Classical Semiconductors (Transistors) Advantages & Disadvantages

Semiconductor:

- Conducts electric current
 - Better than insulators
 - Not as good as conductors

Si:

- 4 valence electrons
- · Forms Tetrahedral crystal

Doping:

- n-type
- p-type

To make n-type semiconductor, you take pure silicon and inject a small amount of an element with 5 valence electrons, like Phosphorous:

- similar enough to silicon that it can fit into the lattice
- the semiconductor has more mobile charges and so it conducts current better

In p-type doping:

- p-type stands for "positive"
- · element with only three valence electrons is added to the lattice
 - o Ex. Boron
- · Create a "hole":
 - a place where there should be an electron, but there isn't
 - o increases the conductivity of the silicon because electrons can move into it
 - lack of an electron
 - acts as a positive charge

Now it's a common misconception that n-type semiconductors are negatively charged and p-type semiconductors are positively charged.

That's not true, they are both neutral because they have the same number of electrons and protons inside them.

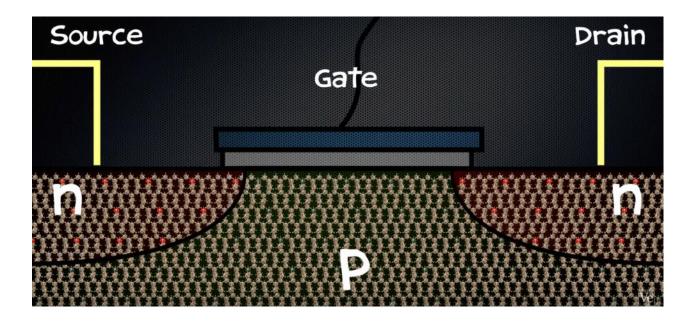
"n" and "p":

Only signs of charge that can move within them

in n-type, it's negative electrons which can move in p-type it's a positive hole that moves.

Transistor:

- made with both n-type and p-type semiconductors
- A common configuration has n on the ends with p in the middle.
- Just like a switch a transistor has an electrical contact at each end and these are called the source and the drain.
- instead of a mechanical switch, there is a third electrical contact called the gate, which is insulated from the semiconductor by an oxide layer.



When a transistor is made:

- n and p-types don't keep to themselves -- electrons actually diffuse from the n-type
 - o where there are more of them into the p-type to fill the holes.

Depletion layer:

- Depleted: Charges that can move
 - o no more free electrons in the n-type
 - Because they've filled the holes in the p-type
- this makes the p-type negative thanks to the added electrons
 - o because the p-type will now repel any electrons that try to come across from the n-type
- the depletion layer actually acts as a barrier
 - preventing the flow of electric current through the transistor
- the transistor is off, it's like an open switch, it's in the zero state.
- To turn it on, you have to apply a small positive voltage to the gate.
 - It actually shrinks the depletion layer so that electrons can move through and form a conducting channel.
 - So the transistor is now on, it's in the one state.
 exploiting the properties of a crystal we've been able to create a switch that doesn't have any moving parts, that can be turned on and off very quickly just with a voltage, and most importantly it can be made tiny.
 - Transistors today are only about 22nm wide;
 - means they are only about 50 atoms across.
- But to keep up with Moore's law, they're going to have to keep getting smaller.
 - Moore's Law states that every two years the number of transistors on a chip should double.
 - And there is a limit, as those terminals get closer and closer together, quantum effects become more significant and electrons can actually tunnel from one side to the other.
 - make a barrier high enough to stop them from flowing
 - real problem for the future of transistors, but we'll probably only face that another ten years down the track.

