Computer Architecture and Operating Systems
Lecture 11: Memory and Caches

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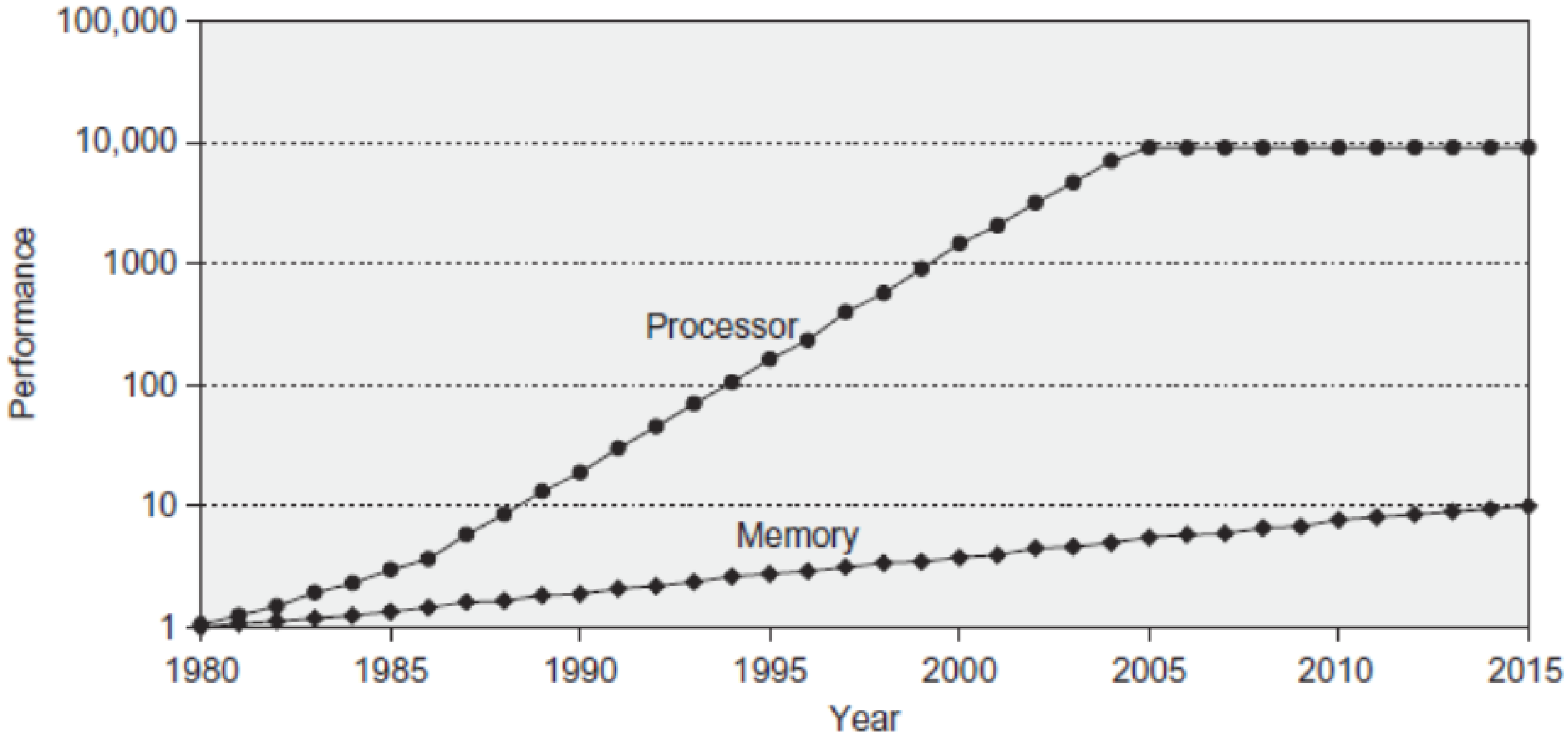
Processor-Memory Performance Gap

- Computer performance depends on:
  - Processor performance
  - Memory performance



Memory Challenge

- Make memory appear as fast as processor
- Ideal memory:
  - Fast
  - Cheap (inexpensive)
  - Large (capacity)

But can only choose two!

