

QUADERNO2 FEDERICO BUSSOLINO S317641

1.

a. L'attributo più selettivo è node-caps;

b. L'altezza massima dell'albero è 7 (maxdepth contando radice-foglia, 6 non contando radice o foglia);

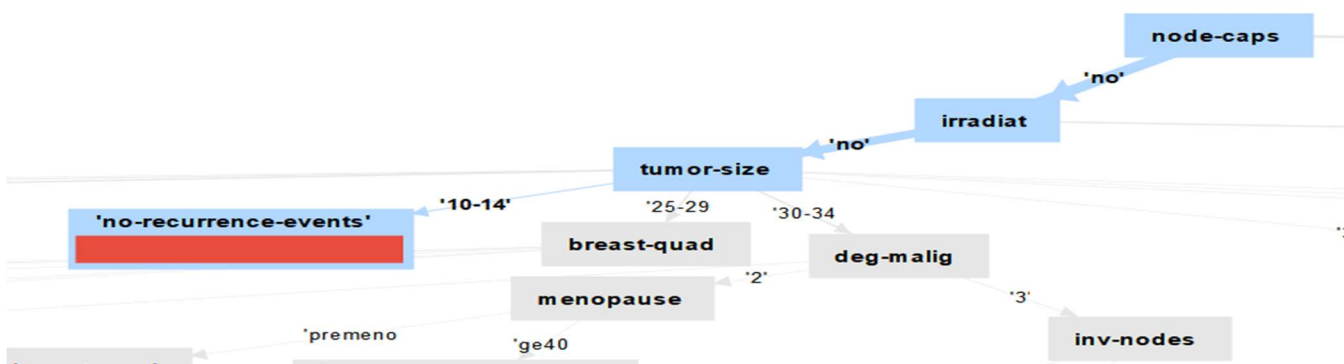
c. partizionamento puro:

node-caps: no

irradiat: no

tumor-size: 10-14

→ 25 casi in cui il tumore non si è ripresentato



Tree

```
node-caps = 'no'
| irradiat = 'no'
| | tumor-size = '0-4'
| | | menopause = 'ge40': {'recurrence-events'=0, 'no-recurrence-events'=4}
| | | menopause = 'premeno'
| | | age = '30-39': {'recurrence-events'=1, 'no-recurrence-events'=1}
| | | age = '40-49': {'recurrence-events'=0, 'no-recurrence-events'=2}
| | tumor-size = '10-14': {'recurrence-events'=0, 'no-recurrence-events'=25}
```

2.

Osservazioni:

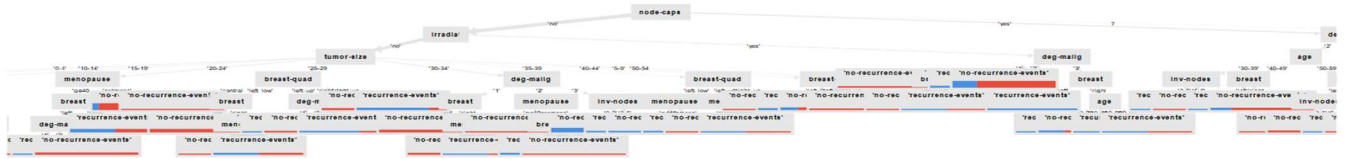
a) Maximal-depth può essere portato fino a 7 con min-gain 0.01 senza modificare l'albero

b) con mingain=0.001 ottengo il massimo numero di ripartizioni tenendo invariato 2 come minimo numero di attributi per foglia, diminuendo ulteriormente mingain gli attributi non vengono ulteriormente suddivisi

e) Mingain=0.01 Maximal-depth=5 → ottengo un albero in cui vi sono ancora partizioni pure, anche se sono di meno, vi sono più attributi per foglia → casi + generali (si può settare il numero di attributi per foglia, ragionevolmente almeno 2 per evitare che un caso specifico di 1 tupla influenzi le decisioni su tutte le tuple aventi gli stessi valori di attributi → rischio overfitting da verificare in fase di test)

(riporto rappresentazione testuale perché più comprensibile)

a) Mingain=0.01, maxdepth=7 →albero uguale a maxdepth=10



b) Mingain=0.001, maxdepth=10 →la foglia a profondità max è 7(maxdepth 8)

