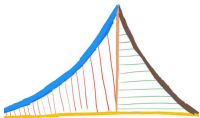


# Digital Design Through Arduino

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## ABOUT THIS BOOK

This book provides a simple introduction to digital design using the Arduino framework. It is suitable for students ranging from primary school to college. The content is sufficient for industry jobs. There is no copyright, so readers are free to print and share.

July 10, 2024

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and

<https://www.gnu.org/licenses/fdl-1.3.en.html>

First manual appeared in 2015

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## 1 INSTALLATION

### 1.1 Termux

1. On your android device, follow the instructions in

```
https://github.com/gadepall/fwc-1
```

to setup and install Debian on Termux.

### 1.2 Platformio

1. Install Packages

```
apt install avra avrdude gcc-avr avr-libc
```

2. Follow the instructions in

```
https://docs.platformio.org/en/stable/core/installation/methods/installer-script.html#super-quick-macos-linux
```

to install platformio.

3. Execute the following on debian

```
cd ide/piosetup/codes  
pio run
```

4. Connect your arduino to the laptop/rpi and type

```
pio run -t nobuild -t upload
```

5. The LED beside pin 13 will start blinking

### 1.3 Arduino Droid

1. Install ArduinoDroid from apkpure
2. Open ArduinoDroid and grant all permissions
3. Connect the Arduino to your phone via USB-OTG
4. For flashing the bin files, in ArduinoDroid,

```
Actions->Upload->Upload Precompiled
```

then go to your working directory and select

```
pio/build/uno/firmware.hex
```

for uploading hex file to the Arduino Uno

5. The LED beside pin 13 will start blinking

## 2 SEVEN SEGMENT DISPLAY

We show how to control a seven segment display.

### 2.1 Components

Component	Value	Quantity
Resistor	220 Ohm	1
Arduino		1
Seven Segment Display		1
Decoder	7447	1
Flip Flop	7474	2
Jumper Wires		20

TABLE 2.1: Components

1. Breadboard: The breadboard can be divided into 5 segments. In each of the green segments, the pins are internally connected so as to have the same voltage. Similarly, in the central segments, the pins in each column are internally connected in the same fashion as the blue columns.
2. Seven Segment Display: The seven segment display in Fig. 2.2 has eight pins, *a, b, c, d, e, f, g* and *dot* that take an active LOW input, i.e. the LED will glow only if the input is connected to ground. Each of these pins is connected to an LED segment. The *dot* pin is reserved for the  $\cdot$  LED.
3. Arduino: The Arduino Uno has some ground pins, analog input pins A0-A3 and digital pins D1-D13 that can be used for both input as well as output. It also has two power pins that can generate 3.3V and 5V. In the following exercises, only the GND, 5V and digital pins will be used.

### 2.2 Display Control through Hardware

#### 2.2.1 Powering the Display:

1. Plug the display to the breadboard in Fig. 2.1 and make the connections in Table 2.2. Henceforth, all 5V and GND connections will be made from the breadboard.

Arduino	Breadboard
5V	Top Green
GND	Bottom Green

TABLE 2.2: Supply for Bread board

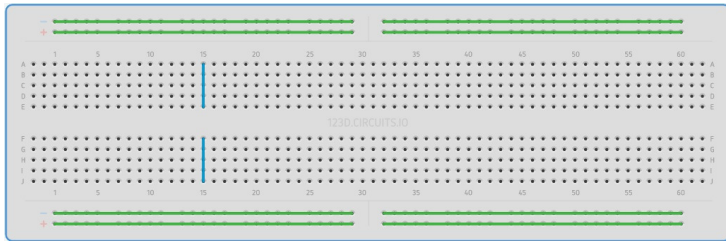


Fig. 2.1: Bread board connections

2. Make the connections in Table 2.3.

Breadboard		Display
5V	Resistor	COM
GND		DOT

TABLE 2.3: Connecting Seven segment display on Bread board

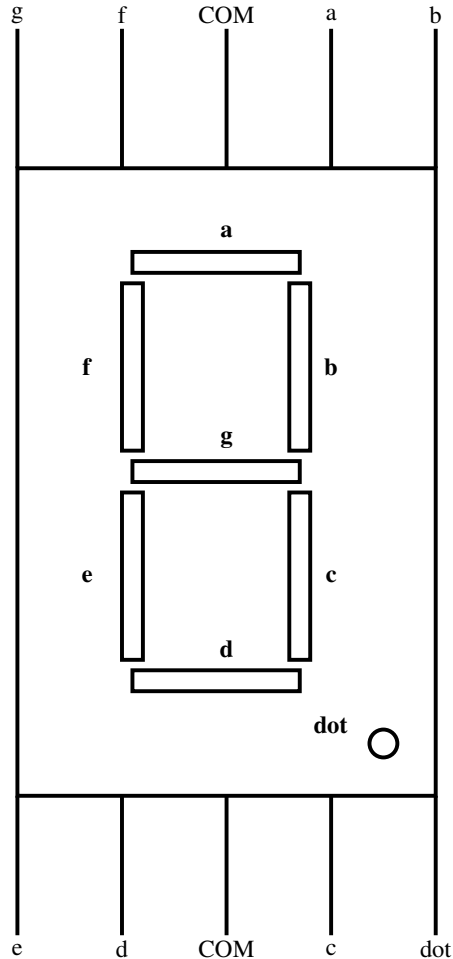


Fig. 2.2: Seven Segment pins

- 3. Connect the Arduino to the computer. The DOT led should glow.
- 2.2.2 *Controlling the Display:* Fig. 2.3 explains how to get decimal digits using the seven segment display. GND=0.
- 1. Generate the number 1 on the display by connecting only the pins *b* and *c* to GND (=0). This corresponds to the first row of 2.4. 1 means not connecting to GND.
- 2. Repeat the above exercise to generate the number 2 on the display.
- 3. Draw the numbers 0-9 as in Fig. 2.3 and complete Table 2.4

a	b	c	d	e	f	g	decimal
0	0	0	0	0	0	1	0

TABLE 2.4



<b>Arduino</b>	2	3	4	5	6	7	8
<b>Display</b>	a	b	c	d	e	f	g

TABLE 2.5

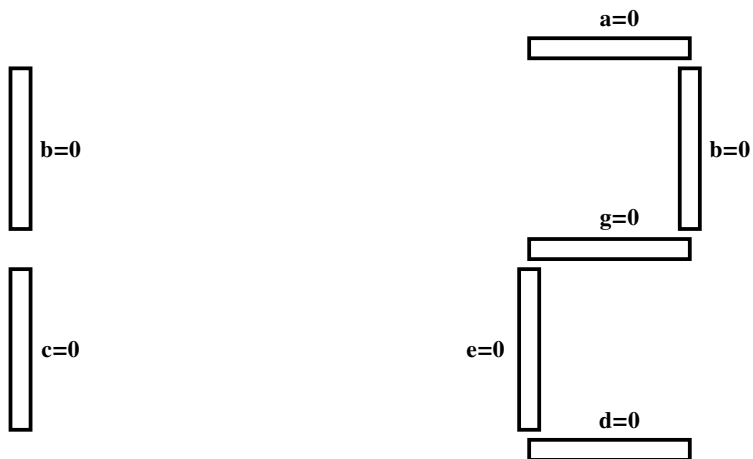


Fig. 2.3: Seven Segment connections

### 2.3 Display Control through Software

1. Make connections according to Table 2.5
2. Download the following code using the arduino IDE and execute

```
ide/sevenseg/codes/sevenseg/sevenseg.cpp
```

3. Now generate the numbers 0-9 by modifying the above program.

## 3 7447

Here we show how to use the 7447 BCD-Seven Segment Display decoder to learn Boolean logic.

## 3.1 Hardware

1. Make connections between the seven segment display in Fig. 2.2 and the 7447 IC in Fig. 3.1 as shown in Table 3.2

Component	Value	Quantity
Resistor	220 Ohm	1
Arduino	UNO	1
Seven Segment Display		1
Decoder	7447	1
Jumper Wires	M-M	20
Breadboard		1

TABLE 3.1: 7447 components

7447	$\bar{a}$	$\bar{b}$	$\bar{c}$	$\bar{d}$	$\bar{e}$	$\bar{f}$	$\bar{g}$
Display	a	b	c	d	e	f	g

TABLE 3.2

2. Make connections to the lower pins of the 7447 according to Table 3.3 and connect  $V_{CC} = 5V$ . You should see the number 0 displayed for 0000 and 1 for 0001.

D	C	B	A	Decimal
0	0	0	0	0
0	0	0	1	1

TABLE 3.3

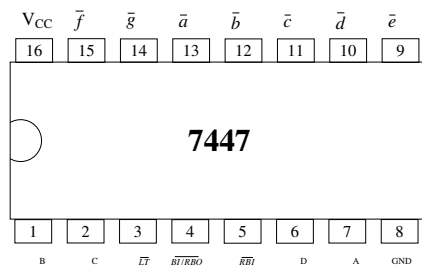


Fig. 3.1

3. Complete Table 3.3 by generating all numbers between 0-9.

Z	Y	X	W	D	C	B	A
0	0	0	0	0	0	0	1
0	0	0	1	0	0	1	0
0	0	1	0	0	0	1	1
0	0	1	1	0	1	0	0
0	1	0	0	0	1	0	1
0	1	0	1	0	1	1	0
0	1	1	0	0	1	1	1
0	1	1	1	1	0	0	0
1	0	0	0	1	0	0	1
1	0	0	1	0	0	0	0

TABLE 3.5: Truth table for incrementing Decoder.

### 3.2 Software

1. Now make the connections as per Table 3.4 and execute the following program

```
ide/7447/codes/gvv_ard_7447/gvv_ard_7447.cpp
```

7447	D	C	B	A
Arduino	5	4	3	2

TABLE 3.4

In the truth table in Table 3.5,  $W, X, Y, Z$  are the inputs and  $A, B, C, D$  are the outputs. This table represents the system that increments the numbers 0-8 by 1 and resets the number 9 to 0. Note that  $D = 1$  for the inputs 0111 and 1000. Using *boolean* logic,

$$D = WXYZ' + W'X'Y'Z \quad (3.1)$$

Note that 0111 results in the expression  $WXYZ'$  and 1000 yields  $W'X'Y'Z$ .

2. The code below realizes the Boolean logic for B, C and D in Table 3.5. Write the logic for A and verify.

```
ide/7447/codes/inc_dec/inc_dec.ino
```

3. Now make additional connections as shown in Table 3.6 and execute the following code. Comment.

```
ide/7447/codes/ip_inc_dec/ip_inc_dec.cpp
```

**Solution:** In this exercise, we are taking the number 5 as input to the arduino and displaying it on the seven segment display using the 7447 IC.

	Z	Y	X	W
<b>Input</b>	0	1	0	1
<b>Arduino</b>	9	8	7	6

TABLE 3.6

4. Verify the above code for all inputs from 0-9.
5. Now write a program where
  - a) the binary inputs are given by connecting to 0 and 1 on the breadboard
  - b) incremented by 1 using Table 3.5 and
  - c) the incremented value is displayed on the seven segment display.
6. Write the truth table for the 7447 IC and obtain the corresponding boolean logic equations.
7. Implement the 7447 logic in the arduino. Verify that your arduino now behaves like the 7447 IC.

### 3.3 Problems

1. Obtain the Boolean Expression for the Logic circuit shown below in Fig. 3.2. (CBSE 2013)

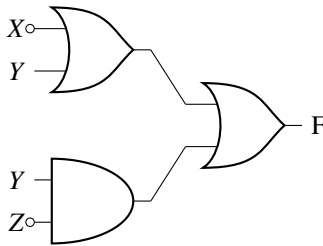


Fig. 3.2

2. Verify the Boolean Expression (CBSE 2013)

$$A + C = A + A'C + BC \quad (3.2)$$

3. Draw the Logic Circuit for the following Boolean Expression (CBSE 2015)

$$f(x, y, z, w) = (x' + y)z + w' \quad (3.3)$$

4. Verify the following (CBSE 2015)

$$U' + V = U'V' + U'V + UV \quad (3.4)$$

5. Draw the Logic Circuit for the given Boolean Expression (CBSE 2015)

$$(U + V')W' + Z \quad (3.5)$$

6. Verify the following using Boolean Laws (CBSE 2015)

$$X + Y' = XY + XY' + X'Y' \quad (3.6)$$

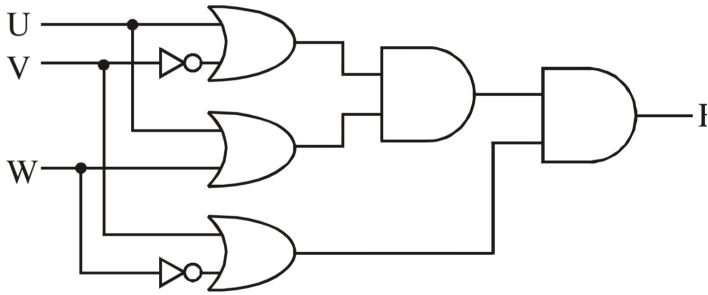


Fig. 3.3

7. Write the Boolean Expression for the result of the Logic Circuit as shown in Fig. 3.3 (CBSE 2016)
8. Draw the logic circuit of the following Boolean Expression using only NAND Gates. (CBSE 2017)

$$XY + YZ \quad (3.7)$$

9. Draw the Logic Circuit of the following Boolean Expression using only NOR Gates (CBSE 2017)

$$(A + B)(C + D) \quad (3.8)$$

10. Draw the Logic Circuit of the following Boolean Expression (CBSE 2018)

$$(U' + V)(V' + W') \quad (3.9)$$

11. Derive a Canonical POS expression for a Boolean function F, represented by Table 3.7 (CBSE 2019)

X	Y	Z	F(X,Y,Z)
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	0

TABLE 3.7

12. For the logic circuit shown in Fig. 3.4, find the simplified Boolean expression for the output. (GATE EC 2000)

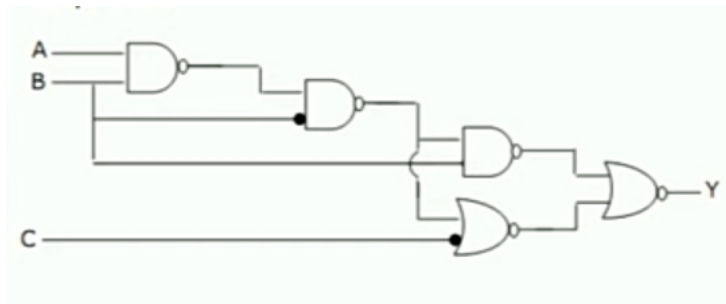


Fig. 3.4

13. Obtain the Boolean Expression for the Logic circuit shown below in Fig. 3.5. (GATE EC 1993)

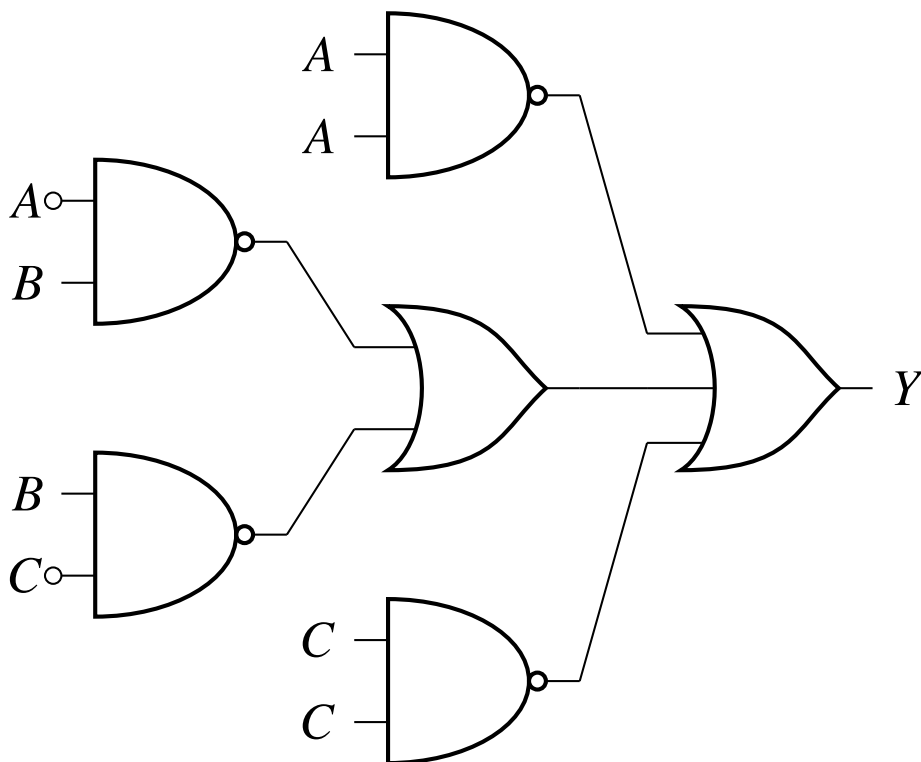


Fig. 3.5

14. Implement Table 3.8 using XNOR logic.

(GATE EC 1993)

A	B	Y
0	0	1
0	1	0
1	0	0
1	1	1

TABLE 3.8

15. For a binary half-sub-tractor having two inputs A and B, find the correct set of logical expressions for the outputs D (=A minus B) and X (=borrow). (GATE EC 1999)
16. Find X in the following circuit in Fig. 3.6 (GATE EC 2007)

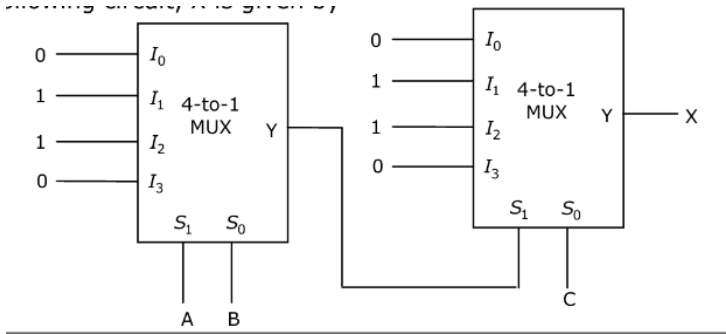


Fig. 3.6

17. A logic circuit implements the boolean function  $F = X' \cdot Y + X \cdot Y' \cdot Z'$ . It is found that the input combination  $X=Y=1$  can never occur. Taking this into account, find a simplified expression for F. (GATE IN 2007)
18. Find the Boolean logic realised by the following circuit in Fig. 3.7 (GATE EC 2010)

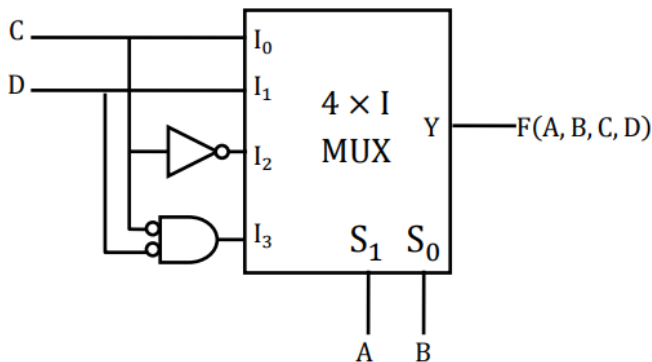


Fig. 3.7

19. Find the logic function implemented by the circuit given below in Fig. 3.8 (GATE EC 2011)

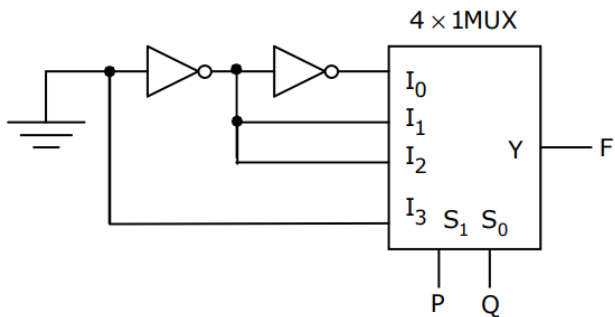


Fig. 3.8

20. Find F in the Digital Circuit given in the figure below in Fig. 3.9. (GATE IN 2016)

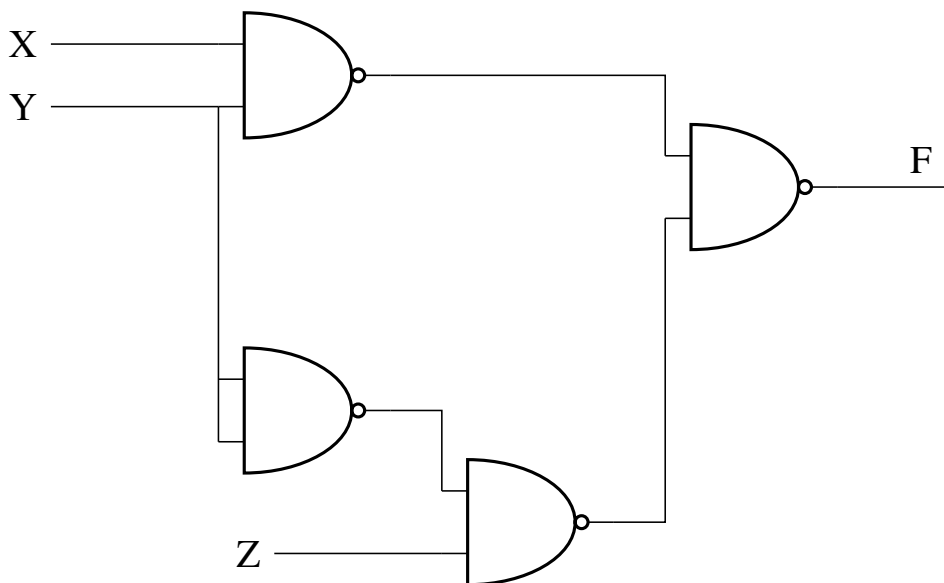


Fig. 3.9

21. Find the logic function implemented by the circuit given below in Fig. 3.10 (GATE EC 2017)



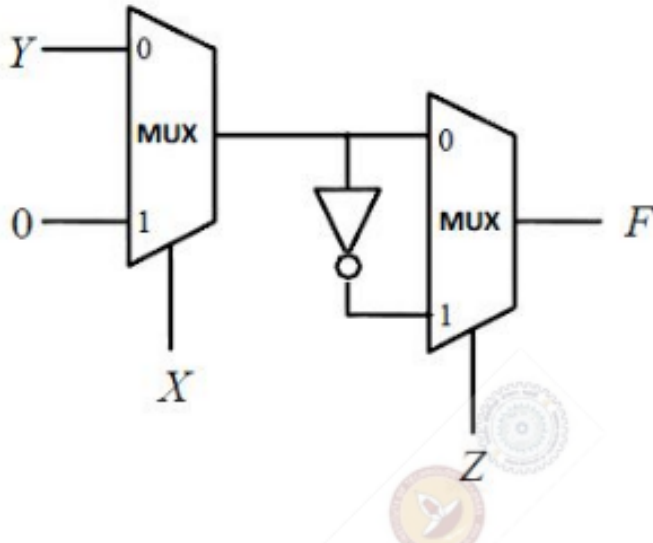


Fig. 3.10

22. Find the logic function implemented by the circuit given below in Fig. 3.11 (GATE EC 2018)

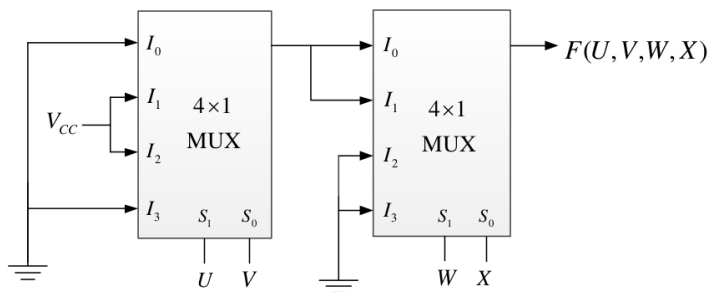


Fig. 3.11

23. Find the logic function implemented by the circuit given below in Fig. 3.12 (GATE EE 2018)

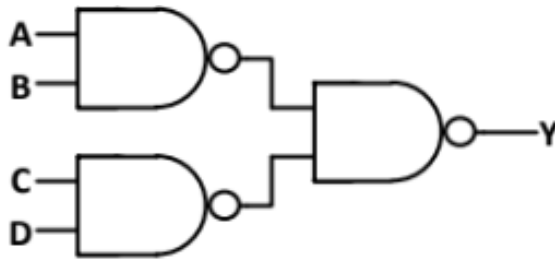


Fig. 3.12

24. Find the logic function implemented by the circuit given below in Fig. 3.13 (GATE EE 2019)

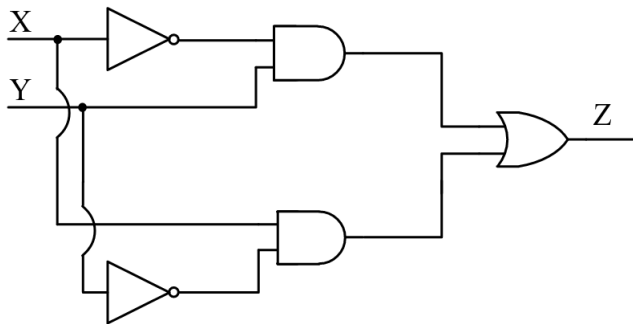


Fig. 3.13

25. Let  $\oplus$  and  $\odot$  denote the Exclusive OR and Exclusive NOR operations, respectively. Which one of the following is NOT CORRECT ? 25 (GATE CS 2018)

- (A)  $\overline{P \oplus Q} = P \odot Q$   
 (B)  $\overline{P \oplus Q} = P \odot Q$   
 (C)  $\overline{P \oplus Q} = P \oplus Q$   
 (D)  $(P \oplus \overline{P}) \oplus Q = (P \odot \overline{P}) \odot \overline{Q}$
26. A Boolean digital circuit is composed using two 4-input multiplexers ( $M1$  and  $M2$ ) and one 2-input multiplexer ( $M3$ ) as shown in the Fig. 3.14.  $X_0$ – $X_7$  are the inputs of the multiplexers  $M1$  and  $M2$  and could be connected to either 0 or 1. The select lines of the multiplexers are connected to Boolean variables  $A$ ,  $B$  and  $C$  as shown.

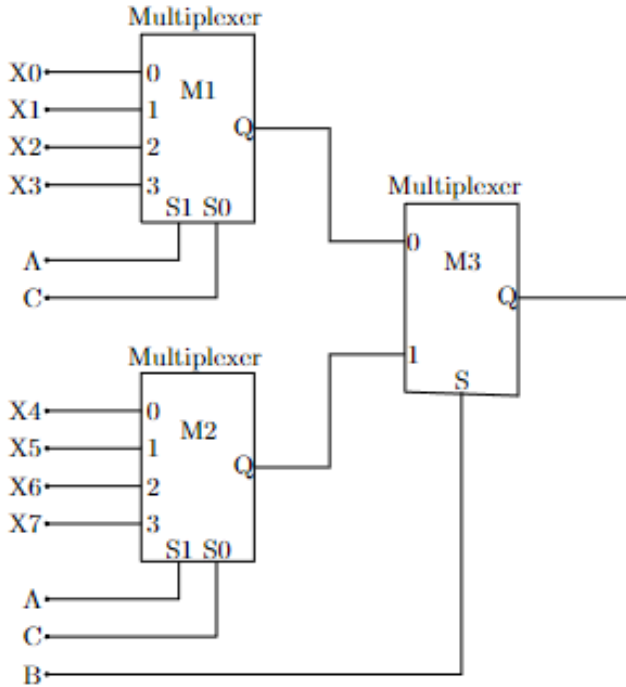


Fig. 3.14: Digital Circuit

Which one of the following set of values of  $(X_0, X_1, X_2, X_3, X_4, X_5, X_6, X_7)$  will realise the Boolean function  $\bar{A} + \bar{A}.\bar{C} + A.\bar{B}.C$  ? (GATE CS2023,44)

- a) (1, 1, 0, 0, 1, 1, 1, 0)
- b) (1, 1, 0, 0, 1, 1, 0, 1)
- c) (1, 1, 0, 1, 1, 1, 1, 0)
- d) (0, 0, 1, 1, 0, 1, 1, 1)

27. For the given digital circuit in Fig. 3.15,  $A = B = 1$ . Assume that AND, OR, and NOT gates have propagation delays of 10ns, 10ns, and 5ns respectively. All lines have zero propagation delay. Given that  $C = 1$  when the circuit is turned on, the frequency of steady-state oscillation of the output  $Y$  is \_\_\_\_\_. (GATE IN 2023)

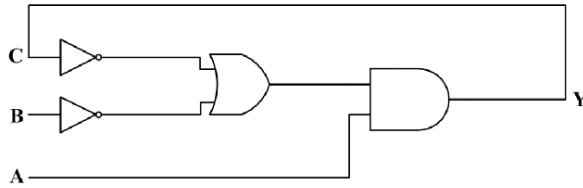


Fig. 3.15: Image

- a) 20MHz
- b) 15MHz
- c) 40MHz
- d) 50MHz

28. Select the Boolean function(s) equivalent to  $x + yz$ , where  $x, y$ , and  $z$  are Boolean variables, and  $+$  denotes logical OR operation. (GATE EC 2022)

- (A)  $x + z + xy$
- (B)  $(x + y)(x + z)$
- (C)  $x + xy + yz$
- (D)  $x + xz + xy$

29. Which one of the following options is CORRECT for the given circuit in Fig. 3.16? (GATE PHYSICS 2023)

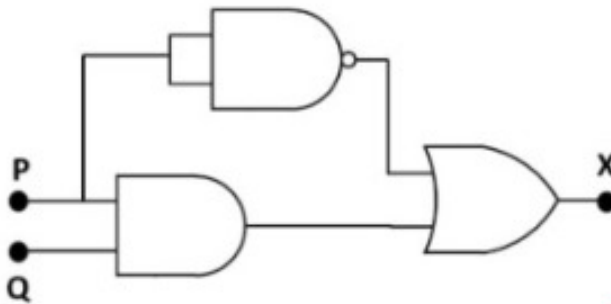


Fig. 3.16

- (A)  $P = 1, Q = 1 ; X = 0$
- (B)  $P = 1, Q = 0 ; X = 1$
- (C)  $P = 0, Q = 1 ; X = 0$
- (D)  $P = 0, Q = 0 ; X = 1$

30. In the circuit diagram shown below in Fig. 3.17, the logic gates operate with a supply voltage of 1V. NAND and XNOR have 200ps and 400ps input-to-output delay, respectively.