Memory Technology

- Static RAM (SRAM)
  - 0.5ns – 2.5ns, $2000 – $5000 per GB
- Dynamic RAM (DRAM)
  - 50ns – 70ns, $20 – $75 per GB
- Magnetic disk
  - 5ms – 20ms, $0.20 – $2 per GB
- Ideal memory
  - Access time of SRAM
  - Capacity and cost/GB of disk

Locality

No need for large memory to access it fast

Just exploit locality

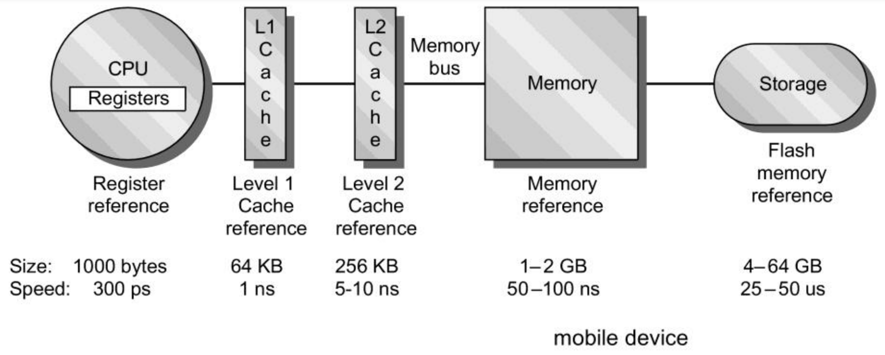
- Temporal Locality:
  - Locality in time
  - If data used recently, likely to use it again soon
  - How to exploit: keep recently accessed data in higher levels of memory hierarchy
- Spatial Locality:
  - Locality in space
  - If data used recently, likely to use nearby data soon
  - How to exploit: when access data, bring nearby data into higher levels of memory hierarchy too

Taking Advantage of Locality

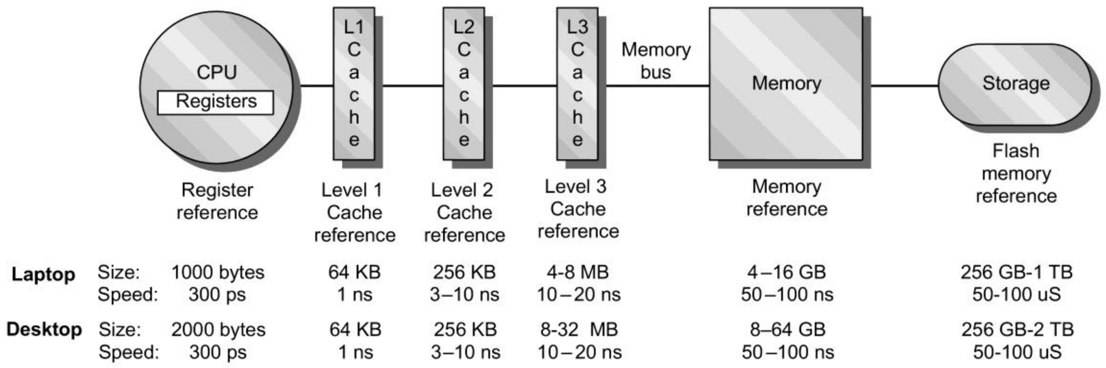
- Memory hierarchy
- Store everything on disk
- Copy recently accessed (and nearby) items from disk to smaller DRAM memory
  - Main memory
- Copy more recently accessed (and nearby) items from DRAM to smaller SRAM memory
  - Cache memory attached to CPU

