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# Advanced Normalization Tools (ANTs)

Release 2.x

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## Abstract

We provide examples and highlights of Advanced Normalization Tools (ANTs), versions 2.x, that address practical problems in real data.

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## 1 Introduction

This update to ANTs documentation was initiated April 29, 2014. *This document does not cover all of ANTs functionality — but summarizes the most frequently used components.* Originally, the ANTs framework provided open-source functionality for deformable image registration with small or large deformations, as shown in figure 1. Independent evaluation of the 0.0 version of ANTs software, applied to “control” data, placed the toolkit as a top performer amongst 14 methods [25]. Developer evaluation showed stronger differences with other methodology in neurodegenerative neuroimaging data, where large deformation is required [10]. ANTs has since grown to include N4 bias correction [35], additional evaluation of multiple modalities and organ systems [34, 36, 27], univariate or multivariate image segmentation [18, 38], tighter integration with the Insight ToolKit [33, ?], a well-evaluated cortical thickness pipeline [?] and, more recently, visualization tools and integration with R[?]. ANTs serves as both a core library for further algorithm development and also as a command-line application-oriented toolkit. ANTs also has a permissive software license that allows it to be employed freely by industry [30]. ANTs enables diffeomorphic normalization with a variety of transformation models, optimal template construction, multiple types of diffeomorphisms, multivariate similarity metrics, diffusion tensor processing and warping, image segmentation with and without priors and measurement of cortical thickness from probabilistic segmentations. The normalization tools, alone, provide a near limitless range of functionality and allow the user to develop customized objective functions. Objective functions in ANTs are of the form:

$$\text{Deformation Cost} + \text{Data Terms},$$

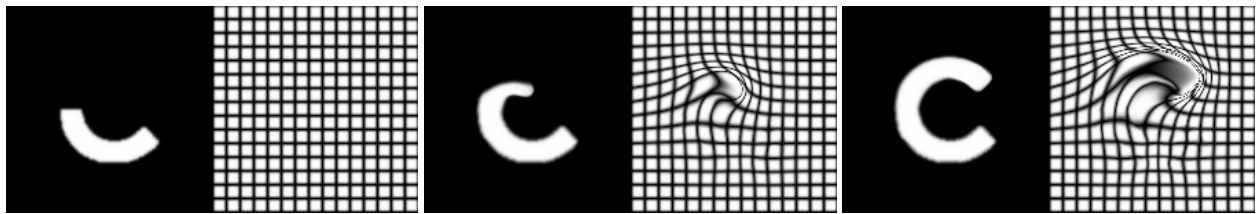


Figure 1: The original goal of ANTs was to develop public, open source large deformation image registration. This is a classic example showing the progress of deforming a half C to a full C along a geodesic diffeomorphism. The deforming grid accompanies each deformed image. See <http://stnava.github.io/C/> for example data and code.

and the command line reflects this balance of two terms. As mentioned above, the data term may combine multiple different measures of similarity that are optimized in parallel, for instance, image similarity and landmark terms. This document seeks to provide a practical overview of basic functionality and some of the common use cases that users seek. Additional information is available online – see <http://stnava.github.io/ANTs/>. For compilation details, see: <https://brianavants.wordpress.com/2012/04/13/updated-ants-compile-instructions-april-12-2012/>. The most important core C++-based ANTs programs are: `antsRegistration`, `antsApplyTransforms`, `Atropos` for segmentation, `N4BiasFieldCorrection` for inhomogeneity correction, `KellyKapowski` for estimating thickness, `ImageMath` image processing utilities and, finally, `sccan` for sparse dimensionality reduction. There are many other programs which are listed in <https://github.com/stnava/ANTs/tree/master/Examples>. The scripts in ANTs wrap the core programs and are in <https://github.com/stnava/ANTs/tree/master/Scripts>. Perhaps the most important are `antsCorticalThickness.sh` as a wrapper of several sub-programs that support our cortical thickness pipeline [?], `antsMultivariateTemplateConstruction2.sh` for template construction and `antsRegistrationSyN.sh` as a basic interface to a few commonly used registration approaches.<sup>1</sup>

## 1.1 Structure of this document and its examples

This document is generated with  $\text{\LaTeX}$  and is version controlled at <https://github.com/stnava/ANTsDoc>. The examples, here, have data and example scripts stored at dedicated github repositories, to which we will refer. Other (simpler) examples will use data and scripts that are stored in the ANTsDoc git repository. These scripts are (loosely speaking) tested and should serve as reproducible examples for the reader to try. All data and code is available via ANTs-related repositories.

## 1.2 Example 1: Quick SyN

If you want a decent, fast registration you might run something like this:

```
1 antsRegistrationSyNQuick.sh -d 2 -f r16slice.nii.gz -m r64slice.nii.gz -o output$0
2 rm output$0* # cleanup
```

The `-d` option denotes image dimensionality, `-f` option denotes the “fixed” image and the `-m` option denotes the “moving” image. The moving image will be deformed to match the fixed image. The inverse of these maps deform the fixed to the moving image. Output is determined by `-o` where the output will be named with prefix=`outputEx1.sh` (the word `output` concatenated with the name of the Example 1 script) and include

<sup>1</sup>This document is a work in progress. Please check for updates with each release.

a prefix0GenericAffine.mat (the low-dimensional affine transform which may be inverted numerically), the prefix1Warp.nii.gz (the diffeomorphic transformation pulling the affine transformed moving image toward the fixed image), and the prefix1InverseWarp.nii.gz (the inverse diffeomorphic transformation pulling the fixed image toward the affine transformed moving image). The caveats for this “canned” approach include: 1. registration performance can always be improved by using prior knowledge [40]; 2. there are many assumptions about the data embedded in the above call and they may not be appropriate for whatever problem is at hand; 3. you must have some facility with the command line to run a shell script. It is, in general, better to understand a little bit about image registration rather than running methods blindly. To aid readers in this, we have two options: 1. github issues <https://github.com/stnava/ANTs/issues>; 2. sourceforge discussion or help sites <http://sourceforge.net/p/advants/discussion/>. Feel free to use either to ask clarifying questions. We note that many issues have been discussed previously and you might find answers by searching the archives.

### 1.3 The antsRegistration Executable

The `antsRegistration` program itself is the central program encapsulating normalization/registration functionality. Its main output is an affine transform file and a deformation field, potentially with inverse. Options allow the user to navigate the similarity and transformations that are available. `antsRegistration` allows multiple similarity and optimization criteria as options. The program is wrapped in `antsRegistrationSyN.sh` for normalization with “out of the box” parameters and in `antsMultivariateTemplateConstruction2.sh` for computationally distributed optimal (multivariate) template construction.

#### Initializing `antsRegistration`

You can use the `-r` option in `antsRegistration` to initialize a registration with an ITK .mat format transformation matrix, with a deformable mapping or with a center of mass alignment. See the scripts for examples. The output transformation will include the initial transformation. **FIXME need to check this.**

### 1.4 The antsApplyTransforms Executable

The `antsApplyTransforms` program applies ANTs mappings to images including scalars, tensors, time-series and vector images. It also composes transforms together and is able to compute inverses of low-dimensional (affine, rigid) maps. `antsApplyTransformsToPoints` similarly works on point sets (see <http://stnava.github.io/chicken/> for details). One may apply an arbitrarily long series of transformations through these programs. Thus, they enable one to compose a series of affine and deformable mappings and/or their inverses. One may therefore avoid repeated interpolations of a single image. Several different interpolation options are available and multiple image types may be transformed including: tensors, vectors, timeseries and  $d$ -dimensional scalar images where  $d = 2, 3, 4$ .

### 1.5 Using `antsApplyTransforms` or `antsApplyTransformsToPoints`

For example: to apply the transform to the moving image and the inverse to the fixed image:

```
1 ln -s r16slice.nii.gz B.nii.gz
2 ln -s r64slice.nii.gz A.nii.gz
3 antsRegistrationSyNQuick.sh -d 2 -f B.nii.gz -m A.nii.gz -o RegA2B
```

```

4 antsApplyTransforms -d 2 -i A.nii.gz -o ADeformed.nii.gz -r B.nii.gz -t RegA2B1Warp.
  nii.gz -t RegA2B0GenericAffine.mat
5 antsApplyTransforms -d 2 -i B.nii.gz -o BDeformed.nii.gz -r A.nii.gz -t [
  RegA2B0GenericAffine.mat,1] -t RegA2B1InverseWarp.nii.gz
6 rm RegA2B* ADeformed.nii.gz BDeformed.nii.gz A.nii.gz B.nii.gz # cleanup

```

The numbers of the transformations (here, 0 and 1 because there is only a deformation and affine mapping) relate to the order in which the transforms are computed, during optimization, and also the order in which they should be applied. There is reasonably complete discussion of this framework in [?].

The usage of `antsApplyTransformsToPoints` is nearly identical. *However*, it is critical to recognize that transforms that are one-to-one and onto in image space may not be in point space. Therefore, points are transformed by the inverses of the transformation that is applied to images. This is discussed in several places in the image registration literature but we first discussed this in [16].

## 1.6 I/O Data Formats In ANTs

ANTs supports 2D, 3D and, in some cases, 4D images. Since ANTs is implemented in concert with the Insight ToolKit (ITK) <http://www.itk.org/>, it is able to read and write the popular data formats supported through ITK. ANTs also uses the ITK view of world-coordinates which can be confusing, at times, when one is mixing software. There is much discussion of this on the web and in ANTs discussion sites/issues. Whatever is relevant for ITK world coordinates is relevant to ANTs as these two software systems agree, in their entirety, about what the voxel to physical space coordinate mapping should be. There are four basic types of data for ANTs.

### Image Volumes

ANTs supports 2D, 3D, 4D images, including

- Nifti (.nii, .nii.gz)
- Analyze (.hdr + .img / .img.gz)
- MetaImage (.mha)
- Other formats through `itk::ImageFileWriter` / `itk::ImageFileReader` such as jpg, tiff, etc. See ITK documentation.

### Affine Transformation File

ANTs uses the `itk::TransformFileReader` / `itk::TransformFileWriter` to handle affine transformation files. These are Matlab like .mat files recording the matrix and offset for the low-dimensional transforms: translation, rigid, affine. The ordering of a matrix transformations parameters breaks down like this: if parameters are,  $a\ b\ c\ d\ e\ f\ g\ h\ i\ j\ k\ l$ , with origin (or FixedParameters),  $M\ N\ O$ , then the matrix components (rotation, scaling, shearing all composed together) are:

$$\begin{matrix} a & b & c \\ d & e & f \\ g & h & i \end{matrix}$$

followed by  $jkl$  (the translation) where  $LMN$  is the center of rotation.

#### Deformation field file

ANTs writes the deformation field using image formats that can store multi-dimensional pixels, usually a nifti-image. The values of each pixel are the displacements in physical space. So,  $y = u(x) + x$  where  $u(x)$  is the displacement at  $x$ .

Labeled point sets—*Currently not supported by antsRegistration, only by old ANTS*

There are three formats supported

- Labeled point sets are saved as an image volume with the intensity = 1,2,3 for label = 1,2,3. For example, figure 16 shows 2D images representing a 3-class labeled point set.
- CSV Format. In this simple format, the point sets are saved as a text csv file. See the chicken example for details.