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| | | tumor-size = '30-34'
| | | | deg-malign = '1'
| | | | | breast = 'left': 'no-recurrence-events' {'recurrence-events'=0, 'no-recurrence-events'=6}
| | | | | breast = 'right'
| | | | | | menopause = 'ge40': 'no-recurrence-events' {'recurrence-events'=0, 'no-recurrence-events'=4}
| | | | | | menopause = 'premeno': 'recurrence-events' {'recurrence-events'=1, 'no-recurrence-events'=1}
| | | | | deg-malign = '2'
| | | | | | menopause = 'ge40': 'no-recurrence-events' {'recurrence-events'=0, 'no-recurrence-events'=2}
| | | | | | menopause = 'premeno'
| | | | | | | breast-quad = 'left_up': 'recurrence-events' {'recurrence-events'=2, 'no-recurrence-events'=2}
| | | | | | | breast-quad = 'right_low': 'no-recurrence-events' {'recurrence-events'=0, 'no-recurrence-events'=}
| | | | | deg-malign = '3'
| | | | | | inv-nodes = '0-2'
| | | | | | breast = 'left'
| | | | | | menopause = 'ge40': 'recurrence-events' {'recurrence-events'=1, 'no-recurrence-events'=1}
| | | | | | menopause = 'premeno': 'no-recurrence-events' {'recurrence-events'=1, 'no-recurrence-events'=}

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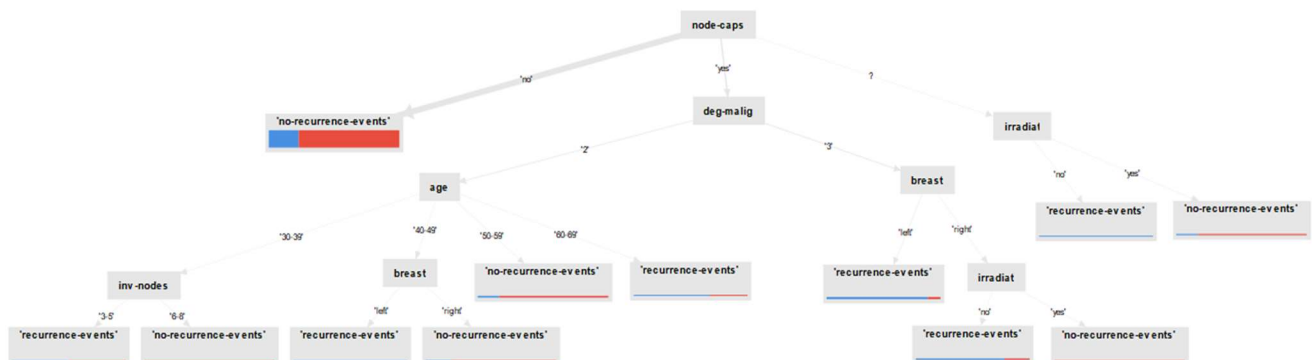
c) Mingain=0.001, maxdepth=5 →la parte di albero precedente ha meno nodi (3)

```

node-caps = 'no'
| irradiat = 'no'
| | tumor-size = '0-4': 'no-recurrence-events' {'recurrence-events'=1, 'no-recurrence-events'=7}
| | tumor-size = '10-14': 'no-recurrence-events' {'recurrence-events'=0, 'no-recurrence-events'=25}
| | tumor-size = '15-19': 'no-recurrence-events' {'recurrence-events'=3, 'no-recurrence-events'=19}
| | tumor-size = '20-24': 'no-recurrence-events' {'recurrence-events'=6, 'no-recurrence-events'=28}
| | tumor-size = '25-29'
| | | breast-quad = 'central': 'no-recurrence-events' {'recurrence-events'=0, 'no-recurrence-events'=2}
| | | breast-quad = 'left_low': 'no-recurrence-events' {'recurrence-events'=2, 'no-recurrence-events'=12}
| | | breast-quad = 'left_up': 'no-recurrence-events' {'recurrence-events'=3, 'no-recurrence-events'=5}
| | | breast-quad = 'right_low': 'no-recurrence-events' {'recurrence-events'=0, 'no-recurrence-events'=4}
| | | breast-quad = 'right_up': 'recurrence-events' {'recurrence-events'=4, 'no-recurrence-events'=1}
| | tumor-size = '30-34'
| | | deg-malign = '1': 'no-recurrence-events' {'recurrence-events'=1, 'no-recurrence-events'=11}
| | | deg-malign = '2': 'no-recurrence-events' {'recurrence-events'=2, 'no-recurrence-events'=6}
| | | deg-malign = '3': 'recurrence-events' {'recurrence-events'=7, 'no-recurrence-events'=7}
| | tumor-size = '35-39'
| | | breast-quad = 'left_low': 'recurrence-events' {'recurrence-events'=3, 'no-recurrence-events'=3}
| | | breast-quad = 'left_up': 'no-recurrence-events' {'recurrence-events'=1, 'no-recurrence-events'=3}
| | | breast-quad = 'right_up': 'no-recurrence-events' {'recurrence-events'=0, 'no-recurrence-events'=2}
| | tumor-size = '40-44'
| | | breast-quad = 'left_low': 'recurrence-events' {'recurrence-events'=2, 'no-recurrence-events'=2}
| | | breast-quad = 'left_up': 'no-recurrence-events' {'recurrence-events'=1, 'no-recurrence-events'=5}
| | | breast-quad = 'right_up': 'no-recurrence-events' {'recurrence-events'=0, 'no-recurrence-events'=3}
| | tumor-size = '5-9': 'no-recurrence-events' {'recurrence-events'=0, 'no-recurrence-events'=3}
| | tumor-size = '50-54'
| | | breast = 'left': 'no-recurrence-events' {'recurrence-events'=0, 'no-recurrence-events'=2}
| | | breast = 'right': 'recurrence-events' {'recurrence-events'=1, 'no-recurrence-events'=1}
| irradiat = 'yes'
| | deg-malign = '1': 'recurrence-events' {'recurrence-events'=2, 'no-recurrence-events'=2}
| | deg-malign = '2': 'no-recurrence-events' {'recurrence-events'=4, 'no-recurrence-events'=13}
| | deg-malign = '3': 'recurrence-events' {'recurrence-events'=8, 'no-recurrence-events'=5}