Memory Hierarchy

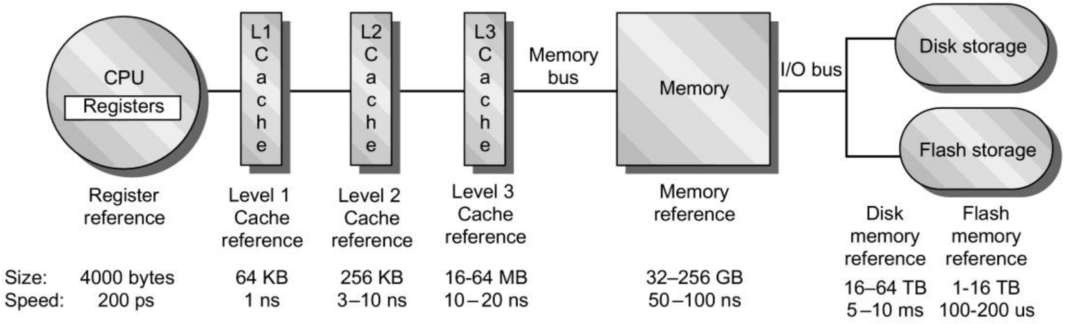
- Personal mobile device



- Laptop or desktop

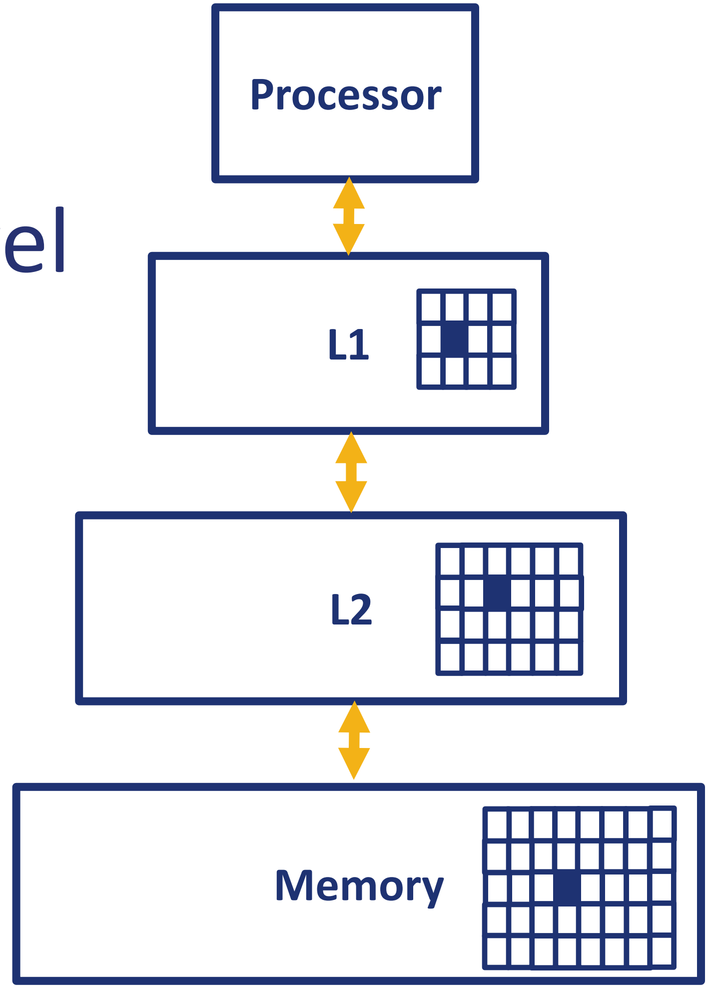


- Server



How It Works?

- **Block** (aka **line**): unit of copying
  - May be multiple words
- If accessed data is present in upper level
  - **Hit**: access satisfied by upper level
    - Hit ratio: hits/accesses
- If accessed data is absent
  - **Miss**: block copied from lower level
    - Time taken: miss penalty
    - Miss ratio: misses/accesses = 1 – hit ratio
  - Then accessed data supplied from upper level



Hits and Misses

- On cache hit, CPU proceeds normally
- On cache miss
  - Stall the CPU pipeline
  - Fetch block from next level of hierarchy
  - Instruction cache miss
    - Restart instruction fetch
  - Data cache miss
    - Complete data access

