

Salary MLR 2nd Draft

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2022-05-02

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```
library(tidyverse)
```

```
## -- Attaching packages ----- tidyverse 1.3.1 --
```

```
## v ggplot2 3.3.5      v purrr  0.3.4
## v tibble  3.1.6      v dplyr  1.0.8
## v tidyr   1.2.0      v stringr 1.4.0
## v readr   2.1.2      v forcats 0.5.1
```

```
## -- Conflicts ----- tidyverse_conflicts() --
```

```
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()    masks stats::lag()
```

```
library(randomForest)
```

```
## randomForest 4.7-1
```

```
## Type rfNews() to see new features/changes/bug fixes.
```

```

##
## Attaching package: 'randomForest'
## The following object is masked from 'package:dplyr':
##
##      combine
## The following object is masked from 'package:ggplot2':
##
##      margin
library(parallel)
library(rpart)
library(readr)
library(janitor)

##
## Attaching package: 'janitor'
## The following objects are masked from 'package:stats':
##
##      chisq.test, fisher.test
library(car)

## Loading required package: carData
##
## Attaching package: 'car'
## The following object is masked from 'package:dplyr':
##
##      recode
## The following object is masked from 'package:purrr':
##
##      some
library(MASS)

##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##      select
library(Hmisc)

## Loading required package: lattice
## Loading required package: survival
## Loading required package: Formula
##
## Attaching package: 'Hmisc'
## The following objects are masked from 'package:dplyr':
##
##      src, summarize

```

```

## The following objects are masked from 'package:base':
##
##   format.pval, units
library(rstatix)

##
## Attaching package: 'rstatix'
## The following object is masked from 'package:MASS':
##
##   select
## The following object is masked from 'package:janitor':
##
##   make_clean_names
## The following object is masked from 'package:stats':
##
##   filter
library(forcats)
library(GGally)

## Registered S3 method overwritten by 'GGally':
##   method from
##   +.gg   ggplot2
library(performance)
library(caret)

##
## Attaching package: 'caret'
## The following object is masked from 'package:survival':
##
##   cluster
## The following object is masked from 'package:purrr':
##
##   lift
library(lmtest)

## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##   as.Date, as.Date.numeric
library(corrplot)

## corrplot 0.92 loaded
library(PerformanceAnalytics)

## Loading required package: xts
##

```

```
## Attaching package: 'xts'
## The following objects are masked from 'package:dplyr':
##
##     first, last
##
## Attaching package: 'PerformanceAnalytics'
## The following object is masked from 'package:graphics':
##
##     legend
library(plotly)

##
## Attaching package: 'plotly'
## The following object is masked from 'package:Hmisc':
##
##     subplot
## The following object is masked from 'package:MASS':
##
##     select
## The following object is masked from 'package:ggplot2':
##
##     last_plot
## The following object is masked from 'package:stats':
##
##     filter
## The following object is masked from 'package:graphics':
##
##     layout
library(mlbench)
```

Intro

blahblahblah Hi

Question - How do the various stats from the ESPN website explain the salaries of NBA players?

Where data is from

Variables explained

Data Exploration

```
# Load dataset

players <- read_csv("players.csv")

## Rows: 558 Columns: 12
## -- Column specification -----
## Delimiter: ","
## chr (5): Name, Position, Team, Height, College
```

```
## dbl (7): Age, Height_i, Weight, Salary, Points, Rebounds, Assists
##
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this message.
active_p <- read_csv("active_players_2.csv")

## Rows: 558 Columns: 9
## -- Column specification -----
## Delimiter: ","
## chr (5): Name, Team, Position, Height, College
## dbl (4): Age, Height_i, Weight, Salary
##
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this message.
# Structure/Dimensions of the data.frame
str(active_p)

## spec_tbl_df [558 x 9] (S3: spec_tbl_df/tbl_df/tbl/data.frame)
## $ Name      : chr [1:558] "Juhann Begarin" "Jaylen Brown" "Kris Dunn" "Carsen Edwards" ...
## $ Team       : chr [1:558] "Boston Celtics" "Boston Celtics" "Boston Celtics" "Boston Celtics" ...
## $ Position   : chr [1:558] "SG" "SG" "PG" "PG" ...
## $ Age        : num [1:558] 19 24 27 23 25 23 35 29 26 21 ...
## $ Height     : chr [1:558] "6' 5\"" "6' 6\"" "6' 3\"" "5' 11\"" ...
## $ Height_i   : num [1:558] 6.5 6.6 6.3 5.11 7.5 6.9 6.9 6.1 7.2 6.4 ...
## $ Weight     : num [1:558] 185 223 205 200 311 240 240 250 250 216 ...
## $ College    : chr [1:558] "nan" "California" "Providence" "Purdue" ...
## $ Salary     : num [1:558] NaN 26758928 5005350 1782621 NaN ...
## - attr(*, "spec")=
## .. cols(
## ..   Name = col_character(),
## ..   Team = col_character(),
## ..   Position = col_character(),
## ..   Age = col_double(),
## ..   Height = col_character(),
## ..   Height_i = col_double(),
## ..   Weight = col_double(),
## ..   College = col_character(),
## ..   Salary = col_double()
## .. )
## - attr(*, "problems")=<externalptr>
# Number of columns containing `NA` or `NaN`
colSums(is.na(active_p))

##      Name      Team Position      Age      Height Height_i      Weight      College
##      0         0         0         0         0         0         0         0
## Salary
##      113
```

Data Cleaning

```
#identifying the rows with NAs
rownames(active_p)[apply(active_p, 2, anyNA)]
```

```
## [1] "9" "18" "27" "36" "45" "54" "63" "72" "81" "90" "99" "108"
## [13] "117" "126" "135" "144" "153" "162" "171" "180" "189" "198" "207" "216"
## [25] "225" "234" "243" "252" "261" "270" "279" "288" "297" "306" "315" "324"
## [37] "333" "342" "351" "360" "369" "378" "387" "396" "405" "414" "423" "432"
## [49] "441" "450" "459" "468" "477" "486" "495" "504" "513" "522" "531" "540"
## [61] "549" "558"

#removing all `Salary` observations with NAs
ap_cl <- active_p[!(is.na(active_p$Salary)), ]

# Checking for leftover `NA` after cleaning
rownames(active_p)[apply(ap_cl, 2, anyNA)]

## character(0)

# Transforming Team, Position, College into factors
ap_cl_f <- transform (
  ap_cl,
  fTeam = as.factor(Team),
  fPosition = as.factor(Position),
  fCollege = as.factor(College)
)

# Rename `fCollege` factor level "nan" as "None"
# levels(ap_cl_f$fCollege)[levels(ap_cl_f$fCollege)=="nan"] <- "None"
#levels(ap_cl_f$fCollege)

str(ap_cl_f)

## 'data.frame': 445 obs. of 12 variables:
## $ Name : chr "Jaylen Brown" "Kris Dunn" "Carsen Edwards" "Bruno Fernando" ...
## $ Team : chr "Boston Celtics" "Boston Celtics" "Boston Celtics" "Boston Celtics" ...
## $ Position : chr "SG" "PG" "PG" "F" ...
## $ Age : num 24 27 23 23 35 29 21 21 26 23 ...
## $ Height : chr "6' 6\"" "6' 3\"" "5' 11\"" "6' 9\"" ...
## $ Height_i : num 6.6 6.3 5.11 6.9 6.9 6.1 6.4 6.5 6.8 6.1 ...
## $ Weight : num 223 205 200 240 240 250 216 215 245 195 ...
## $ College : chr "California" "Providence" "Purdue" "Maryland" ...
## $ Salary : num 26758928 5005350 1782621 1782621 27000000 ...
## $ fTeam : Factor w/ 30 levels "Atlanta Hawks",...: 2 2 2 2 2 2 2 2 2 ...
## $ fPosition: Factor w/ 7 levels "C","F","G","PF",...: 7 5 5 2 1 1 7 6 4 5 ...
## $ fCollege : Factor w/ 119 levels "Alabama","Arizona",...: 15 79 80 50 26 41 36 104 25 75 ...
```

Recoding for Logistic Regression

```
# Start with `ap_cl_f` data.frame, reclassify as tibble

ap_tibble <- as_tibble(ap_cl_f)
class(ap_tibble)

## [1] "tbl_df"      "tbl"        "data.frame"

# Calculate quantiles of Salary for good cutoff point
quantile(ap_tibble$Salary, probs = seq(0,1,1/20))

##      0%      5%      10%      15%      20%      25%      30%      35%
## 925258 1517981 1669178 1669178 1778656 1802057 2103509 2573040
```

```
##      40%      45%      50%      55%      60%      65%      70%      75%
## 3242760 3900751 4447896 5027304 6412964 8222063 9697392 12000000
##      80%      85%      90%      95%     100%
## 14324647 17943158 23600000 31650600 45780966
```

```
ap_tibble <- ap_tibble %>% mutate(Salary.Dummy = if_else(Salary >= 8222063, 1, 0))
```

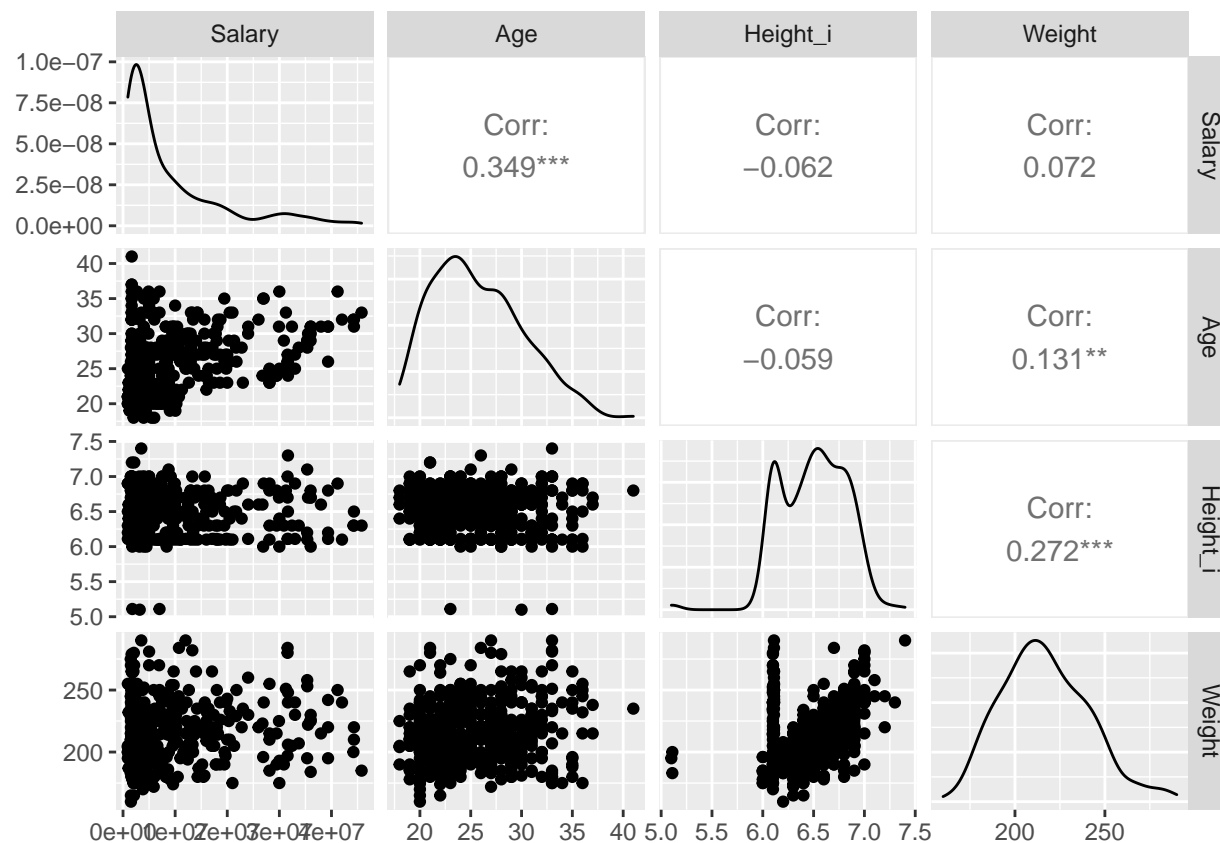
```
str(ap_tibble)
```

```
## tibble [445 x 13] (S3: tbl_df/tbl/data.frame)
##  $ Name      : chr [1:445] "Jaylen Brown" "Kris Dunn" "Carsen Edwards" "Bruno Fernando" ...
##  $ Team      : chr [1:445] "Boston Celtics" "Boston Celtics" "Boston Celtics" "Boston Celtics" ...
##  $ Position  : chr [1:445] "SG" "PG" "PG" "F" ...
##  $ Age       : num [1:445] 24 27 23 23 35 29 21 21 26 23 ...
##  $ Height    : chr [1:445] "6' 6\"" "6' 3\"" "5' 11\"" "6' 9\"" ...
##  $ Height_i   : num [1:445] 6.6 6.3 5.11 6.9 6.9 6.1 6.4 6.5 6.8 6.1 ...
##  $ Weight    : num [1:445] 223 205 200 240 240 250 216 215 245 195 ...
##  $ College   : chr [1:445] "California" "Providence" "Purdue" "Maryland" ...
##  $ Salary    : num [1:445] 26758928 5005350 1782621 1782621 27000000 ...
##  $ fTeam     : Factor w/ 30 levels "Atlanta Hawks",...: 2 2 2 2 2 2 2 2 2 ...
##  $ fPosition  : Factor w/ 7 levels "C","F","G","PF",...: 7 5 5 2 1 1 7 6 4 5 ...
##  $ fCollege   : Factor w/ 119 levels "Alabama","Arizona",...: 15 79 80 50 26 41 36 104 25 75 ...
##  $ Salary.Dummy: num [1:445] 1 0 0 0 1 0 0 0 0 0 ...
```

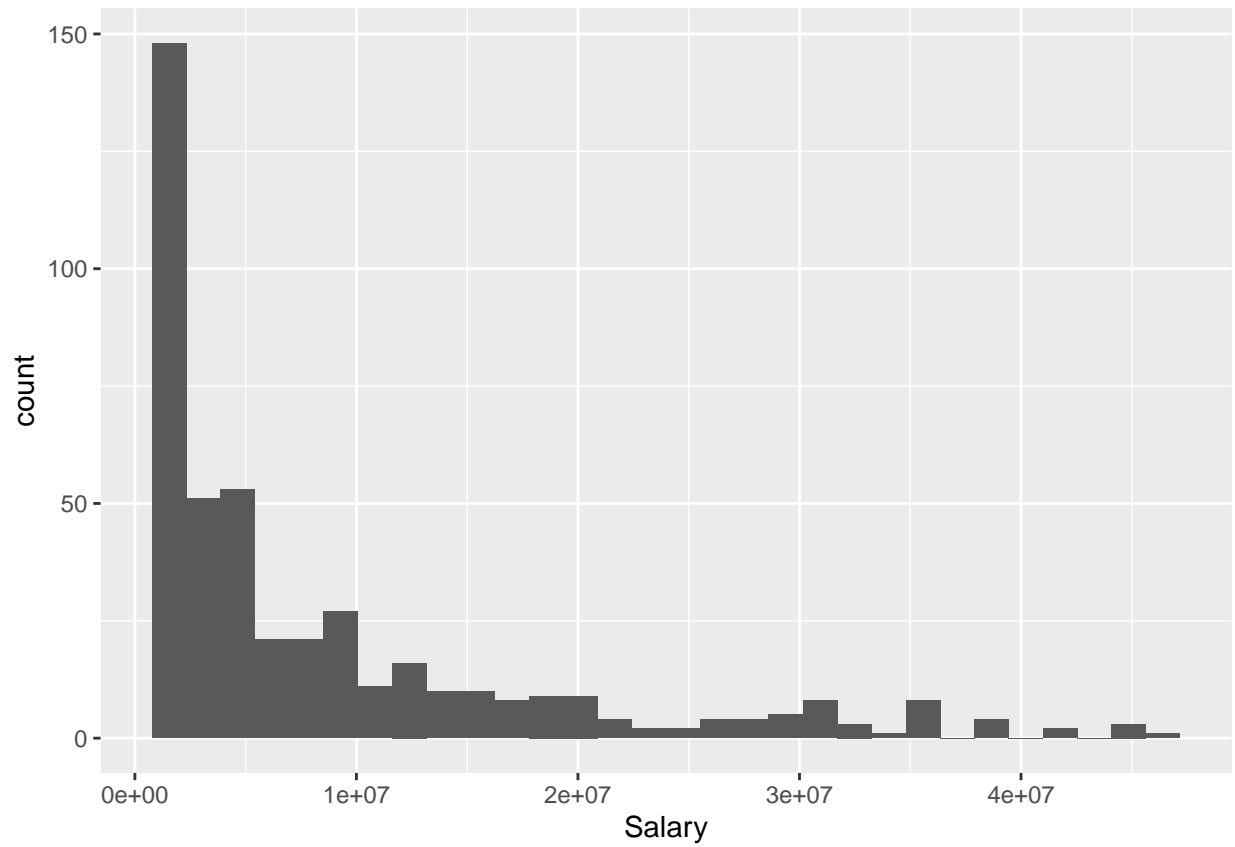
Model Building

Initial Graphs

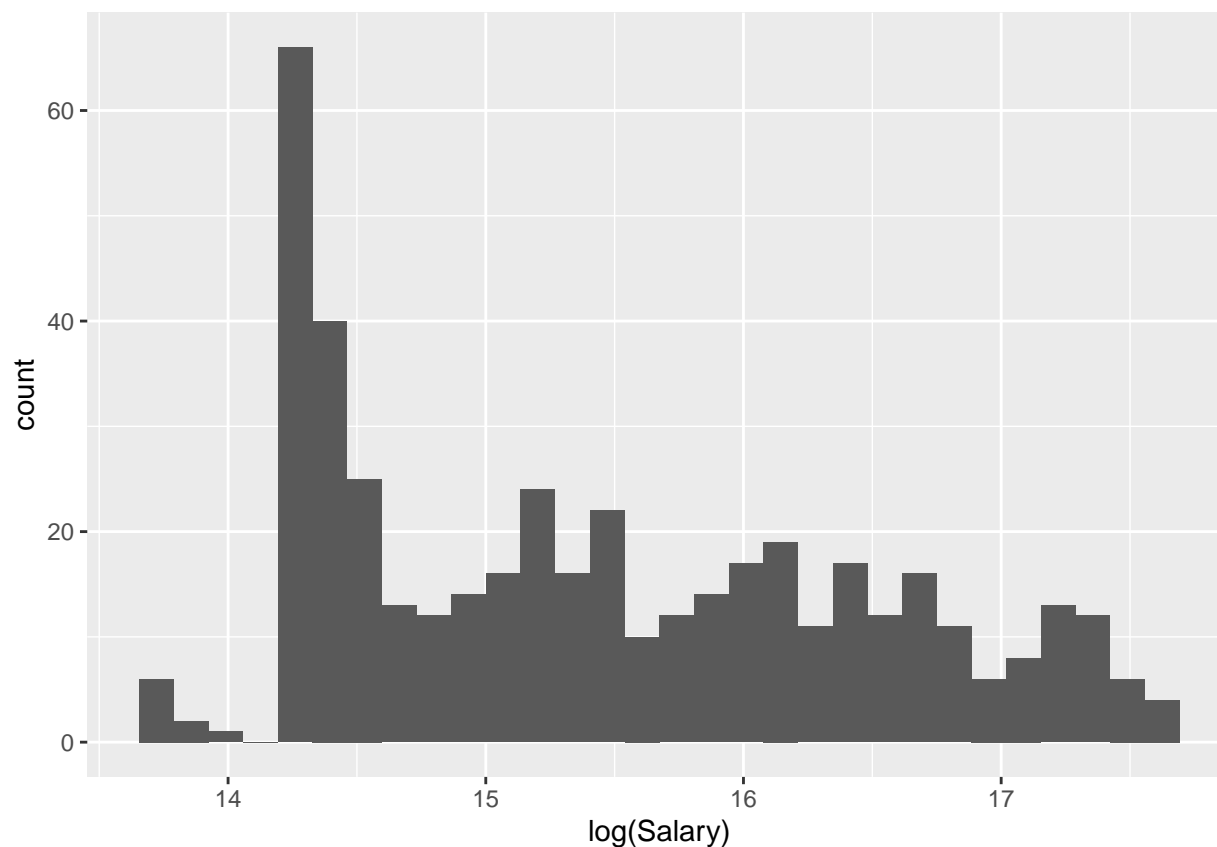
```
# The diagonal consists of the densities of the three variables and the upper panels consist of the cor
ggpairs(ap_tibble, columns = c(9,4,6,7), cardinality_threshold = NULL)
```



```
ggplot(ap_tibble, aes(Salary)) +  
  geom_histogram(bins = 30)
```

```
ggplot(ap_tibble, aes(log(Salary))) +  
  geom_histogram(bins = 30)
```



Full(Initial) Model

```
summary(lm1 <- lm(Salary ~ fTeam+fPosition+fCollege+Age+Height_i+Weight, data=ap_tibble))
```

```
##
## Call:
## lm(formula = Salary ~ fTeam + fPosition + fCollege + Age + Height_i +
##     Weight, data = ap_tibble)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -18232129 -4355864         0  2782057 27394419
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -43409716   16626942  -2.611  0.009506 **
## fTeamBoston Celtics   -2139600    3999655  -0.535  0.593100
## fTeamBrooklyn Nets    1376171    3812791   0.361  0.718412
## fTeamCharlotte Hornets -2482487    3742196  -0.663  0.507620
## fTeamChicago Bulls    1451456    4130193   0.351  0.725526
## fTeamCleveland Cavaliers  2396367    4078738   0.588  0.557310
## fTeamDallas Mavericks -2179304    3816160  -0.571  0.568396
## fTeamDenver Nuggets     618798    3904190   0.158  0.874177
## fTeamDetroit Pistons  -3902716    3911500  -0.998  0.319236
## fTeamGolden State Warriors -1024287    3989880  -0.257  0.797577
## fTeamHouston Rockets  -2388664    3848381  -0.621  0.535292
```

## fTeamIndiana Pacers	-391881	3957015	-0.099	0.921180	
## fTeamLos Angeles Clippers	-1764702	4039118	-0.437	0.662509	
## fTeamLos Angeles Lakers	-3269636	4131496	-0.791	0.429366	
## fTeamMemphis Grizzlies	-2112003	3994901	-0.529	0.597438	
## fTeamMiami Heat	-3585954	4065171	-0.882	0.378449	
## fTeamMilwaukee Bucks	965708	4021669	0.240	0.810403	
## fTeamMinnesota Timberwolves	4551282	4220656	1.078	0.281786	
## fTeamNew Orleans Pelicans	-647960	3745909	-0.173	0.862790	
## fTeamNew York Knicks	-1878918	3824003	-0.491	0.623554	
## fTeamOklahoma City Thunder	-2754850	3934686	-0.700	0.484402	
## fTeamOrlando Magic	-1166824	3960187	-0.295	0.768482	
## fTeamPhiladelphia Sixers	605822	3977677	0.152	0.879053	
## fTeamPhoenix Suns	917437	4004371	0.229	0.818947	
## fTeamPortland Trail Blazers	-5390573	4402004	-1.225	0.221737	
## fTeamSacramento Kings	1570102	4017930	0.391	0.696253	
## fTeamSan Antonio Spurs	-473258	3895515	-0.121	0.903389	
## fTeamToronto Raptors	-1433236	4269557	-0.336	0.737351	
## fTeamUtah Jazz	1116045	4098972	0.272	0.785606	
## fTeamWashington Wizards	-1153886	3721264	-0.310	0.756725	
## fPositionF	1204828	4375387	0.275	0.783233	
## fPositionG	10656218	5190359	2.053	0.040968	*
## fPositionPF	2889966	1929730	1.498	0.135332	
## fPositionPG	11138355	2996036	3.718	0.000242	***
## fPositionSF	6497102	2150070	3.022	0.002738	**
## fPositionSG	7196111	2549099	2.823	0.005089	**
## fCollegeArizona	660692	5617835	0.118	0.906462	
## fCollegeArizona State	9982902	7299120	1.368	0.172477	
## fCollegeArkansas	469247	6682154	0.070	0.944064	
## fCollegeAuburn	1571889	7223599	0.218	0.827891	
## fCollegeBaylor	-2481774	6392019	-0.388	0.698109	
## fCollegeBelmont	-4855131	10707722	-0.453	0.650585	
## fCollegeBoise State	-3368144	10882863	-0.309	0.757172	
## fCollegeBoston College	-2494383	10912629	-0.229	0.819359	
## fCollegeBowling Green	4292252	10993543	0.390	0.696504	
## fCollegeBucknell	-955784	11010106	-0.087	0.930883	
## fCollegeButler	5918936	8385665	0.706	0.480858	
## fCollegeBYU	-7249423	10885559	-0.666	0.505965	
## fCollegeCal Poly	-2510893	10854196	-0.231	0.817223	
## fCollegeCalifornia	20654255	10910430	1.893	0.059350	.
## fCollegeCharleston	-7563826	10944739	-0.691	0.490064	
## fCollegeCleveland State	-3436899	10754028	-0.320	0.749509	
## fCollegeColorado	3697341	7210164	0.513	0.608487	
## fCollegeConnecticut	2729879	6316981	0.432	0.665956	
## fCollegeCreighton	117698	8236695	0.014	0.988609	
## fCollegeDavidson	33917971	10894796	3.113	0.002037	**
## fCollegeDayton	4072786	10799793	0.377	0.706364	
## fCollegeDePaul	-3115672	8308080	-0.375	0.707924	
## fCollegeDrexel	-6131316	10875214	-0.564	0.573337	
## fCollegeDuke	3327920	4889327	0.681	0.496640	
## fCollegeFlorida	7222763	6360647	1.136	0.257094	
## fCollegeFlorida State	2056866	5638667	0.365	0.715544	
## fCollegeFresno State	28832960	10936707	2.636	0.008835	**
## fCollegeGeorge Washington	-4562823	10945256	-0.417	0.677079	
## fCollegeGeorgetown	-4952188	7222440	-0.686	0.493475	

## fCollegeGeorgia	1704338	7265198	0.235	0.814694	
## fCollegeGeorgia Tech	-162680	7296193	-0.022	0.982227	
## fCollegeGonzaga	3856775	5893987	0.654	0.513404	
## fCollegeHouston	-4382913	8216914	-0.533	0.594167	
## fCollegeIllinois	-2109111	8695076	-0.243	0.808516	
## fCollegeIndiana	2041078	5902780	0.346	0.729759	
## fCollegeIowa State	-1846631	6292715	-0.293	0.769385	
## fCollegeIUPUI	-11029514	11901368	-0.927	0.354836	
## fCollegeKansas	6022649	5599807	1.076	0.283047	
## fCollegeKansas State	-3378939	7184555	-0.470	0.638492	
## fCollegeKentucky	7582646	4841408	1.566	0.118398	
## fCollegeLehigh	29182543	11042973	2.643	0.008676	**
## fCollegeLiberty	-3208200	10817453	-0.297	0.767004	
## fCollegeLouisiana-Lafayette	-9654690	10882355	-0.887	0.375718	
## fCollegeLouisville	5632489	6343176	0.888	0.375303	
## fCollegeLoyola (MD)	3748003	10921836	0.343	0.731724	
## fCollegeLSU	356961	6584833	0.054	0.956806	
## fCollegeMarquette	6687787	7321909	0.913	0.361799	
## fCollegeMarshall	-11070017	10986738	-1.008	0.314502	
## fCollegeMaryland	-1916231	6356430	-0.301	0.763279	
## fCollegeMemphis	5812091	6643567	0.875	0.382387	
## fCollegeMiami (FL)	-811418	8207611	-0.099	0.921317	
## fCollegeMichigan	3993331	5748518	0.695	0.487821	
## fCollegeMichigan State	7610990	6394741	1.190	0.234950	
## fCollegeMinnesota	2246389	10908141	0.206	0.836986	
## fCollegeMississippi State	-7276374	10965548	-0.664	0.507498	
## fCollegeMissouri	-688399	7200677	-0.096	0.923903	
## fCollegeMissouri State	-2738954	10820839	-0.253	0.800357	
## fCollegeMurray State	1990539	8321722	0.239	0.811122	
## fCollegenan	3285715	4643254	0.708	0.479746	
## fCollegeNebraska	-1116174	8350171	-0.134	0.893756	
## fCollegeNevada	-5189084	8364267	-0.620	0.535494	
## fCollegeNew Mexico	-2333981	11045614	-0.211	0.832800	
## fCollegeNew Mexico JC	5006924	11080370	0.452	0.651700	
## fCollegeNew Mexico State	19434510	11053679	1.758	0.079777	.
## fCollegeNorth Carolina	-949428	5521054	-0.172	0.863586	
## fCollegeNorth Carolina State	3651398	10887643	0.335	0.737590	
## fCollegeNotre Dame	-4567492	10892999	-0.419	0.675306	
## fCollegeOhio	-3366614	10864360	-0.310	0.756879	
## fCollegeOhio State	6567510	7284072	0.902	0.368009	
## fCollegeOklahoma	540170	7256431	0.074	0.940712	
## fCollegeOklahoma State	4055621	8379129	0.484	0.628743	
## fCollegeOld Dominion	-3988140	10922934	-0.365	0.715293	
## fCollegeOle Miss	-2925069	10901041	-0.268	0.788638	
## fCollegeOregon	755727	6247375	0.121	0.903801	
## fCollegeOregon State	-4591241	10728739	-0.428	0.669016	
## fCollegePenn State	-4050789	11386818	-0.356	0.722293	
## fCollegePittsburgh	10090316	11007453	0.917	0.360077	
## fCollegeProvidence	-4574929	10858708	-0.421	0.673840	
## fCollegePurdue	-4613061	11090707	-0.416	0.677764	
## fCollegeRadford	-12134400	10912877	-1.112	0.267094	
## fCollegeSaint Joseph's	-1392672	8514159	-0.164	0.870183	
## fCollegeSaint Mary's	-6101377	8244976	-0.740	0.459896	
## fCollegeSalt Lake CC UT	-8037516	10865039	-0.740	0.460048	