At time  $t = T$ ,  $A(t) = 0$ ,  $B(t) = 1$  and  $Z(t) = 0$ . When the inputs are changed to  $A(t) = 1$ ,  $B(t) = 0$  at  $t = 2T$ , a 1 V pulse is observed at Z. the pulse width of the 1V pulse is ps.

(GATE BM 2022)

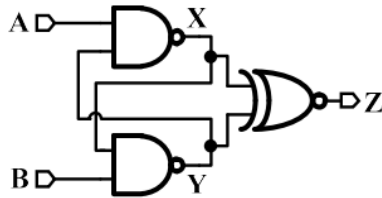


Fig. 3.17

- a) 100
- b) 200
- c) 400
- d) 600

31. Consider a Boolean gate (D) where the output (Y) is related to the inputs (A) and (B) as,  $Y = A + B$ , where + denotes logical OR operation. The Boolean inputs '0' and '1' are also available separately. Using instances of only D gates and inputs '0' and '1', (select the correct option(s)). (GATE EC 2022)

- a) NAND logic can be implemented
- b) OR logic cannot be implemented
- c) NOR logic can be implemented
- d) AND logic cannot be implemented.

32. Let  $R1$  and  $R2$  be two 4-bit registers that store numbers in 2's complement form. For the operation  $R1 + R2$ , which one of the following values of  $R1$  and  $R2$  gives an arithmetic overflow? (GATE CS 2022)

- a)  $R1 = 1011$  and  $R2 = 1110$
- b)  $R1 = 1100$  and  $R2 = 1010$
- c)  $R1 = 0011$  and  $R2 = 0100$
- d)  $R1 = 1001$  and  $R2 = 1111$

33. The maximum clock frequency in MHz of a 4-stage ripple counter, utilize flip-flops, with each flip-flop having a propagation delay of 20 ns, is \_\_\_\_\_. (round off to one decimal place) (GATE EE 2022)

34. The logic block shown in Fig. 3.18 has an output  $F$  given by \_\_\_\_\_. (GATE IN 2021)

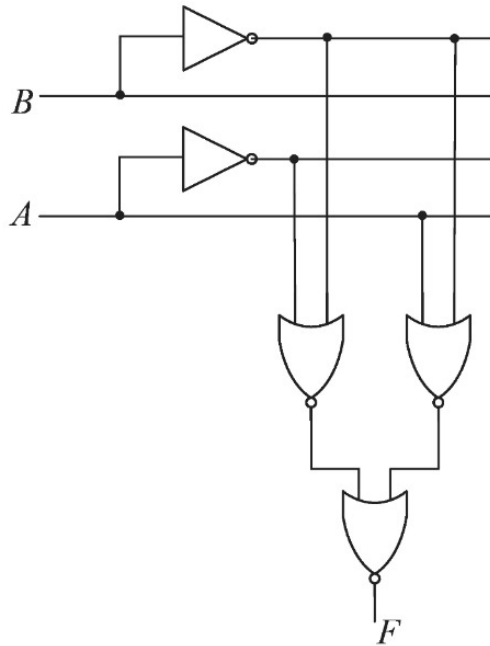


Fig. 3.18

- a)  $A + B$
- b)  $A \cdot \bar{B}$
- c)  $A + \bar{B}$
- d)  $\bar{B}$

35. Consider the following Boolean expression

$$F = (X + Y + Z)(\bar{X} + Y)(\bar{Y} + Z)$$

Which of the following Boolean expressions is/are equivalent to  $\bar{F}$  (complement of F)?

(Gate CS 2021,42)

- a)  $(\bar{X} + \bar{Y} + \bar{Z})(X + \bar{Y})(Y + \bar{Z})$
- b)  $X\bar{Y} + \bar{Z}$
- c)  $(X + \bar{Z})(\bar{Y} + \bar{Z})$
- d)  $X\bar{Y} + Y\bar{Z} + \bar{X}\bar{Y}\bar{Z}$

36. The propagation delays of the XOR gate, AND gate and multiplexer (MUX) in the circuit shown in Fig. 3.19 are  $4ns$ ,  $2ns$  and  $1ns$ , respectively. If all the inputs  $P, Q, R, S$  and  $T$  are applied simultaneously and held constant, the maximum propagation delay of the circuit is

(GATE-EC2021,31)

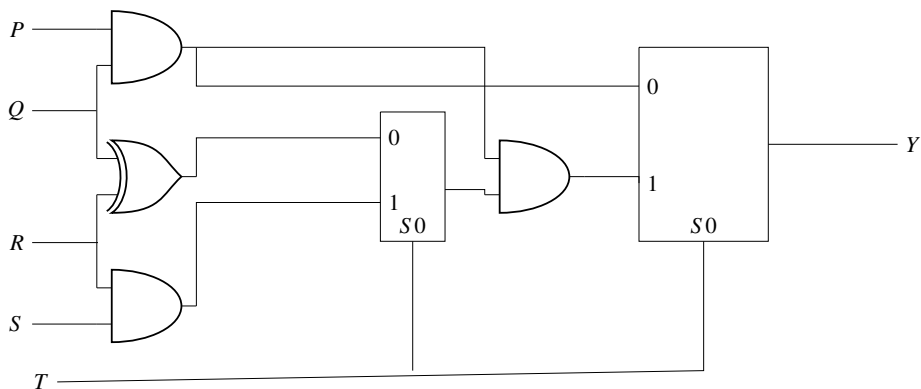


Fig. 3.19: circuit daigram

- a)  $3ns$
- b)  $5ns$
- c)  $6ns$
- d)  $7ns$

37. The following combination of logic gates in Fig. 3.20 represent the operation (GATE PH 2021)

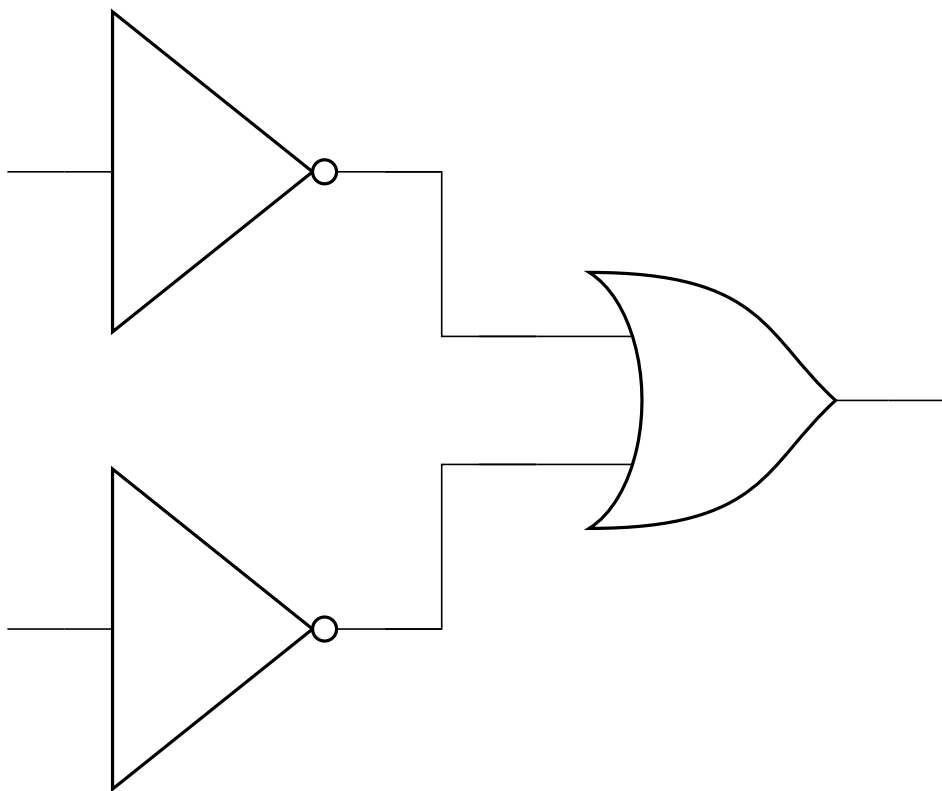


Fig. 3.20: combination circuit

- a) OR
- b) NAND
- c) AND
- d) NOR

38. Consider the boolean Function  $z(a, b, c)$  from below Fig. 3.21.

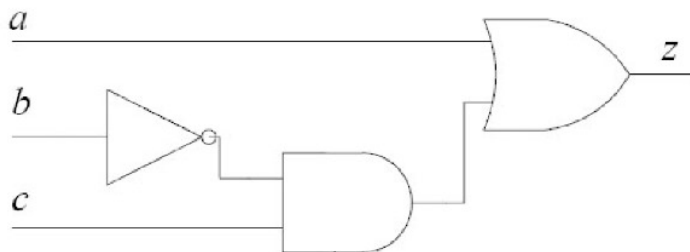


Fig. 3.21: circuit diagram



Which of the following minterm lists represent the circuit given above?

- a)  $z = \Sigma(0, 1, 3, 7)$
- b)  $z = \Sigma(1, 4, 5, 6, 7)$
- c)  $z = \Sigma(2, 4, 5, 6, 7)$
- d)  $z = \Sigma(2, 3, 5)$

39. In the latch circuit shown in Fig. 3.22, the NAND gates have non-zero but unequal propagation delays. The present input condition is:  $P = Q = '0'$ . If the input condition is changed simultaneously to  $P = Q = '1'$ , the outputs  $X$  and  $Y$  are

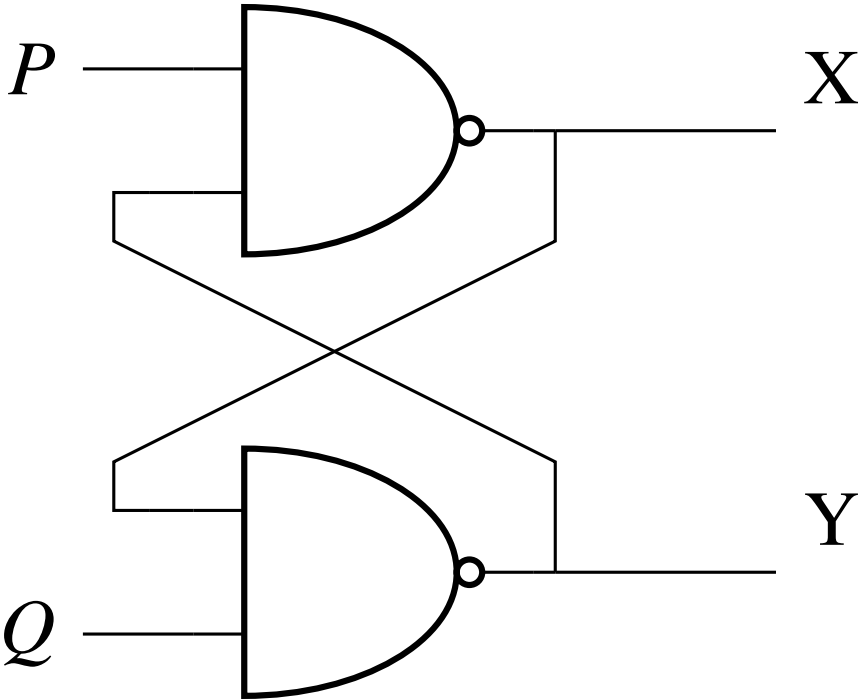


Fig. 3.22

- a)  $X = '1', Y = '1'$
- b) either  $X = '1', Y = '0'$  or  $X = '0', Y = '1'$
- c) either  $X = '1', Y = '1'$  or  $X = '0', Y = '0'$
- d)  $X = '0', Y = '0'$

(GATE EC 2017)

40. Consider three 4-variable functions  $f_1, f_2$ , and  $f_3$ , which are expressed in sum-of-minterms as

$$f_1 = \Sigma(0, 2, 5, 8, 14), \quad f_2 = \Sigma(2, 3, 6, 8, 14, 15), \quad f_3 = \Sigma(2, 7, 11, 14)$$

For the following circuit in Fig. 3.23 with one AND gate and one XOR gate, the output function  $f$  can be expressed as:

(GATE-CS2019,30)

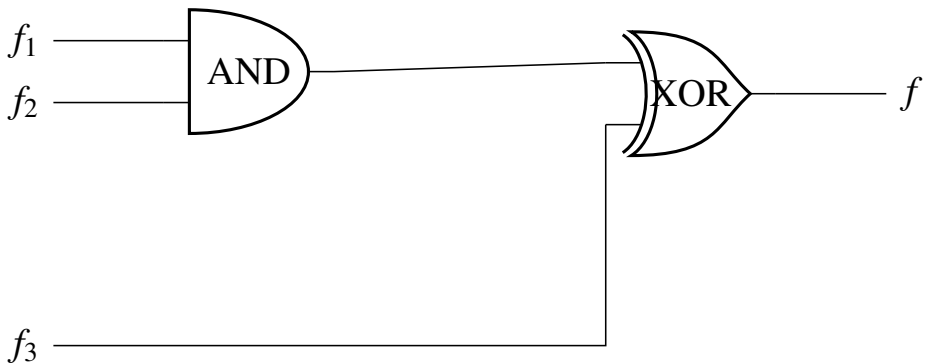


Fig. 3.23: Circuit Daigram

- a)  $\sum (7, 8, 11)$
- b)  $\sum (2, 7, 8, 11, 14)$
- c)  $\sum (2, 14)$
- d)  $\sum (0, 2, 3, 5, 6, 7, 8, 11, 14, 15)$

41. In the circuit shown in Fig. 3.24, what are the values of  $F$  for  $EN = 0$  and  $EN = 1$ , respectively? (GATE-EC2019,14)

- a) 0 and  $D$
- b)  $Hi - Z$  and  $D$
- c) 0 and 1
- d)  $Hi - Z$  and  $\overline{D}$

42. In the circuit shown in Fig. 3.25,  $A$  and  $B$  are the inputs and  $F$  is the output. What is the functionality of the circuit? (GATE-EC2019,15)

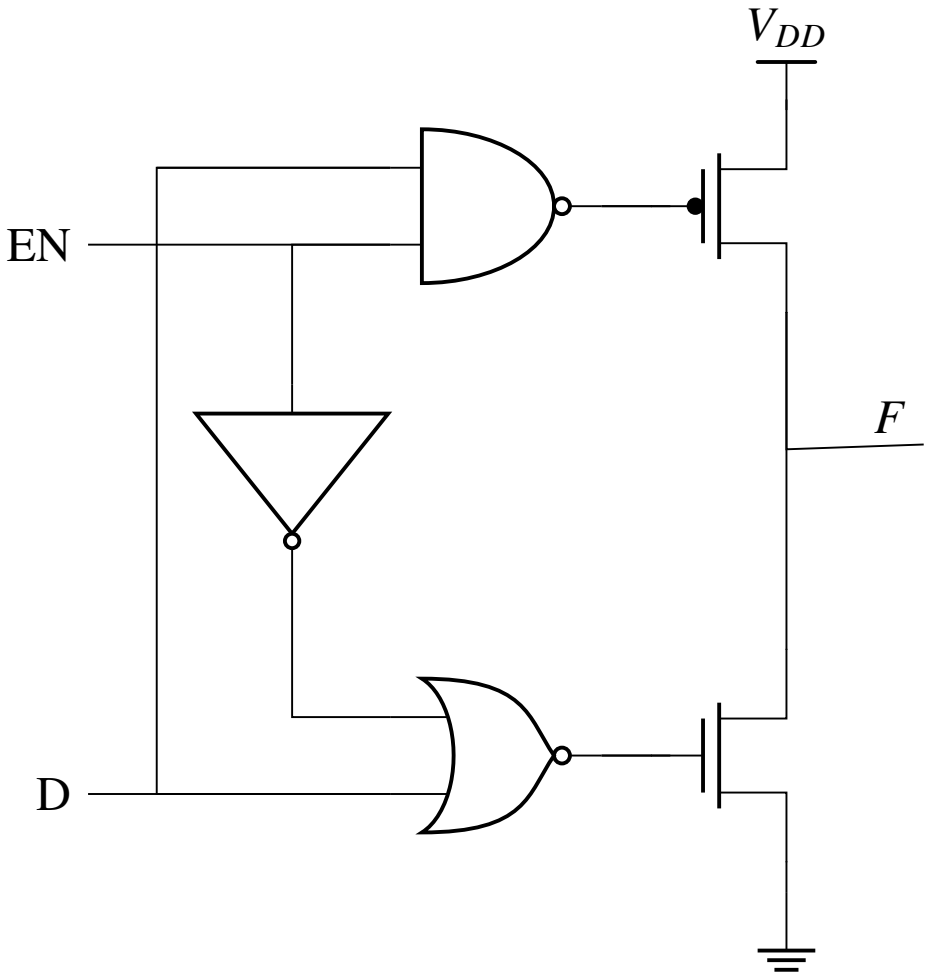
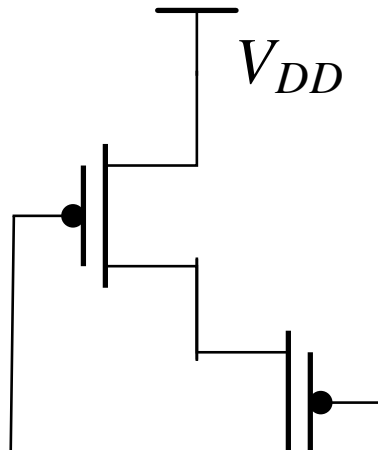


Fig. 3.24: Circuit Diagram



- a) Latch
- b) XNOR
- c) SRAM Cell
- d) XOR

43. In the circuit shown below in Fig. 3.26, assume that the comparators are ideal and all components have zero propagation delay. In one period of the input signal  $V_{in} = 6 \sin(\omega t)$ , the fraction of the time for which the output OUT is in logic HIGH is (GATE-IN2019,34)

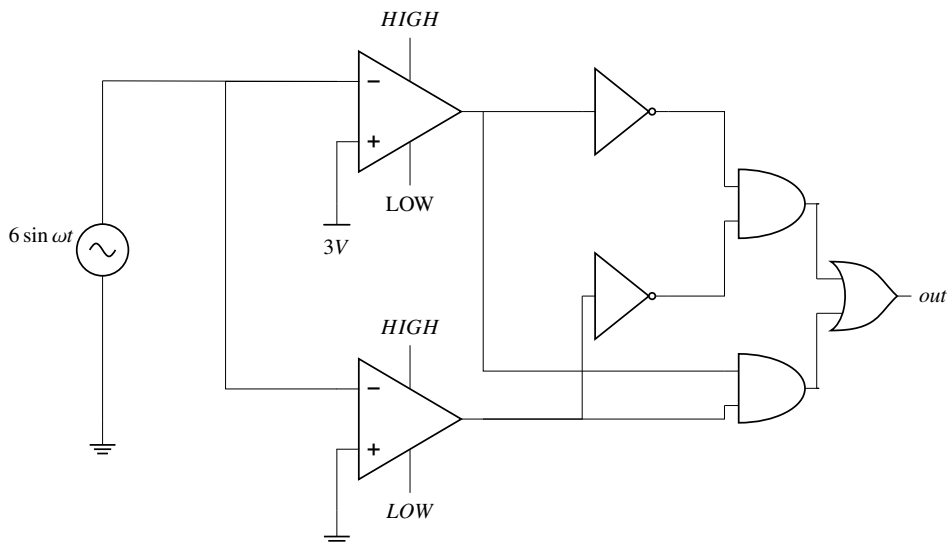


Fig. 3.26: Circuit Daigram

- a)  $\frac{1}{12}$
- b)  $\frac{1}{2}$
- c)  $\frac{3}{5}$
- d)  $\frac{5}{6}$

44. Fig. 3.27 shows the  $i$ th full-adder block of a binary adder circuit.  $C_i$  is the input carry and  $C_{i+1}$  is the output carry of the circuit. Assume that each logic gate has a delay of 2 nanosecond, with no additional time delay due to the interconnecting wires. If the inputs  $A_i$ ,  $B_i$  are available and stable throughout the carry propagation, the maximum time taken for an input  $C_i$ , to produce a steady-state output  $C_{i+1}$  is \_\_\_\_\_ nanosecond. (GATE-IN2019,22)

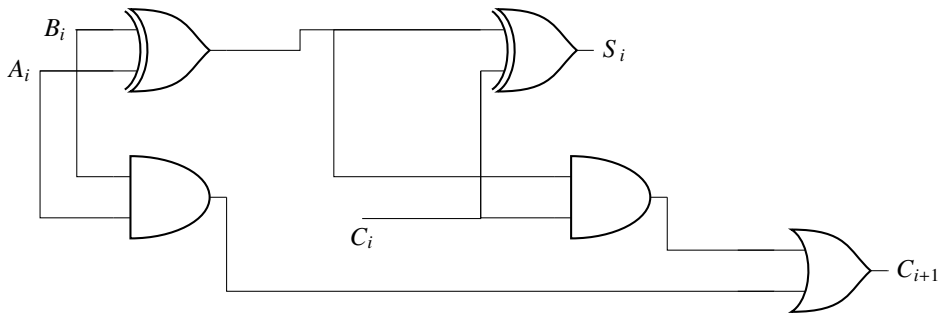


Fig. 3.27: Full Adder

45. The Boolean operation performed by the following circuit in Fig. 3.28 at the output  $O$  is \_\_\_\_\_ (GATE IN2020 – 12)

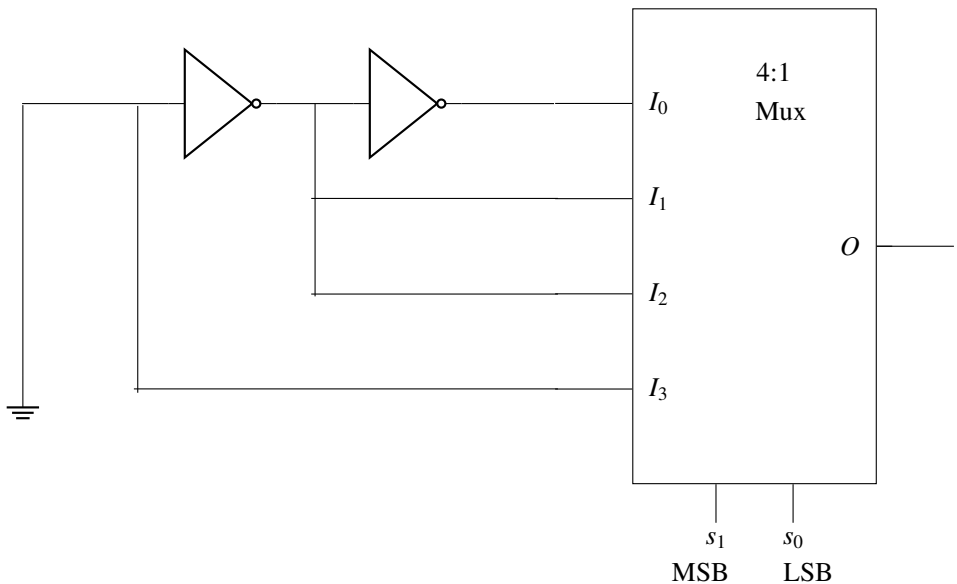


Fig. 3.28: Circuit Diagram

- a)  $O = S_1 \oplus \overline{S_0}$   
 b)  $O = S_1 \bullet \overline{S_0}$   
 c)  $O = S_1 + \overline{S_0}$   
 d)  $O = S_0 \bullet \overline{S_1}$
46. The chip select logic for a certain DRAM chip in a memory system design is shown below in Fig. 3.29. Assume that the memory system has 16 address lines denoted by  $A_{15}$  to  $A_0$ . What is the range of addresses (in hexadecimal) of the memory system that can get enabled by the chip select (CS) signal? (GATE CS2019 – 2)

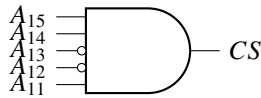
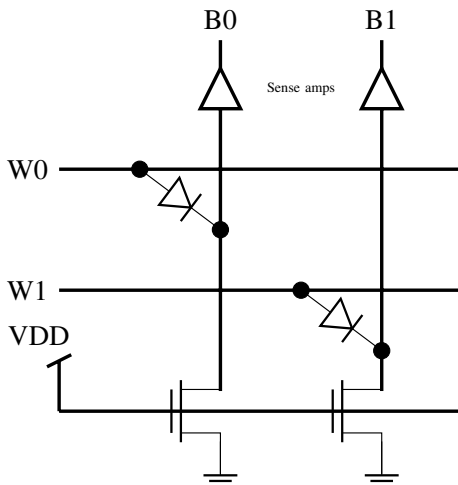


Fig. 3.29: Logic Diagram

- a)  $C800$  to  $CFFF$   
 b)  $CA00$  to  $CAFF$   
 c)  $CA00$  to  $C8FF$   
 d)  $DA00$  to  $DFFF$
47. A  $6\frac{1}{2}$  digit time counter is set in the time period mode of operation and range is set as 'ns'. For an input signal the time-counter displays 1000000. with the same input signal, The time counter is changed to 'frequency' mode of operation and the range is set as 'HZ'. The display will show the number \_\_\_\_\_. (GATE IN2020 – 43)
48. A  $2 \times 2$  ROM array is built with the help of diodes as shown in the circuit below in Fig. 3.30. Here  $W_0$  and  $W_1$  are signals that select the word lines and  $B_0$  and  $B_1$  are signals that are output of the sense amps based on the stored data corresponding to the bit lines during the read operation.



$$\begin{matrix} B_0 & B_1 \\ W_0 & \begin{bmatrix} D_{00} & D_{01} \end{bmatrix} \\ W_1 & \begin{bmatrix} D_{10} & D_{11} \end{bmatrix} \end{matrix}$$

Bits stored in the ROM Array

Fig. 3.30:  $2 \times 2$  ROM array

During the read operation, the selected word line goes high and the other word line is in a high impedance state. As per the implementation shown in the circuit diagram above, what are the bits corresponding to  $D_{ij}$  (where  $i = 0$  or  $1$  and  $j = 0$  or  $1$ ) stored in the ROM? (GATE EC2018,32)

- a)  $\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$

- b)  $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$   
 c)  $\begin{pmatrix} 1 & 0 \\ 1 & 0 \end{pmatrix}$   
 d)  $\begin{pmatrix} 1 & 1 \\ 0 & 0 \end{pmatrix}$

49. The two inputs A and B are connected to an R-S latch via two AND gates as shown in Fig. 3.31. If  $A = 1$  and  $B = 0$ , the output  $Q\bar{Q}$  is

