

Intro to Computer Network
HW4

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1) Dijkstra's (link state) algorithm

| | | D(B) | D(C) | D(D) | D (E) | D (F) | D (G) | D (H) |
|------|----------|-------|------|----------|-------|-------|----------|----------|
| step | N' | P (B) | P(C) | P(D) | P(E) | P(F) | P(G) | P(H) |
| 0 | A | 1, A | 2, A | ∞ | 1, A | 5, A | ∞ | ∞ |
| 1 | AE | 1, A | 2, A | ∞ | | 4, E | 6, E | ∞ |
| 2 | AEB | | 2, A | 2, B | | 4, E | 6, E | ∞ |
| 3 | AEBD | | 2, A | | | 4, E | 6, E | 4, D |
| 4 | AEBDC | | | | | 4, E | 6, E | 4, D |
| 5 | AEBDCF | | | | | | 6, E | 4, D |
| 6 | AEBDCFH | | | | | | 6, E | |
| 7 | AEBDCFHG | | | | | | | |

1) Find E, not in N' such that D (E) is minimum

Add E to N'

$$\begin{aligned} D(B) &= \min\{D(B), D(E)+c(E, B)\} = \min\{1, 1+\infty\} = 1 \\ D(C) &= \min\{D(C), D(E)+c(E, C)\} = \min\{2, 1+\infty\} = 2 \\ D(D) &= \min\{D(D), D(E)+c(E, D)\} = \min\{\infty, 1+\infty\} = \infty \\ D(F) &= \min\{D(F), D(E)+c(E, F)\} = \min\{5, 1+3\} = 4 \\ D(G) &= \min\{D(G), D(E)+c(E, G)\} = \min\{\infty, 1+5\} = 6 \\ D(H) &= \min\{D(H), D(E)+c(E, H)\} = \min\{\infty, 1+\infty\} = \infty \end{aligned}$$

2) Find B, not in N' such that D (B) is minimum

Add B to N'

$$\begin{aligned} D(C) &= \min\{D(C), D(B)+c(B, C)\} = \min\{2, 1+\infty\} = 2 \\ D(D) &= \min\{D(D), D(B)+c(B, D)\} = \min\{\infty, 1+1\} = 2 \\ D(F) &= \min\{D(F), D(B)+c(B, F)\} = \min\{4, 1+\infty\} = 4 \\ D(G) &= \min\{D(G), D(B)+c(B, G)\} = \min\{6, 1+\infty\} = 6 \\ D(H) &= \min\{D(H), D(B)+c(B, H)\} = \min\{\infty, 1+\infty\} = \infty \end{aligned}$$

3) Find D not in N' such that D (D) is minimum

Add D to N'

$$\begin{aligned} D(C) &= \min\{D(C), D(D)+c(D, C)\} = \min\{2, 2+4\} = 2 \\ D(F) &= \min\{D(F), D(D)+c(D, F)\} = \min\{4, 2+2\} = 4 \\ D(G) &= \min\{D(G), D(D)+c(D, G)\} = \min\{6, 2+\infty\} = 6 \\ D(H) &= \min\{D(H), D(D)+c(D, H)\} = \min\{\infty, 2+2\} = 4 \end{aligned}$$

- 4) Find C, not in N' such that D (C) is minimum

Add C to N'

$$D(F) = \min\{D(F), D(C) + c(C, F)\} = \min\{4, 2 + 5\} = 4$$

$$D(G) = \min\{D(G), D(C) + c(C, G)\} = \min\{6, 2 + \infty\} = 6$$

$$D(H) = \min\{D(H), D(C) + c(C, H)\} = \min\{4, 2 + \infty\} = 4$$

- 5) Find F, not in N' such that D (F) is minimum

Add F to N'

$$D(G) = \min\{D(G), D(F) + c(F, G)\} = \min\{6, 4 + 2\} = 6$$

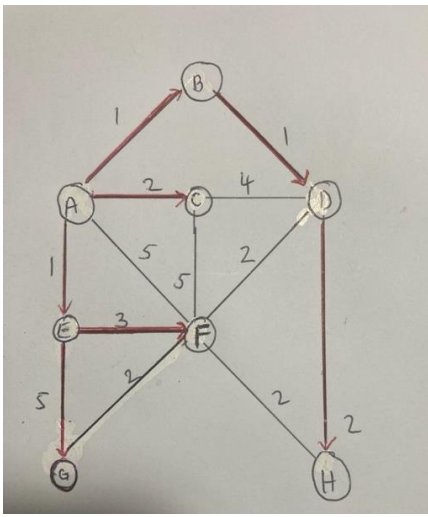
$$D(H) = \min\{D(H), D(F) + c(F, H)\} = \min\{4, 4 + 2\} = 4$$