```
## fCollegeSan Diego State      9244590      7253561      1.274 0.203517
## fCollegeSMU                  -4825688      7272754     -0.664 0.507522
## fCollegeSouth Carolina      -4588005     10681331     -0.430 0.667855
## fCollegeSt. John's          -6903125     10934001     -0.631 0.528316
## fCollegeStanford             781509      6103557      0.128 0.898206
## fCollegeSyracuse            -1627849      6331447     -0.257 0.797281
## fCollegeTCU                  -2381903      8336740     -0.286 0.775304
## fCollegeTennessee           6904659      6421508      1.075 0.283167
## fCollegeTennessee State     12472584     11084456      1.125 0.261428
## fCollegeTexas                7193501      5372870      1.339 0.181673
## fCollegeTexas A&M            6348154      6736758      0.942 0.346821
## fCollegeTexas Tech          156150      8670496      0.018 0.985644
## fCollegeUC Santa Barbara    -4543256     10815854     -0.420 0.674758
## fCollegeUCLA                 8760281      5414101      1.618 0.106747
## fCollegeUNLV                 6960075      7410230      0.939 0.348388
## fCollegeUSC                  3612676      5610377      0.644 0.520135
## fCollegeUSC Upstate         -5806804     10900473     -0.533 0.594644
## fCollegeUtah                 4123587      7198620      0.573 0.567207
## fCollegeUtah State          -2882745     10855217     -0.266 0.790766
## fCollegeVanderbilt          -1368396      6621199     -0.207 0.836414
## fCollegeVillanova            -148498      5520203     -0.027 0.978558
## fCollegeVirginia             522108      5781111      0.090 0.928102
## fCollegeVirginia Commonwealth -561324     10687760     -0.053 0.958151
## fCollegeVirginia Tech       -1338244     10510698     -0.127 0.898774
## fCollegeWake Forest          4051041      6318899      0.641 0.521968
## fCollegeWashington           2105986      5699779      0.369 0.712037
## fCollegeWashington State     15483585      8425597      1.838 0.067139 .
## fCollegeWeber State          31799371     11072060      2.872 0.004381 **
## fCollegeWest Virginia        -5678638      8274292     -0.686 0.493077
## fCollegeWestern Texas Coll. (J.C.) -6332252     10759470     -0.589 0.556639
## fCollegeWichita State         6661369      8415955      0.792 0.429294
## fCollegeWisconsin            -4235075      8582977     -0.493 0.622087
## fCollegeWyoming              1513570      8402762      0.180 0.857179
## fCollegeXavier               -5456878      8094128     -0.674 0.500739
## fCollegeYale                 -5344975     10870850     -0.492 0.623320
## Age                          632383      129540      4.882 1.74e-06 ***
## Height_i                     -1394      1908175     -0.001 0.999418
## Weight                        131345      38186      3.440 0.000669 ***
```

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 9385000 on 288 degrees of freedom
## Multiple R-squared:  0.4155, Adjusted R-squared:  0.09891
## F-statistic: 1.312 on 156 and 288 DF, p-value: 0.02448
```

```
shapiro.test(resid(lm1))
```

```
##
## Shapiro-Wilk normality test
##
## data:  resid(lm1)
## W = 0.9352, p-value = 5.455e-13
```

```
bptest(lm1)
```

```
##
## studentized Breusch-Pagan test
##
## data:  lm1
## BP = 181.76, df = 156, p-value = 0.07744
```

```
log(Full Model)
```

```
summary(lm_l1 <- lm(log(Salary) ~ fTeam+fPosition+fCollege+Age+Height_i+Weight, data=ap_tibble))
```

```
##
## Call:
## lm(formula = log(Salary) ~ fTeam + fPosition + fCollege + Age +
##     Height_i + Weight, data = ap_tibble)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.9390 -0.5096  0.0000  0.5006  2.0837
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    1.019e+01  1.704e+00   5.981 6.57e-09 ***
## fTeamBoston Celtics    -3.519e-01  4.098e-01  -0.859 0.391211
## fTeamBrooklyn Nets     -3.157e-01  3.907e-01  -0.808 0.419695
## fTeamCharlotte Hornets  -2.616e-01  3.834e-01  -0.682 0.495661
## fTeamChicago Bulls      5.956e-02  4.232e-01   0.141 0.888167
## fTeamCleveland Cavaliers  3.029e-01  4.179e-01   0.725 0.469158
## fTeamDallas Mavericks  -2.849e-01  3.910e-01  -0.729 0.466886
## fTeamDenver Nuggets    -1.534e-01  4.000e-01  -0.384 0.701595
## fTeamDetroit Pistons   -4.307e-01  4.008e-01  -1.075 0.283378
## fTeamGolden State Warriors -3.802e-01  4.088e-01  -0.930 0.353184
## fTeamHouston Rockets   -4.673e-01  3.943e-01  -1.185 0.236914
## fTeamIndiana Pacers     2.479e-05  4.054e-01   0.000 0.999951
## fTeamLos Angeles Clippers -2.494e-01  4.138e-01  -0.603 0.547291
## fTeamLos Angeles Lakers  -9.898e-01  4.233e-01  -2.338 0.020058 *
## fTeamMemphis Grizzlies  -1.615e-01  4.093e-01  -0.395 0.693389
## fTeamMiami Heat        -7.197e-01  4.165e-01  -1.728 0.085068 .
## fTeamMilwaukee Bucks   -4.504e-01  4.121e-01  -1.093 0.275300
## fTeamMinnesota Timberwolves  3.236e-01  4.325e-01   0.748 0.454928
## fTeamNew Orleans Pelicans -1.511e-01  3.838e-01  -0.394 0.694192
## fTeamNew York Knicks    -3.476e-01  3.918e-01  -0.887 0.375776
## fTeamOklahoma City Thunder -3.002e-01  4.031e-01  -0.745 0.457064
## fTeamOrlando Magic     -3.362e-02  4.058e-01  -0.083 0.934023
## fTeamPhiladelphia Sixers -2.516e-01  4.076e-01  -0.617 0.537461
## fTeamPhoenix Suns       4.483e-02  4.103e-01   0.109 0.913068
## fTeamPortland Trail Blazers -7.391e-01  4.510e-01  -1.639 0.102380
## fTeamSacramento Kings   -1.278e-02  4.117e-01  -0.031 0.975255
## fTeamSan Antonio Spurs  -1.354e-01  3.991e-01  -0.339 0.734708
## fTeamToronto Raptors    -2.856e-01  4.375e-01  -0.653 0.514437
## fTeamUtah Jazz         -1.014e-01  4.200e-01  -0.241 0.809467
## fTeamWashington Wizards  -2.724e-01  3.813e-01  -0.714 0.475550
## fPositionF             -1.160e-01  4.483e-01  -0.259 0.796030
```

## fPositionG	1.439e+00	5.318e-01	2.705	0.007235	**
## fPositionPF	2.784e-01	1.977e-01	1.408	0.160200	
## fPositionPG	1.122e+00	3.070e-01	3.655	0.000306	***
## fPositionSF	6.935e-01	2.203e-01	3.148	0.001816	**
## fPositionSG	8.278e-01	2.612e-01	3.169	0.001692	**
## fCollegeArizona	-5.687e-03	5.756e-01	-0.010	0.992124	
## fCollegeArizona State	2.313e-01	7.479e-01	0.309	0.757384	
## fCollegeArkansas	-1.152e-01	6.847e-01	-0.168	0.866477	
## fCollegeAuburn	-1.507e-01	7.401e-01	-0.204	0.838788	
## fCollegeBaylor	-3.934e-01	6.549e-01	-0.601	0.548492	
## fCollegeBelmont	-1.104e+00	1.097e+00	-1.006	0.315289	
## fCollegeBoise State	-3.856e-01	1.115e+00	-0.346	0.729723	
## fCollegeBoston College	2.154e-03	1.118e+00	0.002	0.998464	
## fCollegeBowling Green	8.366e-01	1.126e+00	0.743	0.458233	
## fCollegeBucknell	-2.955e-01	1.128e+00	-0.262	0.793568	
## fCollegeButler	-1.978e-01	8.592e-01	-0.230	0.818121	
## fCollegeBYU	-1.074e+00	1.115e+00	-0.963	0.336431	
## fCollegeCal Poly	-7.272e-02	1.112e+00	-0.065	0.947907	
## fCollegeCalifornia	1.678e+00	1.118e+00	1.501	0.134481	
## fCollegeCharleston	-1.227e+00	1.121e+00	-1.095	0.274615	
## fCollegeCleveland State	-3.873e-01	1.102e+00	-0.352	0.725461	
## fCollegeColorado	5.909e-01	7.388e-01	0.800	0.424476	
## fCollegeConnecticut	3.018e-02	6.472e-01	0.047	0.962846	
## fCollegeCreighton	-1.533e-01	8.439e-01	-0.182	0.855972	
## fCollegeDavidson	1.766e+00	1.116e+00	1.582	0.114654	
## fCollegeDayton	6.805e-01	1.107e+00	0.615	0.539034	
## fCollegeDePaul	-7.680e-01	8.512e-01	-0.902	0.367714	
## fCollegeDrexel	-1.065e+00	1.114e+00	-0.956	0.339791	
## fCollegeDuke	2.588e-01	5.010e-01	0.517	0.605780	
## fCollegeFlorida	3.140e-01	6.517e-01	0.482	0.630327	
## fCollegeFlorida State	8.523e-02	5.777e-01	0.148	0.882829	
## fCollegeFresno State	1.469e+00	1.121e+00	1.311	0.190801	
## fCollegeGeorge Washington	-1.022e+00	1.121e+00	-0.911	0.363084	
## fCollegeGeorgetown	-7.592e-01	7.400e-01	-1.026	0.305807	
## fCollegeGeorgia	3.399e-01	7.444e-01	0.457	0.648330	
## fCollegeGeorgia Tech	1.457e-01	7.476e-01	0.195	0.845559	
## fCollegeGonzaga	4.516e-01	6.039e-01	0.748	0.455193	
## fCollegeHouston	-1.001e+00	8.419e-01	-1.189	0.235234	
## fCollegeIllinois	-6.296e-01	8.909e-01	-0.707	0.480322	
## fCollegeIndiana	7.484e-02	6.048e-01	0.124	0.901609	
## fCollegeIowa State	6.467e-02	6.448e-01	0.100	0.920171	
## fCollegeIUPUI	-1.109e+00	1.219e+00	-0.909	0.364023	
## fCollegeKansas	3.708e-01	5.738e-01	0.646	0.518624	
## fCollegeKansas State	-1.062e+00	7.361e-01	-1.443	0.150095	
## fCollegeKentucky	4.924e-01	4.961e-01	0.993	0.321723	
## fCollegeLehigh	2.263e+00	1.131e+00	2.000	0.046470	*
## fCollegeLiberty	-1.035e+00	1.108e+00	-0.934	0.351132	
## fCollegeLouisiana-Lafayette	-1.647e+00	1.115e+00	-1.477	0.140777	
## fCollegeLouisville	4.744e-01	6.499e-01	0.730	0.465988	
## fCollegeLoyola (MD)	-1.505e-01	1.119e+00	-0.134	0.893140	
## fCollegeLSU	-2.511e-01	6.747e-01	-0.372	0.710035	
## fCollegeMarquette	3.169e-01	7.502e-01	0.422	0.673011	
## fCollegeMarshall	-1.677e+00	1.126e+00	-1.490	0.137322	
## fCollegeMaryland	-2.306e-01	6.513e-01	-0.354	0.723507	

## fCollegeMemphis	8.919e-01	6.807e-01	1.310	0.191148
## fCollegeMiami (FL)	1.562e-01	8.410e-01	0.186	0.852744
## fCollegeMichigan	1.357e-01	5.890e-01	0.230	0.817940
## fCollegeMichigan State	6.134e-01	6.552e-01	0.936	0.349983
## fCollegeMinnesota	-5.505e-01	1.118e+00	-0.493	0.622692
## fCollegeMississippi State	-1.327e+00	1.124e+00	-1.181	0.238645
## fCollegeMissouri	-2.656e-02	7.378e-01	-0.036	0.971306
## fCollegeMissouri State	-4.607e-01	1.109e+00	-0.416	0.678059
## fCollegeMurray State	4.170e-01	8.526e-01	0.489	0.625176
## fCollegenan	2.281e-01	4.757e-01	0.479	0.631961
## fCollegeNebraska	-9.216e-01	8.556e-01	-1.077	0.282321
## fCollegeNevada	-8.471e-01	8.570e-01	-0.988	0.323790
## fCollegeNew Mexico	-8.228e-01	1.132e+00	-0.727	0.467787
## fCollegeNew Mexico JC	8.206e-01	1.135e+00	0.723	0.470359
## fCollegeNew Mexico State	1.207e+00	1.133e+00	1.066	0.287349
## fCollegeNorth Carolina	-1.272e-01	5.657e-01	-0.225	0.822241
## fCollegeNorth Carolina State	4.695e-01	1.116e+00	0.421	0.674188
## fCollegeNotre Dame	4.433e-02	1.116e+00	0.040	0.968344
## fCollegeOhio	-1.321e+00	1.113e+00	-1.187	0.236257
## fCollegeOhio State	2.907e-01	7.463e-01	0.390	0.697179
## fCollegeOklahoma	-1.639e-02	7.435e-01	-0.022	0.982432
## fCollegeOklahoma State	7.368e-01	8.585e-01	0.858	0.391469
## fCollegeOld Dominion	-5.627e-01	1.119e+00	-0.503	0.615503
## fCollegeOle Miss	-2.728e-01	1.117e+00	-0.244	0.807203
## fCollegeOregon	-2.058e-02	6.401e-01	-0.032	0.974379
## fCollegeOregon State	-9.986e-01	1.099e+00	-0.908	0.364412
## fCollegePenn State	-9.945e-01	1.167e+00	-0.852	0.394691
## fCollegePittsburgh	1.013e+00	1.128e+00	0.899	0.369657
## fCollegeProvidence	-2.831e-01	1.113e+00	-0.254	0.799349
## fCollegePurdue	-9.438e-01	1.136e+00	-0.831	0.406907
## fCollegeRadford	-1.869e+00	1.118e+00	-1.671	0.095753
## fCollegeSaint Joseph's	-5.300e-01	8.724e-01	-0.608	0.543962
## fCollegeSaint Mary's	-9.261e-01	8.448e-01	-1.096	0.273894
## fCollegeSalt Lake CC UT	-1.128e+00	1.113e+00	-1.014	0.311647
## fCollegeSan Diego State	2.396e-01	7.432e-01	0.322	0.747425
## fCollegeSMU	-7.416e-01	7.452e-01	-0.995	0.320461
## fCollegeSouth Carolina	-9.239e-01	1.094e+00	-0.844	0.399259
## fCollegeSt. John's	-6.082e-01	1.120e+00	-0.543	0.587648
## fCollegeStanford	4.214e-02	6.254e-01	0.067	0.946317
## fCollegeSyracuse	-5.396e-01	6.487e-01	-0.832	0.406254
## fCollegeTCU	-8.616e-01	8.542e-01	-1.009	0.313972
## fCollegeTennessee	4.604e-01	6.580e-01	0.700	0.484637
## fCollegeTennessee State	1.619e+00	1.136e+00	1.426	0.154963
## fCollegeTexas	6.648e-01	5.505e-01	1.208	0.228190
## fCollegeTexas A&M	5.730e-01	6.903e-01	0.830	0.407123
## fCollegeTexas Tech	-4.151e-01	8.884e-01	-0.467	0.640655
## fCollegeUC Santa Barbara	-7.964e-01	1.108e+00	-0.719	0.472957
## fCollegeUCLA	6.803e-01	5.547e-01	1.226	0.221071
## fCollegeUNLV	1.039e+00	7.593e-01	1.369	0.172176
## fCollegeUSC	2.117e-01	5.748e-01	0.368	0.712893
## fCollegeUSC Upstate	-6.704e-01	1.117e+00	-0.600	0.548787
## fCollegeUtah	6.648e-01	7.376e-01	0.901	0.368130
## fCollegeUtah State	-1.221e+00	1.112e+00	-1.098	0.273143
## fCollegeVanderbilt	-3.627e-01	6.784e-01	-0.535	0.593354


```
## fCollegeVillanova          -1.298e-01  5.656e-01  -0.229  0.818650
## fCollegeVirginia           -1.059e-01  5.923e-01  -0.179  0.858169
## fCollegeVirginia Commonwealth -2.968e-01  1.095e+00  -0.271  0.786539
## fCollegeVirginia Tech      -3.159e-01  1.077e+00  -0.293  0.769470
## fCollegeWake Forest        1.980e-01  6.474e-01   0.306  0.760007
## fCollegeWashington         1.117e-01  5.840e-01   0.191  0.848389
## fCollegeWashington State    6.777e-01  8.633e-01   0.785  0.433087
## fCollegeWeber State        1.994e+00  1.134e+00   1.758  0.079800
## fCollegeWest Virginia      -8.985e-01  8.478e-01  -1.060  0.290096
## fCollegeWestern Texas Coll. (J.C.) -1.320e+00  1.102e+00  -1.197  0.232158
## fCollegeWichita State       5.866e-01  8.623e-01   0.680  0.496855
## fCollegeWisconsin          -9.329e-01  8.794e-01  -1.061  0.289640
## fCollegeWyoming            8.380e-02  8.610e-01   0.097  0.922531
## fCollegeXavier             -1.139e+00  8.293e-01  -1.373  0.170670
## fCollegeYale               -1.058e+00  1.114e+00  -0.950  0.342838
## Age                        7.574e-02  1.327e-02   5.706  2.87e-08 ***
## Height_i                   2.641e-03  1.955e-01   0.014  0.989234
## Weight                     1.312e-02  3.913e-03   3.352  0.000909 ***
```

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
## Residual standard error: 0.9616 on 288 degrees of freedom
## Multiple R-squared:  0.4318, Adjusted R-squared:  0.1241
## F-statistic: 1.403 on 156 and 288 DF, p-value: 0.007015
```

```
shapiro.test(resid(lm_l1))
```

```
##
## Shapiro-Wilk normality test
##
## data:  resid(lm_l1)
## W = 0.99129, p-value = 0.01014
```

```
bptest(lm_l1)
```

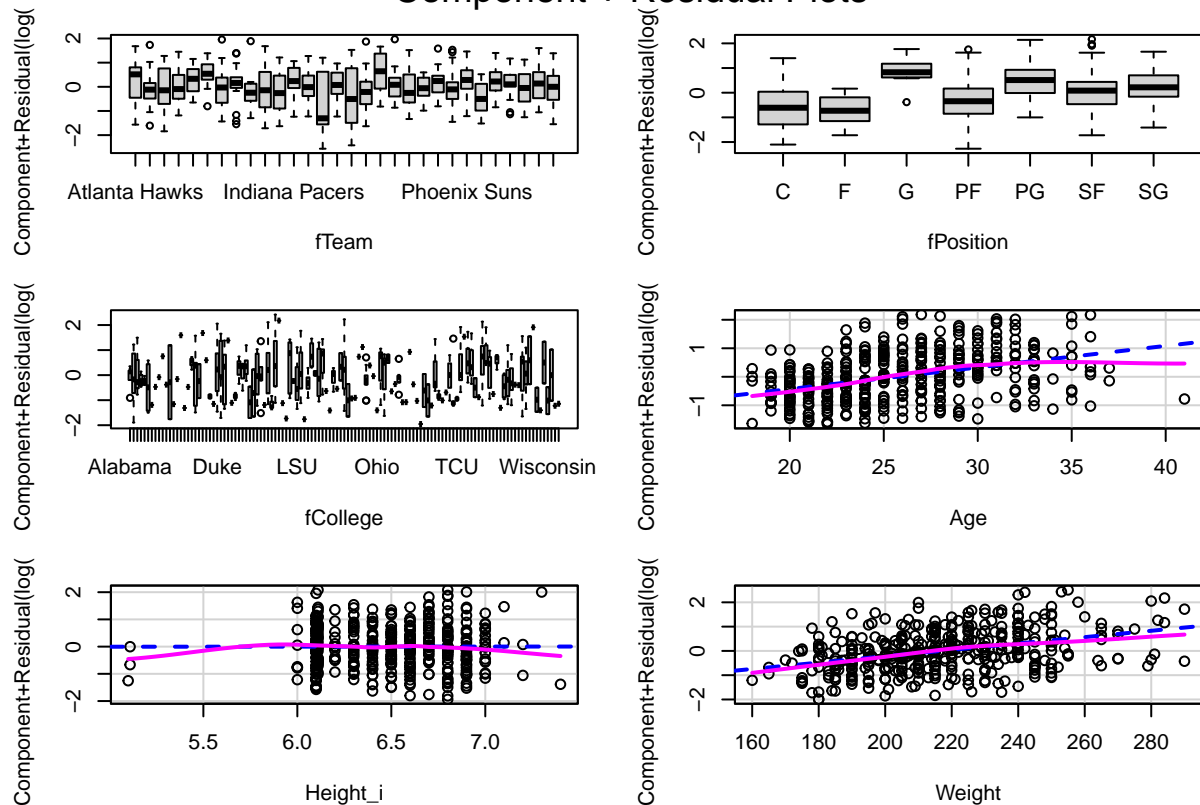
```
##
## studentized Breusch-Pagan test
##
## data:  lm_l1
## BP = 183.73, df = 156, p-value = 0.06393
```

Check for Polynomial Terms

Age, Height_i, and Weight appear to be misspecified.

