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#### Outline

#### 1. Motivation

1.1. The Basic Problem That We Studied

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#### What Are Prime Numbers?

#### **Definition: Prime number**

A prime number is a number that has exactly two divisors.

#### Example:

- 2 is prime (two divisors: 1 and 2).
- 3 is prime (two divisors: 1 and 3).
- 4 is not prime (three divisors: 1, 2, and 4).

**Theorem: Prime numbers** 

There is no largest prime number.

#### **Proof:**

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- 2. Let q be the product of the first p numbers.
- 3. Then q+1 is not divisible by any of them.
- 4. But q + 1 is greater than 1, thus divisible by some prime number not in the first p numbers.

The proof used reductio ad absurdum.

#### What's Still To Do?

- Answered Questions
  - How many primes are there?
- Open Questions
  - Is every even number the sum of two primes?

### An Algorithm For Finding Prime Numbers.

## FindPrimeNumbers int main (void) std::vector<bool> is\_prime (100, true); for (int i = 2; i < 100; i++) if (is\_prime[i]) std::cout << i << "\_"; for (int j = i; j < 100; is\_prime [j] = false, j+=i); return 0:

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### References I (1)

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- [2] William Labov. Sociolinguistic Patterns. Philadelphia: University of Pennsylvania Press, 1972.