# Proceedings of the ninth South African

SYMPOSIUM
ON
NUMERICAL MATHEMATICS

Durban 18, 19 & 20 July 1983

sanum & the dept.of computer science university of natal durban

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edited by JA Snyman

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#### PREFACE

Since the first symposium on Numerical Mathematics held in 1975, the Symposia, organised by the Department of Computer Science of the University of Natal, have become major annual events on the South African mathematical calendar. The ninth Symposium, the second to be organised in conjunction with the South African Society for Numerical Mathematics (SANUM), was held in Durban on 18, 19 and 20 July 1983. A total of 29 papers were read to a gathering of more than 40 delegates.

The Proceedings are a published record of most of the papers presented. The choice was left to the authors as to whether they wished to publish their papers in full or as a summary. All contributions included in the Proceedings are published as received from authors.

Invited papers were read by Professor LM Delves of the University of Liverpool and by Professor Victor Pereyra of the University of Venezuela.

The organisers again wish to express their gratitude to IBM (South Africa) for their generous financial support, not only of the Ninth Symposium, but for their sponsorship over the years since the inaugural Symposium in 1975. Through their assistance we are able to look forward to celebrating the Tenth Symposium on Numerical Mathematics on 2-4 July 1984. This support has enabled us to regularly invite overseas speakers thus greatly stimulating research in this field in Southern Africa. Our sincere thanks also to Univac for their generous contribution to our Ninth Symposium.

The Society also wishes to express a special word of appreciation and thanks to Ms Ethel Carte of the Computer Science Department for assisting with the organisation of the Symposium.

JA Snyman (Secretary SANUM)

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