Euclid of Alexandria

euclid@alexandria.edu

27th International Symposium of Prime Numbers

Outline

1. Motivation

1.1. The Basic Problem That We Studied

1. Motivation

1.1 The Basic Problem That We Studied

1. Motivat.

What Are Prime Numbers?

Definition

A prime number is a number that has exactly two divisors.

Definition

- 2 is prime (two divisors: 1 and 2).
- 3 is prime (two divisors: 1 and 3).
- 4 is not prime (three divisors: 1, 2, and 4).

The proof uses reductio ad absurdum

Theorem

There is no largest prime number.

Proof

1 Suppose p were the largest prime number.

The proof uses reductio ad absurdum

Theorem

There is no largest prime number.

Proof

- 1 Suppose *p* were the largest prime number.
- Let q be the product of the first p numbers.

The proof uses reductio ad absurdum

Theorem

There is no largest prime number.

Proof

- 1 Suppose *p* were the largest prime number.
- Let q be the product of the first p numbers.
- Then q + 1 is not divisible by any of them.

The proof uses reductio ad absurdum

Theorem

There is no largest prime number.

Proof

- 1 Suppose *p* were the largest prime number.
- Let q be the product of the first p numbers.
- Then q + 1 is not divisible by any of them.
- But q + 1 is greater than 1, thus divisible by some prime number not in the first p numbers.

The proof used reductio ad absurdum.

What's Still To Do?

- Answered Questions
 - How many primes are there?
- Open Questions
 - Is every even number the sum of two primes?

An Algorithm For Finding Prime Numbers.

Finding Prime Numbers

```
int main (void)
{
    std::vector<bool> is_prime (100, true);
    for (int i = 2; i < 100; i++)
        if (is_prime[i])
        {
            std::cout << i << "_";
            for (int j = i; j < 100; is_prime [j] = false, j+=i);
        }
    return 0;
}</pre>
```

An Algorithm For Finding Prime Numbers.

Finding Prime Numbers

```
int main (void)
{
    std::vector<bool> is_prime (100, true);
    for (int i = 2; i < 100; i++)
        if (is_prime[i])
        {
            std::cout << i << "_";
            for (int j = i; j < 100; is_prime [j] = false, j+=i);
        }
    return 0;
}</pre>
```

Note the use of std::.