## 1.7 The ImageMath executable

This is a multi-purpose program that has the following syntax: `ImageMath ImageDimension outputfilename Operation InputFileName parameters ...` Most basic scalar image operations – and some tensor operations – may be performed with this program. Some operations output text files, some output images and some output only to the terminal. ImageMath allows one to multiply images together (m), to negate images (Neg), to take an image to a power (pow), to test the invertibility of transformations (InvId), to compute the fractional anisotropy of an image (TensorFA) and to compute the gradient or laplacian of an image (Gradient, Laplacian). Many other operations are available. Like all other ANTs programs, one may call ImageMath from the command line to see all of its options. ImageMath is used heavily in ANTs scripts.

## 1.8 ANTs Scripts

The ANTs/Scripts directory contains (hopefully) user-friendly wrappings of ANTs tools that enable higher-level error checking and combinations of basic ANTs functions. These scripts are called as `bash antsscriptname.sh` and provide usage when called from the command line. For instance, try `bash antsRegistrationSyN.sh`. Additionally, if you run ants in tcsh shells, you will need to call it as follows (using antsRegistration as an example):

```
antsRegistration -d 2 -m CC\[r16slice.nii,r64slice.nii,1,2\] ...
```

instead of

```
antsRegistration -d 2 -m CC[r16slice.nii,r64slice.nii,1,2 ] ...
```

because tcsh does not interpret the brackets as intended. Using the bash shell script interface also avoids this. The key change involves using the slash to force tcsh to interpret the bracket literally.

## 2 Image registration with ANTs

There are two general applications of image registration. The first application is transforming labeled data from a template image space into an individual space. This strategy is important when appearance alone is not enough to locate a structure as, for example, in the case of hippocampus segmentation. The template provides a prediction of the hippocampus-amygdala boundary. Mapping multiple templates to an individual (multi-template labeling) can further improve accuracy [39, 17]. The second application operates in the “inverse” direction of the first: instead of mapping template to individual, we map individual(s) to the template. Voxel-based population studies of either functional or structural variables depend on mapping to a template space. The common coordinate system enables a statistical evaluation of the likelihood of consistent activation across a group or, in other contexts, the differences in anatomy between two groups.

The ANTs toolkit enables both types of mapping. The main challenge in image and brain mapping is defining the way in which images/anatomy are compared. There are two components to the comparison. The shape transformation space defines the range of shape variation that will be allowed in the optimization. The appearance similarity space defines the statistical assumptions that determine when one image is considered to appear similar to another.

These two components interact in a weighted optimization within a multiple resolution gradient descent framework. Each component may use either “strict” or “flexible” assumptions about the shape or appearance similarity. The selection of these models should be done in a principled way that fits the problem at hand. No single choice is appropriate for all scenarios (see the “no free lunch” theorem).

Thus, ANTs enables many operating points from both the transformation and appearance domains such that users may make choices appropriate for their problems. The ANTs command-line syntax, shown in figure 2, reflects these operating points and the various components that interact in the optimization. ANTs may be used to navigate the transformation and similarity metric space.

<b>Quick</b>	<b>Start:</b>	<b>call</b>
<code>antsRegistrationSyNQuick.sh</code> (after copying the contents of ANTs/Scripts/ to your bin directory) to get usage and apply a normalization to some of your existing data. It is instructional to read the script, modify some of the parameters and re-run to witness the effect of your changes – image registration is an art as well as science. Many other “ready to go” scripts are available in ANTs/Scripts. Often, the user must set his/her ANTSPATH environment variable – which points to the location of ANTs binaries – within these scripts or export the ANTSPATH variable into the user or script environment. Note: All ANTs programs provide usage when called from the command line. Most require the image dimension to be specified as the first parameter. E.g. <code>ImageMath ImageDimension</code> where <code>ImageDimension</code> is 2, 3, 4.		

### 2.1 World coordinates: Use your header!

ANTs uses the direction/orientation, spacing and origin in its definitions of the mapping between images. That is, ANTs uses the ITK standard definitions of an image space. So, the image orientation, direction matrix, origin and spacing are important! If in doubt about, for example, which side is viewed as left or right by ANTs, then take a look at ITK-SNAP <http://www.itksnap.org> and label an image’s known left side. Then apply an ANTs or ITK mapping to the image to see how the data is transformed. *ITK and ANTs do not use the s-form that may be stored in some Nifti images.*



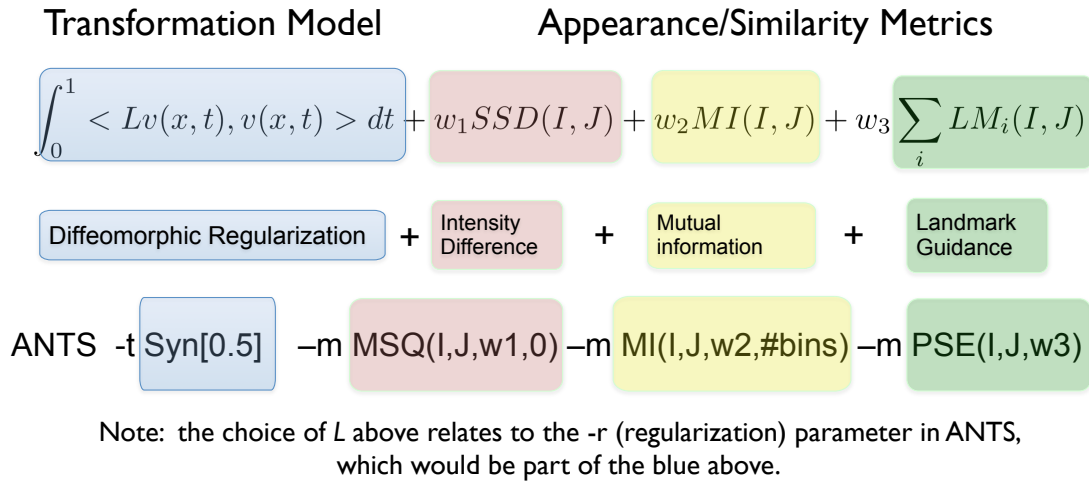


Figure 2: The relationship between the variational form that defines the optimization goals and the ANTs command line. The SyN option implements the method in [10] and evaluated in [25]. The newer version of the ants registration executable is called `antsRegistration` and uses a similar command line that is connected to the variational objective function.

DICOM, ITK and ANTs use LPS coordinate systems. In contrast, the nifti coordinate system is RPI. These coordinate system differences create much confusion especially when switching between software. Very few medical imaging software systems are internally consistent w.r.t. the treatment of world coordinates across file formats. However, ANTs and ITK tools will be consistent. ITK-SNAP will be mostly consistent with ANTs and ITK although it allows coordinates to be transformed and, in that case, all bets are off. As above, if you have a concern, please perform a straightforward experiment to test your concerns. Keep in mind that viewing images with software that does not conform to ITK world coordinates will make the images “look wrong” with respect to image orientation. This caveat may include NiPy, FSL, SPM etcetera.

## 2.2 ANTs Transformation Models

The ANTs toolkit provides a hierarchy of transformations with adjustable levels of complexity, regularization, degrees of freedom and behavior as optimizers. The simplest transformation model is the translation, followed by the rigid and/or affine transform. The most complex – and most flexible – is a symmetric diffeomorphic transformation based on optimizing and integrating a time-varying velocity field. Computation time also increases with transformation model complexity, but most normalization needs may be met with under an hour of computation. We provide an overview of some of the ANTs models below and try to communicate intuition on what one gains/loses with each choice. An overview of available models and similarity terms is in Table 1.

**General Parameters:** ANTs registration options include control of iterations (and, optionally, convergence criterion) via `-c 5000x5000x5000` which specifies that the affine registration uses a 3 level image pyramid with each level 5000 iterations at most. Multi-resolution options include `-s` for smoothing and `-f` for “shrink factors” i.e. downsampling rates (e.g. 8 means  $1/8^{th}$  resolution). `MI[fixed,moving,1,32,Regular,0.1]` means to use Mutual Information as similarity metric with 32 bins and regularly spaced samples of 10% of the image; lower sampling rates increases speed and is useful in low-dimensional registration. `MI[fixed,moving,1,32]` means to use Mutual Information as similarity metric with 32 bins and dense



Category	Transformation, $\phi$	Similarity Measures	Brief Description
<b>Linear</b>	Rigid <sup>†</sup>	MI, MeanSquares, GC	Rigid registration.
	Similarity <sup>†</sup>	MI, MeanSquares, GC	Rotation + uniform scaling.
	Affine <sup>†</sup>	MI, MeanSquares, GC	Affine registration.
<b>Elastic</b>	GaussianDisplacementField	CC, MI, MeanSquares, Demons	Demons-like algorithm.
	BSplineDisplacementField	CC, MI, MeanSquares, Demons	FFD variant.
<b>Diffeo.</b>	Exponential <sup>†</sup>	CC, MI, MeanSquares, Demons	$\min v(\mathbf{x})$
	SyN <sup>†</sup>	CC, MI, MeanSquares, Demons	locally in time $\min v(\mathbf{x}, t)$
	BSplineSyN <sup>†</sup>	CC, MI, MeanSquares, Demons	locally in time $\min v(\mathbf{x}, t)$
	TimeVaryingVelocityField <sup>†</sup>	CC, MI, MeanSquares, Demons	$\min v(\mathbf{x}, t)$ over all time

Table 1: Transformations and a subset of the similarity metrics available in ANTs. Similarity metric acronyms: CC = neighborhood cross correlation (the preferred metric), MeanSquares = mean squared difference, MI = mutual information, PSE = point-set expectation (to be added soon-ish **FIXME**) [28]. ANTs also provides the inverse of those transformations denoted by the ‘†’ symbol. The brief descriptions of the diffeomorphic algorithms contrast the way in which the velocity field is optimized and used to parameterize  $\phi$ , the mapping. All ANTs Diff algorithms generate  $\phi(\mathbf{x}, t)$  over  $t \in [0, 1]$  through gradient descent.

sampling of the image and would be typically used in deformable registration. See `antsRegistration --help` for more information.

Affine and Rigid Registration—**FIXME—this section and figures**

The ANTs affine mapping syntax is shown in the affine mapping figure 3.

Affine mapping may become nontrivial when the region of interest occupies only a small portion of the image data. In such cases, ANTs enables the user to define a mask to focus the optimization effort on the region of interest. Example code for (affine) registration with a mask: <http://stnava.github.io/BasicBrainMapping/>. The difference between this command and a regular ANTs call is the `-x` option, which specifies the mask, defined in the template space. The mask option also affects the deformable optimization.

**Rigid Registration:** ANTs will also perform rigid registration. For example,

```
1 imgs=" -f r16slice.nii.gz -m r64slice.nii.gz "
2 antsRegistrationSyNQuick.sh -d 2 $imgs -o output$0 -t r
3 rm output$0* # cleanup
```

The jacobian of the resulting affine mapping should be unity. Compare the `antsRegistrationSyNQuick.sh` and `antsRegistrationSyN.sh` scripts to see how one might improve or modify registration parameters for different problems.