```
crPlots(lm_l1)
```

Component + Residual Plots



```
#summary(lm(Salary ~ fTeam+fPosition+fCollege+poly(Age,2)+poly(Height_i,2)+poly(Weight,2),data=ap_tibble))
#summary(lm(Salary ~ fTeam+fPosition+fCollege+poly(Age,3)+poly(Height_i,3)+poly(Weight,3),data=ap_tibble))
#summary(lm(Salary ~ fTeam+fPosition+fCollege+poly(Age,4)+poly(Height_i,4)+poly(Weight,4),data=ap_tibble))
#summary(lm(Salary ~ fTeam+fPosition+fCollege+poly(Age,3)+Height_i+poly(Weight,2),data=ap_tibble))
#summary(lm(Salary ~ fTeam+fPosition+fCollege+poly(Age,3)+Height_i+poly(Weight,3),data=ap_tibble))
#summary(lm(Salary ~ fTeam+fPosition+fCollege+poly(Age,3)+Height_i+poly(Weight,4),data=ap_tibble))
summary(lm(Salary ~ fTeam+fPosition+fCollege+poly(Age,3)+Height_i+Weight,data=ap_tibble))
```

```
##
```

```
## Call:
```

```
## lm(formula = Salary ~ fTeam + fPosition + fCollege + poly(Age,
##      3) + Height_i + Weight, data = ap_tibble)
```

```
##
```

```
## Residuals:
```

```
##      Min      1Q   Median      3Q      Max
## -15845192 -4236590         0  2817577 26638013
```

```
##
```

```
## Coefficients:
```

```
##      Estimate Std. Error t value Pr(>|t|)
## (Intercept) -28100952  15781292  -1.781 0.076031 .
## fTeamBoston Celtics -2498579  3911629  -0.639 0.523493
## fTeamBrooklyn Nets  1208781  3717723   0.325 0.745313
## fTeamCharlotte Hornets -2219790  3642960  -0.609 0.542785
## fTeamChicago Bulls  1652120  4025361   0.410 0.681800
## fTeamCleveland Cavaliers  2377524  3984428   0.597 0.551177
## fTeamDallas Mavericks -3389325  3729024  -0.909 0.364166
```

## fTeamDenver Nuggets	437732	3812044	0.115	0.908662	
## fTeamDetroit Pistons	-3846509	3809424	-1.010	0.313476	
## fTeamGolden State Warriors	-350777	3887045	-0.090	0.928158	
## fTeamHouston Rockets	-1858619	3759594	-0.494	0.621427	
## fTeamIndiana Pacers	-1004796	3859340	-0.260	0.794778	
## fTeamLos Angeles Clippers	-2114869	3932077	-0.538	0.591099	
## fTeamLos Angeles Lakers	1093475	4154710	0.263	0.792594	
## fTeamMemphis Grizzlies	-2076115	3907834	-0.531	0.595644	
## fTeamMiami Heat	-429517	4040691	-0.106	0.915420	
## fTeamMilwaukee Bucks	377816	3924182	0.096	0.923367	
## fTeamMinnesota Timberwolves	4431981	4114690	1.077	0.282338	
## fTeamNew Orleans Pelicans	-385444	3657333	-0.105	0.916141	
## fTeamNew York Knicks	-1171706	3729507	-0.314	0.753620	
## fTeamOklahoma City Thunder	-3153191	3832208	-0.823	0.411300	
## fTeamOrlando Magic	-941755	3860819	-0.244	0.807463	
## fTeamPhiladelphia Sixers	486633	3875890	0.126	0.900173	
## fTeamPhoenix Suns	1692378	3913939	0.432	0.665778	
## fTeamPortland Trail Blazers	-5537907	4289388	-1.291	0.197721	
## fTeamSacramento Kings	1268408	3926289	0.323	0.746889	
## fTeamSan Antonio Spurs	-286506	3791591	-0.076	0.939819	
## fTeamToronto Raptors	-262010	4164719	-0.063	0.949881	
## fTeamUtah Jazz	1601893	3992059	0.401	0.688521	
## fTeamWashington Wizards	-2087478	3632563	-0.575	0.565975	
## fPositionF	2519006	4279585	0.589	0.556588	
## fPositionG	8219984	5088842	1.615	0.107349	
## fPositionPF	3291038	1886069	1.745	0.082073	.
## fPositionPG	10784169	2920784	3.692	0.000266	***
## fPositionSF	6255406	2093384	2.988	0.003050	**
## fPositionSG	6395862	2488767	2.570	0.010680	*
## fCollegeArizona	1382765	5493872	0.252	0.801460	
## fCollegeArizona State	10784722	7115422	1.516	0.130704	
## fCollegeArkansas	1450593	6511372	0.223	0.823867	
## fCollegeAuburn	1898033	7031083	0.270	0.787394	
## fCollegeBaylor	-3602280	6297436	-0.572	0.567756	
## fCollegeBelmont	-5083373	10466785	-0.486	0.627575	
## fCollegeBoise State	-5279062	10640005	-0.496	0.620168	
## fCollegeBoston College	-3404067	10626862	-0.320	0.748955	
## fCollegeBowling Green	3047889	10717258	0.284	0.776317	
## fCollegeBucknell	-2129193	10726865	-0.198	0.842801	
## fCollegeButler	5005869	8183586	0.612	0.541225	
## fCollegeBYU	-7660288	10636835	-0.720	0.472011	
## fCollegeCal Poly	-5109108	10636425	-0.480	0.631352	
## fCollegeCalifornia	21163722	10657701	1.986	0.048014	*
## fCollegeCharleston	-9169410	10749959	-0.853	0.394389	
## fCollegeCleveland State	-5129372	10506415	-0.488	0.625773	
## fCollegeColorado	1849371	7069392	0.262	0.793816	
## fCollegeConnecticut	2865171	6154223	0.466	0.641884	
## fCollegeCreighton	-1509364	8096986	-0.186	0.852255	
## fCollegeDavidson	33677639	10605701	3.175	0.001660	**
## fCollegeDayton	2591182	10579730	0.245	0.806694	
## fCollegeDePaul	-4753693	8139829	-0.584	0.559678	
## fCollegeDrexel	-8446967	10639340	-0.794	0.427890	
## fCollegeDuke	3092084	4807875	0.643	0.520656	
## fCollegeFlorida	13470522	6446073	2.090	0.037526	*

## fCollegeFlorida State	1935365	5537669	0.349	0.726978	
## fCollegeFresno State	28125947	10649255	2.641	0.008718	**
## fCollegeGeorge Washington	-7497793	10734801	-0.698	0.485459	
## fCollegeGeorgetown	-5582970	7052110	-0.792	0.429207	
## fCollegeGeorgia	2040386	7094103	0.288	0.773848	
## fCollegeGeorgia Tech	-580477	7119767	-0.082	0.935077	
## fCollegeGonzaga	3777179	5786363	0.653	0.514427	
## fCollegeHouston	-4761057	8019032	-0.594	0.553169	
## fCollegeIllinois	-3488387	8502914	-0.410	0.681924	
## fCollegeIndiana	1007865	5784293	0.174	0.861799	
## fCollegeIowa State	-3623880	6161080	-0.588	0.556870	
## fCollegeIUPUI	-4038890	11705180	-0.345	0.730309	
## fCollegeKansas	4947024	5498897	0.900	0.369069	
## fCollegeKansas State	-4989749	7051286	-0.708	0.479747	
## fCollegeKentucky	6494719	4782295	1.358	0.175510	
## fCollegeLehigh	27483171	10764435	2.553	0.011195	*
## fCollegeLiberty	-2389168	10590315	-0.226	0.821674	
## fCollegeLouisiana-Lafayette	-12350528	10641111	-1.161	0.246755	
## fCollegeLouisville	5014092	6222956	0.806	0.421061	
## fCollegeLoyola (MD)	4464526	10633872	0.420	0.674917	
## fCollegeLSU	1999235	6427567	0.311	0.755996	
## fCollegeMarquette	3292324	7175419	0.459	0.646702	
## fCollegeMarshall	-12040813	10696791	-1.126	0.261259	
## fCollegeMaryland	-2934526	6227120	-0.471	0.637822	
## fCollegeMemphis	4498849	6475068	0.695	0.487747	
## fCollegeMiami (FL)	-870338	8077425	-0.108	0.914270	
## fCollegeMichigan	3078492	5644098	0.545	0.585879	
## fCollegeMichigan State	7111058	6257510	1.136	0.256739	
## fCollegeMinnesota	3041650	10619794	0.286	0.774769	
## fCollegeMississippi State	-5835428	10679555	-0.546	0.585209	
## fCollegeMissouri	-1132507	7034778	-0.161	0.872217	
## fCollegeMissouri State	-4390876	10661196	-0.412	0.680754	
## fCollegeMurray State	705079	8138762	0.087	0.931024	
## fCollegenan	3174190	4535979	0.700	0.484633	
## fCollegeNebraska	-1288031	8189270	-0.157	0.875133	
## fCollegeNevada	-5857444	8152967	-0.718	0.473071	
## fCollegeNew Mexico	-4463277	10769091	-0.414	0.678853	
## fCollegeNew Mexico JC	564927	10879279	0.052	0.958623	
## fCollegeNew Mexico State	16437669	10840045	1.516	0.130527	
## fCollegeNorth Carolina	-1063109	5382619	-0.198	0.843570	
## fCollegeNorth Carolina State	2000823	10621694	0.188	0.850719	
## fCollegeNotre Dame	-5636466	10622718	-0.531	0.596104	
## fCollegeOhio	-2697562	10627270	-0.254	0.799806	
## fCollegeOhio State	5798889	7152955	0.811	0.418213	
## fCollegeOklahoma	17897	7094417	0.003	0.997989	
## fCollegeOklahoma State	4013545	8155318	0.492	0.622999	
## fCollegeOld Dominion	-9205156	10704741	-0.860	0.390557	
## fCollegeOle Miss	-2656805	10650493	-0.249	0.803189	
## fCollegeOregon	856521	6129671	0.140	0.888969	
## fCollegeOregon State	-5714923	10536958	-0.542	0.587986	
## fCollegePenn State	-5892811	11105678	-0.531	0.596099	
## fCollegePittsburgh	8694966	10721574	0.811	0.418052	
## fCollegeProvidence	-5989598	10598828	-0.565	0.572436	
## fCollegePurdue	-3314444	10820431	-0.306	0.759589	

```

## fCollegeRadford -14426877 10659952 -1.353 0.177006
## fCollegeSaint Joseph's -2965471 8376739 -0.354 0.723590
## fCollegeSaint Mary's -6047256 8056433 -0.751 0.453503
## fCollegeSalt Lake CC UT -10880073 10643457 -1.022 0.307535
## fCollegeSan Diego State 7854033 7132262 1.101 0.271736
## fCollegeSMU -5285879 7151073 -0.739 0.460408
## fCollegeSouth Carolina -4521499 10443725 -0.433 0.665385
## fCollegeSt. John's -8794906 10660997 -0.825 0.410081
## fCollegeStanford 1121244 5941628 0.189 0.850454
## fCollegeSyracuse -1418323 6229719 -0.228 0.820065
## fCollegeTCU -2697656 8177543 -0.330 0.741728
## fCollegeTennessee 6738844 6249945 1.078 0.281842
## fCollegeTennessee State 9770533 10813158 0.904 0.366980
## fCollegeTexas 7398399 5242145 1.411 0.159234
## fCollegeTexas A&M 4934943 6604185 0.747 0.455530
## fCollegeTexas Tech 2204694 8452618 0.261 0.794412
## fCollegeUC Santa Barbara -8660385 10617693 -0.816 0.415376
## fCollegeUCLA 8027049 5310660 1.511 0.131766
## fCollegeUNLV 5032114 7306594 0.689 0.491565
## fCollegeUSC 3799320 5468361 0.695 0.487756
## fCollegeUSC Upstate -7223806 10616061 -0.680 0.496764
## fCollegeUtah 2909863 7074883 0.411 0.681164
## fCollegeUtah State -3429652 10601561 -0.324 0.746550
## fCollegeVanderbilt -894356 6466689 -0.138 0.890099
## fCollegeVillanova -527126 5426549 -0.097 0.922685
## fCollegeVirginia -97997 5698792 -0.017 0.986292
## fCollegeVirginia Commonwealth 258139 10403851 0.025 0.980222
## fCollegeVirginia Tech -1184659 10271646 -0.115 0.908262
## fCollegeWake Forest 5093695 6173462 0.825 0.410005
## fCollegeWashington 1943710 5575400 0.349 0.727629
## fCollegeWashington State 15316326 8210495 1.865 0.063141 .
## fCollegeWeber State 30495429 10781106 2.829 0.005006 **
## fCollegeWest Virginia -5746988 8089955 -0.710 0.478044
## fCollegeWestern Texas Coll. (J.C.) -6269050 10547757 -0.594 0.552748
## fCollegeWichita State 4937906 8257823 0.598 0.550335
## fCollegeWisconsin -8412031 8439429 -0.997 0.319727
## fCollegeWyoming 301299 8228168 0.037 0.970815
## fCollegeXavier -5822278 7941972 -0.733 0.464097
## fCollegeYale -5860643 10670185 -0.549 0.583260
## poly(Age, 3)1 54655272 11709494 4.668 4.69e-06 ***
## poly(Age, 3)2 -42509394 11928551 -3.564 0.000428 ***
## poly(Age, 3)3 -24531140 11073435 -2.215 0.027526 *
## Height_i 698756 1871492 0.373 0.709151
## Weight 116620 37351 3.122 0.001978 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 9134000 on 286 degrees of freedom
## Multiple R-squared: 0.4502, Adjusted R-squared: 0.1465
## F-statistic: 1.482 on 158 and 286 DF, p-value: 0.0021

```

The end result is that only Age has been misspecified, and has been re-specified as poly(Age,3).

Reduced Model

```
summary(lm_log1 <- lm(log(Salary) ~ fTeam+fPosition+fCollege+poly(Age,3)+Height_i+Weight, data=ap_tibble))
```

```
##
## Call:
## lm(formula = log(Salary) ~ fTeam + fPosition + fCollege + poly(Age,
##     3) + Height_i + Weight, data = ap_tibble)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.0695 -0.4836  0.0000  0.4824  2.0273
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    12.043683    1.618465   7.441 1.17e-12 ***
## fTeamBoston Celtics    -0.374141    0.401161  -0.933 0.351789
## fTeamBrooklyn Nets     -0.340770    0.381275  -0.894 0.372199
## fTeamCharlotte Hornets  -0.233372    0.373607  -0.625 0.532702
## fTeamChicago Bulls      0.087408    0.412825   0.212 0.832467
## fTeamCleveland Cavaliers  0.313679    0.408627   0.768 0.443334
## fTeamDallas Mavericks   -0.400137    0.382434  -1.046 0.296310
## fTeamDenver Nuggets     -0.160452    0.390948  -0.410 0.681806
## fTeamDetroit Pistons    -0.419976    0.390679  -1.075 0.283286
## fTeamGolden State Warriors -0.315033    0.398640  -0.790 0.430025
## fTeamHouston Rockets    -0.425153    0.385569  -1.103 0.271099
## fTeamIndiana Pacers     -0.054030    0.395798  -0.137 0.891514
## fTeamLos Angeles Clippers -0.283448    0.403258  -0.703 0.482693
## fTeamLos Angeles Lakers  -0.558302    0.426090  -1.310 0.191149
## fTeamMemphis Grizzlies   -0.143422    0.400772  -0.358 0.720708
## fTeamMiami Heat         -0.389433    0.414397  -0.940 0.348135
## fTeamMilwaukee Bucks    -0.500471    0.402448  -1.244 0.214677
## fTeamMinnesota Timberwolves  0.320329    0.421986   0.759 0.448419
## fTeamNew Orleans Pelicans -0.114140    0.375081  -0.304 0.761115
## fTeamNew York Knicks     -0.270026    0.382483  -0.706 0.480774
## fTeamOklahoma City Thunder -0.344376    0.393016  -0.876 0.381635
## fTeamOrlando Magic       -0.002917    0.395950  -0.007 0.994127
## fTeamPhiladelphia Sixers  -0.256713    0.397496  -0.646 0.518909
## fTeamPhoenix Suns        0.134262    0.401398   0.334 0.738259
## fTeamPortland Trail Blazers -0.746262    0.439902  -1.696 0.090893 .
## fTeamSacramento Kings    -0.030373    0.402664  -0.075 0.939925
## fTeamSan Antonio Spurs    -0.116766    0.388850  -0.300 0.764178
## fTeamToronto Raptors     -0.166230    0.427117  -0.389 0.697424
## fTeamUtah Jazz           -0.055919    0.409409  -0.137 0.891455
## fTeamWashington Wizards  -0.359851    0.372541  -0.966 0.334892
## fPositionF              0.026966    0.438897   0.061 0.951052
## fPositionG              1.201822    0.521891   2.303 0.022007 *
## fPositionPF             0.313371    0.193428   1.620 0.106314
## fPositionPG             1.080926    0.299544   3.609 0.000363 ***
## fPositionSF             0.669712    0.214689   3.119 0.001997 **
## fPositionSG             0.745132    0.255238   2.919 0.003786 **
## fCollegeArizona          0.085742    0.563429   0.152 0.879153
## fCollegeArizona State     0.325108    0.729729   0.446 0.656282
## fCollegeArkansas         -0.008287    0.667780  -0.012 0.990107
```

## fCollegeAuburn	-0.115713	0.721079	-0.160	0.872623
## fCollegeBaylor	-0.471312	0.645839	-0.730	0.466130
## fCollegeBelmont	-1.090632	1.073431	-1.016	0.310476
## fCollegeBoise State	-0.544291	1.091196	-0.499	0.618302
## fCollegeBoston College	-0.078651	1.089848	-0.072	0.942520
## fCollegeBowling Green	0.731551	1.099119	0.666	0.506216
## fCollegeBucknell	-0.398495	1.100104	-0.362	0.717444
## fCollegeButler	-0.268787	0.839275	-0.320	0.749004
## fCollegeBYU	-1.080330	1.090871	-0.990	0.322846
## fCollegeCal Poly	-0.294131	1.090829	-0.270	0.787632
## fCollegeCalifornia	1.762453	1.093011	1.612	0.107961
## fCollegeCharleston	-1.337265	1.102472	-1.213	0.226142
## fCollegeCleveland State	-0.527030	1.077495	-0.489	0.625128
## fCollegeColorado	0.432306	0.725008	0.596	0.551462
## fCollegeConnecticut	0.053908	0.631152	0.085	0.931993
## fCollegeCreighton	-0.277264	0.830394	-0.334	0.738704
## fCollegeDavidson	1.750097	1.087678	1.609	0.108715
## fCollegeDayton	0.574159	1.085014	0.529	0.597097
## fCollegeDePaul	-0.901192	0.834788	-1.080	0.281254
## fCollegeDrexel	-1.263824	1.091128	-1.158	0.247719
## fCollegeDuke	0.260423	0.493076	0.528	0.597798
## fCollegeFlorida	0.980413	0.661083	1.483	0.139165
## fCollegeFlorida State	0.100377	0.567921	0.177	0.859834
## fCollegeFresno State	1.408751	1.092144	1.290	0.198129
## fCollegeGeorge Washington	-1.274873	1.100918	-1.158	0.247826
## fCollegeGeorgetown	-0.802373	0.723236	-1.109	0.268180
## fCollegeGeorgia	0.394645	0.727542	0.542	0.587941
## fCollegeGeorgia Tech	0.122449	0.730174	0.168	0.866939
## fCollegeGonzaga	0.471640	0.593426	0.795	0.427404
## fCollegeHouston	-1.017824	0.822399	-1.238	0.216869
## fCollegeIllinois	-0.740160	0.872024	-0.849	0.396712
## fCollegeIndiana	-0.005835	0.593214	-0.010	0.992159
## fCollegeIowa State	-0.094649	0.631855	-0.150	0.881032
## fCollegeIUPUI	-0.419290	1.200436	-0.349	0.727135
## fCollegeKansas	0.287996	0.563945	0.511	0.609968
## fCollegeKansas State	-1.193704	0.723151	-1.651	0.099898
## fCollegeKentucky	0.411688	0.490453	0.839	0.401944
## fCollegeLehigh	2.108315	1.103957	1.910	0.057162
## fCollegeLiberty	-0.911002	1.086100	-0.839	0.402292
## fCollegeLouisiana-Lafayette	-1.888017	1.091309	-1.730	0.084700
## fCollegeLouisville	0.440683	0.638201	0.691	0.490435
## fCollegeLoyola (MD)	-0.087411	1.090567	-0.080	0.936172
## fCollegeLSU	-0.074724	0.659185	-0.113	0.909826
## fCollegeMarquette	-0.014981	0.735882	-0.020	0.983772
## fCollegeMarshall	-1.768418	1.097019	-1.612	0.108060
## fCollegeMaryland	-0.308302	0.638628	-0.483	0.629638
## fCollegeMemphis	0.765476	0.664057	1.153	0.249985
## fCollegeMiami (FL)	0.194588	0.828388	0.235	0.814455
## fCollegeMichigan	0.070056	0.578836	0.121	0.903753
## fCollegeMichigan State	0.586704	0.641745	0.914	0.361364
## fCollegeMinnesota	-0.463466	1.089123	-0.426	0.670763
## fCollegeMississippi State	-1.174394	1.095252	-1.072	0.284507
## fCollegeMissouri	-0.048929	0.721458	-0.068	0.945976
## fCollegeMissouri State	-0.567238	1.093369	-0.519	0.604302

## fCollegeMurray State	0.315173	0.834678	0.378	0.706009
## fCollegenan	0.231327	0.465192	0.497	0.619379
## fCollegeNebraska	-0.901567	0.839858	-1.073	0.283963
## fCollegeNevada	-0.898709	0.836135	-1.075	0.283353
## fCollegeNew Mexico	-1.022391	1.104434	-0.926	0.355375
## fCollegeNew Mexico JC	0.410371	1.115735	0.368	0.713292
## fCollegeNew Mexico State	0.947580	1.111711	0.852	0.394726
## fCollegeNorth Carolina	-0.127039	0.552020	-0.230	0.818152
## fCollegeNorth Carolina State	0.326403	1.089318	0.300	0.764670
## fCollegeNotre Dame	-0.040278	1.089423	-0.037	0.970533
## fCollegeOhio	-1.214985	1.089890	-1.115	0.265882
## fCollegeOhio State	0.247982	0.733578	0.338	0.735578
## fCollegeOklahoma	-0.044424	0.727575	-0.061	0.951356
## fCollegeOklahoma State	0.735074	0.836376	0.879	0.380204
## fCollegeOld Dominion	-1.077595	1.097835	-0.982	0.327144
## fCollegeOle Miss	-0.211418	1.092271	-0.194	0.846659
## fCollegeOregon	0.018247	0.628634	0.029	0.976864
## fCollegeOregon State	-1.060304	1.080628	-0.981	0.327327
## fCollegePenn State	-1.158480	1.138953	-1.017	0.309944
## fCollegePittsburgh	0.883148	1.099561	0.803	0.422537
## fCollegeProvidence	-0.398284	1.086973	-0.366	0.714325
## fCollegePurdue	-0.787739	1.109700	-0.710	0.478365
## fCollegeRadford	-2.072153	1.093241	-1.895	0.059045
## fCollegeSaint Joseph's	-0.644945	0.859084	-0.751	0.453429
## fCollegeSaint Mary's	-0.894140	0.826235	-1.082	0.280082
## fCollegeSalt Lake CC UT	-1.376906	1.091550	-1.261	0.208184
## fCollegeSan Diego State	0.135275	0.731456	0.185	0.853408
## fCollegeSMU	-0.750477	0.733385	-1.023	0.307028
## fCollegeSouth Carolina	-0.880228	1.071066	-0.822	0.411862
## fCollegeSt. John's	-0.781249	1.093349	-0.715	0.475472
## fCollegeStanford	0.072780	0.609349	0.119	0.905011
## fCollegeSyracuse	-0.484707	0.638895	-0.759	0.448678
## fCollegeTCU	-0.855784	0.838656	-1.020	0.308390
## fCollegeTennessee	0.442793	0.640969	0.691	0.490240
## fCollegeTennessee State	1.361532	1.108954	1.228	0.220546
## fCollegeTexas	0.698902	0.537613	1.300	0.194644
## fCollegeTexas A&M	0.457468	0.677298	0.675	0.499948
## fCollegeTexas Tech	-0.206779	0.866866	-0.239	0.811636
## fCollegeUC Santa Barbara	-1.173666	1.088908	-1.078	0.282014
## fCollegeUCLA	0.630161	0.544640	1.157	0.248228
## fCollegeUNLV	0.885205	0.749335	1.181	0.238457
## fCollegeUSC	0.241331	0.560813	0.430	0.667284
## fCollegeUSC Upstate	-0.805572	1.088740	-0.740	0.459961
## fCollegeUtah	0.577608	0.725571	0.796	0.426650
## fCollegeUtah State	-1.243961	1.087253	-1.144	0.253526
## fCollegeVanderbilt	-0.295474	0.663197	-0.446	0.656274
## fCollegeVillanova	-0.139847	0.556525	-0.251	0.801774
## fCollegeVirginia	-0.135298	0.584445	-0.231	0.817094
## fCollegeVirginia Commonwealth	-0.216397	1.066977	-0.203	0.839425
## fCollegeVirginia Tech	-0.266175	1.053418	-0.253	0.800699
## fCollegeWake Forest	0.320538	0.633125	0.506	0.613051
## fCollegeWashington	0.116028	0.571790	0.203	0.839341
## fCollegeWashington State	0.675958	0.842035	0.803	0.422776
## fCollegeWeber State	1.868116	1.105667	1.690	0.092197


