

gradB :

$$\vec{v} = -c\{B_z + \frac{mc}{q}\}(\frac{cE_A \sin\{2\pi(\frac{t}{T} - \frac{LR_0}{\lambda})\} + \frac{\pi}{2}}{B_z^2} \xi_r)^{-1} (E_A \sin\{2\pi(\frac{t}{T} - \frac{LR_0}{\lambda})\} + \frac{\pi}{2}) - \frac{\mu}{q} \xi_r + \frac{mc^2}{q} \frac{(E_A \sin\{2\pi(\frac{t}{T} - \frac{LR_0}{\lambda})\} + \frac{\pi}{2})^2 \xi_r}{B_z^3} \vec{e}_\theta$$

$$\text{so, } v_{\text{grad}} = \frac{c}{B_z} \frac{\mu}{q} \xi_r$$

$$\text{assumption } B_z = \frac{B_E}{L^3} \text{ (in magnetic equator) , } B_E = 3.11 \times 10^{-5} \text{ T} = 3.11 \times 10^{-1} \text{ G} \text{ if } L = 6, B_z = 1.4 \times 10^{-7} \text{ T} = 1.4 \times 10^{-3} \text{ G}$$

$$\text{assumption : } v_{\text{perp}} = 0.01c = 3.0 \times 10^8 \text{ cm/s}$$

$$\mu = \frac{mv_{\text{perp}}^2}{2B_z} = \frac{(9.1 \times 10^{-28} \text{ g}) \times (3.0 \times 10^8 \text{ cm/s})^2}{2.0 \times 1.4 \times 10^{-3} \text{ G}}$$

$$\xi_r = \frac{\partial B_z}{\partial r} = \frac{\partial B_z}{\partial L} \frac{\partial L}{\partial r} = -3 \frac{B_E}{L^4} \frac{1}{R_0} = \frac{-3 \times 3.1 \times 10^{-1} \text{ G}}{6^4 \times 6 \times 10^8 \text{ cm}}$$

$$v_{\text{grad}} = \frac{c}{B_z} \frac{\mu}{q} \xi_r = \frac{3.0 \times 10^{10} \text{ cm/s}}{1.4 \times 10^{-3} \text{ G}} \times \frac{1}{4.8 \times 10^{-10} \text{ statC}} \times \frac{(9.1 \times 10^{-28} \text{ g}) \times (3.0 \times 10^8 \text{ cm/s})^2}{2.0 \times 1.4 \times 10^{-3} \text{ G}} \times \frac{-3 \times 3.1 \times 10^{-1} \text{ G}}{6^4 \times 6 \times 10^8 \text{ cm}}$$

$$v_{\text{grad}} = -\frac{3.0 \times 9.1 \times 3.0 \times 3 \times 3.1}{1.4 \times 4.8 \times 2.0 \times 1.4 \times 6^4 \times 6 \times 10^5} \text{ cm/s} \approx 1500 \text{ cm/s}$$

from basic space plasma physics

$$v_{\nabla} = \frac{mv_{\text{perp}}^2}{2qB^3} (\vec{B} \times \nabla B)$$

$$v_{\nabla} = \frac{9.1 \times 10^{-31} \text{ kg} \times (3.0 \times 10^6 \text{ m/s})^2}{2 \times (1.6 \times 10^{-19} \text{ C}) \times (1.4 \times 10^{-7} \text{ T})^3 (1.4 \times 10^{-7} \text{ T})} \times (-3 \frac{B_E}{L^4} \frac{1}{R_0})$$

$$v_{\nabla} = \frac{9.1 \times 10^{-31} \text{ kg} \times (3.0 \times 10^6 \text{ m/s})^2}{2 \times (1.6 \times 10^{-19} \text{ C}) \times (1.4 \times 10^{-7} \text{ T})^3 (1.4 \times 10^{-7} \text{ T})} \times (-3 \frac{3.11 \times 10^{-5} \text{ T}}{6^4} \frac{1}{6.0 \times 10^6 \text{ m}})$$

$$v_{\nabla} = -\frac{9.1 \times 9.0 \times 1.4 \times 3 \times 3.11}{2 \times 1.6 \times 1.4^3 \times 6^4 \times 6} \frac{10^{-31}}{10^{-34}} \text{ m/s}$$

$$v_{\nabla} = -\frac{9.1 \times 9.0 \times 1.4 \times 3 \times 3.11}{2 \times 1.6 \times 1.4^3 \times 6^4 \times 6} 10^3 \text{ m/s} = 0.015 \times 10^3 \text{ m/s} = 15 \text{ m/s}$$