Miss Types

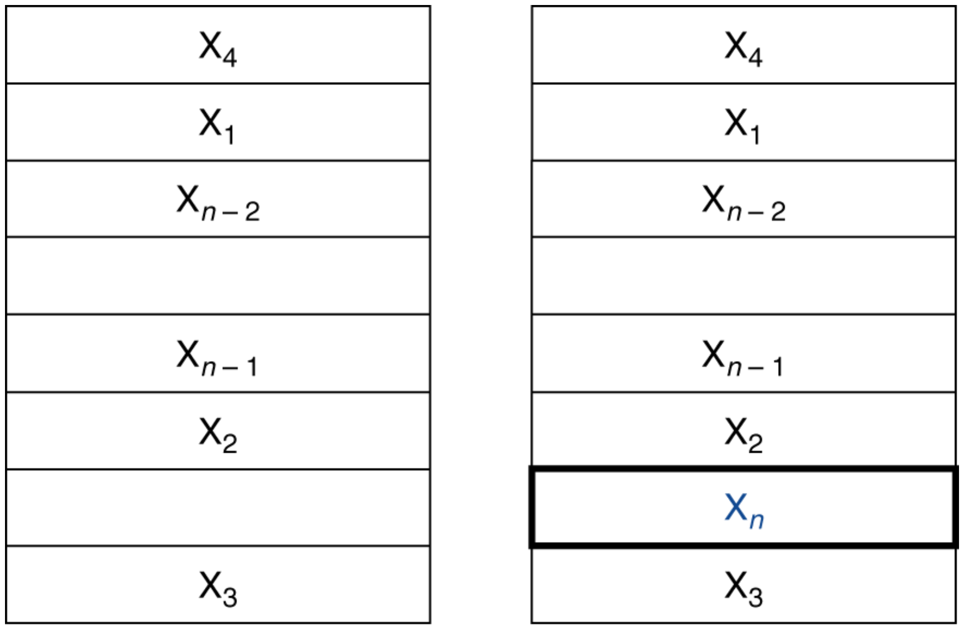
- **Compulsory**: first time data accessed
- **Capacity**: cache too small to hold all data of interest
- **Conflict**: data of interest maps to a location in cache mapped to different data

Memory Performance

- **Hit**: data found in that level of memory hierarchy
- **Miss**: data not found (must go to next level)
  - **Hit Rate** = # hits / # memory accesses = 1 – Miss Rate
  - **Miss Rate** = # misses / # memory accesses = 1 – Hit Rate
- **Average memory access time (AMAT):** average time for processor to access data
  - **AMAT** = $t_{cache} + MR_{cache}[t_{MM} + MR_{MM}(t_{VM})]$

Cache Memory

- Cache memory
  - The level of the memory hierarchy closest to the CPU
- Given accesses X_1, …, $X_{n–1}$, X_n