### Deformable Registration

Affine mapping is adequate when the difference between images involves only rotation, scaling or shearing. Other data requires more deformable mappings to capture shape differences and find a good alignment of image features. Figure 4 shows how deformable mapping may improve the correspondence of the deformed beetle to the ford image. Most ANTs-based applications use symmetric diffeomorphic normalization. How-

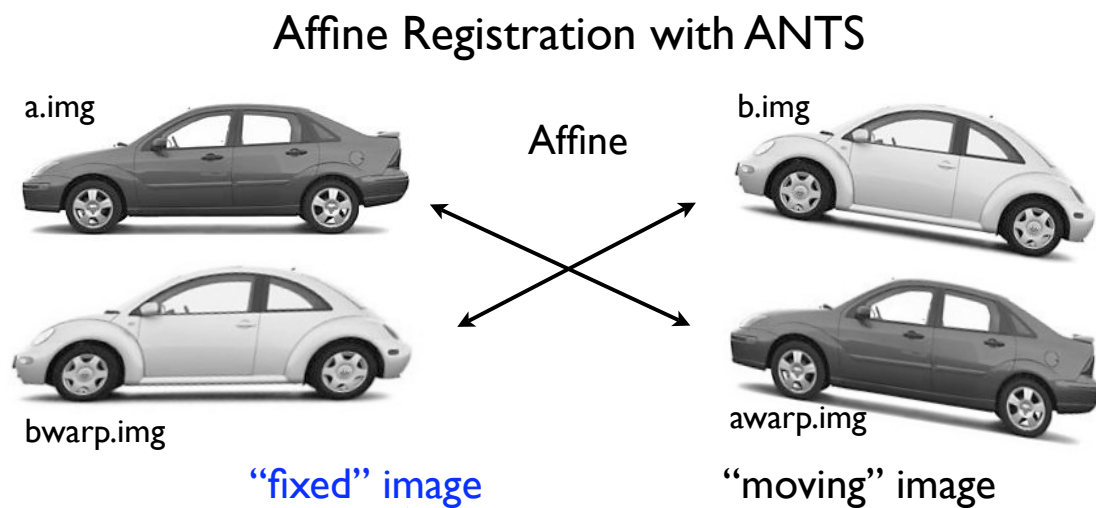


Figure 3: The anatomy of an ANTs optimization and application of the resulting warping.



Figure 4: This example shows the degree to which the beetle (b.img) may be deformed to the ford (a.img) under different transformation models. Left to right increases the degrees of freedom in the mapping and thus the registration accuracy.

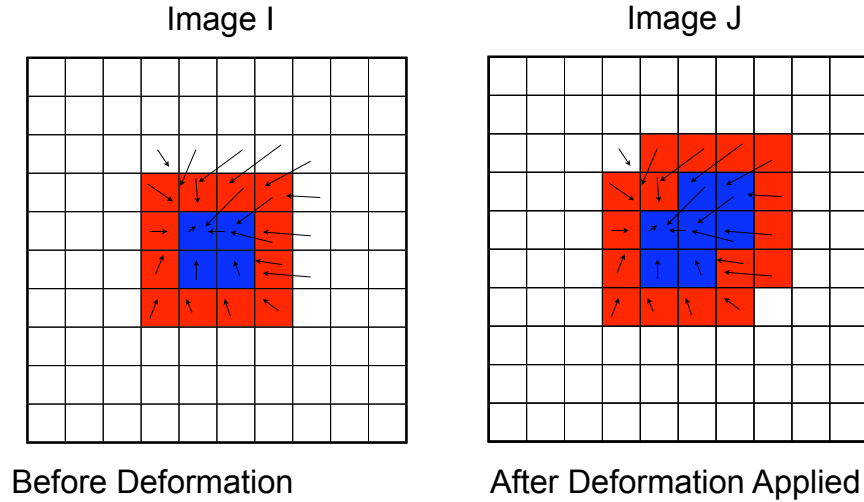


Figure 5: A deformation in a digital domain.

ever, ANTs also enables a simpler parameterization of a deformable mapping via a regularized vector space. We term these types of transformations as “elastic”. The original Demons algorithm provides a classic example of using a regularized vector space for nonlinear registration. Caveats are that a regularized vector space may not preserve the underlying topology and may also prove too inflexible to capture the shape changes one is after. Both of these shortcomings motivate the use of diffeomorphisms.

**Elastic/Vector Space Transformations.** If we assume no affine transformation, then an elastic transformation involves computing a mapping from image  $I(\mathbf{x})$  to image  $J(\mathbf{x})$  through a deformation field  $\mathbf{u}(\mathbf{x})$ . The deformation is defined in the physical space of the image and dictates the positional difference between corresponding features in the two images. Thus, if a feature defined at  $I(\mathbf{x})$  matches a feature in  $J$  at position  $\mathbf{y}$  then the deformation field at  $\mathbf{x}$  should give  $\mathbf{u}(\mathbf{x}) = \mathbf{y} - \mathbf{x}$ . Such a deformation field may be applied to deform image  $J$  into image  $I$  by composing the mapping  $J_{deformed}(\mathbf{x}) = J(\mathbf{x} + \mathbf{u}(\mathbf{x}))$ . In a perfect world, then  $I(\mathbf{x}) = J_{deformed}(\mathbf{x})$ , though this is rarely the case. Figure 5 visualizes the deformation of an image under this standard model. Gradient descent optimization of an elastic mapping may be summarized (crudely) as:

$$\begin{aligned}
 &\text{Compute the similarity gradient: } \nabla E = \partial_{\mathbf{u}} \Pi(I, J(\mathbf{x} + \mathbf{u}(\mathbf{x}))). \\
 &\text{Update the deformation field: } \mathbf{u}(\mathbf{x}) \leftarrow \mathbf{u}(\mathbf{x}) + \delta \nabla E. \\
 &\text{Regularize the deformation field: } \mathbf{u}(\mathbf{x}) \leftarrow G_{\sigma} \star \mathbf{u}(\mathbf{x}), \tag{1}
 \end{aligned}$$

where  $\Pi$  is the similarity,  $\delta$  is a gradient step length and  $G_{\sigma}$  is a gaussian smoother. This optimization is captured in the following ANTs command (FIXME)

```

1 dim=2
2 nm=output$0
3 antsRegistration -d $dim -r [ r16slice.nii.gz , r64slice.nii.gz ,1] \
4     -m mattes[ r16slice.nii.gz , r64slice.nii.gz, 1 , 32, regular,
5         0.1 ] \
6     -t affine[ 0.1 ] \
7     -c [500x500x50,1.e-8,20] \
8     -s 4x2x1vox \
9     -f 3x2x1 -1 1 \

```

```

9          -m cc[ r16slice.nii.gz , r64slice.nii.gz, 1 , 4 ] \
10         -t GaussianDisplacementField[ .5, 3, 0.5 ] \
11         -c [ 50x50x50,0,5 ] \
12         -s 1x0.5x0vox \
13         -f 4x2x1 -l 1 -u 1 -z 1 \
14         -o [ ${nm} , ${nm}_diff.nii.gz, ${nm}_inv.nii.gz ]
15 rm output$0* # cleanup

```

Here, we use the CC metric (a cross-correlation implementation) with window radius 4, weight 1 and gradient step length 1.5. The optimization will be performed over three resolutions with a maximum of 30 iterations at the coarsest level, 20 at the next coarsest and 10 at the full resolution. We use a Gaussian regularizer with a sigma of 3 that operates only on the deformation field and not on the similarity gradient, as 0 is passed as the first parameter to `GaussianDisplacementField`. One may see the correspondence, yet again, between the ANTs call and the optimization scheme. The optimization will stop when either the energy cannot be smoothly minimized or the maximum number of iterations is reached. BSpline regularization is also available in ANTs – see the DMFFD section below.

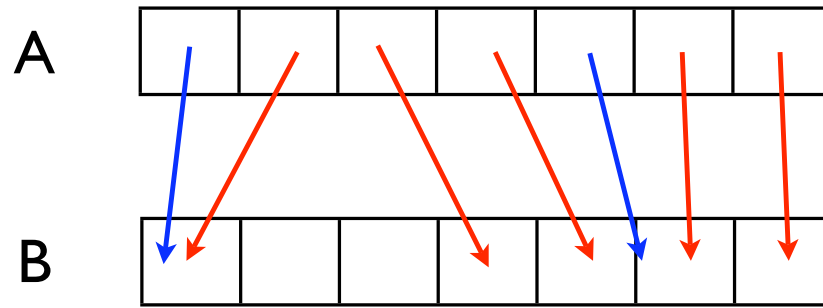
**Warping and Invertibility.** ANTs uses physical space to define mappings. The origin etc is in the coordinates of the world in which the picture (e.g. MRI) was taken. Then, warping between physical coordinates is relatively easy. Differences in bounding boxes etc present no problem – assuming you avoid inconsistent headers i.e. origins, directions, data orientation. One may use `PrintHeader` to check the data and run simple, fast tests (few iterations) to perform sanity checks before running through loads of data. An ANTs deformation consists of a standard naming prefix plus a standard naming extension. We usually assume `nii` but other file types may be used. The value of a voxel of a deformation/warp component image is the physical space displacement from that voxel. Note that an inverse warp – in the digital domain – is only approximate as shown in figure 6. A few important notes follow. (1) Deformation directionality: Warps/deformations applied to images occur in the opposite direction from warps/deformations applied to points. That is, if we map image B to A using

```

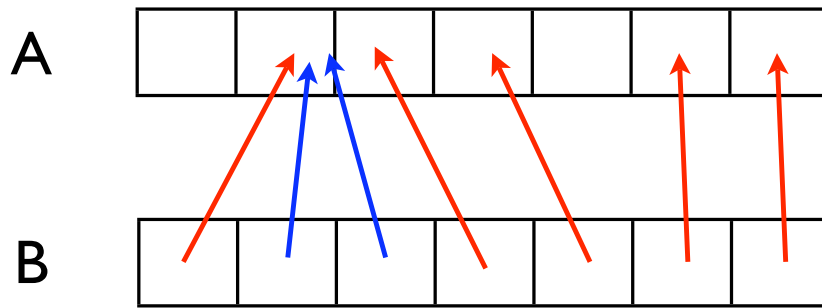
1 dim=2
2 nm=output$0
3 antsRegistration -d $dim -r [ r16slice.nii.gz , r64slice.nii.gz ,1] \
4         -m mattes[ r16slice.nii.gz , r64slice.nii.gz, 1 , 32, regular,
5         0.1 ] \
6         -t affine[ 0.1 ] \
7         -c [500x500x50,1.e-8,20] \
8         -s 4x2x1vox \
9         -f 3x2x1 -l 1 \
10        -m cc[ r16slice.nii.gz , r64slice.nii.gz, 1 , 4 ] \
11        -t GaussianDisplacementField[ .5, 3, 0.5 ] \
12        -c [ 50x50x50,0,5 ] \
13        -s 1x0.5x0vox \
14        -f 4x2x1 -l 1 -u 1 -z 1 \
15        -o [ ${nm} , ${nm}_diff.nii.gz, ${nm}_inv.nii.gz ]
16 rm output$0* # cleanup

```

then we get a deformation called `OUTPUT1Warp.nii.gz` and an affine transform called `OUTPUT0GenericAffine.mat`. This composite mapping – when applied to B – will transform B into the space of A. However, if we have points defined in B that we want to map to A, we have to



Warp pulls B into space of A, but is not dense in B.



