

Physics - Interference + Tutorial Sheet

- Q1. What is interference of light? Explain

The modifications in the distribution of light energy obtained by the superposition of two waves of equal frequency and constant phase difference in a region of superposition is called interference.

Q2. Is there any conservation of energy in the phenomenon of Interference? Explain. Ans

There is no loss of energy due to interference. The energy is only transferred from the points of minimum displacement to maximum displacement i.e. there is only redistribution of energy. Thus, energy is conserved.

What are conditions to get good interference pattern?

→ Conditions for sustained interference:

 - The two sources should continuously emit waves of the same wavelength or frequency.
 - The amplitude of two waves must be equal or nearly equal.
 - The distance between sources and screen should not be too large as it reduces intensity and too close can cause overlap.
 - The separation between coherent sources must be small if they are very close to each other the background must be blank.



Q4.

Explaining why two independent sources can never be coherent?

In actual practice, it is not possible to have two independent sources which are coherent because in case of any change in phase at the same time when the waves are emitted from the sources affects two coherent sources differently. They will not be in same phase and move with different phase diff.

Q6.

Name two broad methods for production of coherent sources.

Method 1: Use a single source and the beam is arranged to split it into two beams coming from two different sources called virtual sources.

Method 1: Young Double Slit

Method 2: Fresnel Bi-prism

Spherical

Q5.

What are the conditions for minimum or maximum intensity in an interference pattern? If path difference is even multiple of $\lambda/2$ then two waves arrive in same phase producing maximum intensity or if the crest of one wave falls upon crest of other and trough of one wave falls upon trough of other then intensity minimizes.

If path diff is an odd multiple of $\lambda/2$ then waves arrive in different phase producing minimum intensity. If the crest of one wave falls on trough of other wave and vice-versa. Then the resultant will be minima.



Q11

Q2. what is Fresnel Biprism? How will you determine wavelength of light using Fresnel Biprism?
After YDSE, Fresnel brought another way to perform same experiment to study Interference pattern.
Biprism is a combination of two prism with their bases joined and their two faces making an angle of about 179° and other angle of 30° .
Each half of prism produces virtual image of source by refraction. The Fresnel used the biprism to get two coherent sources of monochromatic light from a single source calling it Fresnel Biprism.

The measurement of fringe width in a biprism is enable one to determine wavelength of light if D (distance of source to centre of screen) and d (distance b/w sources) are known i.e.:-

$$\lambda = \frac{d}{D} \beta.$$

Q8. What is effect of interference pattern when monochromatic light in Fresnel Biprism is replaced by white light?

Instead of monochromatic light, when white light is used in the biprism experiment, then the central fringe will be white as all colours will meet in phase. All other fringes will be coloured. These coloured fringes will be due to fact that different colours of white sources will meet in diff. phases. These fringes will overlap each other at very small distance from C.



Q9. Why does the centre of Newton's ring appear dark in reflected light? (Ans. If we know, for bright fringe, $n = \sqrt{1 + \frac{2R}{\lambda}}$ then for dark fringe, $n = \sqrt{1 - \frac{2R}{\lambda}}$ which is less than 1. So there is destructive interference.)

When $n = 1$, then $\lambda = 2R$. At this point, diameter of dark ring is zero and bright ring is $\sqrt{\frac{2R}{4}} = \sqrt{\frac{R}{2}}$.

∴ therefore the central ring is dark. (As while counting or drawing rings 1, 2, 3, etc. the central ring is not counted.)

Q10. What change would you expect in interference pattern of Newton's ring if plane mirror replace transparent plate?

$$\frac{a-b}{d} = R$$

Newton's rings will be formed on the plane mirror. As the radius of curvature of the mirror is very large, so the fringes will be very close to each other. This is because the angle between the two rays reflected from the two surfaces of the lens is very small. The fringes will be very bright and distinct.

Q11.

Explain the terms: fringes of equal thickness and fringes of equal inclination.

Fringes of equal inclination:- These fringes are formed when light from an extended source falls on a thin film of an optically denser medium.

Fringes of equal thickness! These periodic fringes appear in the images. The sources must be monochromatic for the fringe thickness to be constant and good intensity.

Q12.