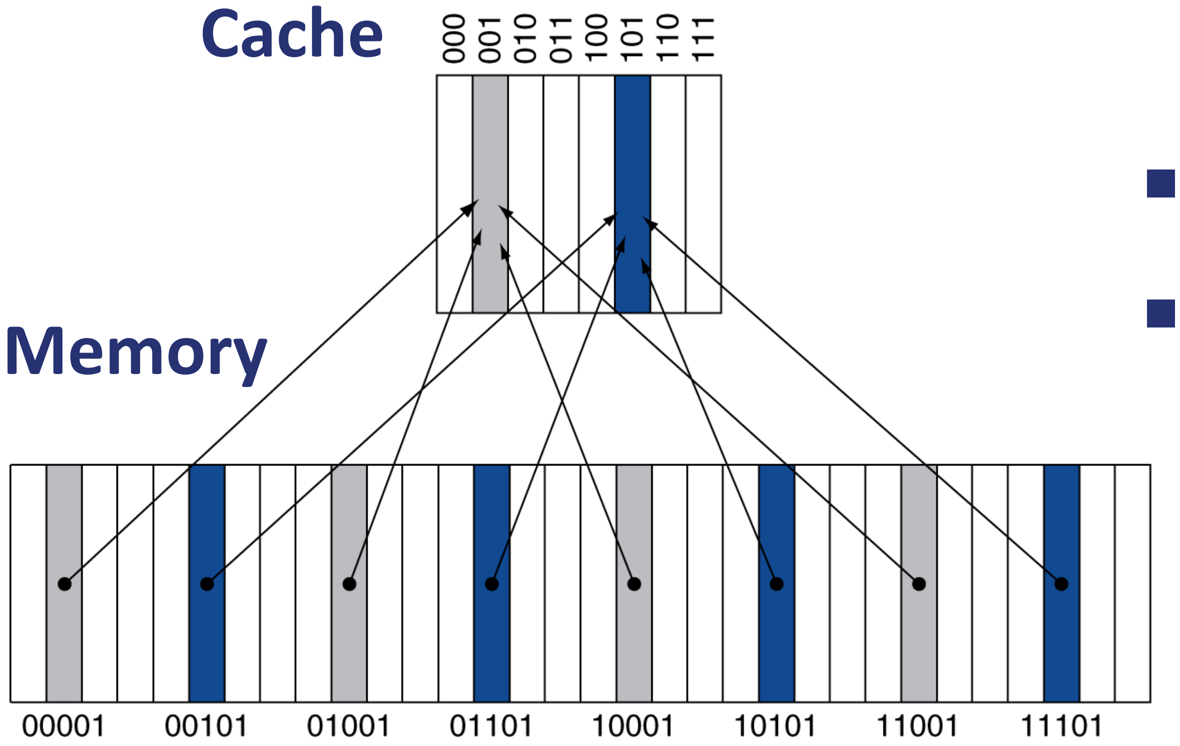


a. Before the reference to X_n b. After the reference to X_n

- How do we know if the data is present?
- Where do we look?

Direct Mapped Cache

- Location determined by address
- Direct mapped: only one choice
  - (Block address) modulo (#Blocks in cache)



- #Blocks is a power of 2
- Use low-order address bits

Tags and Valid Bits

- How do we know which particular block is stored in a cache location?
  - Store block address as well as the data
  - Actually, only need the high-order bits
  - Called the tag
- What if there is no data in a location?
  - Valid bit: 1 = present, 0 = not present
  - Initially 0

Direct Mapped Cache Example

- 8-blocks, 1 word/block, direct mapped
- Initial state

Index	V	Tag	Data
000	N		
001	N		
010	N		
011	N		
100	N		
101	N		
110	N		
111	N		

Direct Mapped Cache Example

Word addr	Binary addr	Hit/miss	Cache block
22	10 110	Miss	110

Index	V	Tag	Data
000	N		
001	N		
010	N		
011	N		
100	N		
101	N		
110	**Y**	**10**	**Mem[10110]**
111	N		

Direct Mapped Cache Example

Word addr	Binary addr	Hit/miss	Cache block
26	11 010	Miss	010

Index	V	Tag	Data
000	N		
001	N		
010	**Y**	**11**	**Mem[11010]**
011	N		
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Direct Mapped Cache Example

Word addr	Binary addr	Hit/miss	Cache block
22	10 110	Hit	110
26	11 010	Hit	010

Index	V	Tag	Data
000	N		
001	N		
010	**Y**	**11**	**Mem[11010]**
011	N		
100	N		
101	N		
110	**Y**	**10**	**Mem[10110]**
111	N		

Direct Mapped Cache Example

Word addr	Binary addr	Hit/miss	Cache block
16	10 000	Miss	000
3	00 011	Miss	011
16	10 000	Hit	000

Index	V	Tag	Data
000	**Y**	**10**	**Mem[10000]**
001	N		
010	Y	11	Mem[11010]
011	**Y**	**00**	**Mem[00011]**
100	N		
101	N		
110	**Y**	**10**	**Mem[10110]**
111	N		