- 6) Find H, not in N' such that D (H) is minimum

Add H to N'

$$D(G) = \min\{D(G), D(H) + c(H, G)\} = \min\{6, 4 + \infty\} = 6$$

Resulting shortest -path tree from A



2) Distance-vector Algorithm

Step 1

Node A

| Destination | Vector | Hop |
|-------------|----------|------|
| A | 0 | A |
| B | 1 | B |
| C | 2 | C |
| D | ∞ | ---- |
| E | 1 | E |
| F | 5 | F |
| G | ∞ | ---- |
| H | ∞ | ---- |

Node B

| Destination | Vector | Hop |
|-------------|----------|------|
| A | 1 | A |
| B | 0 | B |
| C | ∞ | ---- |
| D | 1 | D |
| E | ∞ | ---- |
| F | ∞ | ---- |
| G | ∞ | ---- |
| H | ∞ | ---- |

Node C

| Destination | Vector | Hop |
|-------------|----------|------|
| A | 2 | A |
| B | ∞ | ---- |
| C | 0 | C |
| D | 4 | D |
| E | ∞ | ---- |
| F | 5 | F |
| G | ∞ | ---- |
| H | ∞ | ---- |

Node D

| Destination | Vector | Hop |
|-------------|----------|------|
| A | ∞ | ---- |
| B | 1 | B |
| C | 4 | C |
| D | 0 | D |
| E | ∞ | ---- |
| F | 2 | F |
| G | ∞ | ---- |
| H | 2 | H |

Node E

| Destination | Vector | Hop |
|-------------|----------|------|
| A | 1 | A |
| B | ∞ | ---- |
| C | ∞ | ---- |
| D | ∞ | ---- |
| E | 0 | E |
| F | 3 | F |
| G | 5 | G |
| H | ∞ | ---- |

Node F

| Destination | Vector | Hop |
|-------------|----------|------|
| A | 5 | A |
| B | ∞ | ---- |
| C | 5 | C |
| D | 2 | D |
| E | 3 | E |
| F | 0 | F |
| G | 2 | G |
| H | 2 | H |

Node G

| Destination | Vector | Hop |
|-------------|----------|------|
| A | ∞ | ---- |
| B | ∞ | ---- |
| C | ∞ | ---- |
| D | ∞ | ---- |
| E | 5 | E |
| F | 2 | F |
| G | 0 | G |
| H | ∞ | ---- |

Node H

| Destination | Vector | Hop |
|-------------|----------|------|
| A | ∞ | ---- |
| B | ∞ | ---- |
| C | ∞ | ---- |
| D | 2 | D |
| E | ∞ | ---- |
| F | 2 | F |
| G | ∞ | ---- |
| H | 0 | H |

Update

Step2

Node A

| Destination | Vector | Hop |
|-------------|--------|-----|
| A | 0 | A |
| B | 1 | B |
| C | 2 | C |
| D | 2 | B |
| E | 1 | E |
| F | 4 | E |
| G | 6 | E |
| H | 7 | F |

A to D

$$D_A(D) = \min \{c(A, B) + D_B(D), c(A, C) + D_C(D), c(A, F) + D_F(D)\} = \min \{1+1, 2+4, 5+2\} = \min \{2, 6, 7\} = 2$$

A to F

$$D_A(F) = \min \{c(A, F) + D_F(F), c(A, C) + D_C(F), c(A, E) + D_E(F)\} = \min \{5+0, 2+5, 1+3\} = \min \{5, 7, 4\} = 4$$

A to G

$$D_A(G) = \min \{c(A, F) + D_F(G), c(A, E) + D_E(G)\} = \min \{5+2, 1+5\} = \min \{7, 6\} = 6$$

A to H

$$D_A(H) = \min \{c(A, F) + D_F(H)\} = \min \{5+2\} = \min \{7\} = 7$$

Node B

| Destination | Vector | Hop |
|-------------|----------|------|
| A | 1 | A |
| B | 0 | B |
| C | 3 | A |
| D | 1 | D |
| E | 2 | A |
| F | 3 | D |
| G | ∞ | ---- |
| H | 3 | D |

B to C

$$D_B(C) = \min \{c(B, A) + D_A(C), c(B, D) + D_D(C)\} = \min \{1+2, 1+4\} = \min \{3, 5\} = 3$$