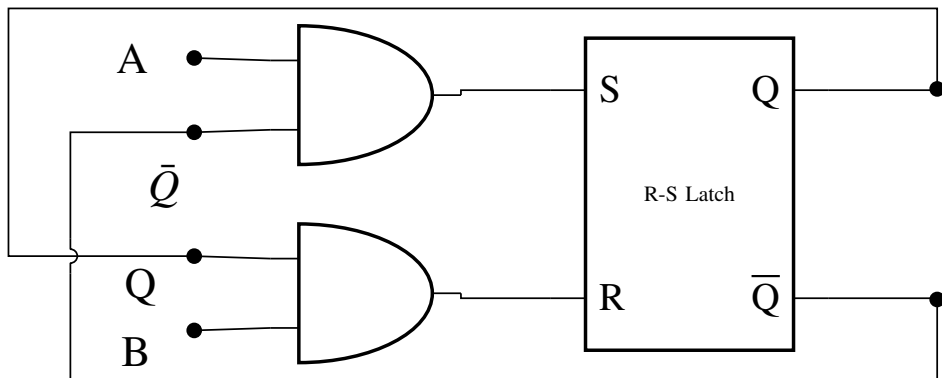


Fig. 3.31

(GATE IN2017,43)

- a) 00  
 b) 10  
 c) 01  
 d) 11

50. A and B are logical inputs and X is the logical output shown in Fig. 3.32. The output X is related to A and B by

(GATE IN 2017)

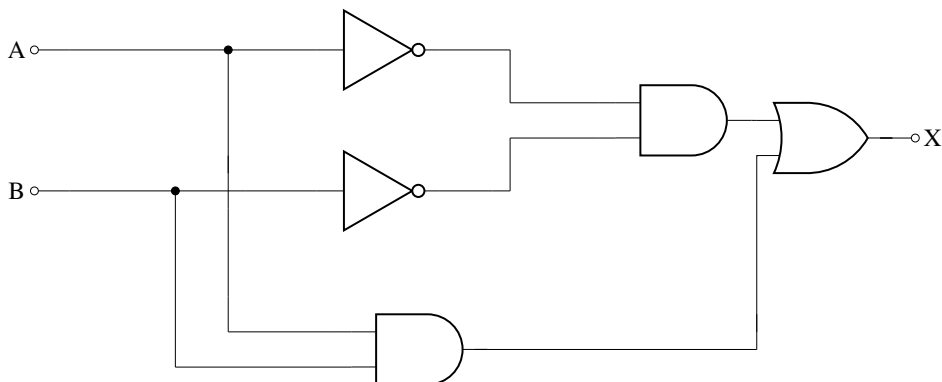


Fig. 3.32: Logic Gate Structure

- A.  $X = \overline{A}B + \overline{B}A$
- B.  $X = AB + \overline{B}A$
- C.  $X = AB + (\overline{B})(\overline{A})$
- D.  $X = (\overline{A})(\overline{B}) + \overline{B}A$

51. The functionality implemented by the circuit below in Fig. 3.33 is (GATE 2016 EC)

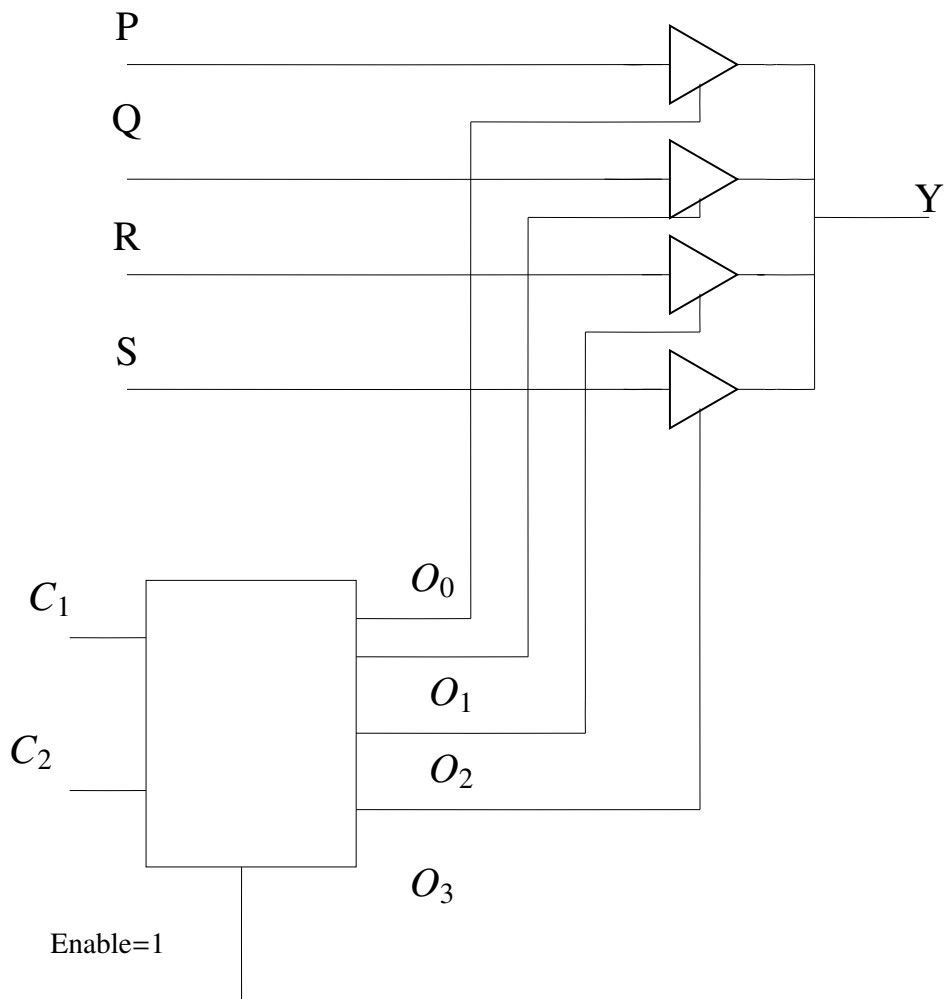


Fig. 3.33: Multiplexer

- A. 2-to-1 multiplexer
- B. 4-to-1 multiplexer
- C. 7-to-1 multiplexer
- D. 6-to-1 multiplexer

52. A 2-bit flash Analog to Digital Converter (ADC) is given in Fig. 3.34. The input is



$0 \leq V_{IN} \leq 3$  Volts. The expression of the LSB of the output  $B_0$  as a boolean function of  $X_2, X_1$ , and  $X_0$  is (GATE EE2016 37)

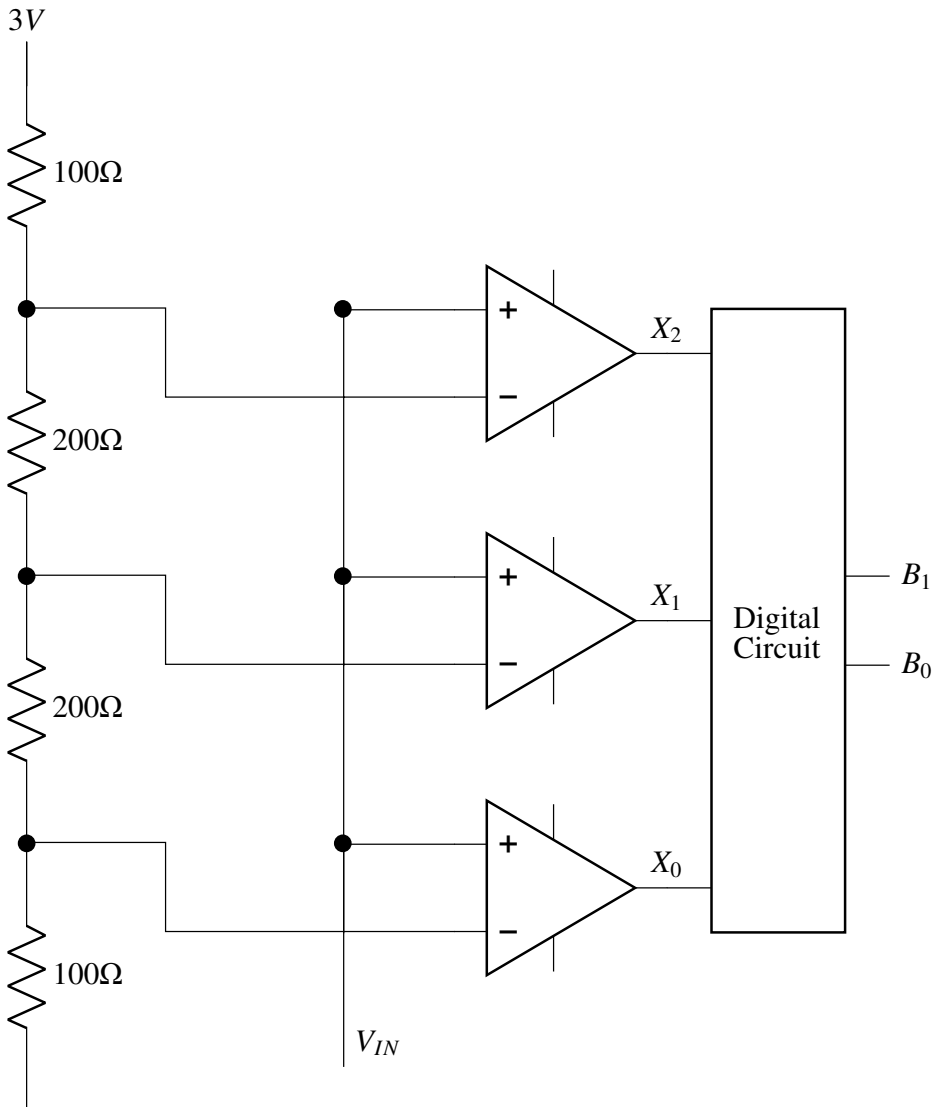


Fig. 3.34

- a)  $X_0 \left[ \overline{X_2 \oplus X_1} \right]$
- b)  $\overline{X_0} \left[ \overline{X_2 \oplus X_1} \right]$
- c)  $X_0 \left[ X_2 \oplus X_1 \right]$
- d)  $\overline{X_0} \left[ X_2 \oplus X_1 \right]$

53. Consider the Boolean function  $Z(a, b, c)$ . Which one of the following minterm lists represents the circuit given below in Fig. 3.35?

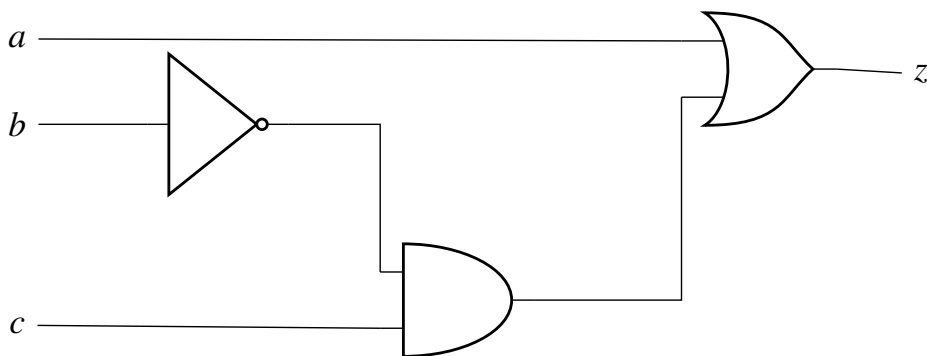


Fig. 3.35

- A.  $z = \sum (0, 1, 3, 7)$
- B.  $z = \sum (1, 4, 5, 6, 7)$
- C.  $z = \sum (2, 4, 5, 6, 7)$
- D.  $z = \sum (2, 3, 5)$

(GATE CS 2020)

54. The logic gates shown in the digital circuit below in Fig. 3.36 use strong pull-down nMOS transistors for LOW logic level at the outputs. When the pull-downs are off, high -value resistors set the output logic levels to HIGH (i.e. the pull-ups are weak). Note that some nodes are intentionally shorted to implement “wierd logic”. Such shorted nodes will be HIGH only if the outputs of all the gates whose outputs are shorted are HIGH.

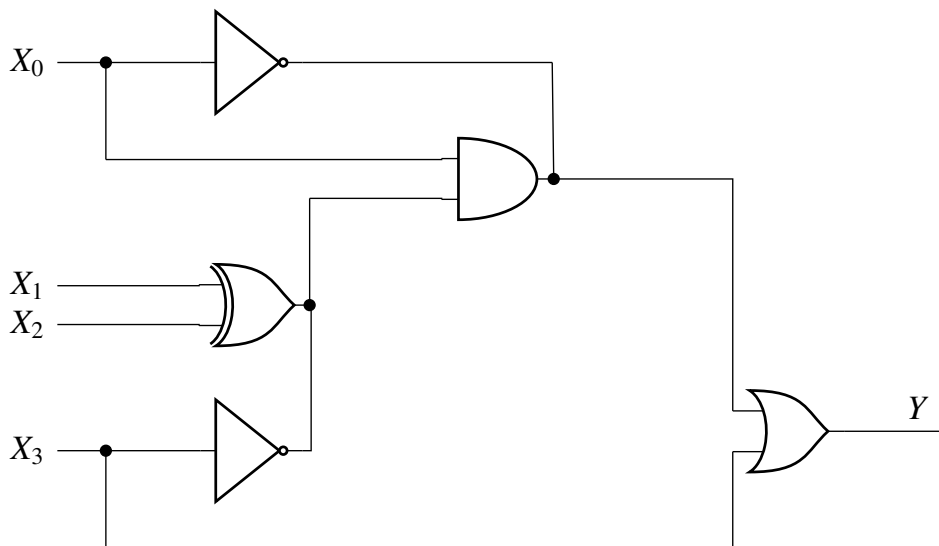


Fig. 3.36

The number of distinct values of  $X_3X_2X_1X_0$  (out of the 16 possible values) that give  $Y=1$  is —. (GATE-EC 2018, 47)

55. In the logic circuit shown in Fig. 3.37,  $y$  is given by (GATE-EE 2018,14)

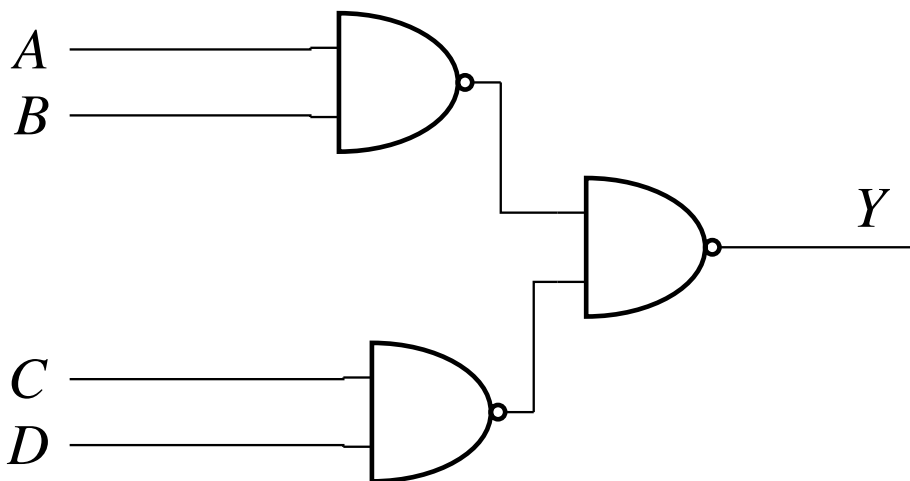


Fig. 3.37

- a)  $Y = ABCD$
- b)  $Y = (A + B)(C + D)$
- c)  $Y = A + B + C + D$
- d)  $Y = AB + CD$



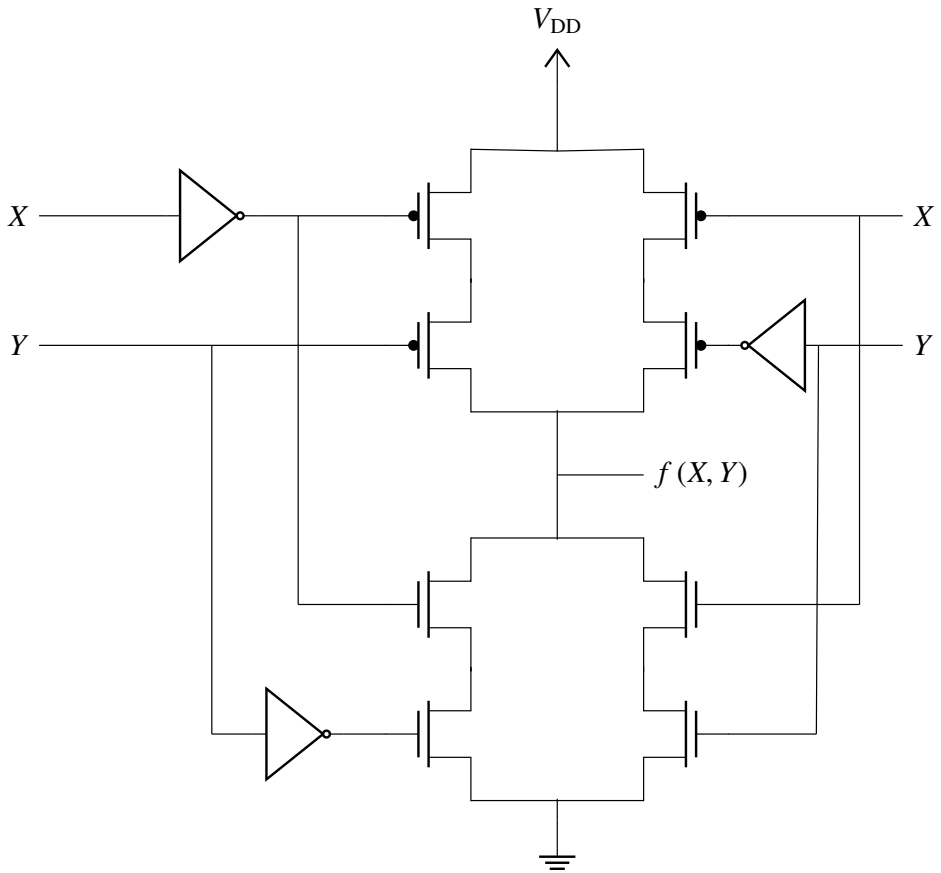


Fig. 3.39

- a) NOR
- b) AND
- c) NAND
- d) XOR

58. For the following circuit Fig. 3.40, the correct logic values for the entries  $X_2$  and  $Y_2$  in the truth table in Table 3.9 are (PH2019,36)

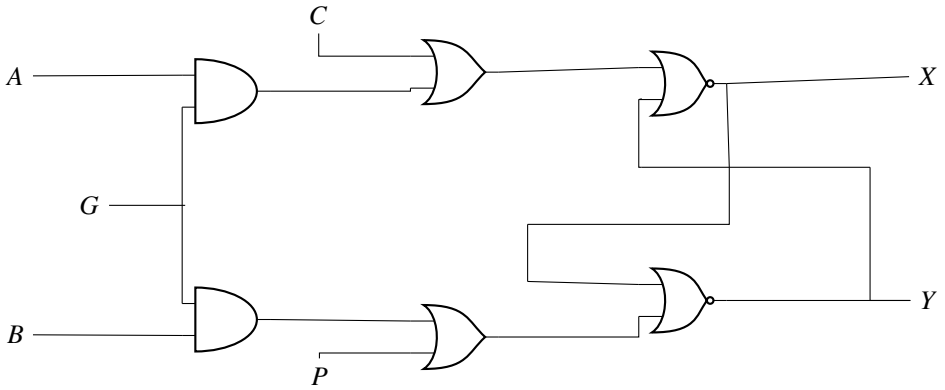


Fig. 3.40

<b>G</b>	<b>A</b>	<b>B</b>	<b>P</b>	<b>C</b>	<b>X</b>	<b>Y</b>
1	0	1	0	0	0	1
0	0	0	1	0	X2	Y2
1	0	0	0	1	0	1

TABLE 3.9

- a) 1 and 0
- b) 0 and 0
- c) 0 and 1
- d) 1 and 1

59. Which one the following is not a valid identity?

- a)  $(x \oplus y) \oplus z = x \oplus (y \oplus z)$
- b)  $(x + y) \oplus z = x \oplus (y + z)$
- c)  $x \oplus y = x + y, \text{ if } xy = 0$
- d)  $x \oplus y = (xy + x'y')'$

(GATE CS 2019)

60. Let  $p$  and  $q$  be two propositions. Consider the following two formulae in propositional logic.

$$S_1 : (\neg p \vee (p \wedge q)) \rightarrow q \quad (3.10)$$

$$S_2 : q \rightarrow (\neg p \vee (p \wedge q)) \quad (3.11)$$

Which one of the following choices is correct?

(GATE-CS2021)

- a) Both  $S_1$  and  $S_2$  are tautologies.
- b)  $S_1$  is a tautology but  $S_2$  is not a tautology.

- c)  $S_1$  is not a tautology but  $S_2$  is a tautology.  
 d) Neither  $S_1$  nor  $S_2$  is a tautology.

61. P, Q, and R are the decimal integers corresponding to the 4-bit binary number 1100 consider in single magnitude, 1's complement, and 2's complement representations, respectively. The 6-bit 2's complement representation of  $(P + Q + R)$  is

(GATE EC-2020,38)

- a) 110101  
 b) 110010  
 c) 111101  
 d) 111001

62. The Boolean expression  $F(X, Y, Z) = \overline{X}Y\overline{Z} + X\overline{Y}\overline{Z} + XY\overline{Z} + XYZ$  converted into the canonical product of sum (POS) form is

(GATE EC-2015,36)

- a)  $(X + Y + Z)(X + Y + \overline{Z})(X + \overline{Y} + \overline{Z})(\overline{X} + Y + \overline{Z})$   
 b)  $(X + \overline{Y} + Z)(\overline{X} + Y + \overline{Z})(\overline{X} + \overline{Y} + Z)(\overline{X} + \overline{Y} + \overline{Z})$   
 c)  $(X + Y + Z)(\overline{X} + Y + \overline{Z})(X + \overline{Y} + Z)(\overline{X} + \overline{Y} + \overline{Z})$   
 d)  $(X + \overline{Y} + \overline{Z})(\overline{X} + Y + Z)(\overline{X} + \overline{Y} + Z)(X + Y + Z)$

63. A 3-input majority gate is defined by the logic function  $M(a, b, c) = ab + bc + ca$ . Which one of the following gates is represented by the function  $M(\overline{M(a, b, c)}, M(a, b, \overline{c}), c)$ ?

- a) 3-input NAND gate  
 b) 3-input XOR gate  
 c) 3-input NOR gate  
 d) 3-input XNOR gate

(GATE-EC 2015, 48)

## 4 KARNAUGH MAP

### 4.1 Incrementing Decoder

We explain Karnaugh maps (K-map) by finding the logic functions for the incrementing decoder

1. The incrementing decoder takes the numbers  $0, \dots, 9$  in binary as inputs and generates the consecutive number as output. The corresponding truth table is available in Table 3.5
2. Using Boolean logic, output  $A$  in Table 3.5 can be expressed in terms of the inputs  $W, X, Y, Z$  as

$$A = W'X'Y'Z' + W'XY'Z' + W'X'YZ' + W'XYZ' + W'X'Y'Z \quad (4.1)$$

3. K-Map for  $A$ : The expression in (4.1) can be minimized using the K-map in Fig 4.1 In Fig 4.1, the *implicants* in boxes 0,2,4,6 result in  $W'Z'$  The implicants in boxes 0,8 result in  $W'X'Y'$  Thus, after minimization using Fig 4.2, (4.1) can be expressed as

$$A = W'Z' + W'X'Y' \quad (4.2)$$

Using the fact that

$$\begin{aligned} X + X' &= 1 \\ XX' &= 0, \end{aligned} \quad (4.3)$$

derive (4.2) from (4.1) algebraically



A 4x4 Karnaugh map for function A. The horizontal axis is labeled XW with values 00, 01, 11, 10. The vertical axis is labeled ZY with values 00, 01, 11, 10. The map contains 1s at (00,00), (00,01), (00,10), (10,00), (10,01), and (00,10). There are two groupings: a red group covering the first column (XW=00) and a green group covering the first row (ZY=00). The cell (00,10) is the intersection of these two groups.

	$XW$	00	01	11	10
$ZY$	00	1	0	0	1
	01	1	0	0	1
	11	0	0	0	0
	10	1	0	0	0

Fig. 4.1: K-map for A

4. K-Map for B: From Table 3.5, using boolean logic,

$$B = WX'Y'Z' + W'XY'Z' + WX'YZ' + W'XYZ' \quad (4.4)$$

		$XW$			
		00	01	11	10
$ZY$	00	0	1	0	1
	01	0	1	0	1
	11	0	0	0	0
	10	0	0	0	0

Fig. 4.2: K-map for  $B$ 

Show that (4.4) can be reduced to

$$B = WX'Z' + W'XZ' \quad (4.5)$$

using Fig 4.2

5. Derive (4.5) from (4.4) algebraically using (4.3)
6. K-Map for  $C$ : From Table 3.5, using boolean logic,

$$C = WXY'Z' + W'X'YZ' + WX'YZ' + W'XYZ' \quad (4.6)$$

		$XW$			
		00	01	11	10
$ZY$	00	0	0	1	0
	01	1	1	0	1
	11	0	0	0	0
	10	0	0	0	0

Fig. 4.3: K-map for  $C$ 

Show that (4.6) can be reduced to

$$C = WXY'Z' + X'YZ' + W'YZ' \quad (4.7)$$

using Fig 4.3

7. Derive (4.7) from (4.6) algebraically using (4.3)
8. K-Map for  $D$ : From Table 3.5, using boolean logic,

$$D = WXYZ' + W'X'Y'Z \quad (4.8)$$

$ZY \backslash XW$					
		00	01	11	10
00		0	0	0	0
01		0	0	1	0
11		0	0	0	0
10		1	0	0	0

Fig. 4.4: K-map for  $D$ 

9. Minimize (4.8) using Fig 4.4

10. Execute the code in

```
ide/7447/codes/inc_dec/inc_dec.cpp
```

and modify it using the K-Map equations for A,B,C and D Execute and verify

11. Display Decoder: Table 4.1 is the truth table for the display decoder in Fig. 3.1. Use K-maps to obtain the minimized expressions for  $a, b, c, d, e, f, g$  in terms of  $A, B, C, D$  with and without don't care conditions

#### 4.2 Dont Care

We explain Karnaugh maps (K-map) using don't care conditions

1. Don't Care Conditions: 4 binary digits are used in the incrementing decoder in Table 4.1 However, only the numbers from 0-9 are used as input/output in the decoder and

D	C	B	A	a	b	c	d	e	f	g	Decimal
0	0	0	0	0	0	0	0	0	0	1	0
0	0	0	1	1	0	0	1	1	1	1	1
0	0	1	0	0	0	1	0	0	1	0	2
0	0	1	1	0	0	0	0	1	1	0	3
0	1	0	0	1	0	0	1	1	0	0	4
0	1	0	1	0	1	0	0	1	0	0	5
0	1	1	0	0	1	0	0	0	0	0	6
0	1	1	1	0	0	0	1	1	1	1	7
1	0	0	0	0	0	0	0	0	0	0	8
1	0	0	1	0	0	0	1	1	0	0	9

TABLE 4.1: Truth table for display decoder.

we *don't care* about the numbers from 0-5 This phenomenon can be addressed by revising the truth table in Table 4.1 to obtain Table 4.2

Z	Y	X	W	D	C	B	A
0	0	0	0	0	0	0	1
0	0	0	1	0	0	1	0
0	0	1	0	0	0	1	1
0	0	1	1	0	1	0	0
0	1	0	0	0	1	0	1
0	1	0	1	0	1	1	0
0	1	1	0	0	1	1	1
0	1	1	1	1	0	0	0
1	0	0	0	1	0	0	1
1	0	0	1	0	0	0	0
1	0	1	0	-	-	-	-
1	0	1	1	-	-	-	-
1	1	0	0	-	-	-	-
1	1	0	1	-	-	-	-
1	1	1	0	-	-	-	-
1	1	1	1	-	-	-	-

TABLE 4.2

2. The revised K-map for A is available in Fig 4.5. Show that

$$A = W' \quad (4.9)$$

		$XW$			
		00	01	11	10
$ZY$	00	1	0	0	1
	01	1	0	0	1
	11	-	-	-	-
	10	1	0	-	-

Fig. 4.5: K-map for A with don't cares

3. The revised K-map for B is available in Fig 4.6 Show that

$$B = WX'Z' + W'X \quad (4.10)$$

$ZY \backslash XW$		00	01	11	10
		00	01	11	10
00	0	1	0	1	
01	0	1	0	1	
11	-	-	-	-	
10	0	0	-	-	