InverseWarp pulls A into space of B, but is not dense in A.

↑ Has inverse arrow  
in target domain

↑ No inverse arrow  
in target domain

Figure 6: Digital invertibility presents some limitations. Here, we see that invertibility is not exact but is gained only by interpolation. Thus, in three-dimensional scenarios in particular, there are fundamental limits to the degree of invertibility that may be achieved. The second and third voxels – from left – in image A undergo an expansion by a factor of 2. That is, under the mapping, 2 voxels are mapped to 4. This gives the definition of the Jacobian – computed by ANTsJacobian – which is a unitless measure defined by the ratio of volumes. Thus,  $J(\mathbf{x}) = V(\phi(\mathbf{x}))/V(\mathbf{x})$  where  $V$  represents the volume operation and  $\mathbf{x}$ , here, may be a small object. Thus, if  $\phi$  – the mapping – causes expansion, then  $J(\mathbf{x}) > 1$ .

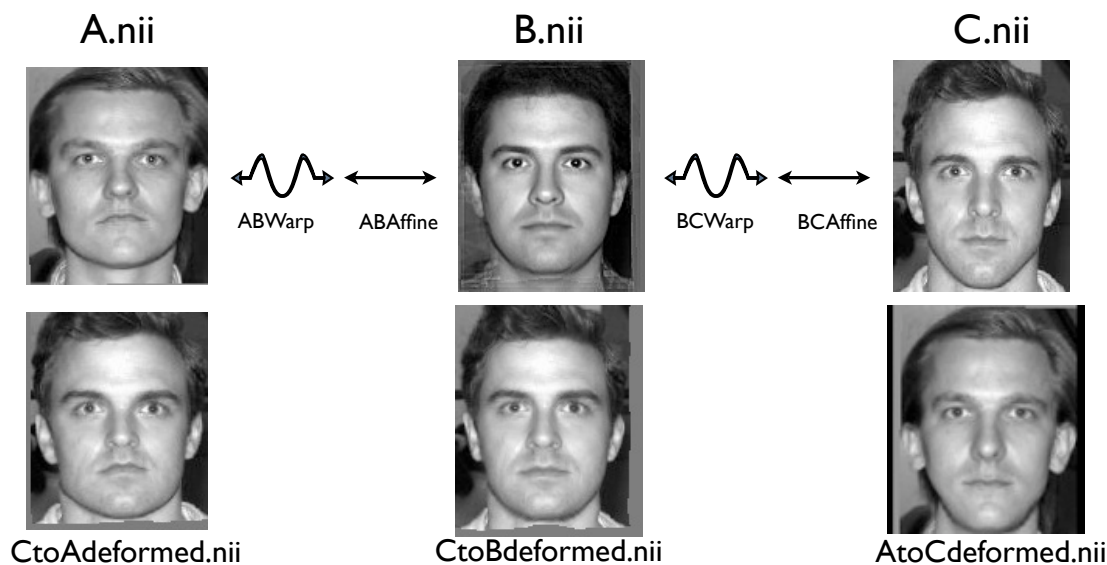


Figure 7: Here, we detail how one applies a deformation and associated inverses. We also see how `antsApplyTransforms` can be used to concatenate a series of transformations. In brief, read parameters left to right, then pass to `antsApplyTransforms`. To warp C to A (in short-hand): `antsApplyTransforms -t ABWarp -t ABAffine -t BCWarp -t BCAffine`. Use the inverse composite transform to warp A to C (in short-hand): `antsApplyTransforms -t [BCAffine,1] -t BCInverseWarp -t [ABAffine,1] -t ABInverseWarp`. Note, to focus on the key idea, we dropped the other parameters needed for a proper `antsApplyTransforms` call.

use `OUTPUT1InverseWarp.nii.gz` and the inverse of `OUTPUT0GenericAffine.mat`. This is because the domain and range of the map's definition need to be dense in a way that is appropriate for the data type. Figure 6 illustrates the concept. (2) Older Image Formats: older image formats (e.g. Analyze) may not have proper origin/offset/direction support! In these cases, we recommend converting to nii and verifying that data overlays properly. (3) Transform Composition: Composition of transforms may be achieved with `antsApplyTransforms`. (4) Warping with inverses and concatenations – viable when using diffeomorphisms – are described in figure 7.

**Diffeomorphic Transformations.** The elastic mapping space – as indicated above – may prove inadequate for some large deformation mapping scenarios. Figures 4 illustrate the changing performance one may get in switching from affine to elastic to diffeomorphic normalization. Figure 8 shows how one may use ANTs to achieve a state-of-the-art diffeomorphic mapping. The ANTs diffeomorphic model chosen for this example – symmetric normalization [10, 24] – is invariant to the order of the input images (although the affine mapping is not). An additional advantage of the diffeomorphic model over the elastic model is that both forward and inverse transformations are computed thus allowing one to deform fixed to moving and also moving to fixed. The transformation model chosen here – `SyN[0.1, 3, 0.0]` – may be replaced with other diffeomorphic transformation models. The most general is global-in-time SyN via `SyN[0.1, 3, 0.0]`, where the time step for integration is 0.01 (lower is more accurate). A fast approximate solution may be gained through exponential mapping via `Exponential[0.1, 3, 0.5, 10]`, where 10 integrations points are used. Update schemes for diffeomorphic optimization are similar to the elastic case and are described elsewhere [10].

## Symmetric Diffeomorphic Mapping with ANTs

### Affine+ Diffeomorphic SyN

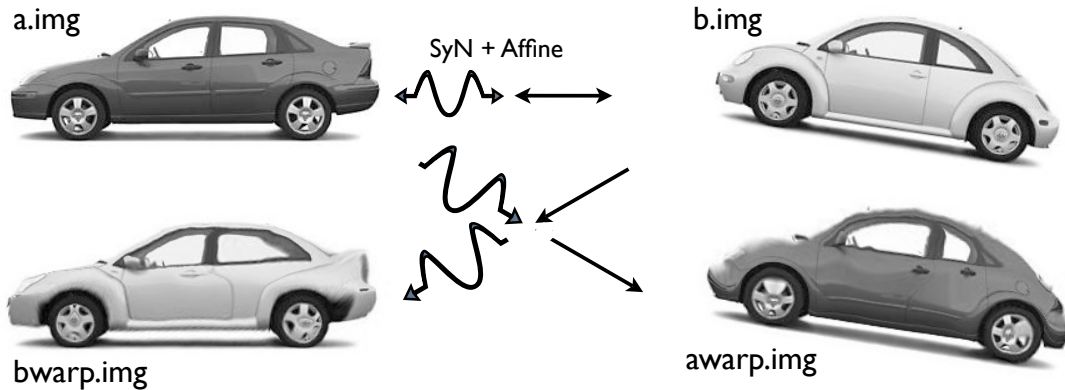


Figure 8: This example shows the benefit of the symmetric normalization model – invertibility, symmetry, highly deformable and accurate registration. This example may be recreated by the reader via: <http://stnava.github.io/cars/>.

### 2.3 ANTs Similarity Terms

Here is a script that will let you experiment with different similarity term and transformation model combinations. A few are listed, with parameters that are a reasonable starting point. This example implements an elastic mapping driven by neighborhood cross-correlation and initialized by mutual information affine:

```

1 dim=2
2 nm=output$0
3 antsRegistration -d $dim -r [ r16slice.nii.gz , r64slice.nii.gz ,1] \
4     -m mattes[ r16slice.nii.gz , r64slice.nii.gz, 1 , 32, regular,
5         0.1 ] \
6     -t affine[ 0.1 ] \
7     -c [500x500x50,1.e-8,20] \
8     -s 4x2x1vox \
9     -f 3x2x1 -l 1 \
10    -m cc[ r16slice.nii.gz , r64slice.nii.gz, 1 , 4 ] \
11    -t GaussianDisplacementField[ .5, 3, 0.5 ] \
12    -c [ 50x50x50,0,5 ] \
13    -s 1x0.5x0vox \
14    -f 4x2x1 -l 1 -u 1 -z 1 \
15    -o [ ${nm}, ${nm}_diff.nii.gz, ${nm}_inv.nii.gz ]
rm output$0* # cleanup

```

This example implements a greedy syn mapping that includes elastic regularization and is driven by mutual information and initialized by global correlation with a similarity transform:

```

1 dim=2
2 nm=output$0
3 antsRegistration -d $dim -r [ r16slice.nii.gz , r64slice.nii.gz ,1] \

```



```

4      -m gc[ r16slice.nii.gz , r64slice.nii.gz, 1 , 32, regular, 0.1
      ] \
5      -t similarity[ 0.1 ] \
6      -c [500x500x50,1.e-8,20] \
7      -s 4x2x1vox \
8      -f 3x2x1 -l 1 \
9      -m mattes[ r16slice.nii.gz , r64slice.nii.gz, 1 , 48 ] \
10     -t syn[ .15, 3, 0.5 ] \
11     -c [ 50x50x50,0,5 ] \
12     -s 1x0.5x0vox \
13     -f 4x2x1 -l 1 -u 1 -z 1 \
14     -o [${nm},${nm}_diff.nii.gz,${nm}_inv.nii.gz]
15 rm output$0* # cleanup

```

This example uses smoothing without downsampling (ie scale-space) and implements a greedy syn driven by two unequally weighted similarity metrics and no affine mapping:

```

1 dim=2
2 nm=output$0
3 # registration is performed at a coarse 1/2 scale
4 antsRegistration -d $dim -r [ r16slice.nii.gz , r64slice.nii.gz ,1] \
5     -m mattes[ r16slice.nii.gz , r64slice.nii.gz, 1 , 32 ] \
6     -m cc[ r16slice.nii.gz , r64slice.nii.gz, 0.5 , 2 ] \
7     -t SyN[ .15, 3, 0 ] \
8     -c [ 50x50x50,0,5 ] \
9     -s 4x2x0vox \
10    -f 2x2x2 -l 1 -u 1 -z 1 \
11    -o [${nm},${nm}_diff.nii.gz,${nm}_inv.nii.gz]
12 rm output$0* # cleanup

```

Convergence occurs under two conditions: (1) either the maximum number of iterations are reached at a given optimization level or (2) the slope of the change in the optimization objective is negative or very small.