```

d) Mingain=0.05, maxdepth=10 →tutto l'albero è rappresentabile in un immagine (pochi split)



e)Mingain=0.01, maxdepth=5 →buon albero 7 nodi foglia con 2 soli attributi su 35 foglie

```
node-caps = 'no'
| irradiat = 'no'
| | tumor-size = '0-4': 'no-recurrence-events' ('recurrence-events'=1, 'no-recurrence-events'=7)
| | tumor-size = '10-14': 'no-recurrence-events' ('recurrence-events'=0, 'no-recurrence-events'=25)
| | tumor-size = '15-19': 'no-recurrence-events' ('recurrence-events'=3, 'no-recurrence-events'=19)
| | tumor-size = '20-24': 'no-recurrence-events' ('recurrence-events'=6, 'no-recurrence-events'=28)
| | tumor-size = '25-29'
| | | breast-quad = 'central': 'no-recurrence-events' ('recurrence-events'=0, 'no-recurrence-events'=2)
| | | breast-quad = 'left_low': 'no-recurrence-events' ('recurrence-events'=2, 'no-recurrence-events'=12)
| | | breast-quad = 'left_up': 'no-recurrence-events' ('recurrence-events'=3, 'no-recurrence-events'=5)
| | | breast-quad = 'right_low': 'no-recurrence-events' ('recurrence-events'=0, 'no-recurrence-events'=4)
| | | breast-quad = 'right_up': 'recurrence-events' ('recurrence-events'=4, 'no-recurrence-events'=1)
| | tumor-size = '30-34'
| | | deg-malign = '1': 'no-recurrence-events' ('recurrence-events'=1, 'no-recurrence-events'=11)
| | | deg-malign = '2': 'no-recurrence-events' ('recurrence-events'=2, 'no-recurrence-events'=6)
| | | deg-malign = '3': 'recurrence-events' ('recurrence-events'=7, 'no-recurrence-events'=7)
| | tumor-size = '35-39'
| | | breast-quad = 'left_low': 'recurrence-events' ('recurrence-events'=3, 'no-recurrence-events'=3)
| | | breast-quad = 'left_up': 'no-recurrence-events' ('recurrence-events'=1, 'no-recurrence-events'=3)
| | | breast-quad = 'right_up': 'no-recurrence-events' ('recurrence-events'=0, 'no-recurrence-events'=2)
| | tumor-size = '40-44'
| | | breast-quad = 'left_low': 'recurrence-events' ('recurrence-events'=2, 'no-recurrence-events'=2)
| | | breast-quad = 'left_up': 'no-recurrence-events' ('recurrence-events'=1, 'no-recurrence-events'=5)
| | | breast-quad = 'right_up': 'no-recurrence-events' ('recurrence-events'=0, 'no-recurrence-events'=3)
| | tumor-size = '5-9': 'no-recurrence-events' ('recurrence-events'=0, 'no-recurrence-events'=3)
| | tumor-size = '50-54'
| | | breast = 'left': 'no-recurrence-events' ('recurrence-events'=0, 'no-recurrence-events'=2)
| | | breast = 'right': 'recurrence-events' ('recurrence-events'=1, 'no-recurrence-events'=1)
| irradiat = 'yes'
| | deg-malign = '1': 'recurrence-events' ('recurrence-events'=2, 'no-recurrence-events'=2)