Fig. 4.6: K-map for  $B$  with don't cares

4. The revised K-map for  $C$  is available in Fig 4.7 Show that

$$C = X'Y + W'Y + WXY' \quad (4.11)$$

$ZY \backslash XW$		00	01	11	10
		00	01	11	10
00	0	0	1	0	
01	1	1	0	1	
11	-	-	-	-	
10	0	0	-	-	

Fig. 4.7: K-map for  $C$  with don't cares

5. The revised K-map for  $D$  is available in Fig 4.8 Show that

$$D = W'Z + WXY \quad (4.12)$$



		$XW$			
		00	01	11	10
$ZY$	00	0	0	0	0
	01	0	0	1	0
	11	-	-	-	-
	10	1	0	-	-

Fig. 4.8: K-map for  $D$  with don't cares

6. Verify the incrementing decoder with don't care conditions using the arduino
7. Display Decoder: Use K-maps to obtain the minimized expressions for  $a, b, c, d, e, f, g$  in terms of  $A, B, C, D$  with don't care conditions
8. Verify the display decoder with don't care conditions using arduino

### 4.3 Problems

1. Obtain the Minimal Form for the Boolean Expression (CBSE 2013)

$$H(P, Q, R, S) = \sum (0, 1, 2, 3, 5, 7, 8, 9, 10, 14, 15) \quad (4.13)$$

2. Write the POS form for the function  $G$  shown in Table 4.3. (CBSE 2013)

U	V	W	G
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

TABLE 4.3

3. Reduce the following Boolean Expression to its simplest form using K-Map (CBSE 2015)

$$F(X, Y, Z, W) = (0, 1, 4, 5, 6, 7, 8, 9, 11, 15) \quad (4.14)$$

4. Derive a Canonical POS expression for a Boolean function F, represented by the following truth table (CBSE 2015)

X	Y	Z	F
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

TABLE 4.4

5. (CBSE 2015) Reduce the following Boolean Expression to its simplest form using K-map

$$F(X, Y, Z, W) = \sum(0, 1, 6, 8, 9, 10, 11, 12, 15) \quad (4.15)$$

6. Reduce the following Boolean Expression to its simplest form using K-map. (CBSE 2016)

$$F(X, Y, Z, W) = \sum(2, 6, 7, 8, 9, 10, 11, 13, 14, 15) \quad (4.16)$$

7. Derive a Canonical POS expression for a Boolean function F, represented in Table 4.5 (CBSE 2016)

P	Q	R	F(P, Q, R)
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

TABLE 4.5

8. Verify the following

(CBSE 2016)

$$A' + B'C = A'B'C' + A'BC' + A'BC + A'B'C + AB'C \quad (4.17)$$

9. Reduce the following boolean expression to it's simplest form using K-Map (CBSE 2017)

$$F(X, Y, Z, W) = \sum(0, 1, 2, 3, 4, 5, 10, 11, 14) \quad (4.18)$$

10. Reduce the following Boolean Expression to its simplest form using K-Map. (CBSE 2017)

$$E(U, V, Z, W) = (2, 3, 6, 8, 9, 10, 11, 12, 13) \quad (4.19)$$

11. Derive a canonical POS expression for a Boolean function  $G$ , represented by Table 4.6 (CBSE 2017)

X	Y	Z	G(X,Y,Z)
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	1

TABLE 4.6

12. Derive a canonical POS expression for a Boolean function  $FN$ , represented by Table 4.7. (CBSE 2018)

X	Y	Z	FN(X,Y,Z)
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

TABLE 4.7

13. Reduce the following Boolean expression in the simplest form using K-Map.

$$F(P, Q, R, S) = \sum(0, 1, 2, 3, 5, 6, 7, 10, 14, 15) \quad (4.20)$$

(CBSE 2019)

14. Fig. 4.9 below shows a multiplexer where  $S_0$  and  $S_1$  are the select lines,  $I_0$  to  $I_3$  are the input lines,  $EN$  is the enable line and  $F(P, Q, R)$  is the output. Find the boolean expression for output  $F$  as function of inputs  $P, Q, R$  using K-map. (GATE EC 2020)

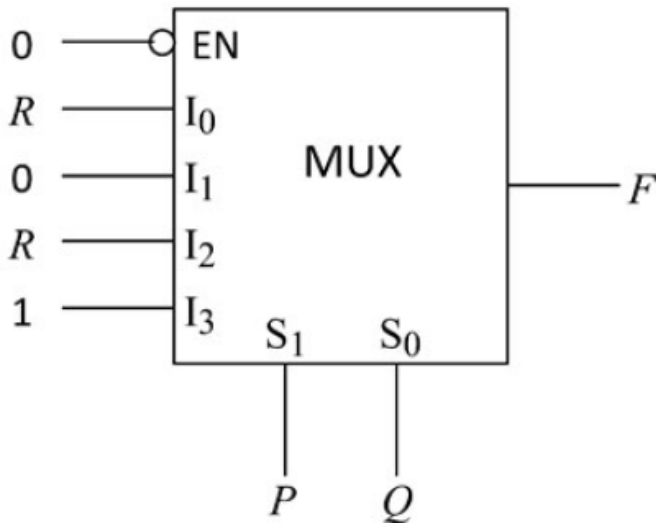


Fig. 4.9

15. The four variable function  $f$  is given in terms of min-terms as

$$f(A, B, C, D) = \sum m(2, 3, 8, 10, 11, 12, 14, 15) \quad (4.21)$$

Using the K-map minimize the function in the sum of products form. (GATE EC 1991)

16. Find the logic realized by the circuit in Fig. 4.10. (GATE EC 1992)

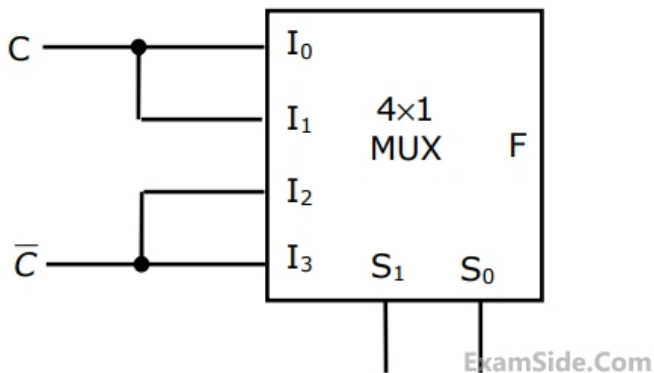


Fig. 4.10

17. A combinational circuit has three inputs A, B and C and an output F. F is true only for the following input combinations. (GATE EC 1992)
- A is false and B is true
  - A is false and C is true
  - A, B and C are all false
  - A, B and C are all true
- Write the truth table for F. use the convention, true = 1 and false = 0.
  - Write the simplified expression for F as a Sum of Products.
  - Write the simplified expression for F as a product of Sums.
18. Draw the logic circuit for Table 4.8 using only NOR gates. (GATE EC 1993)

C	B	A	Y
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	0

TABLE 4.8

19. Implement the following Boolean function in a 8x1 multiplexer. (GATE EC 1993)

$$Q = BC + ABD' + A'C'D \quad (4.22)$$

20. Minimize the following Boolean function in 4.23.

$$F = A'B'C' + A'BC' + A'BC + ABC' \quad (4.23)$$

21. Find the Boolean expression for Table 4.9.

(GATE EC 2005)

A	B	C	X
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	0

TABLE 4.9

22. Minimize the logic function represented by the following Karnaugh map. (CBSE

YZ

		00	01	11	10
X	0	1	1	1	0
	1	0	0	1	0

2021)

23. Find the output for the Karnaugh map shown below

(GATE EE 2019)

PQ

		00	01	11	10
RS	00	0	1	1	0
	01	1	1	1	1
	11	1	1	1	1
	10	0	0	0	0

24. The propagation delays of the XOR gate, AND gate and multiplexer (MUX) in the circuit shown in the Fig. 4.11 are 4 ns, 2 ns and 1 ns, respectively. If all the inputs P, Q, R, S and T are applied simultaneously and held constant, the maximum

propagation delay of the circuit is

(Gate EC-2021)

- a) 3 ns
- b) 5 ns
- c) 6 ns
- d) 7 ns

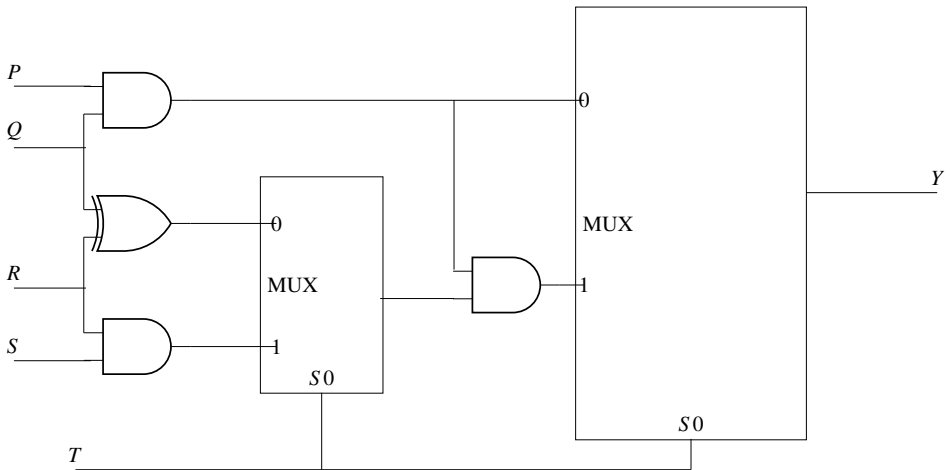


Fig. 4.11

25. Consider the 2-bit multiplexer(MUX) shown in Fig. 4.12. For output to be the XOR of R and S, the values for W, X, Y and Z are ?  
(GATE EC-2022)

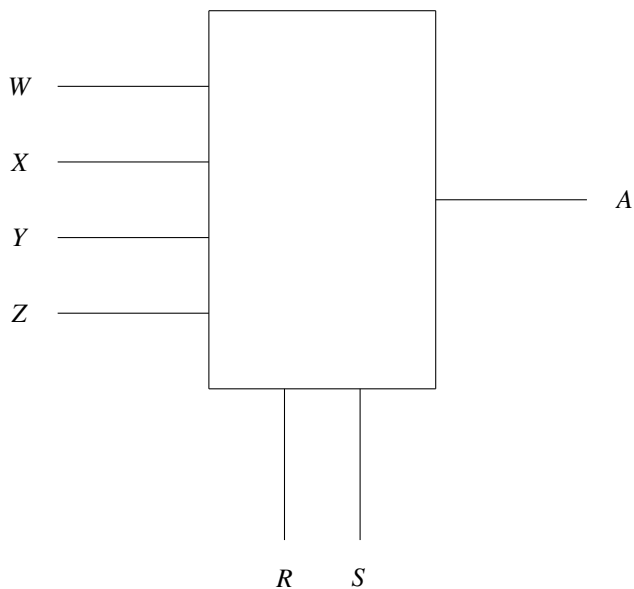


Fig. 4.12

- a)  $W = 0, X = 0, Y = 1, Z = 1$   
 b)  $W = 1, X = 0, Y = 1, Z = 0$   
 c)  $W = 0, X = 1, Y = 1, Z = 0$   
 d)  $W = 1, X = 1, Y = 0, Z = 0$
26.  $A = a_1a_0$  and  $B = b_1b_0$  are two 2-bit unsigned binary numbers. If  $F(a_1, a_0, b_1, b_0)$  is a Boolean function such that  $F = 1$  only when  $A > B$ , and  $F = 0$  otherwise, then  $F$  can be minimized to the form \_\_\_\_\_. (GATE IN-2022)
27. The logic block shown in Fig. 4.13 has an output  $F$  given by \_\_\_\_\_. (GATE IN 2022)



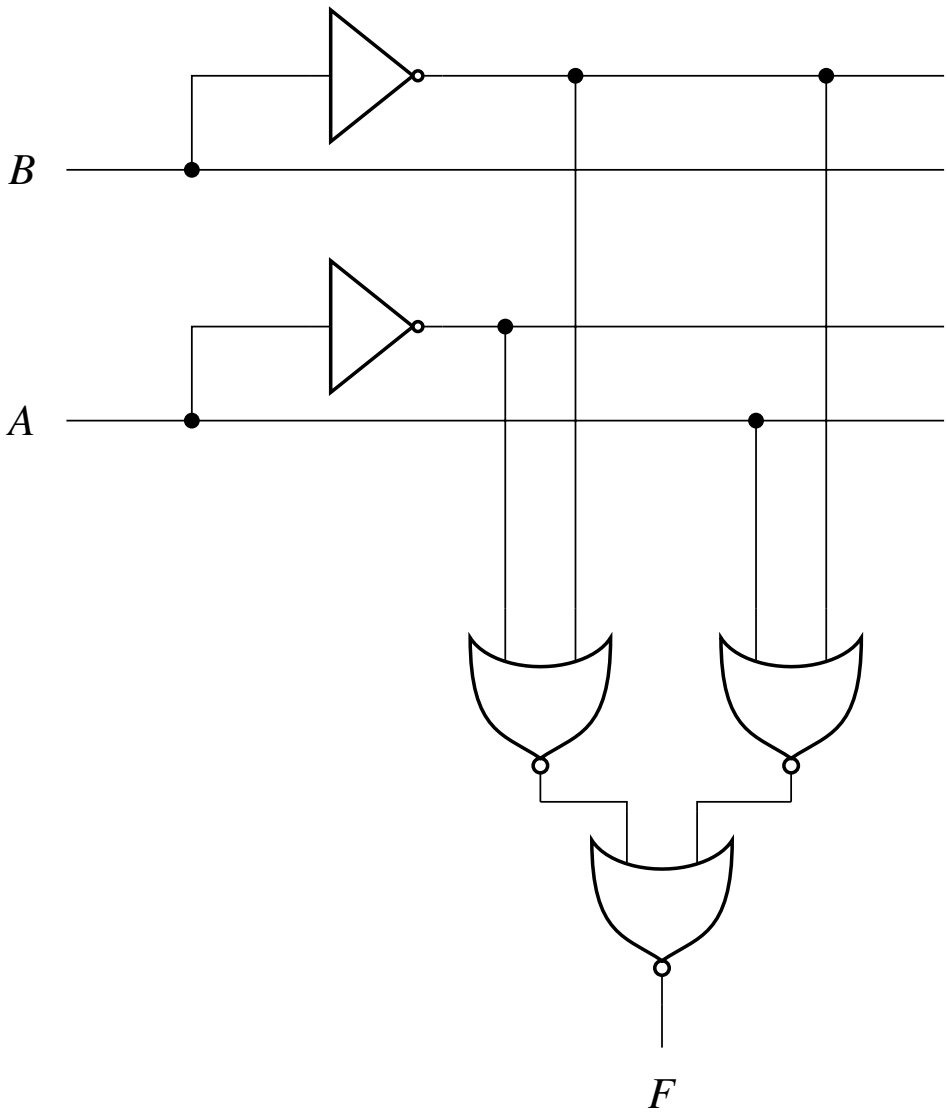


Fig. 4.13: Circuit

- a)  $A + B$
- b)  $A \cdot \bar{B}$
- c)  $A + \bar{B}$
- d)  $\bar{B}$

28. A  $4 \times 1$  multiplexer with two selector lines is used to realize a Boolean function  $F$  having four Boolean variables  $X$ ,  $Y$ ,  $Z$ , and  $W$  as shown below.  $S_0$  and  $S_1$  denote the least significant bit (LSB) and most significant bit (MSB) of the selector lines of

the multiplexer, respectively.  $I_0, I_1, I_2, I_3$  are the input lines of the multiplexer.

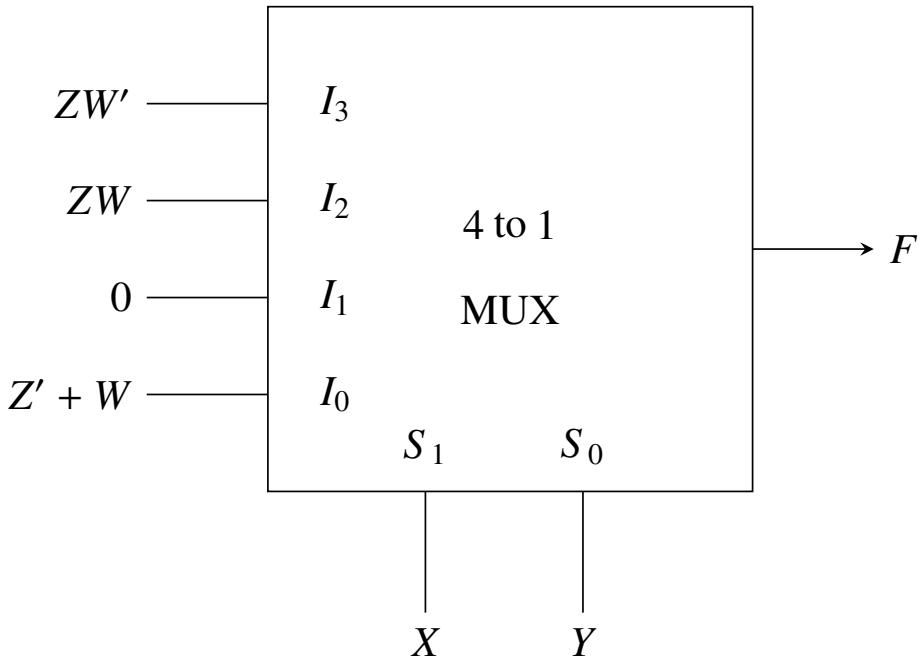


Fig. 4.14:  $4 \times 1$  multiplexer

The canonical sum of product representation of  $F$  is:

(GATE IN-2021)

- (A)  $F(X, Y, Z, W) = \Sigma m(0, 1, 3, 14, 15)$
- (B)  $F(X, Y, Z, W) = \Sigma m(0, 1, 3, 11, 14)$
- (C)  $F(X, Y, Z, W) = \Sigma m(2, 5, 9, 11, 14)$
- (D)  $F(X, Y, Z, W) = \Sigma m(1, 3, 7, 9, 15)$

29. The output expression for the Karnaugh map shown below in Fig. 4.15 is (GATE EE 2019)

PQ		00	01	11	10
RS	00	0	1	1	0
	01	1	1	1	1
	11	1	1	1	1
	10	0	0	0	0

Fig. 4.15

- a)  $QR' + S$
- b)  $QR + S$
- c)  $QR' + S'$
- d)  $QR + S'$

30. In the circuit shown below in Fig. 4.16, X and Y are digital inputs, and Z is a digital output. The equivalent circuit is a (GATE EE 2019)

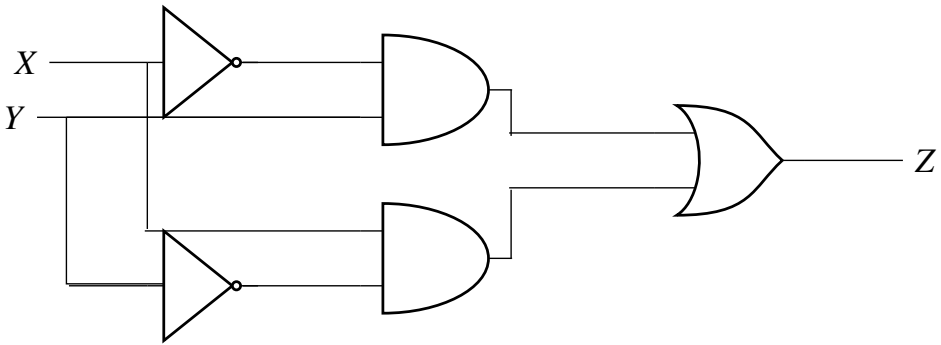


Fig. 4.16

- a) NAND gate
- b) NOR gate
- c) XOR gate
- d) XNOR gate

31. The output F of the digital circuit shown in Fig. 4.17 can be written in the form(s) \_\_\_\_\_ (GATE IN 2022)

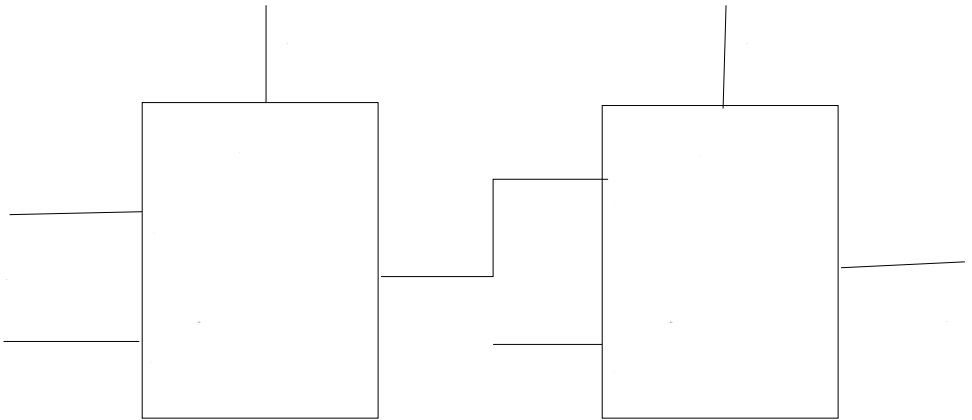


Fig. 4.17

- a)  $\overline{A \cdot B}$
- b)  $\overline{A+B}$
- c)  $\overline{A+B}$
- d)  $\overline{A \cdot B}$

32. If  $X = X_1X_0$  and  $Y = Y_1Y_0$  are 2-bit binary numbers. The Boolean function S that satisfies the condition "If  $X > Y$ , then  $S = 1$ ", in its minimized form, is ?

- a)  $X_1Y_1 + X_0Y_0$
- b)  $X_1\overline{Y_1} + X_0\overline{Y_0}Y_1 + X_0\overline{Y_0}X_1$

- c)  $X_1 \overline{Y_1} X_0 \overline{Y_0}$   
 d)  $X_1 Y_1 + X_0 \overline{Y_0} Y_1 + X_0 \overline{Y_0} X_1$

(GATE IN 2019)

33. Fig. 4.18 below shows the  $i^{th}$  full-adder block of a binary adder circuit.  $C_i$  is the input carry and  $C_{i+1}$  is the output carry of the circuit. Assume that each logic gate has a delay of 2 nanosecond, with no additional time delay due to the interconnecting wires. Of the inputs  $A_i$ ,  $B_i$  are available and stable throughout the carry propagation, the maximum time taken for an input  $C_i$  to produce a steady-state output  $C_{i+1}$  is \_\_\_\_\_ nanosecond. (GATE IN 2019)

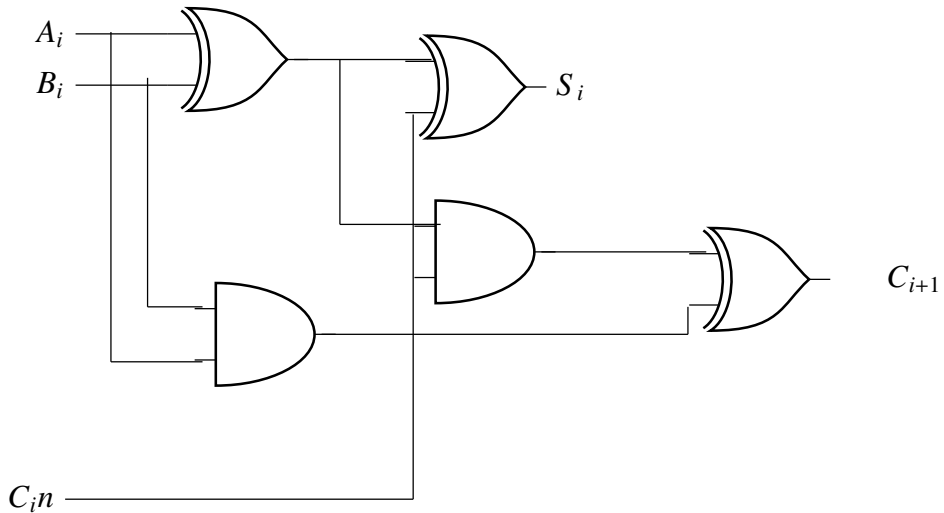


Fig. 4.18

34. The Product of sum expression of a Boolean function  $F(A, B, C)$  three variables is given by

$$F(A, B, C) = (A + B + \overline{C})(A + \overline{B} + \overline{C}) \times (\overline{A} + B + C)(\overline{A} + \overline{B} + \overline{C}) \quad (4.24)$$

The canonical sum of product expression of  $F(A, B, C)$  is given by

- a)  $\overline{A}\overline{B}C + \overline{A}BC + A\overline{B}\overline{C} + ABC$   
 b)  $\overline{A}\overline{B}\overline{C} + \overline{A}B\overline{C} + A\overline{B}C + ABC$   
 c)  $\overline{A}B\overline{C} + \overline{A}BC + A\overline{B}\overline{C} + ABC$   
 d)  $\overline{A}\overline{B}C + \overline{A}BC + A\overline{B}\overline{C} + ABC$

(GATE IN 2018)

35. A four-variable Boolean function is realized using  $4 \times 1$  multiplexers as shown in the Fig. 4.19.

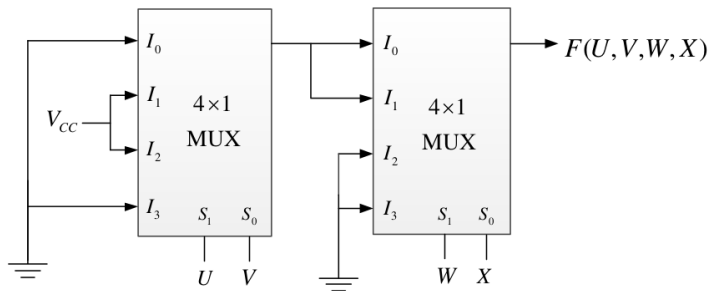


Fig. 4.19

The minimized expression for

- a)  $(UV + \bar{U}\bar{V})\bar{W}$
- b)  $(UV + \bar{U}\bar{V})(\bar{W}\bar{X} + \bar{W}X)$
- c)  $(U\bar{V} + \bar{U}V)\bar{W}$
- d)  $(U\bar{V} + \bar{U}V)(\bar{W}\bar{X} + \bar{W}X)$

(GATE EC 2018)

36. A function  $F(A, B, C)$  defined by three Boolean variables A, B and C when expressed as sum of products is given by

$F = (\bar{A} \cdot \bar{B} \cdot \bar{C}) + (\bar{A} \cdot B \cdot \bar{C}) + (A \cdot \bar{B} \cdot \bar{C})$  where,  $\bar{A}$ ,  $\bar{B}$  and  $\bar{C}$  are the complements of the respective variables. The product of sums (POS) form of the function F is

- (A)  $(A + B + C) \cdot (A + \bar{B} + C) \cdot (\bar{A} + B + C)$
- (B)  $(\bar{A} + \bar{B} + \bar{C}) \cdot (\bar{A} + B + \bar{C}) \cdot (A + \bar{B} + \bar{C})$
- (C)  $(A + B + \bar{C}) \cdot (A + \bar{B} + \bar{C}) \cdot (\bar{A} + B + \bar{C}) \cdot (\bar{A} + \bar{B} + C) \cdot (\bar{A} + \bar{B} + C)$
- (D)  $(\bar{A} + \bar{B} + C) \cdot (\bar{A} + B + C) \cdot (A + \bar{B} + C) \cdot (A + B + \bar{C}) \cdot (A + B + C)$

(GATE EC 2018)

37. In the Karnaugh map shown below in Fig. 4.20, X denotes a don't care term. What is the minimal form of the function represented by the Karnaugh map?

