarrow Radius 
ightarrow Region annulus r1 r2 = outside (circle r1) /\lambda circle r2
```

This demonstrates the extensibility of such DSLs and how complex entities can be described as a construction of primitives. One might also consider how this DSL could be expanded to support regions that move over time. It makes sense that such a feature would be useful to the Navy as one would hope that their ships are not static. We could add this feature as follows.

```
type Transformation = Region \to Region scale :: Transformation \to Time \to Transformation transform :: Time \to Transformation \to Region \to Region
```

A transformation takes a region and adjusts it in some way. The scale function is used to increase or decrease the magnitude of a transformation. Imagine a ship travelling at 15 metres per second and that the ship has some region around it representing the range of its weapons. One could create a transformation that displaces a region 15 metres in the direction the ship is travelling. They could then apply transform to their initial region, passing the transformation and the elapsed time. This would use

the scale function to increase the displacement of the region relative to the time elapsed before applying the scaled transformation to the initial region to acquire the new region.

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