Direct Mapped Cache Example

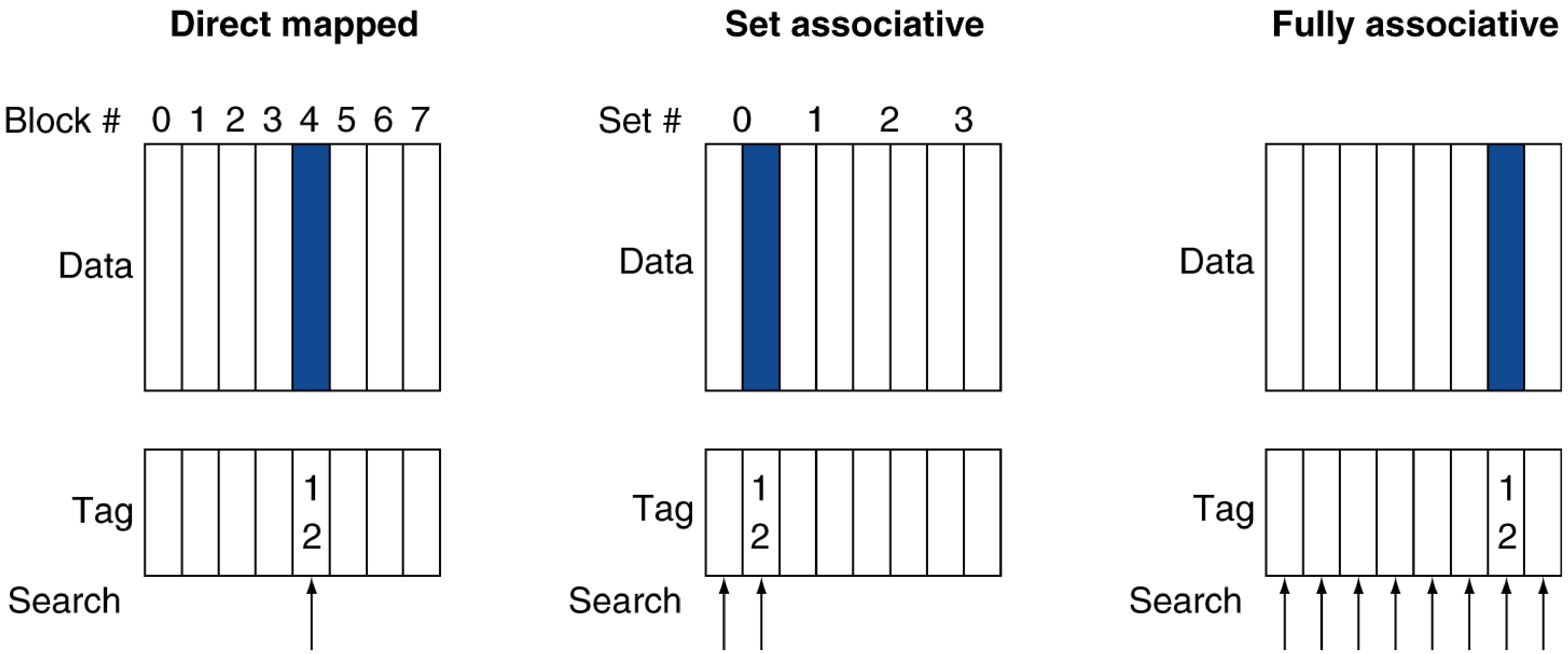
Word addr	Binary addr	Hit/miss	Cache block
18	10 010	Miss	010

Index	V	Tag	Data
000	Y	10	Mem[10000]
001	N		
010	**Y**	**10**	**Mem[10010]**
011	Y	00	Mem[00011]
100	N		
101	N		
110	Y	10	Mem[10110]
111	N		