| | deg-malign = '2': 'no-recurrence-events' ('recurrence-events'=4, 'no-recurrence-events'=13)
| | deg-malign = '3': 'recurrence-events' ('recurrence-events'=8, 'no-recurrence-events'=5)
node-caps = 'yes'
| deg-malign = '2'
| | age = '30-39'
| | | inv-nodes = '3-5': 'recurrence-events' ('recurrence-events'=1, 'no-recurrence-events'=1)
| | | inv-nodes = '6-8': 'no-recurrence-events' ('recurrence-events'=0, 'no-recurrence-events'=2)
| | age = '40-49'
| | | breast = 'left': 'recurrence-events' ('recurrence-events'=2, 'no-recurrence-events'=0)
| | | breast = 'right': 'no-recurrence-events' ('recurrence-events'=1, 'no-recurrence-events'=4)
| | age = '50-59': 'no-recurrence-events' ('recurrence-events'=2, 'no-recurrence-events'=10)
| | age = '60-69': 'recurrence-events' ('recurrence-events'=2, 'no-recurrence-events'=1)
| | deg-malign = '3'
| | | breast = 'left': 'recurrence-events' ('recurrence-events'=16, 'no-recurrence-events'=2)
| | | breast = 'right'
| | | | irradiat = 'no': 'recurrence-events' ('recurrence-events'=7, 'no-recurrence-events'=2)
| | | | irradiat = 'yes': 'no-recurrence-events' ('recurrence-events'=0, 'no-recurrence-events'=3)
node-caps = '?'
| irradiat = 'no': 'recurrence-events' ('recurrence-events'=2, 'no-recurrence-events'=0)
| irradiat = 'yes': 'no-recurrence-events' ('recurrence-events'=1, 'no-recurrence-events'=5)
```

3.

a)

accuracy: 66.35% +/- 4.40% (micro average: 66.35%)			
	true 'recurrence-events'	true 'no-recurrence-events'	class precision
pred. 'recurrence-events'	135	193	41.16%
pred. 'no-recurrence-events'	161	563	77.76%
class recall	45.61%	74.47%	

b)

accuracy: 65.78% +/- 4.07% (micro average: 65.78%)			
	true 'recurrence-events'	true 'no-recurrence-events'	class precision
pred. 'recurrence-events'	136	200	40.48%
pred. 'no-recurrence-events'	160	556	77.65%
class recall	45.95%	73.54%	

c)

accuracy: 67.87% +/- 3.95% (micro average: 67.87%)			
	true 'recurrence-events'	true 'no-recurrence-events'	class precision
pred. 'recurrence-events'	125	167	42.81%
pred. 'no-recurrence-events'	171	589	77.50%
class recall	42.23%	77.91%	

d)

accuracy: 72.65% +/- 4.06% (micro average: 72.72%)			
	true 'recurrence-events'	true 'no-recurrence-events'	class precision
pred. 'recurrence-events'	78	69	53.06%
pred. 'no-recurrence-events'	218	687	75.91%
class recall	26.35%	90.87%	

e)

accuracy: 67.96% +/- 3.92% (micro average: 67.97%)			
	true 'recurrence-events'	true 'no-recurrence-events'	class precision
pred. 'recurrence-events'	125	166	42.96%
pred. 'no-recurrence-events'	171	590	77.53%
class recall	42.23%	78.04%	