Describe Newton's rings experiment for measuring the wavelength of monochromatic light and give the necessary theory. What will happen if little water is introduced b/w the lens and the plate?

To determine whether the wavelength λ of light from the source is given by $\lambda = \frac{d^2}{4R}$, replace the point source by a given source of monochromatic light. Focus the travelling microscope on the Newton's ring formed.

d_n and d_{n+m} of n th and $(n+m)$ th dark rings and Radius of curvature R . Taking $\mu = 1$, the wavelength λ will be :-

$$\frac{d_n^2}{4R} = n\lambda \quad \text{--- (1)}$$

for d_{n+m} the diameter of $(n+m)$ th dark ring,

$$\frac{d_{n+m}^2}{4R} = (n+m)\lambda \quad \text{--- (2)}$$

Sub (1) and (2),

$$\frac{d_{n+m}^2}{4R} - \frac{d_n^2}{4R} = m\lambda$$

$$\lambda = \frac{4(d_{n+m}^2 - d_n^2)}{4Rm}$$

$$\text{If } \mu = 1 \text{ then } \lambda = \frac{d_{n+m}^2 - d_n^2}{4Rm}$$



DATE _____

PAGE _____

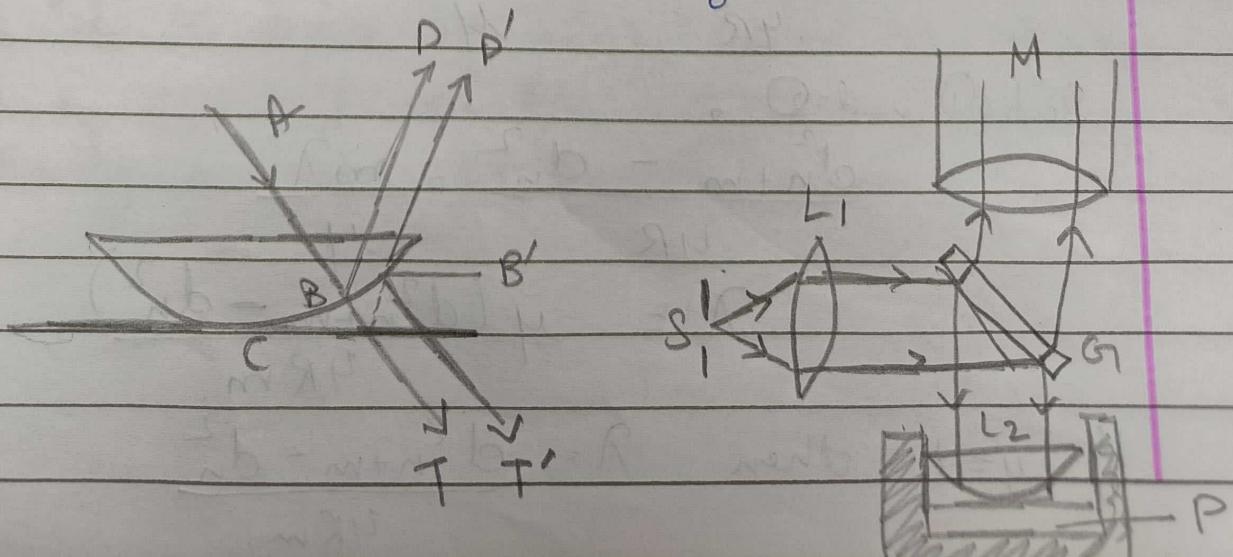
Let the refractive index of material of glass be n_1 and glass plate is n_2 , and the refractive index of water be n then
 $n_1 > n > n_2$.

If water is placed b/w a convex lens and glass plate then reflection in both cases will be lesser to rarer and the two interfering rays are reflected under same condition. So centre point will be bright as in refracted system.

Q13. What are Newton's rings? Describe and explain formation of Newton's rings in reflected monochromatic light.

When the air film is illuminated normally by monochromatic light circular interference fringes are observed. The fringes are concentric circles.

With monochromatic light bright and dark circular fringes are produced in air film. The rings gradually become narrower as their radii increase. The interference rings so formed were first navigated by Newton and were called Newton's rings.



The convex surface of lens makes contact with the glass plate at point C and encloses a thin film of air or rare transparent liquid.

