## **Introduction to Data Science Topic-3**

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- References:
- M. A. Pathak, Beginning Data Science with R, 2014, Springer-Verlag.
- K.-T. Tsai, Machine Learning for Knowledge Discovery with R: Methodologies for Modeling, Inference, and Prediction, 2021, Chapman and Hall/CRC.
- Evaluation: Homework: 70%, Term Project: 30%
- Office hours: By appointment

## **Course Outline**

#### 10 Topics and 10 Homeworks:

- Introduction of Data Science
- Introduction of R and Python
- Getting Data into R and Python
- Data Visualization
- Exploratory Data Analysis
- Regression (Supervised Learning)
- Classification (Supervised Learning)
- Text Mining
- Clustering (Unsupervised Learning)
- Neural Network and Deep Learning

# Getting Data into R

#### References:

Ch. 3, M. A. Pathak, Beginning Data Science with R, 2014, Springer-Verlag.

https://www.kaggle.com/code/dongdongxzoez/r-topic-3?scriptVersionId=105348041



## **Reading Data – Case Study: Health Survey**

#### Reading Data - Case Study: Health Survey

```
data <- read.csv("survey.csv") #read csv file
## View the first few rows of the data frame
head(data, 10)</pre>
```

##		sex	height	weight	handedness	exercise	smoke
##	1	Female	68	158	Right	Some	Never
##	2	Male	70	256	Left	None	Regul
##	3	Male	NA	204	Right	None	Occas
##	4	Male	63	187	Right	None	Never
##	5	Male	65	168	Right	Some	Never
##	6	Female	68	172	Right	Some	Never
##	7	Male	72	160	Right	Freq	Never
##	8	Female	62	116	Right	Freq	Never
##	9	Male	69	262	Right	Some	Never
##	10	Male	66	189	Right	Some	Never

## **Reading Data – Check Type and Structure**

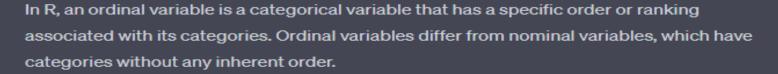
```
#class() function is used to determine the class or data type of an object
class(data)
## [1] "data.frame"
# Check the structure of the data frame
str(data)
## 'data.frame': 237 obs. of 6 variables:
   $ sex : chr "Female" "Male" "Male" "Male" ...
   $ height : int 68 70 NA 63 65 68 72 62 69 66 ...
   $ weight : int 158 256 204 187 168 172 160 116 262 189 ...
## $ handedness: chr "Right" "Left" "Right" "Right" ...
## $ exercise : chr "Some" "None" "None" "None" ...
               : chr "Never" "Regul" "Occas" "Never" ...
## $ smoke
```

## **Cleaning Up Data - Identifying Data Types**

• A factor can be converted into an ordinal variable using the ordered() function.

```
> data$smoke
[1] Never Regul Occas Never Never Never ...
Levels: Heavy Never Occas Regul
> data$smoke = ordered(data$smoke, levels=c('Never', 'Occas', 'Regul', 'Heavy'));data$smoke
[1] Never Regul Occas Never Never Never ...
Levels: Never < Occas < Regul < Heavy</p>
```





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For example, consider a survey that asks respondents to rate their satisfaction with a product on a scale of "Very Dissatisfied," "Dissatisfied," "Neutral," "Satisfied," and "Very Satisfied." In this case, the variable "satisfaction" is ordinal because there is a clear order to the categories from least satisfied to most satisfied. The ordinal nature of this variable allows us to say that "Satisfied" is a higher level of satisfaction than "Dissatisfied," but it doesn't provide information about the exact difference in satisfaction levels.

Ordinal variables are often encountered in social sciences, psychology, and surveys where Likert scales or other ranking systems are used to measure attitudes, opinions, or perceptions. Analyzing ordinal data requires specific statistical methods designed for such data types, as they have characteristics that are distinct from continuous numerical variables. Common statistical analyses for ordinal data include ordinal logistic regression and non-parametric tests like the Mann-Whitney U test and the Kruskal-Wallis test.

In R, you can represent and work with ordinal variables using specialized packages like "ordinal" or by converting categorical variables into ordinal factors. The "ordinal" package provides tools for modeling and analyzing ordinal data. You can create an ordinal variable using the 'ordered()' function in R, specifying the levels and their order.