4.

a) $k=2 \rightarrow$ considerazioni: se si vuole intervenire in ottica preventiva rispetto al ripresentarsi dei tumori conviene prendere un classificatore con alto recall per recurrence-events

accuracy: 67.22% +/- 4.20% (micro average: 67.21%)

	true 'recurrence-events'	true 'no-recurrence-events'	class precision
pred. 'recurrence-events'	134	183	42.27%
pred. 'no-recurrence-events'	162	573	77.96%
class recall	45.27%	75.79%	

b) $k=5 \rightarrow$ per non allarmare inutilmente le persone conviene scegliere un classificatore con + accuracy

accuracy: 72.63% +/- 3.76% (micro average: 72.62%)

	true 'recurrence-events'	true 'no-recurrence-events'	class precision
pred. 'recurrence-events'	112	104	51.85%
pred. 'no-recurrence-events'	184	652	77.99%
class recall	37.84%	86.24%	

c) $k=10 \rightarrow$ accuracy elevata, buon class recall per recurrence-events

accuracy: 75.04% +/- 2.31% (micro average: 75.00%)

	true 'recurrence-events'	true 'no-recurrence-events'	class precision
pred. 'recurrence-events'	107	74	59.12%
pred. 'no-recurrence-events'	189	682	78.30%
class recall	36.15%	90.21%	

d) $k=15 \rightarrow$ perdita di class recall per recurrence-events

accuracy: 74.39% +/- 2.84% (micro average: 74.43%)

	true 'recurrence-events'	true 'no-recurrence-events'	class precision
pred. 'recurrence-events'	86	59	59.31%
pred. 'no-recurrence-events'	210	697	76.85%
class recall	29.05%	92.20%	

e) $k=8 \rightarrow$ alternativa migliore di $k=5$: buon compromesso accuracy e class recall recurrence-events

accuracy: 73.55% +/- 3.32% (micro average: 73.48%)

	true 'recurrence-events'	true 'no-recurrence-events'	class precision
pred. 'recurrence-events'	113	96	54.07%
pred. 'no-recurrence-events'	183	660	78.29%
class recall	38.18%	87.30%	

naïve-bayes ottiene prestazioni migliori: ottimo recall per recurrence-events e buona precisione

accuracy: 73.27% +/- 3.87% (micro average: 73.19%)

	true 'recurrence-events'	true 'no-recurrence-events'	class precision
pred. 'recurrence-events'	143	129	52.57%
pred. 'no-recurrence-events'	153	627	80.38%
class recall	48.31%	82.94%	

5. MATRICE DI CORRELAZIONE

Attributes	age	menopa...	tumor-s...	inv-nod...	node-ca...	deg-malig	breast	breast-...	irradiat
age	1	0.241	-0.045	-0.001	0.052	-0.043	0.067	-0.024	-0.011
menopau...	0.241	1	0.019	-0.011	0.130	-0.161	0.077	-0.096	-0.075
tumor-size	-0.045	0.019	1	-0.131	0.058	0.133	-0.022	-0.056	-0.022
inv-nodes	-0.001	-0.011	-0.131	1	-0.465	-0.213	0.040	0.063	0.399
node-caps	0.052	0.130	0.058	-0.465	1	0.098	0.024	-0.036	-0.197
deg-malig	-0.043	-0.161	0.133	-0.213	0.098	1	-0.073	0.018	-0.074
breast	0.067	0.077	-0.022	0.040	0.024	-0.073	1	0.175	-0.019
breast-qu...	-0.024	-0.096	-0.056	0.063	-0.036	0.018	0.175	1	-0.005
irradiat	-0.011	-0.075	-0.022	0.399	-0.197	-0.074	-0.019	-0.005	1

Gli attributi sono incorrelati, alcuni sono debolmente correlati → si può applicare l'ipotesi naïve

La coppia di attributi maggiormente correlata è: inv-nodes e node-caps