```

## fCollegeWest Virginia          -0.876868    0.829673   -1.057  0.291457
## fCollegeWestern Texas Coll. (J.C.) -1.266890    1.081735   -1.171  0.242507
## fCollegeWichita State           0.449096    0.846889    0.530  0.596323
## fCollegeWisconsin              -1.327434    0.865514   -1.534  0.126210
## fCollegeWyoming                -0.006288    0.843848   -0.007  0.994060
## fCollegeXavier                 -1.138664    0.814496   -1.398  0.163197
## fCollegeYale                   -1.059210    1.094291   -0.968  0.333891
## poly(Age, 3)1                   6.632580    1.200878    5.523  7.49e-08 ***
## poly(Age, 3)2                  -4.034700    1.223344   -3.298  0.001097 **
## poly(Age, 3)3                  -2.816061    1.135647   -2.480  0.013725 *
## Height_i                        0.067048    0.191933    0.349  0.727098
## Weight                          0.011685    0.003831    3.050  0.002500 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9368 on 286 degrees of freedom
## Multiple R-squared:  0.4646, Adjusted R-squared:  0.1688
## F-statistic: 1.571 on 158 and 286 DF,  p-value: 0.0005046
# Removal of `fTeam` due to no significance
summary(lm_log2 <- lm(log(Salary) ~ fPosition+fCollege+poly(Age,3)+Height_i+Weight,data=ap_tibble))

##
## Call:
## lm(formula = log(Salary) ~ fPosition + fCollege + poly(Age, 3) +
##     Height_i + Weight, data = ap_tibble)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.9859 -0.4699  0.0000  0.4992  1.8599
##
## Coefficients:
##
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   12.117721   1.477341   8.202 6.06e-15 ***
## fPositionF     -0.086967   0.403461  -0.216  0.82948
## fPositionG      1.235310   0.483952   2.553  0.01117 *
## fPositionPF     0.279807   0.185492   1.508  0.13244
## fPositionPG     1.057613   0.275625   3.837  0.00015 ***
## fPositionSF     0.635628   0.204997   3.101  0.00211 **
## fPositionSG     0.688469   0.237414   2.900  0.00400 **
## fCollegeArizona  0.055245   0.532422   0.104  0.91742
## fCollegeArizona State  0.025576   0.680079   0.038  0.97003
## fCollegeArkansas -0.122212   0.621649  -0.197  0.84427
## fCollegeAuburn   -0.046540   0.678701  -0.069  0.94537
## fCollegeBaylor   -0.454477   0.589873  -0.770  0.44160
## fCollegeBelmont  -0.768565   1.018843  -0.754  0.45120
## fCollegeBoise State -0.415831   1.018326  -0.408  0.68330
## fCollegeBoston College -0.311669   1.018865  -0.306  0.75988
## fCollegeBowling Green  0.691339   1.024226   0.675  0.50018
## fCollegeBucknell  -0.712422   1.024108  -0.696  0.48716
## fCollegeButler    -0.362499   0.782809  -0.463  0.64363
## fCollegeBYU       -1.558654   1.020159  -1.528  0.12755
## fCollegeCal Poly   -0.696183   1.018534  -0.684  0.49478
## fCollegeCalifornia  1.411555   1.023466   1.379  0.16881
## fCollegeCharleston -1.376754   1.024445  -1.344  0.17995

```

## fCollegeCleveland State	-0.603581	1.019888	-0.592	0.55440
## fCollegeColorado	0.205323	0.684289	0.300	0.76433
## fCollegeConnecticut	-0.061817	0.589238	-0.105	0.91651
## fCollegeCreighton	-0.519901	0.780406	-0.666	0.50578
## fCollegeDavidson	1.502171	1.018014	1.476	0.14105
## fCollegeDayton	0.304262	1.020250	0.298	0.76573
## fCollegeDePaul	-1.212032	0.778966	-1.556	0.12072
## fCollegeDrexel	-1.538127	1.019568	-1.509	0.13240
## fCollegeDuke	0.053454	0.461872	0.116	0.90794
## fCollegeFlorida	0.667880	0.611133	1.093	0.27529
## fCollegeFlorida State	0.107562	0.532929	0.202	0.84018
## fCollegeFresno State	1.211215	1.023660	1.183	0.23761
## fCollegeGeorge Washington	-1.441765	1.019703	-1.414	0.15838
## fCollegeGeorgetown	-1.046503	0.682489	-1.533	0.12619
## fCollegeGeorgia	0.301886	0.677633	0.446	0.65626
## fCollegeGeorgia Tech	0.122146	0.680779	0.179	0.85772
## fCollegeGonzaga	0.288661	0.551769	0.523	0.60123
## fCollegeHouston	-0.960029	0.780881	-1.229	0.21983
## fCollegeIllinois	-0.994444	0.803835	-1.237	0.21696
## fCollegeIndiana	-0.370406	0.549223	-0.674	0.50054
## fCollegeIowa State	-0.233615	0.591569	-0.395	0.69318
## fCollegeIUPUI	-0.882552	1.107211	-0.797	0.42600
## fCollegeKansas	-0.004379	0.526047	-0.008	0.99336
## fCollegeKansas State	-1.287976	0.680876	-1.892	0.05946
## fCollegeKentucky	0.158730	0.455085	0.349	0.72748
## fCollegeLehigh	1.405990	1.019040	1.380	0.16865
## fCollegeLiberty	-1.257512	1.019405	-1.234	0.21828
## fCollegeLouisiana-Lafayette	-1.763779	1.017260	-1.734	0.08392
## fCollegeLouisville	0.230565	0.593388	0.389	0.69787
## fCollegeLoyola (MD)	-0.182419	1.019218	-0.179	0.85807
## fCollegeLSU	-0.121002	0.623830	-0.194	0.84633
## fCollegeMarquette	-0.152052	0.683998	-0.222	0.82423
## fCollegeMarshall	-1.756584	1.026894	-1.711	0.08814
## fCollegeMaryland	-0.271483	0.593567	-0.457	0.64772
## fCollegeMemphis	0.592409	0.627057	0.945	0.34551
## fCollegeMiami (FL)	-0.024938	0.778373	-0.032	0.97446
## fCollegeMichigan	-0.160240	0.531642	-0.301	0.76330
## fCollegeMichigan State	0.445161	0.589990	0.755	0.45110
## fCollegeMinnesota	-0.604685	1.017826	-0.594	0.55288
## fCollegeMississippi State	-1.169741	1.019252	-1.148	0.25199
## fCollegeMissouri	-0.149374	0.679018	-0.220	0.82602
## fCollegeMissouri State	-0.913975	1.021617	-0.895	0.37167
## fCollegeMurray State	0.292069	0.778957	0.375	0.70795
## fCollegenan	0.008729	0.433229	0.020	0.98394
## fCollegeNebraska	-1.167982	0.779184	-1.499	0.13488
## fCollegeNevada	-0.909498	0.779824	-1.166	0.24438
## fCollegeNew Mexico	-1.736878	1.018038	-1.706	0.08897
## fCollegeNew Mexico JC	0.253290	1.026353	0.247	0.80523
## fCollegeNew Mexico State	0.786111	1.034831	0.760	0.44803
## fCollegeNorth Carolina	-0.291903	0.509312	-0.573	0.56696
## fCollegeNorth Carolina State	0.293789	1.019026	0.288	0.77330
## fCollegeNotre Dame	-0.500569	1.019419	-0.491	0.62374
## fCollegeOhio	-1.513938	1.014534	-1.492	0.13663
## fCollegeOhio State	0.209518	0.679142	0.309	0.75790

## fCollegeOklahoma	-0.126917	0.678691	-0.187	0.85178
## fCollegeOklahoma State	0.372287	0.785870	0.474	0.63602
## fCollegeOld Dominion	-1.568101	1.021626	-1.535	0.12581
## fCollegeOle Miss	-0.229161	1.018945	-0.225	0.82220
## fCollegeOregon	-0.113425	0.589202	-0.193	0.84747
## fCollegeOregon State	-1.167058	1.023934	-1.140	0.25524
## fCollegePenn State	-0.760438	1.079070	-0.705	0.48151
## fCollegePittsburgh	0.756957	1.025777	0.738	0.46110
## fCollegeProvidence	-0.776948	1.018884	-0.763	0.44630
## fCollegePurdue	-1.169669	1.037993	-1.127	0.26066
## fCollegeRadford	-1.979371	1.018938	-1.943	0.05296
## fCollegeSaint Joseph's	-0.938819	0.799722	-1.174	0.24131
## fCollegeSaint Mary's	-1.095724	0.778699	-1.407	0.16038
## fCollegeSalt Lake CC UT	-1.691322	1.016909	-1.663	0.09727
## fCollegeSan Diego State	-0.087486	0.677631	-0.129	0.89736
## fCollegeSMU	-1.125113	0.683484	-1.646	0.10073
## fCollegeSouth Carolina	-1.027340	1.019405	-1.008	0.31433
## fCollegeSt. John's	-0.789460	1.018580	-0.775	0.43889
## fCollegeStanford	-0.182160	0.563671	-0.323	0.74678
## fCollegeSyracuse	-0.671259	0.591894	-1.134	0.25762
## fCollegeTCU	-1.088543	0.779655	-1.396	0.16364
## fCollegeTennessee	0.185135	0.584538	0.317	0.75167
## fCollegeTennessee State	0.657758	1.022068	0.644	0.52033
## fCollegeTexas	0.513432	0.505430	1.016	0.31049
## fCollegeTexas A&M	0.171219	0.627040	0.273	0.78499
## fCollegeTexas Tech	-0.300202	0.802715	-0.374	0.70867
## fCollegeUC Santa Barbara	-1.582938	1.018485	-1.554	0.12114
## fCollegeUCLA	0.377604	0.504005	0.749	0.45429
## fCollegeUNLV	0.701892	0.686767	1.022	0.30755
## fCollegeUSC	0.200199	0.520737	0.384	0.70090
## fCollegeUSC Upstate	-0.809992	1.018855	-0.795	0.42721
## fCollegeUtah	0.426715	0.681985	0.626	0.53197
## fCollegeUtah State	-1.371865	1.019650	-1.345	0.17946
## fCollegeVanderbilt	-0.423046	0.623086	-0.679	0.49767
## fCollegeVillanova	-0.332992	0.522212	-0.638	0.52416
## fCollegeVirginia	-0.359020	0.548623	-0.654	0.51333
## fCollegeVirginia Commonwealth	-0.367610	1.013399	-0.363	0.71704
## fCollegeVirginia Tech	-0.363104	1.018403	-0.357	0.72167
## fCollegeWake Forest	0.276855	0.593225	0.467	0.64104
## fCollegeWashington	0.110843	0.528198	0.210	0.83392
## fCollegeWashington State	0.206812	0.779871	0.265	0.79104
## fCollegeWeber State	1.165131	1.016695	1.146	0.25267
## fCollegeWest Virginia	-1.176820	0.778427	-1.512	0.13159
## fCollegeWestern Texas Coll. (J.C.)	-1.358568	1.024063	-1.327	0.18559
## fCollegeWichita State	0.449360	0.784443	0.573	0.56716
## fCollegeWisconsin	-1.283548	0.804188	-1.596	0.11147
## fCollegeWyoming	-0.374736	0.780720	-0.480	0.63157
## fCollegeXavier	-1.233072	0.778434	-1.584	0.11419
## fCollegeYale	-1.100493	1.019347	-1.080	0.28114
## poly(Age, 3)1	6.266113	1.072683	5.842	1.29e-08 ***
## poly(Age, 3)2	-4.591228	1.081594	-4.245	2.88e-05 ***
## poly(Age, 3)3	-2.517846	1.054401	-2.388	0.01753 *
## Height_i	0.074499	0.179522	0.415	0.67843
## Weight	0.011134	0.003517	3.166	0.00170 **

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9199 on 315 degrees of freedom
## Multiple R-squared:  0.4313, Adjusted R-squared:  0.1985
## F-statistic: 1.852 on 129 and 315 DF,  p-value: 7.096e-06
summary(lm_log3 <- lm(log(Salary) ~ fPosition+poly(Age,3)+Height_i+Weight,data=ap_tibble))

##
## Call:
## lm(formula = log(Salary) ~ fPosition + poly(Age, 3) + Height_i +
##     Weight, data = ap_tibble)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.83140 -0.75071 -0.00053  0.68054  2.13922
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  13.378512   1.245474  10.742 < 2e-16 ***
## fPositionF   -0.487400   0.342620  -1.423 0.155582
## fPositionG    0.737517   0.412604   1.787 0.074561 .
## fPositionPF   0.175011   0.164275   1.065 0.287310
## fPositionPG   0.709369   0.234428   3.026 0.002626 **
## fPositionSF   0.318113   0.181414   1.754 0.080221 .
## fPositionSG   0.403881   0.202681   1.993 0.046923 *
## poly(Age, 3)1  6.765514   0.956954   7.070 6.25e-12 ***
## poly(Age, 3)2 -3.106151   0.953222  -3.259 0.001208 **
## poly(Age, 3)3 -3.153080   0.943404  -3.342 0.000903 ***
## Height_i      -0.007768   0.157832  -0.049 0.960770
## Weight         0.008309   0.003119   2.664 0.008013 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9368 on 433 degrees of freedom
## Multiple R-squared:  0.1893, Adjusted R-squared:  0.1687
## F-statistic: 9.191 on 11 and 433 DF,  p-value: 7.444e-15
summary(lm_log4 <- lm(log(Salary) ~ fPosition+poly(Age,3)+Weight,data=ap_tibble))

##
## Call:
## lm(formula = log(Salary) ~ fPosition + poly(Age, 3) + Weight,
##     data = ap_tibble)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.83384 -0.75300  0.00348  0.68066  2.13764
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  13.330870   0.782775  17.030 < 2e-16 ***
## fPositionF   -0.489098   0.340488  -1.436 0.15159
## fPositionG    0.737585   0.412128   1.790 0.07420 .
```

```
## fPositionPF      0.174562    0.163833    1.065  0.28725
## fPositionPG      0.711135    0.231400    3.073  0.00225 **
## fPositionSF      0.316997    0.179784    1.763  0.07857 .
## fPositionSG      0.403881    0.202448    1.995  0.04667 *
## poly(Age, 3)1    6.769471    0.952473    7.107 4.89e-12 ***
## poly(Age, 3)2   -3.110142    0.948675   -3.278  0.00113 **
## poly(Age, 3)3   -3.153257    0.942313   -3.346  0.00089 ***
## Weight           0.008296    0.003104    2.673  0.00781 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9357 on 434 degrees of freedom
## Multiple R-squared:  0.1893, Adjusted R-squared:  0.1706
## F-statistic: 10.13 on 10 and 434 DF,  p-value: 2.258e-15
anova(lm_log4,lm_log3,lm_log2,lm_log1)
```

```
## Analysis of Variance Table
##
## Model 1: log(Salary) ~ fPosition + poly(Age, 3) + Weight
## Model 2: log(Salary) ~ fPosition + poly(Age, 3) + Height_i + Weight
## Model 3: log(Salary) ~ fPosition + fCollege + poly(Age, 3) + Height_i +
##          Weight
## Model 4: log(Salary) ~ fTeam + fPosition + fCollege + poly(Age, 3) + Height_i +
##          Weight
##   Res.Df    RSS  Df Sum of Sq    F Pr(>F)
## 1     434 380.00
## 2     433 380.00   1     0.002 0.0024 0.9608
## 3     315 266.54 118    113.459 1.0957 0.2692
## 4     286 250.97  29     15.575 0.6120 0.9438
```

Stepwise Model Selection

```
summary(lm_step <- step(lm_logsm <- lm(log(Salary) ~ fTeam+fPosition+fCollege+poly(Age,3)+Height_i+Weight))

## Start:  AIC=63.13
## log(Salary) ~ fTeam + fPosition + fCollege + poly(Age, 3) + Height_i +
##          Weight
##
##           Df Sum of Sq  RSS    AIC
## - fCollege   118   112.484 363.45 -8.079
## - fTeam       29    15.575 266.54 31.921
## - Height_i     1     0.107 251.08 61.317
## <none>                250.97 63.127
## - Weight       1     8.165 259.13 75.375
## - fPosition     6    14.621 265.59 76.325
## - poly(Age, 3)  3    45.448 296.42 131.192
##
## Step:  AIC=-8.08
## log(Salary) ~ fTeam + fPosition + poly(Age, 3) + Height_i + Weight
##
##           Df Sum of Sq  RSS    AIC
## - fTeam       29    16.550 380.00 -46.264
## - Height_i     1     0.007 363.46 -10.070
## <none>                363.45 -8.079
```

```

## - fPosition      6      15.007 378.46 -2.075
## - Weight         1       8.063 371.52 -0.316
## - poly(Age, 3)   3      65.521 428.97 59.678
##
## Step: AIC=-46.26
## log(Salary) ~ fPosition + poly(Age, 3) + Height_i + Weight
##
##           Df Sum of Sq    RSS    AIC
## - Height_i  1      0.002 380.00 -48.261
## <none>                        380.00 -46.264
## - fPosition  6     13.866 393.87 -42.315
## - Weight     1      6.228 386.23 -41.030
## - poly(Age, 3) 3     62.593 442.60 15.589
##
## Step: AIC=-48.26
## log(Salary) ~ fPosition + poly(Age, 3) + Weight
##
##           Df Sum of Sq    RSS    AIC
## <none>                        380.00 -48.261
## - fPosition  6     14.709 394.71 -43.361
## - Weight     1      6.254 386.26 -42.997
## - poly(Age, 3) 3     63.348 443.35 14.350
##
## Call:
## lm(formula = log(Salary) ~ fPosition + poly(Age, 3) + Weight,
##     data = ap_tibble)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.83384 -0.75300  0.00348  0.68066  2.13764
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 13.330870   0.782775  17.030 < 2e-16 ***
## fPositionF   -0.489098   0.340488  -1.436  0.15159
## fPositionG    0.737585   0.412128   1.790  0.07420 .
## fPositionPF   0.174562   0.163833   1.065  0.28725
## fPositionPG   0.711135   0.231400   3.073  0.00225 **
## fPositionSF   0.316997   0.179784   1.763  0.07857 .
## fPositionSG   0.403881   0.202448   1.995  0.04667 *
## poly(Age, 3)1  6.769471   0.952473   7.107 4.89e-12 ***
## poly(Age, 3)2 -3.110142   0.948675  -3.278  0.00113 **
## poly(Age, 3)3 -3.153257   0.942313  -3.346  0.00089 ***
## Weight        0.008296   0.003104   2.673  0.00781 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9357 on 434 degrees of freedom
## Multiple R-squared:  0.1893, Adjusted R-squared:  0.1706
## F-statistic: 10.13 on 10 and 434 DF, p-value: 2.258e-15
shapiro.test(resid(lm_log2))
##

```

```
## Shapiro-Wilk normality test
##
## data: resid(lm_log2)
## W = 0.9903, p-value = 0.004962
bptest(lm_log2)

##
## studentized Breusch-Pagan test
##
## data: lm_log2
## BP = 147.16, df = 129, p-value = 0.1308
shapiro.test(resid(lm_step))

##
## Shapiro-Wilk normality test
##
## data: resid(lm_step)
## W = 0.9816, p-value = 1.996e-05
bptest(lm_step)

##
## studentized Breusch-Pagan test
##
## data: lm_step
## BP = 47.163, df = 10, p-value = 8.819e-07
```

Logistic Regression

```
# Transforming Team, Position, College into factors
ap_tibble <- transform (
  ap_tibble,
  nTeam = as.numeric(fTeam),
  nPosition = as.numeric(fPosition),
  nCollege = as.numeric(fCollege),
  fSalary.Dummy = as.factor(Salary.Dummy)
)

#cross validation
set.seed(999)
n <- nrow(ap_tibble)
n

## [1] 445
floor(0.7*n)

## [1] 311
#randomly sample 70% of the rows

train <- sample(1:n, 311)

tn <- ap_tibble[train,]
test <- ap_tibble[-train,]
```

```
summary(glmFit <- train(fSalary.Dummy ~ nTeam+nPosition+nCollege+Age+Height_i+Weight, data=ap_tibble, m
```

```
##
## Call:
## NULL
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.8917  -0.8587  -0.6293   1.1236   2.1465
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -3.488752   2.432577  -1.434  0.15152
## nPosition    0.140870   0.069198   2.036  0.04178 *
## Age          0.154183   0.025267   6.102 1.05e-09 ***
## Height_i     -0.809923   0.355835  -2.276  0.02284 *
## Weight       0.015820   0.006056   2.612  0.00899 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 576.54  on 444  degrees of freedom
## Residual deviance: 521.62  on 440  degrees of freedom
## AIC: 531.62
##
## Number of Fisher Scoring iterations: 4
```

```
confusionMatrix(glmFit)
```

```
## Bootstrapped (25 reps) Confusion Matrix
##
## (entries are percentual average cell counts across resamples)
##
##              Reference
## Prediction    0      1
##              0 55.5 23.9
##              1  9.6 11.1
##
## Accuracy (average) : 0.6657
```

```
summary(glmFit2 <- train(fSalary.Dummy ~ nTeam+nPosition+nCollege+poly(Age,3)+Height_i+Weight, data=ap_
```

```
##
## Call:
## NULL
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.7211  -0.8556  -0.5179   0.9954   2.3404
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)    0.11247   2.39580   0.047  0.9626
## nPosition      0.11246   0.07163   1.570  0.1164
```



```

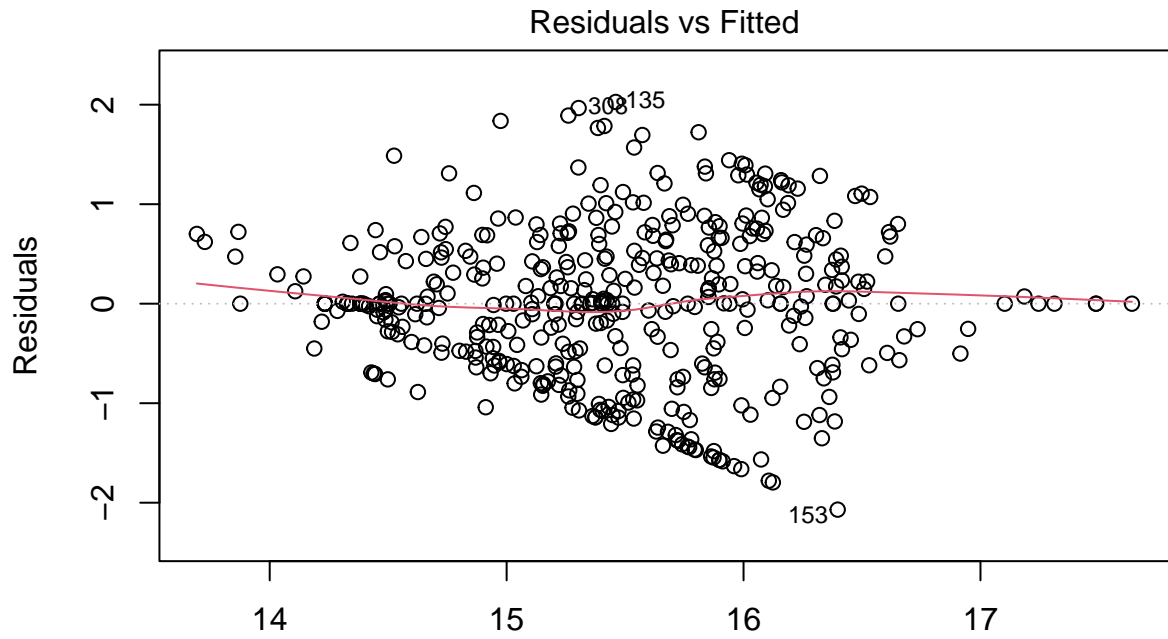
## `poly(Age, 3)1` 14.48770 2.78133 5.209 1.90e-07 ***
## `poly(Age, 3)2` -12.71575 2.84126 -4.475 7.63e-06 ***
## `poly(Age, 3)3` -8.55996 3.49842 -2.447 0.0144 *
## Height_i -0.69734 0.36772 -1.896 0.0579 .
## Weight 0.01433 0.00631 2.271 0.0232 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 576.54 on 444 degrees of freedom
## Residual deviance: 491.18 on 438 degrees of freedom
## AIC: 505.18
##
## Number of Fisher Scoring iterations: 4
confusionMatrix(glmFit2)

## Bootstrapped (25 reps) Confusion Matrix
##
## (entries are percentual average cell counts across resamples)
##
## Reference
## Prediction 0 1
## 0 52.7 17.7
## 1 12.3 17.3
##
## Accuracy (average) : 0.6999
#comparing the plots
# Rename variables

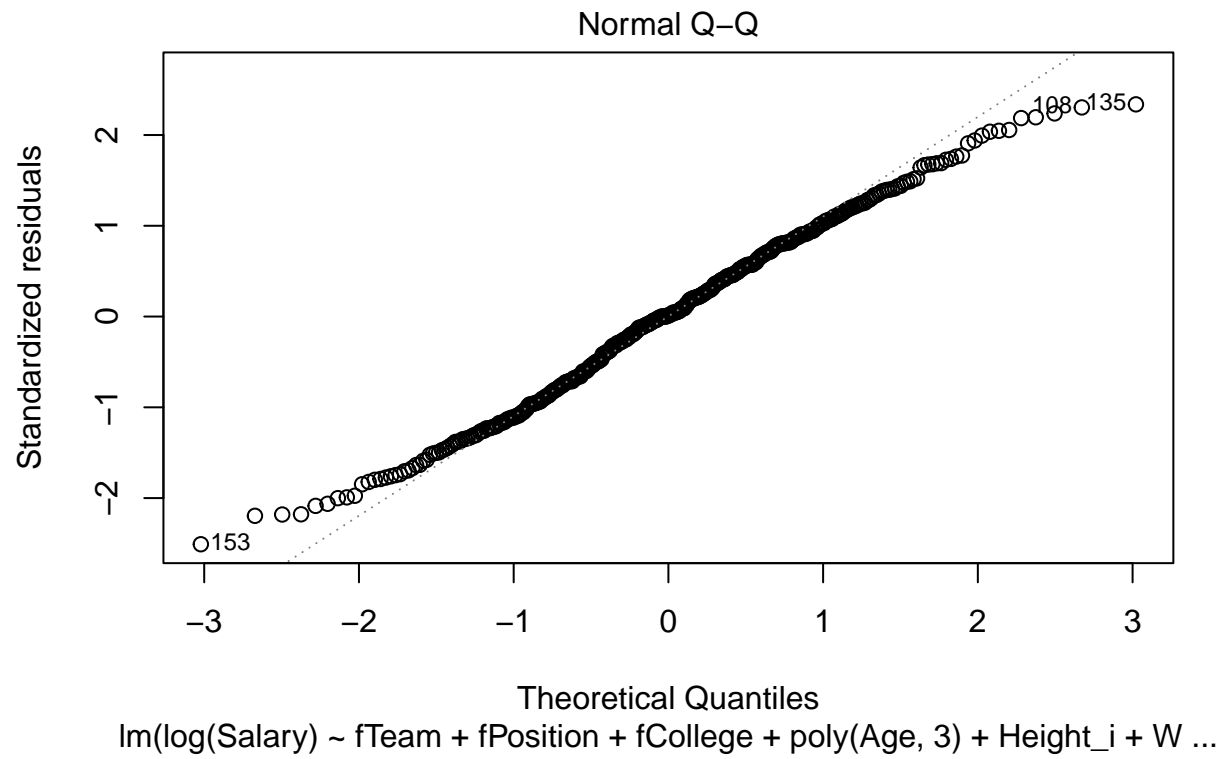
plot(lm_log1, 1:2)

## Warning: not plotting observations with leverage one:
## 1, 27, 46, 69, 74, 77, 85, 102, 104, 122, 133, 137, 138, 141, 190, 217, 223, 227, 231, 241, 249, 2

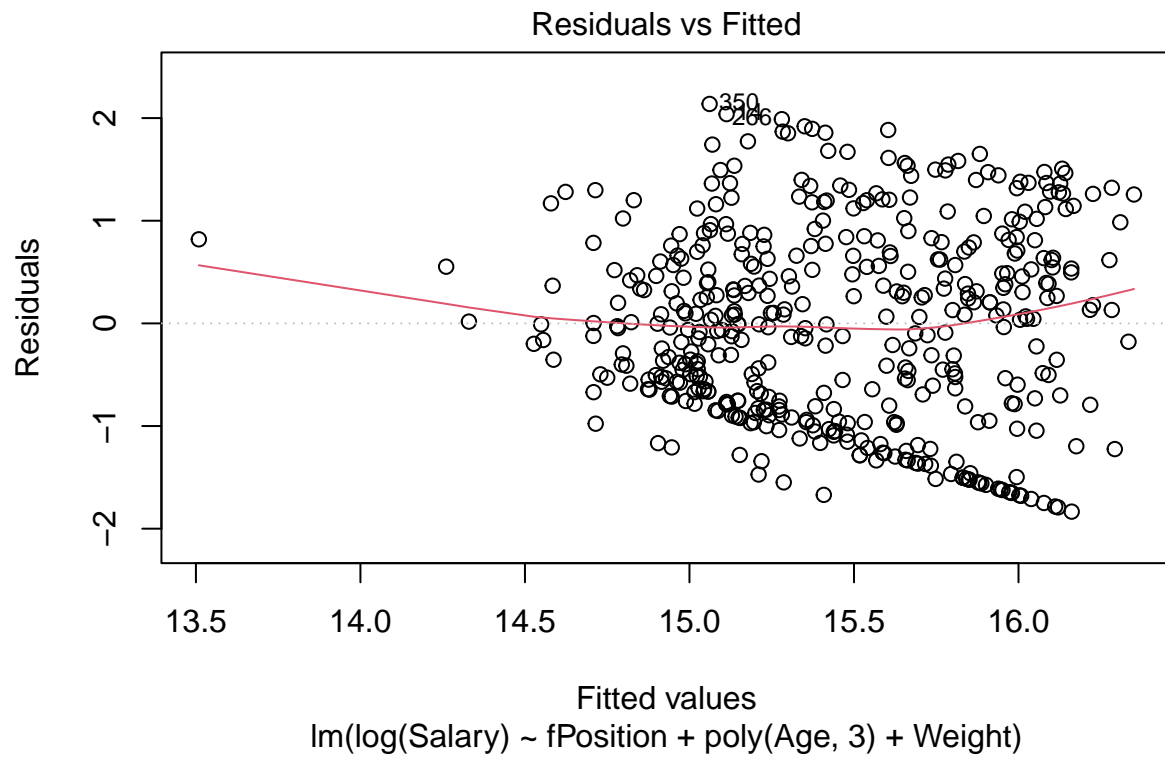
```