## 2.4 Choosing a Metric

ANTS supports both volumetric registration and point set registration. The image / point set similarity metrics in ANTS are unified in the form of a function on the images or the point sets:

**Similarity[fixedImage,movingImage,weight,parameters].**

The similarity type for the deformation transformation is specified by `-m` option, which contains two parts: similarity type and the parameters inside the brackets. The possible similarity metrics for volumetric images are:

- **Cross correlation estimate:** `-m CC[fixedImage,movingImage,weight,radius].`  
This metric works well for intra-modality image registration. For example, `-m CC[fixed.nii,moving.nii,1,5]` specifies:

- the fixed image: `fixed.nii`
  - the moving image: `moving.nii`
  - weight for this metric is 1 (i.e. only this metric drives the registration).
  - the region radius for computing cross correlation is 5
- **Mutual information:**

```
-m MI[fixedImage,movingImage,weight,number-of-histogram-bins,
samplingStrategy,samplingPercentage]
```

This metric works both well for intra-modality and inter-modality image registration. For example, the first three parameters in `-m MI[fixed.nii,moving.nii,1,32]` similar to the example above in cross correlation, except that the last parameter means that the number of bins in computing mutual information is 32.
  - **Global correlation:**

```
-m GC[fixedImage,movingImage,weight,0, samplingStrategy,samplingPercentage]
```

This metric works both well for intra-modality and inter-modality image registration. For example, `-m GC[fixed.nii,moving.nii,1,0,Random,0.1]` uses 10% random sampling of the image to estimate the global correlation.
  - **Mean square difference:**

```
-m MeanSquares[fixedImage,movingImage,weight,0]
```

This metric works for intra-modality image registration. The last parameter 0 is a padding value of no real meaning. For example, `-m MeanSquares[fixed.nii,moving.nii,1,0]`.

ANTs also support registration of point sets **FIXME—only old ANTS so far ... will be added to antsRegistration in the near future**. The supported formats for point sets can be found in I/O section. The similarity metrics for point sets are:

- **Point set expectation:**

```
-m PSE [fixedImage,movingImage,fixedPoints,movingPoints,weight,
pointSetPercentage,pointSetSigma,boundaryPointsOnly,
kNeighborhood,PartialMatchingIterations=100000]
```

  - `fixedImage`: defines the space domain of the fixed point set.
  - `movingImage`: defines the space domain of the moving point set.
  - `fixedPoints/Image`: defines the coordinates of the fixed point set or label image. It can be an image with discrete positive labels, a VTK format point set file, or a text file. Details can be found in I/O section (TODO).
  - `movingPoints/Image`: defines the coordinates of the moving point set or label image.
  - `weight`: weight for this metric. 1 means that only this metric drives the registration.
  - `pointSetPercentage`: the percentage of points to be randomly sampled used in the registration.
  - `pointSetSigma`: the standard deviation of the Parzen window used to estimate the expectation.
  - `boundaryPointsOnly`: 1 (or “true”) means only the boundary points in the label image is used to drive registration.

fixed image | moving image | MSE

Figure 9: registration using mean square intensity difference

- `kNeighborhood` is a positive discrete number. The first  $k$  neighbors are used to compute the deformation during the registration.
- `PartialMatchingIterations` controls the symmetry in the matching. This option assumes the complete labeling is in the first set of label parameters ... more iterations leads to more symmetry in the matching - 0 iterations means full asymmetry

- Jensen-Tsallis BSpline

```
-m JTB[fixedImage,movingImage,fixedPoints,movingPoints,weight,
pointSetPercentage,pointSetSigma,boundaryPointsOnly,kNeighborhood,alpha,
meshResolution,splineOrder,numberOfLevels,useAnisotropicCovariances]
```

- `fixedImage`: defines the space domain of the fixed point set.
- `movingImage`: defines the space domain of the moving point set.
- `fixedPoints`: defines the coordinates of the fixed point set. It can be an image with discrete positive labels, a VTK format point set file, or a text file. Details can be found in I/O section (TODO).
- `movingPoints`: defines the coordinates of the moving point set.
- `weight`: weight for this metric. 1 means that only this metric drives the registration.
- `pointSetPercentage`: the percentage of points to be randomly sampled used in the registration.
- `pointSetSigma`: the sigma for the Parzen window used to estimate probabilities.
- `boundaryPointsOnly`: [TODO] 1 (or “true”) means only the boundary points in the point sets are used to drive registration.
- `kNeighborhood` is a positive discrete number. The first  $k$  neighbors are used to compute the deformation during the registration.
- `alpha`
- `meshResolution`
- `splineOrder`
- `numberOfLevels`
- `useAnisotropicCovariances`

Fig. 2.4 shows the registration result using intensity difference. Here is also an example script to register a pair of images using mean square intensity difference and computing the metrics of the registration image.

```
1 # use intensity difference with radius 0 -- radius no effect on intensity
   difference
2 antsRegistration -d 2 -m MeanSquares[r16slice.nii.gz,r64slice.nii.gz,1,0] -t \
3   GaussianDisplacementField[0.5,3,0.5] -c 50x50x30 -f 4x2x1 -s 0x0x0 -o $0test.nii.
   gz
```

```

4 antsApplyTransforms -d 2 -i r16slice.nii.gz -o $0resMSQ.nii.gz -t $0test.nii.gz0Warp
  .nii.gz -r r16slice.nii.gz
5 MeasureImageSimilarity 2 0 r16slice.nii.gz $0resMSQ.nii.gz $0metricexamplelog.txt
6 MeasureImageSimilarity 2 1 r16slice.nii.gz $0resMSQ.nii.gz $0metricexamplelog.txt
7 MeasureImageSimilarity 2 2 r16slice.nii.gz $0resMSQ.nii.gz $0metricexamplelog.txt
8 ConvertToJpg $0resMSQ.nii.gz $0resMSQ.jpg
9 rm $0* # cleanup

```

## 2.5 Notes on basic brain mapping

There is “maximally robust” brain mapping and there is “fast” brain mapping. These two goals may, at times, be adversarial. A simple and “fast” brain registration example is here <http://stnava.github.io/BasicBrainMapping/>. This example shows a non-optimized use of `antsRegistration` and compares it to the case where the registration is *masked* in order to focus the registration. Such strategies may be used for brains with missing data e.g. lesions.

## 2.6 Normalization across different modalities: E.g. DTI

The `ImageMath` program – via `TensorFA` and `TensorMeanDiffusion` – may derive scalar images from DTI. Such images may be used to distortion correct DTI to T1 or to map DTI together. See the ANTS/Scripts program called `antsIntermodalityIntrasubject.sh` for an example of how one might implement the strategy outlined in [34]. Figure 10 shows what might happen if your tensor entries are stored in the wrong order. ANTs expects the nifti standard ordering of the DT six vector.

## 2.7 Multivariate Normalization with ANTs

Multivariate normalization may be performed in two ways with ANTs. First, as shown in figure 11, intra-subject mappings may be used to conform all modalities into a common subject space defined by the “anchor” modality. In brain imaging, this is usually the T1 component.

A second type of multivariate normalization is able to use the T1 and DTI components directly in the optimization of the mapping. We usually assume that one has resampled data to the space of T1. In this case, dense features within white matter are gained by using the DT component in addition to the T1 component. One might also weight the T1 CC metric slightly more than the FA CC metric, 1.25 vs. 1.0. *The convergence criterion for the multivariate scenario is a slave to the **last** metric you pass on the ANTs command line.*

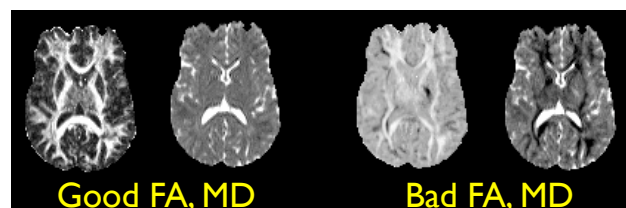


Figure 10: The FA and mean diffusion of the tensor may be corrupted, as at right, if the order of the DT entries is wrong.

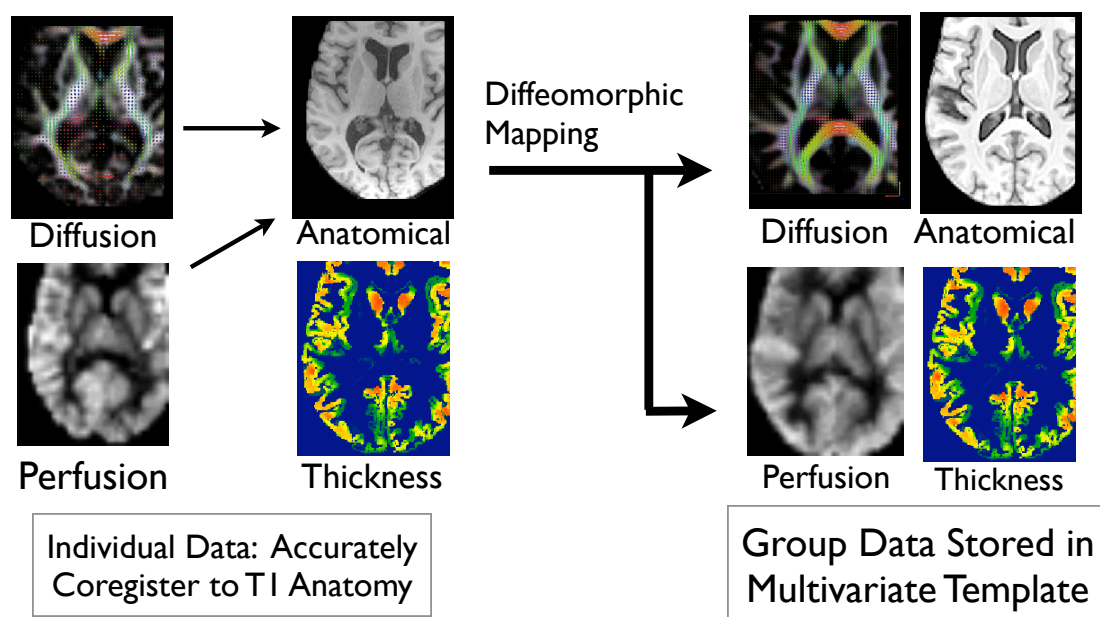


Figure 11: The current version of ANTs may perform normalization of multiple modalities by combining *intrasubject*, *intermodality* mappings with *intersubject*, *intramodality* maps to a group template. In brain imaging, the intersubject maps are usually guided by the T1 component.

## 2.8 Notes on large deformation mapping

Figure 12 defines what one might expect from a high-resolution, large deformation, successful normalization. Major and many minor features are well aligned between these images to an extent that is approaching the limits allowable by biological variation. **Turning “Failures” into Successes:** Below are some pointers to follow if you are unable to recreate such normalization quality. Usually, reasons for registration failure are one of a very few things:

1. The initialization is so off mark that affine registration fails – thus meaning all subsequent deformable registration will not be meaningful.
2. The information within headers is inconsistent e.g. origins are defined in different ways, the “directions” are not correct or some combination of these. The PrintHeader executable can help one in debugging this type of problem.
3. The similarity or transformation model is inappropriate or has too small a capture region for the problem.

Large deformation mapping is challenging not only because of the amount of deformation, but also because the “true” solution becomes more difficult to find as the distance between images increases. Keeping this in mind, fixing registration failures means 1. better initialization or 2. increasing the capture range of the registration. Key changes may include more multi-resolution levels, increasing the radius of the neighborhood correlation, more dense or more focused sampling and/or allowing more iterations during the optimization. Note: the coarsest levels of the computation take only about 10 percent of the time (a few minutes depending on the machine) but account for the large majority of the shape variation. Therefore, inspecting results after only low resolution registration is performed can save significant time and make parameter optimization more rapid.