## Cleaning Up Data -Check for unique

• We use the unique() command to get a list of unique values.

```
##Cleaning up data - Data entry error
unique(data$sex) #get unique value

## [1] "Female" "Male" NA "F" "M"

unique(data$height)

## [1] 68 70 NA 63 65 72 62 69 66 61 75 71 73 67 79 74 64 76 60 77 59
```

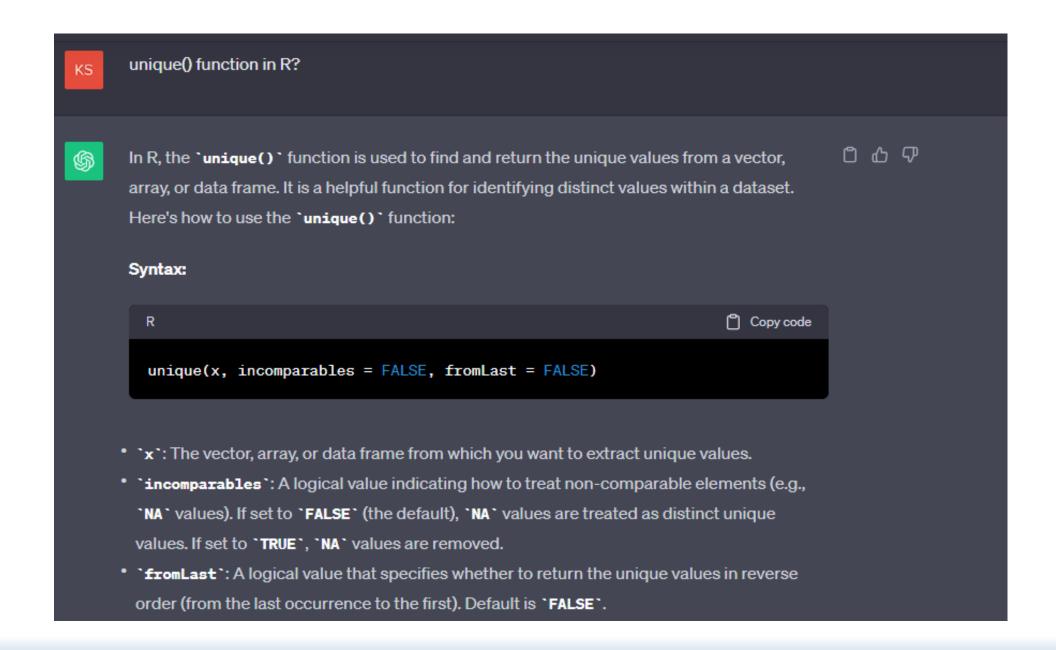
```
##Cleaning up data - Data entry error
unique(data$sex) #get unique value

## [1] "Female" "Male" NA "F" "M"

\[ \frac{1}{1} \]
data$sex[data$sex == 'F'] = 'Female' # replace 'F" to 'Female'
data$sex[data$sex == 'M'] = 'Male' # replace 'M' to 'Male'
unique(data$sex)

[1] "Female" "Male" NA
```

• Replace any occurrences of 'F' and 'M' in the "sex" column with 'Female' and 'Male'. It's a common data preprocessing step used to ensure consistency and clarity in the representation of categories within a dataset. This process can be particularly useful when dealing with categorical variables that might have multiple representations for the same category.



## **Check for Missing Values (NA or NaN)**

```
# Count rows with complete cases (no missing values)
cat("Number of complete rows:", sum(complete.cases(data)), "\n")

## Number of complete rows: 207

# Count rows with missing values
cat("Number of rows with missing values:", sum(!complete.cases(data)), "\n")

## Number of rows with missing values: 30
```

#### how many ways the missing values presents in the datasets



Missing values can be represented in datasets in various ways, depending on how the dataset is structured and how missing data is recorded. Here are some common ways that missing values can be represented in datasets:

