# My Courses / My courses / Algorithms and Data Structures, MSc (Spring 2023) / Old exams / Exam 13 May 2020

Started on Wednesday, 19 April 2023, 10:16

**State** Finished

Completed on Wednesday, 19 April 2023, 10:19

**Time taken** 2 mins 45 secs

**Grade** 0.00 out of 25.00 (0%)

#### Question 1

Complete

Mark 0.00 out of 1.00

Which pair of functions satisfies  $f(N) \sim g(N)$ ?

### Select one:

$$\circ$$
 a.  $f(N) = 2N \log_2 N$  and  $g(N) = 2N + \log_2 N$ 

$$\circ$$
 b.  $f(N) = N \log_2 N$  and  $g(N) = N + \log_2 N$ 

$$\circ$$
 c.  $f(N) = 2N \log_2 N$  and  $g(N) = 2N + N$ 

$$\circ$$
 d.  $f(N) = 2N \log_2 N + \log_2 N$  and  $g(N) = 2N \log_2 N$ 

### Question 2

Not answered

Marked out of 1.00

For which pair of functions does it hold that f(N) is O(g(N))?

$$\bigcirc$$
 a.  $f(N) = N^3$  and  $g(N) = (\log N)^3$ 

$$\bigcirc$$
 b.  $f(N)=N^3$  and  $g(N)=3N$ 

$$\circ$$
 c.  $f(N) = 3N$  and  $g(N) = N^3 \log N$ 

$$\bigcirc$$
 d.  $f(N) = N^3$  and  $g(N) = N^2 \log N$ 

# Question $\bf 3$

Not answered

 $\circ$  c.  $\sim 2n$  $\odot$  d.  $\sim n \log_2 n$ 

```
Marked out of 1.00
 How many stars are printed?
 # python
 for i in range(n):
     if i % 2 == 0: # i is even
          print('**')
      else:
          print('*')
 // java
 for (int i = 0; i < n; i++) {
     if (i % 2 == 0) // i is even
          System.out.println("**");
      else
          System.out.println("*");
 Select one:
  \odot a. \sim n
  \odot b. \sim \frac{3}{2}n
```

## Question 4

Not answered

Marked out of 1.00

What is the asymptotic running time of the following piece of code?

(Give the smallest correct estimate.)

```
# python
i = 0
while i < n:
    print('*')
    i = i + 1
i = 1
while i < n:
    print('*')
    i = i * 2</pre>
```

```
// java
int i = 0;
while (i < n) {
    System.out.println("*");
    i = i + 1;
}
i = 1;
while (i < n) {
    System.out.println("*");
    i = i * 2;
}</pre>
```

- $\bigcirc$  a.  $O(n \log n)$
- $\bigcirc$  b.  $O(n^2)$
- $\circ$  c. O(n)
- $\bigcirc$  d.  $O(\log n)$

## Question 5

Not answered

Marked out of 1.00

Find a recurrence relation for the number A of arithmetic operations (additions, subtractions, multiplications, and divisions) performed by the following recursive method. The base case is A(0) = 0.

```
# python
def c(N):
    if N == 0:
        return 42
    else:
        return 2 * c(N - 1) + 2
```

```
// java
static int c(int N) {
   if (N == 0)
     return 42;
   else
     return 2 * c(N - 1) + 2;
}
```

Select one:

- $\circ$  a. A(N) = A(N-1) + 3
- $\bigcirc$  b. A(N) = 2 \* A(N-1) + 2
- $\bigcirc$  c. A(N) = 2 \* A(N-1) + 3
- $\bigcirc$  d. A(N) = A(N-1) + 2

#### Question 6

Not answered

Marked out of 1.00

#### (hard)

Recall that f(n) is O(g(n)) if there exists  $n_0 \ge 0$  and C > 0 such that  $f(n) \le C \cdot g(n)$  holds for all  $n \ge n_0$ . I claim the following:



Claim. Let h be a non-decreasing real function and assume that f and g are functions so that f(n) is O(g(n)). Then h(f(n)) is O(h(g(n))).

- igcup a. False, unless h is continuous.
- $\circ$  b. True. Consider, for instance,  $f(n) = 2\log_2 n$ ,  $g(n) = \log_2 n$ , and  $h(x) = 2^x$ .
- $\circ$  c. True, as seen from the definition, with  $n_0 = \min\{ n \mid f(n) \leq g(n) \}$  and C = f(0).
- Od. The claim makes no sense.
- $\circ$  e. True, as seen from the definition, with  $n_0=1$  and C=1.
- $\bigcirc$  f. Always true, no matter which function h is.
- $\circ$  g. False. Consider, for instance, f(n)=2n, g(n)=n, and  $h(x)=2^x$ .