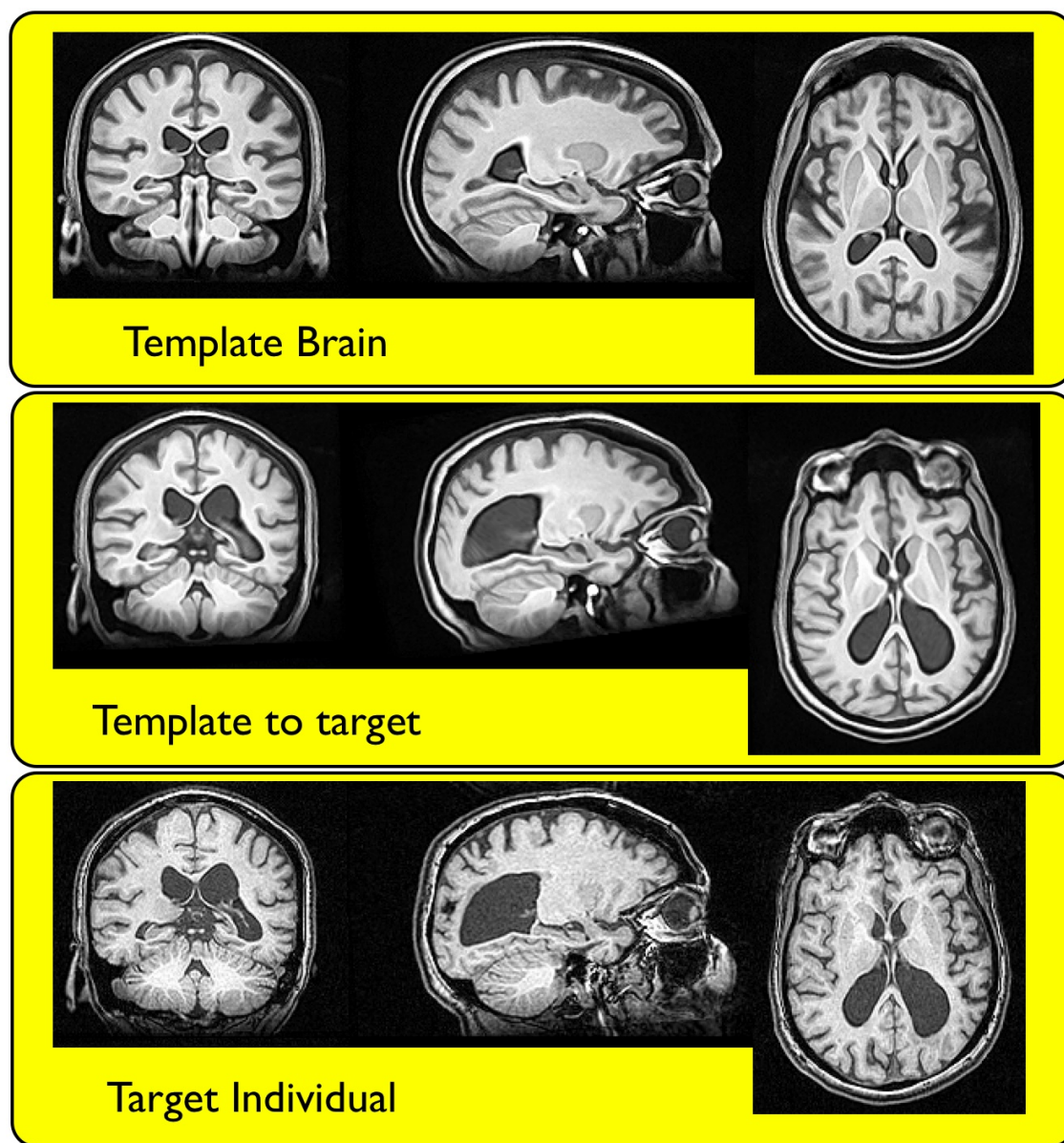


Figure 12: ANTs succeeds in a challenging normalization scenario. Comparing the template mapping to the individual shows that much of the cortex is well-aligned, as is the hippocampus, despite the relatively large difference between the initial template and the target. Here, one might note a limitation of whole brain mapping: occipital lobe sulcal variation is highly idiosyncratic and extremely difficult to capture, in particular when there is such severe atrophy nearby.



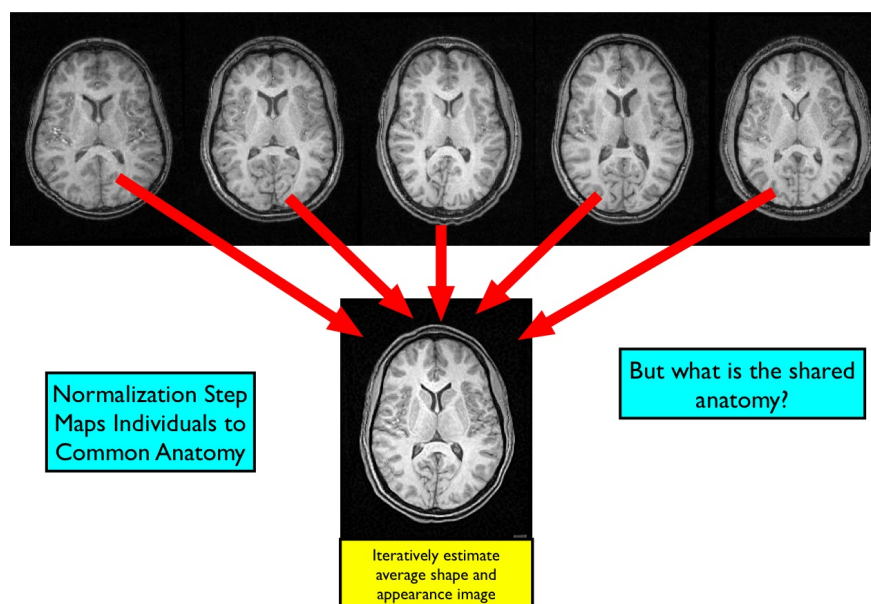


Figure 13: This example may be recreated by the user. The shared anatomy – across this dataset – is recovered in the derived optimal template.

## 2.9 Optimal Template Construction with ANTs

A useful script for setting up optimal template construction is available in ANTs/Scripts. This method is described in [6, 16, 24, 41, 9], where more recent publications are more descriptive and incorporate more recent features and optimization strategies. Two versions of this algorithm are available : serial and parallel. Data and a script for building an average face template is available at <http://ntustison.github.io/TemplateBuildingExample/>. Two key points about optimal templates: 1. The outcome stabilizes at around ten images, for most populations. That is, if we randomly select images from individuals within the same demographic distribution, we will end up with very similar average images. 2. Optimality, for the ANTs-SyN approach, is defined by the minimum shape and appearance distance image. See the template page for some examples of this and users may contact ANTs developers for previously derived template images that may be useful.

The goal of template construction is to derive a “most representative” single image from a population. The steps are:

1. Make a directory for your data. Copy or link all the images into it.
2. On the command line, within that directory, run the following command: `bash antsMultivariateTemplateConstruction2.sh` to get usage.
3. Follow the example outlined in the TemplateBuildingExample above but modified for your own data and needs.
4. The script should exit and store a log of what happened.
5. If there is a problem, check the path to the programs, the fact that all the images you want to use are being listed and that the template output name is ok.



The script is fairly easy to alter so that you can send the whole thing to distributed computing. Typically, one would use `voxbo` or the `qsub` program available in the Sun Grid Engine. This is what is done in `antsMultivariateTemplateConstruction2.sh`. Figure 13 shows the data and a result similar to what may be recreated by the user.

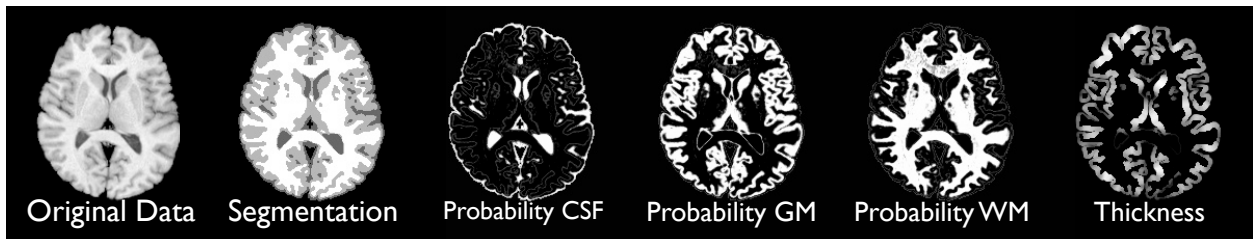


Figure 14: ANTs provides basic Markov Random Field regularized Gaussian model tissue segmentation. The ANTs program `N3BiasFieldCorrection` is very valuable as preprocessing for this naive approach to segmentation. The last panel – far right – shows the thickness derived from the white matter and gray matter probabilities where a prior on thickness was used to prevent thickness overestimation. Thickness was derived with DiReCT [19], a software tool available in binary form only – a future release may provide code.

### 3 Image Segmentation and Labeling

ANTs has tools for both tissue based segmentation and prior-based segmentation that leverages spatial priors, usually based on a template mapping.

#### 3.1 Basic Segmentation

A basic MRF segmentation algorithm is available in ANTs `ImageMath`. We apply the segmentation to the example data in: `ANTs/Examples/Data/r16slice.nii`.

```
ImageMath 2 r16slice.nii Segment r16slice.nii 4 0
% output = r16slice_seg.nii, r16slice_prob_0.nii, r16slice_prob_1.nii, r16slice_prob_2.nii .
```

The parameter 4 indicates 3 tissues plus background are sought. The 0 indicates that there are no prior images available to guide the segmentation. Output is shown in figure 14 and – with priors – in figure 15.

#### 3.2 Prior and Template-based Image Segmentation

The same algorithm may be augmented to perform Prior-based segmentation.

```
ImageMath 2 r16sliceprior.nii Segment r16slice.nii 4 0.5
  csfprior.nii wmprior.nii gmprior.nii
% output = r16sliceprior_seg.nii r16sliceprior_prob_0.nii
% r16sliceprior_prob_1.nii r16sliceprior_prob_2.nii .
```

The parameter 4 indicates 3 tissues plus background are sought. The 0.5 indicates we weight the priors equally as the data term and use a spatially varying set of Gaussians to estimate the segmentation. In this way, data from the priors may be used to modify and guide the segmentation in a locally varying way, accomodating for both inhomogeneity and the different imaging signature that different tissues provide. Prior images should be of the same size and dimension as the input data and should have intensities in the range  $[0, 1]$ .