The light from a monochromatic extended source is held parallel by a convex lens L, and is incident at angle of 45° . The glass plate reflects the light vertically downwards. The reflected part suffers phase change of π because the air film is backed by glass plate. These two reflected rays interfere and give rise to interference pattern in form of circular rings.

Q14. What are applications of high reflection and anti-reflection coating?

Anti-Reflection Coating: - reduces the reflection of light from surface.

- Used on eyeglasses, photographic lenses and solar cells to reduce glare, improve aesthetic, make the wearer's eyes more visible and on solar cells to reduce reflection losses to improve efficiency.

High Reflection Coating: - applied to increase reflectance of light from surface while reducing absorption and scatter.

- On medical devices like endoscopy and microscope
- improves efficiency of lasers.

Q15. What is the purpose of glass plate incline at 45° in Newton ring experiment?

The angle b/w the incoming ray and the glass plate is 45° degree to make turns the light rays to 90° and that's why they fall normally on the plano convex lens.

$$\frac{S}{I} = \frac{zP}{zI} = \frac{wT}{wI}$$

Ques 16.4 Find the ratio of intensity at the centre of a bright fringe in an interference pattern to intensity at one point quarter of distance b/w two fringes from source.

Ques 17 Two waves of a single source having amplitudes A₁ & A₂ interfere to give an intensity I = I₁ + I₂ + 2I₁I₂ cos φ. If the resulting amplitude is $A_m^2 = A_1^2 + A_2^2 + 2A_1A_2 \cos \phi$.

What is phase difference b/w two waves if the ratio of intensities is 16 : 9?

$$\text{B } I \propto A^2 \text{ So,}$$

Simplifying

$$I_1 = I_2 \Rightarrow I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \phi = 4I_1$$

Since $I_1 = I_2$, intensity ratio = number of maxima

When the maximum occurs at centre, $\phi = 0$.

$$I_{12} = 4I_1 - I_1 = 3I_1$$

Now $I_1 = I_2$ so number of maxima = 16 : 9

Since the phase diff. b/w two successive fringes is 2π , the phase diff. b/w two points separated by a distance equal to one quarter of distance b/w the two successive fringes is $\frac{\pi}{2}$.

$$\phi = 2\pi \left(\frac{1}{4}\right) = \frac{\pi}{2} \text{ radian}$$

$$I_{12} = 4I_1 \cos^2 \left(\frac{\pi/2}{2}\right) = 2I_1 - 1$$

Not yet get 16 : 9 ratio of intensities

Using eq ① and ②, get no. of maxima

$$\frac{I_{12}}{I_{12}} = \frac{4I_1}{2I_1} = 2.$$

Ques 17

$$I_{max} = (a_1 + a_2)^2 \times 2 \times 0.1 \times 2 = R$$

$$I_{min} = (a_1 - a_2)^2 \times 2 \times 0.1 \times 2 = \mu$$

$$\frac{I_{max}}{I_{min}} = \frac{(a_1 + a_2)^2}{(a_1 - a_2)^2} = \frac{2a_1(a_1 + a_2)^2}{(a_1 + a_2)(a_1 - a_2)} = \frac{2a_1(a_1 + a_2)^2}{a_1(a_1 - a_2)} = \frac{2(a_1 + a_2)^2}{a_1 - a_2}$$

$$\frac{I_{max}}{I_{min}} = \frac{a_1 + a_2}{a_1 - a_2} \times 2 \times 0.1 \times 2 = \frac{f(1-\mu)}{f(1+\mu)}$$

Given, $\frac{I_1}{I_2} = \frac{\sqrt{a_1^2}}{\sqrt{a_2^2}} = \frac{\sqrt{81}}{\sqrt{1}} = f$

$$\frac{a_1}{a_2} = \frac{9}{1} \Rightarrow (1-\mu) \cdot \frac{9}{1} = 0.2$$

$$a_1 = 9a_2$$

Thus, $2 \cdot f = \mu \Rightarrow 2 \cdot 9 = \mu \Rightarrow \mu = 0.8$

$$\frac{I_{max}}{I_{min}} = \frac{9a_2 + a_2}{f(1-\mu)a_2 - a_2} = \frac{10a_2}{48a_2} = \frac{5}{4}$$

