My Courses / My courses / Algorithms and Data Structures, MSc (Spring 2023) / Mandatory Activities

/ Analysis of Algorithms

Question 1

Not yet answered

Marked out of 1.00

Consider the pair of functions $f,g\colon \mathbf{N} \to \mathbf{R}$ given by

$$f(n) = 1/n$$

and

$$g(n) = 0$$
.

Which claims are true?

Select one or more:

- \checkmark a. $f \sim g$
- \square b. $f \leq g$
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- \Box d. $f \in O(g)$

Question 2

Not yet answered

Marked out of 1.00

True or false: For every pair of functions $f,g\colon \mathbf{N}\to \mathbf{R}$, if $f\in O(g)$ then $f\sim g$.

Select one:

O a. true

o b. false

Clear my choice

Question $\bf 3$

Not yet answered

Marked out of 1.00

True or false: $N \in O(N^2)$ for $N \ge 1$.

Select one:

O a. false

ob. true

Clear my choice

Question 4	
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Not yet answered

Marked out of 1.00

True or false: $N \in O(N)$ for N > 1.

Select one:

- o a. true
- O b. false

Clear my choice

Question **5**

Not yet answered

Marked out of 1.00

True or false: $N + \log_2 N \in O(N)$ for $N \geq 1$.

Select one:

- O a. false
- ob. true

Clear my choice

Question 6

Not yet answered

Marked out of 1.00

True or false: $N\log_2 N\in O(N)$ for $N\geq 1$.

Select one:

- O a. true
- o b. false

Clear my choice

Not yet answered

Marked out of 1.00

Consider $f(N) = \log_2(N^2 + 1)$ and $g(N) = \log_2 N$ for N > 1. Which function is linearly dominated by the other?

Select one:

- O a. Neither.
- o b. Both.
- \bigcirc c. $f \in O(g)$
- \bigcirc d. $g \in O(f)$

Clear my choice

Question 8

Not yet answered

Marked out of 1.00

Which pair of functions satisfy $f(N) \sim g(N)$?

Select one:

$$\circ$$
 a. $f(N) = N \log N + N$ and $g(N) = 2N \log N + N$

$$\bullet$$
 b. $f(N) = 2\sqrt{N} + N$ and $g(N) = \sqrt{N} + N$

$$\circ$$
 c. $f(N) = N$ and $g(N) = N + N^2$

$$\bigcirc$$
 d. $f(N) = 2N$ and $g(N) = \sqrt{N}$

Clear my choice

Question 9

Not yet answered

Marked out of 1.00

Which pair of functions $f, g \colon \mathbf{N} \to \mathbf{R}$ satisfy $f \in O(g)$?

Select one:

$$\bigcirc$$
 a. $f(N)=N^3$ and $g(N)=3N$ for $N\geq 1$

$$ullet$$
 b. $f(N)=N+N+N$ and $g(N)=N$ for $N\geq 1$

$$\bigcirc$$
 c. $f(N) = (N+1) \cdot (N+1) \cdot (N+1)$ and $g(N) = N+1$ for $N \ge 1$

$$\bigcirc$$
 d. $f(N) = (\log_2 N) \cdot (\log_2 N) \cdot (\log_2 N)$ and $g(N) = \log_2 N$ for $N \ge 1$

Clear my choice

 \wedge

Not yet answered

Marked out of 1.00

What is the running time of the following piece of code? (Choose the smallest correct estimate.)

```
//java
if (N < 1000)
    for (int i = 0; i < N*N; i = i+1) A[i] = 0;
else
    for (int i = 0; i < N; i = i+1) A[i] = i*i*i;</pre>
```

```
#python
if N < 1000:
    for i in range(N*N): A[i] = 0
else:
    for i in range(N): A[i] = i*i*i</pre>
```

Select one:

- \bigcirc a. linearithmic in N
- \odot b. linear in N
- \circ c. quadratic in N
- \circ d. cubic N

Clear my choice

Question 11

Not yet answered

Marked out of 1.00

How many stars are printed?

```
for (int i = N; i > 1; i = i/2) StdOut.print("*");
```

```
#python
i = N
while (i > 1):
    print ('*')
    i = i // 2
```

Select one:

- \circ a. $\sim N$
- O b. $\sim \frac{1}{2}N^2$
- \circ c. $\sim \log N$
- \circ d. $\sim N \log N$

Clear my choice

Not yet answered

Marked out of 1.00

How many stars are printed?

```
#python3
i = 1
while i < N:
    i = i+2
    stdio.write("*")
```

```
// java
for (int i = 1 ; i < N; i = i+2)
    StdOut.print("*");</pre>
```

Select one:

- \bigcirc a. $\sim \frac{1}{2}N^2$
- \circ b. $\sim N$
- \circ c. $\sim \log_2 N$
- \odot d. $\sim N/2$

Clear my choice

Question 13

Not yet answered

Marked out of 1.00

How many array accesses does the following piece of code perform?

Python:

```
for i in range(N):
    for j in range(N):
        A[i] = j;
```

Java:

```
for (int i = 0; i < N; ++i)
  for (int j = 0; j < N; ++j)
    A[i] = j;</pre>
```

Select one:

- \odot a. $\sim {1\over 2} N^2$
- lefton b. $\sim N^2$
- \odot c. $\sim N^{1/2}$
- $\bigcirc \text{ d. } \sim 2N^2$

Clear my choice

Not yet answered

Marked out of 1.00

Let
$$f(n) = n^3 + n$$
 and $g(n) = 2n^2$ for $n \in \mathbf{Z}$. What is

$$\lim_{n \to \infty} \frac{f(n)}{g(n)}$$

Select one:

- O a. 1
- O b. The limit does not exist.
- O c. 2
- \bigcirc d. $-\infty$
- e. +∞
- \bigcirc f. $\frac{1}{2}$

Clear my choice

Question 15

Not yet answered

Marked out of 1.00

What is the limit of the sequence x_1, x_2, \dots

given by
$$x_i = 5 - (1/i)$$
 for $i \to \infty$?

Select one:

- \bigcirc a. $-\infty$
- O b. The limit does not exist.
- \circ c. $+\infty$
- O d. 0
- **○** e. 5
- \bigcirc f. $\frac{1}{2}$
- O g. 1

Clear my choice

Question 16

Not yet answered

Marked out of 1.00

Define f(n)=2n+5 and $g(n)=n^2+1$ for $n\geq 1$. Which statements are true?

Select one or more:

- \square a. $f \leq g$
- \Box b. $q \leq f$
- \square c. $f \sim g$
- \square e. $g \in O(f)$