Information

# Class S

The following questions are about the data structure defined by the following code:

```
class S:
    def __init__(self):
        self.a = [None]
        self.n = 0
    def size(self):
        return self.n
    def push(self, value):
        if self.n == len(self.a):
            self._resize(2 * len(self.a))
        self.a[self.n] = value
        self.n += 1
    def _resize(self, capacity):
        temp = [None] * capacity
        for i in range(self.n):
            temp[i] = self.a[i]
        self.a = temp
    def peek(self):
        return self.a[self.n - 1]
    def decimate(self):
        temp = [None] * (len(self.a) // 2)
        for i in range(self.n // 2):
            temp[i] = self.a[2 * i]
        self.a = temp
        self.n = self.n // 2
```

```
public class S {
    int[] a = new int[1];
    int n = 0;
    public int size() { return n; }
    public void push(int value) {
        if (n == a.length) resize(2 * a.length);
        a[n] = value;
        n += 1;
    private void resize(int capacity){
        int[] temp = new int[capacity];
        for (int i = 0; i < n; i++) temp[i] = a[i];
        a = temp;
    public int peek() { return a[n - 1]; }
    public void decimate() {
        int[] temp = new int[a.length / 2];
        for (int i = 0; i < n / 2; i++) temp[i] = a[2 * i];
        a = temp;
        n = n / 2;
    }
```

Answer:

Question 7
Not answered
Marked out of 1.00
What is the result of the following operations on a newly created object s of class S? Your answer must be exactly the string that is printed (not including the newline symbol) and not contain any additional explanation.
<pre># python s.push(3); s.push(4); s.push(5) print(s.peek())</pre>
<pre>// java s.push(3); s.push(4); s.push(5); System.out.println(s.peek());</pre>
Answer:
0
Question 8 Not answered
Marked out of 1.00
What is the result of the following operations on a newly created object s of class S? Your answer must be exactly the string that is printed (not including the newline symbol) and not contain any additional explanation.
<pre># python s.push(3); s.push(4); s.push(5); s.push(6); s.push(7); s.push(8) s.decimate() print(s.peek())</pre>
<pre>// java s.push(3); s.push(4); s.push(5); s.push(6); s.push(7); s.push(8); s.decimate(); System.out.println(s.peek());</pre>

question. "Draw" here means "show in such a way that it is nt to draw, e.g., an array of characters as

 $\bigcirc$  a.  $O(\log n)$ O b. Constant  $\circ$  c. O(n)

 $\bigcirc$  d.  $O(n \log n)$ 

stion 11	
answered	
red out of 2.00	
ard) I claim the following:	
Claim. The amortized cost of the operations S.push(), S.peek(), S.size(), and S.decimate() is constant.	
ecall that the amortized cost is the average number of array accesses that any sequence of these operations cause se, starting from an empty data structure.	es in the worst
the claim is true, write "True." followed by a concise argument.	
the claim is false, write "False." followed by a concise argument.	

Question 12	
Not answered	
Marked out of 1.00	
Add a method determine_sum() that returns the sum of the elements in the data structure. You can assume that all the elements are integers. You can use linear time. Don't change any other methods. Provide only the code for determine_sum:	õ
	/.

Question 13		
ot answered		
arked out of 1.00		
add a method fast_sum() that returns the sum of the elements in the data structure in <i>constant</i> worst-case hat all the elements are integers. You are allowed to change other methods and add new variables, but (of the class's original functionality or efficiency.		
rovide the complete class; try to closely follow the style of the original class.		

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following lines <b>p q</b> , add a

Answer:

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Question 15	
Not answered	
Marked out of 1.00	
Consider the key-value pairs	
A 0	
B 1 C 2	
	/mbol table, and let's agree to draw the result like this:
A:0 \	
B:1	
\ C:2	
Starting from an empty data structu	ire, insert the key-value pairs
C 1 O 2	
R 3	
0 4	
N 5 A 6	
in this order and draw the result.	

Question 16			
Not answered			
Marked out of 1.00			
Here's a heap of the lette	ers in <b>VIRUS</b> :		
V			

Call delMax() and insert('T') in that order and draw the result in the same style.

https://learnit.itu.dk/mod/quiz/review.php?attempt = 91670&cmid = 171378



Not answered

Marked out of 1.00

Let's draw 2-3-Trees using , | \/ like this:



Draw the 2-3 Tree resulting from inserting the letters of **VIRUS** in that order into an empty data structure.

#### Question 18

Not answered

Marked out of 1.00

I want to find the median of a sequence of n integers. To make things simple for this exercise, the integers are distinct and there is an odd number of them. For instance, the median of

# 10, 4, 1, 3, 8, 21, 7

is **7**.