		<i>ba</i>			
		00	01	11	10
<i>cd</i>	00	1	1	0	1
	01	X	0	0	0
	11	X	0	0	0
	10	1	1	0	X

Fig. 4.20

- (A)  $b'd' + a'd'$   
 (B)  $a'b' + b'd' + a'bd'$   
 (C)  $b'd' + a'bd'$   
 (D)  $a'b' + b'd' + a'd'$

(GATE EC 2008)

38. Consider the minterm list form of a Boolean function given below.

$$F(P, Q, R, S) = \sum m(0, 2, 5, 7, 9, 11) + d(3, 8, 10, 12, 14)$$

Here, denotes a minterm and denotes a don't care term. The number of essential prime implicants of the function is

(GATE CS 2018)

39. In the circuit shown below in Fig. 4.21, P and Q are the inputs. The logical function realized by the circuit shown below in Fig. 4.21 is

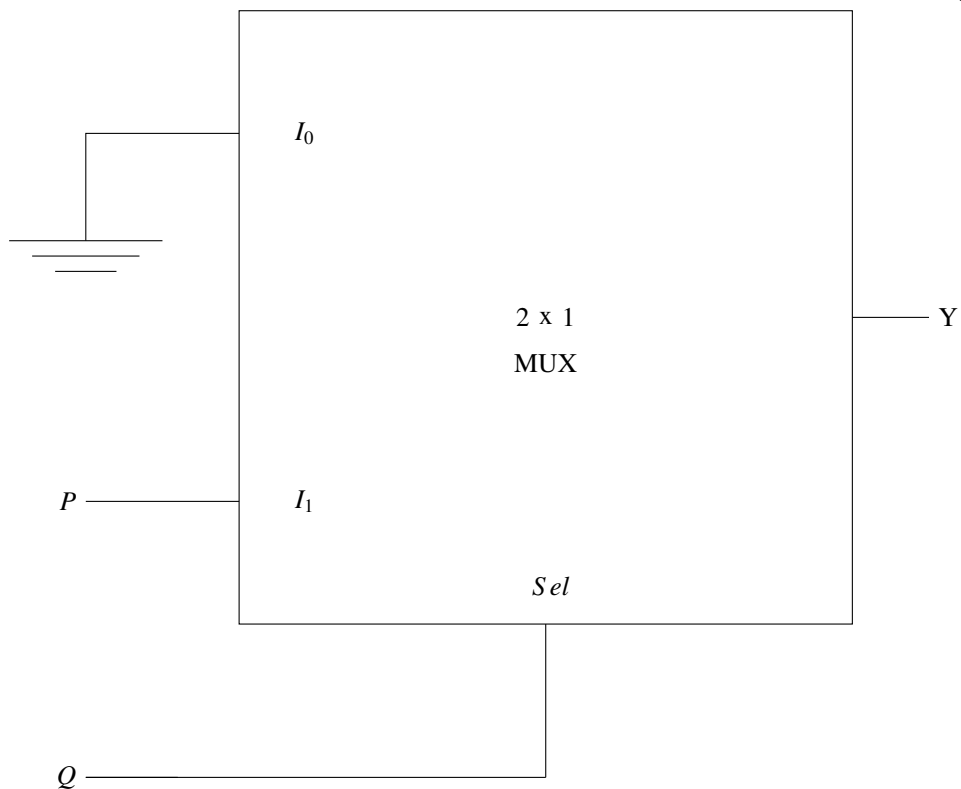


Fig. 4.21

- a)  $Y=PQ$
- b)  $Y=P+Q$
- c)  $Y= \overline{PQ}$
- d)  $Y= \overline{P + Q}$



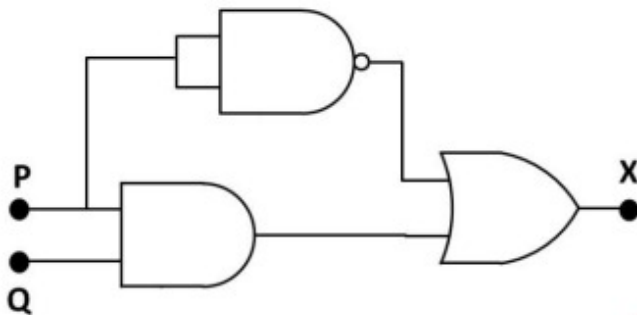


Fig. 4.22: k-maps

In Fig. 4.22, which of the following is correct?

- (a)  $P = 1, Q = 1; X = 0$
- (b)  $P = 1, Q = 0; X = 0$
- (c)  $P = 0, Q = 1; X = 0$
- (d)  $P = 0, Q = 0; X = 1$

(GATE PH2023,24)

40. Consider the 2-bit multiplexer(MUX) shown in Fig. 4.23. For OUTPUT to be the XOR of C and D, th values for  $A_0, A_1, A_2$  and  $A_3$  are \_\_\_\_ (GATE EC 2022)

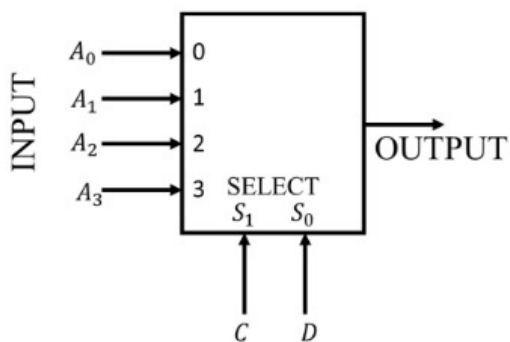


Fig. 4.23: MUX

- (A)  $A_0 = 0, A_1 = 0, A_2 = 1, A_3 = 1$
- (B)  $A_0 = 1, A_1 = 0, A_2 = 1, A_3 = 0$
- (C)  $A_0 = 0, A_1 = 1, A_2 = 1, A_3 = 0$
- (D)  $A_0 = 1, A_1 = 1, A_2 = 0, A_3 = 0$

41. The simplified form of the Boolean function  $F(W, X, Y, Z) = \sum(4, 5, 10, 11, 12, 13, 14, 15)$  with the minimum number of terms and smallest number of literals in each terms is \_\_\_\_\_

- a)  $WX + \bar{W}X\bar{Y} + W\bar{X}Y$
- b)  $WX + WY + X\bar{Y}$
- c)  $X\bar{Y} + WY$
- d)  $\bar{X}Y + \bar{W}\bar{Y}$

(GATE IN 2023)

42. Q, R, S are Boolean variables  $\oplus$  and is the XOR operator. Select the CORRECT option(s).

- a)  $(Q \oplus R) \oplus S = Q \oplus (R \oplus S)$
- b)  $(Q \oplus R) \oplus S = 0$  when any of the Boolean variables (Q, R, S) are 0 and the third variable is 1
- c)  $(Q \oplus R) \oplus S = 1$  when  $Q = R = S = 1$
- d)  $((Q \oplus R) \oplus (R \oplus S)) \oplus (Q \oplus S) = 1$

(Gate BM 2023)

43. The output F of the digital circuit shown in Fig. 4.24 can be written in the form(s)\_\_\_\_\_

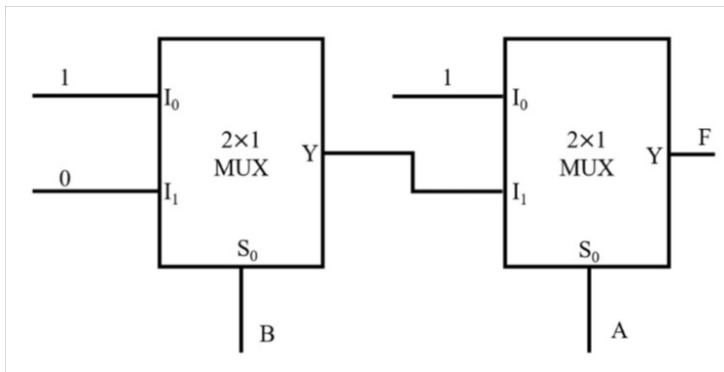


Fig. 4.24

- a)  $\overline{A \cdot B}$
- b)  $\overline{A + B}$
- c)  $\overline{A + B}$
- d)  $\overline{A \cdot B}$

(GATE IN 2022)

44.  $\mathbf{A} = a_1a_0$  and  $\mathbf{B} = b_1b_0$  are two 2-bit unsigned binary numbers. If  $\mathbf{F}(a_1, a_0, b_1, b_0)$  is a Boolean function such that  $\mathbf{F} = 1$  only when  $\mathbf{A} > \mathbf{B}$ , and  $\mathbf{F} = 0$  otherwise, then  $\mathbf{F}$  can be minimized to the form \_\_\_\_\_

- a)  $a_1\bar{b}_1 + a_1a_0\bar{b}_0$
- b)  $a_1\bar{b}_1 + a_1a_0\bar{b}_0 + a_0\bar{b}_0\bar{b}_1$
- c)  $a_1a_0\bar{b}_0 + a_0\bar{b}_0\bar{b}_1$
- d)  $a_1\bar{b}_1 + a_1a_0\bar{b}_0 + a_0\bar{b}_0b_1$

(GATE IN-2022)

45. The minimum number of two-input NAND gates required to implement the following Boolean expression is \_\_\_\_\_

$$Y = [A\bar{B}(C + BD) + \bar{A}\bar{B}]C$$

(GATE-PH-2022)

46. In the circuit shown below in Fig. 4.25,  $Y$  is a 2-bit ( $Y_1Y_0$ ) output of the combinational logic. What is the maximum value of  $Y$  for any given digital inputs,  $A_1A_0$  and  $B_1B_0$  ?

(GATE-BM2021)

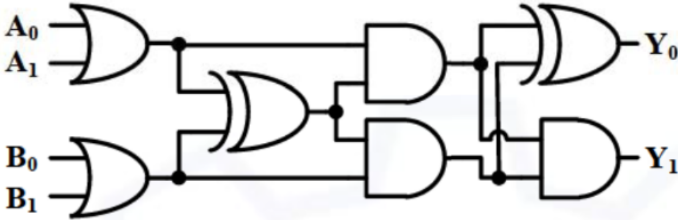


Fig. 4.25

- (A) 01  
(B) 10  
(C) 00  
(D) 11
47. Match the Boolean expression with its minimal realization in Table 4.10

	Boolean expression		Minimal realization
$P$	$\bar{X}\bar{Y}\bar{Z} + \bar{X}Y\bar{Z} + \bar{X}YZ$	$K$	$X(Y + Z)$
$Q$	$XYZ + \bar{X}\bar{Y}\bar{Z} + \bar{X}YZ$	$L$	$\bar{X}(Y + \bar{Z})$
$R$	$XY + \bar{X}YZ + \bar{X}Y\bar{Z} + \bar{X}\bar{Y}\bar{Z}$	$M$	$Z$
$S$	$\bar{X}\bar{Y}\bar{Z} + \bar{X}Y\bar{Z} + \bar{X}YZ + \bar{X}\bar{Y}Z$	$N$	$Y(X + Z)$

TABLE 4.10

(GATE BM 2020)

- (A)  $P - K, Q - L, R - N, S - M$   
(B)  $P - L, Q - K, R - N, S - M$   
(C)  $P - L, Q - N, R - M, S - K$   
(D)  $P - M, Q - K, R - L, S - N$

48. A  $4 \times 1$  multiplexer with two selector lines is used to realize a Boolean function  $F$  having four Boolean variables  $X, Y, Z$  and  $W$  as shown below in Fig. 4.26.  $S_0$  and  $S_1$  denote the least significant bit (*LSB*) and most significant bit (*MSB*) of the selector lines of the multiplexer respectively.  $I_0, I_1, I_2, I_3$  are the input lines of the multiplexer.

(GATE-IN2021,35)

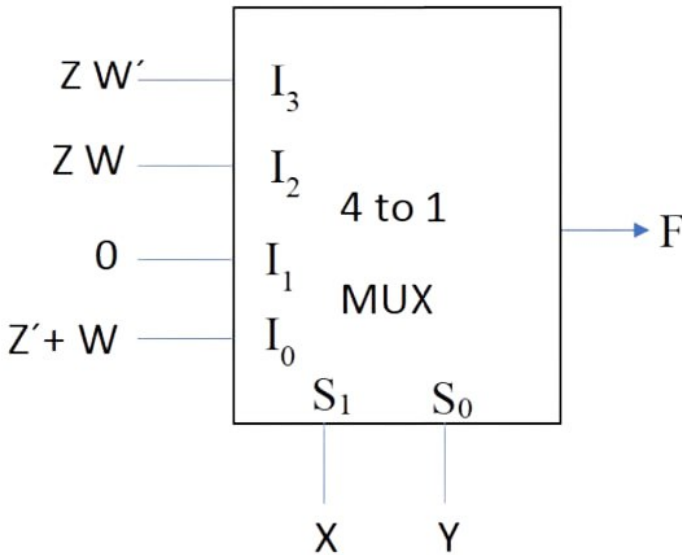


Fig. 4.26: Multiplexer

**The canonical sum of product representations of  $F$  is**

- a)  $F(X, Y, Z, W) = \sum m(0, 1, 3, 14, 15)$
  - b)  $F(X, Y, Z, W) = \sum m(0, 1, 3, 11, 14)$
  - c)  $F(X, Y, Z, W) = \sum m(2, 5, 9, 11, 14)$
  - d)  $F(X, Y, Z, W) = \sum m(1, 3, 7, 9, 15)$
49. The output expression for the Karnaugh map shown below in Fig. 4.27 is (GATE-EE2019,35)

		$PQ$			
		00	01	11	10
$RS$	00	0	1	1	0
	01	1	1	1	1
	11	1	1	1	1
	10	0	0	0	0

Fig. 4.27: K-MAP

- a)  $Q\bar{R} + S$
- b)  $Q\bar{R} + \bar{S}$
- c)  $QR + S$
- d)  $QR + \bar{S}$

50. The Boolean expression for the shaded regions as shown in Fig. 4.28 is \_\_\_\_\_.  
(GATE IN2020 – 11)

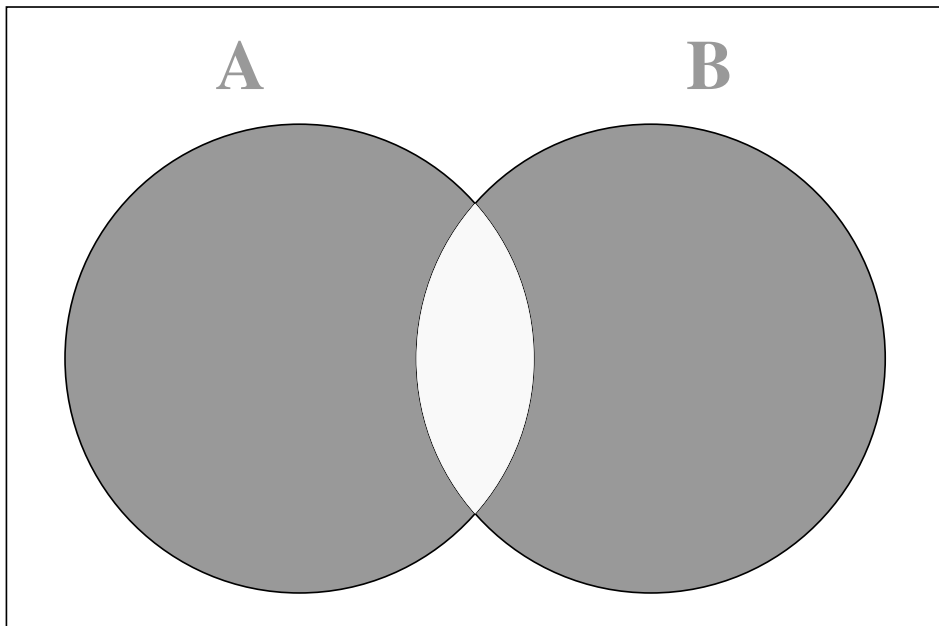


Fig. 4.28: Venn Diagram

- a)  $(A + B) \cdot (\overline{A} + \overline{B})$
- b)  $(A + \overline{B}) \cdot (\overline{A} + B)$
- c)  $(\overline{A} + B) \cdot (\overline{A} + \overline{B})$
- d)  $(\overline{A} + \overline{B}) \cdot (A + B)$

51. The output expression of the Karnaugh map shown below in Fig. 4.29 is (GATE EE-2017, 36)

		CD			
		00	01	11	10
AB	00	0	0	0	0
	01	1	0	0	1
	11	1	0	1	1
	10	0	0	0	0

Fig. 4.29

- A.  $B\bar{D} + BCD$
- B.  $B\bar{D} + AB$
- C.  $\bar{B}D + ABC$
- D.  $B\bar{D} + ABC$

52. A Boolean function  $F$  of three variables  $X, Y$ , and  $Z$  is given as  $F(X, Y, Z) = (X' + Y + Z) \cdot (X + Y' + Z') \cdot (X' + Y + Z') \cdot (X'Y'Z' + X'YZ' + XYZ')$ .

Which one of the following is true?

(GATE IN2021,31)

- a)  $F(X, Y, Z) = (X + Y + Z') \cdot (X' + Y' + Z')$
- b)  $F(X, Y, Z) = (X' + Y) \cdot (X + Y' + Z')$
- c)  $F(X, Y, Z) = X'Z' + YZ'$
- d)  $F(X, Y, Z) = X'Y'Z + XYZ$

53. Fig. 4.30 below shows a multiplier where  $S_1$  and  $S_0$  are select lines,  $I_0$  to  $I_3$  are the input data lines,  $EN$  is the enable line, and  $F(P, Q, R)$  is the output.  $F$  is (GATE EC 2020)

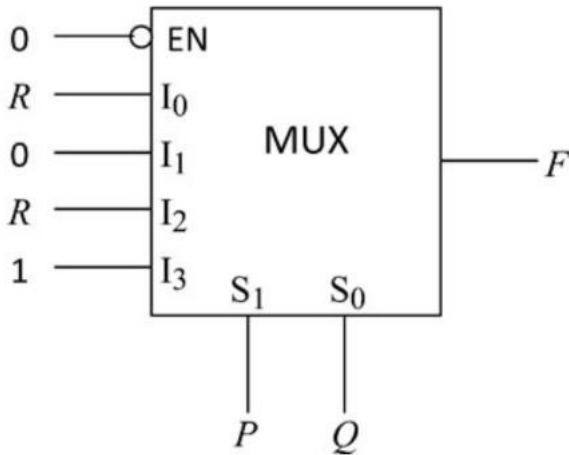


Fig. 4.30

- (A)  $PQ + \bar{Q}R$ .
- (B)  $P + Q\bar{R}$ .
- (C)  $P\bar{Q}R + \bar{P}Q$ .
- (D)  $\bar{Q} + PR$ .

54. The product of sum expression of a Boolean function  $F(A, B, C)$  of three variables is given by

$$F(A, B, C) = (A + B + \bar{C}) \cdot (A + \bar{B} + \bar{C}) \cdot (\bar{A} + B + C) \cdot (\bar{A} + \bar{B} + \bar{C}) \quad (4.25)$$

The canonical sum of product expression of  $F(A, B, C)$  is given by (GATE IN 2018)

- (A)  $\bar{A} \bar{B} C + \bar{A} B \bar{C} + A \bar{B} C + A B C$
- (B)  $\bar{A} \bar{B} \bar{C} + \bar{A} B \bar{C} + A \bar{B} C + A B \bar{C}$
- (C)  $A B \bar{C} + A \bar{B} \bar{C} + \bar{A} B C + \bar{A} B C + \bar{A} \bar{B} \bar{C}$
- (D)  $\bar{A} \bar{B} \bar{C} + \bar{A} B C + A B \bar{C} + A B \bar{C} + A B C$

55. Digital input signals  $A, B, C$  with  $A$  as the MSB and  $C$  as the LSB are used to realize the Boolean function  $F = m_0 + m_2 + m_3 + m_5 + m_7$ , where  $m_i$  denotes the  $i^{th}$  minterm. In addition,  $F$  has a don't care for  $m_1$ . The simplified expression for  $F$  is given by (GATE-2018,EE,37)

- a)  $\bar{A}\bar{C} + \bar{B}C + AC$
- b)  $\bar{A} + C$
- c)  $\bar{C} + A$
- d)  $\bar{A}C + BC + A\bar{C}$

56. Consider the minterm list form of a Boolean function  $F$  given below.

$$F(P, Q, R, S) = \sum m(0, 2, 5, 7, 9, 11) + d(3, 8, 10, 12, 14) \quad (4.26)$$

Here,  $m$  denotes a minterm and  $d$  denotes a don't care term. The number of essential prime implicants of the function  $F$  is \_\_\_\_\_. (GATE-2018,CS,49)



5 7474

We show how to use the 7474 D-Flip Flop ICs in a sequential circuit to realize a decade counter.

5.1 Components

Component	Value	Quantity
Resistor	220 Ohm	1
Arduino		1
Seven Segment Display		1
Decoder	7447	1
Flip Flop	7474	2
Jumper Wires		20

TABLE 5.1

5.2 Decade Counter

1. Generate the CLOCK signal using the **blink** program.
2. Connect the Arduino, 7447 and the two 7474 ICs according to Table 5.2 and Fig. 5.2. The pin diagram for 7474 is available in Fig. 5.1

	INPUT				OUTPUT				CLOCK		5V			
	W	X	Y	Z	A	B	C	D						
Ar-duino	D6	D7	D8	D9	D2	D3	D4	D5	D13					
7474	5	9			2	12			CLK1	CLK2	1	4	10	13
7474			5	9			2	12	CLK1	CLK2	1	4	10	13
7447					7	1	2	6			16			

TABLE 5.2

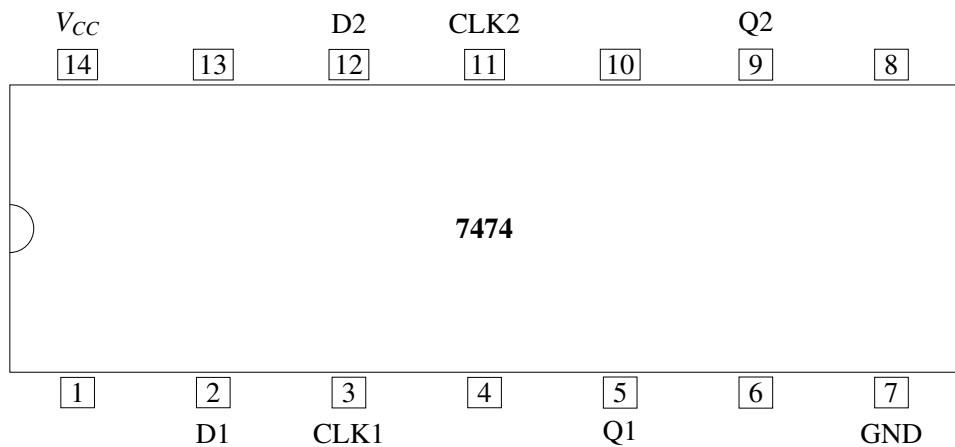


Fig. 5.1

3. Realize the decade counter in Fig. 5.2.

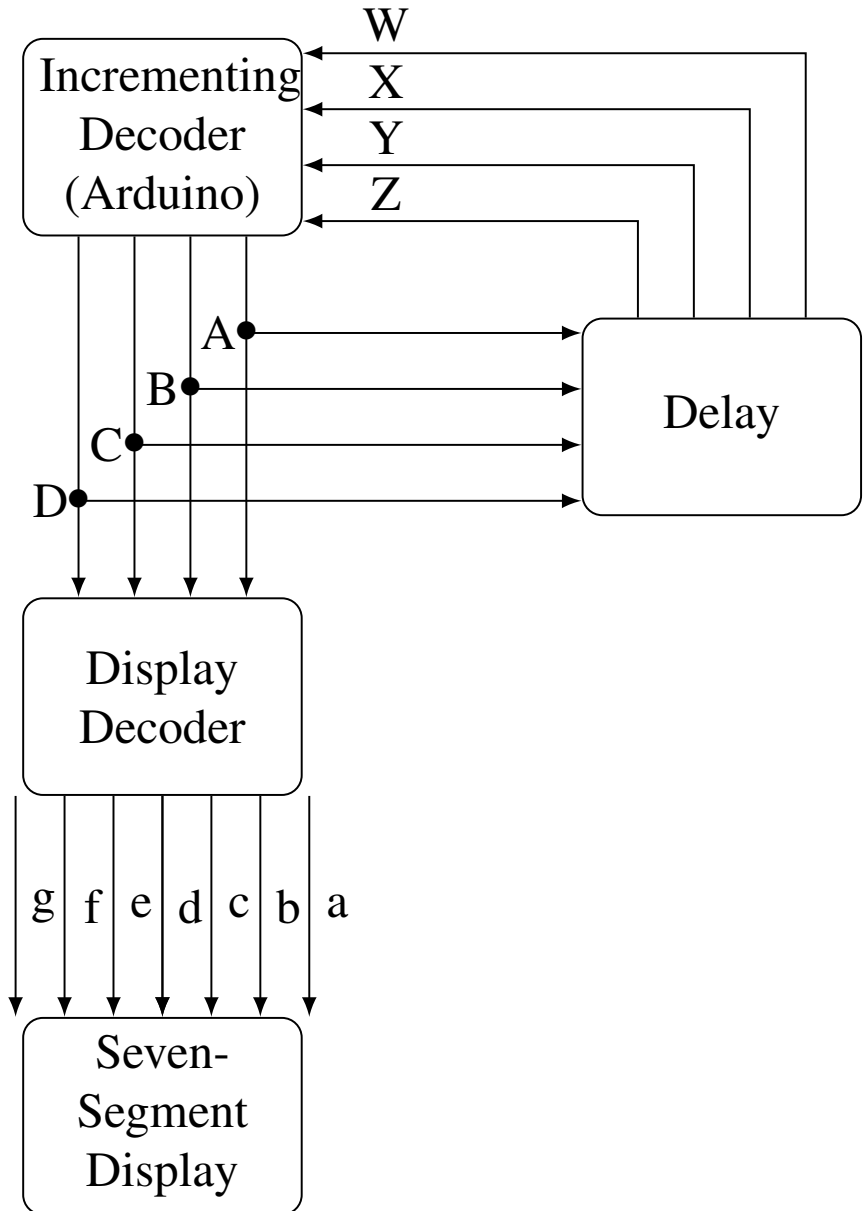


Fig. 5.2

### 5.3 Problems

1. A counter is constructed with three  $D$  flip-flops. The input-output pairs are named  $(D_0, Q_0)$ ,  $(D_1, Q_1)$ , and  $(D_2, Q_2)$ , where the subscript 0 denotes the least

significant bit. The output sequence is desired to be the Gray-code sequence 000, 001, 011, 010, 110, 111, 101, and 100, repeating periodically. Note that the bits are listed in the  $Q_2 Q_1 Q_0$  format. The combinational logic expression for  $D_1$  is (GATE-EE2021,37)

- a)  $Q_2 Q_1 Q_0$
- b)  $Q_2 Q_0 + Q_1 \bar{Q}_0$
- c)  $\bar{Q}_2 Q_0 + Q_1 \bar{Q}_0$
- d)  $Q_2 Q_1 + \bar{Q}_2 \bar{Q}_1$

2. The propagation delay of the exclusive-OR(XOR) gate in the circuit in Fig. 5.3 is 3 ns. The propagation delay of all the flip-flops is assumed to be zero. The Clock(clk) frequency provided to the circuit is 500 MHz.

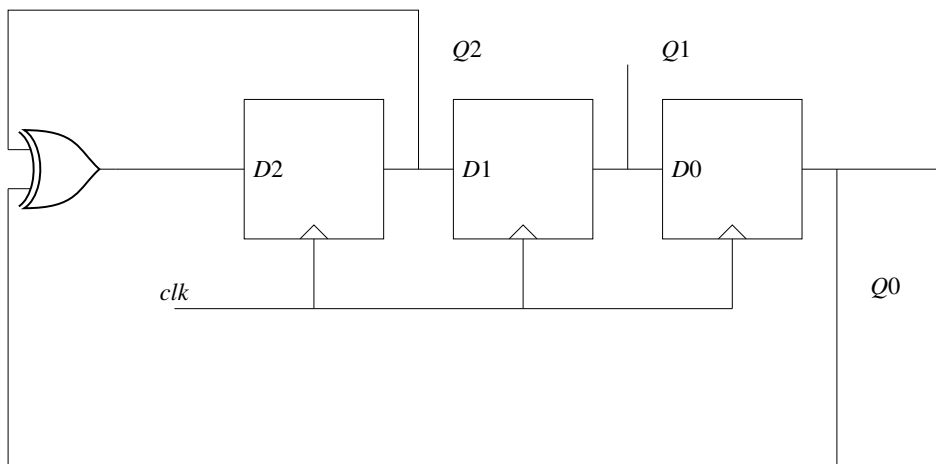


Fig. 5.3: Propagation Delay

Starting from the initial value of the flip-flop outputs  $Q_2 Q_1 Q_0 = 111$  with  $D_2 = 1$ , the minimum number of triggering clock edges after which the flip-flop outputs  $Q_2 Q_1 Q_0$  becomes 1 0 0 (in integer) is \_\_\_\_

(GATE-EC2021,46)

3. The maximum clock frequency in MHz of a 4-stage ripple counter, utilizing flip-flops, with each flip-flop having a propagation delay of 20 ns, is \_\_\_\_\_. (round off to one decimal place) (GATE EE 2022)
4. The digital circuit shown in Fig. 5.4

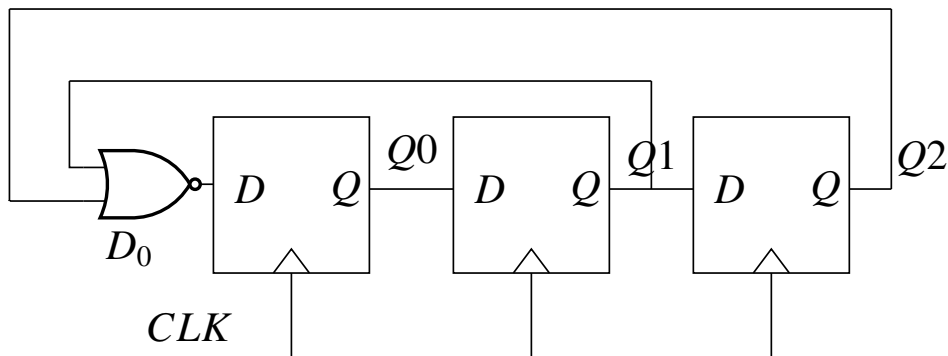


Fig. 5.4

- (A) is a divide-by-5 counter  
 (B) is a divide-by-7 counter  
 (C) is a divide-by-8 counter  
 (D) does not function as a counter due to disjoint cycles of states

GATE IN 2022

5. The propagation delay of the exclusive-OR(XOR) gate in the circuit in Fig. 5.5 is 3ns. The propagation delay of all the flip-flops is assumed to be zero. The clock(Clk) frequency provided to the circuit is 500MHz.