B to E

$$D_B(E) = \min \{c(B, A) + D_A(E)\} = \min \{1+1\} = \min \{2\} = 2$$

B to F

$$D_B(F) = \min \{c(B, A) + D_A(F), c(B, D) + D_D(F)\} = \min \{1+5, 1+2\} = \min \{6, 3\} = 3$$

B to G

$$D_B(G) = \min \{c(B, A) + D_A(G), c(B, D) + D_D(G)\} = \min \{1+\infty, 1+\infty\} = \min \{\infty, \infty\} = \infty$$

B to H

$$D_B(D) = \min \{c(B, D) + D_D(H)\} = \min \{1+2\} = \min \{3\} = 3$$

Node C

| Destination | Vector | Hop |
|-------------|--------|-----|
| A | 2 | A |
| B | 3 | A |
| C | 0 | C |
| D | 4 | D |
| E | 3 | A |
| F | 5 | F |
| G | 7 | F |
| H | 6 | D |

C to B

$$D_C(B) = \min \{c(C, A) + D_A(B), c(C, D) + D_D(B)\} = \min \{2+1, 4+1\} = \min \{3, 5\} = 3$$

C to D

$$D_C(D) = \min \{c(C, D) + D_D(D), c(C, F) + D_F(D)\} = \min \{4+0, 5+2\} = \min \{4, 7\} = 4$$

C to E

$$D_C(E) = \min \{c(C, A) + D_A(E), c(C, F) + D_F(E)\} = \min \{2+1, 5+3\} = \min \{3, 8\} = 3$$

C to F

$$D_C(F) = \min \{c(C, F) + D_F(F), c(C, A) + D_A(F), c(C, D) + D_D(F)\} = \min \{5+0, 2+5, 4+2\} \\ = \min \{5, 7, 6\} = 5$$

C to G

$$D_C(G) = \min \{c(C, F) + D_F(G)\} = \min \{5+2\} = \min \{7\} = 7$$

C to H

$$D_C(H) = \min \{c(C, D) + D_D(H), c(C, F) + D_F(H)\} = \min \{4+2, 5+2\} = \min \{6, 7\} = 6$$

Node D

| Destination | Vector | Hop |
|-------------|--------|-----|
| A | 2 | B |
| B | 1 | B |
| C | 4 | C |
| D | 0 | D |
| E | 5 | F |
| F | 2 | F |
| G | 4 | F |
| H | 2 | H |

D to A

$$D_D(A) = \min \{c(D, B) + D_B(A), c(D, C) + D_C(A), c(D, F) + D_F(A)\} = \min \{1+1, 4+2, 2+5\} = \min \{2, 6, 7\} = 2$$

D to C

$$D_D(C) = \min \{c(D, C) + D_C(C), c(D, F) + D_F(C)\} = \min \{4+0, 2+5\} = \min \{4, 7\} = 4$$

D to E

$$D_D(E) = \min \{c(D, F) + D_F(E)\} = \min \{2+3\} = \min \{5\} = 5$$

D to F

$$D_D(F) = \min \{c(D, F) + D_F(F), c(D, C) + D_C(F), c(D, H) + D_H(F)\} = \min \{2+0, 4+5, 2+2\} = \min \{2, 9, 4\} = 2$$

D to G

$$D_D(G) = \min \{c(D, F) + D_F(G)\} = \min \{2+2\} = \min \{4\} = 4$$

D to H

$$D_D(H) = \min \{c(D, H) + D_H(H), c(D, F) + D_F(H)\} = \min \{2+0, 2+2\} = \min \{2, 4\} = 2$$

Node E

| Destination | Vector | Hop |
|-------------|--------|-----|
| A | 1 | A |
| B | 2 | A |
| C | 3 | A |
| D | 5 | F |
| E | 0 | E |
| F | 3 | F |
| G | 5 | G |
| H | 5 | F |

E to B

$$D_E(B) = \min \{c(E, A) + D_A(B)\} = \min \{1 + 1\} = \min \{2\} = 2$$

E to C

$$D_E(C) = \min \{c(E, A) + D_A(C), c(E, F) + D_F(C)\} = \min \{1 + 2, 3 + 5\} = \min \{3, 8\} = 3$$

E to D

$$D_E(D) = \min \{c(E, F) + D_F(D)\} = \min \{3 + 2\} = \min \{5\} = 5$$

E to F

$$D_E(F) = \min \{c(E, F) + D_F(F), c(E, A) + D_A(F), c(E, G) + D_G(F)\} = \min \{3 + 0, 1 + 5, 5 + 2\} \\ = \min \{3, 6, 7\} = 3$$