Associative Caches

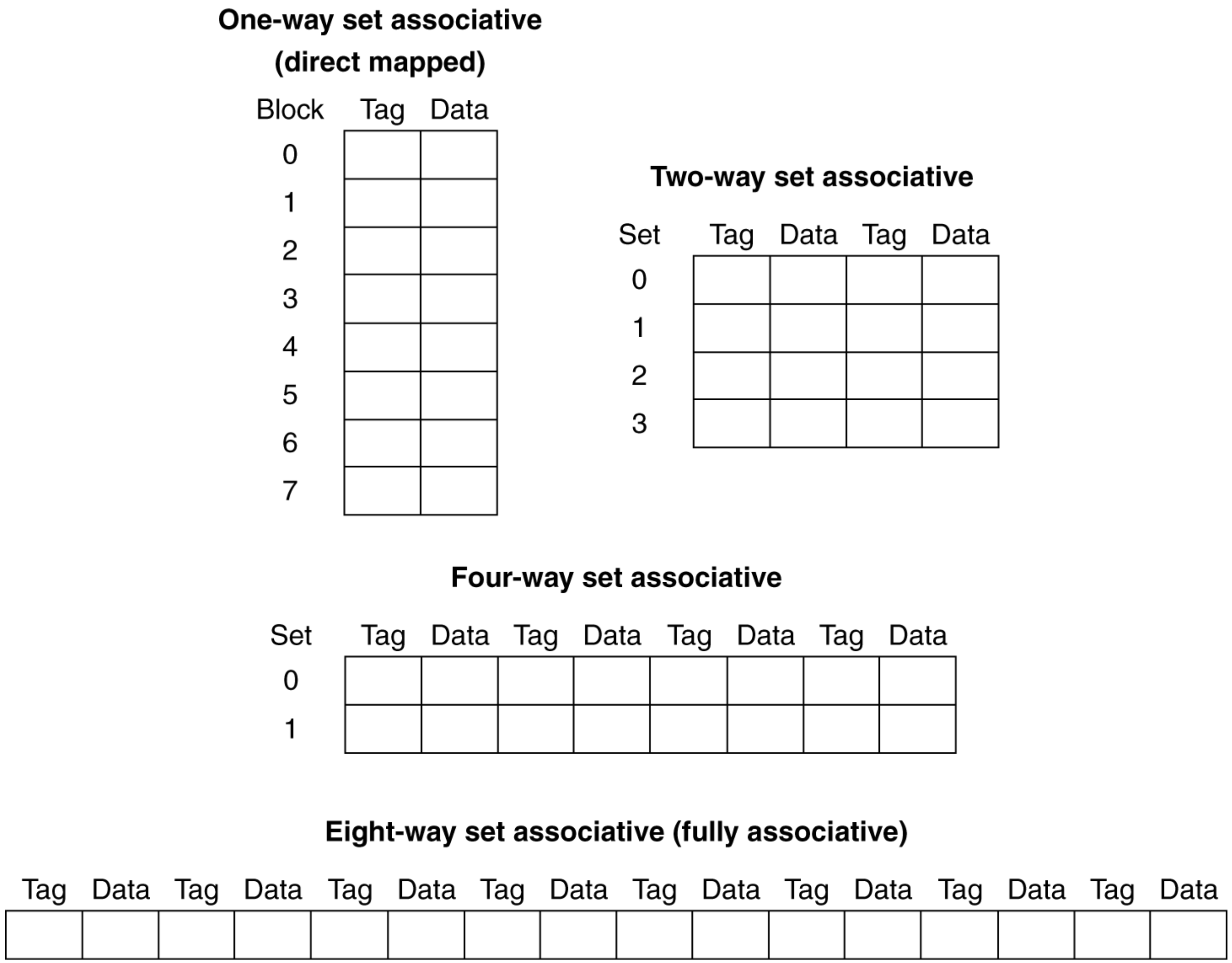
- Fully associative
  - Allow a given block to go in any cache entry
  - Requires all entries to be searched at once
  - Comparator per entry (expensive)
- *n*-way set associative
  - Each set contains *n* entries
  - Block number determines which set
    - (Block number) modulo (#Sets in cache)
  - Search all entries in a given set at once
  - *n* comparators (less expensive)

Associative Cache Examples



Spectrum of Associativity

- For a cache with 8 entries



How Much Associativity

- Increased associativity decreases miss rate
  - But with diminishing returns
- Simulation of a system with 64KB D-cache, 16-word blocks, SPEC2000
  - 1-way: 10.3%
  - 2-way: 8.6%
  - 4-way: 8.3%
  - 8-way: 8.1%

Replacement Policy

- Direct mapped
  - No choice
- Set associative
  - Prefer non-valid entry, if there is one
  - Otherwise, choose among entries in the set
- Least-recently used (LRU)
  - Choose the one unused for the longest time
    - Simple for 2-way, manageable for 4-way, too hard beyond that
- Random
  - Gives approximately the same performance as LRU for high associativity

Write-Through

- On data-write hit, could just update the block in cache
  - But then cache and memory would be inconsistent
- Write through: also update memory
- But makes writes take longer
  - e.g., if base CPI = 1, 10% of instructions are stores, write to memory takes 100 cycles
    - Effective CPI = 1 + 0.1×100 = 11
- Solution: write buffer
  - Holds data waiting to be written to memory
  - CPU continues immediately
    - Only stalls on write if write buffer is already full

Write-Back

- Alternative: On data-write hit, just update the block in cache
  - Keep track of whether each block is dirty
- When a dirty block is replaced
  - Write it back to memory
  - Can use a write buffer to allow replacing block to be read first

Write Allocation

- What should happen on a write miss?
- Alternatives for write-through
  - Allocate on miss: fetch the block
  - Write around: don't fetch the block
    - Since programs often write a whole block before reading it (e.g., initialization)
- For write-back
  - Usually fetch the block

Any Questions?

```
            .text
__start:    addi t1, zero, 0x18
            addi t2, zero, 0x21
cycle:      beq t1, t2, done
            slt t0, t1, t2
            bne t0, zero, if_less
            nop
            sub t1, t1, t2
            j cycle
            nop
if_less:    sub t2, t2, t1
            j cycle
done:       add t3, t1, zero
```