(GATE EC 2021)

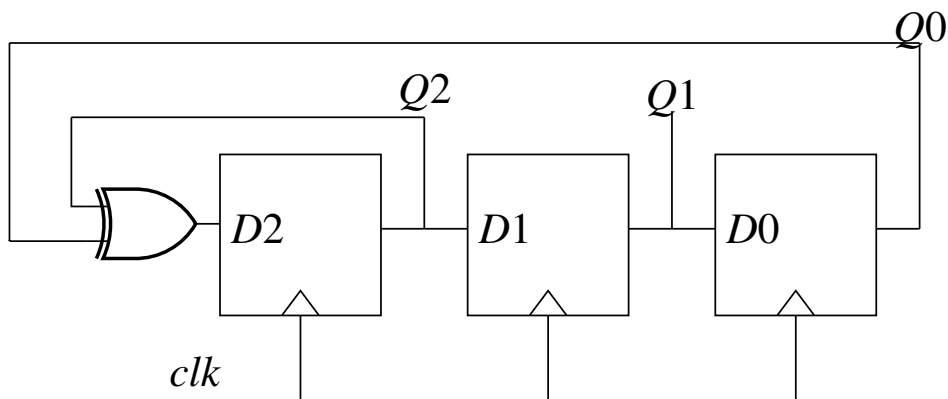


Fig. 5.5

Starting from the initial value of the flip-flop outputs  $Q_2Q_1Q_0 = 111$  with  $D_2 = 1$ , the minimum number of triggering clock edges after which the flip-flop outputs  $Q_2Q_1Q_0$  becomes 1 0 0 (in integer) is \_\_\_\_

6. For the 3-bit binary counter shown in Fig. 5.6, the output increments at every positive transition in the clock (CLK). Assume ideal diodes and the starting state of the counter as 000. If output high is 1V and output low is 0V, the current  $I$  (in mA)

flowing through the  $50\Omega$  resistor during the 5th clock cycle is (up to one decimal place)  
(GATE IN 2018)

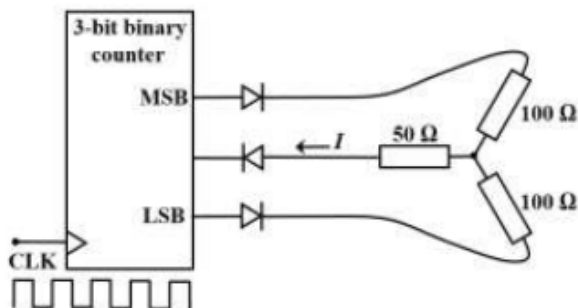


Fig. 5.6

7. Consider the sequential circuit shown in Fig. 5.7, where both flip-flops used are positive edge-triggered D flip-flops.

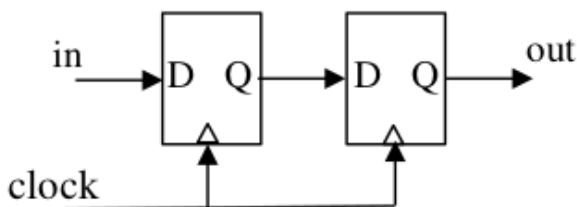


Fig. 5.7

The number of states in the state transition diagram of this circuit that have a transition back to the same state on some value of "in" is \_\_\_\_\_. (GATE IN 2018)

8. The synchronous sequential circuit shown below in Fig. 5.8 works at a clock frequency of  $1\text{GHz}$ . The throughput, in  $\text{Mbits/s}$ , and the latency, in  $\text{ns}$ , respectively, are

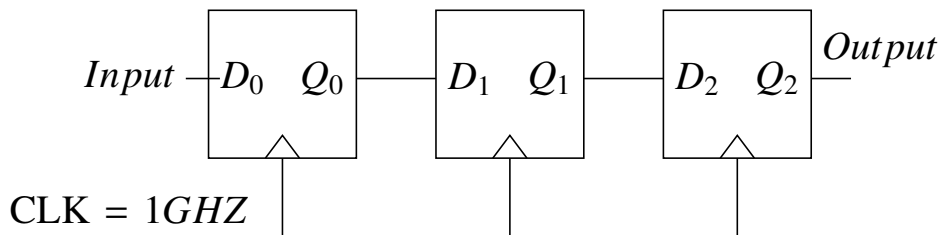


Fig. 5.8

- a) 1000, 3
- b) 333.33, 1
- c) 2000, 3
- d) 333.33, 3

(GATE EC 2023)

9. In a given sequential circuit in Fig. 5.9, initial states are  $Q_1 = 1$  and  $Q_2 = 0$ . For a clock frequency of  $1\text{MHz}$ , the frequency of signal  $Q_2$  in kHz, is (rounded off to the nearest integer)

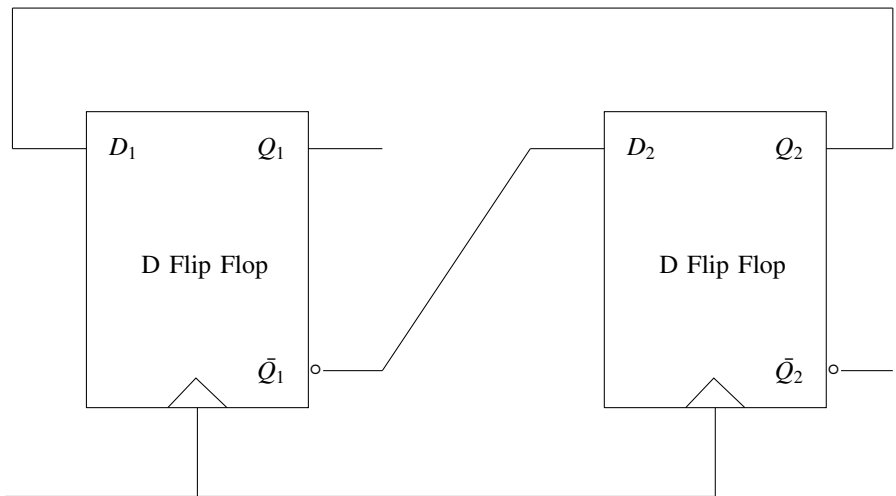


Fig. 5.9

(GATE EC 2023)

10. Neglecting the delays due to the logic gates in the circuit shown in Fig. 5.10, the decimal equivalent of the binary sequence  $[ABCD]$  of initial logic states, which will not change with clock, is \_\_\_\_\_.

(EE GATE 2023)

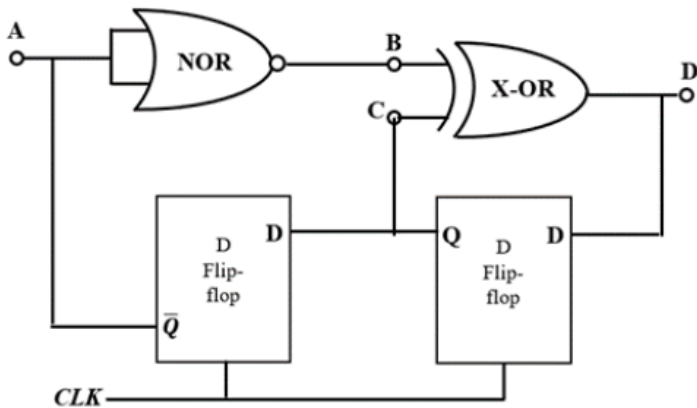


Fig. 5.10

11. Consider a sequential digital circuit consisting of T flip-flops and D flip-flops as shown in Fig. 5.11. CLKIN is the clock input to the circuit. At the beginning,  $Q_1, Q_2$  and  $Q_3$  have values 0, 1 and 1, respectively.

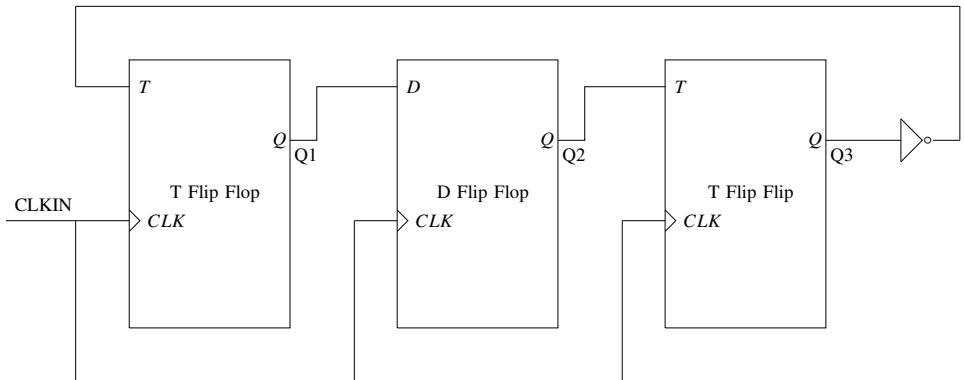


Fig. 5.11

Which of the given values of  $(Q_1, Q_2, Q_3)$  can NEVER be obtained with this digital circuit?

- (0, 0, 1)
- (1, 0, 0)
- (1, 0, 1)
- (1, 1, 1)

(GATE CS2023,43)

12. In the circuit shifter in Fig. 5.12, the initial binary content of the shift register A is 1101 and that of shift register B is 1010. The shift registers are positive edge triggered,



and the gates have no delay. when the shift control is high, what will be the binary content of the shift registers  $A$  and  $B$  after clock pulses?

(GATE IN 2023)

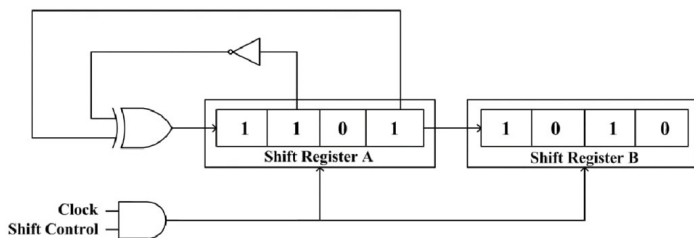


Fig. 5.12: circuit Diagram

- a)  $A = 1101, B = 1101$
- b)  $A = 1110, B = 1001$
- c)  $A = 0101, B = 1101$
- d)  $A = 1010, B = 1111$

13. For the circuit shown in Fig. 5.13, the clock frequency is  $f_0$  and the duty cycle is 25%. For the signal at the  $Q$  output of the Flip-Flop, (GATE EC 2022)

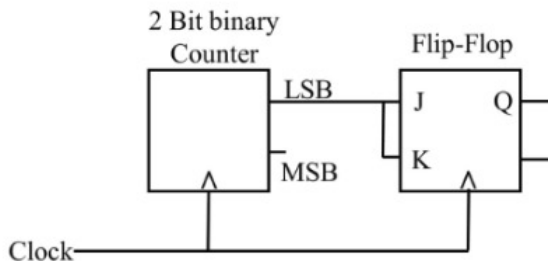


Fig. 5.13: Circuit

- a) frequency is  $\frac{f_0}{4}$  and duty cycle is 50%
- b) frequency is  $\frac{f_0}{4}$  and duty cycle is 25%
- c) frequency is  $\frac{f_0}{2}$  and duty cycle is 50%
- d) frequency is  $f_0$  and duty cycle is 25%

14. The digital circuit shown in Fig. 5.14

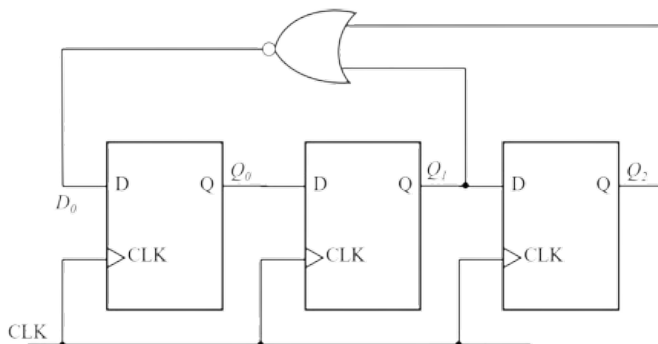


Fig. 5.14

- a) is a divide-by-5 counter
- b) is a divide-by-7 counter
- c) is a divide-by-8 counter
- d) does not function as a counter due to disjoint cycles of states

(GATE-IN-2022)

15. Given below in Fig. 5.15 is the diagram of a synchronous sequential circuit with one  $J-K$  flip-flop and one  $T$  flip-flop with their outputs denoted as  $A$  and  $B$  respectively, with  $J_A = (A' + B')$ ,  $K_A = (A+B)$  and  $T_B = A$ . Starting from the initial state ( $AB = 00$ ), the sequence of states ( $AB$ ) visited by the circuit is

(GATE-IN2021)

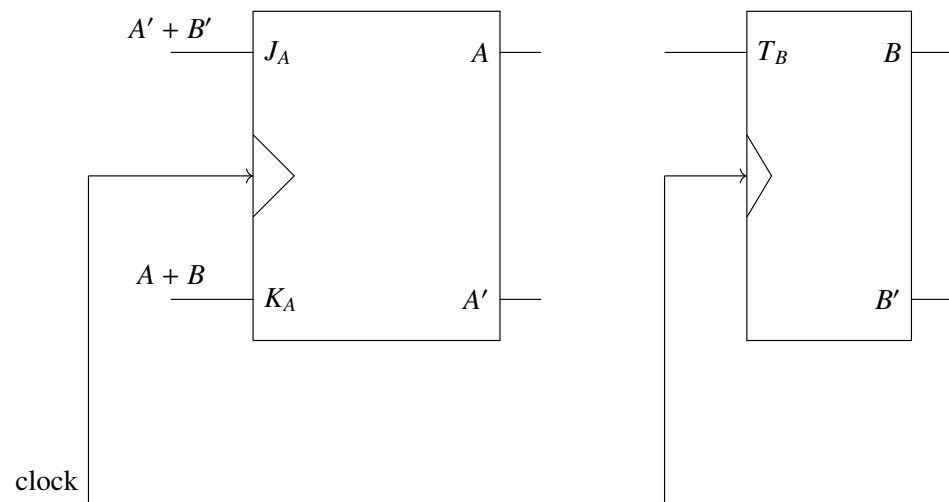


Fig. 5.15

- a)  $00 \rightarrow 01 \rightarrow 10 \rightarrow 11 \rightarrow 00 \dots$
- b)  $00 \rightarrow 10 \rightarrow 01 \rightarrow 11 \rightarrow 00 \dots$

c)  $00 \rightarrow 10 \rightarrow 11 \rightarrow 01 \rightarrow 00 \dots$

d)  $00 \rightarrow 01 \rightarrow 11 \rightarrow 00 \dots$

16. Consider the *D*-Latch shown in Fig. 5.16, which is transparent when its clock input *CK* is high and has zero propagation delay. In the figure, the clock signal *CLK1* has 50% duty cycle and *CLK2* is a one fifth period delayed version of *CLK1*. The duty cycle at the output of the latch in percentage is \_\_\_\_\_. (GATE-EC2017)

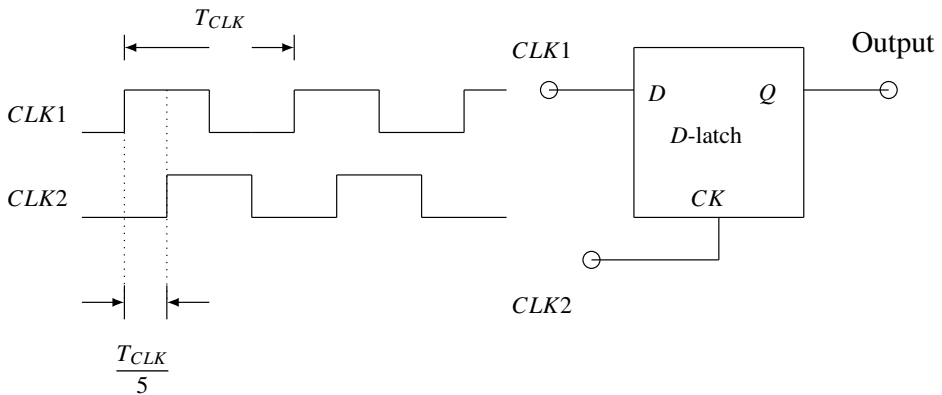


Fig. 5.16

17. A 4-bit shift register circuit configured for right-shift operation, i.e.

$D_{in} \rightarrow A, A \rightarrow B, B \rightarrow C, C \rightarrow D$ , is shown in Fig. 5.17. If the present state of the shift register is  $ABCD = 1101$ , the number of clock cycles required to reach the state  $ABCD = 1111$  is

(GATE-EC 2017)

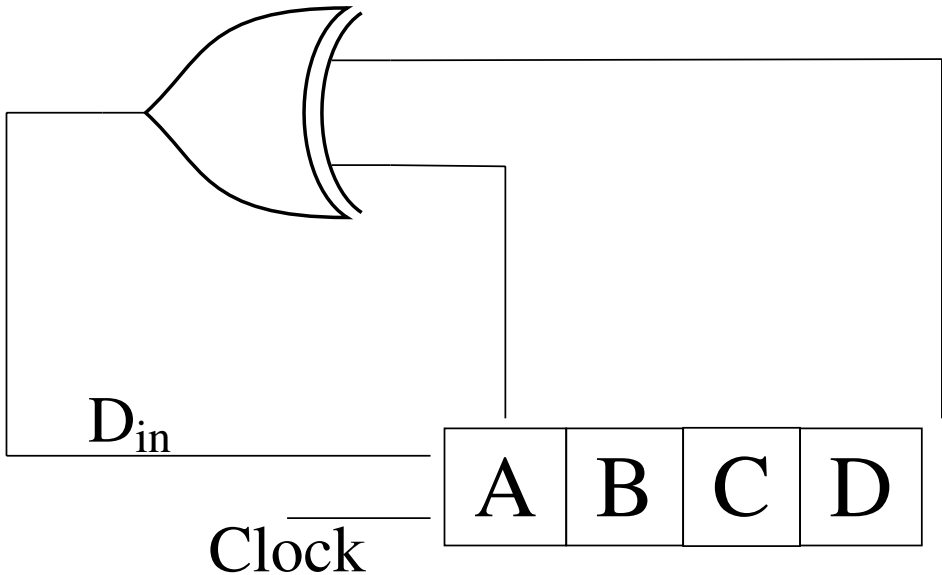


Fig. 5.17

18. In the circuit shown in Fig. 5.18, the clock frequency, i.e., the frequency of the clk signal, is 12 KHz. The frequency of the signal at **Q2** is \_\_\_\_ KHz. (GATE-EC2019,25)

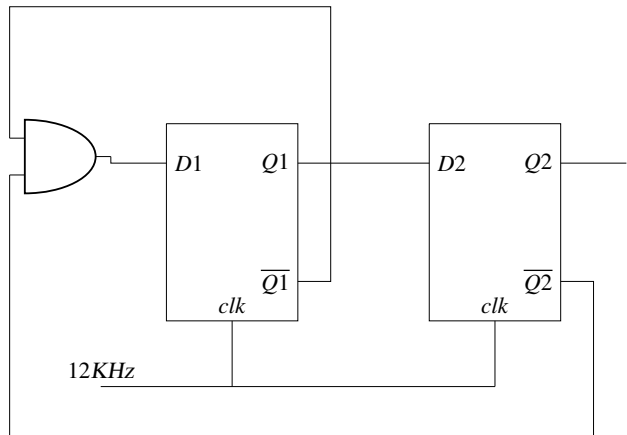


Fig. 5.18

19. The circuit shown in Fig. 5.19 below uses ideal positive edge-triggered synchronous  $J - K$  flip flops with outputs  $X$  and  $Y$ . If the initial state of the output is  $X = 0$  and  $Y = 0$  just before the arrival of the first clock pulse, the state of the output just before the arrival of the second clock pulse is (GATE-IN2019,12)

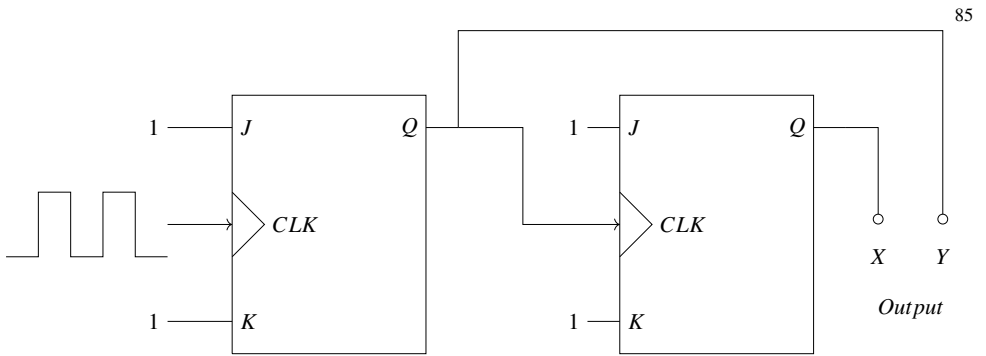


Fig. 5.19

- a)  $X = 0, Y = 0$
- b)  $X = 0, Y = 1$
- c)  $X = 1, Y = 0$
- d)  $X = 1, Y = 1$

20. Consider a 4-bit counter constructed out of four flip-flops. It is formed by connecting the J and K inputs to logic high and feeding the Q output to the clock input of the following flip-flop (see Fig. 5.20). The input signal to the counter is a series of square pulses and the change of state is triggered by the falling edge. At time  $t=t_0$  the outputs are in logic low state ( $Q_0 = Q_1 = Q_2 = Q_3 = 0$ ). Then at  $t=t_1$ , the logic state of the outputs is (GATE-PH2020,30)

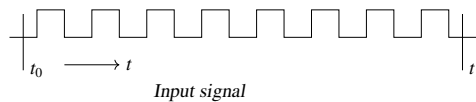
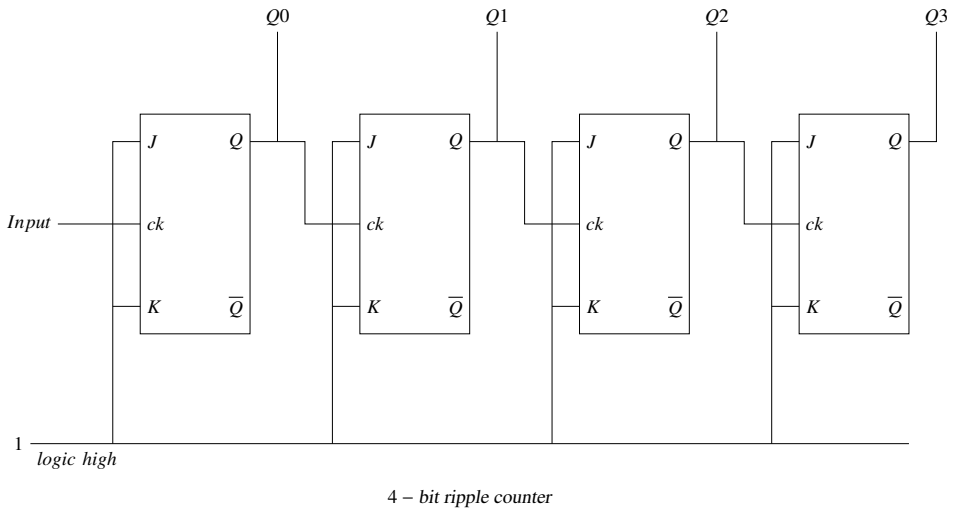


Fig. 5.20

- a)  $Q0 = 1, Q1 = 0, Q2 = 0$  and  $Q3 = 0$
- b)  $Q0 = 0, Q1 = 0, Q2 = 0$  and  $Q3 = 1$
- c)  $Q0 = 1, Q1 = 0, Q2 = 1$  and  $Q3 = 0$
- d)  $Q0 = 0, Q1 = 1, Q2 = 1$  and  $Q3 = 1$

21. Two T-flip flops are interconnected as shown in Fig. 5.21. The present state of the flip flops are:  $A = 1, B = 1$ . The input  $x$  is given as 1,0,1 in the next three clock cycles. The decimal equivalent of  $(AB_y)_2$  with  $A$  being the MSB and  $y$  being the LSB, after the 3<sup>rd</sup> clock cycle is \_\_\_\_\_.