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- 1. NA or NaN: In R, missing values are often represented as "NA" (Not Available) for numerical data or "NaN" (Not a Number) for calculations that result in undefined values.
- 2. **Blank Cells**: In spreadsheet software like Microsoft Excel or Google Sheets, missing values are often represented as empty or blank cells.
- Placeholder Values: Some datasets use specific placeholder values to indicate missing data. For example, a dataset might use "-9999" or "9999" to represent missing values.
- Question Marks or Symbols: Missing values can be denoted using question marks ("?") or other symbols like asterisks ("\*") in text-based datasets.
- Special Codes: Datasets may use special codes or labels to indicate missing values. For example, "999" might represent missing data in a dataset where all other values are integers.
- 6. Categorical Labels: In categorical data, missing values might be represented by a specific category label such as "Unknown," "Not Applicable," or "N/A."
- 7. **Dots or Dashes**: Some datasets use dots (".") or dashes ("-") to indicate missing values in text data.
- Data Attributes: Missing values can also be specified using data attributes or metadata,
  where a separate file or information in the dataset's documentation indicates which values
  are missing.

are missing.

- Sparse Data Structures: In cases where the dataset is stored as a sparse data structure,
   missing values may be represented by the absence of a data point in a specific location.
- 10. No Indication: In some cases, missing values are not explicitly indicated in the dataset, and their presence is inferred from the context or analysis.

It's important to be aware of how missing values are represented in a dataset, as the choice of representation can affect data cleaning, imputation, and analysis processes. Additionally, understanding the specific representation of missing data is crucial for handling and interpreting the dataset accurately.

## **Check for total Missing Values (NA or NaN)**

#### Missing Values

```
# Count rows with complete cases (no missing values)
cat("Number of complete rows:", sum(complete.cases(data)), "\n")

## Number of complete rows: 207

# Count rows with missing values
cat("Number of rows with missing values:", sum(!complete.cases(data)), "\n")

## Number of rows with missing values: 30
```

#### Check for the total number of missing values in each column

```
# Count rows with missing values
cat("Number of rows with missing values:", sum(!complete.cases(data$sex)), "\n")

## Number of rows with missing values: 1

# Count rows with missing values
cat("Number of rows with missing values:", sum(!complete.cases(data$height)), "\n")
```



complete.cases() function in R?



In R, the `complete.cases()` function is used to identify rows in a data frame or matrix that the have complete cases, i.e., rows with no missing (NA) values. It returns a logical vector of the same length as the number of rows in the data structure, with each element set to `TRUE` for rows with no missing values and `FALSE` for rows containing at least one missing value.

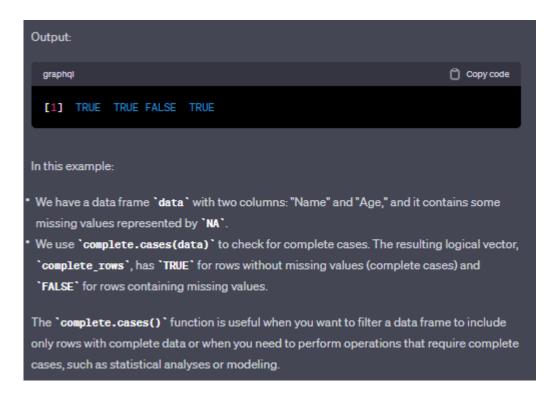
#### Syntax:

```
R Copy code complete.cases(data)
```

\* `data`: The data frame or matrix for which you want to identify complete cases.

#### Example:

```
# Create a data frame with missing values
data <- data.frame(
   Name = c("Alice", "Bob", NA, "David"),
   Age = c(25, 30, NA, 35)
)
# Identify complete cases using complete.cases
complete_rows <- complete.cases(data)
# Print the result
print(complete_rows)</pre>
```



#### Check for the Position of the Missing values in each columns

```
###Cleaning up data - Missing value
which(is.na(data$sex)) #check where is the missing value

## [1] 137

which(is.na(data$height)) #check where is the missing value

## [1] 3 12 15 25 26 29 31 35 58 68 70 81 83 84 90 92 96 108 121
## [20] 133 157 173 179 203 213 217 225 226
```

#### which(is.na()) function in R



In R, you can use the `which(is.na())` combination of functions to identify the indices (positions) of missing (NA) values within a vector, matrix, or data frame.



Here's how it works:

- `is.na(x)` is used to check for missing values within the data structure `x`. It returns a
  logical vector where `TRUE` indicates missing values (NA) and `FALSE` indicates nonmissing values.
- 2. `which()` is used to find the indices (positions) where a condition is `TRUE` within a logical vector. In this case, it's used to find the indices where `is.na()` is `TRUE`.