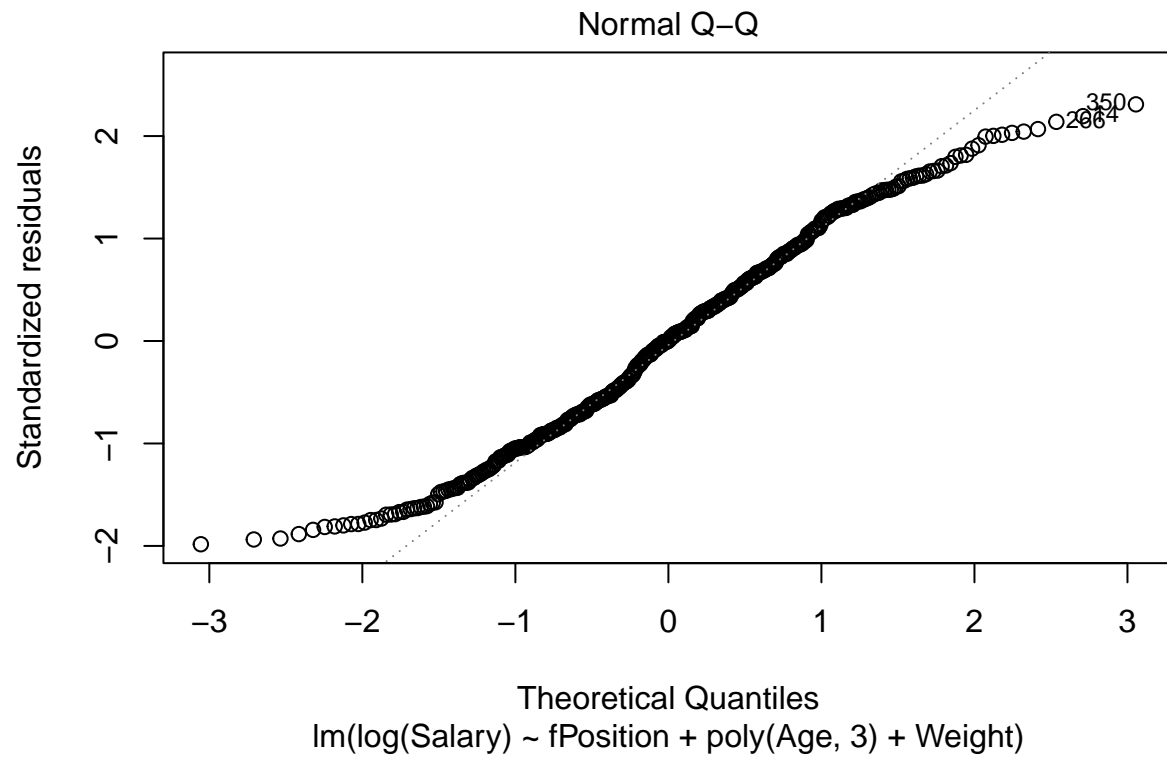


$\text{lm}(\log(\text{Salary}) \sim \text{fTeam} + \text{fPosition} + \text{fCollege} + \text{poly}(\text{Age}, 3) + \text{Height}_i + \text{W} \dots$



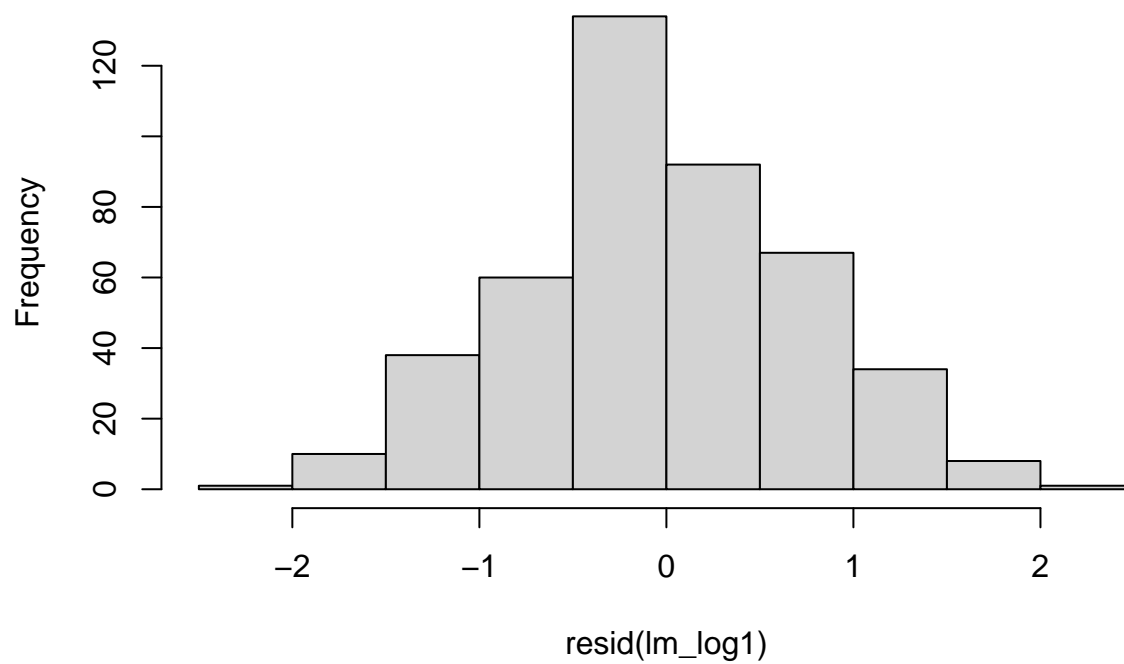
```
plot(lm_log4, 1:2)
```





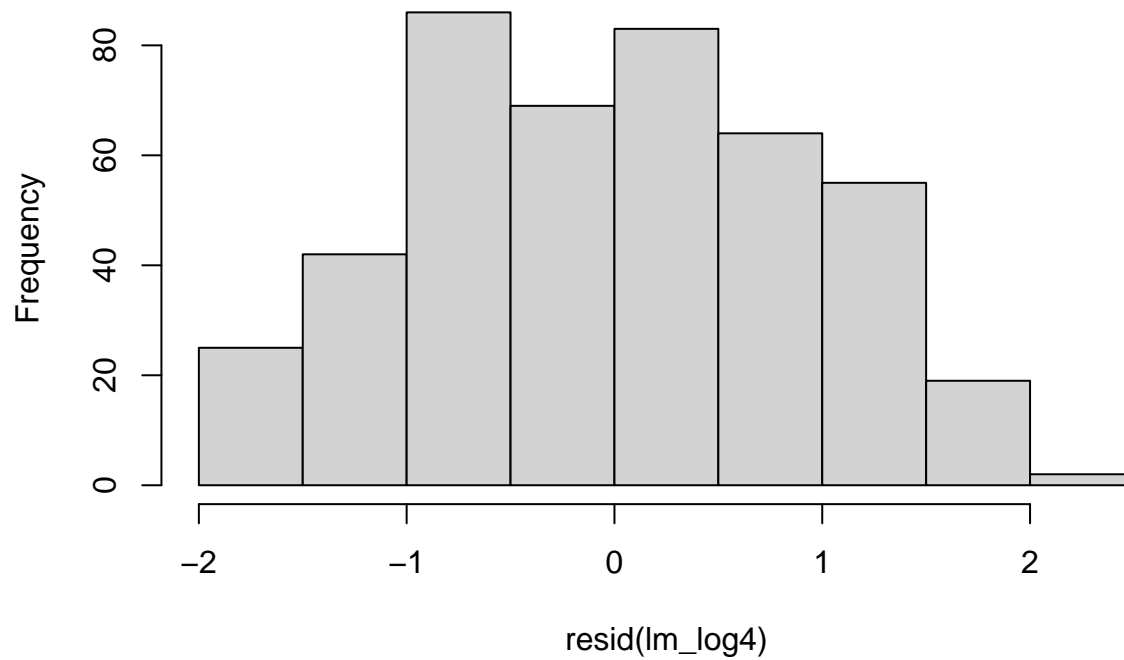
```
hist(resid(lm_log1))
```

Histogram of resid(lm_log1)



```
hist(resid(lm_log4))
```

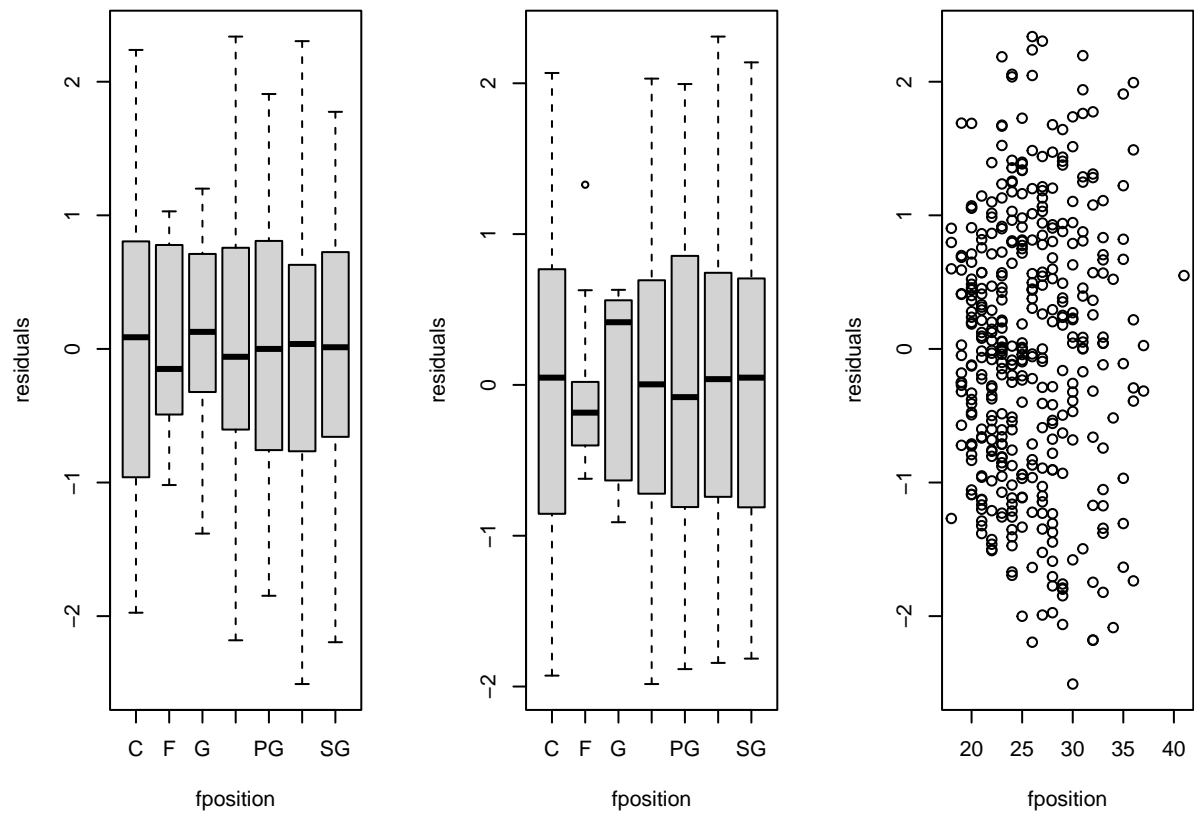
Histogram of resid(lm_log4)



```
par(mfrow=c(1,3), mar=c(4.5, 4.5, 2, 2))

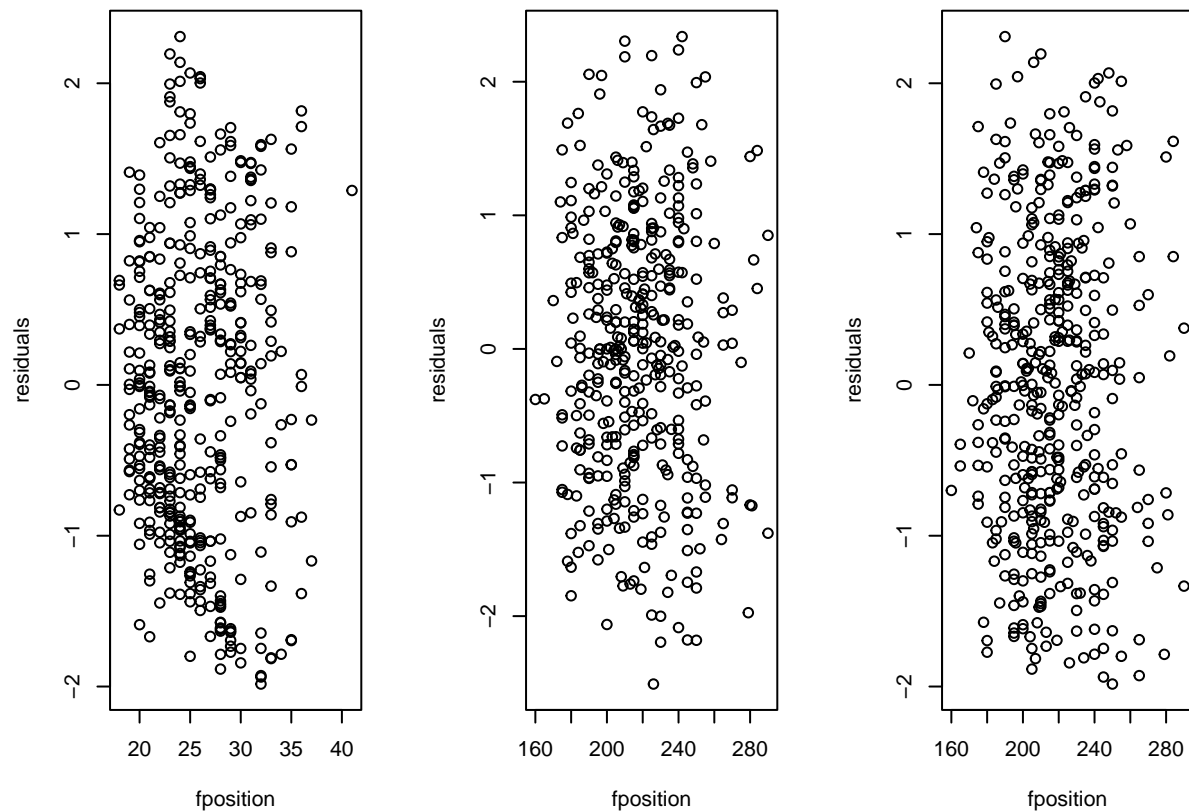
plot(ap_tibble$fPosition, rstandard(lm_log1), xlab="fposition", ylab="residuals")
plot(ap_tibble$fPosition, rstandard(lm_log4), xlab="fposition", ylab="residuals")

plot(ap_tibble$Age, rstandard(lm_log1), xlab="fposition", ylab="residuals")
```



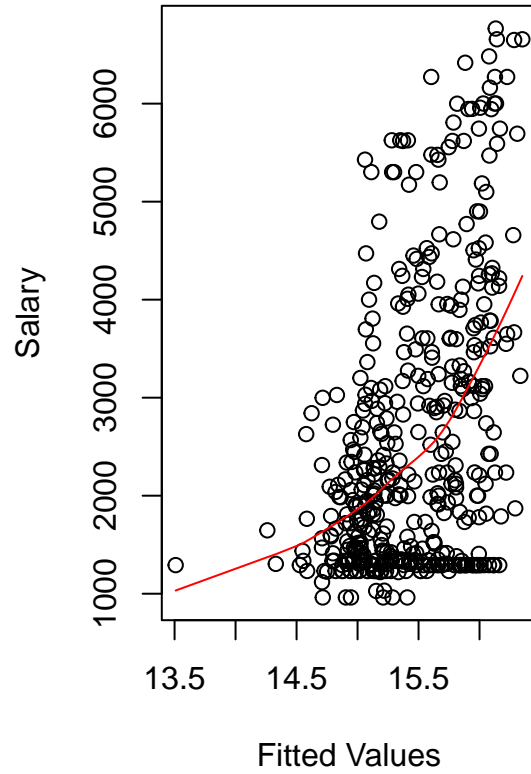
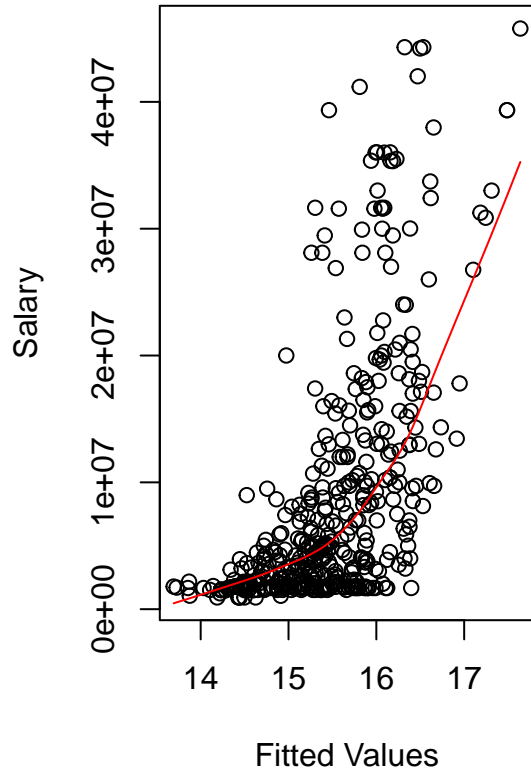
```
plot(ap_tibble$Age, rstandard(lm_log4), xlab="fposition", ylab="residuals")

plot(ap_tibble$Weight, rstandard(lm_log1), xlab="fposition", ylab="residuals")
plot(ap_tibble$Weight, rstandard(lm_log4), xlab="fposition", ylab="residuals")
```

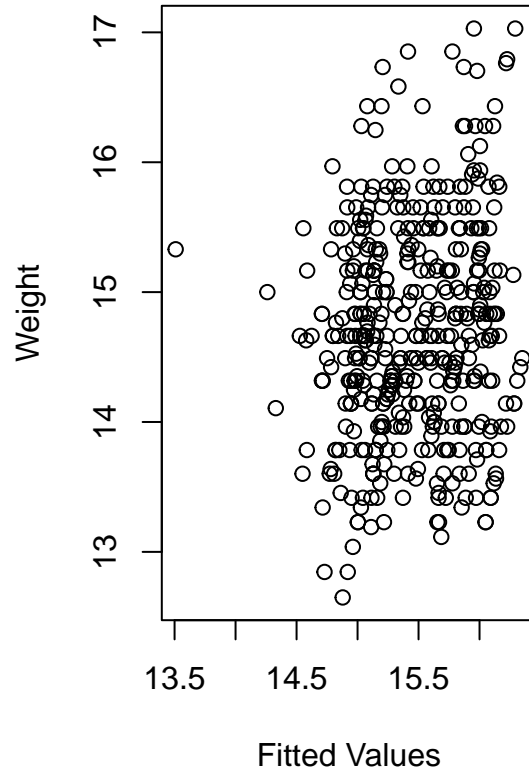
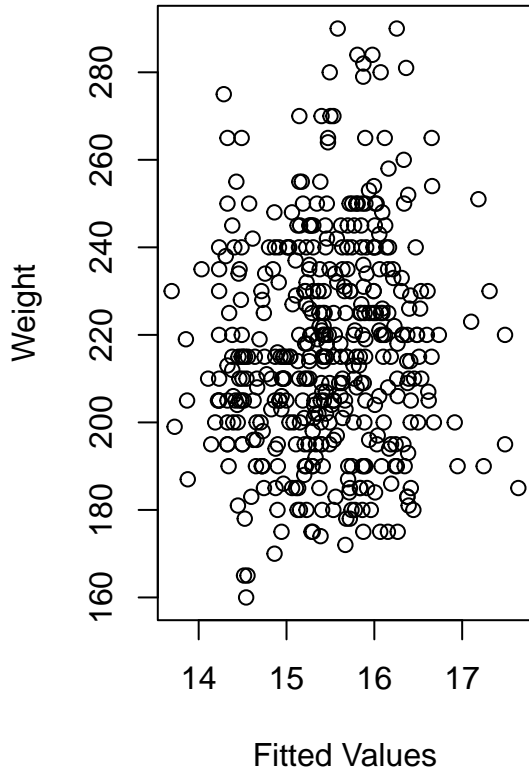
```
#normality check
par(mfrow=c(1,2), mar=c(4.5, 4.5, 2, 2))
plot(predict(lm_log1), ap_tibble$Salary,
      xlab = "Fitted Values", ylab = "Salary")
abline()
lines(lowess(predict(lm_log1), ap_tibble$Salary), col='red')

plot(predict(lm_log4), sqrt(ap_tibble$Salary),
      xlab = "Fitted Values", ylab = "Salary")
lines(lowess(predict(lm_log4), sqrt(ap_tibble$Salary)), col='red')
```