Math Formulas

Monday, October 9, 2023

Newton's Law of Cooling

$$\frac{dT}{dt} = K[M(t) - T(t)]$$

Trigonometric and Logarithmic Equations

$$\sin x = \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{(2n+1)!} = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \dots$$

$$\cos x = \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n}}{(2n)!} = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots$$

$$\ln(1+x) = \sum_{n=1}^{\infty} (-1)^{n-1} \frac{x^n}{n} = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \cdots$$

$$\mathbf{r}(t) = 8t^3 \mathbf{i} + 4t^3 \mathbf{j} + 6t^3 \mathbf{k}$$

$$\mathbf{r}'(t) = (3 \cdot 8t^2) \mathbf{i} + (3 \cdot 4t^2) \mathbf{j} + (3 \cdot 6t^2) \mathbf{k}$$
$$= 24t^2 \mathbf{i} + 12t^2 \mathbf{j} + 18t^2 \mathbf{k}$$

$$\mathbf{r}''(t) = (2 \cdot 24t) \,\mathbf{i} + (2 \cdot 12t) \,\mathbf{j} + (2 \cdot 18t) \,\mathbf{k}$$

= 48t $\mathbf{i} + 24t \,\mathbf{j} + 36t \,\mathbf{k}$

$$\mathbf{r}'''(t) = 48 \,\mathbf{i} + 24 \,\mathbf{j} + 36 \,\mathbf{k}$$

Tangent Vector

$$\frac{ds}{dt} = \left| \mathbf{r}'(t) \right| = \sqrt{(24t^2)^2 + (12t^2)^2 + (18t^2)^2} = 6\sqrt{29}t^2$$

Tangent Unit Vector

$$\mathbf{T}(t) = \frac{\mathbf{r}'(t)}{|\mathbf{r}'(t)|} = \frac{48 \mathbf{i} + 24 \mathbf{j} + 36 \mathbf{k}}{6\sqrt{29}t^2} = \frac{8}{\sqrt{29}} \mathbf{i} + \frac{4}{\sqrt{29}} \mathbf{j} + \frac{6}{\sqrt{29}} \mathbf{k}$$

Arc Length

If a = 1 and b = 2:

$$L = \int_{a}^{b} |\mathbf{r}'(t)| \, dt = \int_{1}^{2} \left(\frac{8}{\sqrt{29}} \mathbf{i} + \frac{4}{\sqrt{29}} \mathbf{j} + \frac{6}{\sqrt{29}} \mathbf{k} \right) dt = \left| \frac{8}{\sqrt{29}} \mathbf{i} + \frac{4}{\sqrt{29}} \mathbf{j} + \frac{6}{\sqrt{29}} \mathbf{k} \right|_{1}^{2} = \frac{8}{\sqrt{29}} \mathbf{i} + \frac{4}{\sqrt{29}} \mathbf{j} + \frac{6}{\sqrt{29}} \mathbf{k}$$

Normal Vectors

$$\mathbf{N}(t) = \frac{\mathbf{T}'(t)}{|\mathbf{T}'(t)|} = \frac{\frac{8}{\sqrt{29}}\mathbf{i} + \frac{4}{\sqrt{29}}\mathbf{j} + \frac{6}{\sqrt{29}}\mathbf{k}}{\sqrt{\left(\frac{8}{\sqrt{29}}\right)^2 + \left(\frac{4}{\sqrt{29}}\right)^2 + \left(\frac{6}{\sqrt{29}}\right)^2}} = \frac{8}{\sqrt{29}}\mathbf{i} + \frac{4}{\sqrt{29}}\mathbf{j} + \frac{6}{\sqrt{29}}\mathbf{k}$$

Binormal Vectors

$$\mathbf{B}(t) = \mathbf{T}(t) \times \mathbf{N}(t)$$

$$\frac{dT}{dt} = K[M(t) - T(t)]$$

$$\sin x = \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{(2n+1)!} = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} + \cdots$$

$$\cos x = \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n}}{(2n)!} = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \cdots$$

$$\ln(1+x) = \sum_{n=1}^{\infty} (-1)^{n-1} \frac{x^n}{n} = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \cdots$$