Deciding whether to replace missing data or leave it as-is in a dataset depends on several factors, including the nature of the data, the analysis you plan to perform, and the potential impact of missing values on your research or application. Here are some considerations to help you decide when to replace missing data and when not to:

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#### When to Replace Missing Data:

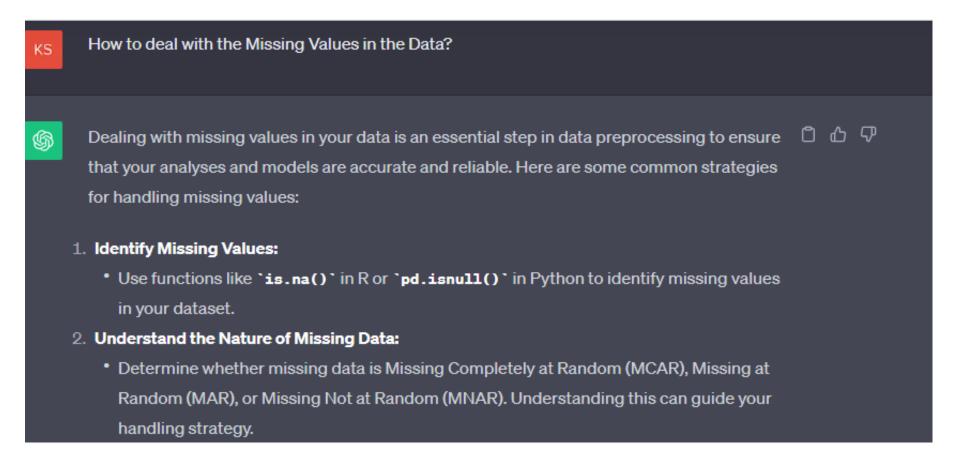
- Missing Completely at Random (MCAR): If the missing data is completely at random and
  the likelihood of data being missing is unrelated to any variables, you may consider
  replacing missing values. In this case, imputation methods like mean imputation or
  regression imputation can be applied.
- 2. **Statistical Analysis**: For some statistical analyses, missing values can cause issues or bias the results. Replacing missing values with appropriate imputed values can help ensure the validity of your analysis.
- Machine Learning: Many machine learning algorithms do not handle missing values well. In such cases, you may need to replace missing data with imputed values to make your data suitable for modeling.
- Preserving Data Integrity: In cases where you want to maintain the structure and integrity
  of your dataset, replacing missing data with imputed values can be preferable.
- Data Visualization: If you plan to create visualizations from your data, dealing with missing data can be challenging. Imputing missing values can make it easier to generate meaningful visualizations.

#### When Not to Replace Missing Data:

- Missing Not at Random (MNAR): If you suspect that the reason for missing data is related
  to the value itself (e.g., people with high income are less likely to disclose their income),
  imputation may introduce bias. In such cases, it might be better to leave the data as-is and
  conduct sensitivity analyses.
- Small Sample Size: If your dataset is already small and imputing missing data would further
  reduce the sample size, it may be better to perform analyses with the available data and
  acknowledge the limitations due to missing values.
- Transparency and Reporting: In some cases, it's essential to report the proportion and nature of missing data as part of your analysis. Replacing missing data without acknowledging it can be misleading.
- Domain Knowledge: Consider whether you have domain knowledge that suggests that
  missing data should not be replaced. In some fields, missing data might be informative and
  should not be imputed.
- Data Collection Costs: If the cost or effort required to collect missing data is prohibitively
  high, it might be more practical to analyze the available data as-is.

Ultimately, the decision to replace missing data should be guided by the goals of your analysis, the characteristics of your dataset, and your understanding of the domain. It's important to carefully consider the potential impact of imputation on your results and to document your data preprocessing steps transparently.

## How to deal with the Missing Values in the Data?



## **Different Types of Data Imputation**

#### 3. Data Imputation:

- Mean/Median Imputation: Replace missing numerical values with the mean or median of the column.
- Mode Imputation: Replace missing categorical values with the mode (most frequent category) of the column.
- Regression Imputation: Predict missing values using regression models based on other variables.
- K-Nearest Neighbors (K-NN) Imputation: Replace missing values with values from the K-nearest neighbors.
- Multiple Imputation: Generate multiple imputed datasets and analyze them separately, then combine results.
- Imputation using Machine Learning: Train a machine learning model to predict missing values.