Of the suggestions below, what's a correct way of doing this?

- $\bigcirc$  a. Insert into a heap pq and return the element at position pq[(n-1)/2].
- Ob. Mergesort the input and report the element in the middle of the resulting sequence.
- c. Shuffle the input in linear time, partition once by the first element in the shuffled list, and report the maximum of the left part.
- Od. Hash the elements (assuming constant lookup time) and report the key with the most collisions.
- e. Use two stacks for odd and even elements, respectively. Report the stacktop of the even stack.
- of. Compute the average (add the elements using a linear scan, divide by their number) and round to the nearest integer.

# Question 19

Not answered

Marked out of 1.00

We are running some graph algorithm on the following undirected, weighted, 6-vertex graph:

The algorithm already added the edges A–D, A–B, and B–C to a tree, in that order. Now it adds B–E. Which algorithm are we observing?

- O a. DFS
- ob. Dijkstra's
- oc. Kruskal's
- Od. Prim's

Information

# Island Infection

# Description

The world consists of R rows, each of length C. Each position is 0 ("water"), 1 ("land"), 2 ("virus"), or 3 ("human"). The virus spreads in the obvious fashion to non-water positions with a shared border. For instance, here is the development in a small world with R=1 and C=10:

```
0101211030 -> 0102221030 -> 0102222030
```

Note that the process stops here, and the human will never be infected.

Here are a few rounds of development in a world with R=4 and C=6:

```
111001 112001 122001 222001
112000 122000 222000 222000
011103 -> 012103 -> 022203 -> 022203
101111 101111 102111 102211
```

The process will continue beyond these 4 rounds, and you can convince yourself that the human will eventually ("før eller senere") be infected.

More precisely, a tile position marked 1 or 3 turns into a 2 in round i (we call that "getting infected") exactly if any of the at most 4 adjacent tiles (to the north, south, east, or west) contains a 2 in round i-1. Note that infections don't spread "diagonally across corners", as shown in the bottom left position in the larger example. No position ever changes back from 2, and no water position ever changes.

To fix notation, there are R rows, C columns, and K ones.

The goal is to determine if the human gets infected.

# Kattis problem

There are test cases on itu.islandinfection for you to run against. The algs4 libraries are available for both Python 3 and Java.

# Input

Input begins with R and C on the first line, followed by R lines of C symbols describing the starting world. There is exactly one 2 and exactly one 3 in the input. Example input for the larger example above:

```
4 6
111001
112000
011103
101111
```

# Output

The output is a single integer: 1 if the human will get infected, 0 otherwise.

# Test groups

There are test groups for various parameters for internal use; all you need to know is that test groups 1 and 2 have R=1.

Question 20
Not answered
Marked out of 2.00
Describe briefly and precisely, in prose, how to efficiently solve island infection when R=1.
On a separate line, state the asymptotic worst-case running time in terms of the parameters given in the problem description. Use the formulation "The running time is …" followed by a big-Oh expression. If you need, use $^a$ and $_a$ for superscripts and subscripts, such as $x^2$ for $x^2$ and $x^2$ and $x^2$ for $x^3$ and $x^4$ for $x^4$ and $x^4$ for $x^4$ and $x^4$ for $x^4$ for $x^4$ and $x^4$ for $x^4$ and $x^4$ for $x^4$ for $x^4$ for $x^4$ and $x^4$ for
On a separate line, state the submission ID of an implementation of your solution on <pre>itu.kattis.com</pre> . Use the formulation "My Kattis implementation is" followed by an integer. Important: The Kattis user of the submission ID must use your ITU email.

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Question 21	
Not answered	
Marked out of 3.00	
Describe briefly and precisely, in prose, how to efficien	tly solve island infection in general.
On a separate line, state the asymptotic worst-case rui	nning time in terms of the parameters given in the problem description. Use

On a separate line, state the submission ID of an implementation of your solution on itu.kattis.com. Use the formulation "My Kattis implementation is ..." followed by an integer. *Important*. The Kattis user of the submission ID must use your ITU email.

the formulation "The running time is ..." followed by a big-Oh expression. If you need, use ^ and \_ for superscripts and subscripts,

Information

## This is the end of the Exam Quiz.

such as x^2 for  $x^2$  and  $\log_2 n$  for  $\log_2 n$  .

## Remember:

- 1. Click "Finish Attempt ..." and click "Submit all and finish" at the bottom of the following page.
- 2. Then click "Finish Exam" up in the right corner after you submitted the quiz.
- 3. Finally uninstall the ProctorExam extension when you're done.