(GATE IN2020 – 40)

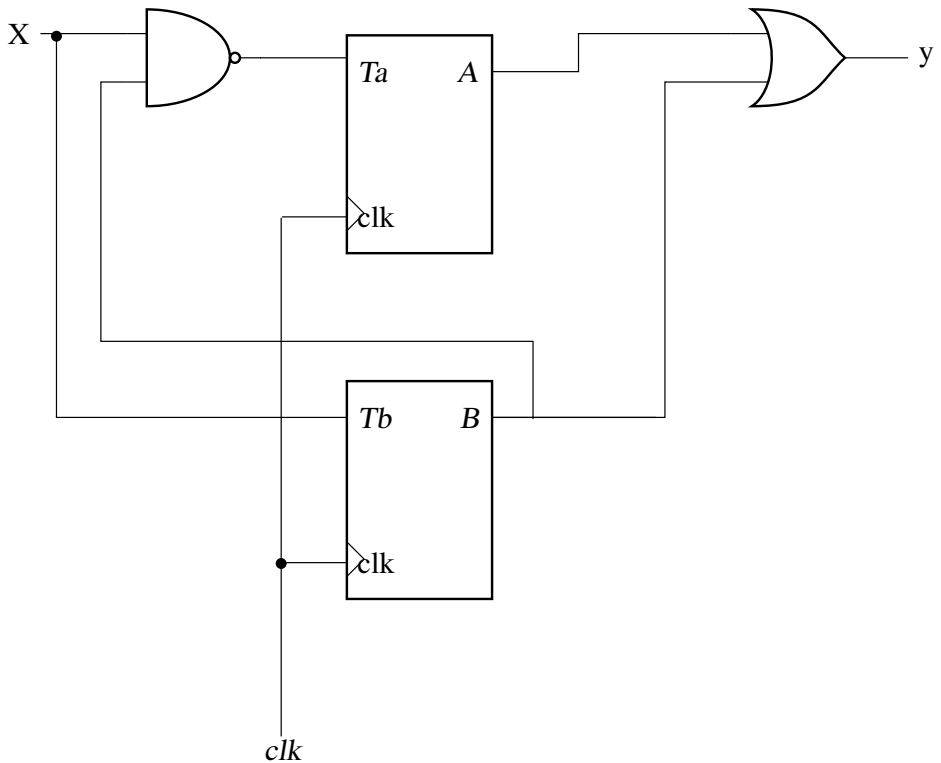


Fig. 5.21

22. For the components in the sequential circuit shown in Fig. 5.22 below,  $t_{pd}$  is the propagation delay,  $t_{setup}$  is the setup time, and  $t_{hold}$  is the hold time. The maximum clock frequency (rounded off to the nearest integer) at which the given circuit can operate reliably is \_\_\_\_\_MHZ. (GATE EC2020 – 50)

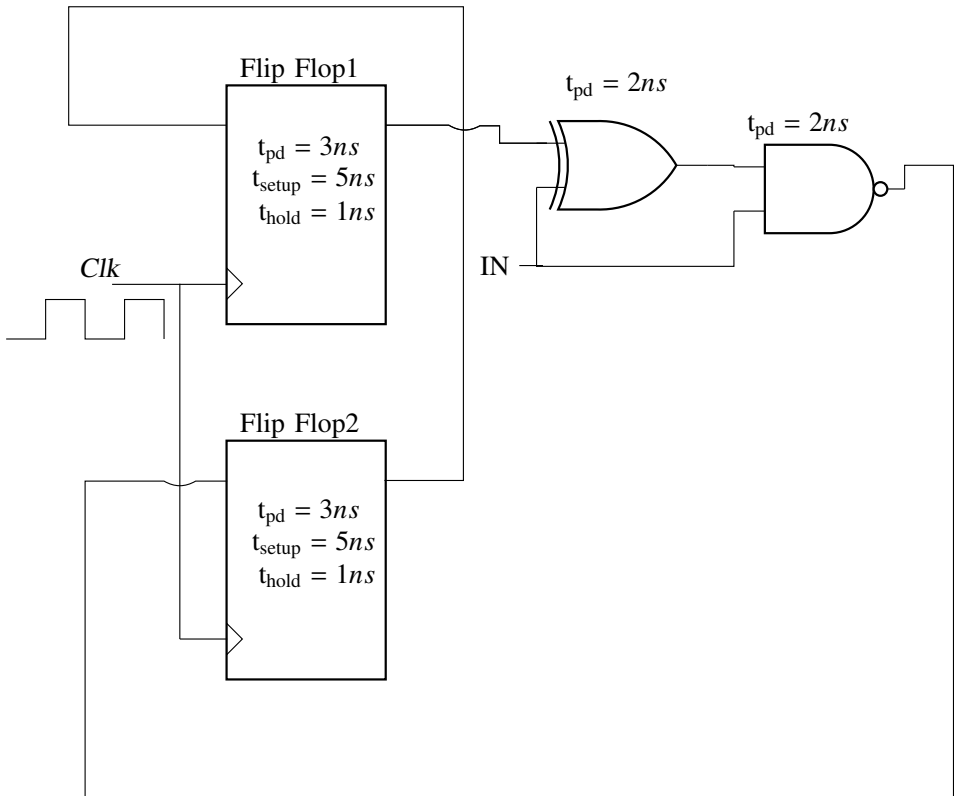


Fig. 5.22

23. A 2-bit synchronous counter using two J-K flip flops is shown in Fig. 5.23. The expression for the inputs to the J-K flip flops are also shown in the figure. The output sequence of the counter starting from  $Q_1 Q_2 = 00$  is GATE-IN2018,44

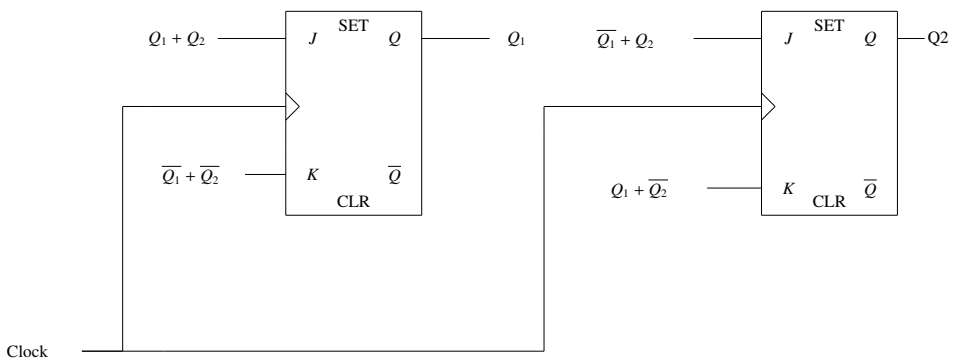


Fig. 5.23



- A.  $00 \rightarrow 11 \rightarrow 10 \rightarrow 01 \rightarrow 00 \dots$
- B.  $00 \rightarrow 01 \rightarrow 10 \rightarrow 11 \rightarrow 00 \dots$
- C.  $00 \rightarrow 01 \rightarrow 11 \rightarrow 10 \rightarrow 00 \dots$
- D.  $00 \rightarrow 10 \rightarrow 11 \rightarrow 01 \rightarrow 00 \dots$

24. Which of the following statements is true about digital circuits shown in Fig. 5.24?  
(Gate EE-2018,36)

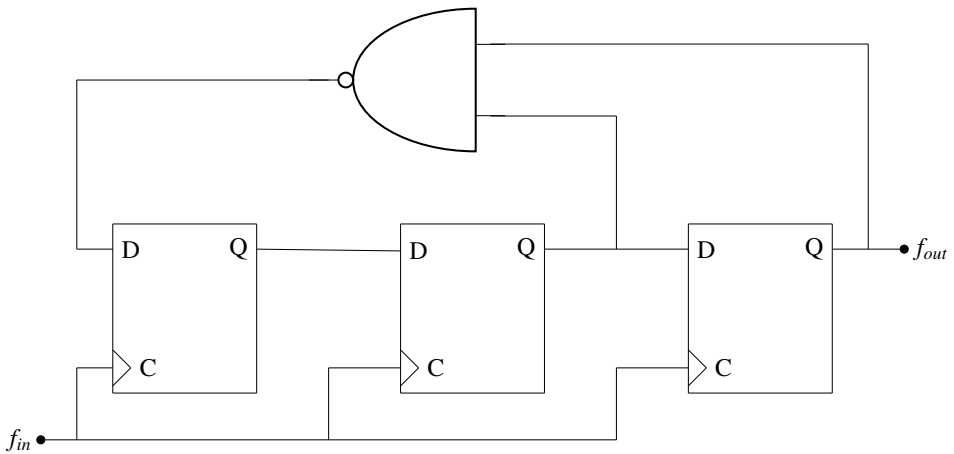


Fig. 5.24

- a) It can be used for dividing the input frequency by 3 .
  - b) It can be used for dividing the input frequency by 5 .
  - c) It can be used for dividing the input frequency by 7 .
  - d) It cannot be reliably used as frequency divider due to disjoint internal cycles .
25. In the circuit shown below, a positive edge-triggered  $D$  Flip-Flop is used for sampling input data  $D_{in}$  using clock  $CK$ . The  $XOR$  gate outputs 3.3 volts for logic HIGH and 0 volts for logic LOW levels. The data bit and clock periods are equal and the value of  $\Delta T/T_{CK} = 0.15$ ., where the parameters  $\Delta T$  and  $T_{CK}$  are shown in Fig. 5.25. Assume that the Flip-Flop and the  $XOR$  gate are ideal. If the probability of input data bit ( $D_{in}$ ) transition in each clock period is 0.3, the average value (in volts, accurate to two decimal places) of the voltage at node  $X$ , is .....

(GATE-EC 2018,46)

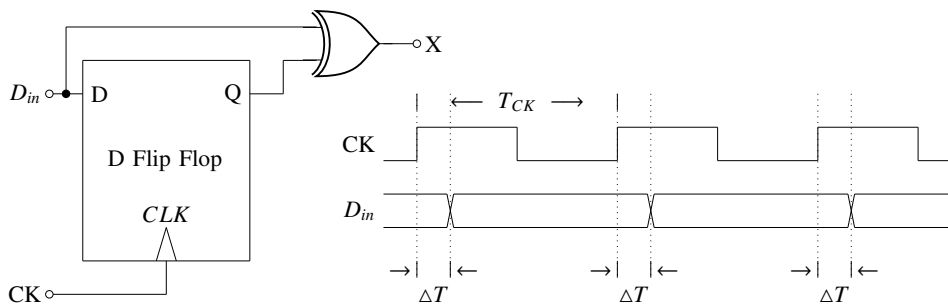


Fig. 5.25

26. Assume that all the digital gates in the circuit shown in Fig. 5.26 are ideal, the resistor  $R=10\text{k}\Omega$  and the supply voltage is  $5\text{V}$ . The  $D$  flip-flops  $D_1, D_2, D_3, D_4$  and  $D_5$  are initialized with logic values 0, 1, 0, 1, and 0, respectively. The clock has a 30% duty cycle.

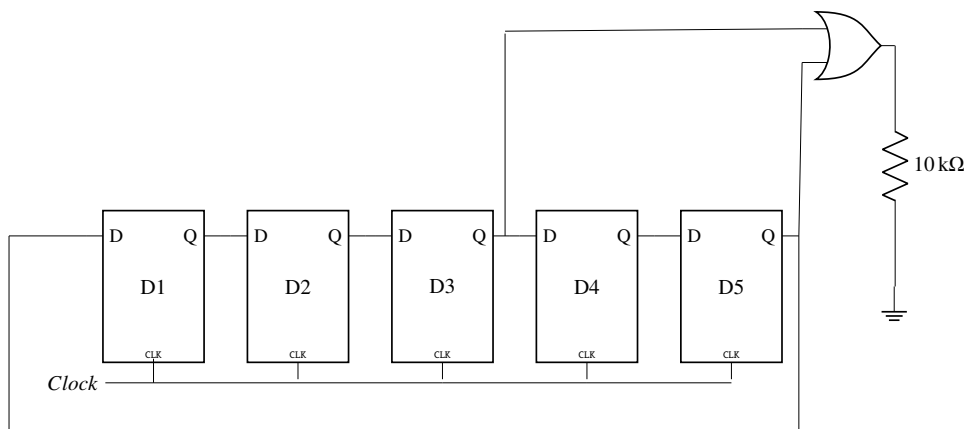


Fig. 5.26

The average power dissipated ( $\text{mW}$ ) in the resistor  $R$  is \_\_\_\_\_.

(GATE EC 2016)

27. The digital circuit shown in Fig. 5.27 generates a modified clockpulse at the output. Sketch the output waveform. (GATE EE 2004)

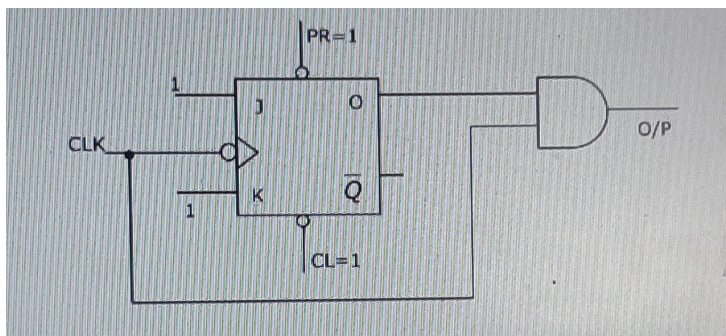


Fig. 5.27

28. The circuit shown in Fig. 5.28 below uses ideal positive edge-triggered synchronous J-K flip flops with outputs X and Y. If the initial state of the output is  $X=0$  and  $Y=0$ , just before the arrival of the first clock pulse, the state of the output just before the arrival of the second clock pulse is (GATE IN 2019)

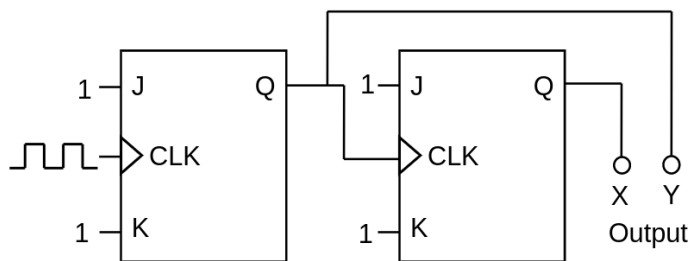


Fig. 5.28

29. A counter is constructed with three D flip-flops. The input-output pairs are named  $(D_0, Q_0)$ ,  $(D_1, Q_1)$ , and  $(D_2, Q_2)$ , where the subscript 0 denotes the least significant bit. The output sequence is desired to be the Gray-code sequence 000, 001, 011, 010, 110, 111, 101, and 100, repeating periodically. Note that the bits are listed in the  $Q_2 Q_1 Q_0$  format. Find the combinational logic expression for  $D_1$ . (GATE EE 2021)
30. For the circuit shown in Fig. 5.29, the clock frequency is  $f_0$  and the duty cycle is 25%. For the signal at the  $Q$  output of the Flip-Flop,
- frequency of  $\frac{f_0}{4}$  and duty cycle is 50%
  - frequency of  $\frac{f_0}{4}$  and duty cycle is 25%
  - frequency of  $\frac{f_0}{2}$  and duty cycle is 50%
  - frequency of  $f_0$  and duty cycle is 25%

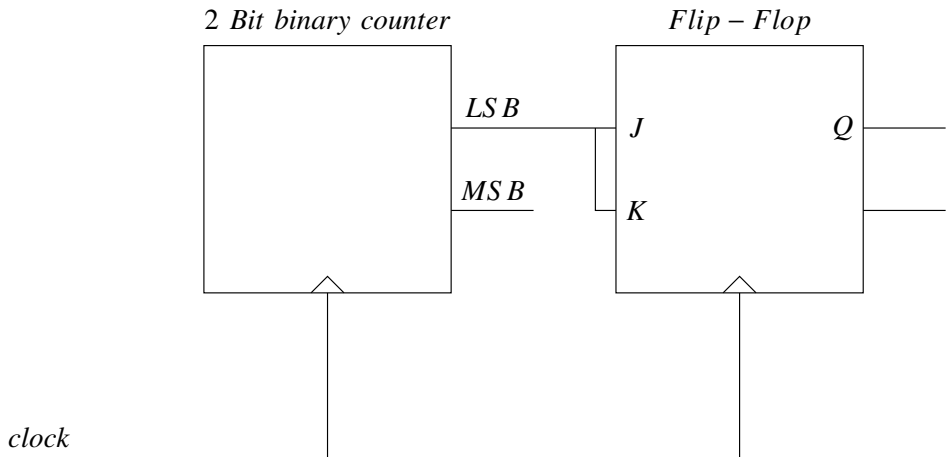


Fig. 5.29

(GATE EC-2022)

31. Two T-flip flops are interconnected as shown in Fig. 5.30. The present state of the flip flops are:  $A = 1, B = 1$ . The input  $x$  is given as 1, 0, 1 in the next three clock cycles. The decimal equivalent of  $(AB)_2$  with  $A$  being the MSB and  $y$  being the LSB, after the 3<sup>rd</sup> clock cycle is \_\_\_\_\_

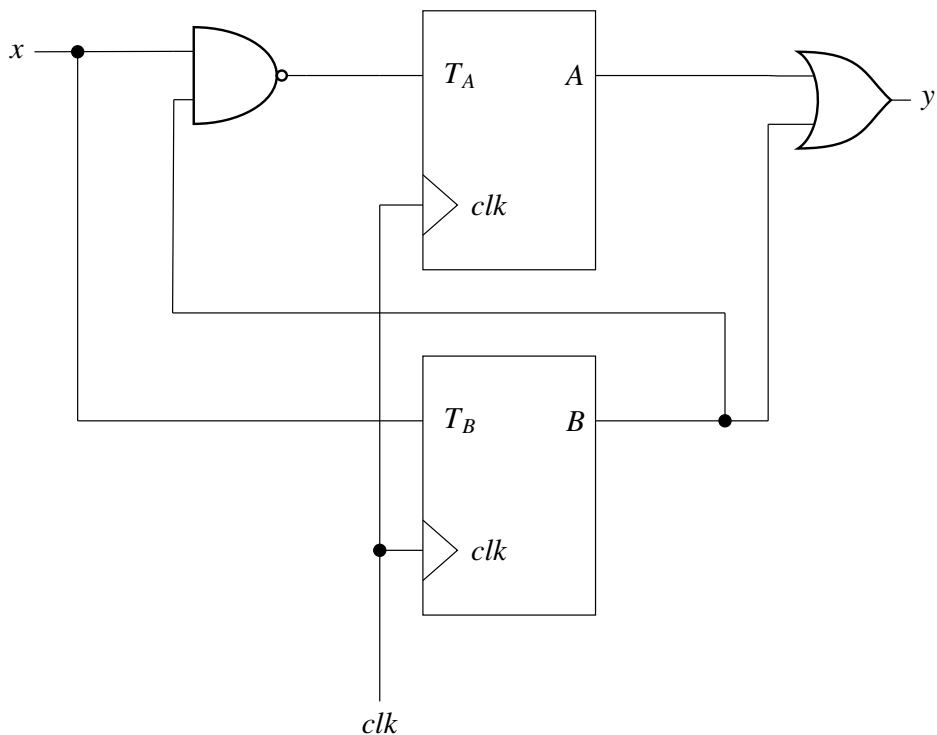


Fig. 5.30

(GATE IN 2020)

32. In the circuit shown below in Fig. 5.31 a positive edge-triggered D flip-flop is used for sampling input data using clock CK. The XOR gate outputs 3.3 volts for logic HIGH and 0 volts for logic LOW levels. The data bit and clock periods are equal and the value of  $\Delta T/T_{ck} = 0.15$ , where the parameters  $\Delta T$  and  $T_{ck}$  are shown in the figure. Assume that the Flip and the XOR gate are ideal.

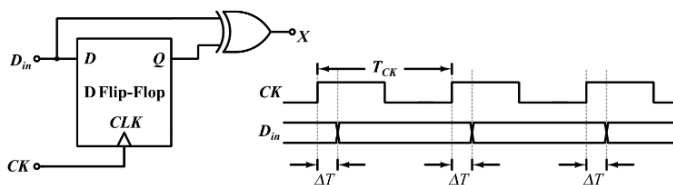


Fig. 5.31

(GATE EC 2018)

33. A 2-bit synchronous counter using two J-K flip flops is shown in Fig. 5.32. The expressions for the inputs to the J-K flip flops are also shown in the figure. The

output sequence of the counter starting from  $Q_1 Q_2 = 00$  is

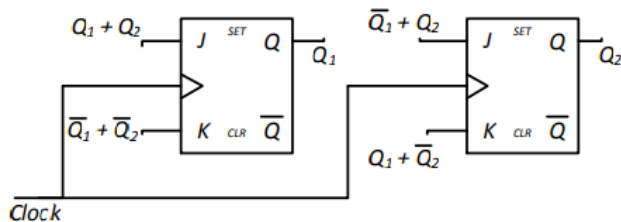


Fig. 5.32

- a)  $00 \rightarrow 11 \rightarrow 10 \rightarrow 01 \rightarrow 00 \dots$
- b)  $00 \rightarrow 01 \rightarrow 10 \rightarrow 11 \rightarrow 00 \dots$
- c)  $00 \rightarrow 01 \rightarrow 11 \rightarrow 10 \rightarrow 00 \dots$
- d)  $00 \rightarrow 10 \rightarrow 11 \rightarrow 01 \rightarrow 00 \dots$

GATE IN 2018

34. A 16-bit synchronous binary up-counter is clocked with the frequency  $f_{CLK}$ . The two most significant bits are **OR**-ed together to form an output  $Y$ . Measurements show that  $Y$  is periodic, and the duration for which  $Y$  remains high in each period is 24 ms. The clock frequency \_\_\_\_\_ MHz.  
(Round off to 2 decimal places.)

(GATE EE2021 – 22)

## 6 FINITE STATE MACHINE

We explain a state machine by deconstructing the decade counter

The block diagram of a decade counter (repeatedly counts up from 0 to 9) is available in Fig 5.2 The *incrementing* decoder and *display* decoder are part of *combinational* logic, while the *delay* is part of *sequential* logic

1. Fig. 6.1 shows a *finite state machine* (FSM) diagram for the decade counter in Fig 5.2  $s_0$  is the state when the input to the incrementing decoder is 0 The *state transition table* for the FSM is Table 3.5, where the present state is denoted by the variables  $W, X, Y, Z$  and the next state by  $A, B, C, D$ .

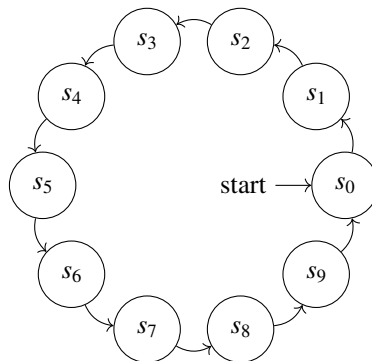


Fig. 6.1: FSM for the decade counter

2. The FSM implementation is available in Fig 6.2 The *flip-flops* hold the input for the time that is given by the *clock* This is nothing but the implementation of the *Delay* block in Fig 5.2

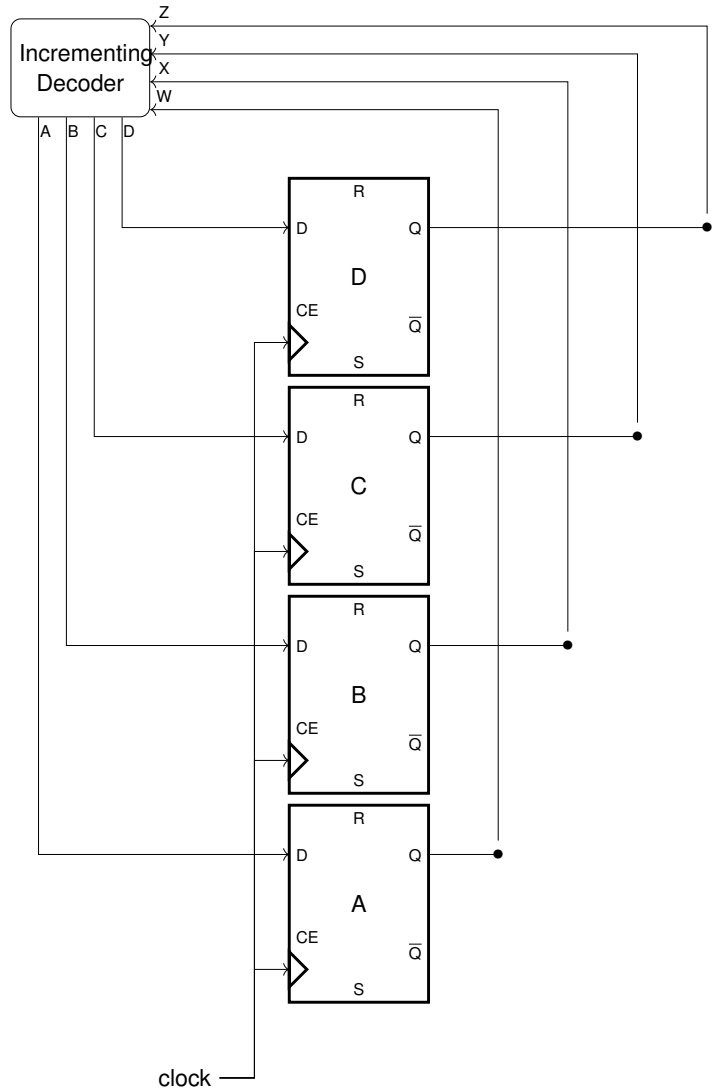


Fig. 6.2: Decade counter FSM implementation using D-Flip Flops

3. The hardware cost of the system is given by

$$\text{No of D Flip-Flops} = \lceil \log_2 (\text{No of States}) \rceil \quad (6.1)$$

For the FSM in Fig 6.1, the number of states is 9, hence the number flipflops required = 4

4. Draw the state transition diagram for a decade down counter (counts from 9 to 0 repeatedly) using an FSM
5. Write the state transition table for the down counter



6. Obtain the state transition equations with and without don't cares
7. Verify your design using an arduino

### 6.1 Problems

1. The state diagram of a sequence detector is shown in Fig. 6.3. State  $S_0$  is the initial state of the sequence detector. If the output is 1, then (GATE EC 2020)

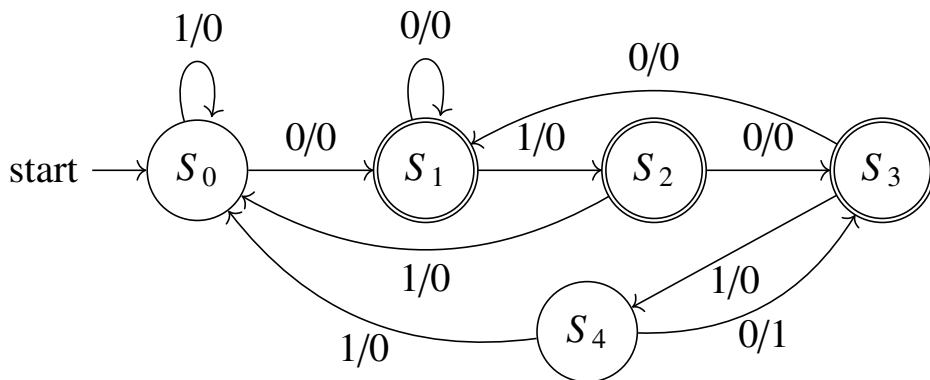


Fig. 6.3

- a) the sequence 01010 is detected
  - b) the sequence 01011 is detected
  - c) the sequence 01110 is detected
  - d) the sequence 01001 is detected
2. A sequence detector is designed to detect precisely 3 digital inputs, with overlapping sequences detectable. For the sequence (1,0,1) and input data (1,1,0,1,0,0,1,1,0,1,0,1,1,0), what is the output of this detector?
    - a) 1,1,0,0,0,0,1,1,0,1,0,0
    - b) 0,1,0,0,0,0,0,1,0,1,0,0
    - c) 0,1,0,0,0,0,0,1,0,1,1,0
    - d) 0,1,0,0,0,0,0,0,1,0,0,0
- (GATE EE 2020)
3. Consider a 3-bit counter, designed using T flip-flops, as shown below in Fig. 6.4

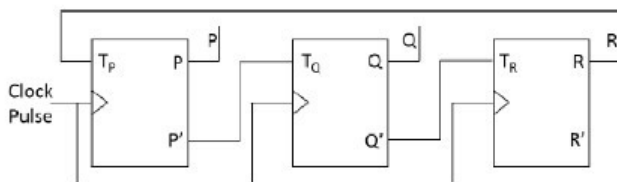


Fig. 6.4

Assuming the initial state of the counter given by  $PQR$  as 000, what are the next three states? (GATE-CS2021)

- (A) 011, 101, 000
- (B) 010, 101, 000
- (C) 010, 101, 000
- (D) 010, 101, 000

4. The state diagram of a sequence detector is shown below. state  $S_0$  is the initial state of the sequence detector. If the output is 1, then (GATE-EC2020,39)

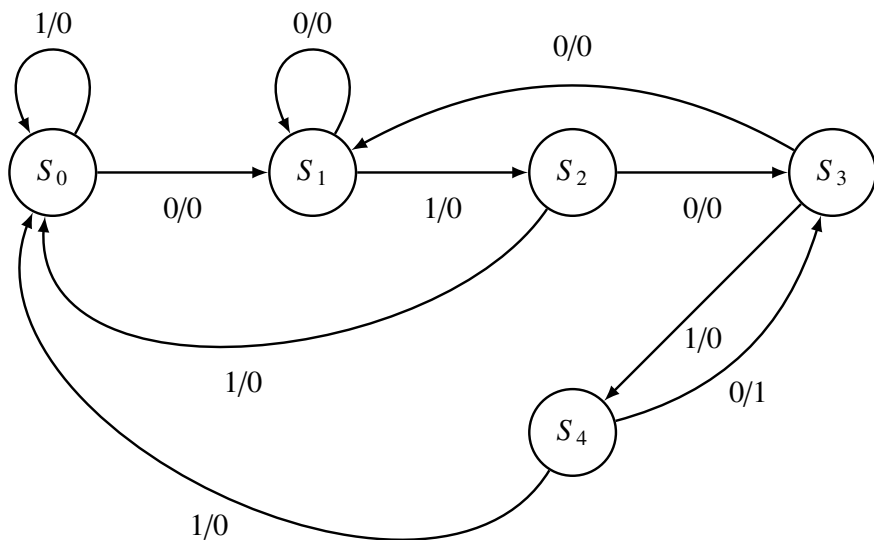


Fig. 6.5

- a) the sequence 01010 is detected.
- b) the sequence 01011 is detected.
- c) the sequence 01110 is detected.
- d) the sequence 01001 is detected.