#### 4. Remove Rows/Columns:

- If missing data is extensive or cannot be reasonably imputed, consider removing entire rows or columns with missing values.
- Be cautious with this approach, as it can lead to loss of valuable information.

#### 5. Imputation with Domain Knowledge:

 Use domain-specific knowledge to impute missing values. For example, if you have historical data, you may know that missing values should be zero or another specific value.

#### 6. Missing Data Indicators:

'Create a binary indicator variable that denotes whether a value is missing or not. This allows you to include missingness as a feature in your analysis.

#### 7. Data Sampling:

 In cases of MCAR or MAR, you can sample data with complete cases for certain analyses to avoid imputation.

#### 8. Advanced Techniques:

 Explore advanced imputation techniques like Random Forest imputation, Bayesian imputation, or deep learning-based imputation methods.

#### 9. Consider the Impact on Analysis:

 Be aware of how your chosen imputation method may impact the results of your analysis or modeling. Some methods can introduce bias.

#### 10. Documentation and Reporting:

 Clearly document how missing data was handled in your analysis. Be transparent in reporting the proportion of missing data and the methods used for imputation or handling.

#### 11. Validation:

 If you impute missing data, validate the imputed values to ensure they make sense in the context of your data.

#### 12. Consultation:

 Consider consulting with domain experts or statisticians, especially when dealing with complex missing data scenarios.

Remember that there is no one-size-fits-all approach to handling missing data, and the choice of strategy should depend on the nature of the data, the research question, and the impact on the analysis or modeling task.

## Replace continuous data with mean

```
df$sex[df$sex == 'F'] = 'Female' # replace 'F" to 'Female'
df$sex[df$sex == 'M'] = 'Male' # replace 'M' to 'Male'
#caculate mean of female height
female.height <- mean(df$height[which(df$sex == 'Female')], na.rm=T)
#caculate mean of male height
male.height <- mean(df$height[which(df$sex == 'Male')], na.rm=T)
#replace NA with mean of female & male height
df$height[which(df$sex == 'Female' & is.na(df$height))] = female.height
df$height[which(df$sex == 'Male' & is.na(df$height))] = male.height
```

# How to deal with the missing value in the categorical dataset?



Handling missing values in categorical data requires different strategies compared to numerical data. Here are several methods for dealing with missing values in categorical data:

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#### 1. Imputation with Mode:

 Replace missing categorical values with the mode (most frequent category) of the respective column. This is a simple and often effective approach.

#### 2. Create a New Category:

 Introduce a new category label, such as "Missing" or "Unknown," to represent missing values. This allows you to retain information about the absence of data.

#### 3. Use Domain Knowledge:

If you have domain expertise or knowledge about the data, you can manually assign
missing values based on context. This is particularly useful when missing values can be
reasonably inferred.

#### 4. Predictive Imputation:

 Train a machine learning model (e.g., decision tree or random forest) to predict missing categorical values based on other features. The model should be trained on rows with complete data.

#### 5. Multiple Imputation:

 Perform multiple imputation, where you create multiple imputed datasets with different imputed values for missing categories. This approach captures uncertainty associated with imputation.

#### 6. Hot Deck Imputation:

 Match each record with missing data to a similar record with complete data based on other attributes. Replace the missing value with the corresponding category from the matched record.

#### 7. Weighted Imputation:

Assign weights to categories based on their frequency in the dataset. Use these weights
to randomly sample and impute missing values. This approach preserves the
distribution of existing data.

#### 8. K-Nearest Neighbors (K-NN) Imputation:

 Use the K-NN algorithm to find similar data points with complete information and impute missing values based on the majority category in their neighborhood.

#### 9. Regression Imputation:

 Fit a regression model where the categorical variable with missing data is the dependent variable, and other variables serve as predictors. Predict missing categories based on the model's coefficients.

#### 10. Consider a Separate Category:

 In some cases, it may be appropriate to consider missing data as a separate category if it carries meaningful information.

#### 11. Missing Data Indicator:

 Create a binary indicator variable that flags whether a value in the categorical column is missing or not. This can be useful if missingness carries information.

#### 12. Remove Rows:

If missing data is extensive and cannot be reasonably imputed, consider removing rows
with missing categorical values. Be cautious with this approach, as it may lead to a
significant loss of data.

#### 13. Consult with Domain Experts:

 Collaborate with experts in the domain relevant to your data to make informed decisions about handling missing values.