E to G

$$D_E(G) = \min \{c(E, G) + D_G(G), c(E, F) + D_F(G)\} = \min \{5 + 0, 3 + 2\} = 5$$

E to H

$$D_E(H) = \min \{c(E, F) + D_F(H)\} = \min \{3 + 2\} = \min \{5\} = 5$$

Node F

| Destination | Vector | Hop |
|-------------|--------|-----|
| A | 4 | E |
| B | 3 | D |
| C | 5 | C |
| D | 2 | D |
| E | 3 | E |
| F | 0 | F |
| G | 2 | G |
| H | 2 | H |

F to A

$$D_F(A) = \min \{c(F, A) + D_A(A), c(F, C) + D_C(A), c(F, E) + D_E(A)\} = \min \{5+0, 5+2, 3+1\} \\ = \min \{5, 7, 4\} = 4$$

F to B

$$D_F(B) = \min \{c(F, A) + D_A(B), c(F, D) + D_D(B)\} = \min \{5+1, 2+1\} = \min \{6, 3\} = 3$$

F to C

$$D_F(C) = \min \{c(F, C) + D_C(C), c(F, A) + D_A(C), c(F, D) + D_D(C)\} = \min \{5+0, 5+2, 2+4\} \\ = \min \{5, 7, 6\} = 5$$

F to D

$$D_F(D) = \min \{c(F, D) + D_D(D), c(F, C) + D_C(D), c(F, H) + D_H(D)\} = \min \{2+0, 5+4, 2+2\} \\ = \min \{2, 9, 4\} = 2$$

F to E

$$D_F(E) = \min \{c(F, E) + D_E(E), c(F, A) + D_A(E), c(F, G) + D_G(E)\} = \min \{3+0, 5+1, 2+5\} \\ = \min \{3, 6, 7\} = 3$$

F to G

$$D_F(G) = \min \{c(F, G) + D_G(G), c(F, E) + D_E(G)\} = \min \{2+0, 3+5\} = \min \{2, 8\} = 2$$

F to H

$$D_F(H) = \min \{c(F, H) + D_H(H), c(F, D) + D_D(H)\} = \min \{2+0, 2+2\} = \min \{2, 4\} = 2$$

Node G

| Destination | Vector | Hop |
|-------------|----------|------|
| A | 6 | E |
| B | ∞ | ---- |
| C | 7 | F |
| D | 4 | F |
| E | 5 | E |
| F | 2 | F |
| G | 0 | G |
| H | 4 | F |

G to A

$$D_G(A) = \min \{c(G, F) + D_F(A), c(F, E) + D_E(A)\} = \min \{2+5, 5+1\} = \min \{7, 6\} = 6$$

G to B

$$D_G(B) = \min \{c(G, E) + D_E(B), c(G, F) + D_F(B)\} = \min \{5+\infty, 2+\infty\} = \min \{\infty, \infty\} = \infty$$

G to C

$$D_G(C) = \min \{c(G, F) + D_F(C)\} = \min \{2+5\} = \min \{7\} = 7$$

G to D

$$D_G(D) = \min \{c(G, F) + D_F(D)\} = \min \{2+2\} = \min \{4\} = 4$$

G to E

$$D_G(E) = \min \{c(G, E) + D_E(E), c(G, F) + D_F(E)\} = \min \{5+0, 2+3\} = 5$$

G to F

$$D_G(F) = \min \{c(G, F) + D_F(F), c(G, E) + D_E(F)\} = \min \{2+0, 5+3\} = \min \{2, 8\} = 2$$

G to H

$$D_G(H) = \min \{c(G, F) + D_F(H)\} = \min \{2+2\} = \min \{4\} = 4$$

Node H

| Destination | Vector | Hop |
|-------------|--------|-----|
| A | 7 | F |
| B | 3 | D |
| C | 6 | D |
| D | 2 | D |
| E | 5 | F |
| F | 2 | F |
| G | 4 | F |
| H | 0 | H |

H to A

$$D_H(A) = \min \{c(H, F) + D_F(A)\} = \min \{2+5\} = \min \{7\} = 7$$

H to B

$$D_H(B) = \min \{c(H, D) + D_D(B)\} = \min \{2+1\} = \min \{3\} = 3$$

H to C

$$D_H(C) = \min \{c(H, F) + D_F(C), c(H, D) + D_D(C)\} = \min \{2+5, 2+4\} = \min \{7, 6\} = 6$$