5. The state transition diagram for the circuit shown in Fig. 6.6 is (GATE-IN2019,39)

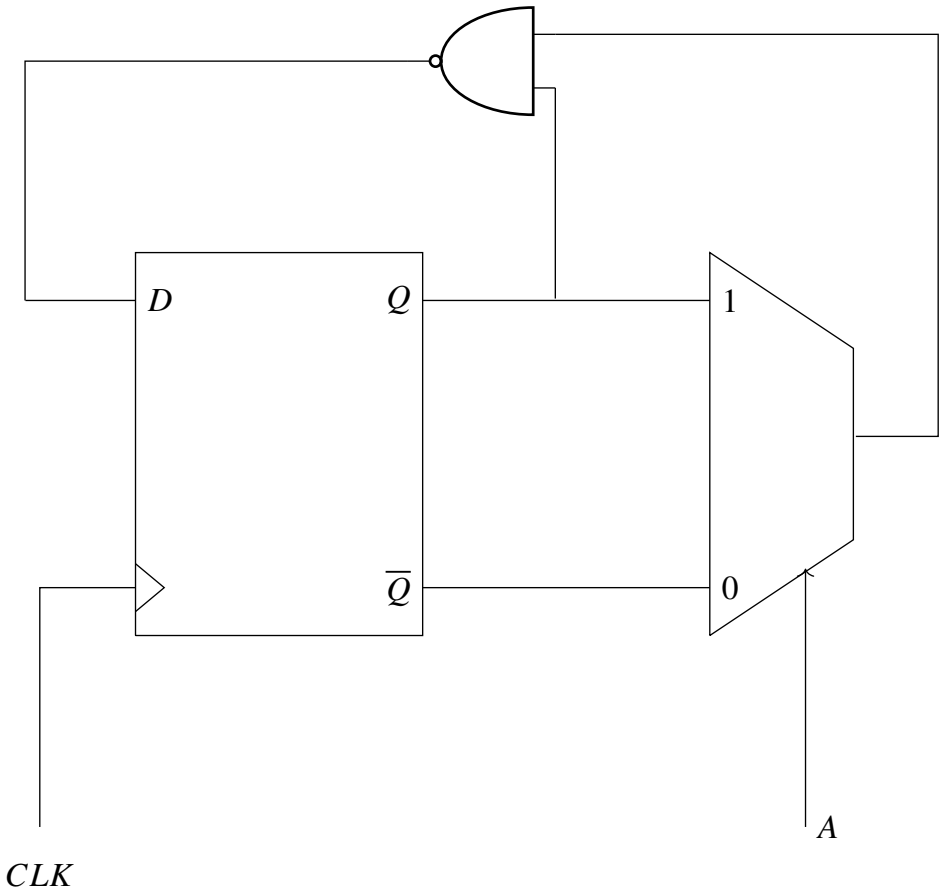


Fig. 6.6

a) Fig. 6.7

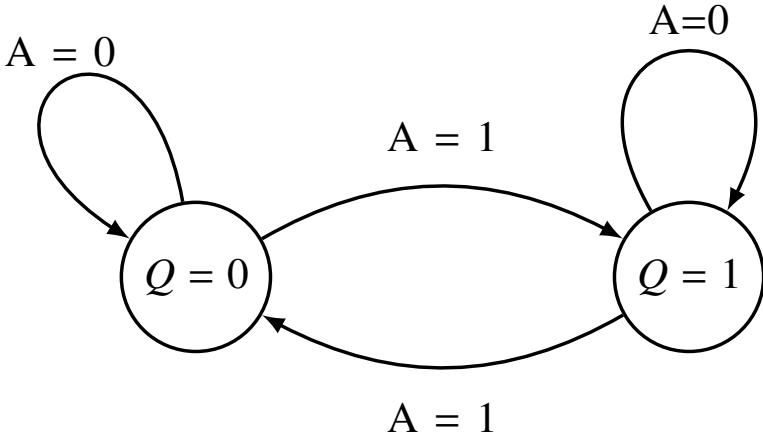


Fig. 6.7

b) Fig. 6.8

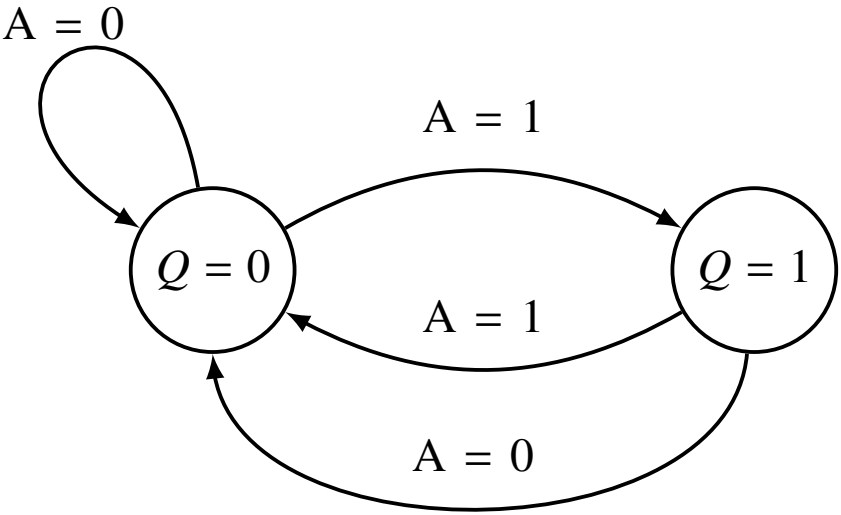


Fig. 6.8

c) Fig. 6.9

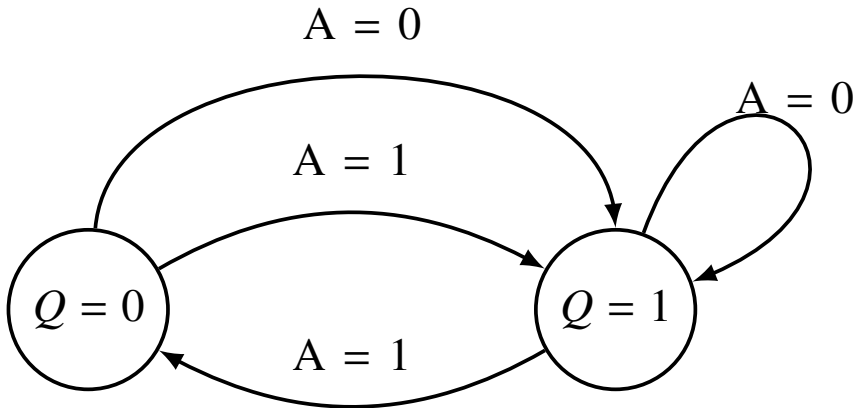


Fig. 6.9

d) Fig. 6.10

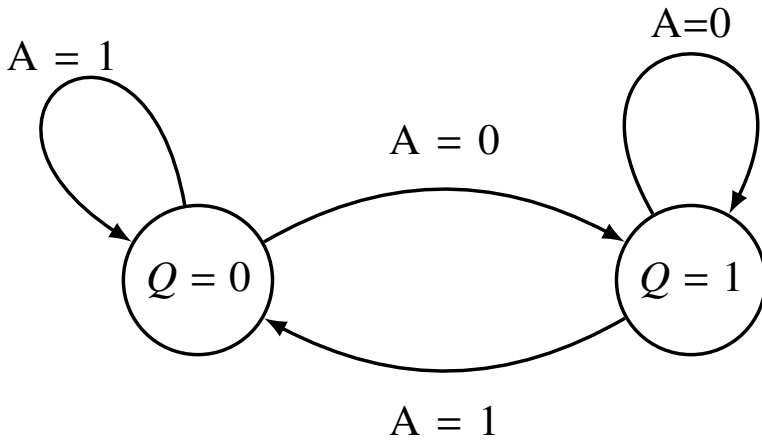


Fig. 6.10

6. A sequence detector is designed to detect precisely 3 digital inputs, with overlapping sequences detectable. For the sequence (1,0,1) and input data (1, 1, 0, 1, 0, 0, 1, 1, 0, 1, 0, 1, 1, 0), the output sequence is (GATE EE2020 – 15)

- a) (1, 1, 0, 0, 0, 0, 1, 1, 0, 1, 0, 0)
- b) (0, 1, 0, 0, 0, 0, 0, 1, 0, 1, 0, 0)
- c) (0, 1, 0, 0, 0, 0, 0, 1, 0, 1, 1, 0)
- d) (0, 1, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0)

7. A finite state machine (FSM) is implemented using the D flip-flops *A* and *B*, and logic gates, as shown in Fig. 6.11 below. The four possible states of the FSM are  $Q_A Q_B = 00, 01, 10$  and  $11$ .

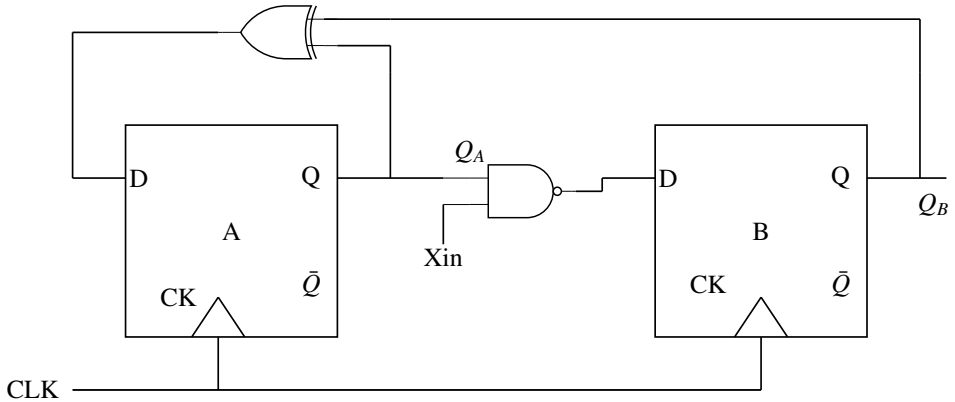


Fig. 6.11

Assume that  $X_{IN}$  is held at a constant logic level throughout the operation of the FSM. When the FSM is initialized to the state  $Q_A Q_B = 00$  and clocked, after a few clock cycles, it starts cycling through

- all of the four possible states if  $X_{IN} = 1$
- three of the four possible states if  $X_{IN} = 0$
- only two of the four possible states if  $X_{IN} = 1$
- only two of the four possible states if  $X_{IN} = 0$

(GATE EC 2017)

### 7.1 Setup

We show how to setup the assembly programming environment for the arduino.

1. Copy the .inc file to your home directory

```
cp assembly/setup/m328Pdef/m328Pdef.inc ~/
```

2. Execute

```
avra assembly/setup/codes/hello.asm
```

3. Then flash the .hex file

```
hello.hex
```

4. You should see the led beside pin 13 light up.
5. Now edit **hello.asm** by modifying the line to

```
ldi r17,0b00000000
```

Save and execute. The led should turn off.

6. What do the following instructions do?

```
ldi r16,0b00100000
out DDRB,r16
```

**Solution:** The Atmega328p microcontroller for the arduino board has 32 internal 8-bit registers, R0-R31. R16-R31 can be used directly for i/o. The first instruction loads an 8-bit binary number into R16. The second instruction loads the value in R16 to the DDRB register. Each bit of the DDRB register corresponds to a pin on the arduino. The second instruction declares pin 13 to be an output port. Both the instructions are equivalent to `pinMode(13, OUTPUT)`.

7. What do the following instructions do?

```
ldi r17,0b00100000
out PortB,r17
```

**Solution:** The instructions are equivalent to `digitalWrite(13)`.

### 7.2 Seven Segment Display

We show how to control a seven segment display through AVR-Assembly.

1. See Table 2.1 for components.
2. Complete Table 7.1 for all the digital pins using Fig. 7.1.

Port Pin	Digital Pin
PD2	2
PB5	13

TABLE 7.1

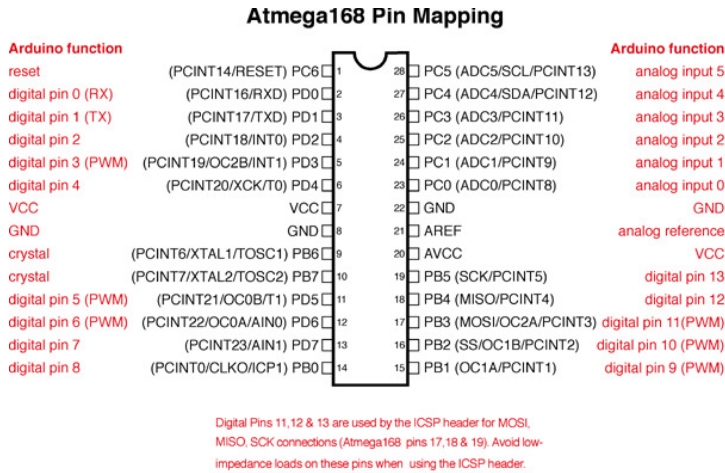


Fig. 7.1

3. Make connections according to Table 7.2.

Arduino	2	3	4	5	6	7	8
	PD2	PD3	PD4	PD5	PD6	PD7	PB0
Display	a	b	c	d	e	f	g
0	0	0	0	0	0	0	1

TABLE 7.2

4. Execute the following code. The number 2 should be displayed.

```
assembly/sevenseg/codes/sevenseg.asm
```

5. Now generate the numbers 0-9 by modifying the above program.

### 7.3 7447

We show how to program the 7447 BCD-Seven segment display decoder through AVR-Assembly.

1. Verify the AND,OR and XOR operations in assembly using the following code and making pin connections according to Table 3.4

```
wget https://raw.githubusercontent.com/gadepall/arduino/master/assembly/7447/
count/codes/and_or_xor.asm
```

2. Suppose R20=0b00000010, R16=0b00000001. Explain the following routine

```
loopw: lsl r16 ;left shift
        dec r20 ;counter --
        brne loopw ;if counter != 0
        ret
```



**Solution:** The routine shifts R16 by 2 bits to the left (the count in R20=2). At the end of the routine, R16=0b00000100.

3. What do the following instructions do?

```
rcall loopw
out PORTD,r16 ;writing output to pins 2,3,4,5
```

**Solution:** **rcall** calls for execution of the **loopw** routine, which shifts R16 by 2 bits to the left and writes R16 to the display through PORTD.

4. Use the following routine for finding the complement of a number.

```
wget https://raw.githubusercontent.com/gadepall/arduino/master/assembly/7447/
count/codes/complement.asm
```

5. Write an assembly program for implementing the following equations. Note that ZYXW is the input nibble and DCBA is the output nibble. Display DCBA on the seven segment display for each input ZYXW from 0-9.

$$A = W' \quad (7.1)$$

$$B = WX'Z' + W'X \quad (7.2)$$

$$C = WXY' + X'Y + W'Y \quad (7.3)$$

$$D = WXY + W'Z \quad (7.4)$$

6. Repeat the above exercise by getting ZYXW as manual inputs to the arduino from the GND and 5V pins on the breadboard.

#### 7.4 Display Control

We show how to program the 7447 BCD-Seven segment display decoder through AVR-Assembly.

1. Connect the 7447 IC to the seven segment display.
2. Make connections between the 7447 and the arduino according to Table 3.4.
3. Execute the following program. The number 5 will be displayed.

```
assembly/7447/io/codes/op_7447.asm
```

4. Now generate the numbers 0-9 by modifying the above program.
5. Execute the following program after making the connections in Table 7.3. The number 3 will be displayed. What does the program do?

```
assembly/7447/io/codes/ip_7447.asm
```

	Z	Y	X	W
<b>Input</b>	0	0	1	1
<b>Arduino</b>	13	12	11	10

TABLE 7.3

**Solution:** The program reads from pins 10-13 and displays the equivalent decimal value on the display by writing to pins 2-5 of the arduino.

6. Explain the following instructions

```
ldi r17, 0b11000011 ; identifying input pins 10,11,12,13
ldi r17, 0b11111111 ;
out PORTB,r17 ;
in r17,PINB
```

**Solution:** First define pins 10,11,12 and 13 as input pins. Then ensure that these pins have the input 1 by default. Load the inputs from the pins in port B (which includes pins 10-13) into R17.

### 7.5 Blink through TIMER

We show how to use the Atmega328p timer to blink the builtin led with a delay.

1. Connect the Arduino to the computer and execute the following code

```
assembly/timer/codes/timer.asm
```

2. Explain the following instruction

```
sbi DDRB, 5
```

3. What do the following instructions do?

```
ldi r16, 0b00000101
out TCCR0B, r16
```

**Solution:** The system clock (SYSCLK) frequency of the Atmega328p is 16 MHz. TCCR0B is the Timer Counter Control Register. When

$$TCCR0B = 0b101 \quad (7.5)$$

$$\Rightarrow CLK = \frac{SYSCLK}{1024} \quad (7.6)$$

$$= \frac{16M}{1K} = 16kHz. \quad (7.7)$$

4. Explain the PAUSE routine.

```
ldi r19, 0b01000000 ;times to run the loop = 64 for 1 second delay
PAUSE: ;this is delay (function)
lp2: ;loop runs 64 times
    IN r16, TIFR0 ;tifr is timer interrupt flag (8 bit timer runs 256
        times)
    ldi r17, 0b00000010
    AND r16, r17 ;need second bit
    BREQ PAUSE
    OUT TIFR0, r17 ;set tifr flag high
    dec r19
```

```
brne lp2
ret
```

**Solution:** TIFR0 is the timer interrupt flag and TIFR0=0bxxxxxx10 after every 256 cycles. PAUSE routine waits till TIFR0=0bxxxxxx10, this checking is done by the AND and BREQ instructions above.

5. Explain the lp2 routine.

**Solution:** R19 = 64 and is used as a count for lp2. The lp2 routine returns after 64 PAUSE routines.

6. What is the blinking delay?

**Solution:** The blinking delay is given by

$$delay = \frac{CLK}{lp2 \times PAUSE} seconds \quad (7.8)$$

$$= \frac{16 \times 1024}{64 \times 256} seconds = 1second \quad (7.9)$$

### 7.6 Blink through Cycle Delays

1. Connect pin 8 of the Arduino to an led and execute the following code

```
assembly/timer/codes/cycle_delay.asm
```

2. Explain how the delay is obtained

```
ldi r16,0x50
ldi r17,0x00
ldi r18,0x00

w0:
dec r18
brne w0
dec r17
brne w0
dec r16
brne w0
pop r18
pop r17
pop r16
ret
```

**Solution:** The w0 loop is executed using the counts in R16=2<sup>6</sup> + 2<sup>4</sup> = 80, R17=R18=2<sup>8</sup> = 256. Thus

$$delay \approx 80 \times 256 \times 256 cycles \quad (7.10)$$

$$= \frac{80 \times 256 \times 256}{2^4 \times 2^{20}} seconds \quad (7.11)$$

$$= 0.3125 seconds \quad (7.12)$$

The actual time is slightly more since each instruction takes a few cycles to execute.

- Should you use timer delay or cycle delay?

**Solution:** Timer delay is an accurate method for giving delays. Cycle delay is a crude method and should be avoided.

## 7.7 Memory

This manual shows how to use the Atmega328p internal memory for a decade counter through a loop.

- Execute the following code by connecting the Arduino to 7447 through pins 2,3,4,5. The seven segment display should be connected to 7447.

```
assembly/memory/codes/mem.asm
```

- Explain the following instructions

```
ldi x1,0x00
ldi xh,0x01
ldi r16,0b00000000
st x,r16
```

**Solution:** X=R27:R26, Y=R29:R28, and Z=R31:R30 where R27:R26 represents XH:XL. The above instructions load 0b00000000 into the memory location X=0x0100.

- What does the **loop\_cnt** routine do?

```
ldi r16,0b00000000
ldi r17,0x09
loop_cnt:
inc r16
inc x1
st x,r16
dec r17
brne loop_cnt
```

**Solution:** The routine loads the numbers 1-9 in memory locations 0x0101 - 0x0109.

- Revise your code by using a timer for giving the delay.

## 7.8 Problems

- In a given 8-bit general purpose micro-controller there are following flags. C-Carry, A-Auxiliary Carry, O-Overflow flag, P-Parity (0 for even, 1 for odd) R0 and R1 are the two general purpose registers of the micro-controller. After execution of the following instructions, the decimal equivalent of the binary sequence of the flag pattern [CAOP] will be \_\_\_\_.

```
MOV R0,+0x60
MOV R1,+0x46
ADD R0,R1
```

(EE GATE 2023)

2. Consider the given C-code and its corresponding assembly code, with a few operands U1-U4 being unknown. Some useful information as well as the semantics of each unique assembly instruction is annotated as inline comments in the code.

```
int a[10],b[10],i;
//int is 32-bit
for (i=0;i<10;i++)
a[i]=b[i]*8;
```

```
;r1-r5 are 32-bit integer registers
;initialize r1=0,r2=0
;initialize r3,r4 with base address of a,b

L01:jeq r1,r2,end ;if(r1==r2) goto end
L02:lw r5,0(r4) ;r5<-Memory[r4+0]
L03:shl r5,r5,U1 ;r5<-r5<<U1
L04:sw r5,0(r3) ;Memory[r3+0]<- r5
L05:add r3,r3,U2 ;r3<-r3+U2
L06:add r4,r4,U3
L07:add r1,r1,1
L08:jmp U4 ;goto U4
L09:end
```

3. Which one of the following options is a CORRECT replacement for operands in the position (U1,U2,U3,U4) in the above assembly code?
- (8,4,1,L02)
  - (3,4,4,L01)
  - (8,1,1,L02)
  - (3,1,1,L01)
4. An 8085 microprocessor accesses two memory locations (2001H) and (2002H), that contain 8-bit numbers 98H and B1H, respectively. The following program is executed:

```
LXI H,2001H
MVI A,21H
INX H
ADD M
INX H
MOV M,A
HLT
```

At the end of this program, the memory location 2003H contains the number in decimal (*base*10) form \_\_\_\_\_.

(GATE EE2020 – 54)

5. Which of the following is the correct binary equivalent of the hexadecimal F6C?  
(GATE PH2020, 6)

- a) 011011111100
- b) 111101101100
- c) 110001101111
- d) 011011000111

6. A portion of an assembly language program written for an 8-bit microprocessor is given below along with explanations. The code is intended to introduce a software time delay. The processor is driven by a 5 MHz clock. The time delay (in  $\mu$ s) introduced by the program is

MVI B, 64H; Move immediate the given byte into register B. Takes 7 clock periods.

LOOP: DCR B ; Decrement register B. Affects Flags. Takes 4 clock periods.

JNZ LOOP ; Jump to address with Label LOOP if zero flag is not set. Takes 10 clock periods when jump is performed and 7 clock periods when jump is not performed.

(GATE IN 2018)

7. A  $10\frac{1}{2}$  digit Counter-timer is set in the 'frequency mode' of operation (with  $T_s = 1$  s). For a specific input, the reading obtained is 1000. Without disconnecting this input, the Counter-timer is changed to operate in the 'Period mode' and the range selected is microseconds ( $\mu$ s, with  $f_s = 1$  MHz). The Counter Will then display (GATE IN 2021)

- a) 0
- b) 10
- c) 100
- d) 1000

8. Consider three registers **R1**, **R2**, **R3** that store numbers in *IEEE – 754* single precision floating point format. Assume that **R1** and **R2** contain the values (in hexadecimal notation) 0x42200000 and 0xC1200000, respectively. If  $\mathbf{R3} = \frac{\mathbf{R1}}{\mathbf{R2}}$ , what is the value stored in **R3**? (GATE-EC2021,31)

- a) 0x40800000
- b) 0xC0800000
- c) 0x83400000
- d) 0xC8500000

9. The content of the registers are  $R_1 = 25H$ ,  $R_2 = 30H$  and  $R_3 = 40H$ . The following

machine instructions are executed.

*PUSH*{ $R_2$ }

*PUSH*{ $R_2$ }

*PUSH*{ $R_3$ }

*POP*{ $R_1$ }

*POP*{ $R_2$ }

*POP*{ $R_3$ }

After execution, the content of registers  $R_1$ ,  $R_2$ ,  $R_3$  are

(GATE-EC2021,32)

- a)  $R_1 = 40H, R_2 = 30H, R_3 = 25H$
- b)  $R_1 = 25H, R_2 = 30H, R_3 = 40H$
- c)  $R_1 = 30H, R_2 = 40H, R_3 = 25H$
- d)  $R_1 = 40H, R_2 = 25H, R_3 = 30H$

### 8.1 Blink

We show how to control an led using AVR-GCC. AVR-GCC is a C compiler for the Atmega328p.

1. Execute the following

```
cd avr-gcc/setup/codes  
  
make
```

2. Now open **main.c**. Explain the following lines.

```
PORTB = ((0 << PB5));  
    _delay_ms(500);  
//turn led on  
PORTB = ((1 << PB5));  
    _delay_ms(500);
```

**Solution:** `((0 << PB5))` writes 0 to pin 13 (PB5). `_delay_ms(500)` introduces a delay of 500 ms.

3. Modify the above code to keep the led on.
4. Repeat the above exercise to keep the led off.

### 8.2 Display Control

We show how to control a seven segment display using AVR-GCC with arduino

1. Connect the arduino to the seven segment display
2. Execute the following code

```
avr-gcc/sevenseg/codes/main.c
```

3. Modify the above code to generate numbers between 0-9.
4. Now connect the arduino to the seven segment display through 7447.
5. Execute the following code

```
avr-gcc/input/codes/main.c
```

6. Modify the above code to work without the 7447.

### 8.3 GCC-Assembly

We show how to write a function in assembly and call it in a C program while programming the ATmega328P microcontroller in the Arduino. This is done by controlling an LED.

1. Execute

```
cd avr-gcc/gcc-assembly/codes  
make
```



2. Modify **main.c** and **Makefile** to turn the builtin led on.
3. Repeat the above exercise to turn the LED off.
4. Explain how the **disp\_led(0)** function is related to **Register R24** in **disp\_led** routine in **displedasm.S**.

**Solution:** The function argument 0 in **disp\_led(0)** is passed on to R24 in the assembly routine for further operations. Also, the registers R18-R24 are available for storing more function arguments according to the Table 8.1. More details are available in official ATMEL AT1886 reference.

Register	r19	r18	r21	r20	r23	r22	r25	r24
Function Argument	b7	b6	b5	b4	b3	b2	b1	b0

TABLE 8.1: Relationship between Register in assembly and function argument in C

5. Write an assembly routine for controlling the seven segment display and call it in a C program.
6. Build a decade counter with **main.c** calling all functions from assembly routines.

## 8.4 LCD

We show how to interface an Arduino to a  $16 \times 2$  LCD display using AVR-GCC. This framework provides a useful platform for displaying the output of AVR-Assembly programs.

1. The required components are listed in Table 8.2

Component	Value	Quantity
Resistor	220 Ohm	1
	1K	1
Arduino	Uno	1
Jumper Wires		20

TABLE 8.2

2. Plug the LCD in Fig. 8.1 to the breadboard.
3. Connect the Arduino pins to LCD pins as per Table 8.3.

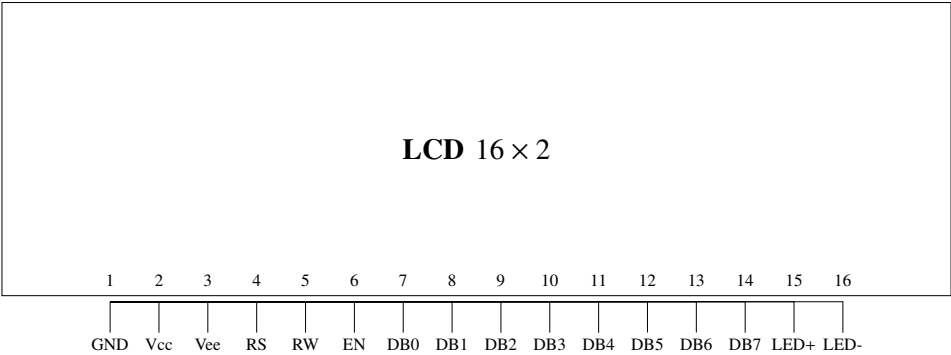


Fig. 8.1: LCD

TABLE 8.3: Arduino to LCD Pin Connection.

Arduino Pins	LCD Pins	LCD Pin Label	LCD Pin Description
GND	1	GND	
5V	2	Vcc	
GND	3	Vee	
D12	4	RS	Register Select
GND	5	R/W	Read/Write
D11	6	EN	Enable
D5	11	DB4	Serial Connection
D4	12	DB5	Serial Connection
D3	13	DB6	Serial Connection
D2	14	DB7	Serial Connection
5V	15	LED+	Backlight
GND	16	LED-	Backlight

4. Execute

cd avr-gcc/lcd/codes  
make

5. Modify the above code to display a string.
6. Modify the above code to obtain a decade counter so that the numbers from 0 to 9 are displayed on the lcd repeatedly.
7. Repeat the above exeries to display a string on the first line and a number on the second line of the lcd.
8. Write assembly routines for driving the lcd.

8.5 Problems

- 1) The representation of the decimal number  $(27.625)_{10}$  in base-2 number is
- (A) 11011.110

- (B) 11101.101
- (C) 11011.101
- (D) 10111.110

(GATE IN 2018)