The choice of method depends on the nature of your data, the reason for missingness, and the specific requirements of your analysis or modeling task. It's essential to document how you handled missing categorical values in your data preprocessing, as this information is critical for reproducibility and transparency.

## Replace categorical data with bootstrap

```
bootstrap <- function(series){</pre>
    tb <- table(series[complete.cases(series)])
    prob <- tb / sum(tb)</pre>
    smpl <- sample(names(tb), prob=prob, size=sum(!complete.cases(series)))</pre>
    series[!complete.cases(series)] <- smpl</pre>
    return (series)
df$smoke <- ordered(df$smoke, levels=c('Never', 'Occas', 'Regul', 'Heavy'))</pre>
df$smoke[!complete.cases(df)] <- names(which.max(table(df$smoke)))</pre>
df$exercise <- ordered(df$smoke, levels=c('None', 'Some', 'Freq'))</pre>
df$exercise[!complete.cases(df)] <- names(which.max(table(df$exercise)))</pre>
df$handedness <- bootstrap(df$handedness)</pre>
df$sex <- bootstrap(df$sex)
```

## **Summary Data**

```
In [7]:
       cat("Number of non NA row:", dim(df[complete.cases(df),])[1])
       cat("\nNumberof non NA row:", dim(df[!complete.cases(df),])[1])
       Number of non NA row: 237
       Number of non NA row: 0
In [8]:
       summary(df)
                             height
                                           weight
                                                       handedness
            sex
        Length:237
                         Min. :59.00
                                       Min. : 0.0 Length:237
        Class :character
                                                      Class :character
                        Median :67.00
                                       Median :169.0
                                                      Mode :character
        Mode :character
```

# Homework 3 (submitted to e3.nycu.edu.tw before Oct 11, 2023)

- Use R, Python, and suitable computer packages to analyze the data set with missing data (NA) that you select.
- Try to solve the missing value or another data error issue.
- Use Different Types of Data Imputation Methods for handling missing data in your datasets.
- Explain the results you obtain
- Discuss possible problems you plan to investigate for future studies

#### Possible sources of open datasets:

- UCI Machine Learning Repository
  - (<a href="https://archive.ics.uci.edu/ml/datasets.php">https://archive.ics.uci.edu/ml/datasets.php</a>)
- Kaggle Datasets (<a href="https://www.kaggle.com/datasets">https://www.kaggle.com/datasets</a>)



# Getting Data into Python

References:

Ch. 3, M. A. Pathak, Beginning Data Science with R, 2014, Springer-Verlag.



## Import dependencies

```
import pandas as pd
import numpy as np
from colorama import Fore, Back, Style
import matplotlib.pyplot as plt
import warnings
warnings.filterwarnings('ignore')
from sklearn.model_selection import train_test_split, KFold
from sklearn.linear_model import LinearRegression
from sklearn.preprocessing import OneHotEncoder, OrdinalEncoder
from sklearn.compose import ColumnTransformer
from sklearn.metrics import mean_squared_error
from sklearn.preprocessing import FunctionTransformer
```

## **Reading Data – House Prices Prediction**

```
df = pd.read_csv('../input/house-prices-advanced-regression-techniques/train.csv')
model = LinearRegression()
df.head(6)
```

	ld	MSSubClass	MSZoning	LotFrontage	LotArea	Street	Alley	LotShape	LandContour	Utilities	 PoolArea	PoolQC	Fence	Mi
0	1	60	RL	65.0	8450	Pave	NaN	Reg	LvI	AllPub	 0	NaN	NaN	
1	2	20	RL	80.0	9600	Pave	NaN	Reg	LvI	AllPub	 0	NaN	NaN	
2	3	60	RL	68.0	11250	Pave	NaN	IR1	LvI	AllPub	 0	NaN	NaN	
3	4	70	RL	60.0	9550	Pave	NaN	IR1	LvI	AllPub	 0	NaN	NaN	
4	5	60	RL	84.0	14260	Pave	NaN	IR1	LvI	AllPub	 0	NaN	NaN	
5	6	50	RL	85.0	14115	Pave	NaN	IR1	LvI	AllPub	 0	NaN	MnPrv	