H to D

$$D_H(D) = \min \{c(H, D) + D_D(D), c(H, F) + D_F(D)\} = \min \{2+0, 2+2\} = \min \{2, 4\} = 2$$

H to E

$$D_H(E) = \min \{c(H, F) + D_F(E)\} = \min \{2+3\} = \min \{5\} = 5$$

H to F

$$D_H(F) = \min \{c(H, F) + D_F(F), c(H, D) + D_D(F)\} = \min \{2+0, 2+2\} = \min \{2, 4\} = 2$$

H to G

$$D_H(G) = \min \{c(H, F) + D_F(G)\} = \min \{2+2\} = \min \{4\} = 4$$

Update

Step 3

Node A

| Destination | Vector | Hop |
|-------------|--------|-----|
| A | 0 | A |
| B | 1 | B |
| C | 2 | C |
| D | 2 | B |
| E | 1 | E |
| F | 4 | E |
| G | 6 | E |
| H | 4 | B |

A to H

$$D_A(H) = \min \{c(A, B) + D_B(H), c(A, C) + D_C(H), c(A, E) + D_E(H), c(A, F) + D_F(H),\}$$
$$= \min \{1+3, 2+6, 1+5, 5+2\} = \min \{4, 8, 6, 7\} = 4$$

Node B

| Destination | Vector | Hop |
|-------------|--------|-----|
| A | 1 | A |
| B | 0 | B |
| C | 3 | A |
| D | 1 | D |
| E | 2 | A |
| F | 3 | D |
| G | 5 | D |
| H | 3 | D |

B to G

$$D_B(G) = \min \{c(B, A) + D_A(G), c(B, D) + D_D(G)\} = \min \{1+6, 1+4\} = \min \{7, 5\} = 5$$

Node C

| Destination | Vector | Hop |
|-------------|--------|-----|
| A | 2 | A |
| B | 3 | A |
| C | 0 | C |
| D | 4 | D |
| E | 3 | A |
| F | 5 | F |
| G | 7 | F |
| H | 6 | D |

Node D

| Destination | Vector | Hop |
|-------------|--------|----------|
| A | 2 | B |
| B | 1 | B |
| C | 4 | C |
| D | 0 | D |
| E | 3 | B |
| F | 2 | F |
| G | 4 | F |
| H | 2 | H |

D to E

$$D_D(E) = \min \{c(D, B) + D_B(E), c(D, C) + D_C(E), c(D, F) + D_F(E), c(D, H) + D_H(E)\} = \min \{1+2, 4+3, 2+3, 2+5\} = \min \{3, 7, 5, 7\} = 3$$

Node E

| Destination | Vector | Hop |
|-------------|--------|-----|
| A | 1 | A |
| B | 2 | A |
| C | 3 | A |
| D | 3 | A |
| E | 0 | E |
| F | 3 | F |
| G | 5 | G |
| H | 5 | F |

E to D

$D_E(D) = \min \{c(E, A) + D_A(D), c(E, F) + D_F(D), c(E, G) + D_G(D)\} = \min \{1+2, 3+2, 5+4\}$
 $= \min \{3, 5, 9\} = 3$

Node F

| Destination | Vector | Hop |
|-------------|--------|-----|
| A | 4 | E |
| B | 3 | D |
| C | 5 | C |
| D | 2 | D |
| E | 3 | E |
| F | 0 | F |
| G | 2 | G |
| H | 2 | H |

Node G

| Destination | Vector | Hop |
|-------------|--------|-----|
| A | 6 | E |
| B | 5 | F |
| C | 7 | F |
| D | 4 | F |
| E | 5 | E |
| F | 2 | F |
| G | 0 | G |
| H | 4 | F |

G to B

$$D_G(B) = \min \{c(G, E) + D_E(B), c(G, F) + D_F(B)\} = \min \{5+2, 2+3\} = \min \{7, 5\} = 5$$

Node H

| Destination | Vector | Hop |
|-------------|--------|-----|
| A | 4 | D |
| B | 3 | D |
| C | 6 | D |
| D | 2 | D |
| E | 5 | F |
| F | 2 | F |
| G | 4 | F |
| H | 0 | H |

H to A

$$D_H(A) = \min \{c(H, D) + D_D(A), c(H, F) + D_F(A)\} = \min \{2+2, 2+4\} = \min \{4, 6\} = 4$$