$$I_{max} : I_{min} = 5 : 4$$

Ques 18

for monofilament

$$y = \frac{n \times R \times D}{d}$$

$$\text{when } R = 600 \text{ mm}, n = 12, D = 18 \text{ mm}, PZ = 0.0 = 0.15$$

$$y = \frac{12 \times 600 \times 18}{12 \times 0.15 \times 18} = 12000 \text{ mm} = 120 \text{ m}$$

$$\text{when } R = 480, n = ?, D = 1, PZ = 0.1 = \mu$$

$$y = \frac{480 \times n \times 1}{0.15} = 3200n \text{ m} \quad \text{Eq ②}$$

Equate eq ① and ②,

$$\frac{480 \times n \times 18}{0.15} = 3200n \times 1$$

$$115 = n$$

Q20.

$$\lambda = 6 \times 10^{-5} \text{ cm} = 6 \times 10^{-3} \text{ m}$$

$$\mu = 1.5$$

$$n = 5 \quad t = ?$$

$$(4-1)t = n\lambda$$

$$(1.5-1)t = 5 \times 6 \times 10^{-3}$$

$$t = \frac{6 \times 10^{-3}}{3 \times 10^{-2}}$$

$$t = 6 \times 10^{-2} \text{ m}$$

Q20.

$$x_0 = \frac{\beta}{\lambda} (\mu - 1)t$$

$$x_0 = 5\beta \quad \lambda = 6 \times 10^{-3} \text{ m} \quad \mu = 1.5$$

$$5\beta = \frac{\beta}{\lambda} (\mu - 1)t$$

$$30 \times 10^{-3} = 0.5 t$$

$$6 \times 10^{-6} \text{ m} = t$$

Q21. ~~β~~ $= 0.431 \text{ mm}^{-2} = 431 \text{ m}^{-1} = 431 \times 10^{-6} \text{ m}^{-1}$ m/s

$$\lambda = 5.89 \times 10^{-7} \text{ cm} = 5.89 \times 10^{-7} \text{ m}$$

$$x_0 = 1.89 \times 10^{-3} \text{ m}$$

$$\mu = 1.59 \quad t = ? \text{ s} \quad 0.08 \text{ m} = R \text{ m/s}$$

$$x_0 = \frac{\beta}{\lambda} (\mu - 1)t$$

$$1.89 \times 10^{-3} = \frac{431 \times 10^{-6}}{5.89 \times 10^{-7}} (1.59 - 1)t$$

$$t = 2.1 \text{ s}$$

$$t = \frac{5.89 \times 1.89}{431 \times 0.59} \times 10^{-6} = 6.5$$

$$t = 4.38 \times 10^{-6} \text{ m.}$$

Q22.

$$d_{n+1} = 2 \times 1.0 = 3 \text{ m}$$

$$d_n = 24.2 \times 10^{-3} \text{ m}$$

$$R = 1 \text{ m}$$

$$\lambda = \frac{d_{n+1}^2 + d_n^2}{4 \times R \times 1.0}$$

$$\lambda = \frac{49 \times 10^{-6} + 17.64 \times 10^{-6}}{4 \times 1.0}$$

$$\lambda = \frac{31.36 \times 10^{-6}}{4 \times 1.0}$$

$$\lambda = 7.84 \times 10^{-6} \text{ m}$$

Q23.

Let diameter of n^{th} dark ring be, $m \text{ cm}$ (Q)

$$y = \left(\frac{\text{diam}}{\text{dia}_1} \right)^2$$

$$y = \frac{d^2}{\left(\frac{d}{2}\right)^2}$$

$$y = 4 \frac{d^2}{d^2} = 4$$

$$\boxed{y > 1}$$

thus y increases with increase of value of d
 means as d increases y increases



Q28. $2d = n\lambda \times P_{8.1} \times P_{8.2} = +$

$$\frac{1}{2} \times 0.0589 \times 10^{-3} \text{ m}^2 \times 200 \times \lambda = +$$

$$589 \times 10^{-9} \text{ m} = \lambda \quad \text{Ans. ab}$$

$$589 \text{ nm} = \lambda \quad \text{Ans. ab}$$

$$m = R$$

Q29.

$$\frac{47150}{28} \times 10^{-10} \text{ m}$$

$$\frac{47150}{28} = 1.50 \text{ m} = \lambda$$

$$\lambda = 4800 \times 10^{-10} \text{ m}$$

$$m = 500$$

$$2(0.1 \times 1.50) = 2(0.1 \times 500) = R$$

$$2(1.50) t = m \lambda$$

$$2(1.50) t = 500 \times 48 \times 10^{-8} = R$$

$$t = 240 \times 10^{-6}$$

~~$$t = 2.4 \times 10^{-4} \text{ m. Ans.}$$~~

Q30. (a) when 180° out of phase. β extends to $\frac{\pi}{2}$

Q31. (b) Comparable to one wavelength of light.