6 rows x 81 columns

### Fill continuous data with custom function

```
def fillMedian(data):
    data = data.select_dtypes(exclude=['object'])
    columns = list(data.columns)
    for col in columns:
        data[col].fillna(value=data[col].median(), inplace=True)
    return data
```

```
def categorical_transformer(data):
    data = data.select_dtypes(exclude=['int64','float64'])
   columns = data.columns
   one_hot_cols = []
    label_cols = []
    for col in columns:
        data[col] = data[col].fillna(data[col].mode()[0])
        if len(data[col].unique()) < 10:</pre>
            one_hot_cols.append(col)
        else:
            label_cols.append(col)
    label_transformer = OrdinalEncoder(handle_unknown='use_encoded_value', unknown_value=-1)
    one_hot_transformer = OneHotEncoder(handle_unknown="ignore")
    preprocessor = ColumnTransformer(
        transformers=[
            ("num", label_transformer, label_cols),
            ("cat", one_hot_transformer, one_hot_cols),
    _data = preprocessor.fit_transform(data)
    return _data
```

## **Fit and Transform**

```
X = df.drop(['SalePrice'], axis=1)
y = df.SalePrice
numeric_transformer = FunctionTransformer(fillMedian)
categorical_transformer = FunctionTransformer(categorical_transformer)
columns = X.columns
preprocessor = ColumnTransformer(
    transformers=[
        ("num", numeric_transformer, columns),
        ("cat", categorical_transformer, columns),
_X = preprocessor.fit_transform(X)
```

## **Data Split**

```
X_train, X_valid, y_train, y_valid = train_test_split(_X, y, test_size = 0.2, random_state=42)
 model.fit(X_train, y_train)
  pred = model.predict(X_valid)
  grid = np.linspace(0, 500000, 1460)
  plt.scatter(pred, y_valid)
  plt.plot(grid, grid, "b-", c='red')
[<matplotlib.lines.Line2D at 0x7feaaa013c50>]
700000
                                                     print(_X.shape)
                                                                                                               Data
600000
                                                     np.isnan(_X).sum()
500000
400000
                                                  (1460, 236)
300000
200000
                                                                                                      Training
                                                                                                                               Test
100000
           100000 200000 300000 400000 500000
```

## **Scoring MSE**

```
def scoring_mse(X_train, X_valid, y_train, y_valid, model):
    model.fit(X_train, y_train)
    preds = model.predict(X_valid)
    return mean_squared_error(y_valid, preds, squared=False)
scoring_mse(X_train, X_valid, y_train, y_valid, LinearRegression())
```

30754.592815992128

```
%%time
                                                                                                               Data
 kf = KFold(n_splits=5, shuffle=True, random_state=1)
 params = {}
                                                                           Validate
                                                                                              Train
                                                                                                                                Train
                                                                                                               Train
 score_list = []
 for fold, (idx_train, idx_valid) in enumerate(kf.split(_X)):
                                                                                             Validate
                                                                                                                                Train
                                                                             Train
                                                                                                               Train
      X_{train} = X[idx_{train}]
                                                                             Train
                                                                                              Train
                                                                                                              Validate
                                                                                                                                Train
      y_train = y[idx_train]
                                                                                                               Train
                                                                            Train
                                                                                              Train
                                                                                                                               Validate
      model = LinearRegression(**params)
                                                                            Train
                                                                                              Train
                                                                                                               Train
                                                                                                                                Train
      model.fit(X_train, y_train)
      del X_train, y_train
      X_{valid} = X[idx_{valid}]
                                                                        https://medium.com/@kn12/k-fold-cross-validation-using-python-code-e8e01039dc6
      y_valid = y[idx_valid]
      y_valid_pred = model.predict(X_valid)
      rmse = mean_squared_error(y_valid, y_valid_pred, squared=False)
      del X_valid, y_valid
      print(f"Fold {fold}: rmse = {rmse:.5f}")
      score_list.append(rmse)
 result_df = pd.DataFrame(score_list, columns=['rmse'])
 print(f"{Fore.GREEN}{Style.BRIGHT}Average mse = {result_df.rmse.mean():.5f}")
Fold 0: rmse = 32107.33766
Fold 1: rmse = 57351.50794
Fold 2: rmse = 26066.51942
Fold 3: rmse = 44514.71104
Fold 4: rmse = 22062.43021
Average mse = 36420.50125
CPU times: user 575 ms, sys: 386 ms, total: 961 ms
```

Wall time: 248 ms

Train

**Train** 

Train

Train

Validate