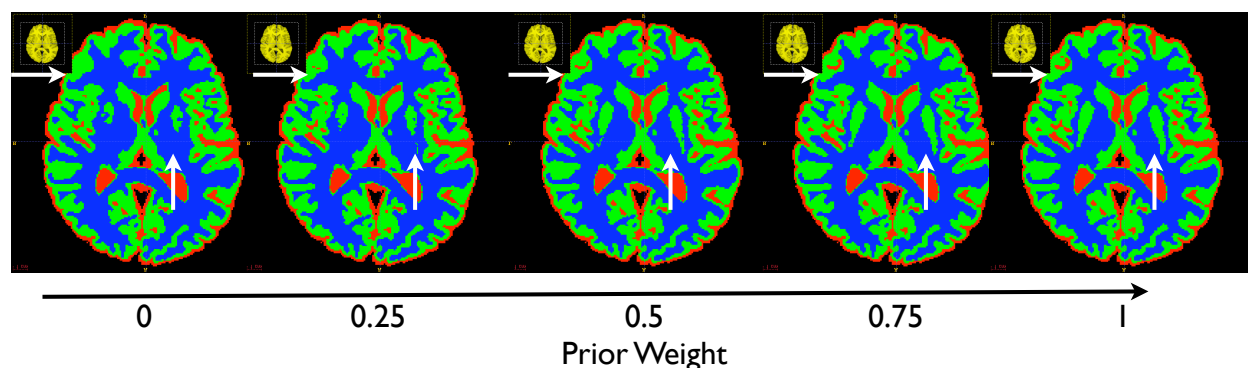


Figure 15: ANTs extends basic Markov Random Field regularized Gaussian model tissue segmentation to include priors, which allow spatially varying tissue models to determine segmentation. The ANTs program N3BiasFieldCorrection is less critical as preprocessing when using this approach to segmentation. Here, we see the improvement in segmentation as the locally varying prior models are weighted more heavily. The last panel – far right – shows the segmentation derived from data driven with an initialization founded purely on prior models based on template mapping. The prior model brings out the caudate and some CSF – highlighted by arrows – as their weight increases.

### 3.3 Cortical Thickness

Two forms of cortical thickness estimation from probability maps are available in ANTs: first, the traditional Laplacian cortical thickness estimation and, second, the more recently developed Diffeomorphic Registration-based Cortical Thickness (DiReCT) [19]. Both methods estimate thickness of an object from probability or binary images that define object boundaries. This tool is mainly of interest in brain mapping and cardiac imaging for morphometric studies. Cortical thickness, for instance, is known to correlate with language development and IQ in adolescents. The laplacian approach to cortical thickness may be used via the program LaplacianThickness, which implements the method described in “Three-dimensional mapping of cortical thickness using Laplace’s Equation” by Jones, et al []. Super-sampling and controlling segmentation accuracy for input to this program is up to the user. Otherwise, the Laplacian method may grossly overestimate thickness in closed sulci.

### 3.4 User/Label-Guided Normalization for Hippocampus Mapping

See the link for details on hippocampus labeling: <http://picsl.upenn.edu/ANTS/hipptutorial.php>. **Expectation-Based Point-Set Registration.** Here, we apply the expectation-based point set registration method for mapping labeled points sets, as described in [28]. ITK-SNAP may be used to label images and exported segmentation images may be input to the PSE metric below, as labeled data. The Frown and Smile data is used as example. This data is available in the ANTS/Examples/Data/ directory.

```
ANTs 2 -o PSEtest -i 91x70x55x40x30 -r Gauss[3,0.] -t SyN[0.2]
-m PSE[Frown.nii,Smile.nii,Frown.nii,Smile.nii,0.75,0.1,11,0,10]
-m MSQ[Frown.nii,Smile.nii,1,0] --number-of-affine-iterations 0

antsApplyTransforms 2 Frown.nii FrownToSmile.nii -R Smile.nii
-i PSEtestAffine.txt PSEtestInverseWarp.nii
```

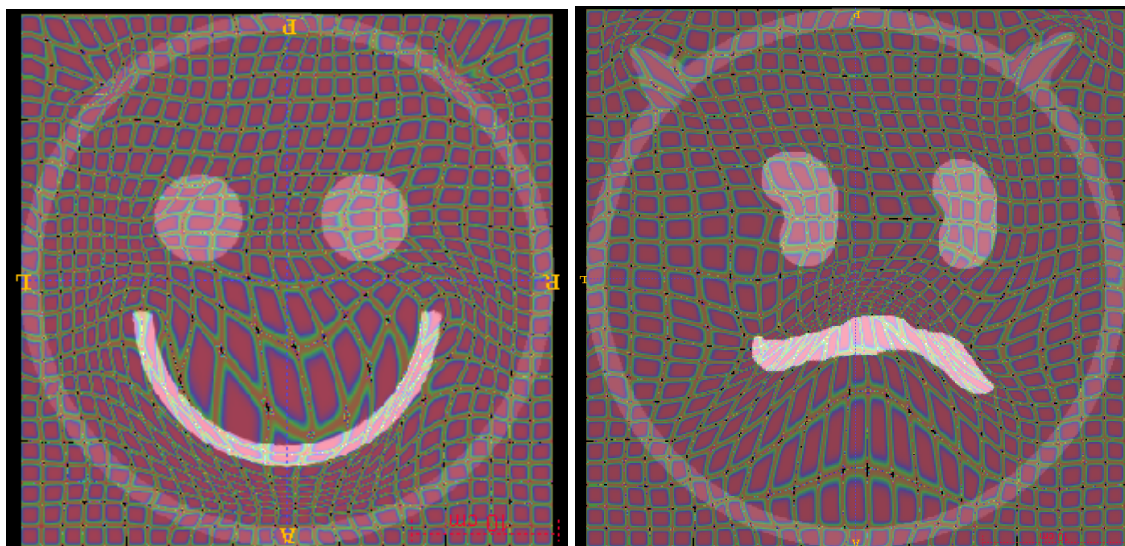


Figure 16: Expected output for the frown to smile shows a smooth, though large deformation. The grids are overlaid on the deformed images.

```
antsApplyTransforms 2 Smile.nii SmileToFrown.nii -R Frown.nii  
PSEtestWarp.nii PSEtestAffine.txt
```

```
CreateWarpedGridImage 2 PSEtestInverseWarp.nii grid1.nii  
CreateWarpedGridImage 2 PSEtestWarp.nii grid2.nii
```

This example should run on the downloaded ANTs data so you may see the results.

## 4 Application to Studies

### 4.1 Brain Mapping in the Presence of Lesions

Many cases violate the basic assumption of a one-to-one mapping from a template image to a target image. Brain lesions caused by stroke or traumatic brain injury are a common instance of this.

The ANTs toolkit handles this situation by a constrained cost-function masking approach. In short, the mapping within an excluded region (as determined by an inclusive mask) is determined by the solution outside of the region. To achieve this with ANTs, one would use a call similar to this:

```
ANTs 3 -m PR[tp22_s1.nii,template.nii.gz,1,4] -i 50x20x0
      -o tp22map -t SyN[0.5] -x mask.nii.gz -r Gauss[3,0]
```

The additional parameter needed for this approach is the `-x mask.nii.gz` which is the mask defined in the "fixed" (or individual) image space. Mask values above 0.5 are considered non-outlier or non-lesioned regions. The labeling may be performed with ITK-SNAP. Figure 17 illustrates the approach. Once the ANTs mapping is solved, one is able to estimate the location of the lesion in the template space by mapping the inverse lesion mask to the template. To take the negative image of the inclusive mask and warp the mask to the template :

```
ImageMath 3 lesionmask.nii.gz Neg inclusivemask.nii.gz
antsApplyTransforms 3 lesionmask.nii.gz lesiontotemplate.nii.gz
      -R template.nii.gz -i tp22mapAffine.txt tp22mapInverseWarp.nii
```

More details on this approach are being prepared for publication. See also: [http://www.ncrn.org/papers/methodology\\_papers/sp\\_norm\\_kim.pdf](http://www.ncrn.org/papers/methodology_papers/sp_norm_kim.pdf).

### 4.2 Statistical Mapping with ANTs: Morphometry, Function, Jacobian, Thickness

ANTs has been applied in a wide array of imaging studies [5, 4, 14, 19, 25, 26, 28, 37, 41, 12, 10, 22, 24, 31, 32, 42, 1, 3, 15]. All of these studies benefit in some way from normalization whether the topic is cortical thickness, Jacobian-based morphometry, volumetric morphometry or functional studies. From a broad perspective, each of these applications requires the same steps:

1. Preprocess images – bias correction, segmentation, etc. Potentially construct an optimal template.
2. Normalize images – run `antsRegistrationSyN.sh` to map a population of images to a template and store the deformations.
3. Derive any data from the deformation that may be necessary, e.g. the log-Jacobian.
4. Apply the warp to any images one may want to analyze in template space.
5. Perform statistics in template space over the region of interest, e.g. all cortex.

We now illustrate this procedure using ANTs tools and example images from ANTs/Examples/Data. The expected output is in figure 18.

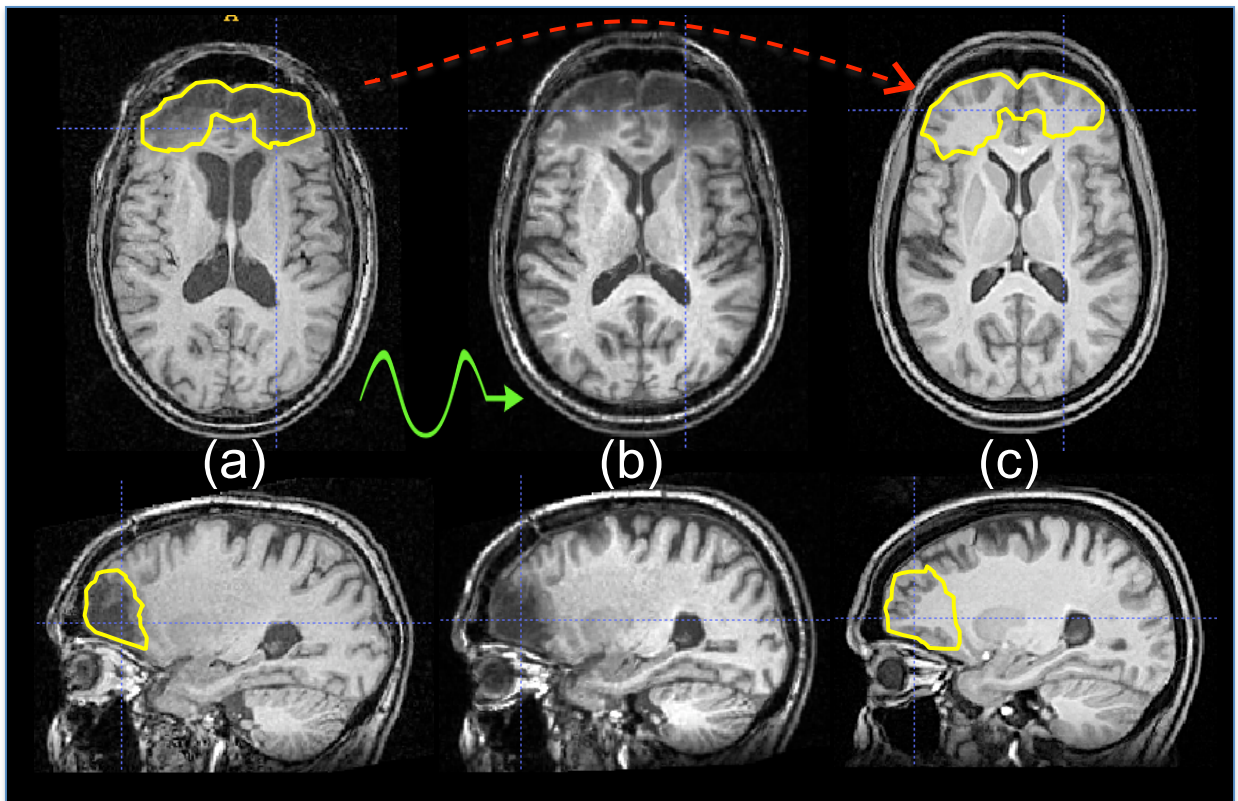


Figure 17: Here, we see a semi-automated approach for lesion analysis based on diffeomorphic normalization. The user outlines the lesion site in the subject space, as shown in (a). Diffeomorphic mapping is then used to deform the subject image in (a) into the space of the reference template. The deformed subject is shown in panel (b). Panel (c) shows the reference template space with the estimated position of the subject's lesion overlaid on the healthy tissue of the template. This approach enables one to compare the subject image against prior information stored in the template space such as anatomical labels or statistics on the appearance of lesioned and/or normal tissue.