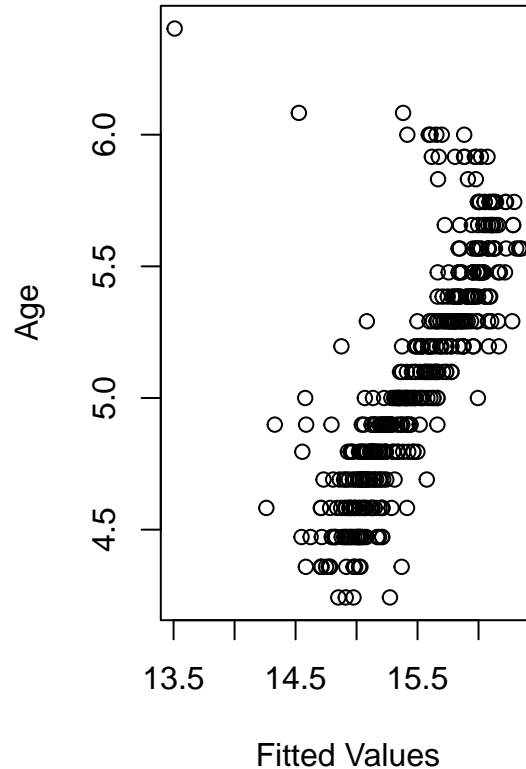
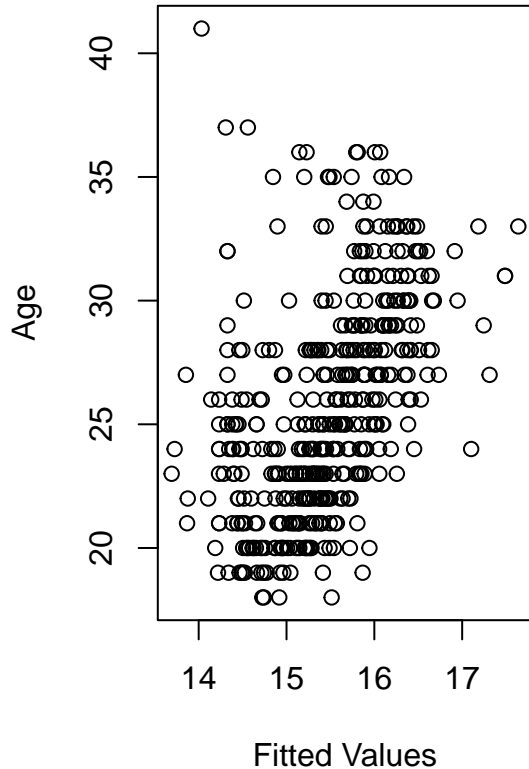
```
plot(predict(lm_log1), ap_tibble$Weight,
      xlab = "Fitted Values", ylab = "Weight")

plot(predict(lm_log4), sqrt(ap_tibble$Weight),
      xlab = "Fitted Values", ylab = "Weight")
```



```
plot(predict(lm_log1), ap_tibble$Age,
      xlab = "Fitted Values", ylab = "Age")

plot(predict(lm_log4), sqrt(ap_tibble$Age),
      xlab = "Fitted Values", ylab = "Age")
```



Model Checking

Outliers

Remove outliers & high leverage from data

```
ap_cl_f_wo <- ap_tibble[-which(abs(rstandard(lm_step)) > 2
                                | hatvalues(lm_step) > .1),]
```

```
summary(lm1_wo <- lm(log(Salary) ~ fTeam+fPosition+fCollege+poly(Age,3)+Height_i+Weight,
                      data=ap_cl_f_wo))
```

```
##
## Call:
## lm(formula = log(Salary) ~ fTeam + fPosition + fCollege + poly(Age,
##      3) + Height_i + Weight, data = ap_cl_f_wo)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.1397 -0.4790  0.0000  0.4899  1.8739
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    11.7791977    1.5959108     7.381 2.03e-12 ***
## fTeamBoston Celtics    -0.5393965    0.4118931    -1.310 0.191481
## fTeamBrooklyn Nets    -0.3305199    0.3713975    -0.890 0.374308
## fTeamCharlotte Hornets -0.1739976    0.3602481    -0.483 0.629499
```

## fTeamChicago Bulls	0.0635036	0.4042121	0.157	0.875282	
## fTeamCleveland Cavaliers	0.3361198	0.4050216	0.830	0.407353	
## fTeamDallas Mavericks	-0.6163239	0.3751462	-1.643	0.101592	
## fTeamDenver Nuggets	-0.2030649	0.3782618	-0.537	0.591831	
## fTeamDetroit Pistons	-0.4397854	0.3773732	-1.165	0.244911	
## fTeamGolden State Warriors	-0.5778167	0.4059471	-1.423	0.155802	
## fTeamHouston Rockets	-0.4902463	0.3719001	-1.318	0.188568	
## fTeamIndiana Pacers	-0.1031768	0.3817314	-0.270	0.787150	
## fTeamLos Angeles Clippers	-0.2210872	0.3890599	-0.568	0.570340	
## fTeamLos Angeles Lakers	-0.6982741	0.4349105	-1.606	0.109562	
## fTeamMemphis Grizzlies	-0.3109094	0.3994209	-0.778	0.437027	
## fTeamMiami Heat	-0.7020907	0.4114268	-1.706	0.089091	.
## fTeamMilwaukee Bucks	-0.7726938	0.4003687	-1.930	0.054680	.
## fTeamMinnesota Timberwolves	0.1953093	0.4216583	0.463	0.643606	
## fTeamNew Orleans Pelicans	-0.2379120	0.3748767	-0.635	0.526210	
## fTeamNew York Knicks	-0.2534616	0.3763232	-0.674	0.501203	
## fTeamOklahoma City Thunder	-0.4049589	0.3824510	-1.059	0.290632	
## fTeamOrlando Magic	-0.0683007	0.3815633	-0.179	0.858073	
## fTeamPhiladelphia Sixers	-0.2655867	0.3895609	-0.682	0.495987	
## fTeamPhoenix Suns	-0.0011708	0.4047239	-0.003	0.997694	
## fTeamPortland Trail Blazers	-0.7465743	0.4245698	-1.758	0.079829	.
## fTeamSacramento Kings	0.0318074	0.3945302	0.081	0.935804	
## fTeamSan Antonio Spurs	-0.1293054	0.3745541	-0.345	0.730199	
## fTeamToronto Raptors	-0.0124533	0.4406227	-0.028	0.977474	
## fTeamUtah Jazz	-0.0003289	0.4024707	-0.001	0.999349	
## fTeamWashington Wizards	-0.3672619	0.3591758	-1.023	0.307471	
## fPositionPF	0.4247647	0.1914246	2.219	0.027336	*
## fPositionPG	1.2774752	0.2955907	4.322	2.19e-05	***
## fPositionSF	0.7334905	0.2106636	3.482	0.000582	***
## fPositionSG	0.9755366	0.2543788	3.835	0.000157	***
## fCollegeArizona	0.1523401	0.5555321	0.274	0.784126	
## fCollegeArizona State	0.2338294	0.7042212	0.332	0.740122	
## fCollegeArkansas	0.0378729	0.6476039	0.058	0.953409	
## fCollegeAuburn	-0.1784902	0.6957118	-0.257	0.797719	
## fCollegeBaylor	-0.5222221	0.6278505	-0.832	0.406292	
## fCollegeBelmont	-1.1098313	1.0368488	-1.070	0.285418	
## fCollegeBoise State	-0.2810676	1.0578421	-0.266	0.790678	
## fCollegeBoston College	-0.2711400	1.0499872	-0.258	0.796429	
## fCollegeBowling Green	0.7262524	1.0606648	0.685	0.494123	
## fCollegeBucknell	-0.3558443	1.0612991	-0.335	0.737671	
## fCollegeButler	-0.3365202	0.8092456	-0.416	0.677860	
## fCollegeBYU	-0.8632846	1.0563565	-0.817	0.414532	
## fCollegeCal Poly	-0.1783480	1.0500395	-0.170	0.865259	
## fCollegeCalifornia	1.8511441	1.0598734	1.747	0.081870	.
## fCollegeCharleston	-1.4382428	1.0684892	-1.346	0.179436	
## fCollegeCleveland State	-0.6110414	1.0374950	-0.589	0.556391	
## fCollegeColorado	0.3701865	0.7000433	0.529	0.597383	
## fCollegeConnecticut	-0.0357990	0.6106987	-0.059	0.953299	
## fCollegeCreighton	-0.2554259	0.8003035	-0.319	0.749856	
## fCollegeDavidson	1.9398140	1.0585913	1.832	0.068007	.
## fCollegeDayton	0.6210884	1.0486310	0.592	0.554165	
## fCollegeDePaul	-0.7118328	0.8096993	-0.879	0.380126	
## fCollegeDrexel	-1.0903740	1.0578095	-1.031	0.303582	
## fCollegeDuke	0.0651937	0.4844321	0.135	0.893048	

## fCollegeFlorida	0.9908595	0.6469161	1.532	0.126798
## fCollegeFlorida State	0.0700704	0.5512542	0.127	0.898949
## fCollegeFresno State	1.1909302	1.0528841	1.131	0.259030
## fCollegeGeorge Washington	-1.3026513	1.0723350	-1.215	0.225531
## fCollegeGeorgetown	-0.5715929	0.7048359	-0.811	0.418117
## fCollegeGeorgia	0.3924855	0.7041831	0.557	0.577750
## fCollegeGeorgia Tech	0.1761395	0.7065353	0.249	0.803322
## fCollegeGonzaga	0.4847763	0.5751350	0.843	0.400049
## fCollegeHouston	-1.1227212	0.7941859	-1.414	0.158631
## fCollegeIllinois	-1.5087994	1.0526543	-1.433	0.152943
## fCollegeIndiana	-0.0032225	0.5744873	-0.006	0.995529
## fCollegeIowa State	-0.0199612	0.6415514	-0.031	0.975202
## fCollegeKansas	0.0265974	0.5752924	0.046	0.963159
## fCollegeKansas State	-1.1844075	0.6977239	-1.698	0.090770
## fCollegeKentucky	0.2844623	0.4780613	0.595	0.552329
## fCollegeLehigh	2.0429998	1.0629476	1.922	0.055676
## fCollegeLiberty	-0.9269506	1.0473142	-0.885	0.376919
## fCollegeLouisiana-Lafayette	-1.7593571	1.0582728	-1.662	0.097599
## fCollegeLouisville	0.4637780	0.6175574	0.751	0.453326
## fCollegeLoyola (MD)	-0.0141200	1.0542243	-0.013	0.989324
## fCollegeLSU	-0.0865207	0.6394517	-0.135	0.892474
## fCollegeMarquette	0.2107798	0.7127502	0.296	0.767670
## fCollegeMarshall	-1.8800821	1.0609209	-1.772	0.077523
## fCollegeMaryland	-0.2157877	0.6506138	-0.332	0.740402
## fCollegeMemphis	1.0272661	0.6925148	1.483	0.139160
## fCollegeMiami (FL)	0.2304093	0.8006953	0.288	0.773754
## fCollegeMichigan	0.2150105	0.5608070	0.383	0.701735
## fCollegeMichigan State	0.6840266	0.6229508	1.098	0.273182
## fCollegeMinnesota	-0.2475194	1.0554207	-0.235	0.814761
## fCollegeMississippi State	-1.2517796	1.0568824	-1.184	0.237313
## fCollegeMissouri	-0.0279019	0.6977023	-0.040	0.968130
## fCollegeMissouri State	-0.4958923	1.0559280	-0.470	0.639008
## fCollegeMurray State	0.4975385	0.8093310	0.615	0.539246
## fCollegenan	0.1798764	0.4506371	0.399	0.690097
## fCollegeNebraska	-0.8963405	0.8151654	-1.100	0.272513
## fCollegeNevada	-0.8312788	0.8089590	-1.028	0.305079
## fCollegeNew Mexico	-0.9670665	1.0633218	-0.909	0.363925
## fCollegeNew Mexico JC	0.3451578	1.0884386	0.317	0.751408
## fCollegeNew Mexico State	0.7275715	1.0816742	0.673	0.501766
## fCollegeNorth Carolina	-0.0877460	0.5332940	-0.165	0.869435
## fCollegeNorth Carolina State	0.4452804	1.0487248	0.425	0.671478
## fCollegeNotre Dame	0.1455667	1.0540693	0.138	0.890266
## fCollegeOhio	-1.2606605	1.0511879	-1.199	0.231493
## fCollegeOhio State	0.3016359	0.7102582	0.425	0.671411
## fCollegeOklahoma	-0.1490039	0.7028404	-0.212	0.832268
## fCollegeOklahoma State	0.6748970	0.8095165	0.834	0.405199
## fCollegeOld Dominion	-0.8945644	1.0657649	-0.839	0.402022
## fCollegeOle Miss	-0.2997999	1.0555320	-0.284	0.776611
## fCollegeOregon	0.1726480	0.6089412	0.284	0.776998
## fCollegeOregon State	-1.0483486	1.0428320	-1.005	0.315674
## fCollegePittsburgh	1.0005420	1.0645945	0.940	0.348159
## fCollegeProvidence	-0.2693593	1.0535391	-0.256	0.798403
## fCollegePurdue	-0.7162766	1.0757346	-0.666	0.506087
## fCollegeRadford	-2.0962804	1.0536562	-1.990	0.047671 *

```

## fCollegeSaint Joseph's      -1.3464206  1.0512933  -1.281  0.201409
## fCollegeSaint Mary's        -0.9181562  0.7981416  -1.150  0.251030
## fCollegeSalt Lake CC UT     -1.1399288  1.0590357  -1.076  0.282735
## fCollegeSan Diego State      0.0991510  0.7086451   0.140  0.888832
## fCollegeSMU                  -0.5725004  0.7111157  -0.805  0.421499
## fCollegeSouth Carolina       -0.8609753  1.0323397  -0.834  0.405030
## fCollegeSt. John's          -0.7810305  1.0538784  -0.741  0.459288
## fCollegeStanford             0.2310066  0.5906767   0.391  0.696046
## fCollegeSyracuse            -0.3807328  0.6205544  -0.614  0.540048
## fCollegeTCU                  -0.7173919  0.8108158  -0.885  0.377078
## fCollegeTennessee           0.3893596  0.6217869   0.626  0.531726
## fCollegeTennessee State      1.3681412  1.0678449   1.281  0.201237
## fCollegeTexas                0.7140150  0.5213325   1.370  0.171972
## fCollegeTexas A&M            0.6343792  0.6545300   0.969  0.333323
## fCollegeTexas Tech          -0.8134292  1.0533638  -0.772  0.440672
## fCollegeUC Santa Barbara     -0.8584267  1.0549003  -0.814  0.416518
## fCollegeUCLA                 0.7497652  0.5273326   1.422  0.156258
## fCollegeUNLV                 0.9858305  0.7265290   1.357  0.175966
## fCollegeUSC                  0.2821557  0.5443195   0.518  0.604637
## fCollegeUSC Upstate          -0.7379822  1.0478384  -0.704  0.481871
## fCollegeUtah                 0.6303246  0.6998579   0.901  0.368594
## fCollegeUtah State           -1.1151941  1.0526581  -1.059  0.290379
## fCollegeVanderbilt           -0.2613473  0.6405825  -0.408  0.683615
## fCollegeVillanova            0.0902803  0.5483647   0.165  0.869356
## fCollegeVirginia             -0.0704476  0.5646633  -0.125  0.900808
## fCollegeVirginia Commonwealth -0.1914164  1.0270818  -0.186  0.852298
## fCollegeVirginia Tech        -0.1755801  1.0158853  -0.173  0.862913
## fCollegeWake Forest          0.2961353  0.6171933   0.480  0.631759
## fCollegeWashington           0.1707733  0.5541155   0.308  0.758179
## fCollegeWashington State      0.6906445  0.8151584   0.847  0.397619
## fCollegeWeber State           1.7767243  1.0646036   1.669  0.096317
## fCollegeWest Virginia        -0.9605252  0.8014206  -1.199  0.231782
## fCollegeWestern Texas Coll. (J.C.) -1.3441585  1.0441243  -1.287  0.199094
## fCollegeWichita State         0.4124782  0.8241941   0.500  0.617165
## fCollegeWisconsin            -1.6875448  1.0653374  -1.584  0.114376
## fCollegeWyoming              -0.0526230  0.8144087  -0.065  0.948529
## fCollegeXavier               -0.9931141  0.7852655  -1.265  0.207095
## fCollegeYale                 -1.1484477  1.0592025  -1.084  0.279236
## poly(Age, 3)1                 7.0833306  1.1536748   6.140  3.01e-09 ***
## poly(Age, 3)2                -1.9400855  1.1821414  -1.641  0.101950
## poly(Age, 3)3                -2.7813226  1.1184886  -2.487  0.013510 *
## Height_i                     -0.0062739  0.1918515  -0.033  0.973937
## Weight                       0.0146404  0.0038146   3.838  0.000155 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9006 on 265 degrees of freedom
## Multiple R-squared:  0.4979, Adjusted R-squared:  0.2061
## F-statistic: 1.706 on 154 and 265 DF, p-value: 7.106e-05
summary(lm1_wo_step <- step(lm1_wo))

## Start:  AIC=28.6
## log(Salary) ~ fTeam + fPosition + fCollege + poly(Age, 3) + Height_i +
##           Weight

```

```

##
##           Df Sum of Sq    RSS      AIC
## - fCollege 116  106.409 321.33 -34.476
## - fTeam    29   19.384 234.30   6.868
## - Height_i  1    0.001 214.92  26.600
## <none>                                214.92  28.598
## - Weight    1   11.946 226.86  49.319
## - fPosition  4   16.150 231.07  51.029
## - poly(Age, 3) 3   40.015 254.93  94.312
##
## Step: AIC=-34.48
## log(Salary) ~ fTeam + fPosition + poly(Age, 3) + Height_i + Weight
##
##           Df Sum of Sq    RSS      AIC
## - fTeam    29   20.264 341.59 -66.791
## - Height_i  1    0.138 321.46 -36.296
## <none>                                321.33 -34.476
## - fPosition  4   12.632 333.96 -26.282
## - Weight    1   10.009 331.33 -23.594
## - poly(Age, 3) 3   69.177 390.50  41.415
##
## Step: AIC=-66.79
## log(Salary) ~ fPosition + poly(Age, 3) + Height_i + Weight
##
##           Df Sum of Sq    RSS      AIC
## - Height_i  1    0.118 341.71 -68.646
## <none>                                341.59 -66.791
## - fPosition  4   11.510 353.10 -60.872
## - Weight    1    7.947 349.54 -59.132
## - poly(Age, 3) 3   63.697 405.29  -0.977
##
## Step: AIC=-68.65
## log(Salary) ~ fPosition + poly(Age, 3) + Weight
##
##           Df Sum of Sq    RSS      AIC
## <none>                                341.71 -68.646
## - fPosition  4   12.582 354.29 -61.459
## - Weight    1    7.833 349.54 -61.127
## - poly(Age, 3) 3   64.650 406.36  -1.869
##
## Call:
## lm(formula = log(Salary) ~ fPosition + poly(Age, 3) + Weight,
##     data = ap_cl_f_wo)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.8899 -0.7047  0.0319  0.6788  1.9272
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 12.961870  0.780418  16.609 < 2e-16 ***
## fPositionPF  0.234813  0.162588   1.444 0.149439
## fPositionPG  0.851080  0.229742   3.705 0.000241 ***

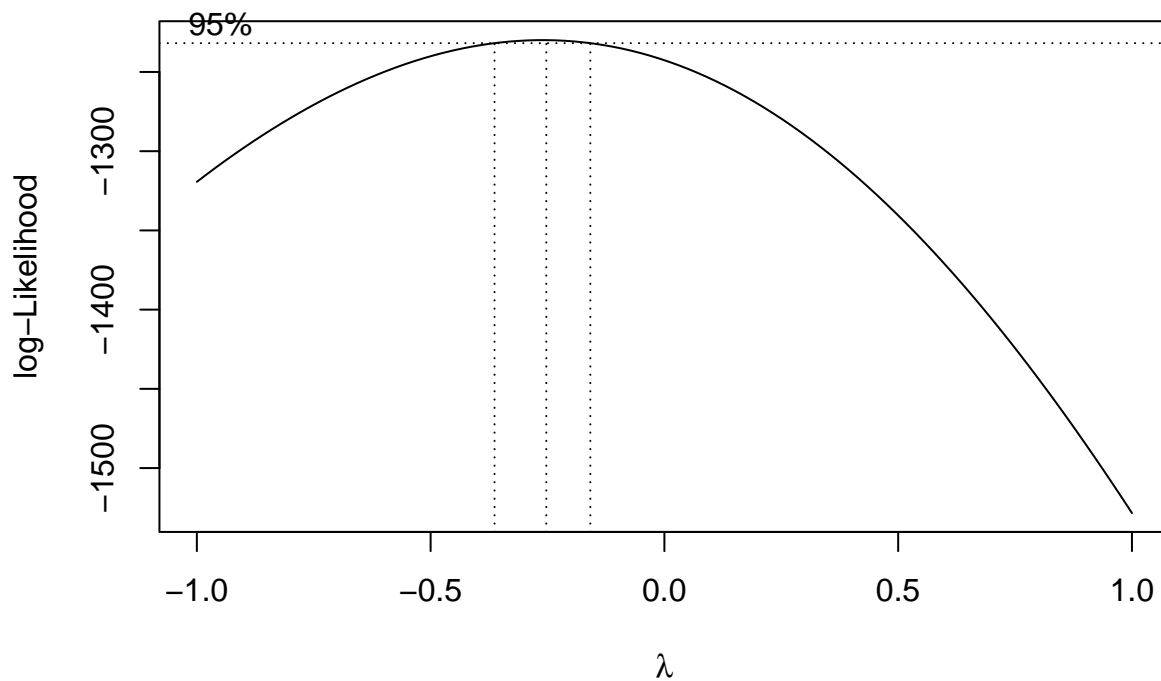
```



```
## fPositionSF      0.364046    0.177851    2.047 0.041302 *
## fPositionSG      0.516664    0.201353    2.566 0.010643 *
## poly(Age, 3)1     7.244927    0.929501    7.794 5.36e-14 ***
## poly(Age, 3)2    -1.482737    0.922096   -1.608 0.108601
## poly(Age, 3)3    -3.428536    0.913288   -3.754 0.000199 ***
## Weight           0.009496    0.003094    3.069 0.002287 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9118 on 411 degrees of freedom
## Multiple R-squared:  0.2017, Adjusted R-squared:  0.1861
## F-statistic: 12.98 on 8 and 411 DF,  p-value: < 2.2e-16
```

Box Cox

```
boxcox(lm1,lambda=seq(-1, 1, by=0.05))
```



```
BoxCoxTrans(ap_tibble$Salary)
```

```
## Box-Cox Transformation
##
## 445 data points used to estimate Lambda
##
## Input data summary:
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##  925258 1802057  4447896  8813696 12000000 45780966
##
```

```

## Largest/Smallest: 49.5
## Sample Skewness: 1.75
##
## Estimated Lambda: -0.2
## With fudge factor, Lambda = 0 will be used for transformations
# Performing
summary(lm_trans_step <- step(lm1_trans <- lm(log(Salary)~fTeam + fPosition + fCollege + poly(Age,3) + Height_i + Weight)

## Start: AIC=63.13
## log(Salary) ~ fTeam + fPosition + fCollege + poly(Age, 3) + Height_i +
## Weight
##
##           Df Sum of Sq  RSS    AIC
## - fCollege 118  112.484 363.45 -8.079
## - fTeam     29   15.575 266.54 31.921
## - Height_i   1    0.107 251.08 61.317
## <none>                250.97 63.127
## - Weight     1    8.165 259.13 75.375
## - fPosition   6   14.621 265.59 76.325
## - poly(Age, 3) 3   45.448 296.42 131.192
##
## Step: AIC=-8.08
## log(Salary) ~ fTeam + fPosition + poly(Age, 3) + Height_i + Weight
##
##           Df Sum of Sq  RSS    AIC
## - fTeam     29   16.550 380.00 -46.264
## - Height_i   1    0.007 363.46 -10.070
## <none>                363.45 -8.079
## - fPosition   6   15.007 378.46 -2.075
## - Weight     1    8.063 371.52 -0.316
## - poly(Age, 3) 3   65.521 428.97 59.678
##
## Step: AIC=-46.26
## log(Salary) ~ fPosition + poly(Age, 3) + Height_i + Weight
##
##           Df Sum of Sq  RSS    AIC
## - Height_i   1    0.002 380.00 -48.261
## <none>                380.00 -46.264
## - fPosition   6   13.866 393.87 -42.315
## - Weight     1    6.228 386.23 -41.030
## - poly(Age, 3) 3   62.593 442.60 15.589
##
## Step: AIC=-48.26
## log(Salary) ~ fPosition + poly(Age, 3) + Weight
##
##           Df Sum of Sq  RSS    AIC
## <none>                380.00 -48.261
## - fPosition   6   14.709 394.71 -43.361
## - Weight     1    6.254 386.26 -42.997
## - poly(Age, 3) 3   63.348 443.35 14.350
##
## Call:
## lm(formula = log(Salary) ~ fPosition + poly(Age, 3) + Weight,

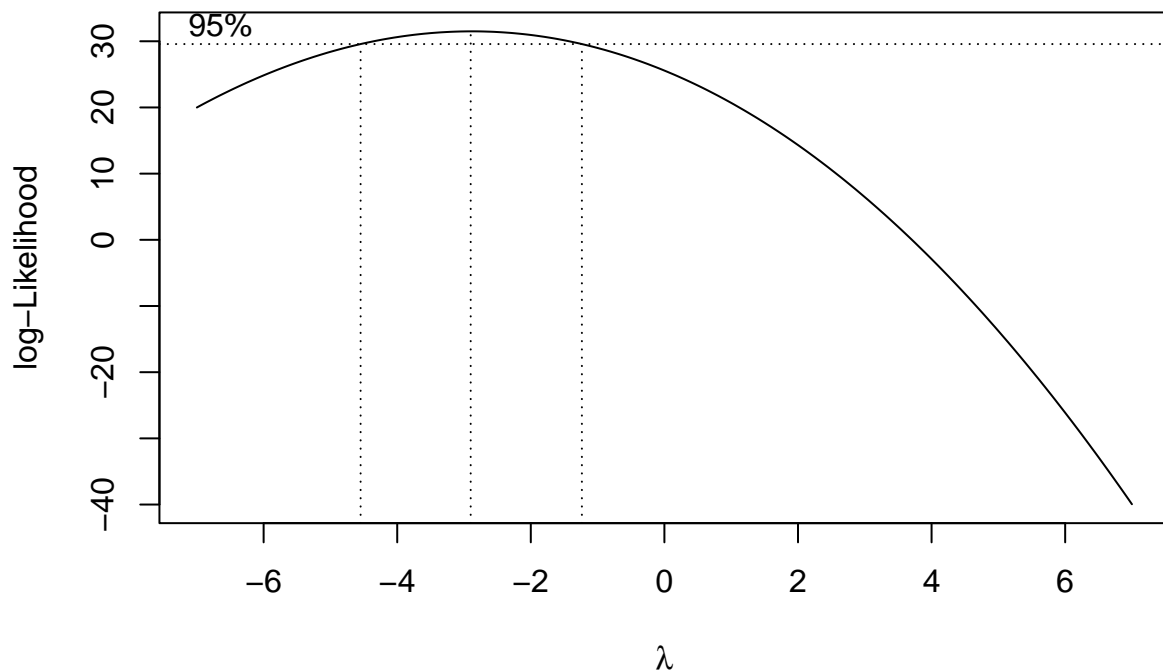
```

```
##      data = ap_tibble)
##
## Residuals:
##      Min        1Q      Median        3Q        Max
## -1.83384 -0.75300  0.00348  0.68066  2.13764
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  13.330870   0.782775  17.030 < 2e-16 ***
## fPositionF   -0.489098   0.340488  -1.436  0.15159
## fPositionG    0.737585   0.412128   1.790  0.07420 .
## fPositionPF   0.174562   0.163833   1.065  0.28725
## fPositionPG   0.711135   0.231400   3.073  0.00225 **
## fPositionSF   0.316997   0.179784   1.763  0.07857 .
## fPositionSG   0.403881   0.202448   1.995  0.04667 *
## poly(Age, 3)1  6.769471   0.952473   7.107 4.89e-12 ***
## poly(Age, 3)2 -3.110142   0.948675  -3.278  0.00113 **
## poly(Age, 3)3 -3.153257   0.942313  -3.346  0.00089 ***
## Weight        0.008296   0.003104   2.673  0.00781 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9357 on 434 degrees of freedom
## Multiple R-squared:  0.1893, Adjusted R-squared:  0.1706
## F-statistic: 10.13 on 10 and 434 DF,  p-value: 2.258e-15
```