Curvature

$$\kappa = \frac{\left| \mathbf{r}'(t) \times \mathbf{r}''(t) \right|}{|\mathbf{r}'(t)|^3}$$
 where T: Tangent Unit Vector

Torsion

$$\tau = \frac{\left[\mathbf{r}'(t) \times \mathbf{r}''(t)\right] \cdot \mathbf{r}'''(t)}{\left|\mathbf{r}'(t) \times \mathbf{r}''(t)\right|^{2}}$$

Line Integrals

$$W = \int_{a}^{b} \mathbf{F}(\mathbf{r}(t)) \cdot \mathbf{r}'(t) dt = \int_{a}^{b} m \mathbf{r}''(t) \cdot \mathbf{r}'(t) dt$$
where $ds = |\mathbf{r}'(t)| dt$

Green's Theorem

$$\int_{C} P dx + Q dy = \iint_{D} \left(\frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y} \right) dA$$

$$\operatorname{curl} \mathbf{F} = \mathbf{\nabla} \times \mathbf{F} = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ P & Q & R \end{vmatrix} = \left(\frac{\partial R}{\partial y} - \frac{\partial Q}{\partial z} \right) \mathbf{i} + \left(\frac{\partial P}{\partial z} - \frac{\partial R}{\partial x} \right) \mathbf{j} + \left(\frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y} \right) \mathbf{k}$$

https://spacemath.gsfc.nasa.gov/Calculus/10Page120.pdf

Problem 2 – The [definite] integral of the dose rate formula D(T) with respect to time is the accumulated total dose.

A) Perform this integration for one 10-hour orbit of the spacecraft assuming that the total dose over the time interval T: [0h, 10h] is equal to twice the dose rate over the time interval T: [0h, 5h]. Answer:

Total Dose =
$$120 \int_{0}^{5} \left(\frac{7+3T}{25}\right)^{2} dT$$

= $\frac{120}{625} \int_{0}^{5} (49+42T+9T^{2}) dT$
= $\frac{120}{625} \left(49T+21T^{2}+3T^{3}\right)_{0}^{5}$
= $\frac{120}{625} \left(49x5+21x25+3x125\right)$ = 220 milliGrays = **0.22 Grays/orbit**.

https://spacemath.gsfc.nasa.gov/Calculus/10Page113.pdf

Problem 2 –What is the total mass in tons of impacting objects each year, over the surface of Earth, in the mass range from 1 gram to 10^{20} grams? (Use π = 3.14 and assume a spherical Earth with a radius of 6,378 km).

Answer: The total mass is the area under the curve: Mass = N(m) dm

$$M = \int_{1}^{10^{20}} 0.025 m^{-0.9} dm$$

$$=0.025\frac{1}{0.1}[(10^{20})^{0.1}-(1)^{0.1}]$$

= 0.025(10)(100-1)

= 24.75 grams/km²/year

Area of Earth =
$$4\pi (6378)^2$$
 = $5.1 \times 10^8 \text{ km}^2$

So the total meteoritic mass per year is

$$24.75 \text{ grams/km}^2 \times 5.1 \times 10^8 \text{ km}^2 = 1.26 \times 10^{10} \text{ grams}$$

or $1.26 \times 10^7 \text{ kg}$

or 12,600 tons.

https://spacemath.gsfc.nasa.gov/Calculus/10Page121.pdf

| Θ in degrees | T: Time (hrs) | R in Re | G in Grays/hr |
|--------------|---------------|---------|---------------|
| 0 | 0.0 | 1.0 | 0.08 |
| 40 | 0.5 | 2.1 | 0.23 |
| 80 | 1.2 | 3.4 | 1.5 |
| 120 | 2.3 | 4.0 | 2.4 |
| 160 | 3.7 | 4.3 | 2.4 |
| 200 | 5.3 | 4.3 | 2.4 |
| 240 | 6.7 | 4.1 | 2.4 |
| 280 | 7.8 | 3.4 | 1.6 |
| 320 | 8.5 | 2.1 | 0.19 |