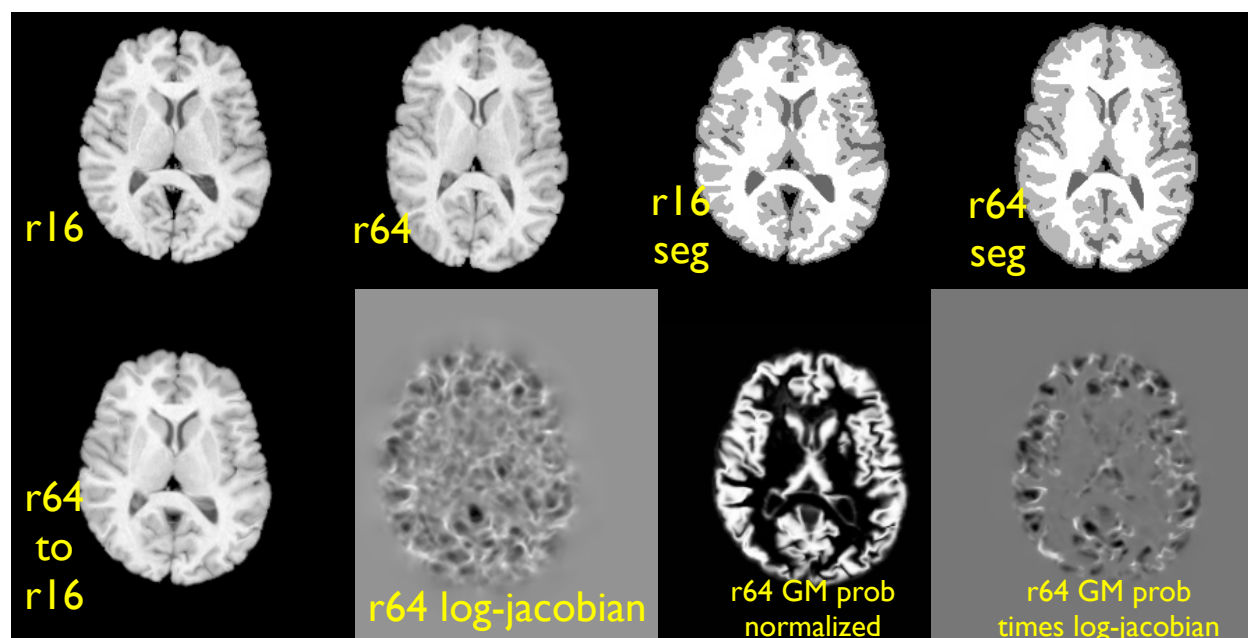


Figure 18: The output from the ANTs morphometry example.

```

1. ImageMath 2 r64slice.nii Segment r64slice.nii 4 0
1. ImageMath 2 r16slice.nii Segment r16slice.nii 4 0
2. sh ants.sh 2 r16slice.nii r64slice.nii SPM 100x100x100
3. SmoothImage 2 r64slice_prob_1.nii 1. r64slice_prob_1.nii
3. antsApplyTransforms 2 r64slice_prob_1.nii r64slice_prob_1_norm.nii
   -R r16slice.nii SPMWarp.nii SPMAffine.txt
3. ANTsJacobian 2 SPMWarp.nii SPM 1 # take the log
4. ImageMath 2 SPMlogjacobianmask.nii m SPMlogjacobian.nii r64slice_prob_1_norm.nii
5. Repeat for a population and run statistics on log jacobians.

```

This example uses a standard Jacobian-based approach to morphometry. Here, we use the log-Jacobian because it is symmetric about zero and mask with the gray matter segmentation to restrict the analysis to the cortex. The Jacobian is discussed in figure 6 and visualization of the Jacobian is shown in figure 19. This Jacobian comes from the mapping shown in figure 12. Similar analyses may be performed on thickness images, functional images or fractional anisotropy images derived from the diffusion tensor modality. In all these cases, steps similar to those above would be performed.

### 4.3 Statistics with ANTs and R

**R** is an open-source, cutting-edge statistical package used by statisticians world-wide. ANTs is designed to interface with **R** via an `ImageMath` tool that converts image sets into an **R** compatible format. Three steps are required. First, convert image data into vector and matrix formats through a mask of your statistical region of interest. Second, read that data into **R** and run your statistics. Third, write out the data from **R** and convert back to an image. Here are the steps, in code examples,

1. Create a vector for your output:



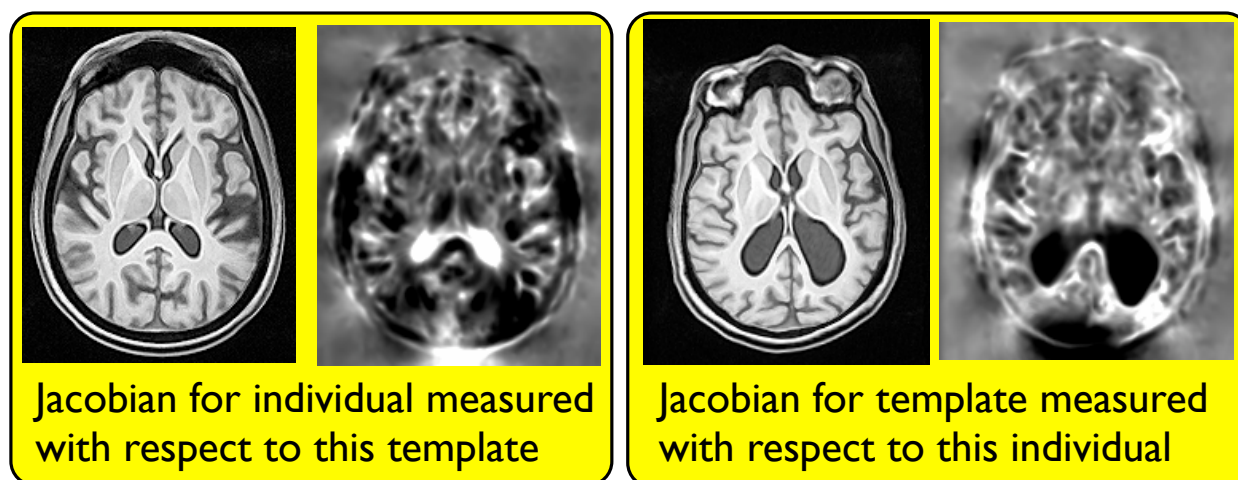


Figure 19: The Jacobian: Note that the bright values in the template image ventricles (left) indicate that the ventricles are relatively larger in the subject image. Similarly, the dark jacobian values in the individual image show that the template has smaller ventricles. This example is described on the large deformation page Large Def. Once one gains the Jacobian (or more appropriately, the log-Jacobian), then one may compute statistics across the population.

```
ImageMath 3 testresultvec.nii ConvertImageSetToMatrix 1 mask.nii image1.nii
```

Here, we assume all images are called image1.nii, image2.nii, ... , imageN.nii so we can use a wildcard to pass to ImageMath and create a matrix for all your input data:

```
ImageMath 3 datamatrix.nii ConvertImageSetToMatrix 1 mask.nii image*.nii
```

2. Run **R** by reading your data above, performing whatever statistics you want and then writing out.
3. Convert the test result back to an image.

```
ImageMath 3 testresult.nii ConvertVectorToImage mask.nii testresultvec.nii
```

Most statistical requirements may be met with this setup.

## 5 Dependencies and Related Software

### 5.1 Dependencies and Compilation

ANTs depends on the most recent version of the Insight ToolKit (ITK) – [www.itk.org](http://www.itk.org). File types that may be read and written are all of those available in itk and a few more <http://picsl.upenn.edu/ANTS/ioants.php>.

ANTs and ITK are both compiled through pointing CMake – [www.cmake.org](http://www.cmake.org) – to a CMakeLists.txt file. The ANTs CMakeLists.txt is in the Examples directory.

See below for more details on compilation and binaries:

**Compile and download:** <http://picsl.upenn.edu/ANTS/download.php>. We maintain a dashboard to give users an idea of what to expect from compilation:

<http://picsl.upenn.edu/cdash/index.php?project=ANTS>

### 5.2 Visualization and Quantification of ANTs Results

Use **itk SNAP** : [www.itksnap.org](http://www.itksnap.org) or mricro / mricron for viewing images. The ANTs program StackSlices can be used to conveniently scan through a dataset in any of its axes. It is useful for checking both input data quality and output normalization quality. MeasureImageSimilarity will supply numerical measures of image similarity via three different metrics.

### 5.3 Statistics Beyond ANTs

Use SPM, **R** or npm (from Chris Rorden's mricron) for computing population statistics.

### 5.4 Pipelining with ANTs

Use PipeDream for automating large-scale processing:

**PipeDream Homepage** : <https://sourceforge.net/projects/neuropipedream/>

PipeDream is integrated with ANTs and automates more complex studies such as multivariate diffusion tensor and T1 cortical thickness studies, longitudinal mapping and reconstruction of nifti images from Dicom.

## 6 Annotated Bibliography

The original statement of the symmetric normalization and template construction methodology was given in [6] with a more recent template paper here [9]. A follow up study that used landmark guidance to compare the chimpanzee cortex to the human cortex was published here [8] – this study used *in vivo* MRI and template-based normalization to confirm volumetric numbers derived from an early 20th century post-mortem study comparing one human and one chimp. This conference article has some additional detail and alternative updates to the methodology, in particular application to shape-based interpolation [7]. Network based studies were performed here [20, 21]. The main SyN paper is here [13]. Applications to neurodegeneration are here [2, 11, 23, 14, 19, 41, 26]. Hippocampus focused work is here [29, 41]. The main evaluation papers include [13] and [25] for the cortex and deep brain structures whereas [29] evaluates the use of automated and semi-automated normalization for high-throughput hippocampus morphometry. An additional evaluation paper is being developed.

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