Box-Cox w/o outliers and high leverage

Very poor results compared to keeping the high leverage points and the outliers.

```
boxcox(lm1_wo, lambda=seq(-7, 7, by=0.05))
```



```
BoxCoxTrans(ap_cl_f_wo$Salary)
```

```
## Box-Cox Transformation
```

```
##
```

```
## 420 data points used to estimate Lambda
```

```
##
```

```
## Input data summary:
```

```
##      Min.  1st Qu.  Median    Mean  3rd Qu.    Max.
##  925258  1824003  4405020  8530876 10820081 45780966
```

```
##
```

```
## Largest/Smallest: 49.5
```

```
## Sample Skewness: 1.86
```

```
##
```

```
## Estimated Lambda: -0.2
```

```
## With fudge factor, Lambda = 0 will be used for transformations
```

```
summary(lm_wo_step_trans <- step(lm1_wo_trans <- lm(log(Salary)~fTeam + fPosition + fCollege + poly(Age
```

```
## Start:  AIC=28.6
```

```
## log(Salary) ~ fTeam + fPosition + fCollege + poly(Age, 3) + Height_i +
```

```
##      Weight
```

```
##
```

```
##      Df Sum of Sq  RSS    AIC
## - fCollege  116  106.409 321.33 -34.476
## - fTeam     29   19.384 234.30   6.868
## - Height_i   1    0.001 214.92  26.600
## <none>                214.92  28.598
```

```

## - Weight      1      11.946 226.86  49.319
## - fPosition   4      16.150 231.07  51.029
## - poly(Age, 3) 3      40.015 254.93  94.312
##
## Step: AIC=-34.48
## log(Salary) ~ fTeam + fPosition + poly(Age, 3) + Height_i + Weight
##
##           Df Sum of Sq    RSS    AIC
## - fTeam    29     20.264 341.59 -66.791
## - Height_i   1       0.138 321.46 -36.296
## <none>                321.33 -34.476
## - fPosition   4     12.632 333.96 -26.282
## - Weight      1     10.009 331.33 -23.594
## - poly(Age, 3) 3     69.177 390.50  41.415
##
## Step: AIC=-66.79
## log(Salary) ~ fPosition + poly(Age, 3) + Height_i + Weight
##
##           Df Sum of Sq    RSS    AIC
## - Height_i   1       0.118 341.71 -68.646
## <none>                341.59 -66.791
## - fPosition   4     11.510 353.10 -60.872
## - Weight      1       7.947 349.54 -59.132
## - poly(Age, 3) 3     63.697 405.29  -0.977
##
## Step: AIC=-68.65
## log(Salary) ~ fPosition + poly(Age, 3) + Weight
##
##           Df Sum of Sq    RSS    AIC
## <none>                341.71 -68.646
## - fPosition   4     12.582 354.29 -61.459
## - Weight      1       7.833 349.54 -61.127
## - poly(Age, 3) 3     64.650 406.36  -1.869
##
## Call:
## lm(formula = log(Salary) ~ fPosition + poly(Age, 3) + Weight,
##     data = ap_cl_f_wo)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.8899 -0.7047  0.0319  0.6788  1.9272
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  12.961870   0.780418  16.609 < 2e-16 ***
## fPositionPF    0.234813   0.162588   1.444 0.149439
## fPositionPG    0.851080   0.229742   3.705 0.000241 ***
## fPositionSF    0.364046   0.177851   2.047 0.041302 *
## fPositionSG    0.516664   0.201353   2.566 0.010643 *
## poly(Age, 3)1  7.244927   0.929501   7.794 5.36e-14 ***
## poly(Age, 3)2 -1.482737   0.922096  -1.608 0.108601
## poly(Age, 3)3 -3.428536   0.913288  -3.754 0.000199 ***
## Weight         0.009496   0.003094   3.069 0.002287 **

```

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9118 on 411 degrees of freedom
## Multiple R-squared:  0.2017, Adjusted R-squared:  0.1861
## F-statistic: 12.98 on 8 and 411 DF,  p-value: < 2.2e-16
```

Comparing Models

```
performance::compare_performance(lm_log1,lm_log2,lm_log3,lm_step, rank = TRUE)
```

```
## # Comparison of Model Performance Indices
##
## Name      | Model |      R2 | R2 (adj.) |  RMSE | Sigma | AIC weights | BIC weights | Performance-Score
## -----
## lm_log2   |   lm | 0.431 |    0.198 | 0.774 | 0.920 |    < 0.001 |    < 0.001 |             62.45%
## lm_step   |   lm | 0.189 |    0.171 | 0.924 | 0.936 |      0.731 |      0.955 |             35.46%
## lm_log1   |   lm | 0.465 |    0.169 | 0.751 | 0.937 |    < 0.001 |    < 0.001 |             33.43%
## lm_log3   |   lm | 0.189 |    0.169 | 0.924 | 0.937 |      0.269 |      0.045 |              6.93%
```

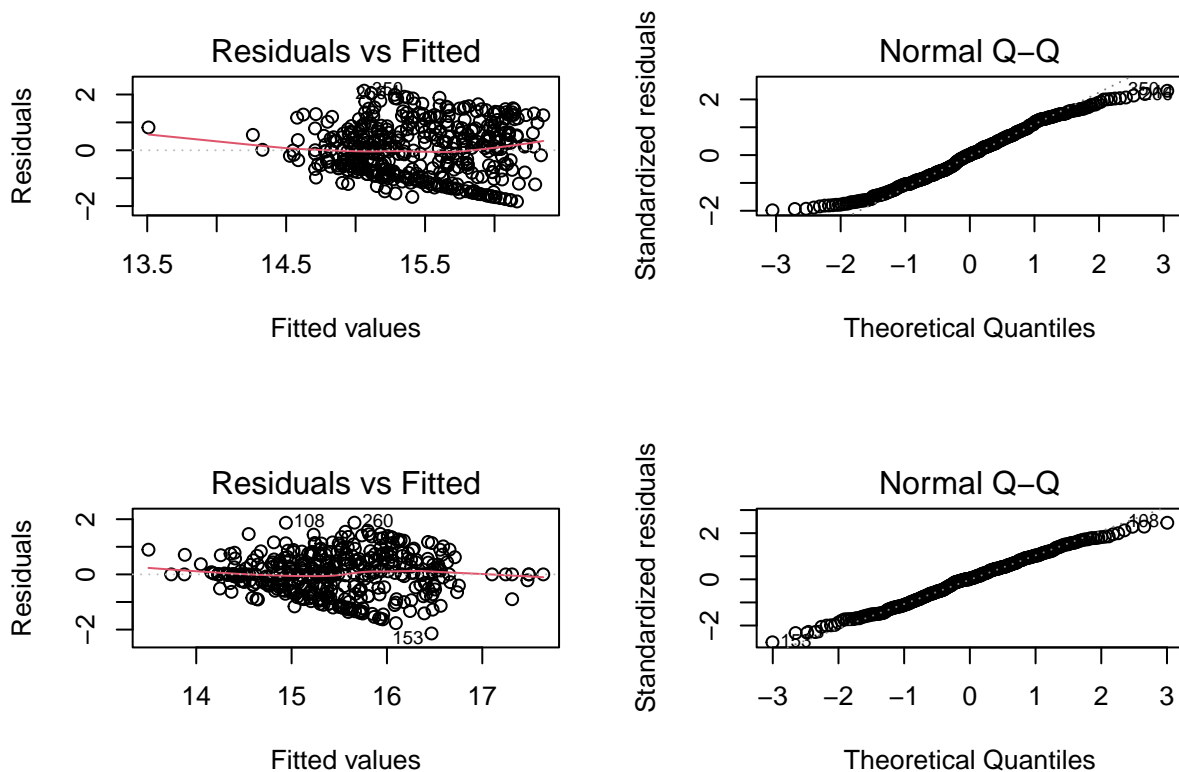
```
anova(lm_trans_step,lm1_trans)
```

```
## Analysis of Variance Table
##
## Model 1: log(Salary) ~ fPosition + poly(Age, 3) + Weight
## Model 2: log(Salary) ~ fTeam + fPosition + fCollege + poly(Age, 3) + Height_i +
##           Weight
##   Res.Df    RSS  Df Sum of Sq      F Pr(>F)
## 1      434 380.00
## 2      286 250.97 148    129.04 0.9936 0.5119
```

```
compare_performance(lm1_wo,lm_wo_step_trans, rank = TRUE)
```

```
## # Comparison of Model Performance Indices
##
## Name      | Model |      R2 | R2 (adj.) |  RMSE | Sigma | AIC weights | BIC weights | Performance
## -----
## lm1_wo     |   lm | 0.498 |    0.206 | 0.715 | 0.901 |    < 0.001 |    < 0.001 |
## lm_wo_step_trans |   lm | 0.202 |    0.186 | 0.902 | 0.912 |      1.00 |      1.00 |
par(mfrow=c(2,2))
plot(lm_step,1:2)
plot(lm1_wo_trans,1:2)
```

```
## Warning: not plotting observations with leverage one:
##   15, 43, 63, 67, 77, 78, 95, 113, 124, 128, 177, 210, 213, 217, 226, 234, 239, 252, 254, 259, 265, 2
```



VIF

```
round(vif(lm_step),2)
```

```
##           GVIF Df  GVIF^(1/(2*Df))
## fPosition  2.97  6           1.09
## poly(Age, 3) 1.08  3           1.01
## Weight     2.89  1           1.70
```

```
round(vif(lm_trans_step),2)
```

```
##           GVIF Df  GVIF^(1/(2*Df))
## fPosition  2.97  6           1.09
## poly(Age, 3) 1.08  3           1.01
## Weight     2.89  1           1.70
```

ROC/AUC

```
set.seed(999)
n <- nrow(ap_tibble)
n
```

```
## [1] 445
```

```
floor(0.7*n)
```

```
## [1] 311
```

```
#randomly sample 70% of the rows

train <- sample(1:n, 311)

glm_train <- glm(fSalary.Dummy ~ poly(Age,3), data=ap_tibble, subset = train, family = binomial)

summary(glm_train)
```

```
##
## Call:
## glm(formula = fSalary.Dummy ~ poly(Age, 3), family = binomial,
##      data = ap_tibble, subset = train)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.4051  -0.9020  -0.5366   1.0295   2.1421
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)   -0.7633     0.1370  -5.572 2.52e-08 ***
## poly(Age, 3)1  14.5161     3.2290   4.496 6.94e-06 ***
## poly(Age, 3)2 -11.6621     3.3093  -3.524 0.000425 ***
## poly(Age, 3)3  -7.5367     3.9924  -1.888 0.059061 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 402.90  on 310  degrees of freedom
## Residual deviance: 353.92  on 307  degrees of freedom
## AIC: 361.92
##
## Number of Fisher Scoring iterations: 5
```

```
ap_test <- ap_tibble[-train,]
head(ap_test)
```

```
##           Name      Team Position Age Height Height_i Weight
## 1   Jaylen Brown Boston Celtics    SG  24  6' 6"      6.60   223
## 2     Kris Dunn Boston Celtics    PG  27  6' 3"      6.30   205
## 3   Carsen Edwards Boston Celtics    PG  23  5' 11"     5.11   200
## 12  Dennis Schroder Boston Celtics    PG  27  6' 3"      6.30   172
## 15  Grant Williams Boston Celtics    PF  22  6' 6"      6.60   236
## 20  Nicolas Claxton Brooklyn Nets    PF  22  6' 11"     6.11   215
##           College   Salary      fTeam fPosition   fCollege Salary.Dummy nTeam
## 1   California 26758928 Boston Celtics    SG California         1      2
## 2   Providence 5005350 Boston Celtics    PG Providence         0      2
## 3     Purdue  1782621 Boston Celtics    PG    Purdue         0      2
## 12      nan  5890000 Boston Celtics    PG      nan         0      2
## 15  Tennessee 2617800 Boston Celtics    PF  Tennessee         0      2
## 20   Georgia  1782621 Brooklyn Nets    PF    Georgia         0      3
##           nPosition nCollege fSalary.Dummy
## 1             7         15             1
## 2             5          79             0
```



```
## 3      5      80      0
## 12     5      60      0
## 15     4      92      0
## 20     4      31      0

probs_test <- predict(glm_train, newdata = ap_test,
                      type = "response")

head(probs_test)

##          1          2          3          12          15          20
## 0.2669248 0.4783374 0.2101948 0.4783374 0.1660439 0.1660439

length(probs_test)

## [1] 134

preds_test <- rep(0,12)
preds_test[probs_test > 0.5] <- 1

length(preds_test)

## [1] 134

length(preds_test)

## [1] 134

head(probs_test)

##          1          2          3          12          15          20
## 0.2669248 0.4783374 0.2101948 0.4783374 0.1660439 0.1660439

head(preds_test)

## [1] 0 0 0 0 0 0

tb1<- table(prediction = preds_test, actual = ap_test$fSalary.Dummy)
addmargins(tb1)

##           actual
## prediction  0  1 Sum
##          0   9  1 10
##          1  13 23 36
##          Sum 22 24 46

#Accuracy
(tb1[1,1] + tb1[2,2]) / 1206

## [1] 0.026534

#Sensitivity
tb1 / 786

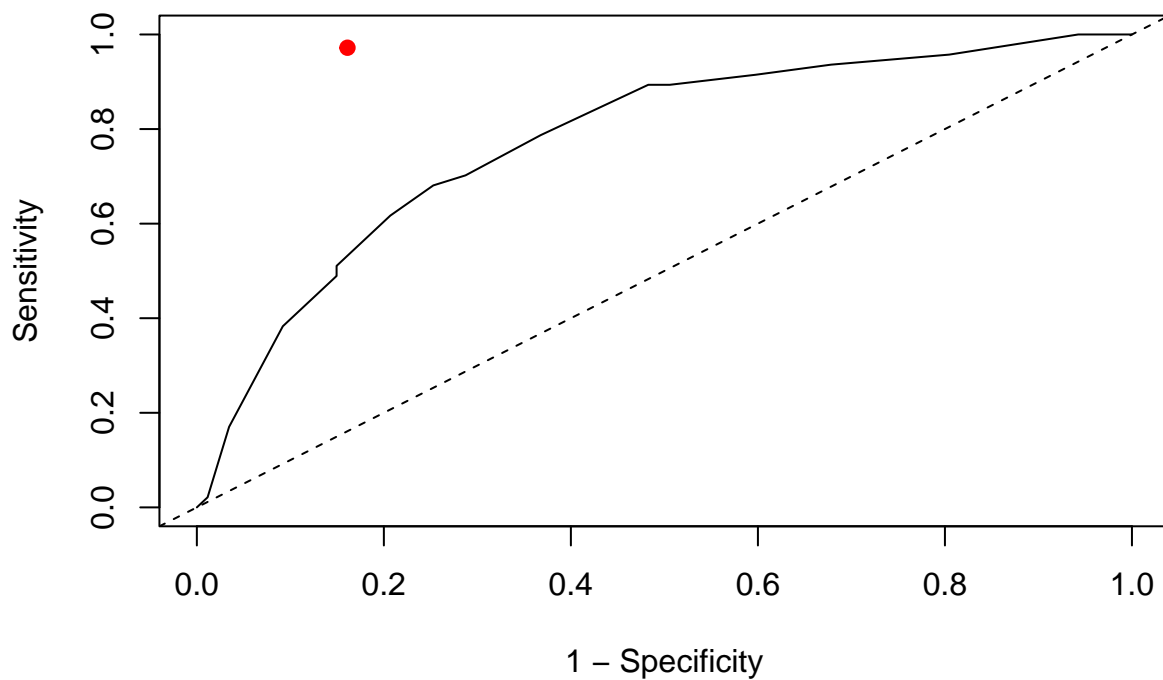
##           actual
## prediction      0      1
##          0 0.011450382 0.001272265
##          1 0.016539440 0.029262087

#Specificity
tb1[1,1] / 148
```

```
## [1] 0.06081081
library(pROC)

## Type 'citation("pROC")' for a citation.
##
## Attaching package: 'pROC'
## The following objects are masked from 'package:stats':
##
##     cov, smooth, var
roc_reduced <- roc(ap_test$fSalary.Dummy, probs_test)

## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
plot(1 - roc_reduced$specificities, roc_reduced$sensitivities, type="l",
     xlab = "1 - Specificity", ylab = "Sensitivity")
# plot red point corresponding to 0.5 threshold:
points(x = 24/149, y = 763/785, col="red", pch=19)
abline(0, 1, lty=2)
```



```
set.seed(999)
n <- nrow(ap_tibble)
n
```

```
## [1] 445
```

```

floor(0.7*n)

## [1] 311
#randomly sample 70% of the rows

train <- sample(1:n, 311)

glm_train <- glm(fSalary.Dummy ~ nTeam+nPosition+nCollege+poly(Age,3)+Height_i+Weight, data=ap_tibble,
summary(glm_train)

##
## Call:
## glm(formula = fSalary.Dummy ~ nTeam + nPosition + nCollege +
##      poly(Age, 3) + Height_i + Weight, family = binomial, data = ap_tibble,
##      subset = train)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.870  -0.859  -0.544   1.020   2.315
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)    2.457222   2.940932   0.836  0.40342
## nTeam           0.002887   0.015193   0.190  0.84927
## nPosition       0.093441   0.085938   1.087  0.27690
## nCollege        -0.002086   0.004161  -0.501  0.61611
## poly(Age, 3)1   14.104543   3.292754   4.284 1.84e-05 ***
## poly(Age, 3)2  -10.679886   3.375668  -3.164  0.00156 **
## poly(Age, 3)3   -7.100286   4.090237  -1.736  0.08258 .
## Height_i        -1.049339   0.463863  -2.262  0.02369 *
## Weight           0.014863   0.007629   1.948  0.05138 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 402.90  on 310  degrees of freedom
## Residual deviance: 346.19  on 302  degrees of freedom
## AIC: 364.19
##
## Number of Fisher Scoring iterations: 5

ap_test <- ap_tibble[-train,]
head(ap_test)

##           Name      Team Position Age Height Height_i Weight
## 1   Jaylen Brown Boston Celtics    SG  24  6' 6"    6.60   223
## 2    Kris Dunn Boston Celtics    PG  27  6' 3"    6.30   205
## 3  Carsen Edwards Boston Celtics    PG  23  5' 11"    5.11   200
## 12 Dennis Schroder Boston Celtics    PG  27  6' 3"    6.30   172
## 15  Grant Williams Boston Celtics    PF  22  6' 6"    6.60   236
## 20 Nicolas Claxton Brooklyn Nets    PF  22  6' 11"    6.11   215
##      College Salary      fTeam fPosition  fCollege Salary.Dummy nTeam

```

```
## 1 California 26758928 Boston Celtics SG California 1 2
## 2 Providence 5005350 Boston Celtics PG Providence 0 2
## 3 Purdue 1782621 Boston Celtics PG Purdue 0 2
## 12 nan 5890000 Boston Celtics PG nan 0 2
## 15 Tennessee 2617800 Boston Celtics PF Tennessee 0 2
## 20 Georgia 1782621 Brooklyn Nets PF Georgia 0 3
```

```
## nPosition nCollege fSalary.Dummy
## 1 7 15 1
## 2 5 79 0
## 3 5 80 0
## 12 5 60 0
## 15 4 92 0
## 20 4 31 0
```

```
probs_test <- predict(glm_train, newdata = ap_test,
                      type = "response")
```

```
head(probs_test)
```

```
## 1 2 3 12 15 20
## 0.3155917 0.4580423 0.4574399 0.3499949 0.1693730 0.2213408
```

```
length(probs_test)
```

```
## [1] 134
```

```
preds_test <- rep(0,12)
```

```
preds_test[probs_test > 0.5] <- 1
```

```
length(preds_test)
```

```
## [1] 134
```

```
length(preds_test)
```

```
## [1] 134
```

```
head(probs_test)
```

```
## 1 2 3 12 15 20
## 0.3155917 0.4580423 0.4574399 0.3499949 0.1693730 0.2213408
```

```
head(preds_test)
```

```
## [1] 0 0 0 0 0 0
```

```
tb2<- table(prediction = preds_test, actual = ap_test$fSalary.Dummy)
addmargins(tb2)
```

```
##          actual
## prediction 0  1 Sum
##          0   8  2 10
##          1  12 24 36
##          Sum 20 26 46
```

```
#Accuracy
```

```
(tb2[1,1] + tb2[2,2]) / 1206
```

```
## [1] 0.026534
```

```

#Sensitivity
tb2[2,2] / 786

## [1] 0.03053435

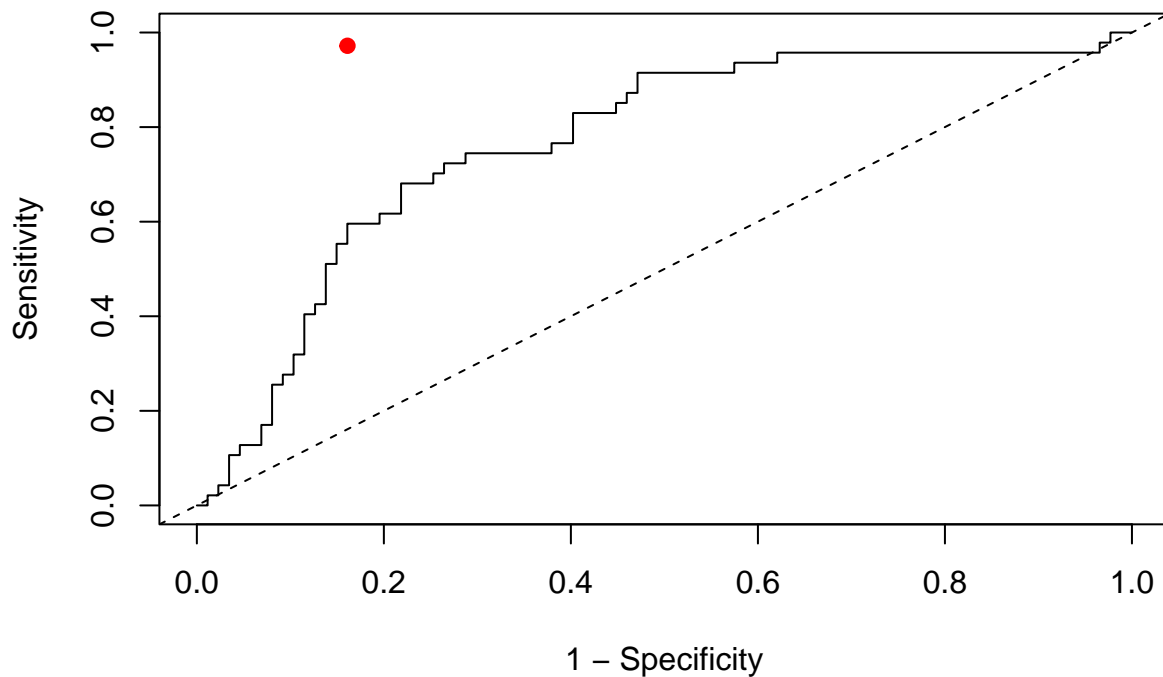
#Specificity
tb2[1,1] / 148

## [1] 0.05405405

library(pROC)
roc_full <- roc(ap_test$fSalary.Dummy, probs_test)

## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
plot(1 - roc_full$specificities, roc_full$sensitivities, type="l",
     xlab = "1 - Specificity", ylab = "Sensitivity")
# plot red point corresponding to 0.5 threshold:
points(x = 24/149, y = 763/785, col="red", pch=19)
abline(0, 1, lty=2)

```



```

auc(roc_full)

## Area under the curve: 0.7674

auc(roc_reduced)

## Area under the curve: 0.7762

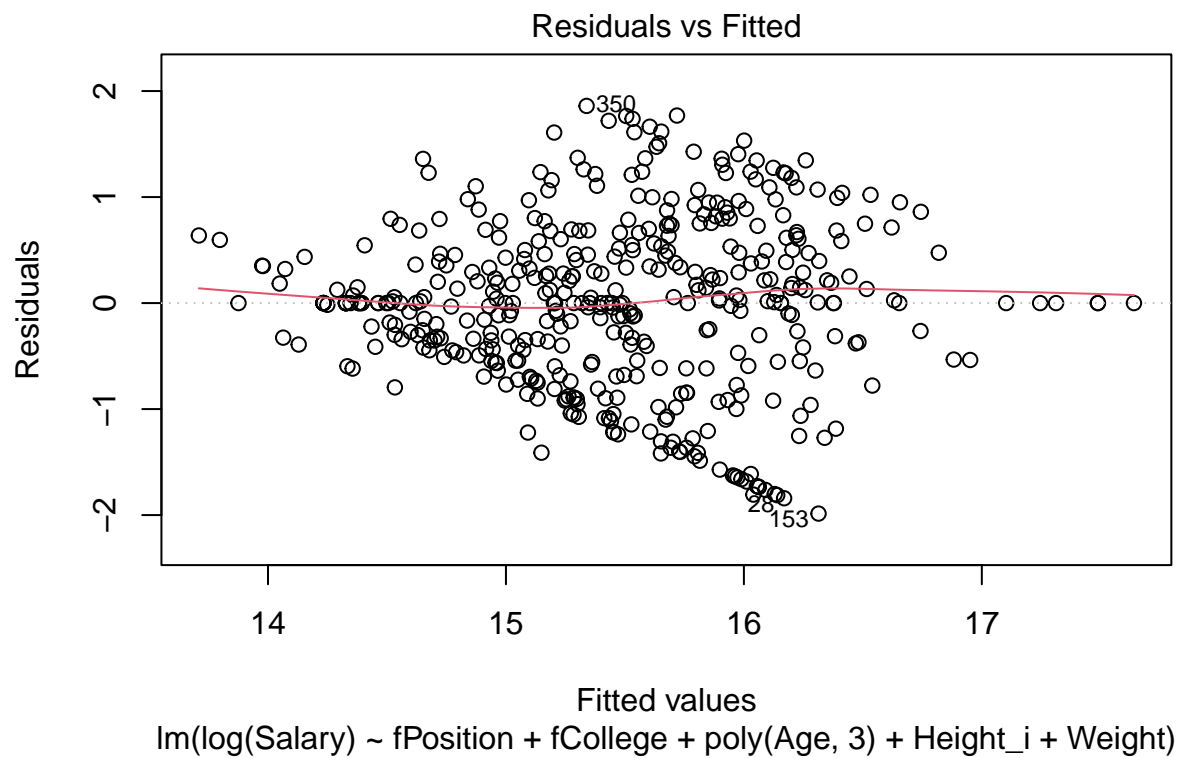
```

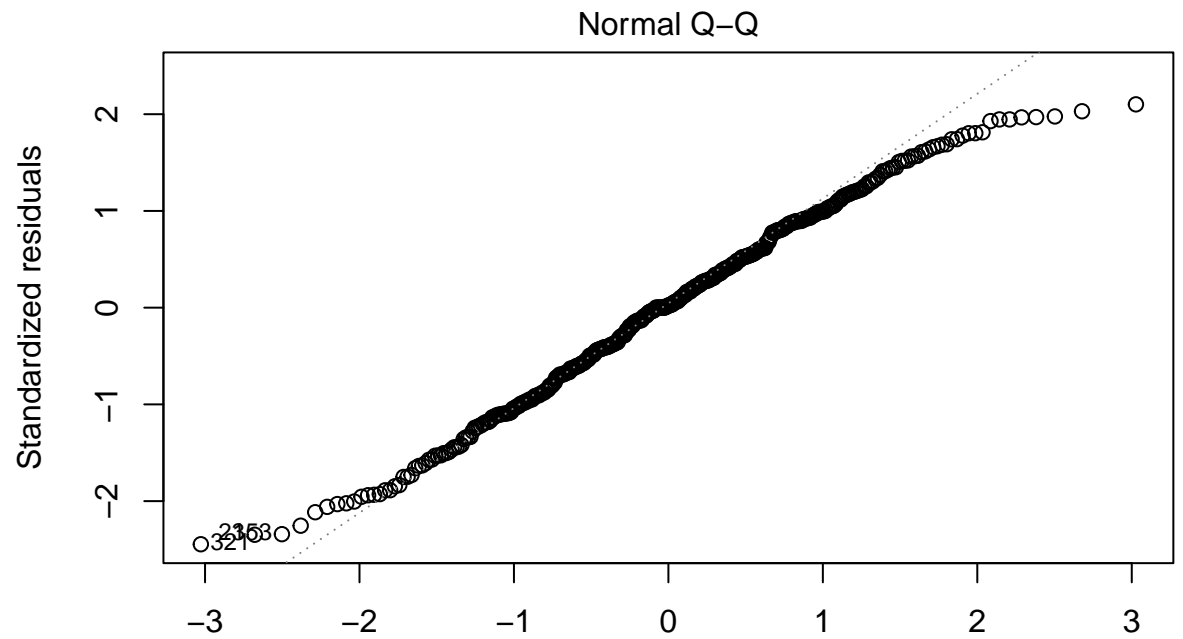
Plots

```
plot(lm_log2, 1:2)
```

```
## Warning: not plotting observations with leverage one:
```

```
## 27, 46, 69, 74, 77, 85, 102, 104, 133, 137, 138, 141, 190, 217, 227, 231, 241, 249, 254, 269, 282,
```



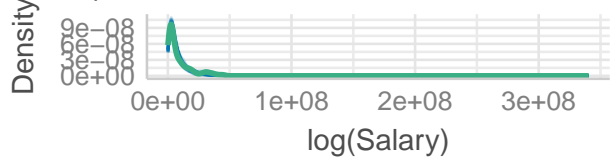


lm(log(Salary) ~ fPosition + fCollege + poly(Age, 3) + Height_i + Weight)

```
check_model(lm_log4)
```

Posterior Predictive Check

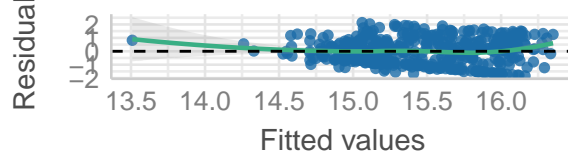
Model-predicted lines should resemble observed data



— Model-predicted data — Observed data

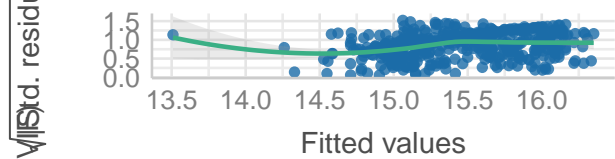
Linearity

Reference line should be flat and horizontal



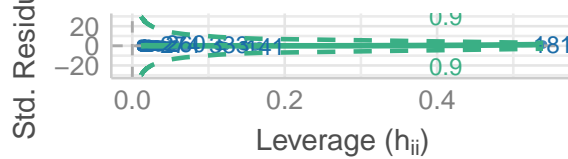
Homogeneity of Variance

Reference line should be flat and horizontal



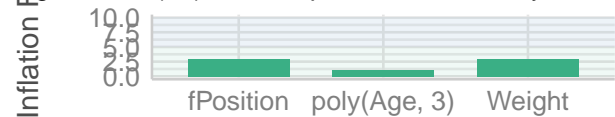
Influential Observations

Points should be inside the contour lines



Collinearity

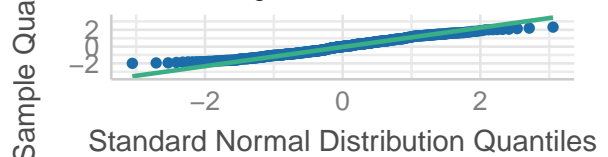
Higher bars (>5) indicate potential collinearity issues



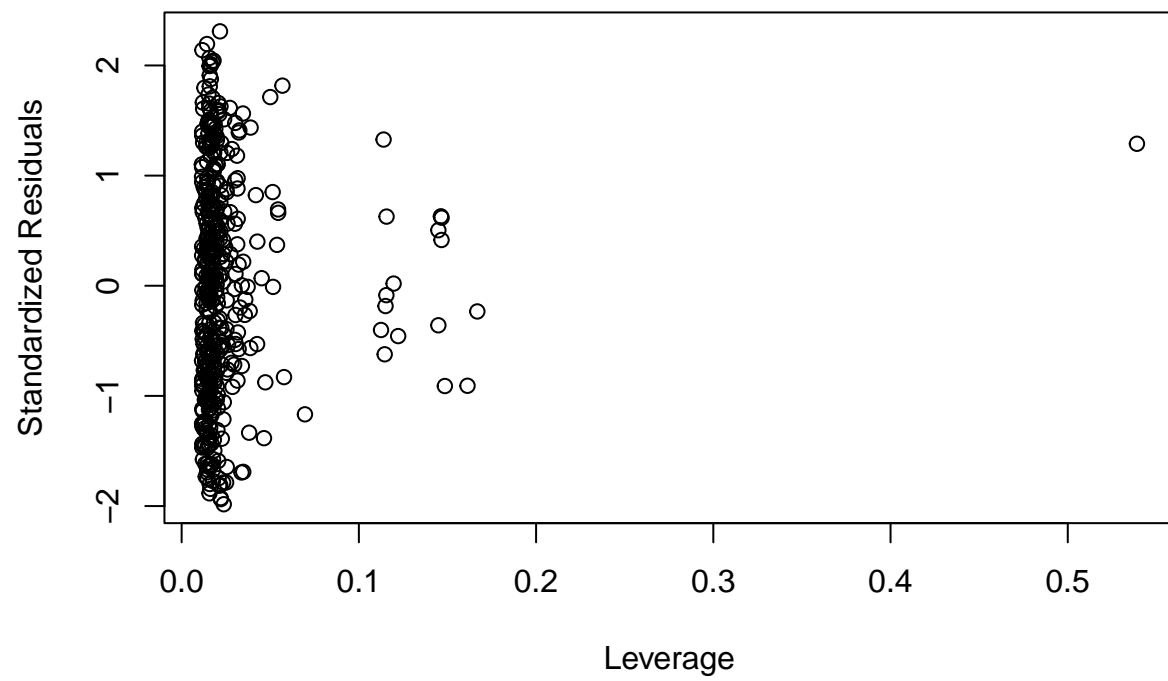
low (< 5) moderate (< 10) high (> 10)

Normality of Residuals

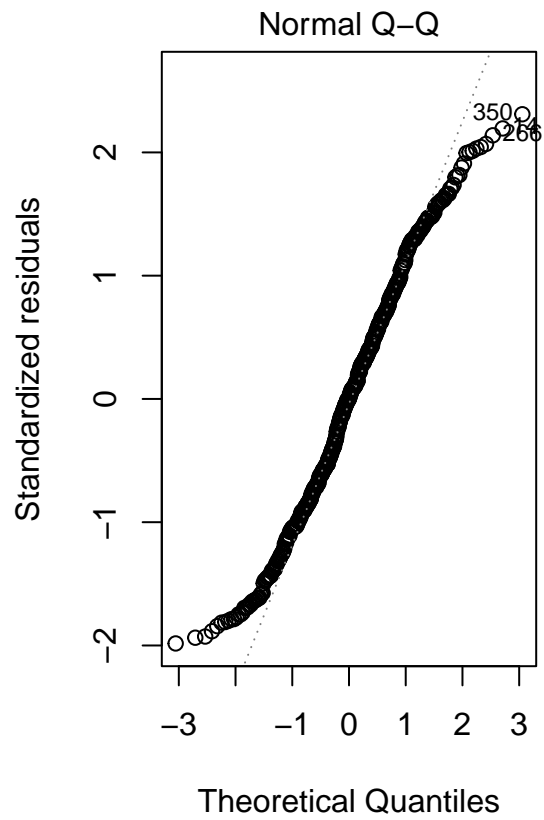
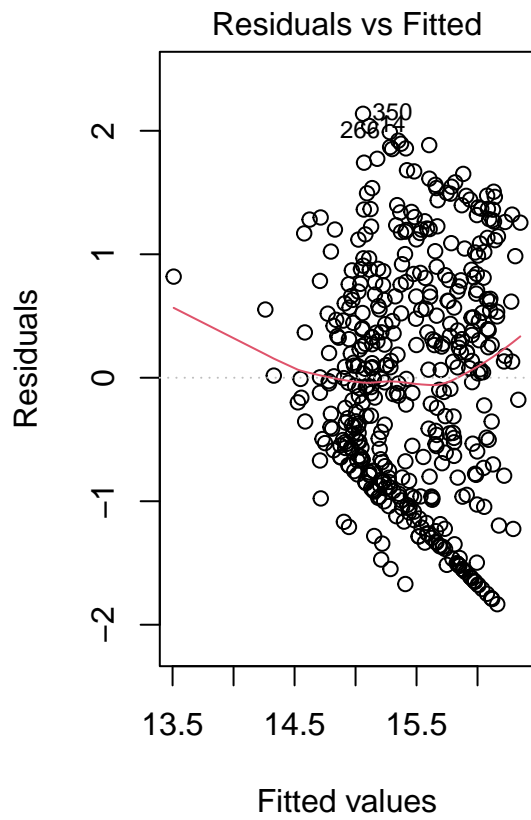
Dots should fall along the line



```
plot(hatvalues(lm_step), rstandard(lm_trans_step), xlab='Leverage', ylab='Standardized Residuals')
```

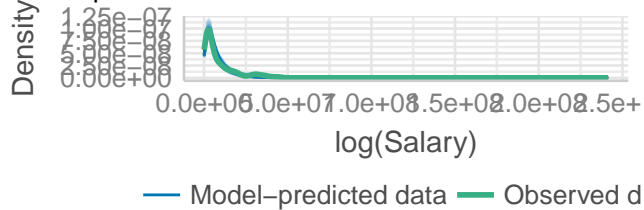
```
par(mfrow=c(1,2), mar=c(4.5, 4.5, 2, 2))  
plot(lm_step, 1:2)
```



```
performance::check_model(lm_step)
```

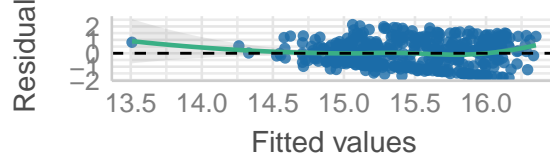
Posterior Predictive Check

Model-predicted lines should resemble observed data



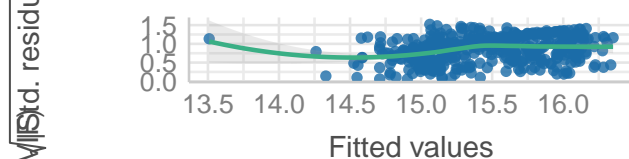
Linearity

Reference line should be flat and horizontal



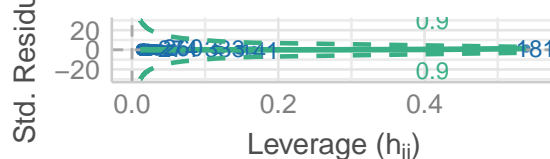
Homogeneity of Variance

Reference line should be flat and horizontal



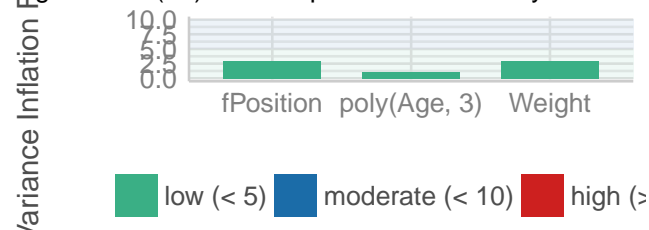
Influential Observations

Points should be inside the contour lines



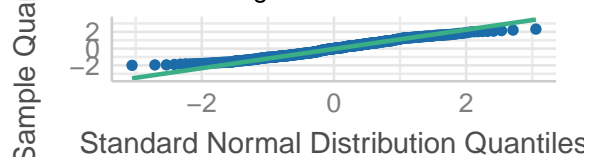
Collinearity

Higher bars (>5) indicate potential collinearity issues



Normality of Residuals

Dots should fall along the line



Final Model - Change

$$\begin{aligned} \log(\widehat{\text{Salary}}) = & 13.330870 - 0.489098(f\text{Position}F) + 0.73758(f\text{Position}G) \\ & + 0.174562(f\text{Position}PF) + 0.711135(f\text{Position}PG) \\ & + 0.316997(f\text{Position}SF) + 0.403881(f\text{Position}SG) \\ & + 6.769471(\text{Age}) - 3.110142(\text{Age})^2 - 3.153257(\text{Age})^3 + 0.008296(\text{Weight}) \end{aligned}$$

Prediction

```
# Steph Curry, Age = 34, Weight = 185, fPosition = PG, Salary = 45780966
newdata <- data.frame(fPosition='PG', Age=34, Weight = 185)
exp(predict(lm_trans_step, newdata, type='response'))
```

```
##          1
## 9417917
```

```
# Miles McBride Age = 20, Weight = 200, fPosition = PG, Salary = 925258
newdata <- data.frame(fPosition='PG', Age=20, Weight = 200)
exp(predict(lm_trans_step, newdata, type='response'))
```

```
##          1
## 4033461
```

```
newdata <- data.frame(fPosition=ap_tibble$fPosition, Age=ap_tibble$Age, Weight = ap_tibble$Weight)
exp(predict(lm_trans_step, newdata, type='response'))
```

```
##          1          2          3          4          5          6          7          8
```

##	4984308	8537257	4995094	2096032	6411921	7581163	3537132	3215994
##	9	10	11	12	13	14	15	16
##	6130537	4792147	6023740	6492755	9668497	3659307	3572870	3334280
##	17	18	19	20	21	22	23	24
##	6544753	4349617	6344794	3001652	3488085	9613913	10445453	10243254
##	25	26	27	28	29	30	31	32
##	8787662	9782022	4098449	8691070	9735534	5568847	3374611	3202418
##	33	34	35	36	37	38	39	40
##	6318667	3478931	9119907	9857477	4956691	3228654	3461139	4033461
##	41	42	43	44	45	46	47	48
##	4748071	3068207	6390165	3418300	11798381	3448000	6643243	10172390
##	49	50	51	52	53	54	55	56
##	7543747	8710380	7810515	8144495	7397451	2493543	4187434	4033461
##	57	58	59	60	61	62	63	64
##	4292953	3557067	3320515	8841498	4298707	4152841	1560487	4923749
##	65	66	67	68	69	70	71	72
##	4353689	3402350	5947200	3663361	5385604	2887368	8623718	4059532
##	73	74	75	76	77	78	79	80
##	5484426	10504758	3591998	5875679	5511577	7857625	4597446	3652850
##	81	82	83	84	85	86	87	88
##	3461139	5363253	9390844	3097476	9600161	4102384	5308460	8918911
##	89	90	91	92	93	94	95	96
##	4040480	2671086	3504438	6544753	3941167	4163656	10259389	4563090
##	97	98	99	100	101	102	103	104
##	2243245	3346367	6241896	10434012	4171798	2162760	4130727	3984114
##	105	106	107	108	109	110	111	112
##	3461139	4730899	3735171	6000120	3869584	5206636	4364772	11040561
##	113	114	115	116	117	118	119	120
##	3936446	3808902	4919026	8463813	8996403	2998965	3370109	3659307
##	121	122	123	124	125	126	127	128
##	11715032	8860864	3790666	6739013	2442713	6352569	6278845	6808475
##	129	130	131	132	133	134	135	136
##	9384586	5170057	6137715	4717492	7330729	4589586	5979852	8048625
##	137	138	139	140	141	142	143	144
##	5767607	7298787	4222316	4130727	8709163	12108208	7238490	11142797
##	145	146	147	148	149	150	151	152
##	8934675	3760504	5881458	8852333	5604945	3904882	8781433	8836347
##	153	154	155	156	157	158	159	160
##	9236121	3381255	4144188	3189861	3153131	3548355	6375131	6621600
##	161	162	163	164	165	166	167	168
##	3839690	3416832	2730311	4144188	3540182	9637449	4668977	2738395
##	169	170	171	172	173	174	175	176
##	4459222	3044575	4783954	8928341	3563065	5544203	9339986	2442713
##	177	178	179	180	181	182	183	184
##	3746230	4339986	10045595	8415937	735930	4040480	9063810	10021062
##	185	186	187	188	189	190	191	192
##	3461139	8352929	6821923	5284690	6574131	6344794	4569882	3718827
##	193	194	195	196	197	198	199	200
##	3172385	3978305	9384586	5382302	3278009	5767607	3746230	11050744
##	201	202	203	204	205	206	207	208
##	3715281	8534317	3092094	3210407	3994490	2954833	7178691	7641185
##	209	210	211	212	213	214	215	216
##	4095146	7002243	10430511	2951213	6907417	3746230	5604945	4944707
##	217	218	219	220	221	222	223	224

##	4292953	3607718	5792848	8637499	2546162	8909954	10147833	8711984
##	225	226	227	228	229	230	231	232
##	2037101	2992018	7359586	3739688	3229094	5275005	8835913	3171724
##	233	234	235	236	237	238	239	240
##	6107839	9675387	6691406	4747086	2760224	8848571	9595456	7673710
##	241	242	243	244	245	246	247	248
##	10085139	7626396	12413322	2624297	4904505	9159819	4664265	9236325
##	249	250	251	252	253	254	255	256
##	4069257	4452937	3832196	4787387	5910384	7631975	8359455	8957654
##	257	258	259	260	261	262	263	264
##	5998659	3933066	7889616	7901517	3673711	6821304	7937203	11798381
##	265	266	267	268	269	270	271	272
##	3713961	4328714	4609671	9080936	4648070	4648070	7504863	10086993
##	273	274	275	276	277	278	279	280
##	6795174	6290415	7113098	7857625	5893075	3790666	2789052	3543354
##	281	282	283	284	285	286	287	288
##	8459369	4152841	4410655	3718827	7330729	7996142	5377220	3790666
##	289	290	291	292	293	294	295	296
##	5148578	6847918	4029196	5206636	2730311	8485854	3796378	3004185
##	297	298	299	300	301	302	303	304
##	5697531	5839699	7759482	8132505	6302770	5813418	6357532	2966465
##	305	306	307	308	309	310	311	312
##	7166115	8308450	11907371	4939395	7555403	2894473	9980858	3338040
##	313	314	315	316	317	318	319	320
##	3005662	9827078	2455790	7330729	3079970	7270168	3175529	2631131
##	321	322	323	324	325	326	327	328
##	5486897	7273145	5069977	12620990	3499562	7755311	2671086	7082949
##	329	330	331	332	333	334	335	336
##	4160501	5263969	3708440	4465027	2145859	3489231	6137715	5069977
##	337	338	339	340	341	342	343	344
##	3673711	4863988	3653254	2882127	3431819	3233184	2602617	3829293
##	345	346	347	348	349	350	351	352
##	3413220	7110186	6011865	2441512	6089736	3475219	3320515	3144826
##	353	354	355	356	357	358	359	360
##	2698595	3975812	3255549	8147618	6060887	8585714	4943602	7621049
##	361	362	363	364	365	366	367	368
##	4422304	4756336	7060572	5067693	3352191	3718827	4917277	8459369
##	369	370	371	372	373	374	375	376
##	4743807	4525823	2814889	3080982	3097476	3446057	7538375	8984175
##	377	378	379	380	381	382	383	384
##	6358691	2441512	10591991	5089871	4292953	4960001	8497847	7324633
##	385	386	387	388	389	390	391	392
##	3017054	7115295	6268464	6341936	3286666	3910394	7499004	3697493
##	393	394	395	396	397	398	399	400
##	9735534	3346367	5950552	2082604	3361355	3751517	5560618	3785139
##	401	402	403	404	405	406	407	408
##	5986853	4639869	2631708	1672339	6293891	3461139	9296626	3187880
##	409	410	411	412	413	414	415	416
##	3112081	3951200	3278009	3360611	7555403	2156909	3341650	3146177
##	417	418	419	420	421	422	423	424
##	5287646	2458447	6956407	3097476	11144300	3352191	6902024	6498495
##	425	426	427	428	429	430	431	432
##	7822693	8486073	7032887	2847477	7657825	6302770	4016256	9870085
##	433	434	435	436	437	438	439	440

##	5617233	2971628	9701211	9339986	9565003	8101351	3814278	9977678
##	441	442	443	444	445			
##	5284690	6681975	4328714	2661191	9934743			

Conclusion

Given that the estimated/predicted salaries are way way off, and that the adjusted R^2 of the `lm_step_trans` is only 0.171, there are obviously other predictors responsible for the majority of variance in the salaries of NBA players, most likely factors such as points scored, assists, rebounds, etc.

It was never expected that non-skill factors would be responsible for explaining the majority of Salary variance.