Q32. (a) division of amplitude.

If planoconvex lens is replaced with greater radius of curvature R then,

for both dark and bright ring, $P = \mu l$

$$d_n \propto \sqrt{R}$$

If radius of curvature increases the diameter of rings will also increase.



Q23. We know, diameter of ring like orbit for elliptical orbit is given by formula
 $D_{n+1} = \sqrt{(n+1) \lambda R}$ is orbital radius of orbit for elliptical orbit
 and we have a No change both type of increase with
 formula $D_{n+1} = \sqrt{(n+2) \lambda R}$ given by above part
 & same type of orbit for elliptical orbit

82)

$$\frac{D_n}{D_{n+1}} = \sqrt{\frac{(n+1)}{(n+2)}} \text{ orbital radius for elliptical orbit } 8/9$$

④

number of orbits remain same. so for number of orbits

The total Sq. is both sides, square of elliptical orbit will be

$$(n+1)^2 / (n+2)^2 = 100 / 81$$

⑤

now above no $49n^2 + 49 = 100 n^2 + 200 n$ not for no want

so divide it by 100, $51n = 51$ now divide it by 51

later all the distance $n = 1$ - unbalanced mass not to
 orbit with orbit of 9 times

⑥

$$\text{now orbital radius } \lambda = \sqrt{4\pi n^2}$$

now no orbital $\lambda = \sqrt{RA}$

$$M_n = \frac{R}{\sqrt{n\lambda}}$$

extension remains the same in

$$M_{n_1} = \sqrt{n\lambda R}$$

$$M_{n_2} = \sqrt{n\lambda R} : \text{no change of A}$$

now after M_1 mass is $2\pi RA M_2$ internal -

no change of mass

$$\text{So if } \frac{M_{n_1}}{M_{n_2}} = \frac{M_2}{M_1} = \frac{10}{9} \text{ orbital radius : also not -}$$

$$\frac{R_{n_2}}{R_{n_1}} = \frac{M_1}{M_2} = \frac{9}{10} \text{ remains of}$$

so now no orbital orbital radius : $\sqrt{RA} = 9 -$
 mass of $M_2 = \frac{10}{9}$ standard circular motion

orbital radius R_{n_1} both cases are same speed

start due to

$$M_1 : M_2 = 49 : 100 \cancel{\text{A.S.}}$$

Ques.

Principle of Anti reflecting coatings:-
 Anti reflecting coating are thin films that reduce the amount of light that reflects off a surface and they work by causing destructive interference b/w reflected light waves.



D/B anti reflecting and high reflecting coating.

①

Reduce reflections and glare Increase surface reflectance and improve clarity of images. and reflect almost all $\text{PP}_{\text{out}} = \text{light of a certain } n$.

②

These are often made from silicon dioxid, titanium oxide or tantalum pentoxide. These are made from metal or dielectric materials with metal nanoparticles like silver.

③

AR ~~coatings~~ are used in high end cameras, microscope.

These are mainly used to make mirrors of lens.

$$\frac{\text{RR}_{\text{in}}}{\mu} = \text{RR}_{\text{out}}$$

$$\frac{\text{RR}_{\text{in}}}{\mu} = \text{RR}_{\text{out}}$$

Applications:-

- Corrective lenses: ARCs can improve aesthetics and ~~reg~~ reduce glare.
- Solar cells: Antireflecting coating can be applied to camera lenses.
- Photolithography: Antireflective coatings are used in microelectronic photolithography to help reduce image distortions associated with reflections of substrate.

$$\frac{\text{RR}_{\text{in}}}{\mu} : \text{PP} = \mu : \mu$$